



# Ground deformation associated with the eruption of Lumpur Sidoarjo mud volcano, east Java, Indonesia



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## ABSTRACT

Ground deformation associated with the eruption of Lumpur Sidoarjo mud volcano between 2006 and 2011 has been investigated from Synthetic Aperture Radar images. Marked subsidence has been observed to the west of, as well as around, the vent. Line-of-sight changes in the both areas decayed since the middle of 2008 with a time constant of 1.5–2.5 years, implying that the ongoing eruption won't last long. This uniform decay time indicates that the western part is connected to the eruption center since the middle of 2008 to form a system with stationary geometry. Our observation that the decay started later to the west than around the vent suggests that the subsidence to the west has been triggered by the mud eruption. A simple modeling suggests that 1) the conduit needs to be narrower at depth than at the surface, 2) the effective rigidity of the mud needs to be lower than that estimated from the drilled sample, or both to explain the observed decay constant of the deformation.

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## 1. Introduction

Mud volcanism is a process that drives materials in the sediment to the surface. It shares common features with magmatic volcanism. For example, both of them often form calderas and aligned vents that are controlled by ambient stress (e.g., Bonini, 2012). Nevertheless, the mechanics of mud volcanism is not as well studied as that of magmatic volcanism because of its rare occurrence. With this background, the eruption of Lumpur Sidoarjo (LUSI), eastern Java Island, Indonesia, provides us with a precious opportunity to observe the mud volcanism from its birth.

LUSI, which has been erupting since 29 May 2006, is located in the eastern Java Island, a region prone to mud volcanism due to an extensive sedimentation (Fig. 1a; Mazzini et al., 2007, 2009). Fig. 2 summarizes the evolution of mud extrusion rates taken from published literatures. The extrusion rate was around 50,000 m<sup>3</sup>/day during the first few months (Istadi et al., 2009). It increased to 125,000 m<sup>3</sup>/day in September 2006, four months after the onset and reached its maximum of 180,000 m<sup>3</sup>/day (Mazzini et al., 2007, 2009; Istadi et al., 2009) before decreasing to 90,000 m<sup>3</sup>/day in August 2008 and less than 10,000 m<sup>3</sup>/day by the middle of 2010 (Mazzini et al., 2009; Rudolph et al., 2013). The extruded mud buried more than an area of 7 km<sup>2</sup>, forced more than 60,000 people to evacuate, and caused more than 4 billion US dollars of damage (e.g., Rudolph et al., 2013).

With this background, it is important to understand the mechanics of the LUSI eruption and an eruption of mud volcano in general. From a practical point of view, it is important to evaluate the longevity of the eruption. Some previous studies estimated the longevity of tens of years from physical modeling (Istadi et al., 2009; Davies et al., 2011; Rudolph et al., 2011). Rudolph et al. (2013) challenged the previous studies with Synthetic Aperture Radar (SAR) data to conclude that the eruption will decay in a few years because the deformation has been decaying with a characteristic time of a few years.

Here we follow a similar path with Rudolph et al. (2013) to derive the evolution of the displacement field associated with the LUSI eruption from SAR images taken from the ALOS satellite (Shimada et al., 2008), which yields good coherence even in vegetated regions like Indonesia. While Rudolph et al. (2013) used SAR images only from the descending orbit, we used images from the ascending orbit as well to gain more insights into the evolution of the deformation. Our main finding is that the deformation associated with the mud eruption extends to the west as well as around the vent. This suggests that the mud is fed from the west of the vent where a gas field extends, as well as from right beneath the vent.

## 2. SAR images and processing

We processed a total of 93 SAR images from five different paths, two of which are from the ascending orbit and three are from the descending orbit (Fig. 1b, Table 1). Images from some paths have spans of more than four years, much of the lifetime of the ALOS satellite, while some span only about a year (Table 1).

