

# Getting the Best Out of Existing Hash Functions; or What if We Are Stuck with SHA?

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**Abstract.** Cascade chaining is a very efficient and popular mode of operation for building various kinds of cryptographic hash functions. In particular, it is the basis of the most heavily utilized SHA function family. Recently, many researchers pointed out various practical and theoretical deficiencies of this mode, which resulted in a renewed interest in building specialized modes of operations and new hash functions with better security. Unfortunately, it appears unlikely that a new hash function (say, based on a new mode of operation) would be widely adopted before being standardized, which is not expected to happen in the foreseeable future.

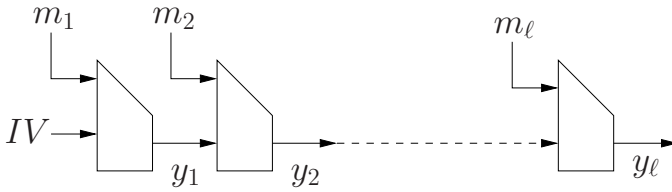
Instead, it seems likely that practitioners would continue to use the cascade chaining, and the SHA family in particular, and try to work around the deficiencies mentioned above. In this paper we provide a thorough treatment of how to soundly design a secure hash function  $H'$  from a given cascade-based hash function  $H$  for various cryptographic applications, such as collision-resistance, one-wayness, pseudorandomness, etc. We require each proposed construction of  $H'$  to satisfy the following “axioms”.

1. The construction consists of one or two “black-box” calls to  $H$ .
2. In particular, one is not allowed to know/use anything about the internals of  $H$ , such as modifying the initialization vector or affecting the value of the chaining variable.
3. The construction should support variable-length inputs.
4. Compared to a single evaluation of  $H(M)$ , the evaluation of  $H'(M)$  should make at most a fixed (small constant) number of extra calls to the underlying compression function of  $H$ . In other words, the efficiency of  $H'$  is negligibly close to that of  $H$ .

We discuss several popular modes of operation satisfying the above axioms. For each such mode and for each given desired security requirement, we discuss the weakest requirement on the compression function of  $H$  which would make this mode secure. We also give the implications of these results for using existing hash functions SHA- $x$ , where  $x \in \{1, 224, 256, 384, 512\}$ .

## 1 Introduction

The *Cascade construction* is a very elegant way to build a hash function  $H$  on arbitrary-length inputs from a given compression function  $h$  on fixed-length



**Fig. 1.** The plain Merkle-Damgård Mode

inputs. Recall that for a given  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ , one can define a hash function  $H$ , parametrized by an initialization vector  $IV \in \{0, 1\}^n$ , as follows (where input  $M = m_1 \parallel \dots \parallel m_\ell$  and  $m_i \in \{0, 1\}^\kappa$  for  $i = 1 \dots \ell$ ):

$$H(m_1 \parallel \dots \parallel m_\ell) = h(m_\ell, h(\dots, h(m_1, IV) \dots))$$

We will refer to this mode, depicted in Figure 1, as the MD mode or the plain MD mode (after Merkle-Damgård).

The most abundant use of the MD mode in practice comes in the design of the industry-standard hash family SHA (which consists of several specific hash functions SHA- $x$ , where  $x \in \{1, 224, 256, 384, 512\}$ ). Unfortunately, despite its elegance and simplicity, the plain MD mode has several deficiencies. For instance, it does not guarantee that a “global” collision of  $H$  implies a “local” collision of the compression function  $h$ , unless one preprocesses the input into a suffix-free form before applying  $H$  [10] (the particular suffix-free encoding of appending the message length is called *MD strengthening*, and is actually used in the SHA family for this reason). More seriously, it was shown by Coron et al. [9] that even MD strengthening falls prey to the “extension attack”<sup>1</sup> which makes it insufficient for domain extension of random oracle. Moreover, this deficiency disqualifies the natural use of “plain MD” in the design of “pseudorandom functions” [3]. Other problems also arise when the MD mode is used in applications such as key derivation [11] and target collision-resistance (or UOWHF’s<sup>2</sup>) [5,25].

Apart from the issues mentioned above, several other deficiencies of the MD mode against exponential-time attacks have been discovered [15,17]. All these deficiencies, coupled with the improved brute-force attacks on the popular SHA-1 hash function proposed recently [26,27], suggest that it is time to design a better, more “secure” mode of operation for building a variable-length input hash function. With this purpose, NIST has been organizing several workshops dedicated to coming up with the next generation hash functions [22]. However, this process will take some time, and it does not appear that such hash functions would be standardized and widely accepted in any foreseeable future. Therefore, practitioners are “stuck” with the prospect of using existing hash functions, despite all their deficiencies. Hence, there is a pressing need to design immediate “fixes” to the MD paradigm, without changing it drastically.

<sup>1</sup> i.e., given  $H(x)$  and any extension  $y$ , one can compute  $H(x \parallel y)$  without knowing  $x$ .

<sup>2</sup> Which stands for Universal One-Way Hash Functions.

There are two aims in coming up with such “fixes” to the MD mode. The first, and so far the most popular, aim is to design a slight variant of the MD mode that provably preserves a given security property of the compression function, and to do so in the most aesthetic and efficient manner. We mention only a few of the many examples of this approach. For collision-resistance, we already mentioned the well known technique of *MD strengthening*. For another example, by viewing the initialization vector as the key and applying a *prefix-free encoding* to the message, one can obtain a variable-length input pseudorandom function from a fixed-length input pseudorandom compression function [3]. In the case of target collision-resistance, Shoup [25] designed an elegant mode for building target collision-resistant (TCR) hash functions (or UOWHFs [23]) from a TCR compression function by cleverly XORing certain masks to the internal chaining variables in the MD construction. The common feature in all these results is that one assumes *exactly the same* property from the compression function  $h$  as the desired property from the hash function  $H$ . In many cases, such as the PRF and TCR examples, this means that a “secure” mode must be sufficiently different from the plain MD so that its implementation requires a non-trivial modification to the SHA implementation. Concretely, the SHA family uses a fixed public IV (as opposed to arbitrary secret IV needed for PRFs), while in the TCR case one cannot XOR the corresponding masks without modifying the internals of SHA.

Of course, we are not saying that the required modifications are too “complicated” to be correctly implemented by a serious programmer. In fact, they are not. Our point is that, irrespective of simplicity and conceptual similarity to the existing implementations, they require one to tinker with the internals of such standard implementations. And this is not only error-prone and requiring low-level programming (which could result in less optimized implementations than those done by the experts), but goes against the whole philosophy of modular design. We do not want our security engineers to know all the low-level cryptographic details. Instead, they should understand the higher-level picture of the protocols they are trying to build, and never need to worry about existing low-level libraries.

