

A GEOMETRIC APPROACH IN SOLVING THE INVERSE KINEMATICS OF PUMA ROBOTS

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December 1983

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ABSTRACT

This paper presents a geometric approach to derive a consistent joint solution of a six-joint PUMA¹ robot. The approach calls for the definition of various possible arm configurations based on the link coordinate systems and human arm geometry. These arm configurations are then expressed in an exact mathematical way to allow the construction of arm configuration indicators and their corresponding decision equations. The arm configuration indicators are prespecified by a user for finding the joint solution. These indicators enable one to find a solution from the possible four solutions for the first three joints, and a solution from the possible two solutions for the last three joints. The solution is calculated in two stages. First a position vector pointing from the shoulder to the wrist is derived. This is used to derive the solution of the first three joints by looking at the projection of the position vector onto the $x_{i-1}-y_{i-1}$ ($i = 1, 2, 3$) plane. The last three joints are solved using the calculated joint solution from the first three joints, the orientation matrices, and the projection of the link coordinate frames onto the $x_{i-1}-y_{i-1}$ ($i = 4, 5, 6$) plane. From the geometry, one can easily find the arm solution consistently. Computer simulation study conducted on a VAX-11/780 computer demonstrated the validity of the arm solution.

This work was supported in part by the Robot Systems Division of the Center for Robotics and Integrated Manufacturing (CRIM) at The University of Michigan, Ann Arbor, MI. Any opinions, findings, and conclusions or recommendations expressed in this article are those of the authors and do not necessarily reflect the views of the funding agency.

¹ PUMA is a trademark of Unimation Inc.

1. INTRODUCTION

An industrial robot is a general purpose manipulator having several rigid links connected in series by revolute or prismatic joints driven by actuators. One end of the chain is attached to a supporting base while the other end is free and attached with a tool to manipulate objects or perform assembly tasks. The motion of the joints results in relative motion of the links. Since the robot servo system requires the reference inputs to be in joint coordinates and a task is generally stated in terms of the Cartesian coordinate system, controlling the position and orientation of the end-effector of a robot arm to reach its object requires the understanding of the kinematic relationship between these two coordinate systems.

The kinematics problem usually consists of two subproblems - the direct and inverse kinematics problems. The direct kinematics problem is to find the position and orientation of the end effector of a manipulator with respect to a reference coordinate system, given the joint variable vector $\mathbf{q}^T = (q_1, q_2, \dots, q_n)$ of the robot arm and the various geometric link parameters, where superscript T on vectors and matrices denotes a transpose operation, and n is the number of degree-of-freedom. The inverse kinematics problem (or arm solution) is to calculate the joint variable vector \mathbf{q} for positioning the end-effector of the robot arm at the desired position with the desired orientation, given the position and orientation of the end effector with respect to the reference coordinate system and the various geometric link parameters. This paper is concerned with the inverse kinematic analysis of simple manipulators consisting of six rotary joints.

In general, the inverse kinematics problem can be solved either by algebraic, iterative, or geometric approach. Several investigators have attempted to solve the problem for the PUMA and Stanford robot arms using the algebraic approach [1]-[6]. This approach suffers from the fact that the solution does not give a clear indication on how to select the correct solution from the several possible solutions for a particular arm configuration. The user often needs to rely on his/her intuition to pick the right answer. The iteration solution [7-8] often requires more computations and it does not guarantee convergence to the correct solution, especially in the singular and degenerate cases. Furthermore, there is no indication on how to choose the correct solution for a particular arm configuration.

If the manipulator under consideration is simple, that is the geometry of the first three joints has revolute or prismatic pairs and the last three joint axes intersect at a point [1], then the geometric approach presents a better approach for obtaining a closed form solution. This paper presents a geometric approach in solving the inverse kinematics problem of a simple robot arm with rotary joints. The approach calls for the definition of various possible arm configurations based on the link coordinate systems and human arm geometry. These

arm configurations are then expressed in an exact mathematical way to allow the construction of three arm configuration indicators (ARM, ELBOW, and WRIST) and their corresponding decision equations. With the assistance of the configuration indicators and the arm geometry, one can easily find the arm solution consistently. The validity of the arm solution was simulated on a VAX-11/780 computer. With appropriate modification and adjustment, the user can generalize and extend the method to most present day industrial robots with rotary joints and obtain the arm solution easily.

2. LINKS, JOINTS, AND COORDINATE TRANSFORMATION

To describe the translational and rotational relationship between adjacent links, a Denavit-Hartenberg matrix representation [9] for each link is used and shown in Figure 1. From Figure 1, an orthonormal coordinate frame system (x_i, y_i, z_i) is assigned to link i , where the z_i axis passes through the axis of motion of joint $i+1$, and the x_i axis is normal to the z_{i-1} axis pointing away from it, while the y_i axis completes the right hand rule. With this orthonormal coordinate frame, link i is characterized by two parameters: a_i , the common normal distance between the z_{i-1} and z_i axes and α_i , the twist angle measured between the z_{i-1} and z_i axes in a plane perpendicular to a_i . Joint i which connects link $i-1$ to link i is characterized by a distance parameter d_i measured between the x_{i-1} and x_i axes and a revolute joint variable θ_i which is the joint angle between the normals and measured in a plane normal to the joint axis. If joint i is prismatic, then it is characterized by an angle parameter θ_i and a joint variable d_i .

Once the link coordinate systems have been established for each link, a homogeneous transformation matrix, A_{i-1}^i , can easily be developed relating the i^{th} coordinate frame to the $i-1^{th}$ coordinate frame. Using the A_{i-1}^i matrix, one can relate a point p_i at rest in link i and expressed in homogeneous coordinates with respect to the i^{th} coordinate system to the $i-1^{th}$ coordinate system established at link ($i-1$) by:

$$\mathbf{p}_{i-1} = \mathbf{A}_{i-1}^i \mathbf{p}_i \quad (1)$$

where $\mathbf{p}_{i-1} = (x_{i-1}, y_{i-1}, z_{i-1}, 1)^T$; $\mathbf{p}_i = (x_i, y_i, z_i, 1)^T$;

$$\mathbf{A}_{i-1}^i = \begin{bmatrix} \cos \theta_i & -\cos \alpha_i \sin \theta_i & \sin \alpha_i \sin \theta_i & a_i \cos \theta_i \\ \sin \theta_i & \cos \alpha_i \cos \theta_i & -\sin \alpha_i \cos \theta_i & a_i \sin \theta_i \\ 0 & \sin \alpha_i & \cos \alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}; \text{ for a rotary joint} \quad (2)$$

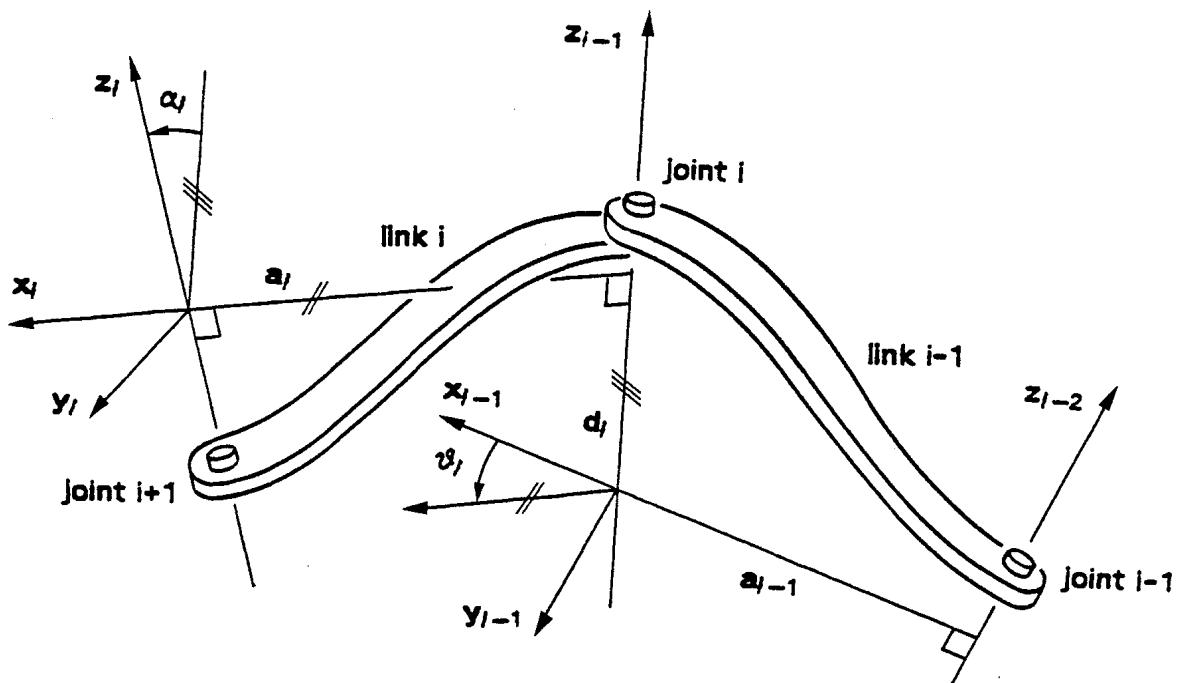
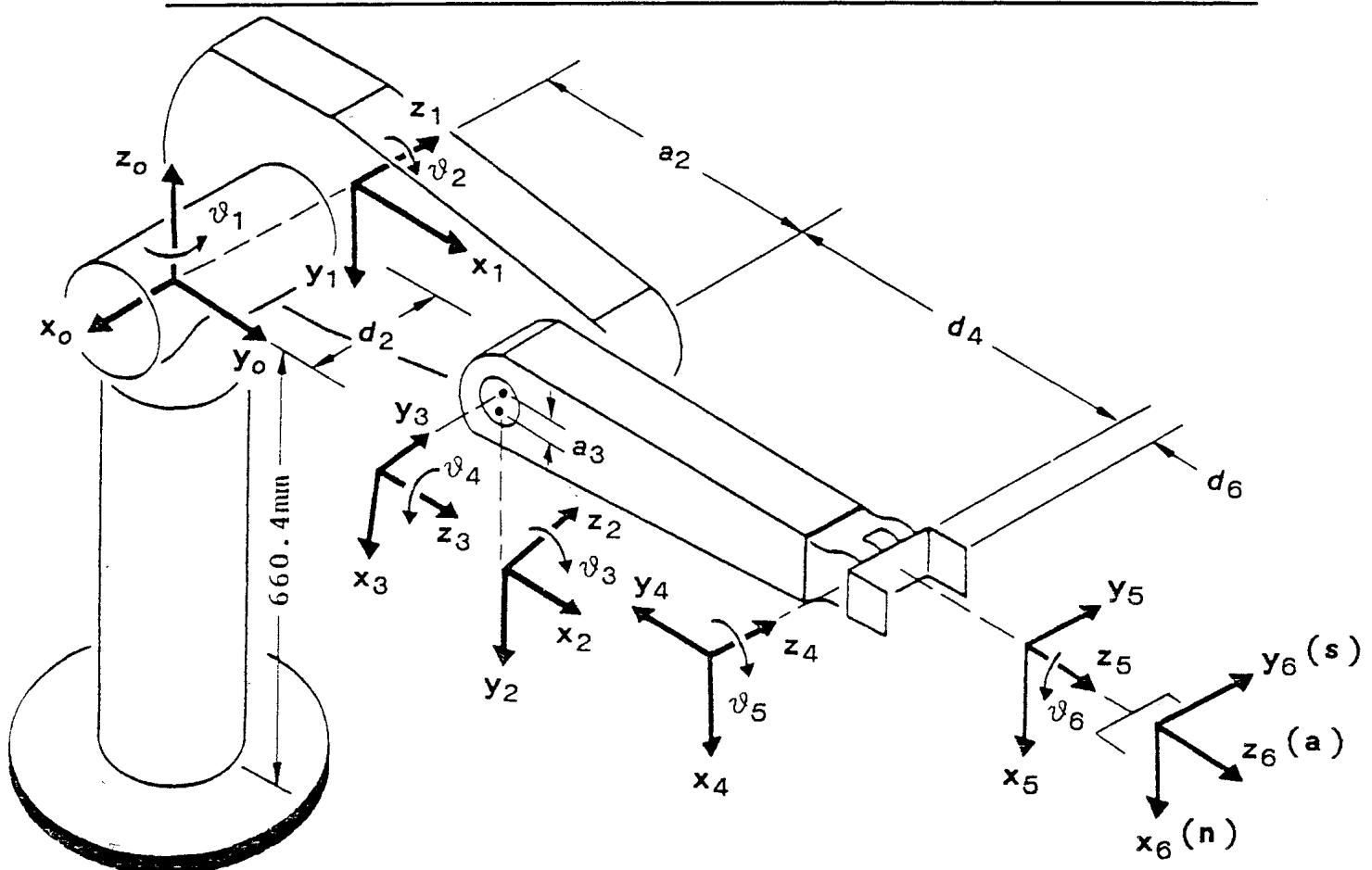


Figure 1 Link Coordinate System and Its Parameters

With the basic rules for establishing an orthonormal coordinate system for each link and the geometric interpretation of the joint and link parameters, a procedure for establishing *consistent* orthonormal coordinate systems for a robot is outlined in [5]. An example of applying this algorithm to a six-joint PUMA robot arm is given in Figure 2. The six A_{i-1}^i homogeneous transformation matrices for the PUMA robot shown in Figure 2 are listed in Figure 3.



PUMA Robot Link Coordinate Parameters					
Joint i	ϑ_i	α_i	a_i	d_i	Range
1	90	-90	0	0	-160 to +160
2	0	0	431.8 mm	149.09 mm	-225 to +45
3	90	90	-20.32 mm	0	-45 to +225
4	0	-90	0	433.07 mm	-110 to +170
5	0	90	0	0	-100 to +100
6	0	0	0	56.25 mm	-266 to +266

Figure 2 Link Coordinate Systems For A PUMA Robot

$$\mathbf{A}_0^1 = \begin{bmatrix} C_1 & 0 & -S_1 & 0 \\ S_1 & 0 & C_1 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \mathbf{A}_1^2 = \begin{bmatrix} C_2 & -S_2 & 0 & a_2 C_2 \\ S_2 & C_2 & 0 & a_2 S_2 \\ 0 & 0 & 1 & d_2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \mathbf{A}_2^3 = \begin{bmatrix} C_3 & 0 & S_3 & a_3 C_3 \\ S_3 & 0 & -C_3 & a_3 S_3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{A}_3^4 = \begin{bmatrix} C_4 & 0 & -S_4 & 0 \\ S_4 & 0 & C_4 & 0 \\ 0 & -1 & 0 & d_4 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \mathbf{A}_4^5 = \begin{bmatrix} C_5 & 0 & S_5 & 0 \\ S_5 & 0 & -C_5 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \mathbf{A}_5^6 = \begin{bmatrix} C_6 & -S_6 & 0 & 0 \\ S_6 & C_6 & 0 & 0 \\ 0 & 0 & 1 & d_6 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

where $C_i \equiv \cos \theta_i$; $S_i \equiv \sin \theta_i$

Figure 3 Coordinate Transformation Matrices For The PUMA in Figure 2

3. KINEMATIC EQUATIONS FOR MANIPULATORS

The homogeneous transformation matrix \mathbf{T}_0^i which specifies the position and orientation of the i^{th} coordinate frame with respect to the base coordinate system is the chain product of successive homogeneous transformation matrices of \mathbf{A}_{i-1}^i , expressed as:

$$\mathbf{T}_0^i = \mathbf{A}_0^1 \mathbf{A}_1^2 \cdots \mathbf{A}_{i-1}^i = \prod_{j=1}^i \mathbf{A}_{j-1}^j = \begin{bmatrix} \mathbf{x}_i & \mathbf{y}_i & \mathbf{z}_i & \mathbf{p}_i \\ 0 & 0 & 0 & 1 \end{bmatrix} ; \text{ for } i = 1, 2, \dots, n \quad (3)$$

Specifically for $i=n$, we obtain the \mathbf{T} matrix, $\mathbf{T} = \mathbf{T}_0^n$, which specifies the position and orientation of the end-point of a manipulator with respect to the base coordinate system. This \mathbf{T} matrix is used so frequently in the kinematic analysis of robot arm that it is called the "arm matrix". Consider the \mathbf{T} matrix to be of the form:

$$\mathbf{T} = \begin{bmatrix} \mathbf{x}_n & \mathbf{y}_n & \mathbf{z}_n & \mathbf{p}_n \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \mathbf{n} & \mathbf{s} & \mathbf{a} & \mathbf{p} \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} n_x & s_x & a_x & p_x \\ n_y & s_y & a_y & p_y \\ n_z & s_z & a_z & p_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (4)$$

where (see Figure 4):

- \mathbf{n} is the normal vector of the hand. Assuming parallel-jaw hand, it is orthogonal to the fingers of the robot arm.
- \mathbf{s} is the sliding vector of the hand. It is pointing in the direction of the finger motion as the gripper opens and closes.
- \mathbf{a} is the approach vector of the hand. It is pointing in the direction normal to the palm of the hand. (i.e., normal to the tool mounting plate of the arm.)
- \mathbf{p} is the position vector of the hand. It points from the origin of the base coordinate system to the origin of the hand coordinate system, which is usually located at the center point of the fully closed fingers.