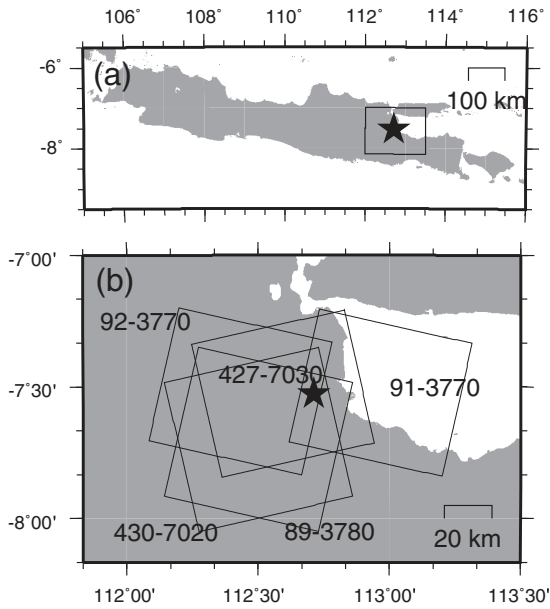
We processed the SAR data by the StaMPS software (Hooper, 2008) to derive the temporal evolution of persistent scatterers. Fig. 3 shows

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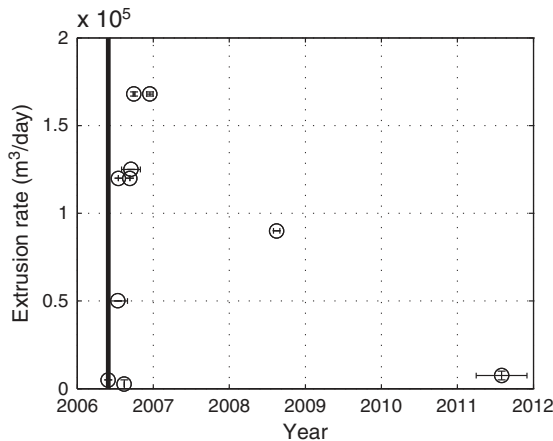
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**Fig. 1.** (a) Location of LUSI mud volcano shown by star. Rectangle depicts the area shown in (b). (b) A close-up map around LUSI shown by star. Rectangles represent the spatial extent of SAR images used in this study. Paths and frames of the SAR images are also shown.

the spatial distribution of total line-of-sight (LOS) changes during the observation period obtained by images from each track. Images from 89–3780 give much smaller total LOS changes (Fig. 3e) because the images from this track spans only about a year. Total displacements from other four tracks (Fig. 3a–d) give similar spatial pattern, with a maximum LOS extension of about 200 mm. A similar pattern between ascending and descending images, which have roughly an opposite sensitivity to east–west displacements, suggests that the observed LOS extension is dominated by subsidence rather than horizontal displacements. The actual maximum LOS extension around the vent is probably larger than the observation because the mud extrusion prevents us from obtaining coherent interferograms close to the vent. Note that the method we employed in this study gives the time series of persistent scatterers only when they are coherent during the whole time period (Hooper, 2008) so that the time series near the vent cannot be obtained because of the decoherence due to mud extrusion. This leads to poorer data coverage near the vent than previous studies (Fukushima et al.,



**Fig. 2.** Temporal evolution of the mud extrusion rate taken from published literatures (Mazzini et al., 2007, 2009, 2012; Istadi et al., 2009). Lengths of error bars, in particular for the extrusion rate, are somewhat arbitrary. The vertical bar indicates the time of the onset of the eruption.

2009; Rudolph et al., 2013). Fig. 3 also shows that the area of LOS extension is not limited around the vent, shown by star, but extended to the west, where the Wanut gas field exists.

While LOS extension is prevailing in most of the area from both ascending and descending images, an exception is seen to the northwest of the vent, where LOS contraction and extension are observed from ascending and descending images, respectively (Fig. 3). This pattern indicates a dominance of westward motion there and the observed deformation is not due to the mud extrusion but due to something else, possibly due to a faulting (Mazzini et al., 2007). Here we do not explore the cause of the deformation observed to the northeast of the vent.

Because of the mud extrusion and accumulation on the surface, it is also possible that the observed LOS extension is due to the elastic response of the Earth by the mud loading. Here we exploit this possibility by simply assuming a point loading of mud with a mass  $M = \rho_e V_e$  where  $\rho_e$  and  $V_e$  are density and volume of the extruded mud as done by Fukushima et al. (2009) who concluded that the deformation caused by mud loading is negligible. Here we test whether we can still ignore the effect of mud loading to explain the deformation field between 2006 and 2011, instead of the first five months of the eruption tested by Fukushima et al. (2009). Note that the extruded mud volume between 2006 and 2011 is about 10 times larger than that during the first five months.