This brings us to the second approach, where one explicitly aims to design a “secure” mode that uses only *black-box calls* to the plain MD mode.<sup>3</sup> For instance, MD strengthening satisfies this property. Other important examples include the HMAC mode for pseudorandom functions [3] and the results for domain extension of random oracle in [9]. The attractive feature of these results is that they result in a hash function with the desired property without tinkering with the internals of SHA, and can use any off-the-shelf implementation. Moreover, all these examples also satisfy the *property-preserving* property described above, and do so without any noticeable efficiency penalties as compared to the solutions following the first approach. Concretely, at the price of one or two (or sometimes zero!) extra calls to the compression function  $h$  — which is negligible for all practical purposes —, one manages to achieve the desired goal without tinkering with the internals of the existing hash functions.

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<sup>3</sup> In practice, with MD strengthening, but we ignore this aspect for now.

OUR GOAL. Not surprisingly, we will emphasize the latter approach in coming up with “fixes” for existing hash functions. That is, we consider the question of building a hash function  $H'$  achieving a given security property  $P$  using a black-box MD-based hash function  $H$  (with an unknown compression function  $h$ ). We require that the proposed construction  $H'$  satisfies the following “axioms”:

1. The construction should consist of one or two “*black-box*” calls to  $H$ . In particular, the construction is not allowed to use any knowledge of or tinker with the internals of the hash function  $H$ .
2. The construction must support variable-length inputs.
3. Compared to a single evaluation of  $H(M)$ , the evaluation of  $H'(M)$  should make at most a fixed (small constant) number of extra calls to the underlying compression function of  $H$ . In other words, the efficiency of  $H'$  is negligibly close to that of  $H$ .

The motivation behind requiring the construction  $H'$  to satisfy these axioms is from the viewpoint of a practitioner who understands the properties of the hash function that are needed for the security of his cryptosystem, but who wants to use an off-the-shelf standardized hash function implementation without tinkering with its internals. Such a practitioner would be willing to sacrifice the *property-preserving* aspect of the “fix” in favor of a black-box implementation.

In fact, the above “axioms” leave very little freedom in choosing the modes of operation for  $H'$ . The resulting modes are essentially the *most widely-utilized* constructions appearing in practical implementations:

1. *Plain MD Construction*: This captures the notion that the application uses the hash function as it is. We will denote this mode of operation as  $H$ .
2. *Encode-then-MD Construction*: In this case, the user encodes the hash function input before applying the plain MD construction. Examples of popular encoding schemes used are suffix-free encoding and prefix-free encoding. We will refer to the corresponding constructions as the *prefix-free MD construction*  $H_{pre}$  and the *suffix-free MD construction*  $H_{suf}$ .
3. *MD-then-Chop Construction*: Here the user applies the plain MD mode and only uses part of the output while discarding the remaining bits. In particular, existing hash functions SHA-224 and SHA-384 are obtained this way from SHA-256 and SHA-512, respectively. We denote the MD-then-chop construction that chops  $s$  bits of the output as  $H_{chop_s}$ .
4. *NMAC/HMAC Construction*: The version of the NMAC construction that we consider simply composes two applications of the plain MD mode with possibly different initialization vectors  $IV_1$  and  $IV_2$ . While not obeying the first axiom, the NMAC construction serves as a nice abstraction for the HMAC construction which does satisfy all our axioms (but is slightly harder to formally analyze in some cases). Concretely, the HMAC construction uses the NMAC construction with  $IV_1 = h(IV, \alpha_1) = H(\alpha_1)$  and  $IV_2 = h(IV, \alpha_2) = H(\alpha_2)$ , where each  $\alpha_i$  is either the null string  $\perp$  (in which case we let  $h(IV, \perp) = IV$ ) or a single  $\kappa$ -bit block. We denote the NMAC construction as  $H_{nmac}$  and the HMAC construction as  $H_{hmac}$ .

Now we can finally rephrase our goal as follows. Given a particular desired security property  $P$  (such as collision-resistance or pseudorandomness) and one of the 4 modes of operation above (which all satisfy our axioms), find the weakest security assumption(s)  $P'$  on the compression function  $h$  which would make the corresponding mode satisfy  $P$  (or determine that the construction is insecure for any  $h$ ). Ideally, this security property  $P'$  for  $h$  would be  $P$  itself (which would result in a *property-preserving mode of operation*). However, unlike most previous work, property preservation is not our primary concern. In particular, we will not declare a mode of operation to be “insecure” for a property  $P$  simply because it is not property-preserving for  $P$ . Instead, we will find the weakest security property  $P'$  of the compression function that makes the resulting construction secure. This will allow the practitioners to decide whether or not it is reasonable to assume that the compression function of existing hash functions, such as SHA, satisfy the property  $P'$ , even if  $P'$  is (slightly) stronger than  $P$ .

**OUR RESULTS.** We achieve our main goal for a very wide variety of security properties including *collision-resistance (CR)*, *pseudorandomness (PR)*, *indifferentiability from random oracle (RO)*, *message authentication (MAC)*, *target collision-resistance (TCR)*, *second preimage-resistance (SPR)*, *randomness extraction (RE)* and *one-wayness (OW)*. In each case, and for each of the four popular modes above, we will identify the needed property  $P'$  on  $h$ . In some cases, the needed  $P'$  easily follows from some existing work (for instance, from [9] in the case of domain extension of random oracle). In other cases, it required some minor, but important modifications to the existing results in order to satisfy our axioms. For example, by assuming that “ $h(IV, random) = random$ ” in addition to  $h$  being a PRF when keyed with the first  $n$  bits of its input, we could build a variable length PRF using the encode-then-MD mode and adjusting the proof of [3]. More interestingly, by making extra assumptions on  $h$ , in some cases we can prove security of the modes which were previously believed “insecure” because they were not property-preserving. Finally, in some cases the proof will involve careful and non-trivial modification of previous results. For example, this is the case when analyzing the one-wayness of the  $H_{suf}$  construction.

In addition to giving an exhaustive “mode  $\times$  property” guide (see figure 2) for achieving a given security property with a given popular mode, in each section we also mention the practical implication of our results when using existing hash functions SHA- $x$ , where  $x \in \{1, 224, 256, 384, 512\}$ .