The elements of the arm matrix for the PUMA robot arm shown in Figure 2 are found to be

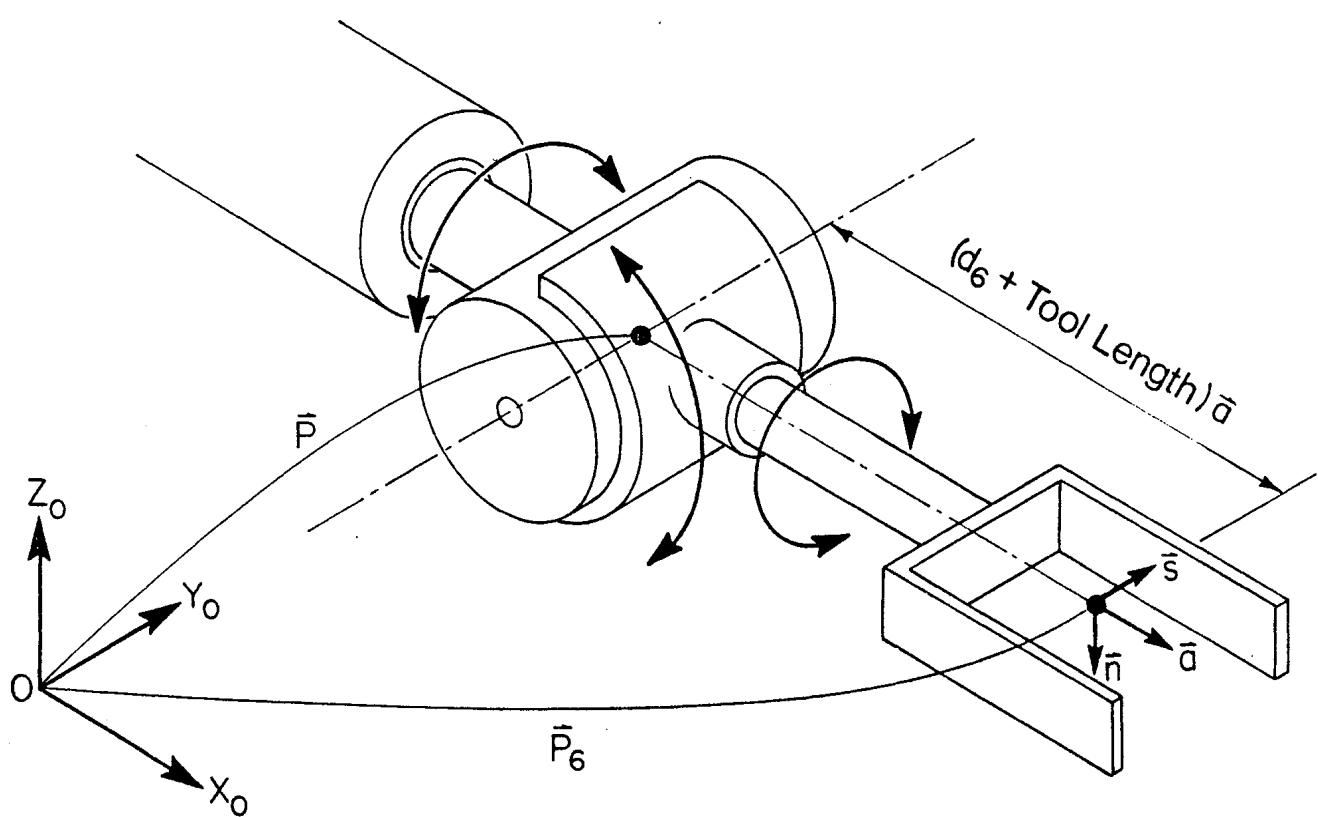


Figure 4 Hand Coordinate System and [$\mathbf{n}, \mathbf{s}, \mathbf{a}$]

$$\begin{aligned}
 n_x &= C_1[C_{23}(C_4C_5C_6 - S_4S_6) - S_{23}S_5C_6] - S_1[S_4C_5C_6 + C_4S_6] \\
 n_y &= S_1[C_{23}(C_4C_5C_6 - S_4S_6) - S_{23}S_5C_6] + C_1[S_4C_5C_6 + C_4S_6] \\
 n_z &= -S_{23}[C_4C_5C_6 - S_4S_6] - C_{23}S_5C_6
 \end{aligned} \tag{5}$$

$$\begin{aligned}
 s_x &= C_1[-C_{23}(C_4C_5S_6 + S_4C_6) + S_{23}S_5S_6] - S_1[-S_4C_5S_6 + C_4C_6] \\
 s_y &= S_1[-C_{23}(C_4C_5S_6 + S_4C_6) + S_{23}S_5S_6] + C_1[-S_4C_5S_6 + C_4C_6] \\
 s_z &= S_{23}(C_4C_5S_6 + S_4C_6) + C_{23}S_5S_6
 \end{aligned} \tag{6}$$

$$\begin{aligned}
 a_x &= C_1(C_{23}C_4S_5 + S_{23}C_5) - S_1S_4S_5 \\
 a_y &= S_1(C_{23}C_4S_5 + S_{23}C_5) + C_1S_4S_5 \\
 a_z &= -S_{23}C_4S_5 + C_{23}C_5
 \end{aligned} \tag{7}$$

$$\begin{aligned}
 p_x &= C_1[d_6(C_{23}C_4S_5 + S_{23}C_5) + S_{23}d_4 + a_3C_{23} + a_2C_2] - S_1(d_6S_4S_5 + d_2) \\
 p_y &= S_1[d_6(C_{23}C_4S_5 + S_{23}C_5) + S_{23}d_4 + a_3C_{23} + a_2C_2] + C_1(d_6S_4S_5 + d_2) \\
 p_z &= d_6(C_{23}C_5 - S_{23}C_4S_5) + C_{23}d_4 - a_3S_{23} - a_2S_2
 \end{aligned} \tag{8}$$

where $C_i \equiv \cos \theta_i$; $S_i \equiv \sin \theta_i$; $C_{ij} \equiv \cos(\theta_i + \theta_j)$; $S_{ij} \equiv \sin(\theta_i + \theta_j)$.

4. THE INVERSE KINEMATICS SOLUTION OF A PUMA ROBOT ARM

This section presents a geometric approach to derive a consistent joint angle solution of a PUMA robot given the arm matrix as in Eq. 4. Based on the link coordinate systems and human arm geometry, various arm configurations of a PUMA robot can be identified with the assistance of three configuration indicators (ARM, ELBOW and WRIST) - two associated with the solution of the first three joints and the other with the last three joints. For a six-joint PUMA robot arm, there are four possible solutions to the first three joints and for each of these four solutions there are two possible solutions to the last three joints. The first two configuration indicators allow one to determine one solution from the possible four solutions for the first three joints. Similarly, the third indicator selects a solution from the possible two solutions for the last three joints. The arm configuration indicators are prespecified by a user for finding the inverse solution. The solution is calculated in two stages. First a position vector pointing from the shoulder to the wrist is derived. This is used to derive the solution of each joint i ($i = 1, 2, 3$) of the first three joints by looking at the

projection of the position vector onto the $x_{i-1}-y_{i-1}$ plane. The last three joints are solved using the calculated joint solution from the first three joints, the orientation submatrices of T_0^i and A_{i-1}^i ($i = 4, 5, 6$), and the projection of the link coordinate frames onto the $x_{i-1}-y_{i-1}$ plane. From the geometry, one can easily find the arm solution consistently. As a verification of the joint solution, the arm configuration indicators can be determined from the corresponding decision equations which are functions of the joint angles.

4.1. DEFINITION OF VARIOUS ARM CONFIGURATIONS

For the PUMA robot arm shown in Figure 2 (and other rotary robot arms), various arm configurations are defined according to human arm geometry and the link coordinate systems which are established using the algorithm in [5] as: (Figure 5)

RIGHT (shoulder) ARM: Positive θ_2 moves the wrist in the *positive z_0* direction while joint 3 is not activated.

LEFT (shoulder) ARM: Positive θ_2 moves the wrist in the *negative z_0* direction while joint 3 is not activated.

ABOVE ARM (elbow above wrist): Position of the wrist of the
 $\begin{cases} \text{RIGHT} \\ \text{LEFT} \end{cases}$ arm with respect to the shoulder coordinate system has
 $\begin{cases} \text{negative} \\ \text{positive} \end{cases}$ coordinate value along the y_2 -axis.

BELOW ARM (elbow below wrist): Position of the wrist of the
 $\begin{cases} \text{RIGHT} \\ \text{LEFT} \end{cases}$ arm with respect to the shoulder coordinate system has
 $\begin{cases} \text{positive} \\ \text{negative} \end{cases}$ coordinate value along the y_2 -axis.

WRIST DOWN: The s unit vector of the hand coordinate system and the y_5 unit vector of the (x_5, y_5, z_5) coordinate system have a positive dot product.

WRIST UP: The s unit vector of the hand coordinate system and the y_5 unit vector of the (x_5, y_5, z_5) coordinate system have a negative dot product.

(Note that the definition of the arm configurations with respect to the link coordinate systems may have to be slightly modified if one uses different link coordinate systems.)

With respect to the above definition of various arm configurations, two arm configuration *indicators* (ARM and ELBOW) are defined for each arm configuration. These two indicators are combined to give one solution out of

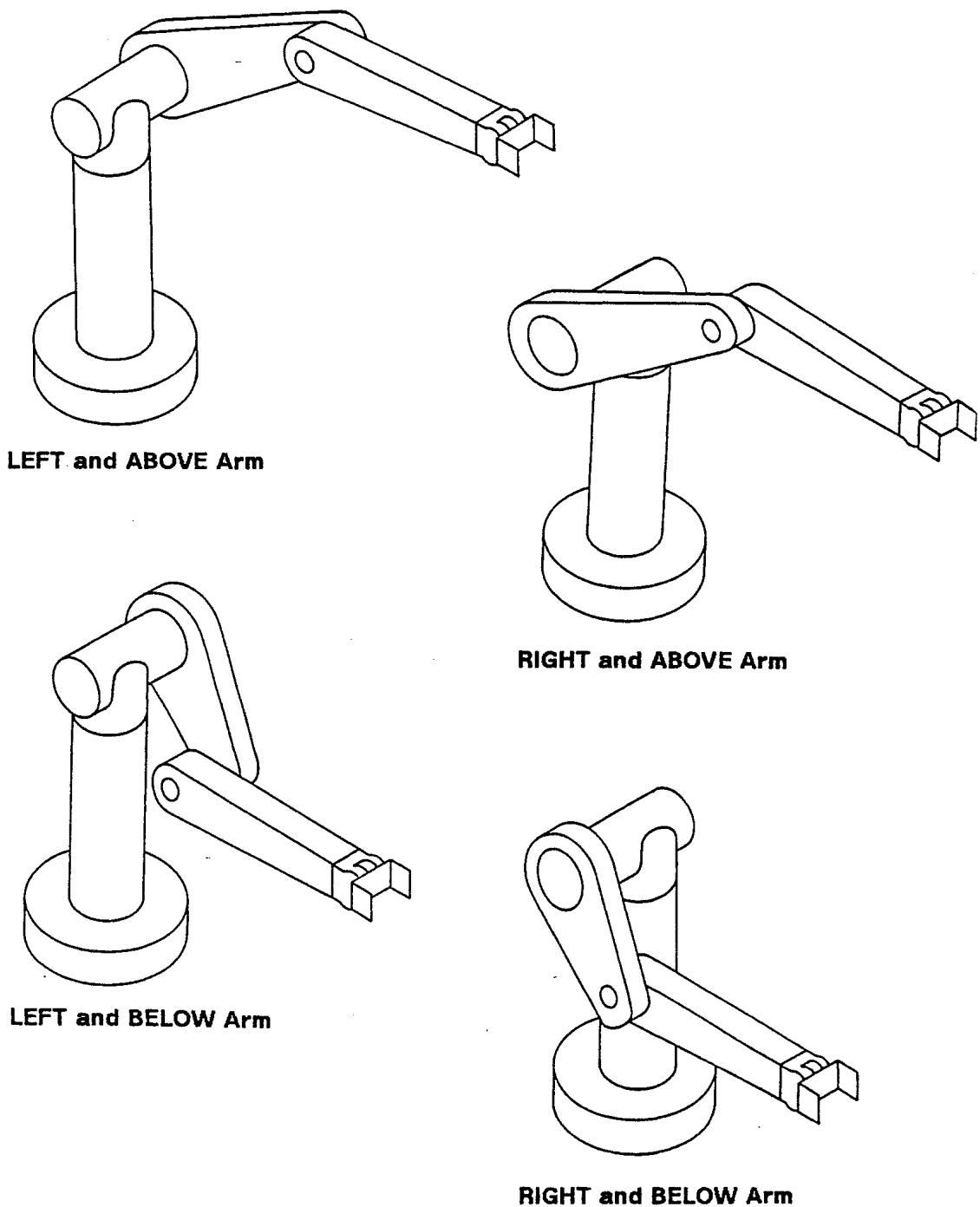


Figure 5. Definition of Various Arm Configurations

the possible four joint solutions for the first three joints. For each of the four arm configurations (Figure 5) defined by these two indicators, the third indicator (WRIST) gives one of the two possible joint solutions for the last three joints. These three indicators can be defined as:

$$ARM = \begin{cases} +1 & ; \text{ } RIGHT \text{ } arm \\ -1 & ; \text{ } LEFT \text{ } arm \end{cases} \quad (9)$$

$$ELBOW = \begin{cases} +1 & ; \text{ } ABOVE \text{ } arm \\ -1 & ; \text{ } BELOW \text{ } arm \end{cases} \quad (10)$$

$$WRIST = \begin{cases} +1 & ; \text{ } WRIST \text{ } DOWN \\ -1 & ; \text{ } WRIST \text{ } UP \end{cases} \quad (11)$$

In addition to these indicators, the user can define a "FLIP" toggle as:

$$FLIP = \begin{cases} +1 & ; \text{ } Flip \text{ } the \text{ } wrist \text{ } orientation \\ -1 & ; \text{ } Do \text{ } not \text{ } flip \text{ } the \text{ } wrist \text{ } orientation \end{cases} \quad (12)$$

The signed values of these indicators and the toggle are prespecified by a user for finding the inverse kinematics solution. These indicators can also be set from the knowledge of the joint angles of the robot arm using the corresponding decision equations. We shall later give the decision equations that determine these indicator values. The decision equations can be used as a verification of the inverse kinematics solution.

4.2. ARM SOLUTION FOR THE FIRST THREE JOINTS OF A PUMA ROBOT ARM

From the kinematics diagram of the PUMA robot arm as in Figure 2, we define a position vector \mathbf{p} which points from the origin of the shoulder coordinate system $(\mathbf{x}_0, \mathbf{y}_0, \mathbf{z}_0)$ to the point where the last three joint axes intersect as (see Figure 4):

$$\mathbf{p} = \mathbf{p}_6 - d_6 \mathbf{a} = (p_x, p_y, p_z)^T \quad (13)$$

which corresponds to the position vector of \mathbf{T}_0^4 :

$$\begin{bmatrix} p_x \\ p_y \\ p_z \end{bmatrix} = \begin{bmatrix} C_1(a_2C_2 + a_3C_{23} + d_4S_{23}) - d_2S_1 \\ S_1(a_2C_2 + a_3C_{23} + d_4S_{23}) + d_2C_1 \\ d_4C_{23} - a_3S_{23} - a_2S_2 \end{bmatrix} \quad (14)$$

Joint One Solution. If we project the position vector \mathbf{p} onto the $\mathbf{x}_0\mathbf{-y}_0$ plane as in Figure 6, we obtain the following equations for solving θ_1 :

$$\theta_1^L = \phi - \alpha ; \quad \theta_1^R = \pi + \phi + \alpha \quad (15)$$

$$r = \sqrt{p_x^2 + p_y^2 - d_2^2} ; \quad R = \sqrt{p_x^2 + p_y^2} \quad (16)$$

$$\sin \phi = \frac{p_y}{R} ; \quad \cos \phi = \frac{p_x}{R} \quad (17)$$

$$\sin \alpha = \frac{d_2}{R} ; \quad \cos \alpha = \frac{r}{R} \quad (18)$$

where the superscript L/R on joint angles indicates the LEFT/RIGHT arm configurations. From Eqs. 15-18, we obtain the sine and cosine functions of θ_1 for LEFT/RIGHT arm configurations:

$$\sin \theta_1^L = \sin(\phi - \alpha) = \sin \phi \cos \alpha - \cos \phi \sin \alpha = \frac{p_y r - p_x d_2}{R^2} \quad (19)$$

$$\cos \theta_1^L = \cos(\phi - \alpha) = \cos \phi \cos \alpha + \sin \phi \sin \alpha = \frac{p_x r + p_y d_2}{R^2} \quad (20)$$

$$\sin \theta_1^R = \sin(\pi + \phi + \alpha) = \frac{-p_y r - p_x d_2}{R^2} \quad (21)$$

$$\cos \theta_1^R = \cos(\pi + \phi + \alpha) = \frac{-p_x r + p_y d_2}{R^2} \quad (22)$$