This problem is known as the Boussinesq problem (Boussinesq, 1878; Jaeger et al., 2007, pp. 408), in which the radial and vertical displacements,  $u_r$  and  $u_z$ , respectively, are given as a function of radial distance  $r$  by

$$u_r = \frac{(1 + \nu)(1 - 2\nu) Mg}{4\pi E_c} \frac{1}{r}, \quad (1)$$

$$u_z = -\frac{1 - \nu^2 Mg}{2\pi E_c} \frac{1}{r} \quad (2)$$

where  $E_c$  and  $\nu$  represent Young's modulus and Poisson's ratio of the crust, respectively, and  $g$  denotes gravitational acceleration.

Assuming  $E_c = 5$  GPa,  $\nu = 0.25$  and  $\rho_e = 1500$  kg/m<sup>3</sup> obtained from drilling samples (Istadi et al., 2009) and  $V_e = 7 \times 10^7$  m<sup>3</sup> from the buried area of  $\sim 7$  km<sup>2</sup> and the average mud height of  $\sim 10$  m, the displacement at  $r = 2$  km  $isu_r = 4.7$  mm and  $u_z = 14.0$  mm. This corresponds to the LOS extension of at most  $\sim 14$  mm, which is larger than the detection threshold but much smaller than the observed LOS extension of up to  $\sim 200$  mm. We can thus safely conclude that the mud loading contributes less than 10% of the observed LOS changes, although it is not completely negligible. Note that there is no mud loading to the west of the vent where significant LOS extension was observed so that the LOS extension is purely due to the depressurization at depth.

### 3. Evolution of displacements

Next we explored the evolution of LOS changes at representative points shown in Fig. 3. The obtained time series, particularly for western points (Fig. 4a,b), shows accelerations in the LOS displacements until early to middle of 2008, or 1.5 to 2 years after the onset of the eruption, before subsequent deceleration.

We then tried to fit each time series in  $t_0 > 2008.408$  yr, or more than two years from the eruption onset, by exponential functions as

$$d = A \exp\left(-\frac{t}{\tau}\right) + C \quad (3)$$

where  $d$  is the observed LOS changes and  $t$  is time.  $A$ ,  $C$ , and  $\tau$  are model parameters to be estimated to minimize the sum of squared residuals. Here  $\tau$  is called the relaxation time where the displacement rate decays by  $1/e$  in  $\tau$  years.