**RELATED WORK.** We have already cited many of the relevant papers. In particular, the variants of the MD mode that are useful in the property-preservation of collision-resistance [10], pseudorandomness [3,4], message-authentication [1,21], random oracles [9] and randomness extraction [11]. We also mention the works of [7,8] concerned with multiple property-preservation; namely, designing a single mode of operation which simultaneously preserves several properties. Unfortunately, the modes of [7,8] do not satisfy our axioms. Finally, we mention the work of Halevi and Krawczyk [14], which concentrated on building TCR hash functions, and is the closest in spirit to our motivation (indeed, we will use their results when discussing the TCR property). The authors built TCR hash

	Plain MD	Encode-then-MD	MD-then-Chop	NMAC/HMAC
CRHF	(1) + (2)	Suf-Free+(1) Pre-Free+(1)+(2)	(1') + (2)	N/HMAC+(1)+(2) $\alpha_1 \neq \perp$
PRF	Append key + (1)+(2)+(4)	SF+(1)+(4) (append) PF+(2')+(3) (prepend)	Prepend key + (2')+(3')	N/H+(3)+(4) <sub>(prepend)</sub> Any $IV_s/\alpha_s$
RO	Not Secure	Suf-Free not secure Pre-Free+(5)	(5) worse security	NMAC/HMAC+(5) $IV_1 \neq IV_2 ; \alpha_1 \neq \alpha_2$
MAC	Append key + (1)+(2)+(6)	SF+(1)+(6) (append) PF+(1)+(2)+(6) <sub>(app.)</sub>	Append key + (1)+(2)+(6')	N/H+(1)+(2)+(6) Any $IV_s/\alpha_s$
TCR	$key \oplus blks$ (7) + (9)	SF+(7) ( $key \oplus blks$ ) PF+(7)+(9)	$key \oplus blks$ (7') + (9)	N/H+(7)+(9) (append) Any $IV_s/\alpha_s (key \oplus blks)$
SPR	(8) + (9)	SF+(9) PF+(8)+(9)	(8') + (9)	N/H+(8)+(9) Any $IV_s/\alpha_s$
RExt	(10) $H_\infty(M) \wedge H_\infty(m_\ell)$	MDS + (10)(SF/PF??) $H_\infty(M) \wedge H_\infty(m_\ell)$	(10) $H_\infty(M)$	NMAC + (10) HMAC??
OWF	(2)+(11)	MDS+(2)+(11) (SF/PF??)	(2')+(11)	NMAC+(2)+(11) HMAC??

Assumptions on compression function:	Misc.
(1)=Collision Resistance (CR)	SF=Suffix-free
(2)=Output Regular	PF=Prefix-free
(3)=standard PRF (sPRF)	MDS=MD Strengthening
(4)=dual PRF (dPRF)	??=not known to be secure
(5)=FIL-RO	RExt=Randomness Extn.
(6)=MAC with $\kappa$ -bit key	$Key \oplus Blks$ =XOR key to each block
(7)=enhanced SPR (eSPR)	
(8)=computed SPR (cSPR)	
(9)=Fixed-point at random $IV$	
(10)=Family of random functions	
(11)=One-way function	

**Fig. 2.** Table for comparing Security Property vs. Mode of operation

functions using the encode-then-MD mode, and showed a simple coding scheme that yields a secure TCR hash function under an appropriately strong assumption on the underlying compression function  $h$  (still weaker than CR, but stronger than TCR).

LOCATION OF THE KEY IN KEYED CONSTRUCTIONS. We note that for keyed constructions, such as constructions of pseudorandom and TCR functions, there are more than one possibilities for each hash function mode of operation. In particular, any construction for these primitives must specify the location of the key. In keeping with the black-box nature of the modes of operation, we prevent popular keying methods such as setting the key to be the  $IV$  or XORing the key into the chaining variables since this violates our basic axioms.

Moreover, we also do not consider the dedicated-key setting [1,8], where there is separate space for the key in each application of the compression function.

This is because existing hash functions do not support such dedicated keys. Even though we may consider the key to be part of the message block bits, we do not analyze this method since it yields constructions with poor input bandwidth (thus violating our last axiom). Hence, we will only consider modes of operation which incur an additive constant overhead compared to the plain MD mode.

ARE WE ASKING TOO MUCH? In our motivation, we advocated the fact that the security officers should not know (or worry about) the low-level details of the hash function implementations. In particular, we do not want them to manually modify the internals of SHA. On the other hand, to use our result they have to be “smart enough” to understand the purpose of their application of the hash function, so they can use our black-box workarounds. For example, they need to know if  $H'$  is used for collision-resistance, key derivation, one-wayness, etc. Aren't we asking too much? Should not the security engineer just believe that the existing hash function will be “magically applicable” for whatever intuitive use (s)he has in mind (therefore making this paper “useless”)?

We give two answers. First, we personally believe that a person designing a cryptographic protocol using a hash function *should* know what security properties this hash function should satisfy. (And this does not contradict our desire to protect them from low-level details!) Second, in order for the security engineer to use a hash function in the “magical” way above, the function should not have the weaknesses of the SHA family we mentioned earlier. Thus, until a new, “magic” hash function is built and standardized, we simply *cannot achieve* a positive answer to our question, even if we *want* our engineers to be “dumb” and not understanding what they is doing (which we personally disagree with)! Until then, we believe that the results of this paper are meaningful and useful.

## 2 Security of MD Modes

We will analyze each of the security properties that actual hash functions are often required to satisfy, and find the minimal assumptions on the compression function that are necessary to prove the security of each of the black-box modes of operation for this security notion. As we discussed, we will not restrict ourselves to the case of property-preservation and in some cases, we will need to make slightly stronger assumptions on the compression function than the security notion desired.

Since the focus of our paper is mostly qualitative, in terms of when (i.e. for which applications) does it make more sense to use some particular mode of operation, so we will keep the discussion “slightly informal” by using more asymptotic definitions for the security notions. We assume basic familiarity with these notions, but provide the formal definitions in the full version of this paper [12]. Due to space constraints, we only give the security of the modes of operation for collision-resistance, pseudorandomness and one-wayness in the main body. The discussion for other security notions can be found in the full version of this paper [12].

## 2.1 Collision Resistance

We will analyze each of the four modes for minimal assumptions required on the compression function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  needed in order to prove its collision resistance. A construction will be called  $\epsilon$  collision resistant if the maximum advantage of an efficient attacker in finding a collision is  $\epsilon$ . As we discussed, in some cases, the security property needed for the compression function  $h$  may be stronger than collision resistance.