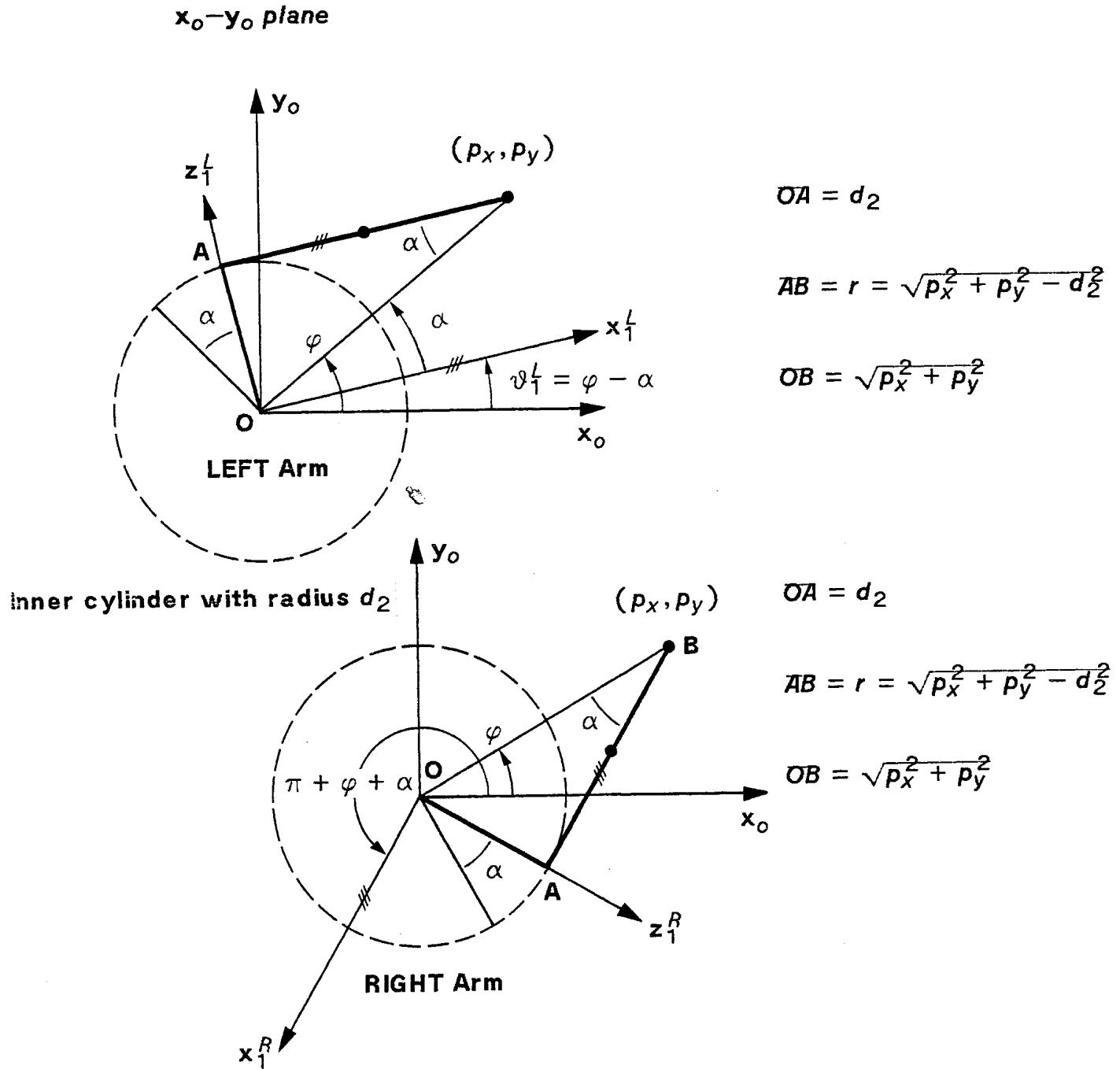


Figure 6. Joint One Solution

Combining Eqs. 19-22 and using the ARM indicator to indicate the LEFT/RIGHT arm configuration, we obtain the sine and cosine functions of θ_1 respectively:

$$\sin \theta_1 = \frac{-ARM \cdot p_y \sqrt{p_x^2 + p_y^2 - d_2^2} - p_x d_2}{p_x^2 + p_y^2} \quad (23)$$

$$\cos \theta_1 = \frac{-ARM \cdot p_x \sqrt{p_x^2 + p_y^2 - d_2^2} + p_y d_2}{p_x^2 + p_y^2} \quad (24)$$

where positive square root is taken in these equations and ARM is defined as in Eq. 9. In order to evaluate θ_1 for $-\pi \leq \theta_1 \leq \pi$, an arc tangent function, $\text{atan2}(\frac{y}{x})$, which returns $\tan^{-1}(\frac{y}{x})$ adjusted to the proper quadrant will be used. It is defined as:

$$\theta = \text{atan2}\left(\frac{y}{x}\right) = \begin{cases} 0^\circ \leq \theta \leq 90^\circ & ; \text{ for } +x \text{ and } +y \\ 90^\circ \leq \theta \leq 180^\circ & ; \text{ for } -x \text{ and } +y \\ -180^\circ \leq \theta \leq -90^\circ & ; \text{ for } -x \text{ and } -y \\ -90^\circ \leq \theta \leq 0^\circ & ; \text{ for } +x \text{ and } -y \end{cases} \quad (25)$$

From Eqs. 23 and 24, and using Eq. 25, θ_1 is found to be:

$$\theta_1 = \text{atan2}\left[\frac{\sin \theta_1}{\cos \theta_1}\right] = \text{atan2}\left[\frac{-ARM \cdot p_y \sqrt{p_x^2 + p_y^2 - d_2^2} - p_x d_2}{-ARM \cdot p_x \sqrt{p_x^2 + p_y^2 - d_2^2} + p_y d_2}\right]; \quad -\pi \leq \theta_1 \leq \pi \quad (26)$$

Joint Two Solution. To find joint 2, we project the position vector \mathbf{p} onto the x_1-y_1 plane as shown in Figure 7. From Figure 7, we have four different arm configurations. Each arm configuration corresponds to different values of joint two as:

Arm Configurations	θ_2	ARM	ELBOW	ARM · ELBOW
LEFT and ABOVE arm	$\alpha - \beta$	-1	+1	-1
LEFT and BELOW arm	$\alpha + \beta$	-1	-1	+1
RIGHT and ABOVE arm	$\alpha + \beta$	+1	+1	+1
RIGHT and BELOW arm	$\alpha - \beta$	+1	-1	-1

where $0^\circ \leq \alpha \leq 360^\circ$ and $0^\circ \leq \beta \leq 90^\circ$.

Table 1. Various Arm Configurations for Joint Two

From the above table, θ_2 can be expressed in one equation for different arm and elbow configurations using the ARM and ELBOW indicators as:

$$\theta_2 = \alpha + (\text{ARM} \cdot \text{ELBOW}) \quad \beta = \alpha + K \cdot \beta \quad (27)$$

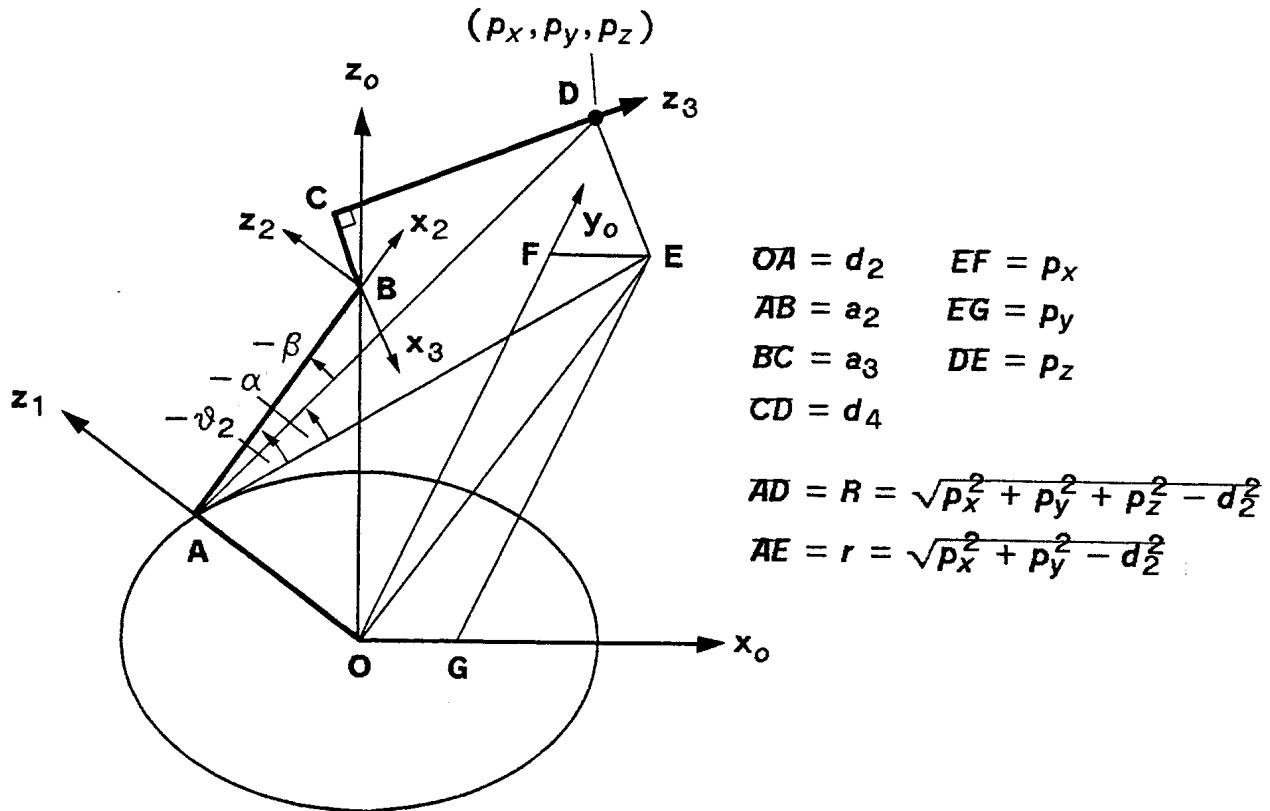
where the combined arm configuration indicator $K = \text{ARM} \cdot \text{ELBOW}$ will give an appropriate signed value and the "dot" represents a multiplication operation on the indicators. From the arm geometry in Figure 7, we obtain:

$$R = \sqrt{p_x^2 + p_y^2 + p_z^2 - d_2^2} \quad ; \quad r = \sqrt{p_x^2 + p_y^2 - d_2^2} \quad (28)$$

$$\sin \alpha = -\frac{p_z}{R} = -\frac{p_z}{\sqrt{p_x^2 + p_y^2 + p_z^2 - d_2^2}} \quad (29)$$

$$\cos \alpha = -\frac{\text{ARM} \cdot r}{R} = -\frac{\text{ARM} \cdot \sqrt{p_x^2 + p_y^2 - d_2^2}}{\sqrt{p_x^2 + p_y^2 + p_z^2 - d_2^2}} \quad (30)$$

$$\cos \beta = \frac{a_2^2 + R^2 - (d_4^2 + a_3^2)}{2a_2R} = \frac{p_x^2 + p_y^2 + p_z^2 + a_2^2 - d_2^2 - (d_4^2 + a_3^2)}{2a_2\sqrt{p_x^2 + p_y^2 + p_z^2 - d_2^2}} \quad (31)$$

**Figure 7. Joint Two Solution**

$$\sin \beta = \sqrt{1 - \cos^2 \beta} \quad (32)$$

From Eqs. 27-32, we can find the sine and cosine functions of θ_2 :

$$\sin \theta_2 = \sin(\alpha + K \cdot \beta) = \sin \alpha \cos \beta + (ARM \cdot ELBOW) \cos \alpha \sin \beta \quad (33)$$

$$\cos \theta_2 = \cos(\alpha + K \cdot \beta) = \cos \alpha \cos \beta - (ARM \cdot ELBOW) \sin \alpha \sin \beta \quad (34)$$

From Eqs. 33 and 34, we obtain the solution for θ_2 :

$$\theta_2 = \text{atan}2\left[\frac{\sin \theta_2}{\cos \theta_2}\right] ; -\pi \leq \theta_2 \leq \pi \quad (35)$$

Joint Three Solution. For joint 3, we project the position vector \mathbf{p} onto the x_2-y_2 plane as shown in Figure 8. From Figure 8, we again have four different arm configurations. Each arm configuration corresponds to different values of joint three as:

Arm Configurations	$(\mathbf{p}_2^4)_y$	θ_3	ARM	ELBOW	ARM · ELBOW
LEFT and ABOVE arm	≥ 0	$\phi - \beta$	-1	+1	-1
LEFT and BELOW arm	≤ 0	$\phi - \beta$	-1	-1	+1
RIGHT and ABOVE arm	≤ 0	$\phi - \beta$	+1	+1	+1
RIGHT and BELOW arm	≥ 0	$\phi - \beta$	+1	-1	-1

Table 2. Various Arm Configurations for Joint Three

where $(\mathbf{p}_2^4)_y$ is the y-component of the position vector from the origin of (x_2, y_2, z_2) to the point where the last three joint axes intersect.

From the arm geometry in Figure 8, we obtain the following equations for finding the solution for θ_3 :

$$R = \sqrt{p_x^2 + p_y^2 + p_z^2 - d_2^2} \quad (36)$$

$$\cos \phi = \frac{a_2^2 + (d_4^2 + a_3^2) - R^2}{2a_2 \sqrt{d_4^2 + a_3^2}} ; \sin \phi = \text{ARM} \cdot \text{ELBOW} \sqrt{1 - \cos^2 \phi} \quad (37)$$

$$\sin \beta = \frac{d_4}{\sqrt{d_4^2 + a_3^2}} ; \cos \beta = \frac{|a_3|}{\sqrt{d_4^2 + a_3^2}} \quad (38)$$

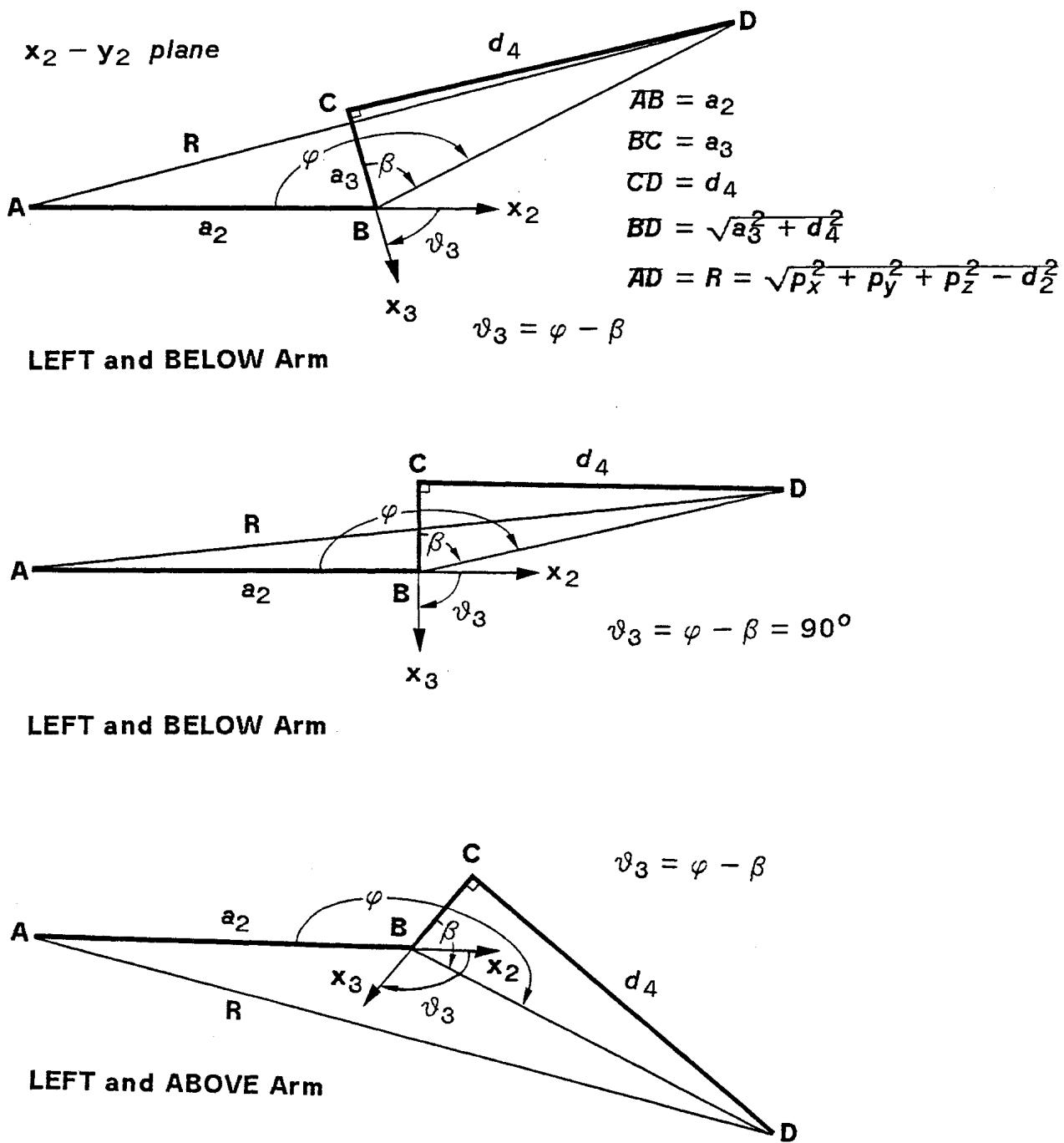


Figure 8. Joint Three Solution

From Table 2, we obtain the equation for θ_3 :

$$\theta_3 = \phi - \beta \quad (39)$$

From Eq. 39, the sine and cosine functions of θ_3 are, respectively:

$$\sin \theta_3 = \sin(\phi - \beta) = \sin \phi \cos \beta - \cos \phi \sin \beta \quad (40)$$

$$\cos \theta_3 = \cos(\phi - \beta) = \cos \phi \cos \beta + \sin \phi \sin \beta \quad (41)$$

From Eqs. 40 and 41, and using Eqs. 36-38, we find the solution for θ_3 :

$$\theta_3 = \text{atan}2\left[\frac{\sin \theta_3}{\cos \theta_3}\right] \quad ; \quad -\pi \leq \theta_3 \leq \pi \quad (42)$$

4.3. ARM SOLUTION FOR THE LAST THREE JOINTS OF A PUMA ROBOT ARM

Knowing the first three joint angles, we can evaluate the T_0^3 matrix which is used extensively to find the solution of the last three joints. The solution of the last three joints of a PUMA robot arm can be found by setting these joints to meet the following criteria:

- (1) Set joint 4 such that a rotation about joint 5 will align the axis of motion of joint 6 with the given approach vector (\mathbf{a} of \mathbf{T})
- (2) Set joint 5 to align the axis of motion of joint 6 with the approach vector.
- (3) Set joint 6 to align the given orientation vector (or sliding vector or \mathbf{y}_6) and normal vector.