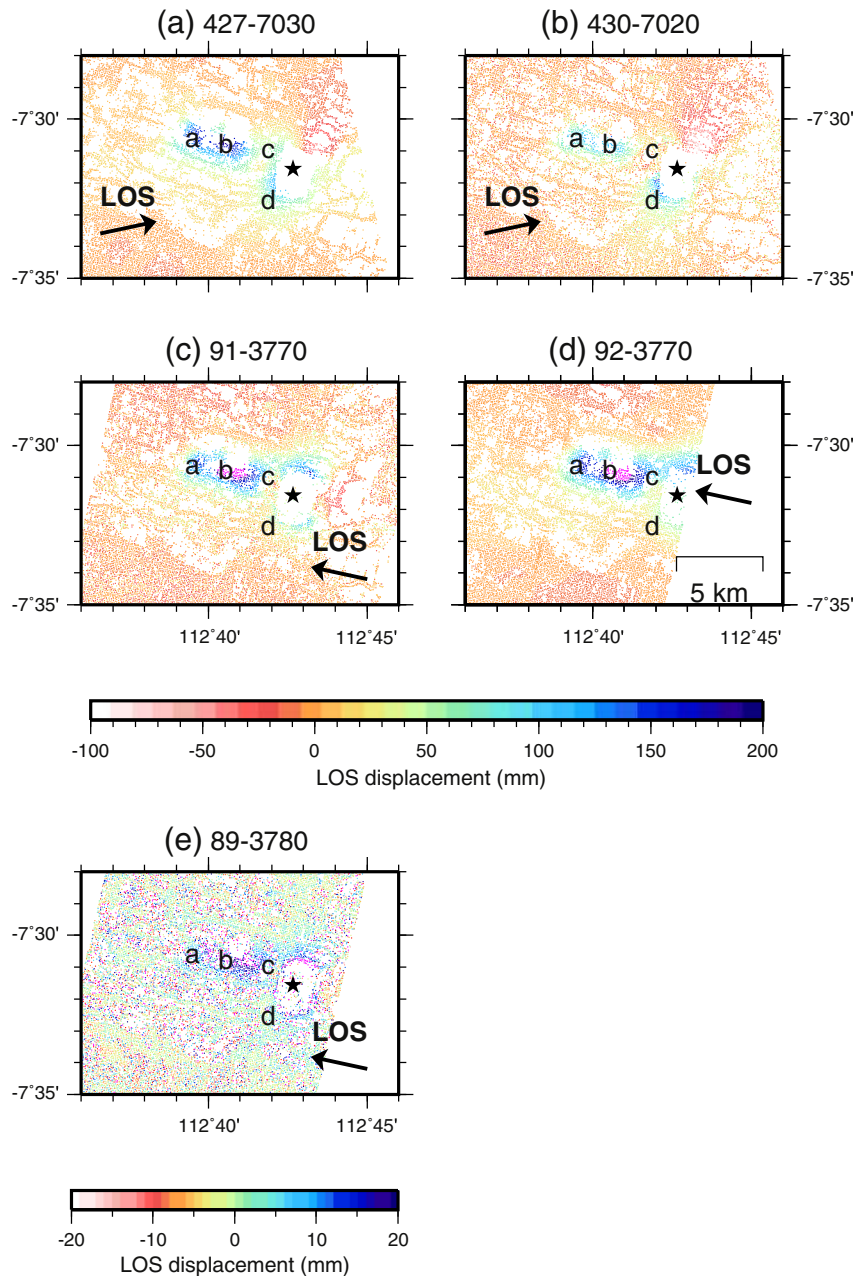
**Table 1**  
List of SAR images used in this study.

Path–frame	LOS direction <sup>a</sup>	Start date	End date	Span (yr)	# of images
89–3780	[−0.719, 0.154, −0.678]	3 Jan. 2007	21 Feb. 2008	1.13	9
91–3770	[−0.611, 0.131, −0.780]	24 Mar. 2007	4 Apr. 2011	4.30	22
92–3770	[−0.611, 0.131, −0.780]	8 Oct. 2006	21 Apr. 2011	4.53	25
427–7030	[0.611, 0.131, −0.780]	30 Dec. 2006	25 Feb. 2011	4.16	21
430–7020	[0.719, 0.154, −0.678]	19 May 2006	9 Jan. 2009	2.62	14