**PLAIN MD CONSTRUCTION.** It is a well-known fact that simply assuming collision resistance of the compression function does not suffice to prove collision resistance of the plain MD construction. Indeed, if the compression function  $h$  has a *fixed-point* such that there is some  $x \in \{0, 1\}^\kappa$  such that:  $h(x, IV) = IV$ . Then the output of the plain MD construction  $H$  collides for the inputs  $x$  and  $x \parallel m$ , for any  $m$ . Thus we, at least, need the compression function to satisfy the following property.

**Assumption 1 (No Fixed-Points)** *A function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  is a  $\epsilon$  secure against fixed points if for a randomly chosen  $IV \in \{0, 1\}^n$  no efficient machine  $A$  has success probability more than  $\epsilon$  of finding a sequence of  $\kappa$ -bit blocks  $x_1 \dots x_i$  such that,*

$$h(x_i, h(\dots, h(x_1, IV) \dots)) = IV$$

If the compression function is such that no efficient attacker can find such fixed points (along with being collision resistant), then the plain MD construction can be proven to be collision resistant. The proof of the following observation is immediate from [10].

**Observation 1** *The plain MD construction can be proven to be collision resistant if the compression function is collision resistant and is secure against fixed-points.*

The *no fixed-points* assumption allows us to prove collision resistance of the plain MD construction, but it is a non-standard assumption and it is not intuitively clear as to which compression functions satisfy this property. But since we are already assuming the compression function to be collision-resistant, perhaps we can prove this result by making a weaker and cleaner additional assumption on the compression function. Fortunately we show that simply assuming output regularity suffices in this case.

**Assumption 2 (Regularity of outputs)** *A function  $h : \{0, 1\}^m \rightarrow \{0, 1\}^n$  is a  $\epsilon$  output regular function if for any efficient machine  $A$  that gives a 1 bit output:*

$$|\Pr[A(x) = 1 | x \leftarrow h(U_m)] - \Pr[A(x) = 1 | x \leftarrow U_n]| \leq \epsilon$$

Here  $U_m$  and  $U_n$  denote the uniform distributions on  $\{0, 1\}^m$  and  $\{0, 1\}^n$ , respectively.



We show that if the compression function is output regular (i.e. for a random input, the output is well distributed over the range) in addition to being collision-resistant, then it is secure against fixed points and thus a CRHF using the observation above.

**Lemma 1.** *The compression function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  is  $(\epsilon_{col} + \epsilon_{reg} + 2^{-n})$ -secure against fixed points if it satisfies the following properties:*

- $h$  is  $\epsilon_{col}$  collision resistant.
- $h$  is an  $\epsilon_{reg}$  output regular function.

**Proof:** To the contrary, say there is an efficient attacker that finds a fixed point  $x_1 \dots x_i$  with non-negligible probability  $\epsilon$ , then we can show that it either breaks the collision resistance or the output regularity assumption for the compression function. In order to show this, choose the initialization vector  $IV$  as  $IV \leftarrow h(x)$  (for  $x \leftarrow U_\kappa \times U_n$ ), instead of  $IV \leftarrow U_n$ . If the success probability of  $A$  changes by a non-negligible amount then we can break the output regularity assumption. Thus,  $\epsilon' \geq \epsilon_{reg} + \Pr[A \text{ succeeds in new game}]$ .

To estimate the success probability of the attacker  $A$  in the new game, say it finds a sequence of  $\kappa$ -bit blocks  $x_1 \dots x_i$  such that  $h(x_i, h(\dots, h(x_1, IV) \dots)) = IV$  with probability  $\epsilon'$ . Let  $y = (x_i, h(\dots, h(x_1, IV) \dots))$ . Then it is the case that  $h(x) = h(y)$  (where  $x$  was used to select the  $IV$ ). Thus, we can deduce that,

$$\begin{aligned} \epsilon' &= \Pr[(A \text{ succeeds}) \wedge (x = y)] + \Pr[(A \text{ succeeds}) \wedge (x \neq y)] \\ &\Rightarrow \epsilon' \leq \Pr[(x = y)] + \epsilon_{col} \\ &\Rightarrow \epsilon' \leq \epsilon_{col} + \sum_{IV \in \{0,1\}^n} \frac{\#\{x \text{ s.t. } h(x) = IV\}}{2^{n+\kappa}} \cdot \frac{1}{\#\{x \text{ s.t. } h(x) = IV\}} \\ &\leq \epsilon_{col} + 2^{-n} \end{aligned}$$

Thus we get that the maximum success probability of an efficient fixed-point finding attacker is  $\epsilon_{reg} + \epsilon_{col} + 2^{-n}$ . □

**Corollary 1.** *The plain MD construction  $H$  using a compression function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  is a  $(\epsilon_{reg} + \epsilon_{col} + 2^{-n})$  collision resistant hash function if  $h$  satisfies the following properties:*

- $h$  is  $\epsilon_{col}$  collision resistant.
- $h$  is an  $\epsilon_{reg}$  output regular function.

**ENCODE-THEN-MD CONSTRUCTION.** It makes sense to only consider deterministic input coding schemes, since the resulting construction must behave like a function. We analyze two of the most popular such coding schemes, i.e. *prefix-free encoding* and *suffix-free encoding*.

We first note that using a prefix-free encoding on the input does not enable us to get rid of any security properties in lemma 1. Hence we can essentially restate

the same result for the prefix-free MD construction  $H_{pre}$  as well. On the other hand, if we use a *suffix-free encoding* (such as Merkle-Damgård strengthening) then the resulting suffix-free MD construction  $H_{suf}$  can be shown to be collision resistant by simply assuming the collision-resistance of the compression function  $h$  [10,19].

**MD-THEN-CHOP CONSTRUCTION.** Note that simply assuming collision resistance of the compression function is not useful for this construction, since we truncate  $s$  bits of the output. For instance, consider the case when  $h$  is collision resistant on these  $s$  bits, and is the constant function for all other bits (noted by Kelsey [16]). However, in our setting this only means that we need to make a stronger assumption on the compression function  $h$ . In particular, we will instead assume that  $h$  is collision resistant even if we remove these  $s$  bits from its output.

**Lemma 2.** *The MD-then-chop construction  $H_{chop_s}$ , using a compression function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ , is a  $(\epsilon_{reg} + \epsilon'_{col} + 2^{n-s})$  collision resistant hash function if the following holds:*

- *The function  $h' : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^{n-s}$  defined as  $h'(x, y) = h(x, y)|_{n-s}$  (i.e. chopping the last  $s$  bits from the output of  $h$ ) is a  $\epsilon'_{col}$  collision resistant function.*
- *$h$  is a  $\epsilon_{reg}$  output regular function.*

The proof of this lemma is essentially the same as for corollary 1.