Mathematically the above criteria respectively mean:

$$\mathbf{z}_4 = \frac{\pm(\mathbf{z}_3 \times \mathbf{a})}{\| \mathbf{z}_3 \times \mathbf{a} \|} \quad ; \quad \text{given } \mathbf{a} = (a_x, a_y, a_z)^T \quad (43)$$

$$\mathbf{a} = \mathbf{z}_5 \quad ; \quad \text{given } \mathbf{a} = (a_x, a_y, a_z)^T \quad (44)$$

$$\mathbf{s} = \mathbf{y}_6 \quad ; \quad \text{given } \mathbf{s} = (s_x, s_y, s_z)^T \text{ and } \mathbf{n} = (n_x, n_y, n_z)^T \quad (45)$$

In Eq. 43, the vector cross product may be taken to be positive or negative. As a result, there are two possible solutions for θ_4 . If the vector cross product is zero (i.e. \mathbf{z}_3 is parallel to \mathbf{a}), it indicates the degenerate case. This happens when the axes of rotation for joint 4 and joint 6 are parallel. It indicates that at this particular arm configuration, a five-axis robot arm rather than a six-axis one would suffice.

Joint Four Solution. Both orientations of the wrist (UP and DOWN) are defined by looking at the orientation of the hand coordinate frame ($\mathbf{n}, \mathbf{s}, \mathbf{a}$) with respect to the $(\mathbf{x}_5, \mathbf{y}_5, \mathbf{z}_5)$ coordinate frame. The sign of the vector cross product in Eq. 43 cannot be determined without referring to the orientation of either the \mathbf{n} or \mathbf{s} unit vector with respect to the \mathbf{x}_5 or \mathbf{y}_5 unit vector, respectively, which have a fixed relation with respect to the \mathbf{z}_4 unit vector from the assignment of the link coordinate frames. (From Figure 2, we have the \mathbf{z}_4 unit vector pointing at the same direction as the \mathbf{y}_5 unit vector)

We shall start with an assumption that the vector cross product in Eq. 43 has a positive sign. This can be indicated by an orientation indicator Ω which is defined as:

$$\Omega = \begin{cases} 0 & ; \text{ if in the degenerate case} \\ \mathbf{s} \cdot \mathbf{y}_5 & ; \text{ if } \mathbf{s} \cdot \mathbf{y}_5 \neq 0 \\ \mathbf{n} \cdot \mathbf{y}_5 & ; \text{ if } \mathbf{s} \cdot \mathbf{y}_5 = 0 \end{cases} \quad (46)$$

From Figure 2, $\mathbf{y}_5 = \mathbf{z}_4$ and using Eq. 43, the orientation indicator Ω can be rewritten as:

$$\Omega = \begin{cases} 0 & ; \text{ if in the degenerate case} \\ \frac{\mathbf{s} \cdot (\mathbf{z}_3 \times \mathbf{a})}{\|\mathbf{z}_3 \times \mathbf{a}\|} & ; \text{ if } \mathbf{s} \cdot (\mathbf{z}_3 \times \mathbf{a}) \neq 0 \\ \frac{\mathbf{n} \cdot (\mathbf{z}_3 \times \mathbf{a})}{\|\mathbf{z}_3 \times \mathbf{a}\|} & ; \text{ if } \mathbf{s} \cdot (\mathbf{z}_3 \times \mathbf{a}) = 0 \end{cases} \quad (47)$$

If our assumption of the sign of the vector cross product in Eq. 43 is not correct, it will be corrected later using the combination of the WRIST indicator and the orientation indicator Ω . The Ω is used to indicate the initial orientation of the \mathbf{z}_4 unit vector (positive direction) from the link coordinate systems

assignment, while the WRIST indicator specifies the user's preference of the orientation of the wrist subsystem according to the definition given in Eq. 11. If both the orientation Ω and the WRIST indicators have the same sign, then the assumption of the sign of the vector cross product in Eq. 43 is correct. Various wrist orientations resulting from the combination of the various values of the WRIST and orientation indicators are tabulated in Table 3.

Wrist Orientation	$\Omega = \mathbf{s} \cdot \mathbf{y}_5$ or $\mathbf{n} \cdot \mathbf{y}_5$	WRIST	$M = WRIST \cdot sign(\Omega)$
DOWN	≥ 0	+1	+1
DOWN	< 0	+1	-1
UP	≥ 0	-1	-1
UP	< 0	-1	+1

Table 3. Various Orientations for The Wrist

Again looking at the projection of the coordinate frame $(\mathbf{x}_4, \mathbf{y}_4, \mathbf{z}_4)$ on the $\mathbf{x}_3-\mathbf{y}_3$ plane and from the Table 3 and Figure 9, it can be shown that the followings are true (see Figure 9):

$$\sin \theta_4 = -M \cdot (\mathbf{z}_4 \cdot \mathbf{x}_3) ; \cos \theta_4 = M \cdot (\mathbf{z}_4 \cdot \mathbf{y}_3) \quad (48)$$

where \mathbf{x}_3 and \mathbf{y}_3 are the x and y column vector of \mathbf{T}_0^3 respectively, $M = WRIST \cdot sign(\Omega)$, and the sign function is defined as:

$$sign(x) = \begin{cases} +1 & ; \text{if } x \geq 0 \\ -1 & ; \text{if } x < 0 \end{cases} \quad (49)$$

Thus the solution for θ_4 with the orientation and WRIST indicators is:

$$\theta_4 = atan2 \left[\frac{\sin \theta_4}{\cos \theta_4} \right] = atan2 \left[\frac{M \cdot (C_1 a_y - S_1 a_z)}{M \cdot (C_1 C_{23} a_x + S_1 C_{23} a_y - S_{23} a_z)} \right]; -\pi \leq \theta_4 \leq \pi \quad (50)$$

If the degenerate case occurs, any convenient value may be chosen for θ_4 as long as the orientation of the wrist (UP/DOWN) is satisfied. This can always be ensured by setting θ_4 equals to the current value of θ_4 . In addition to this,

$$\sin \vartheta_4 = -(z_4 \cdot x_3)$$

$$\cos \vartheta_4 = (z_4 \cdot y_3)$$

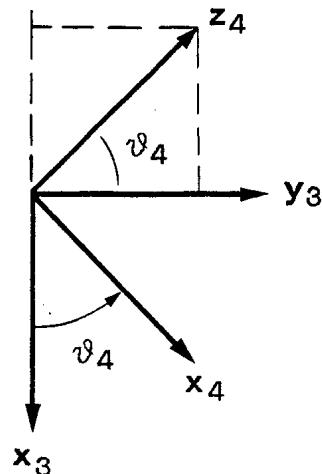


Figure 9 Joint Four Solution

the user can turn on the FLIP toggle to obtain the other solution of θ_4 , that is $\theta_4 = \theta_4 + 180^\circ$.

Joint Five Solution. To find θ_5 , we use the criterion that aligns the axis of rotation of joint six with the approach vector (or $\mathbf{a} = z_5$). Looking at the projection of the coordinate frame (x_5, y_5, z_5) on the x_4-y_4 plane, it can be shown that the followings are true (see Figure 10):

$$\sin \theta_5 = \mathbf{a} \cdot \mathbf{x}_4 ; \quad \cos \theta_5 = -(\mathbf{a} \cdot \mathbf{y}_4) \quad (51)$$

where \mathbf{x}_4 and \mathbf{y}_4 are the x and y column vector of T_0^4 respectively and \mathbf{a} is the approach vector. Thus the solution for θ_5 is:

$$\sin \vartheta_5 = \mathbf{a} \cdot \mathbf{x}_4$$

$$\cos \vartheta_5 = -(\mathbf{a} \cdot \mathbf{y}_4)$$

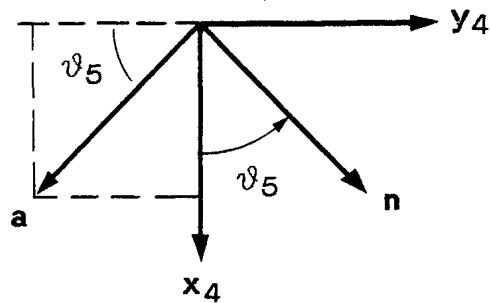


Figure 10 Joint Five Solution

$$\begin{aligned}\theta_5 &= \text{atan2} \left[\frac{\sin \theta_5}{\cos \theta_5} \right] ; \quad -\pi \leq \theta_5 \leq \pi \\ &= \text{atan2} \left[\frac{(C_1 C_{23} C_4 - S_1 S_4) a_x + (S_1 C_{23} C_4 + C_1 S_4) a_y - C_4 S_{23} a_z}{C_1 S_{23} a_x + S_1 S_{23} a_y + C_{23} a_z} \right]\end{aligned}\tag{52}$$

If $\theta_5 \approx 0$, then the degenerate case occurs.

Joint Six Solution. Up to now, we have aligned the axis of joint 6 with the approach vector. Next we need to align the orientation of the gripper to ease picking up the object. The criterion for doing this is to set $\mathbf{s} = \mathbf{y}_6$. Looking at the projection of the hand coordinate frame $(\mathbf{n}, \mathbf{s}, \mathbf{a})$ on the $\mathbf{x}_5-\mathbf{y}_5$ plane, it can be shown that the followings are true (see Figure 11):

$$\sin \theta_6 = \mathbf{n} \cdot \mathbf{y}_5 ; \cos \theta_6 = \mathbf{s} \cdot \mathbf{y}_5 \quad (53)$$

where \mathbf{y}_5 is the y column vector of \mathbf{T}_0^5 and \mathbf{n} and \mathbf{s} are the normal and sliding vectors of \mathbf{T}_0^6 respectively. Thus the solution for θ_6 is:

$$\begin{aligned} \theta_6 &= \text{atan2} \left[\frac{\sin \theta_6}{\cos \theta_6} \right] ; -\pi \leq \theta_6 \leq \pi \\ &= \text{atan2} \left[\frac{(-S_1 C_4 - C_1 C_{23} S_4)n_z + (C_1 C_4 - S_1 C_{23} S_4)n_y + (S_4 S_{23})n_z}{(-S_1 C_4 - C_1 C_{23} S_4)s_z + (C_1 C_4 - S_1 C_{23} S_4)s_y + (S_4 S_{23})s_z} \right] \end{aligned} \quad (54)$$

If the degenerate case occurs, then $(\theta_4 + \theta_6)$ equals to the total angle required to align the sliding vector (\mathbf{s}) and the normal vector (\mathbf{n}). If the FLIP toggle is on

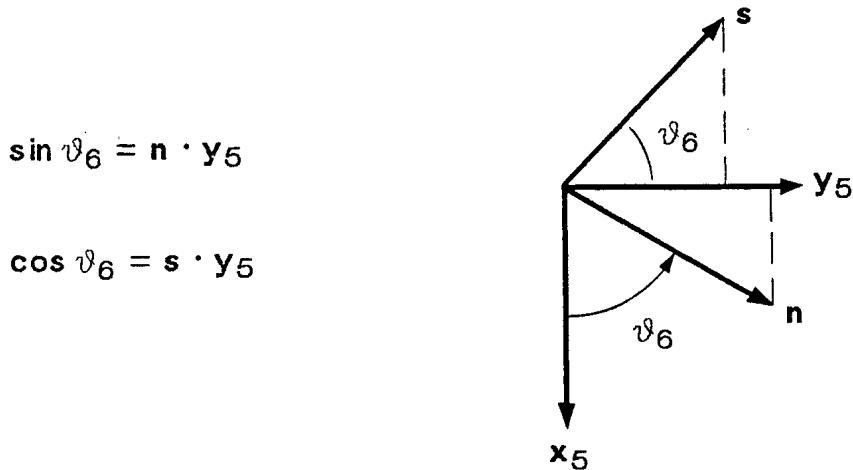


Figure 11 Joint Six Solution

(i.e. FLIP=1), then $\theta_4 = \theta_4 + \pi, \theta_5 = -\theta_5$, and $\theta_6 = \theta_6 + \pi$.

In summary, there are eight solutions to the inverse kinematics problem of a six-joint PUMA robot arm. There are four solutions for the first three joint solutions - two for the right shoulder arm configuration and two for the left shoulder arm configuration. For each arm configuration, Eqs. 26, 35, 42, 49, 52, and 54 give one set of solution $(\theta_1, \theta_2, \theta_3, \theta_4, \theta_5, \theta_6)$ and $(\theta_1, \theta_2, \theta_3, \theta_4 + \pi, -\theta_5, \theta_6 + \pi)$ (with the FLIP toggle on) give another set of solution.

5. DECISION EQUATIONS FOR THE ARM CONFIGURATION INDICATORS

In the previous section, the arm solution of a PUMA robot arm has been derived. The solution is not *unique* and depends on the arm configuration indicators specified by the user. These arm configuration indicators (ARM, ELBOW and WRIST) can also be determined from the joint angles. In this section, we shall derive the respective decision equation for each arm configuration indicator. The signed value of the decision equation (positive, zero, or negative) provide an indication of the arm configuration as defined in Eqs. 9-11.

For the ARM indicator, following the definition of the RIGHT/LEFT arm, a decision equation for the ARM indicator can be found to be:

$$\begin{aligned} g(\theta, \mathbf{p}) &= \mathbf{z}_0 \cdot \frac{\mathbf{z}_1 \times \mathbf{p}'}{\|\mathbf{z}_1 \times \mathbf{p}'\|} = \mathbf{z}_0 \cdot \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ -\sin\theta_1 & \cos\theta_1 & 0 \\ p_x & p_y & 0 \end{vmatrix} \cdot \frac{1}{\|\mathbf{z}_1 \times \mathbf{p}'\|} \\ &= \frac{-p_y \sin\theta_1 - p_x \cos\theta_1}{\|\mathbf{z}_1 \times \mathbf{p}'\|} \end{aligned} \quad (55)$$

where $\mathbf{p}' = (p_x, p_y, 0)^T$ is the projection of the position vector \mathbf{p} (Eq. 14) onto the $\mathbf{x}_0\text{-}\mathbf{y}_0$ plane, $\mathbf{z}_1 = (-\sin\theta_1, \cos\theta_1, 0)^T$ from the third column vector of \mathbf{T}_0^1 , and $\mathbf{z}_0 = (0, 0, 1)^T$.

If $g(\theta, \mathbf{p}) > 0$, then the arm is in the RIGHT arm configuration.

If $g(\theta, \mathbf{p}) < 0$, then the arm is in the LEFT arm configuration.

If $g(\theta, \mathbf{p}) = 0$, then the criterion for finding the LEFT/RIGHT arm configuration cannot be uniquely determined. The arm is within the inner cylinder of radius d_2 in the workspace (see Figure 6). In

this case, it is default to the RIGHT arm ($ARM = +1$).

Since the denominator of the above decision equation is always positive, the determination of the LEFT/RIGHT arm configuration is reduced to checking the sign of the numerator of $g(\theta, \mathbf{p})$:

$$ARM = \text{sign}(g(\theta, \mathbf{p})) = \text{sign}(-p_x \cos \theta_1 - p_y \sin \theta_1) \quad (56)$$

where the sign function is defined in Eq. 49. Substituting the x and y components of \mathbf{p} from Eq. 14, Eq. 56 becomes:

$$ARM = \text{sign}(g(\theta, \mathbf{p})) = \text{sign}(g(\theta)) = \text{sign}(-d_4 S_{23} - a_3 C_{23} - a_2 C_2) \quad (57)$$

Hence from the decision equation in Eq. 57, one can relate its signed value to the ARM indicator for the RIGHT/LEFT arm configuration as:

$$ARM = \text{sign}(-d_4 S_{23} - a_3 C_{23} - a_2 C_2) = \begin{cases} +1 & \Rightarrow \text{RIGHT arm} \\ -1 & \Rightarrow \text{LEFT arm} \end{cases} \quad (58)$$

For the ELBOW arm indicator, we follow the definition of ABOVE/BELLOW arm to formulate the corresponding decision equation. Using $(\mathbf{p}_2^4)_y$ and the ARM indicator in the Table 2, the decision equation for the ELBOW indicator is based on the sign of the y-component of the position vector of $\mathbf{A}_2^3 \cdot \mathbf{A}_3^4$ and the ARM indicator:

$$ELBOW = ARM \cdot \text{sign}(d_4 C_3 - a_3 S_3) = \begin{cases} +1 & \Rightarrow \text{ELBOW above wrist} \\ -1 & \Rightarrow \text{ELBOW below wrist} \end{cases} \quad (59)$$

For the WRIST indicator, we follow the definition of DOWN/UP wrist to obtain a positive dot product of the \mathbf{s} and \mathbf{y}_5 (or \mathbf{z}_4) unit vectors:

$$WRIST = \begin{cases} +1 ; \text{ if } \mathbf{s} \cdot \mathbf{z}_4 > 0 \\ -1 ; \text{ if } \mathbf{s} \cdot \mathbf{z}_4 < 0 \end{cases} = \text{sign}(\mathbf{s} \cdot \mathbf{z}_4) \quad (60)$$

If $\mathbf{s} \cdot \mathbf{z}_4 = 0$, then the WRIST indicator can be found from:

$$WRIST = \begin{cases} +1 ; \text{ if } \mathbf{n} \cdot \mathbf{z}_4 > 0 \\ -1 ; \text{ if } \mathbf{n} \cdot \mathbf{z}_4 < 0 \end{cases} = \text{sign}(\mathbf{n} \cdot \mathbf{z}_4) \quad (61)$$

Combining Eqs. 60 and 61, we have

$$WRIST = \begin{cases} sign(\mathbf{s} \cdot \mathbf{z}_4) & ; \text{ if } \mathbf{s} \cdot \mathbf{z}_4 \neq 0 \\ sign(\mathbf{n} \cdot \mathbf{z}_4) & ; \text{ if } \mathbf{s} \cdot \mathbf{z}_4 = 0 \end{cases} = \begin{cases} +1 & ; WRIST DOWN \\ -1 & ; WRIST UP \end{cases} \quad (62)$$

These decision equations provide a verification of the arm solution. We use them to preset the arm configuration in the direct kinematics and then use the arm configuration indicators to find the inverse kinematics solution. (See Figure 12)

6. COMPUTER SIMULATION

A computer program was written to verify the validity of the inverse solution of the PUMA robot arm shown in Figure 2. The software initially generates all the locations in the workspace of the robot within the joint angles limits. They are inputed into the direct kinematics routine to obtain the arm matrix \mathbf{T} . These joint angles are also used to compute the decision equations to obtain the three arm configuration indicators. These indicators together with the arm matrix \mathbf{T} are fed into the inverse solution routine to obtain the joint angle solution which should agree to the joint angles fed into the direct kinematics routine previously. A computer simulation block diagram is shown in Figure 12 and a list of the computer program written in PASCAL is given in the APPENDIX.