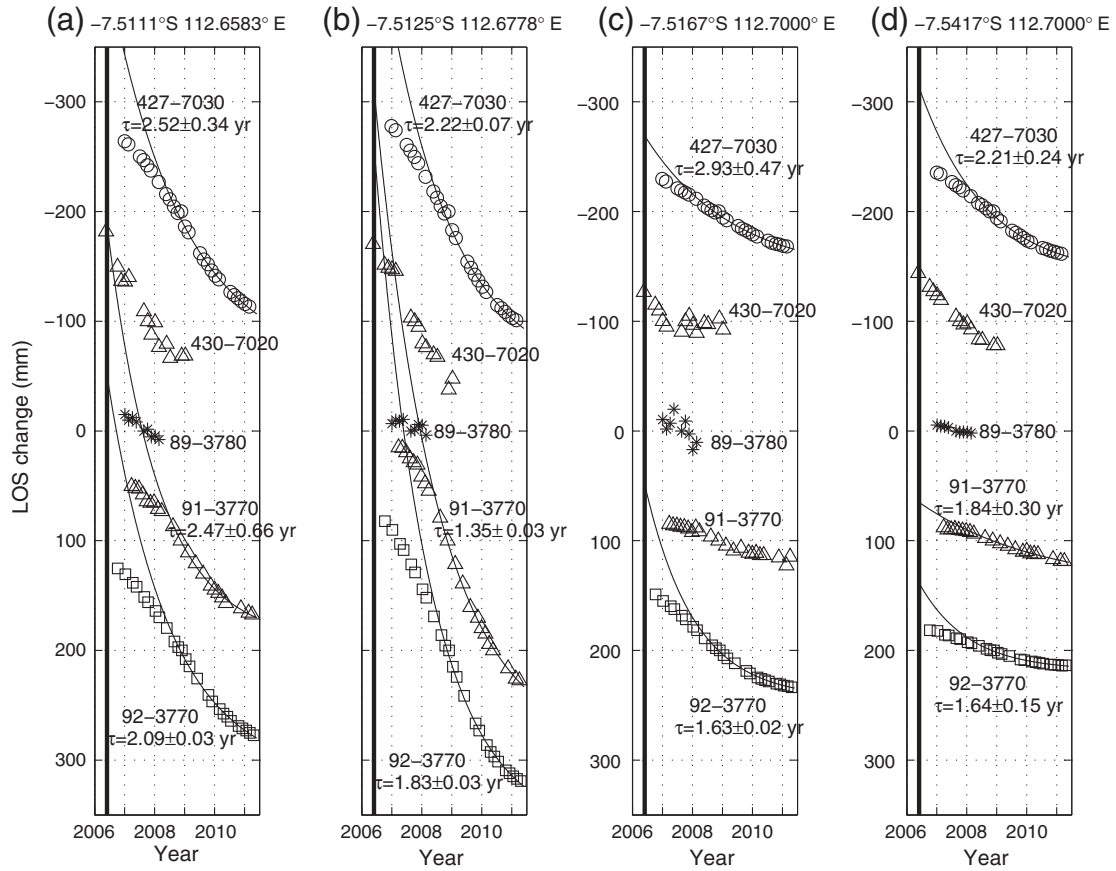
<sup>a</sup> Unit vectors of LOS. The first, second, and third components correspond to the east, north, and vertical components, respectively.

The derived relaxation times do not vary much between western and eastern points; they are mostly between 1.5 and 2.5 years (Fig. 4). Note that a relaxation time is estimated only when an *F*-test

(e.g., Menke, 2012, pp. 111–112) shows that an exponential curve fits the time series better than a linear fit with a confidence of 95%. Thus a relaxation time is not obtained from noisy or short time series. (Fig. 4).



**Fig. 3.** Total LOS displacements derived from SAR images for each path. Note that subsidence leads to a positive LOS displacement. Star depicts the location of the vent. The horizontal projection of the LOS vectors is also shown. Characters a, b, c, and d depict points where temporal evolution is plotted in Fig. 4. SAR images from 89–3780 (e) have shorter time span (Table 1) so that the total LOS change is smaller. Because of this, a different color scale is employed. Note that incoherence of SAR images due to the mud extrusion prevents us to obtain LOS changes close to the vent.



**Fig. 4.** Temporal evolution of LOS changes for four representative points whose location is shown in Fig. 3. Solid curves denote the calculated LOS changes by exponential curves (Eq. (3)) to fit the observed LOS changes more than two years after the onset of the eruption ( $t > 2008.408$ ). They are shown only when an *F*-test (Menke, 2012, p. 111–112) gives a better fit with an exponential fit than a straight-line regression by a confidence level of 95%.

## 4. Discussion

### 4.1. Insights from the observation

As long as an elastic medium is assumed, the relaxation time of around 2 years suggests that the depressurization at depth is also decelerating with a time constant of around 2 years. Because the evolution of depressurization is viewed as a good proxy for that of mud extrusion, our result indicates that the mud eruption will cease soon, contrary to earlier studies (Istadi et al., 2009; Davies et al., 2011; Rudolph et al., 2011) that forecasted that the eruption will likely last for decades. This rapid decay of deformation is qualitatively consistent with the mud extrusion rate that decayed to 5000–10,000 m<sup>3</sup>/day in 2011 from its maximum of ~180,000 m<sup>3</sup>/day and ~90,000 m<sup>3</sup>/day in August 2008 (Istadi et al., 2009; Mazzini et al., 2012, Fig. 2).