**NMAC/HMAC CONSTRUCTION.** We note that using the NMAC construction  $H_{nmac}$  does not help in improving upon the collision resistance of the plain MD construction  $H$ . This is essentially because any collision in the first application of the plain MD construction of  $H_{nmac}$  (using initialization vector  $IV_1$ ) essentially implies a collision for the entire construction. Hence, at best, we can restate lemma 1 for this construction as well.

Since the HMAC construction  $H_{hmac}$  is simply a black-box instantiation of the NMAC construction, this does not help in improving collision resistance. However, we note that it has the best exact security if  $\alpha_1 \neq \perp$ .

## 2.2 Pseudorandomness

An issue in the pseudorandomness analysis of the MD modes of operation is the location of the PRF key. As discussed above, we need to specify the location of the key such that the resulting construction is still a black-box variant of plain MD. For our analysis, we will assume the key length to be the length of a single block (i.e.  $\kappa$  bits for the compression function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ ), and we will denote the key as  $K$ . We will analyze two approaches for keying each MD mode of operation:

1. *Prepend the key to input:* The PRF construction  $H$  outputs  $H(K \parallel X)$  on input  $X$ .
2. *Append the key to input:* The PRF construction  $H$  outputs  $H(X \parallel K)$  on input  $X$ .

Moreover, we will need two versions of pseudorandomness definitions for the compression function, one where the key occupies the last  $n$  bits and other where it occupies the first  $\kappa$  bits. We get the following two assumptions on the compression function in this manner.

- *Standard PRF (sPRF) security:* Here we require that for a uniformly chosen  $K \in \{0, 1\}^n$ , the function  $h(\cdot, K)$  must be indistinguishable from a truly random function.
- *Dual PRF (dPRF) security:* Here we require that for a uniformly chosen  $K \in \{0, 1\}^\kappa$ , the function  $h(K, \cdot)$  must be indistinguishable from a truly random function.

Depending on the maximum distinguishing advantage  $\epsilon$  of an efficient attacker in each case, we call the compression function  $h$   $\epsilon$ -sPRF or  $\epsilon$ -dPRF.

PLAIN MD CONSTRUCTION. In this case if we prepend the PRF key to the hash function input, then the resulting construction is not a PRF. This is because an attacker can use the *extension attack* to find  $H(K \parallel X \parallel Y)$  by simply knowing the output  $H(K \parallel X)$  and computing the compression function on the remaining blocks itself (where it does not need to know the key  $K$ ). On the other hand, if we append the PRF key to the input, then we can show that if the plain MD construction using  $h$  is collision-resistant and satisfies the dual PRF security, then the plain MD construction  $H(\cdot \parallel K)$  is a variable-length input PRF.

**Lemma 3.** *The plain MD construction  $H$  is a  $\mathcal{O}(\ell \cdot (\epsilon_{col} + \epsilon_{reg}) + \epsilon_{dprf})$  PRF<sup>4</sup> (with PRF key appended to the function input) if the following conditions hold:*

- $h$  is  $\epsilon_{col}$  collision resistant.
- $h$  is a  $\epsilon_{reg}$  output regular function.
- $h$  is a  $\epsilon_{dprf}$  dual pseudorandom function.

The proof of this lemma is rather straightforward. Here, output regularity and collision resistance of the compression function together imply the collision resistance of the plain MD construction. Thus, in the last round, the  $n$ -bit chaining variable is different for two different inputs. Hence a distinguisher for the plain MD construction can be used directly by the dual-PRF distinguisher for the compression function.

ENCODE-THEN-MD CONSTRUCTION. Once again, we will discuss two deterministic coding schemes here, *prefix-free encoding* and *suffix-free encoding*. Let us first analyze the suffix-free MD construction  $H_{suf}$ . If we prepend the key to the (encoded) input, the resulting construction is still insecure since the *extension attack* works in this case as well. On the other hand, if we append the key to the (encoded) input then the resulting construction is a PRF if the suffix-free MD construction  $H_{suf}$  using the compression function  $h$  is a dual PRF and collision resistant (for which we only need collision resistance of  $h$  in this case).

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<sup>4</sup>  $\ell$  denotes the maximum number of  $\kappa$ -bit blocks in a hash function input, throughout this paper

For the prefix-free MD construction  $H_{pre}$ , if we append the key to the (encoded) input then we get no advantage as compared to the plain MD construction and we can only restate lemma 3 in this case. On the other hand, if we prepend the PRF key to the (encoded) input then the resulting construction is not vulnerable to the *extension attack* in this case. Indeed, it was shown by Bellare et al. in [3] that the prefix-free MD construction with the PRF key in the IV is a PRF only assuming that the compression function  $h$  satisfies the standard PRF security. However, since we will need to prepend the key to the input (in order to preserve the black-box property of the construction), we will need to impose an extra condition on the compression function. In particular, we require that the function defined as  $h(U_n, \cdot)$  is an output regular function. That is, if the first  $n$  bits of the compression function  $h$  are chosen at random then the resulting function is output regular with high probability.

**Lemma 4.** *The prefix-free MD construction  $H_{pre}$  is a  $\mathcal{O}(\epsilon'_{reg} + \ell \cdot \epsilon_{sprf})$  secure PRF (with PRF key prepended to the input) if the following conditions hold:*

- $h$  is a  $\epsilon_{sprf}$  sPRF.
- $h(U_n, \cdot)$  is a  $\epsilon'_{reg}$  output regular function.

The proof of this lemma is similar to the result of [3].

**MD-THEN-CHOP CONSTRUCTION.** If the PRF key is appended to the input to the MD-then-Chop construction  $H_{chop_s}$ , then a slight variant of lemma 3 can be stated for this construction as well. Indeed, all we need is to specify the dual PRF and collision-resistance properties for the compression function with chopped output.