7. CONCLUSION

The kinematics and inverse kinematics problems of a PUMA robot arm have been discussed. The inverse solution is determined with the assistance of three arm configuration indicators (ARM, ELBOW, and WRIST). There are eight solutions to a six-joint PUMA robot arm - four solutions for the first three joints and for each arm configuration two more solutions for the last three joints. Computer simulation of the direct and inverse kinematics showed that the above derived arm solution is correct. This approach, with appropriate modification and adjustment, can be generalized to other simple industrial robots with rotary joints.

8. ACKNOWLEDGEMENT

The authors would like to thank Robert Horner who wrote a "C" program to verify the above direct and inverse kinematics equations together with their corresponding decision equations. The authors also would like to thank Richard Jungclas who wrote the above kinematic equations in PASCAL and verified

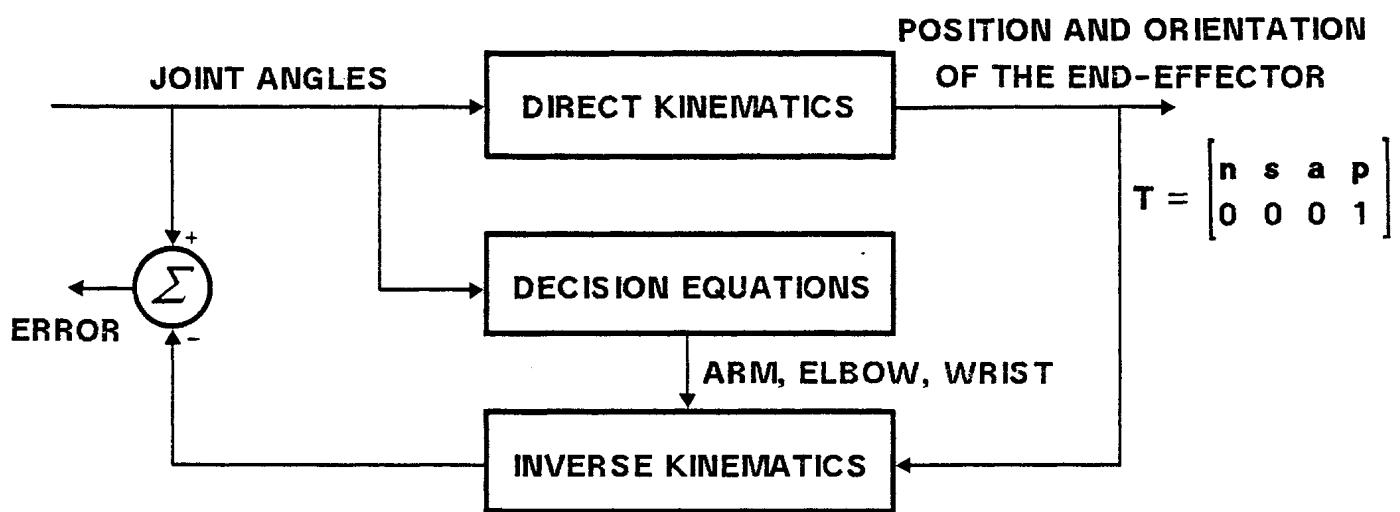


Figure 12. Computer Simulation of Joint Solution

them by controlling a PUMA robot arm from an IBM PC.

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JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
 00      {${linenr:132,$pagesize:60}
 01      {$title:'Main PUMA Program (main.pas)',$subtitle:'Last change 4-3-84'}
 02      {$$SPEED,$DEBUG-, $11st+, $INDEXCK-, $NILCK-, $RANGECK-, $STACKCK-, $OCODE-}
 03
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Written by: Richard M. Jungclas

This system is used for the verification and development of the direct kinematics and the inverse kinematics solutions for a six jointed PUMA robot. The system uses "A Geometric Approach in Solving the Inverse Kinematics of PUMA Robots" developed by C.S.G. Lee and M. Ziegler of the Electrical and Computer Engineering department of the University of Michigan.

The actual PUMA routines were developed for an offline robot programming project using the IBM PC being developed at the Robot Systems Division of CRIM. As a result these solutions have been extensively tested and compared with the solutions reported by VAL II. We have found the solutions from the IBM PC are within +/- 0.005 of a degree for the angles and within +/- 0.005 of a millimeter for positions reported by VAL II. Generally, the IBM PC gives solutions within +/- 0.001 of a degree or of a millimeter.

The actual interface given here is a bit simplistic, but serves to illustrate how the PUMA routines are used. While the interface given below does not allow specifying of either the tool to mount transformation or the robot reference to world transformation, the solutions implemented allow for these transformations. The interface assumes an identity transformation for the tool to mount transformation and assumes that the world coordinate frame is a the base of link0 but oriented the same as the "shoulder" (link1) coordinate frame.

The interface uses a menu driven by single character inputs. The menu is displayed on the top, left part of the screen. The key used to select the menu item is given in parenthesis. The current system status is displayed on the top, right portion of the screen. Data, various prompts and error messages are display on the lower

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
54 half of the screen.

55 Locations can be specified in either world cartesian, robot cartesian
56 or robot joint coordinates frames. The default is the world cartesian
57 coordinate frame. The robot cartesian coordinate frame is exactly the
58 as the VAL II "trans" type locations. The joint coordinate frame is
59 exactly the same as the VAL III "precision point" locations. Locations
60 reported by all three types. The current type is display in the
61 status area of the menu.
62

63 The interface allows you to assign symbolic names of up to 12 characters
64 to any location. The "type" of the location is determined by the
65 current type setting at the time the symbol is defined and cannot be
66 changed. There is no method at the moment of preserving the symbolic
67 names between sessions.
68

69 The current PUMA arm configuration is also display in the status area.
70

71
72
73
74 The main commands are:
75

76 Move Moves the robot to location specified by either a
77 symbolic location or directly from the keyboard.
78 Entries from the keyboard use the "type" from the
79 current setting. The location in all three types is
80 reported for valid solutions.

81 Name Names the current location. The type of the symbolic
82 location is the "type" from the current setting.
83

84 Robot Config. Starts a submenu allowing changes of all the
85 Robot Configuration settings.
86

87 Where Reports the current location in all three types
88
89 Exit Terminates the program.
90

91 The Robot Configuration commands are:
92
93
94 Left/Right Changes the PUMA arm configuration to Left arm or
95 Right arm.
96 Above/Below Changes the PUMA arm configuration to elbow Above
97 the wrist or elbow Below the wrist.
98 Up/Down Changes the PUMA arm configuration to wrist Up or
99 wrist Down.
100

101 Fl1p/NoFl1p Allows the wrist configuration to changed or not.
102
103
104
105
106

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JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
107 Joint/Cartesian Specifies either Joint or Cartesian coordinate
108 frames. When cartesian coordinates are specified
109 a World/Robot menu item will appear to allow
110 selection of the type of cartesian coordinate frames.
111
112 Robot/World Specifies the type of cartesian coordinates. Only
113 present if Cartesian coordinate are chosen.
114
115 Trace/Notrace Permits the tracing of valid location in a file
116 named PUMA.DBG on the current directory.
117
118 Debug/Production Permits the tracing of debugging information in
119 a file named PUMA.DBG on the current directory.
120
121
122 The system uses a standard device call sercom as a mean of collecting
123 debugging information, data, etc.. By default this the file PUMA.DBG
124 is assigned to this device during initialization.
125
126
127 }
128
129 0 {$INCLUDE:'global.inc'}
130 157 {$LIST+}
131 0 {$INCLUDE:'debug.inc'}
132 23 {$LIST+}
133 0 {$INCLUDE:'menu.inc'}
134 48 {$LIST+}
135
136 program robot(input,output);
137
138 uses debug;
139 uses globals;
140 uses menu_functions;
141
142
143 var
144 last move,
145 invalid command,
146 leave pgm: boolean;
147 command,
148 spec: char;
149
150
151
152
153 var [public]
154 sercom: file;
155
156
```

Main PUMA Program (main.pas)
Last change 4-3-84

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15:47:27

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

Syntab 157 Offset Length Variable - INITIALIZE
- 2 2 Return offset, Frame length

10 158 Procedure config_robot; external;

Syntab 158 Offset Length Variable - CONFIG_ROBOT
- 2 2 Return offset, Frame length

10 159 Procedure writeloc(var dev: file1); external;

Syntab 159 Offset Length Variable - WRITELOC
- 4 2 Return offset, Frame length :File1 VarP
+ 6 2 DEV

10 160 Procedure nameloc; external;

Syntab 160 Offset Length Variable - NAMELOC
- 2 2 Return offset, Frame length

10 161 Function move(var tracefil:file1): boolean; external;

Syntab 161 Offset Length Variable - MOVE
- 4 4 Return offset, Frame length :Boolean VarP
- 2 1 (function return) :File1 VarP
+ 6 2 TRACEFIL

MOVE

JG IC Line# Microsoft MS-Pascal Compiler. MS-DOS 8086 Version 3.11, 05/83
10 162 {\$PAGE+}
begin { MAIN }

164 {
165 { Here is where we wake up. The first things that have to be done is
166 to initialize the system.
167 }
168 }
169 {
170 initialize;
171 }
172 { This is the root level of the menu.
173
174 leave_pgm is a flag for program termination. When it is set to
175 true, program execution is done.
176
177 Invalid command is a flag that is used within each menu in the
178 system. When it is true, it indicates that the PREVIOUS command the
179 user typed was invalid. This flag is used in determining whether or
180 not the prompt error should be erased and the menu reprinted. If the
181 last user command was invalid, there is probably an error message in
182 prompt area, meaning the user should be prompted without clear that
183 area first.
184
185 }
186
187 last_move := false;
188 leave_pgm := false;
189 invalid_command := false;
190
191 while not leave_pgm do begin
192
193 if (not invalid_command)
194 then begin
195 display_menu(menu_flag,'PUMA');
196 menu_item('Robot configuration');
197 menu_item('Move');
198 menu_item('Name this location');
199 menu_item('Where');
200 menu_item('Exit the program');
201 end;
202 else invalid_command := false;
203
204 if last_move
205 then begin;
206 data_prompt;
207 write_loc(output);
208 last_move := false;
209 end;
210
211 command_prompt;
212 write('Enter PUMA command: ');
213 repeat until gets(command,spec);
214

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
12      215
12      216      data_prompt;
13      217      case command of
13      218
13      219      'm','M': last_move := move(sercom); !Move the robot
13      220
13      221
13      222      'n','N': nameloc; !Name to current location
13      223
13      224
13      225      'r','R': config_robot; !Change robot configuration
13      226
13      227
13      228      'w','W': begin; !Report robot location
14      229          writeln('Robot_location:');
14      230          writeloc(output);
14      231      end;
13      232
13      233
13      234      'e','E' : leave_pgm := true; !Program termination
13      235
13      236
13      237
13      238      otherwise begin !Invalid commands
14      239          invalid_command := true;
14      240          write('`',command,'') is an invalid command')
14      241      end;
13      242
13      243
12      244      end;
11      245
11      246      end;
11      247      cls;
11      248
12      249      end;
00      250      end.

Syntab 250  Offset Length Variable
0       666  Return offset, Frame length
0       64   TO
0       64   H
0       64   HI
0       64   TOI
28     1    SPEC
0       14   CONFIG
0       24   THETA
30     636  SERCOM
0       8    VERSION
0       24   ROB_XYZ
0       1    COMMAND
26     1    FIRST_STR
0       2    MENU_FLAG
0       1    LAST_MOVE

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
24 1 LEAVE PGM :Boolean Static
0 2 MENU CURSOR :Integer Static External
0 2 COORDS TYPE :Integer Static External
22 1 INVALID_COMMAND :Boolean Static

Errors Warns In Pass One
0 0

```
JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
00      {$LINESIZE:132,$PAGESIZE:60}
01      {$TITLE:'Main program routines(routines.pas)',$SUBTITLE:'Last change: 4-3-84'}
02      {$$SPEED,$DEBUG-,{$LIST+,{$INDEXCK-$NILCK-$RANGECK-$STACKCK-$OCODE-}}
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```

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Written by: Richard M. Jungclas

```
00      {$INCLUDE:'global.inc'}
01      {$LIST+}
02      {$INCLUDE:'debug.inc'}
03      {$LIST+}
04      {$INCLUDE:'menu.inc'}
05      {$LIST+}
06      {$INCLUDE:'puma.inc'}
07      {$LIST+}
08
09
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```


Main program routines(routines.pas)
Last change: 4-3-84

Page 3
04-04-84
14:16:56

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

= 21 96 theta[4] := 0.0;
= 21 97 theta[5] := 0.0;
= 21 98 theta[6] := 0.0;
= 21 99

100 {
101 Find the initial position of robot
102 }
21 103 homotran;
21 104 inverse;
105
106 if not joint_check
21 107 then writewt('Initial robot configuration bad');
108
109
= 21 111 first_STR := nil; !No symbols to start
112 {
113 {
114 Predefined symbols
115 }
21 116 new(temp_STR);
21 117 temp_STR@.symname := 'ready';
21 118 temp_STR@.data := theta;
21 119 temp_STR@.ctype := joint_type;
21 120 temp_STR@.used := true;
21 121 temp_STR@.next_STR := first_STR;
= 21 122 first_STR := temp_STR;
123
124
= 21 125 menu_flag := true; !Full menu to start
= 21 126 coords_type := world_type; !default user to world coords
10 127 end;
128
129 Syntab Offset Length Variable - INITIALIZE
- 2 10 Return offset, Frame length : Integer
- 2 2 I : Integer
- 4 2 J : Boolean
- 6 1 INVERTIBLE : Pointer
- 8 2 TEMP_STR : Pointer

INITIALIZE

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

10 130 {\$PAGE+}
Procedure config_robot;

131
132 {
133 PROCEDURE CONFIG_ROBOT;
134
135 Purpose: Acts as the driver for the robot configuration
136 commands.
137
138 }
139
140 var command, spec: char; leave, invalid_command: boolean; valid_command flag
141 begin
142 command, spec: char; leave, invalid_command: boolean; valid_command flag
143
144 leave, invalid_command: boolean; valid_command flag
145
146 begin
147 leave := false; invalid_command := false;
148 begin
149 { This menu contains the robot configuration programming commands.
150 }
151
152 leave := false;
153 invalid_command := false;
154 begin
155 while not leave do
156 begin
157 if not invalid_command
158 then begin
159 if not invalid_command
160 then begin
161 display menu(menu_flag, 'PUMA/config');
162 bmenu_item('PUMA menu');
163 if config[0] = 1
164 then menu_item('Left arm')
165 else menu_item('Right arm');
166 if config[1] = 1
167 then menu_item('Below elbow')
168 else menu_item('Above elbow');
169 if config[2] = 1
170 then menu_item('Up wrist')
171 else menu_item('Down wrist');
172 if config[3] = 1
173 then menu_item('Noflip wrist')
174 else menu_item('Flip wrist');
175 case coords_type of
176 world_type, robot_type:
177 begin
178 menu item('Joint coordinates');
179 if coords_type = world_type
180 then gmenu item('M', 'Robot coordinates')
181 else menu_item('World coordinates');
182 end;
/

CONFIG_ROBOT

```
JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
      joint type;
      menu_item('Cartesian coordinates');
otherwise
;
end;
if config[5] = 0
  then gmenu_item('E', 'Debug mode')
  else menu_item('Production mode');
if config[6] = 0
  then menu_item('Trace moves')
  else gmenu_item('O', 'No trace');

display_status;
end;

invalid_command := false;
command_prompt;
write('Enter robot programming command: ');
repeat until getc(command,spec);
data_prompt;

case command of
  205
  206
  207
  '--': leave := true;           !Back to PUMA menu
  208
  209
  210
  211
  'l', 'L': config[0] := -1;    !Left Arm
  212
  213
  'r', 'R': config[0] := 1;     !Right arm
  214
  215
  216
  217
  'b', 'B': config[1] := -1;    !Below elbow
  218
  219
  'a', 'A': config[1] := 1;     !Above elbow
  220
  221
  222
  223
  'd', 'D': config[2] := 1;     !Wrist down
  224
  225
  'u', 'U': config[2] := -1;   !Wrist up
  226
  227
  228
  229
  'f', 'F': config[3] := 1;     !Flip of wrist allowed
  230
  231
  'n', 'N': config[3] := -1;   !Noflip of wrist allowed
  232
  233
  234
  'c', 'C': coords_type := robot type; !punch robot cartesian coords
```

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
Last change: 4-3-84

      236   'M': coords_type := robot_type; !Coordinates
      237   'J', 'J': coords_type := joint_type; !punch joint coords.

      240
      241   'm', 'M': coords_type := robot_type; !Coordinates
      242   'w', 'W': coords_type := world_type;

      243
      244   'e', 'E': config[5] := 1; !Debug Mode
      245   'p', 'P': config[5] := 0; !Production mode

      246
      247   't', 'T': begin
      248       config[6] := 1; !Trace on
      249       writeln(sercom);
      250   end;
      251
      252
      253
      254   otherwise begin
      255       write('. ', command, ') is an invalid command');
      256       invalid_command := true;
      257   end;
      258
      259   'O', 'o': config[6] := 0; !Trace off
      260
      261
      262
      263   264   write('. ', command, ') is an invalid command');
      264   265   invalid_command := true;
      265   266   end;
      266
      267   268   end;
      268   269   end;
      269   270   end;
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```

Main program routines(routines.pas)
Last change: 4-3-84

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JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
20 271 {\$PAGE+}
procedure writeloc(var dev: file1);
273
274 {
275 PROCEDURE WRITELOC(var DEV: file1);
276
277 Purpose: Writes out the robot location in robot coords..
278 world coords. and joint angles.
279
280 }
281 var T2, T3, T4, T5, T6: matrix;
282
283 begin
284 itheta := theta;
285 tmatrs(T2, T3, T4, T5, T6);
286 rob_xyz := get_xyzoat(T6);
287
288 if theta :=
289 tmatrs := mat_mult(T6, T0);
290 rob_xyz := mat_mult(H, tmatrs);
291
292 {add base and hand displacements}
293 tmatrs := mat_mult(H, tmatrs);
294 xyz := get_xyzoat(tmatrs);
295
296 writeln(dev, 'world X='',xyz[1]:8:3,' Y='',xyz[2]:8:3,' Z='',xyz[3]:8:3,
297 0='',xyz[4]:8:3,' A='',xyz[5]:8:3,' T='',xyz[6]:8:3);
298 writeln(dev, 'robot X='',rob_xyz[1]:8:3,' Y='',rob_xyz[2]:8:3,' Z='',rob_xyz[3]:8:3,
299 0='',rob_xyz[4]:8:3,' A='',rob_xyz[5]:8:3,' T='',rob_xyz[6]:8:3);
300 writeln(dev, 'joint 1='',theta[1]:8:3,' 2='',theta[2]:8:3,' 3='',theta[3]:8:3,
301 4='',theta[4]:8:3,' 5='',theta[5]:8:3,' 6='',theta[6]:8:3);
302
303 writeln(dev);
304 end;
10 305

Symtab 305 Offset Length Variable - WRITELOC
- 4 386 Return offset, Frame length :F1le VarP
+ 6 2 DEV :Array
- 64 64 T2 :Array
- 128 64 T3 :Array
- 192 64 T4 :Array
- 256 64 T5 :Array
- 320 64 T6 :Array

WRITELOC

JG IC Line# 306 {\$PAGE+} Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

10 307 Procedure nameloc;