Fig. 4 shows that the departure from the exponential decay before mid-2008 is bigger in the western points than those in the east. This reflects an earlier onset of the exponential decay to the east. While Rudolph et al. (2013) derived a longer decay time to the west, their estimate is probably biased by the delayed onset of the exponential decay to the west. Combining our results with an observation that the deformation to the west is subtle, if not null, during the first six months of the eruption, in contrast with a significant deformation around the vent (Fukushima et al., 2009), we conclude that the deformation to the west was triggered by the eruption with some delay, accelerated, and then started to decay later than that around the vent. This temporal evolution suggests that the western subsidence could be connected to the near-vent subsidence. Give that the area of western subsidence corresponds

to a gas field, however, it is also possible to interpret that the western subsidence does not have anything to do with the mud eruption but due to a gas extraction. To confirm the cause of the subsidence, we need independent information such a time series of the amount of gas extraction there.

### 4.2. A simple physical model

Here we consider a simple model to constrain the geometry of the mud volcano system that is consistent with the decay constant of the observed LOS changes after the middle of 2008. See Table 2 for symbols and descriptions of parameters used in this study. Following Zoporowski and Miller (2009), let us assume a situation in which mud with density  $\rho_c$  ascends by velocity  $v$  from a cylindrical reservoir of volume  $V_r$  at depth  $h$  connected to a cylindrical conduit with cross-sectional area  $A$  leading vertically to the surface (Fig. 5).

Conservation of mass and momentum in the one-dimensional conduit is given by

$$\frac{d\rho_c}{dt} + \frac{d(\rho_c v)}{dz} = 0 \quad (4)$$

where  $z$  is the vertical direction with positive upwards and  $t$  represents time. If we assume an isochronic flow in the conduit,  $\rho_c$  and  $v$  are independent of position  $z$ , so that Eq. (4) leads to

$$\frac{d\rho_c}{dt} = 0. \quad (5)$$

**Table 2**  
Parameter symbols and descriptions used in this study.

Symbol	Definition (unit)	Typical value
$A$	Cross-sectional area of the conduit ( $\text{m}^2$ )	$6^{a,b} - \times 10^{3c}$
$a$	Radius of the mud chamber (m)	$1000^d$
$d$	Observed LOS change (m)	
$\eta$	Mud viscosity ( $\text{Pa} \cdot \text{s}$ )	$10^{4e}$
$g$	Gravitational acceleration ( $\text{m/s}^2$ )	9.81
$\Gamma$	Compliance of the mud reservoir ( $\text{m}^3/\text{Pa}$ ) <sup>f</sup>	
$h$	Height of the conduit (m)	$1500^{d,g}$
$I$	Flux of mud into the mud reservoir ( $\text{m}^3/\text{s}$ )	
$\mu_c$	Rigidity of the crust (GPa)	$2^b$
$\mu_m$	Rigidity of mud in the conduit (GPa)	$2^g$
$\nu$	Poisson's ratio	0.25
$p$	Pressure at the mud reservoir (Pa)	
$Q$	Mud discharge rate ( $\text{m}^3/\text{s}$ )	
$\rho_c$	Mud density in the conduit ( $\text{kg/m}^3$ )	$1500^g$
$\rho_e$	Density of the extruded mud ( $\text{kg/m}^3$ )	$1500^g$
$\tau$	Time constant for exponential relaxation (1/s)	
$uz$	Vertical displacement (m)	
$ur$	Radial displacement (m)	
$V_e$	Volume of the extruded mud ( $\text{m}^3$ )	$7 \times 10^7$
$V_r$	Volume of the mud reservoir ( $\text{m}^3$ )	$10^7$
$v$	Velocity of ascending mud	
$\beta$	Compressibility of the mud ( $1/\text{Pa}$ ) <sup>h,i</sup>	$3 \times 10^{-10}$
$E$	Young's modulus of the crust (GPa) <sup>j</sup>	5

a: The value taken in a numerical simulation by Rudolph et al. (2011).

b: Our study suggests a lower value.

c: Visual inspection of the current vent.

d: Depth of the mud reservoir inferred from InSAR observations by Fukushima et al. (2009).

e: The value taken in a numerical simulation by Rudolph et al. (2011) based on sample measurements (Mazzini et al., 2007; Manga et al., 2009; Rudolph and Manga (2010)).

f: The value depends on the shape of the mud reservoir.

g: Depth of the mud source estimated from the P-wave velocity and density of mud samples (Istadi et al., 2009).