On the other hand, if we prepend the PRF key to the input to  $H_{chop_s}$ , then the extension attack does not seem to go through as in the case of plain MD construction. This is because the attacker does not learn the chopped  $s$  bits of the chaining variable by observing the output of  $H_{chop_s}$  for the prefix of an input. Indeed, this construction can be proven to be an arbitrary-length input PRF by making a slightly non-standard assumption on the compression function. In particular, we require the compression function to satisfy the following *resilient sPRF* assumption:

**Assumption 3 (( $s, \epsilon$ )-resilient sPRF)** *The function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  is a ( $s, \epsilon$ )-resilient sPRF if it is a  $\epsilon$ -secure sPRF even if the attacker learns  $s$  bits of the  $n$  bit key.*

**Lemma 5.** *The MD-then-Chop construction  $H_{chop_s}$  is a  $\mathcal{O}(\epsilon'_{reg} + \ell \cdot \epsilon'_{sprf})$  secure PRF (with PRF key prepended to the input) if the following conditions hold:*

- $h$  is a  $(s, \epsilon'_{sprf})$ -resilient sPRF.
- $h(U_n, \cdot)$  is a  $\epsilon'_{reg}$  output regular function.

**NMAC/HMAC CONSTRUCTION.** The NMAC and HMAC constructions were shown to be secure arbitrary-length input PRFs by Bellare [2]. In [2], it is shown

that the HMAC construction with  $\alpha_1 = \alpha_2 = \perp$  (i.e. with the same IV for both invocations of the plain MD construction) is a secure arbitrary-length input PRF if the underlying compression function satisfies both the standard and dual PRF security definitions. This is done by simply prepending a different  $\kappa$ -bit key to each invocation of the plain MD construction <sup>5</sup>.

**Lemma 6.** *The NMAC (resp. HMAC) construction  $H_{nmac}$  (resp.  $H_{hmac}$ ) is a  $\mathcal{O}(q^2\ell \cdot \epsilon_{sprf} + \epsilon_{dprf})$  PRF (with a different  $\kappa$ -bit key prepended to the input in each call to the MD construction) for any  $IV_1$  and  $IV_2$  (resp.  $\alpha_1$  and  $\alpha_2$ ) if the following conditions hold:*

- $h$  is a  $\epsilon_{sprf}$ -secure sPRF.
- $h$  is a  $\epsilon_{dprf}$ -secure dPRF.

### 2.3 One-Wayness

One way functions are also often referred to as preimage resistant functions. A construction is  $\epsilon$ -secure OWF if no efficient attacker can find the input corresponding to the output of the function (on a random input) with probability more than  $\epsilon$ . This security property is even weaker than second preimage resistance.

PLAIN MD CONSTRUCTION. In this case, we will need to assume that the compression function  $h$  is a one way function. Moreover, we will also require that  $h$  is output regular, so that its output is uniformly distributed for a random input. This is essentially because we need the input to a one-way function to be random in order to use the one-wayness property.

**Lemma 7.** *The plain MD construction  $H$  is  $\mathcal{O}(\ell \cdot \epsilon_{reg} + \epsilon_{owf})$ -secure OWF if the following conditions hold:*

- $h$  is an  $\epsilon_{reg}$  output regular function.
- $h$  is a  $\epsilon_{owf}$ -secure one-way function.

The proof of this lemma is based on the fact that an attacker cannot tell the difference between the output of  $H$  on a random input or the compression function  $h$  on a random input, if  $h$  is output regular. Thus the one-wayness attacker for  $h$  can use the one for  $H$  directly.

ENCODE-THEN-MD CONSTRUCTION. If we use an arbitrary suffix-free encoding with the MD construction, then we cannot say much about one-wayness of the construction since the input distribution could be arbitrary. However, if we apply *Merkle-Damgård strengthening* to the input, then we can show that the resulting construction is a one-way function under sufficient assumptions. The proof of this fact is non-trivial though. In particular, we need to make an additional assumption about the compression function.

<sup>5</sup> If the same key is prepended in both invocations, then the construction is secure under a slightly stronger assumption, called security against *related-key attacks* in [3,2]. We ignore this setting here

**Assumption 4** ( $(p, \epsilon)$  **output consistent**) *The function  $h : \{0, 1\}^\kappa \times \{0, 1\}^n \rightarrow \{0, 1\}^n$  is  $(p, \epsilon)$  output consistent if for any  $\kappa$ -bit block  $x$  and uniformly distributed  $y \in \{0, 1\}^n$ , with probability at least  $(1 - \epsilon)$  the number of  $y' \in \{0, 1\}^n$  such that  $h(x, y) = h(x, y')$  is at most  $p$ .*

Note that this property certainly holds for a random compression function (and, thus, holds for most compression functions). By making this additional assumption from the compression function, we can derive the following result.

**Lemma 8.** *The suffix-free MD construction  $H_{suf}$  that uses MD strengthening for suffix-freeness is  $(p_{cons} \cdot (\ell \cdot \epsilon_{reg} + \epsilon_{owf}) + \epsilon_{cons})$ -secure one-way function, where  $\ell$  is the maximum length of an inverted input provided by the OWF attacker, if the following conditions hold:*

- $h$  is an  $\epsilon_{reg}$  output regular function.
- $h$  is a  $\epsilon_{owf}$ -secure one-way function.
- $h$  is a  $(p_{cons}, \epsilon_{cons})$  output consistent.

**Proof:** The proof for this lemma is essentially based on the proof of lemma 7. We construct an one-wayness attacker  $A'$  for the compression function using the attacker  $A$  that has advantage  $\epsilon$  in inverting  $H_{suf}$  with MD strengthening.  $A'$  gets its challenge output  $y$  and chooses a uniformly random  $i \in \{1, \dots, \ell\}^n$ . It then gives  $z = h(\langle i \rangle, y)$  as a challenge to  $A$ .

Now  $A'$  succeeds only if the inverse  $z$  outputted by  $A$  is  $i$ -bit long. If so, then  $A'$  can proceed similar to the case on the plain MD construction in lemma 7 if the chaining variable for  $z$  in the last round, with  $\langle i \rangle$  in the message block, is the challenge  $y$ . However, from our assumptions, with probability at most  $\epsilon_{cons}$  there are more than  $p_{cons}$   $n$ -bit strings  $y'$  such that  $h(\langle i \rangle, y') = h(\langle i \rangle, y)$ . Thus, we get that the success probability of  $A$  is at most  $(p_{cons} \cdot (\ell \cdot \epsilon_{reg} + \epsilon_{owf}) + \epsilon_{cons})$ .  $\square$

As for prefix-free encoding, once again we cannot say anything general (for the same reason as above), but when prepending the message length we are essentially back to the setting of plain MD discussed above, except we need to assume that the output of the compression function on a random IV and a fixed message block is random. In particular, we note that encoding the input in any way does not help as far as one-wayness of the construction is concerned. In fact, we only need more assumptions to prove this property, as compared to the plain MD construction.