```

308 {
309   PROCEDURE NAMELOC;
310
311   Purpose:      Gives the current valid robot location a symbolic
312   name.
313
314 }
315
316   var   command,
317         spec;      char;
318         temp_STR;  STR_ptr;
319         name;      name_lstr;
320         input_line; consol_input_lstr;
321         temp_Type; integer;
322
323 begin
324   write('Enter robot location name? ');
325   readin(input_line);
326   trim(input_line);
327   name:=input_line;
328
329   temp_STR := find_STR(name);
330
331   if temp_STR <> nil
332     then_begin; !Matches existing name
333       if temp_STR@.used
334         then_begin; !Overwrite existing used location?
335           then_write('Overwrite existing used location? ');
336           else write('Overwrite existing unused location? ');
337           repeat until getc(command,spec);
338             if (command <> 'Y') and (command > 'Y')
339               then begin;
340                 data_prompt;
341                 write('Location not changed!');
342                 return;
343               end
344             else if temp_STR@.used
345               then_begin;
346                 data_prompt;
347                 write('Previous references use the redefined location! ');
348               end
349             else data_prompt;
350           end
351           temp_type := temp_STR@.ctype; !Used the existing coords type
352
353   else begin; !allocate new symbol record
354     temp_type := world_type;
355     case coords_type of
356       23   357       world_type, robot_type;
358
NAMELOC

```

Main program routines(routines.pas)
Last change: 4-3-84

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JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

23 359 temp_type := coords_type;

23 360 joint type:
23 361 temp_type := joint_type;
22 362 end;
22 363
22 364
22 365 new(temp_STR);
22 366 temp_STR@.symname := name;
22 367 temp_STR@.ctype := coords_type; current default setting
22 368 temp_STR@.used := false;
22 369 temp_STR@.next_STR := first_STR;
22 370 first_STR := temp_STR;
= 22 371
21 372 end;
22 373 case temp_type of
22 374
22 375 world type:
22 376 Begin {add base and hand displacements}
= 23 377 xyz := rob_xyz;
= 23 378 homotran;
= 23 379 homotran;_xyz;
= 23 380 tmatrix := mat_mult(tmatrix,T0);
= 23 381 tmatrix := mat_mult(H,tmatrix);
= 23 382 temp_STR@.data := get_xyzoat(tmatrix);
22 383 end;
22 384
22 385 robot type:
22 386 temp_STR@.data := rob_xyz;
22 387 joint type:
22 388 temp_STR@.data := theta;
22 389
21 390 end;
10 391
10 392 end;
10 393 end;

Syntab 393 Offset Length Variable - NAMELOC
- 2 170 Return offset, Frame length :Char
- 2 1 COMMAND :Char
- 4 1 SPEC :Array
- 20 14 NAME :Pointer
- 6 2 TEMP STR :Array
- 102 82 INPUT LINE :Integer
- 104 2 TEMP_TYPE :Integer

NAMELOC

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

```
394 {$PAGE+}
20   395 function move(var tracefil: file1): boolean;
396   397 {
398     FUNCTION MOVE(var TRACEFIL: file1): boolean;
399
400     Purpose:      Moves robot to new location returning true
401                 if the location was within robot's workspace.
402   }
403
404   var
405     406       command,
406       spec:           char;          !to hold user's command
407     407       leave,          boolean;        !flag for returning up one level
408     408       full:           full;          !command menu flag
409     409       x,             x;            !Generalize robot coordinates
410     410       y,             y;
411     411       z,             z;
412     412       o,             o;
413     413       a,             a;
414     414       t,             t;            real;
415     415       temp_type,
416     416       temp_coord_type, integer;
417     417       l:              integer;
418     418       temp_ptr:        PTR PTR;
419     419       name_lstr:       name_lstr;
420     420       input_line:      input_line;
421     421       consol_input_lstr;
422
423 begin
424   424       leave := false;
425   425       full := false;
426   426       menu_flag := true;
427   427       c1s:=
428   428
429   429       while not leave do
430   430       begin
431   431       begin
432   432       while not leave do
433   433       begin
434   434       leave := true;
435   435       display menu(full, 'Move command');
436   436       bmenu item('PUMA menu');
437   437       menu item('Direct from Keyboard');
438   438       menu item('Named Location');
439   439
440   440       command prompt;
441   441       write('Enter move input selection: ');
442   442       repeat until getc(command,spec);
443   443       data_prompt;
444   444
445   445       case command of
446
MOVE
```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

```
* 24    448      '-' : return;           !Backout
* 24    449      'd', 'D' : begin;        !Keyboard selection
25    450      case coords_type of
26    451      455      world_type, robot_type: begin;
27    456      457      If coords_type = World_type
27    458      then writeln('World-XYZDAT location');
27    459      else writeln('Robot XYZDAT location');
27    460      write('Enter X position: ');
27    461      readln(x);
27    462      write('Enter Y position: ');
27    463      readln(y);
27    464      write('Enter Z position: ');
27    465      readln(z);
27    466      write('Enter O angle: ');
27    467      readln(o);
27    468      write('Enter A angle: ');
27    469      readln(a);
27    470      write('Enter T angle: ');
27    471      readln(t);
27    472      xyz[1] := x;
27    473      xyz[2] := y;
27    474      xyz[3] := z;
27    475      xyz[4] := o;
27    476      xyz[5] := a;
27    477      xyz[6] := t;
27    478      end;
27    479      joint_type: begin;
27    480      481      joint_type: begin;
27    482      483      writeln('Joint position');
27    484      write('Enter J1 angle: ');
27    485      readln(itheta[1]);
27    486      write('Enter J2 angle: ');
27    487      readln(itheta[2]);
27    488      write('Enter J3 angle: ');
27    489      readln(itheta[3]);
27    490      write('Enter J4 angle: ');
27    491      readln(itheta[4]);
27    492      write('Enter J5 angle: ');
27    493      readln(itheta[5]);
27    494      write('Enter J6 angle: ');
27    495      readln(itheta[6]);
26    496      end;
26    497      498  end;
```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83 .
main program routines(routines.pas)

```
'n', 'N': begin;
  write('Enter robot location name? ');
  readln(input_line);
  trim(input_line);
  name:=input_line;

  if (name = NULL)
    then begin
      leave := false;
      data_prompt;
    end
    else begin;
      temp_STR := first_STR;
      while temp_STR <> nil and then temp_STR^.symname <> name do
        temp_STR := temp_STR^.next_STR;

      if temp_STR <> nil
        then begin; !Matches existing name
          temp_STR^.used := true;
          temp_type := temp_STR^.ctype;
          case temp_type of
            world_type, robot_type:
              xyz := temp_STR^.data;
              joint_type:
                Itheta := temp_STR^.data;
          end;
        end
        else begin; !Symbol not found
          data_prompt;
          leave := false;
          writeln('Location ...,name, ... not found');
        end;
      end;
    end;
  end;

otherwise begin;
  writeln('(: command,) is an invalid selection');
  leave := false;
end;
end;
```

clear upper;
data_prompt;
position_cursor(15,0);

case temp_type of
 world_type, robot_type:
 begin

```
JG IC Line# Microsoft MS-Pascal Compiler. MS-DOS 8086 Version 3.11, 05/83
00      {$LINESIZE:132 $PAGESIZE:60}
1      {$$Title:'PUMA robot routines',$subtitle:'Last change: 4-3-84 rmj'}
2      {$$SPEED,$DEBUG-,LIST+,$INDEXCK-,NILCK-,STACKCK-,$RANGECK-,$OCODE-}
3
4      {$$MESSAGE:'Enter 1 for debugging information, 0 for normal operation',
5      $INCONST:puma_debug,$INCONST:tmatmats_debug,$INCONST:homo_debug}
6
7      {
8
9      }
```

```
11      University of Michigan
12          College of Engineering
13          Center for Robotics and Integrated Manufacturing
14          Robot System Division
15          2514 East Engineering Building
16          Ann Arbor, MI 48109
17          (313) 764-4343
```

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Written by: Richard M. Jungclas

```
21
22
23
24
25
26      {$INCLUDE:'global.inc'}
27
28      0      {$LIST+}
29      0      {$INCLUDE:'debug.inc'}
30      0      {$LIST+}
31      0      {$INCLUDE:'puma.inc'}
32
33      30      {$$Title:'PUMA robot routines',$subtitle:'Last change: 4-3-84 rmj'}
34      33      Implementation of puma;
35      34      Uses Globals;
36      35      Uses debug;
37      36
38      function a2srqq(consts a,b: real): real; external;
```

```
Symtab      38      Offset Length      Variable - A2SRQQ
                  - 12      2      Return offset, Frame length
                  + 6       4      (function return)      :Real
                  + 12      4      A      :Real
                  + 8       4      B      :Real
                                         Const   VarsP
                                         Const   VarsP
                                         :Real
                                         ! Joint limits
39
40
41      var
42      sercom [extern]: file1;
43      max_degree: j_matrix;
```

RUMA robot routines
Last change: 4-3-84 rmj

```

Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
 44 min_degree: j_matrix;
 45 model_verts: rmat_ptr;
 46 A10, !link 1 to link 1-1 transformations
 47 A21,
 48 A32,
 49 A43,
 50 A54,
 51 A65: matrix;
 52
 53 const
 54   D2 = 149.09;
 55   A2 = 431.80;
 56   A3 = -20.32;
 57   D4 = 433.07;
 58   D6 = 56.25;
 59 {
 60   { Most of these constants are pre-calculated to maximize numerical
 61     accuracy, which at best is limited to 7 decimal digits}
 62   f2_a2 = 863.60;
 63   D2_sq = 22227.83;
 64   A2_sq = 186451.2;
 65   A3_sq = 412.9024;
 66   D4_sq = 187549.6;
 67   l1 = 433.5465;
 68   l2 = 187962.5;
 69   l5 = 0.04686926;
 70   l6 = 0.9989010;
 71   f2_a2_l1 = 374410.7;
 72   A2_sq_l2 = 374413.8;
 73   A2_D4_A3 = -1511.287;
 74   PI = 3.141593;
 75   twoPI = 6.283185;
 76   f180_p1 = 67.29578;
 77   p1_180 = 0.01745329;
 78   epsilon = 0.001;
 79

```

A2SR09

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

81 {\$PAGE+}

10 82 procedure inverse;

{

85 PROCEDURE INVERSE;

86

87 Purpose: Calculates the inverse kinematics for the PUMA robot
88 arm. It is given the transformation matrix for the
89 position, and calculates the joint angles for that
90 position.

91

92 Calling convention:

93 inverse;

94

95 Global Variables:

96 xyz Contains the proposed xyzoot position of

97 the puma arm.

98 tmatrix The homogenous transformation matrix

99 describing the proposed arm position.

100 itheta Returns the inverse solution of the arm
101 (ie. each of the six joint angles).

102)

103)

104)

105)

106 var

20 107 i: integer;

20 108 px,py,pz,

20 109 ax,ay,az,

20 110 sx,sy,sz,

20 111 nx,ny,nz,

20 112 s1,s2,s3,s4,s5,s23,

20 113 c1,c2,c3,c4,c5,c23,

20 114 pxsq,

20 115 pysq,

20 116 pzsq,

20 117 rsq,

20 118 r,

20 119 sal,cal,sbt,cbt,

20 120 13,14,

20 121 omega,

20 122 z3ax,z3ay,z3az,

20 123 k1,k2,k3,k4,

20 124 t1,t2,t3,t4: real;

20 125 arm,

20 126 arm below,

20 127 k: boolean;

20 128 begin

20 129 config[4] := 0;

21 = 130 assume no error

131 config[4] := 0;

132

95 xyz Contains the proposed xyzoot position of

96 tmatrix The homogenous transformation matrix

97 describing the proposed arm position.

98 itheta Returns the inverse solution of the arm
99 (ie. each of the six joint angles).

100 index position of the hand

101 approach vector components

102 sliding vector components

103 normal vector components

104 joint sines and cosines

105 px * px

106 py * py

107 pz * pz

108 px*px + py*py + pz*pz - D2*D2

109 sqrt(rsq)

110 !Misc sine and cosines theta 2 solution

111 !Misc theta 3

112 !Orientation indicator

113 !Z3 cross a components

114 !Misc constant terms

115

116 !ARM is negative(left)

117 !ARM * BELOW is negative

118 !WRIST * sign(Omega) is negative

119 !assume no error

```

136
137 if coords_type == world_type
138   then begin; !Base coords differs from robot coords.
139     tmatrix := mat_mult(HI, tmatrix);
140     tmatrix := mat_mult(tmatrix, TOI);
141     xyz := get_xyzzat(tmatrix);
142   end;
143
21   144 nx := tmatrix[1,1];
21   145 ny := tmatrix[1,2];
21   146 nz := tmatrix[1,3];
21
21   147 sx := tmatrix[2,1];
21   148 sy := tmatrix[2,2];
21   149 sz := tmatrix[2,3];
21
21   150 ax := tmatrix[3,1];
21   151 ay := tmatrix[3,2];
21   152 az := tmatrix[3,3];
21
21   153 px := tmatrix[4,1] - D6 * ax;
21   154 py := tmatrix[4,2] - D6 * ay;
21   155 pz := tmatrix[4,3] - D6 * az;
21
21   156 pxsq := px * px;
21   157 pysq := py * py;
21   158 pzsq := pz * pz;
21
21   159 k3 := pxsq + pysq;
21   160 config[4] := px * px;
21   161 config[4] := py * py;
21   162 config[4] := pz * pz;
21
21   163 k1 := k3 - d2sq;
21   164 if (k1 < 0)
21   165   then begin
21   166     k1 := -k1;
21   167     if k1 > epsilon
21   168       then begin;
21   169       writeln('Warning: Invalid Position (k1) .');
21   170     end;
21   171   end;
21   172   config[4] := 1;
21   173   end;
21
21   174 k2 := sqrt(k1);
21   175 rsq := k1 + pzsq;
21   176 if rsq < 0
21   177   then begin
21   178     rsq := -rsq;
21   179     if rsq > epsilon
21   180       then begin;
21   181       writeln('Warning: Invalid Position (rsq) .');
21   182     end;
21   183   end;
21   184   config[4] := 1;
21   185   end;
21
21   186 r := sqrt(rsq);

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

```

21   187      arm := (config[0] = -1);           !Set ARM flag
21   188      arm_below := (arm) xor (config[1] = -1);   !Set ARM * BELOW
21   189
21   190  {
21   191    {
21   192      find theta sub 1
21   193    }
21   194    t1 := py*k2;
21   195    t2 := px*k2;
21   196    if not arm
21   197    then begin
21   198      t1 := -t1;
21   199      t2 := -t2;
21   200    end;
21   201    s1 := t1 - px*d2;
21   202    c1 := t2 + py*d2;
21   203    iftheta[1] := a2srqq(s1,c1);
21   204    if abs(k3) < epsilon
21   205    then begin;           !division by zero (invalid position)
21   206      s1 := 0;
21   207      c1 := 0;
21   208    end
22   209    else begin;
22   210      s1 := s1 / k3;
22   211      c1 := c1 / k3;
22   212    end;
21   213    if abs(s1*s1 + c1*c1 - 1.0) > epsilon
21   214    then writeln('Warning: Illegal Position (1) ');
21   215  {
21   216    find theta sub 2
21   217  }
21   218  if abs(r) < epsilon
21   219  then t1 := -1.0
21   220  else begin;           !division by zero (invalid position)
22   221  sa1 := -pz / r;
22   222  cal := k2 / r;
22   223  if not arm
22   224  then cal := -cal;
22   225  cbt := (A2*D4*A3 + rsq) / (r2_a2 * r);  !cosine beta
22   226  t1 := 1.0 - cbt*cbt;
22   227  end;
21   228  if (t1 < 0)
21   229  then begin
22   230      t1 := -t1;
22   231      if t1 > epsilon
23   232      then begin;
23   233      writeln('Warning: Invalid Position (2)');
23   234      config[4] := 1;
22   235      end;
21   236      sbt := sqrt(t1);
21   237      t2 := cal * sbt;
21   238      t2 := cal * sbt;