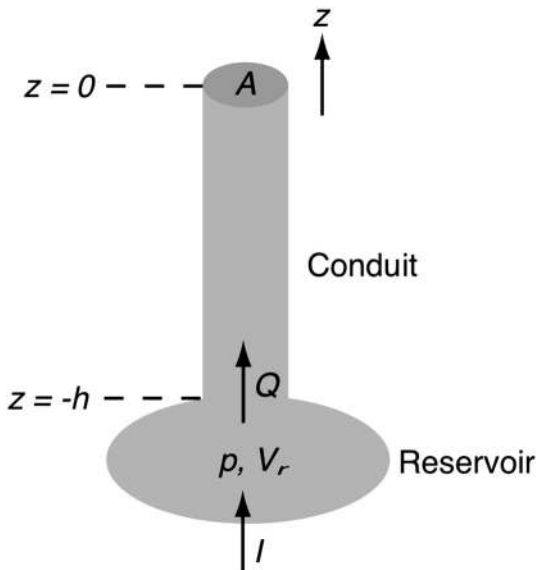
h: Derived from given  $\mu_m$  and  $\nu$  by  $\beta = 3(1 - 2\nu) / (2\mu_m(1 + \nu))$ .

i: Our study suggests a higher value.

j: Derived from given  $\mu_m$  and  $\nu$  by  $E = 2\mu_c(1 + \nu)$ .

Conservation of momentum is described by the one-dimensional Navier–Stokes equation with negligible convection as

$$\frac{d(\rho_c v)}{dt} = -\frac{dp}{dz} - \rho_c g - \frac{8\pi\eta v}{A} \quad (6)$$



**Fig. 5.** A conceptual model of the mud volcano model.

where  $\eta$  and  $g$  denote constant dynamic viscosity and gravitational acceleration, respectively. Here we took a constant viscosity of  $10^4$  Pa·s, the value taken in from a numerical simulation by Rudolph et al. (2011) based on sample measurements (Mazzini et al., 2007; Manga et al., 2009; Rudolph and Manga, 2010). This value is comparable with that of mafic magmas, but we assumed a depth-independent viscosity unlike that in the modeling of magmatic eruptions. While the viscosity increase by vesiculation makes a significant role in conduit processes during magmatic eruptions (e.g., Gonnermann and Manga, 2007), we can assume a constant viscosity in this case because the presence of stable gas hydrates on mud breccia provides little opportunity for degassing (Murton and Biggs, 2003).

Combining Eqs. (5) and (6) and replacing  $-dp/dz$  with  $p/h$  gives a differential equation with respect to flux  $Q = Av$  as

$$\frac{dQ}{dt} = -\frac{8\pi\eta}{\rho_c A} Q + \frac{A}{\rho_c h} p - Ag. \quad (7)$$

Conservation of the fluid mass inside the reservoir is described as

$$\frac{d(\rho_c V_r)}{dt} = \rho_c (I - Q) \quad (8)$$

where  $I$  denotes the influx of mud. Eq. (8) is rewritten using mud compressibility  $\beta$

$$\beta = \frac{1}{\rho_c} \frac{d\rho_c}{dp} \quad (9)$$

as

$$\frac{dp}{dt} = \frac{1}{\beta V_r} \left( I - Q - \frac{dV_r}{dt} \right). \quad (10)$$