**MD-THEN-CHOP CONSTRUCTION.** In order to prove the one-wayness of the MD-then-Chop construction, we need to make a stronger assumption on the compression function  $h$ . In particular, we assume that  $h$  is one-way with  $s$  bits of the output chopped. Let the one-way security of the function  $h$  with truncated output be  $\epsilon'_{owf}$ . Then we can show that  $H_{chop_s}$  is a  $\mathcal{O}(\ell \cdot \epsilon_{reg} + \epsilon'_{owf})$ -secure one-way function (similar to lemma 7)

**NMAC/HMAC CONSTRUCTION.** The NMAC construction is a one-way function under the same conditions on the underlying compression function  $h$  as required in lemma 7. However, we require that random and independent initialization vectors  $IV_1$  and  $IV_2$  are used in the NMAC construction. However, it

turns out that translating these results to the setting of the HMAC construction is not straightforward.

### 3 Implications for Hash Functions in Practice

We will now translate our results into suggestions for usage of actual “cascade construction based” hash functions, such as functions from the SHA family. As we mentioned earlier, we have tried to find the minimal assumptions needed to make each of the four modes of operation secure (for each of the security properties). Thus, we have left part of the “decision making” for the practitioner who uses our results. In particular, the practitioner must consider the following questions:

1. What one needs to assume about the hash function in order for the cryptosystem (that the hash function is being used for) to be provably secure?
2. What level of trust the practitioner is willing to place in the underlying compression function?

The answer to the first question will help in deciding the security property to look for in the hash function mode of operation. The answer to the second question may not be as straightforward since the design of the compression functions is quite complex and mostly based on heuristic. In this case, the practitioner needs to weigh all the properties (s)he desires from the cryptosystem, in terms of efficiency, security etc. Thus, while some may be willing to make a slightly stronger assumption on the compression function to have a more efficient implementation, others may be willing to sacrifice some efficiency for better security. Now we will give some basic recommendations for actual hash functions with respect to the various security properties.

**COLLISION RESISTANCE.** Each of the SHA functions are essentially based on the suffix-free MD construction (using MD strengthening). Hence, collision resistance for each of these hash functions is asymptotically same as finding collisions on the compression function. It does not make much sense to use the “truncated” versions, SHA-224 and SHA-384, since this only sacrifices the collision resistance of the original “untruncated” version (i.e. SHA-256 and SHA-512, respectively). Using the NMAC/HMAC construction does not help in this case.

**PSEUDORANDOMNESS.** We note that using the full SHA-256 or SHA-512 hash functions makes more sense for pseudorandomness than using the chopped versions (SHA-228 or SHA-384), which only have worse security. If any of the SHA functions are used, as it is, for pseudorandomness, then we recommend appending the PRF key to the input instead of prepending it. However, we recommend using these functions in conjunction with a prefix-free encoding (such as prepending input length to the input) in which case the PRF key should be *preended* to the input. Another option would be to compose two calls to SHA-1, with independent keys prepended in each call, to get security based on the sPRF and dPRF security of the compression function.

**RANDOM ORACLE.** Note that none of the SHA functions should be used, as it is, if the security of the cryptosystem requires the *random oracle assumption* for

the hash function. This is because the plain MD construction (even with MD strengthening) is vulnerable to simple attacks in the indistinguishability scenario. One may think that both SHA-224 and SHA-384 that correspond to “chop” versions of the functions SHA-256 and SHA-512 would be secure (since the MD-then-Chop construction is secure). However, note that only 32 bits are chopped in the case of SHA-224, which does not give sufficient security for almost all applications. Hence, only SHA-384 (that chops 128 bits) may be suitable to be used directly to instantiate the random oracle.

We recommend using the HMAC construction involving two black-box calls to the SHA function (while prepending different  $\alpha_1$  and  $\alpha_2$  in each call) for this purpose. Using any of these hash functions in conjunction with a prefix-free encoding will also work for this purpose.

**MESSAGE AUTHENTICATION.** If the SHA functions are used as MACs directly, then the MAC key should be appended to the input. In this case, security depends on both the MAC security and collision resistance of the compression function. Using the HMAC construction does not help in improving the security either. Moreover, when the “chopped” functions SHA-224 or SHA-384 are used as MACs, then their security is only worse than the unchopped versions (SHA-256 and SHA-512).

If one is willing to assume pseudorandomness of the compression function, then the techniques mentioned above for pseudorandomness can be used as well. Another approach would be to assume the *dedicated-key setting*, by inserting the MAC key in each application of the compression function (at the cost of some input bandwidth) and then one could use one of the techniques suggested in [1,21].

**TARGET COLLISION RESISTANCE OR UOWHFs.** We recommend using the technique suggested by Halevi and Krawczyk [14] if the SHA functions are used as UOWHFs. In this case, one XORs the UOWHF key to each block of the input. Since MD strengthening is already used in all these functions, the UOWHF security of this construction is based only on the eSPR [14] (see above) of the compression function.

**SECOND PREIMAGE RESISTANCE.** It makes sense to use the SHA hash functions directly for the purpose of *second preimage resistance* without using any additional techniques, since they do not lead to improved security (note that these functions already incorporate MD strengthening).

**RANDOMNESS EXTRACTION.** All the positive results for *randomness extraction* have reasonable interpretation in practice, only if we are willing to assume that the SHA compression function is close to being a family of random functions. Even though it is theoretically impossible, since the SHA compression function has a short description, it might still be a more reasonable assumption than assuming the compression function to be a FIL-RO.

Under this assumption, we can deduce that the SHA functions are good randomness extractors for input distributions with high min entropy overall and in the last block. On the other hand, as we saw above, it might be a good idea to use chopped function SHA-384 for this purpose to get better extraction properties (SHA-224



does not have sufficient number of chopped bits to give useful advantage). Using the HMAC construction does not help in improving the extraction properties.

ONE-WAYNESS. In the case of “one-wayness”, the security of the chopped functions, SHA-224 and SHA-384, seems to rely on stronger assumptions than the security of the corresponding “unchopped” versions (SHA-256 and SHA-384). This is because the one-way security increases with the number of output bits. On the other hand, it might be the case that SHA-224 still has higher security than SHA-1, which seems intuitive given the bigger IV of SHA-224. Moreover, message encoding or HMAC construction only negatively affects the one-wayness.

## 4 Conclusions

In this work we showed how to efficiently use existing hash functions based on the MD mode (such as the functions in the SHA family) to build cryptographic hash functions satisfying various security properties such as collision-resistance, pseudorandomness, indistinguishability from random oracle, message authentication, target collision-resistance, second preimage-resistance, randomness extraction and one-wayness. Our constructions are black-box, support variable-length inputs and provide the same efficiency as the plain MD construction, under the minimal assumptions on the underlying compression function.