```

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
21 240 if arm below
21 241 then begin
22 242   t2 := -t2;
22 243   t3 := -t3;
21 244 end;
21 245 s2 := sa1*cbt + t2;
21 246 c2 := ca1*cbt - t3;
21 247 itheta[2] := a2srqq(ss2, cc2);
21 248 if abs(ss2*ss2 + cc2*cc2 - 1.0) > epsilon
22 249 then begin;
22 250   writeln('Warning: Invalid Position (2)');
22 251   config[4] := 1;
21 252 end;
253 {
254   {
255     find theta sub 3
256   }
21 257   13 := (A2_12 - rsq) / f2_A2_11;           !cosine phi
21 258   t1 := 1.0 - 13*13;
21 259   if (t1 < 0)
21 260     then begin
21 261       t1 := -t1;
22 262       if t1 > epsilon
23 263         then begin; writeln('Warning: Invalid Position (3)');
23 264         config[4] := 1;
22 265       end;
21 266     end;
21 267   14 := sqrt(t1);                            !sine phi
21 268   if arm below
21 269   then 14 := -14;
21 270   s3 := 14*15 - 13*16;
21 271   c3 := 13*15 + 14*16;
21 272   itheta[3] := a2srqq(ss3, cc3);
21 273   if abs(ss3*ss3 + cc3*cc3 - 1.0) > epsilon
22 274   then begin;
22 275     writeln('Warning: Invalid Position (3)');
22 276     config[4] := 1;
21 277   end;
21 278
279 {
280   Now for the wrist solution
281 }
282   t1 := itheta[2] + itheta[3];
21 283   while t1 < 0.0 do t1 := t1 + twoPI;      !Needed by PC sin() and cos() funcs.
21 284   s23 := sin(t1);
21 285   c23 := cos(t1);
21 286   if abs(s23*s23 + c23*c23 - 1.0) > epsilon
22 287   then begin;
22 288     writeln('Warning: Illegal Position (23)');
22 289     config[4] := 1;
21 290   end;
21 291   t2 := s1 * c23;
21 292

```

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
21 293 t3 := c1 * c23;
21 294 omega := 0.0;
21 295 z3ax := s1*s23*az - c23*ay; !z3 x a components
21 296 z3ay := c23*ax - c1*s23*az;
21 297 z3az := c1*s23*ay - s1*s23*ax;
21 298 if ((z3ax <> 0.0) or (z3ay <> 0.0) or (z3az <> 0.0)) then begin;
22 299
200 omega := sx*z3ax + sy*z3ay + sz*z3az; ls * (z3 x a)
201 if (abs(omega) < epsilon) then omega := nx*z3ax + ny*z3ay + nz*z3az; ln * (z3 x a)
202 end;
203
204 k := (config[2] = -1) xor (omega < 0.0); !WRIST * sign(omega)
205
206
207 308 if (not k) and (config[3] = 1) !Necessary to flip wrist!!!
208 309 then begin;
209 config[2] := - config[2];
210 k := not k;
211 end;
212
213
214 {
215   find theta sub 4
216 }
217 s4 := c1*ay - s1*ax;
218 c4 := t3*ax + t2*ay - s23*az;
219 if k then begin;
220   s4 := -s4;
221   c4 := -c4;
222 end;
223
224 if (abs(s4) < epsilon) and (abs(c4) < epsilon) !Degenerate case
225 then itheta[4] := theta[4] * pi_180 !theta 4 already aligned, use current value
226 else itheta[4] := a2srqq(s4, c4);
227
228 t1 := itheta[4];
229 while t1 < 0.0 do t1 := t1 + twoPI; !Needed by PC sin() and cos() fns.
230 s4 := sin(t1);
231 c4 := cos(t1);
232
233 {
234   find theta sub 5
235 }
236 s5 := ax*(t3*c4 - s1*s4) + ay*(t2*c4 + c1*s4) - az*c4*s23;
237 c5 := ax*c1*s23 + ay*s1*s23 + az*c23;
238 itheta[5] := a2srqq(s5, c5);
239
240 {
241   find theta sub 6
242 }
243 t4 := -s1*c4 - t3*s4;
244 t3 := c1*c4 - t2*s4;
245

```

JG IC Line# Microsoft MS-Pascal Compiler. MS-DOS 8086 Version 3.11. 05/83
 = 21 346 s6 := t4*nx + t3*ny + t2*nz;
 = 21 347 c6 := t4*sx + t3*sy + t2*sz;
 = 21 348 itheta[6] := a2srqq(s6, c6);
 349

```

350
21 351 for 1:=1 to 6 do
    352     itheta[1] := itheta[1] * f180_p1;
21 353
21 354 if puma_debug or wrd(config[5]) = 1 then
21 355     for i:=1 to 6 do begin
22 356         writeln(sercom,'Joint ',i:1, ' has an angle of ',i*theta[1]:8:3);
21 357     end;
21 358
10 359 end;
10 360
```

Symtab	360	Offset	Length	Variable - INVERSE	Return offset, Frame length	Type
	-	2	270	I		:Integer
	-	2	2	PX		:Real
	-	6	4	AY		:Real
	-	18	4	R		:Real
	-	126	4	AZ		:Boolean
	-	204	1	K		:Real
	-	22	4			:Real
	-	26	4			:Real
	-	42	4			:Real
	-	82	4	C1		:Real
	-	86	4	C2		:Real
	-	90	4	C3		:Real
	-	94	4	C4		:Real
	-	98	4	C5		:Real
	-	102	4	C6		:Real
	-	146	4	L3		:Real
	-	170	4	K1		:Real
	-	174	4	K2		:Real
	-	178	4	K3		:Real
	-	182	4	K4		:Real
	-	150	4	L4		:Real
	-	46	4	NY		:Real
	-	50	4	NZ		:Real
	-	10	4	PY		:Real
	-	14	4	PZ		:Real
	-	30	4	SX		:Real
	-	54	4	S1		:Real
	-	58	4	S2		:Real
	-	62	4	S3		:Real
	-	66	4	S4		:Real
	-	70	4	S5		:Real
	-	74	4	S6		:Real
	-	34	4	SY		:Real
	-	38	4	SZ		:Real
	-	78	4	S23		:Real
	-	106	4	C23		:Real

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

- - 186	4	T1	:Real
- - 190	4	T2	:Real
- - 194	4	T3	:Real
- - 198	4	T4	:Real
- - 200	1	ARM	:Boolean
- - 122	4	RSQ	:Real
- - 134	4	CAL	:Real
- - 142	4	CBT	:Real
- - 110	4	PXSQ	:Real
- - 130	4	SAL	:Real
- - 138	4	SBT	:Real
- - 114	4	PYSQ	:Real
- - 118	4	PZSQ	:Real
- - 154	4	OMEGA	:Real
- - 158	4	Z3AX	:Real
- - 162	4	Z3AY	:Real
- - 166	4	Z3AZ	:Real
- - 202	1	ARM_BELOW	:Boolean

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11. 05/83

10 361 {\$PAGE+}
procedure homotran;

{

364 {
365 PROCEDURE HOMOTRAN;

366 Purpose:
367 Finds the homogeneous transformation matrix
368 specifying the current position of the end-effector
369 of the robot from the XYZAT description of the
370 robot location.

371 Calling convention:
372 homotran;
373 }

374 Global variables:

375 xyz xyzat configuration of robot

376 tmatrix returns the homogeneous transformation of the
377 current position of the end effector of the
378 robot arm.

}

384 var

20 o, !OAT angles in radians
20 a,
20 t,
20 cos0,
20 sin0,
20 cosa,
20 sina,
20 cost,
20 sint; real;

20 begin
21 o := xyz[4];
21 a := xyz[5];
21 t := xyz[6];

21 cos0 := dcos(o);
21 cosa := dcos(a);
21 cost := dcos(t);
21 sin0 := dsin(o);
21 sina := dsin(a);
21 sint := dsin(t);

20 401 cos0 := dcos(o);
21 402 cosa := dcos(a);
21 403 cost := dcos(t);
21 404 sin0 := dsin(o);
21 405 sina := dsin(a);
21 406 sint := dsin(t);

20 407 tmatrix[1,1] := (cos0 * sinT) - (sin0 * sina * cost);
21 408 tmatrix[1,2] := (cos0 * sina * cost) + (sin0 * sint);
21 409 tmatrix[1,3] := -(cosa * cost);
21 410 tmatrix[2,1] := (sin0 * sina * sint) + (cos0 * cost);
21 411 tmatrix[2,2] := - (cos0 * sina * sinT) + (sin0 * cost);
21 412 tmatrix[2,3] := cosa * sint;

21 413 tmatrix[3,1] := (cos0 * sinT) - (sin0 * sina * cost);
21 414 tmatrix[3,2] := (cos0 * sina * cost) + (sin0 * sint);
21 415 tmatrix[3,3] := -(cosa * cost);
21 416 tmatrix[4,1] := (sin0 * sina * sint) + (cos0 * cost);
21 417 tmatrix[4,2] := - (cos0 * sina * sinT) + (sin0 * cost);
21 418 tmatrix[4,3] := cosa * sint;

```
JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
= 21 414 tmatrix[3,1] := sin0 * cosa;
= 21 415 tmatrix[3,2] := - (cos0 * cosa);
= 21 416 tmatrix[3,3] := - sinA;
= 21 417 tmatrix[4,1] := xyz[1];
= 21 418 tmatrix[4,2] := xyz[2];
= 21 419 tmatrix[4,3] := xyz[3];

21   421 if homo_debug or wrd(config[6]) = 1
21   422 then_begin
22   423 writeln(sercom,'tmatrix:');
22   424 prmat(tmatrix);
21   425 end;
21   426
10   427 end;

Symtab 427 Offset Length Variable - HOMOTRAN
        - 2      42 Return offset, Frame length
        - 4      4 A :real
        - 8      4 T :real
        - 12     4 COSO :real
        - 16     4 COSA :real
        - 24     4 SINO :real
        - 20     4 SINA :real
        - 28     4 COST :real
        - 32     4 SINT :real
        - 36     4 :real
```

```

431
432     FUNCTION JOINT_CHECK: boolean;
433
434     Purpose:          Determines if all of the joint angles given are
435                         within the PUMA's tolerable limits. It returns true
436                         if everything is okay. It returns false if any of the
437                         angles are bad. When no errors are found the
438                         position of arm is saved.
439
440     Calling convention:
441         good := joint_check;
442
443     Global Variables:
444         xyz           Contains the proposed xyoat position of
445                         the puma arm.
446         tmatrix        The homogenous transformation matrix
447                         describing the proposed arm position.
448         itheta         Contains the inverse solution of the arm
449                         (i.e. each of the six joint angles).
450         rob_xyz        Returns last valid xyoat (robot coords)
451                         position of the puma arm.
452         theta          Returns last valid inverse solutions of the
453                         arm (i.e. each of the six joint angles).
454
455     }
456
457
458     var      1,           !incrementor
459           error: integer;   !error flag
460
461     begin
462
463         error := 0;
464
465     for 1 := 1 to 6 do
466         begin
467
468             {Place into range of -360.0 to 360.0}
469             if (1theta[1] > max_degree[1])
470                 then while 1theta[1] > max_degree[1] do
471                     1theta[1] := 1theta[1] - 360.0
472
473             else while (1theta[1] < min_degree[1]) do
474                 1theta[1] := 1theta[1] + 360.0;
475
476             {outside legal joint limits}
477             if ( (1theta[i]<min_degree[i]) or ( 1theta[i]>max_degree[i] ) )
478                 then begin
479                     choose closest limit
480

```

```

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12:36:45

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
then begin;
  if abs(1theta[1]-min_degree[1]) > abs(1theta[1]+360.0-max_degree[1])
    then 1theta[1] := -1theta[1] + 360.0;
  end

  485
  23 486   else if abs(1theta[1]-360.0-min_degree[1]) < abs(1theta[1]-max_degree[1])
  23 487     then 1theta[1] := 1theta[1] - 360.0;

  23 488
  23 489   writeln('Joint ',i:1,' at ',1theta[1]:8:3,
  23 490     , ' degrees out of ', min_degree[i]:8:3,
  23 491     , ' to ', max_degree[i]:8:3, ' range');

  23 492   error := 1;
  22 493
  22 494
  22 495
  22 496   if 1theta[1] > 180.0
  = 22 497     then 1theta[1] := 1theta[1] - 360.0
  = 22 498     else if 1theta[1] < -180.0
  = 22 499       then 1theta[1] := 1theta[1] + 360.0;
  = 22 500
  21 501
  21 502
  21 503   error := error + config[4];
  = 21 504
  = 21 505   config[4] := error;
  21 506
  21 507   if error = 0
  21 508     then begin
  = 22 509       rob_xyz[1] := tmatrix[4,1];
  = 22 510       rob_xyz[2] := tmatrix[4,2];
  = 22 511       rob_xyz[3] := tmatrix[4,3];
  = 22 512       rob_xyz[4] := xyz[4];
  = 22 513       rob_xyz[5] := xyz[5];
  = 22 514       rob_xyz[6] := xyz[6];
  = 22 515       for i := 1 to 6 do
  = 22 516         theta[i] := 1theta[i]; ! save valid joint angles
  21 517
  21 518
  = 21 519   joint_check := (error = 0);
  * 21 520
  * 21 521   return;
  * 10 522
  Symtab 622  Offset Length Variable - JOINT CHECK
          - 2      8  Return offset, FFrame length :Boolean
          - 2      1  (function return) :Integer
          - 4      2  I ERROR :Integer
          - 6      2

```

```

525 {
526   PROCEDURE ROBOT_CONFIG;
527
528   Purpose: Displays the configuration of current attempted robot
529   location. This routines expects that the current 1
530   valid joint angle solution is in the array ITHETA.
531
532
533
534 }
535
536 var
537   T2,
538   T3,
539   T4,
540   T5,
541   T6: matrix;
542   darm,
543   delbow,
544   dwrist,
545   t23: real;
546
547 begin {ROBOT_CONFIG}
548 {
549   First compute the necessary transformations
550
551 }
552 tmats(T2,T3,T4,T5,T6);
553
554 t23 := 1theta[2]+1theta[3];
555 darm := -D4 * dsin(t23) - A3 * dcos(1theta[2]);
556 if darm < -epsilon
557 then write('Left, ')
558 else write('Right, ');
559
560 delbow := darm * (-A3*dsin(1theta[3]) + D4*dcos(1theta[3]));
561 if (delbow < -epsilon)
562 then write('Below, ')
563 else write('Above, ');
564
565 dwrist := t4[3,1]*t6[2,1] + t4[3,2]*t6[2,2] + t4[3,3]*t6[2,3]; !S * Z4
566 if abs(dwrist) < epsilon
567 then dwrist := t4[3,1]*t6[1,1] + t4[3,2]*t6[1,2] + t4[3,3]*t6[1,3]; !N * Z4
568
569 if dwrist < -epsilon
570 then write('Up, ')
571 else write('Down, ');
572 if 1theta[5] < -epsilon
573 then writeln('Flip')
574 else writeln('Noflip');
575

```

```
      576
 10  577 end;
      577
Symtab 577  Offset Length Variable - ROBOT CONFIG
      -   2    350 Return offset, Frame length :Array
      -   64   64   T2 :Array
      - 128   64   T3 :Array
      - 192   64   T4 :Array
      - 256   64   T5 :Array
      - 320   64   T6 :Array
      - 324   4    DARM :Real
      - 336   4    T23 :Real
      - 328   4    DELBOW :Real
      - 332   4    DWRIST :Real
```

ROBOT_CONFIG

```

581 {
582   PROCEDURE TMATS(var T2, T3, T4, T5, T6: matrix);
583
584   Purpose:      Finds the transformations from link 1 coordinate
585               system back to robot reference (base) coordinate
586               system. Note: uses the transformation notation
587                $x' = x A$  (graphics)
588               instead of usual
589                $x' = A x$  (robotics).
590   The result is that matrix A (graphics) is transpose
591   of matrix A (robotics).
592
593 }
594
595 var
596   s,           ! temporary holds sine and cosine values
597   c: real;
598
599 begin
600   s := dsin(1theta[1]);          ! link 1 to link 0
601   c := dcos(1theta[1]);
602   A10[1,1] := c;
603   A10[1,2] := s;
604   A10[2,1] := -s;
605   A10[2,2] := c;
606   A10[3,1] := 0;
607   A10[3,2] := 0;
608   s := dsin(1theta[2]);          ! link 2 to link 1
609   c := dcos(1theta[2]);
610   A21[1,1] := c;
611   A21[1,2] := s;
612   A21[2,1] := -s;
613   A21[2,2] := c;
614   A21[4,1] := A2 * c;
615   A21[4,2] := A2 * s;
616
617   s := dsin(1theta[3]);          ! link 3 to link 2
618   c := dcos(1theta[3]);
619   A32[1,1] := c;
620   A32[1,2] := s;
621   A32[3,1] := s;
622   A32[3,2] := -c;
623   A32[4,1] := A3 * c;
624   A32[4,2] := A3 * s;
625
626   s := dsin(1theta[4]);          ! link 4 to link 3
627   c := dcos(1theta[4]);
628   A43[1,1] := c;
629   A43[1,2] := s;
630   A43[3,1] := -s;

```

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
= 21   631   A43[3,2] := c;
        632   s := dsin(itheta[6]);           !link 5 to link 4
        633   c := dcos(itheta[6]);
        634   A54[1,1] := c;
        635   A54[1,2] := s;
        636   A54[3,1] := s;
        637   A54[3,2] := -c;
        638
        639
        21   640   s := dsin(itheta[6]);           !link 6 to 5
        21   641   c := dcos(itheta[6]);
        642   A65[1,1] := c;
        643   A65[1,2] := s;
        644   A65[2,1] := -s;
        645   A65[2,2] := c;
        646
        647   {
        648       Finally, find transformations from link 1 back to world. Note: To
        649       is transformation from "robot world" to "real world".
        650
        21   651   T2 := mat_mult(A21,A10);
        21   652   T3 := mat_mult(A32,T2);
        21   653   T4 := mat_mult(A43,T3);
        21   654   T5 := mat_mult(A54,T4);
        21   655   T6 := mat_mult(A65,T5);
        656
        657   {$IF tmats debug $THEN}
        658       writeln(sercom,'A21');
        659       pr mat(A21);
        660       writeln(sercom,'A32');
        661       pr mat(A32);
        662       writeln(sercom,'A43');
        663       pr mat(A43);
        664       writeln(sercom,'A54');
        665       pr mat(A54);
        666       writeln(sercom,'A65');
        667       pr mat(A65);
        668       writeln(sercom,'T0');
        669       pr mat(T0);
        670       writeln(sercom,'T1 or A10');
        671       pr mat(A10);
        672       writeln(sercom,'T2');
        673       pr mat(T2);
        674       writeln(sercom,'T3');
        675       pr mat(T3);
        676       writeln(sercom,'T4');
        677       pr mat(T4);
        678       writeln(sercom,'T5');
        679       pr mat(T5);
        680       writeln(sercom,'T6');
        681       pr mat(T6);
        682
        {$$END}

```

PUMA robot routines
Last change: 4-3-84 rmj

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
10 684 end;

Symtab	684	Offset	Length	Variable - TMATS	Return offset, Frame length	Type
	-	12	74			:VarP
	+	14	2	T2		:Real
	-	4	4	S		:Real
	-	8	4	C		:Real
	+	12	2	T3		:VarP
	+	10	2	T4		:VarP
	+	8	2	T5		:VarP
	+	6	2	T6		:VarP

TMATS

Page 18
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12:36:45

Page 19
04-04-84
12:36:45

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
685 {\$PAGE+}
10 686 procedure init_robot;
687
688 {
689 PROCEDURE INIT_ROBOT;
690
691 Purpose: initializes most of the robot specific data
692 structures. This procedure loads the data for the
693 robot figure from the file called "PUMA.DAT" into the
694 "robot" object data structure. However, it should be
695 noted that this object is really a collection of
696 seven objects, one for each link.
697
698 }
699
700 var invertible: boolean;
701
702 begin {ROBOT_INIT}
703
704 tmatrix := identity_matrix; !Robot to world transform matrix
705
706 = 21 707 {
708 specify the robot to world transformation. By the correct rotation
709 transformation, ceiling mounts, table mounts and slide mounts can be
710 handled as well as translation between the coordinate systems.
711
712 }
713 T0 := identity_matrix;
714 T0[4,3] := 669.4; !Robot base to shoulder
715 T0 := invert_matrix(T0,invertible);
716
717 H := identity_matrix; !Robot to tool transformation (null)
718 HI := identity_matrix;
719
720 {
721 set the joint limits
722 }
723 max_degree[1] := 160.0;
724 max_degree[2] := 45.0;
725 max_degree[3] := 225.0;
726 max_degree[4] := 170.0;
727 max_degree[5] := 100.0;
728 max_degree[6] := 266.0;
729
730 min_degree[1] := -160.0;
731 min_degree[2] := -225.0;
732 min_degree[3] := -45.0;
733 min_degree[4] := -110.0;
734 min_degree[5] := -100.0;
735 min_degree[6] := -266.0;
736
737

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
= 21 738 A10 := identity_matrix;
= 21 739 A10[2,2] := 0.0;
= 21 740 A10[2,3] := -1.0;
= 21 741 A10[3,3] := 0.0;
= 21 742 A21 := identity_matrix;
= 21 743 A21 [4,3] := D2;_matrix;
= 21 744 A21 [4,3] := D2;_matrix;
= 21 745 A32 := A10; !Most similar to A10
= 21 746 A32 [2,3] := 1.0;
= 21 747 A32 [2,3] := 1.0;
= 21 748 A43 := A10; !Most similar to A10
= 21 749 A43 [4,3] := D4; !Most similar to A32
= 21 750 A43 [4,3] := D4;
= 21 751 A54 := A32; !Most similar to A32
= 21 752 A54 := A32;
= 21 753 A65 := A21; !Most similar to A21
= 21 754 A65 [4,3] := D6;
= 21 755 A65 [4,3] := D6;
= 21 756 A65 [4,3] := D6;
= 21 757 end; {ROBOT_INIT}
10 758 offset Length Variable - INIT_ROBOT
Syntab 758 - 2 68 Return offset, Frame length :Boolean
- 2 1 INVERTIBLE

```
JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
      759 {$PAGE+}
      end.
      00 760
```

Symtab	760	Offset	Length	Variable ^b	Return offset,	Frame length	Type	Storage Class
		0	570				:Array	Static Public
		4	24	XYZ			:Array	Static Extern
		0	64	TO			:Array	Static Extern
		0	64	H			:Array	Static Extern
		0	64	HI			:Array	Static Extern
		0	64	T01			:Array	Static Extern
		186	64	A10			:Array	Static
		250	64	A21			:Array	Static
		314	64	A32			:Array	Static
		378	64	A43			:Array	Static
		442	64	A54			:Array	Static
		506	64	A65			:Array	Static
		0	24	THETA			:Array	Static Extern
		92	24	I THETA			:Array	Static Public
		0	14	CONFIG			:Array	Static Extern
		0	636	SERCOM			:File	Static Extern
		28	64	TMATRIX			:Array	Static Public
		0	24	ROB XYZ			:Array	Static Extern
		0	8	VERSION			:Array	Static Extern
		0	2	FIRST STR			:Pointer	Static Extern
		0	1	MENU FLAG			:Boolean	Static Extern
		132	24	MAX DEGREE			:Array	Static
		156	24	MIN DEGREE			:Array	Static
		0	2	COORDS TYPE			:Integer	Static Extern
		0	2	MENU CURSOR			:Integer	Static Extern
		180	6	MODEL VERTS			:Pointer	Static

Errors 0 Warnings 0 In Pass One

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
 00 1 {\$linesize:132,\$pagesize:60}
 2 {\$title:'Global include file (global.inc)',\$subtitle:''}
 3 {\$debug-, \$list+}
 4
 5 {
 6
 7
 8 University of Michigan
 9 College of Engineering
 10 Center for Robotics and Integrated Manufacturing
 11 Robot Systems Division
 12 2510 East Engineering Building
 13 Ann Arbor MI 48109
 14 (313) 764-4343

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Written by: Richard M. Jungclas

```

}
{$include:'GLOBAL.INC'}
{$LIST+}
{$title:'Global Include file (global.inc)',$subtitle:'Last change: 4-3-84'}
interface;
{
  GLOBAL.INC
}
This file contains all declarations of types global to the system.  

It also includes variables and some matrix manipulation routines  

used throughout the system.

unit Globals(
  version,
  !system's version number
  !Generic type two-dimensional arrays
  !general one dimensional matrix type
  !4 x 4 homogeneous matrix type
  !coordinate matrix type
  !two super array pointer types

  !return code from serial I/O routines
  !return code from serial I/O routines
  !return code meaning special key

  !world cartesian coordinates type
  !robot cartesian coordinates type

```

00 12
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```
JC IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
00 30 joint_type, !Joint coordinates type
00 31
00 32 file1, !A text file type
00 33 consol_input_lstr, !String type for consol input.
00 34 name_lstr, !String type for names
00 35 file_lstr, !String standard file name type.
00 36
00 37 STRS, !Symbol Table Record structure
00 38 STR_ptr, !pointer type to symbol table record
00 39 first_STR, !Pointer to symbol list
00 40
00 41 menu_cursor, !Menu item cursor
00 42 menu_flag, !Flag to redraw menu
00 43
00 44 config, !Robot configuration status
00 45 coords_type, !Type of robot coordinates
00 46 T0, !Robot base to world transformation
00 47 TOI, !World to robot base transformation
00 48 H, !Robot to tool transformation
00 49 HI, !Tool to robot transformation
00 50 rob_xyz, !Generalized coords (xyz) for robot
00 51
00 52 ! (Null tool to robot reference)
00 53
00 54 theta, !Robot joint angles
00 55
00 56 find_STR, !function to find symbol table entry
00 57 rotate_matrix, !function to generate rotation matrix
00 58 dsin, !sine function(degrees)
00 59 dcos, !cosine function (1in degrees)
00 60 mat_mult, !matrix manipulation routines
00 61 identity_matrix, !identity matrix,
00 62 invert_matrix, !invert matrix,
00 63 get_xyzoat, !get xyz
00 64 trim; !trim;
00 65
00 66 type consol_input_lstr = lstring(80);
00 67 name_lstr = lstring(12);
00 68 file_lstr = lstring(63);
00 69 fileT = text;
00 70
00 71 r_matrix = super array [1...*][1...*] of real;
00 72 i_matrix = super array [1...*][1...*] of integer;
00 73 g_matrix = super array [1...*][1...*] of real;
00 74
00 75 c_matrix = g_matrix(3);
00 76 i_matrix = r_matrix(4,4);
00 77 j_matrix = g_matrix(6);
00 78
00 79 rmat_ptr = @r_matrix;
00 80 imat_ptr = @i_matrix;
00 81
```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
STR_ptr = @STRS;

```

85
86   {
87     Symbol Table Record
88
89     symname:          The symbolic name string
90     data:             The coordinates of the location
91     ctype:            The coordinates type
92     used:             A boolean flag which (if true) indicates that the
93                      location has been used by the programmer.
94     next_STR:         A link to the next entry in the symbol table (or nil)
95
96   }
97
98   STRS = record
99     symname:          name lstr;
100    data:             [matrix];
101    ctype:            integer;
102    used:             boolean;
103    next_STR:         STR_ptr;
104    end;
105
106
107  const
108    SUCCESS = 0;           {return code from serial I/O routines}
109    NO_SUCCESS = 1;        {return code from serial I/O routines}
110    SPECIAL = 2;          {return code meaning special key}
111    world_type = 0;        {type for world cartesian coordinates}
112    robot_type = 1;        {type for robot cartesian coordinates}
113    joint_type = 2;        {type for joint coordinates}
114
115  var
116    version:             string(7);      {system version number}
117    first_STR:           STR_ptr;
118    menu_flag:            boolean;
119
120    coords_type:          {type of robot coordinates
121                                0 = world cartesian
122                                1 = robot shoulder cartesian
123                                2 = joint }
124
125
126    menu_cursor:          integer;
127    config: array[0..6] of integer; {configuration of the robot arm
128                                [0] -1=lefty, 1=righty
129                                [1] -1=below, 1=above
130                                [2] -1=up, 1=down
131                                [3] -1=noflip, 1=flip
132                                [4] 1=error, 0=valid solution
133                                [5] 1=debug, 0=production
134                                [6] (not used) }
```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83

```
136      rob xyz;
137      rob xyz,
138      theta;
139      T0, _matrix;
140      T0I,
141      H,
142      HI;
143      matrix;

144      function find STR(const name: lstring): STR ptr [pure];
20 145      function rotate matrix(const x,y,z: real): matrix [pure];
20 146      function dsin(const x: real): real [pure];
20 147      function dcos(const x: real): real [pure];
20 148      function mat mult(const m1,m2: matrix): matrix [pure];
20 149      function identity matrix: matrix [pure];
20 150      function invert matrix(source: matrix; var invertible: boolean): matrix [pure];
20 151      function Get xyzat(const m: matrix): ] matrix [pure];
20 152      function GetC(var letter,spec: char): boolean [pure];
20 153      procedure trim(var s: lstring);
20 154      end;
10 155      {*****}
156      {$LIST+}

157      TRIM
```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
25 {\$title: 'Debug Include file (debug.inc)', \$subtitle: '.', \$PAGE+}
0 {\$include: 'DEBUG.INC'}
1 {\$LIST+}
2 {\$title: 'Debug Include file (debug.inc) Last Change: 3-2-84 rm1'}
3 interface;
00 4 interface;
05 5 {
06 6 DEBUG This interface contains routines to aid in debugging PASCAL programs.
07 }
08 7 This interface contains routines to aid in debugging PASCAL programs.
09 8 uses Globals;
10 10 unit debug(pr_mat, heap_space, writeln, breakpt);
11 11 procedure pr_mat(const mi: matrix);
12 12 procedure heap_space;
13 13 procedure writeln(const line: consol_input_lstr);
14 14 procedure breakpt(const line: consol_input_lstr);
15 15 procedure pr_mat(const mi: matrix);
16 16 procedure heap_space;
17 17 procedure writeln(const line: consol_input_lstr);
18 18 procedure breakpt(const line: consol_input_lstr);
19 19 procedure writeln(const line: consol_input_lstr);
20 20 procedure breakpt(const line: consol_input_lstr);
21 21 end; {*****}
22 22 {\$LIST+}
23 23 *****

BREAKPT

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
27 {$title:'Menu Function Include file (menu.inc)',$subtitle:'',$PAGE+}
0 {$include:'MENU.INC'}
1 {$LIST+}
2 {$title:'Menu Function Include file (menu.inc) Last change: 4-3-84 rmj'}
3 interface;
4 {
5   MENU
6 }
7 This interface contains routines to control the cursor as well as
8 maintain the menu system.
9
10
11 unit menu_functions(
12   cts,
13   clear_lower,
14   clear_upper,
15   command_prompt,
16   data_prompt,
17   display_menu,
18   bmenu_item,
19   gmenu_item,
20   menu_item,
21   display_status,
22   highlight,
23   position_cursor,
24   print_border);
25
26 uses globals;
27
28 type
29   pitem = lstring(30);
30   pkey = lstring(3);
31
32 procedure
33   cts;
34   procedure clear_lower;
35   procedure clear_upper;
36   procedure command_prompt;
37   procedure data_prompt;
38   procedure display_menu(var full_flag: boolean; const level: consol_input_1str);
39   procedure bmenu_item(const item: pitem);
40   procedure gmenu_item(const key: pkey; const item: pitem);
41   procedure menu_item(const item: pitem);
42   procedure display_status;
43   procedure highlight(line: consol_input_1str);
44   procedure position_cursor(row, column: integer);
45   procedure print_border;
46
47 end; {*****}
48 {$LIST+}

```

```

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
29 {$title:'PUMA Robot Routines Include file (puma.inc)',$subtitle:' '$PAGE+}
0 {$include:'PUMA.INC'}
1 {$LIST+}
2 {$title:'PUMA Robot Routines Include file (puma.inc) Last change: 4-3-84'}
3
4 interface;
5 {
6   PUMA This interface contains PUMA routines
7 }
8

00 unit puma(init_robot, tmats, inverse, homotran, joint_check, robot_config, xyz, tmatrix, itheta);
11 uses globals;
12
13
14 var
15   itheta,
16   xyz: J_matrix;
17
18   {Current joint angles solution for the robot}
19   {Generalized coords (xyz) for robot for
20   the last request. Either tool to world or
21   joint 6 to robot reference. Possibly invalid
22   (out of reach) }
23   {Robot Transformation matrix for the last
24   request. Either tool to world (usually) or
25   joint 6 to robot reference, depending on
26   context. Possibly invalid (out of reach). }

10 procedure init_robot;
11 procedure tmats(var T2,T3,T4,T5,T6: matrix);
12 procedure inverse;
13 procedure homotran;
14 function joint_check: boolean;
15 procedure robot_config;
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Dummy routine to list include files

```
Page 8  
04-05-84  
11:05:59  
  
JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83  
31 {$title:'Dummy routine to list include files', $subtitle:'$PAGE+'}  
10 32 program dummy(input,output);  
33  
10 34 begin {DUMMY procedure}  
35  
11 36 writeln('Dummy procedure');  
37  
00 38 end.  
  
Symtab 38 Offset Length Variable  
0 20 Return offset, Frame length  
  
Errors Warnings In Pass One  
0 0
```

```

JC IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
24      553   if config[5] = 1 and then coords type = world type
24      554   then writeln(sercom, 'World Cartesian coordinates')
24      555   else writeln(sercom, 'Robot Cartesian coordinates');
24      556   temp coord type := coords type;
24      557   coords type := temp_type;
24      558   if config[5] = 1
24      559   then writeln(sercom, 'Calling homotran');
24      560   homotran;
24      561   if config[5] = 1
24      562   then writeln(sercom, 'Calling inverse');
24      563   inverse;
24      564   coords_type := temp_coord_type;
23      565   end;

23      566   joint_type;
23      567   If config[5] = 1
23      568   then writeln(sercom, 'Joint coordinates');

22      569   570
22      571   end;

22      572   if joint_check
22      573   then begin
22      574   move := true;
22      575   if config[6] = 1
22      576   then writeLoc(sercom);
22      577   end
23      578   else begin;
23      579   writeln('Robot can''t reach this location!');
23      580   leave := false;
23      581   move := false;
23      582   end;
22      583   move := false;
23      584   end;
21      585   end;
10      586   end;
10      587   end;

Symtab 587   Offset Length Variable - MOVE
          - 4       140   Return offset, Frame length
          - 2       1       (function return)
          + 6       2       :Boolean VarP
          - 4       1       :File Char
          - 6       1       :Char Boolean
          - 10      1       :Boolean Real
          - 14      4       :Real
          - 26      4       :Real
          - 30      4       :Real
          - 40      2       :Integer
          - 34      4       :Real
          - 18      4       :Real
          - 22      4       :Real
          - 56      14      :NAME Array
          - 8       1       LEAVE :Boolean
          - 42      2       TEMP_STR :Pointer

```

Main program routines(routines.pas)
Last change: 4-3-84

Page 14
04-04-84
14:16:56

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
- 36 2 TEMP_TYPE :Integer
- 38 2 TEMP_COORD_TYPE :Integer
- 138 82 INPUT_LINE_ :Array

MAIN_ROUTINES

Last change: 4-3-84

04-04-84
14:16:56

JG IC Line# Microsoft MS-Pascal Compiler, MS-DOS 8086 Version 3.11, 05/83
588 {\$PAGE+}
00 589 end.

Symtab	589	Offset	Length	Variable Return offset, Frame length	Type
		0	24	VERSION	:Array
		0	8	TO	:Array
		0	64	H	:Array
		0	64	HI	:Array
		0	64	TOI	:Array
		0	24	XYZ	:Array
		0	14	CONFIG	:Array
		0	24	THETA	:Array
		0	24	I THETA	:Array
		0	24	ROB XYZ	:Array
		0	636	SERCOM	:File
		0	64	TMATRIX	:Array
		0	2	FIRST STR	:Pointer
		0	1	MENU FLAG	:Boolean
		0	2	MENU_CURSOR	:Integer
		0	2	COORDS_TYPE	:Integer

Errors 0 Warnings 0 In Pass One 0