## References

1. An, J.H., Bellare, M.: Constructing VIL-MACs from FIL-MACs: Message Authentication under Weakened Assumptions. In: Wiener, M.J. (ed.) CRYPTO 1999. LNCS, vol. 1666, pp. 252–269. Springer, Heidelberg (1999)
2. Bellare, M.: New Proofs for NMAC and HMAC: Security without Collision-Resistance. In: Dwork, C. (ed.) CRYPTO 2006. LNCS, vol. 4117, Springer, Heidelberg (2006)
3. Bellare, M., Canetti, R., Krawczyk, H.: Pseudorandom Functions Re-visited: The Cascade Construction and Its Concrete Security. In: Proc. 37th FOCS, pp. 514–523. IEEE, Los Alamitos (1996)
4. Bellare, M., Canetti, R., Krawczyk, H.: Keying hash functions for message authentication. In: Kobitz, N. (ed.) CRYPTO 1996. LNCS, vol. 1109, Springer, Heidelberg (1996)
5. Bellare, M., Rogaway, P.: Collision-Resistant Hashing: Towards Making UOWHF's Practical. In: Kaliski Jr., B.S. (ed.) CRYPTO 1997. LNCS, vol. 1294, Springer, Heidelberg (1997)
6. Bellare, M., Rogaway, P.: Random oracles are practical : a paradigm for designing efficient protocols. In: Proceedings of the First Annual Conference on Computer and Communications Security, ACM, New York (1993)
7. Bellare, M., Ristenpart, T.: Multi-Property-Preserving Hash Domain Extension and the EMD Transform. In: Lai, X., Chen, K. (eds.) ASIACRYPT 2006. LNCS, vol. 4284, Springer, Heidelberg (2006)
8. Bellare, M., Ristenpart, T.: Hash Functions in the Dedicated-Key Setting: Design Choices and MPP Transforms. In: Arge, L., Cachin, C., Jurdziński, T., Tarlecki, A. (eds.) ICALP 2007. LNCS, vol. 4596, Springer, Heidelberg (2007)

9. Coron, J.-S., Dodis, Y., Malinaud, C., Puniya, P.: Merkle-Damgård Revisited: How to Construct a Hash Function. In: Shoup, V. (ed.) CRYPTO 2005. LNCS, vol. 3621, pp. 430–448. Springer, Heidelberg (2005)
10. Damgård, I.: A Design Principle for Hash Functions. In: Brassard, G. (ed.) CRYPTO 1989. LNCS, vol. 435, pp. 416–427. Springer, Heidelberg (1990)
11. Dodis, Y., Gennaro, R., Håstad, J., Krawczyk, H., Rabin, T.: Randomness Extraction and Key Derivation Using the CBC, Cascade and HMAC Modes. In: Franklin, M. (ed.) CRYPTO 2004. LNCS, vol. 3152, Springer, Heidelberg (2004)
12. Dodis, Y., Puniya, P.: Getting the Best Out of Existing Hash Functions or What if We Are Stuck with SHA (ful version), <http://people.csail.mit.edu/dodis/ps/sha.ps>
13. FIPS 180-1, Secure hash standard, Federal Information Processing Standards Publication 180-1, U.S. Department of Commerce/N.I.S.T., National Technical Information Service, Springfield, Virginia, April 17 (1995) (supersedes FIPS PUB 180)
14. Halevi, S., Krawczyk, H.: Strengthening Digital Signatures Via Randomized Hashing. In: Dwork, C. (ed.) CRYPTO 2006. LNCS, vol. 4117, pp. 41–59. Springer, Heidelberg (2006)
15. Joux, A.: Multicollisions in Iterated Hash Functions. Application to Cascaded Constructions. In: Franklin, M. (ed.) CRYPTO 2004. LNCS, vol. 3152, pp. 306–316. Springer, Heidelberg (2004)
16. Kelsey, J. In: CRYPTO 2005, Rump Session (2005)
17. Kelsey, J., Kohno, T.: Herding Hash Functions and the Nostradamus Attack. In: Vaudenay, S. (ed.) EUROCRYPT 2006. LNCS, vol. 4004, pp. 183–200. Springer, Heidelberg (2006)
18. RFC 1321, The MD5 message-digest algorithm, Internet Request for Comments 1321, R.L. Rivest (April 1992)
19. Merkle, R.: One way hash functions and DES. In: Brassard, G. (ed.) CRYPTO 1989. LNCS, vol. 435, pp. 428–446. Springer, Heidelberg (1990)
20. Maurer, U., Renner, R., Holenstein, C.: Indifferentiability, Impossibility Results on Reductions, and Applications to the Random Oracle Methodology. In: Naor, M. (ed.) TCC 2004. LNCS, vol. 2951, pp. 21–39. Springer, Heidelberg (2004)
21. Maurer, U.M., Sjödin, J.: Single-Key AIL-MACs from Any FIL-MAC. In: Caires, L., Italiano, G.F., Monteiro, L., Palamidessi, C., Yung, M. (eds.) ICALP 2005. LNCS, vol. 3580, pp. 472–484. Springer, Heidelberg (2005)
22. National Institute of Standards and Technology, NIST’s Plan for New Cryptographic Hash Functions, <http://www.csrc.nist.gov/pki/HashWorkshop/index.html>
23. Naor, M., Yung, M.: Universal One-Way Hash Functions and their Cryptographic Applications. In: STOC 1989, pp. 33–43 (1989)
24. Simon, D.R.: Finding Collisions on a One-Way Street: Can Secure Hash Functions Be Based on General Assumptions? In: Nyberg, K. (ed.) EUROCRYPT 1998. LNCS, vol. 1403, pp. 334–345. Springer, Heidelberg (1998)
25. Shoup, V.: A Composition Theorem for Universal One-Way Hash Functions. In: Preneel, B. (ed.) EUROCRYPT 2000. LNCS, vol. 1807, pp. 445–452. Springer, Heidelberg (2000)
26. Wang, X., Yu, H., Yin, Y.L.: Efficient Collision Search Attacks on SHA-0. In: Shoup, V. (ed.) CRYPTO 2005. LNCS, vol. 3621, pp. 1–16. Springer, Heidelberg (2005)
27. Wang, X., Yin, Y.L., Yu, H.: Finding Collisions in the Full SHA-1. In: Shoup, V. (ed.) CRYPTO 2005. LNCS, vol. 3621, pp. 17–36. Springer, Heidelberg (2005)