$V_r$  and  $p$  are related by

$$dV_r = \Gamma dp \quad (11)$$

where  $\Gamma$  is compliance of the reservoir which depends on the shape of the mud reservoir. For example,

$$\Gamma = \frac{8(1-\nu)a^3}{3\mu_c} \quad (12)$$

for a horizontal circular sill with radius  $a$  embedded in a homogeneous, elastic, and isotropic halfspace with rigidity  $\mu_c$  (Fialko et al., 2001). Eq. (12) is derived with an approximation that the depth of the sill is larger than its radius. Combining Eqs. (10) and (11) gives

$$\frac{dp}{dt} = \frac{I - Q}{\beta V_r + \Gamma}. \quad (13)$$

Eqs. (7) and (13) form a simultaneous differential equation described in matrix form as

$$\frac{d}{dt} \begin{bmatrix} p \\ Q \end{bmatrix} = \mathbf{R} \begin{bmatrix} p \\ Q \end{bmatrix} + \begin{bmatrix} I/(\beta V_r + \Gamma) \\ -Ag \end{bmatrix}, \quad (14)$$

$$\mathbf{R} = \begin{bmatrix} 0 & -1/(\beta V_r + \Gamma) \\ A/(\rho_c h) & -8\pi\eta/(\rho_c A) \end{bmatrix}. \quad (15)$$

Solving this equation, the mud chamber pressure  $p$ , the change of which results in observed LOS changes in this case, is written as

$$p(t) = c_1 e^{\lambda_+ t} + c_2 e^{\lambda_- t} + p(\infty) \quad (16)$$

$$Q(t) = c_3 e^{\lambda_+ t} + c_4 e^{\lambda_- t} + Q(\infty) \quad (17)$$

where  $c_1$ ,  $c_2$ ,  $c_3$ , and  $c_4$  are constants derived by solving Eqs. (14) and (15), and  $\lambda_+$  and  $\lambda_-$  correspond to eigenvalues of  $\mathbf{R}$  that are

$$\lambda_{\pm} = -\frac{4\pi\eta}{\rho_c A} \left( 1 \pm \sqrt{1 - \frac{A^2}{4\pi h \eta (\beta V_r + \Gamma)}} \right) \quad (18)$$

and

$$\begin{aligned} \begin{bmatrix} p(\infty) \\ Q(\infty) \end{bmatrix} &= \mathbf{R}^{-1} \begin{bmatrix} -I/(\beta V_r + \Gamma) \\ Ag \end{bmatrix} \\ &= \frac{A}{\rho_c h (\beta V_r + \Gamma)} \begin{bmatrix} 8\pi\eta l / (\rho_c h) + Ag \\ Al / (\rho_c h) \end{bmatrix}. \end{aligned} \quad (19)$$

If  $A^2 > 4\pi h \eta (\beta V_r + \Gamma)$ , in which the system is underdamped, the temporal evolution of  $p$  is represented by an oscillation with amplitude decaying exponentially. In this case, The amplitude decay has a time constant of  $\rho_c A / (4\pi\eta)$ . If  $A^2 < 4\pi h \eta (\beta V_r + \Gamma)$ , on the other hand, the system is overdamped and the temporal evolution of  $p$  is described by exponential decays with two time constants,  $-1/\lambda_+$  and  $-1/\lambda_-$ .

Here we examine whether the system of LUSI is over or underdamped by applying realistic values (Table 2). If the system were underdamped, the characteristic decay time is  $\rho_c A / (4\pi\eta)$  (Eq. 18). Assuming realistic parameters (see Eq. (12) and Table 2) requires  $A > 1.4 \times 10^4 \text{ m}^2$ , indicating that the radius of the conduit needs to be large than  $\sim 66 \text{ m}$  for the system to be underdamped. This value is larger than the radius of the current vent that is at most  $35 \text{ m}$  and the effective radius suggested by Rudolph et al. (2011) from numerical simulations ( $1 \text{ m}$ ). Thus the system should be highly overdamped with  $A^2 \ll 4\pi h \eta (\beta V_r + \Gamma)$ . Eq. (18) can then be rewritten by

$$\lambda_+ = -\frac{8\pi\eta}{\rho_c A} \left( 1 - \frac{A^2}{16\pi h \eta (\beta V_r + \Gamma)} \right) \quad (20)$$

$$\lambda_- = \frac{-A}{2\rho_c h (\beta V_r + \Gamma)} \quad (21)$$

where  $\lambda_+$  and  $\lambda_-$  correspond to the shorter and longer relaxation time, respectively. Surprisingly, Eq. (21) indicates that the longer relaxation time does not depend on the dynamic viscosity of mud  $\eta$ .

Here we explore possible parameter sets to be consistent with the observation that has a relaxation time of about 2 years or  $\lambda_- = 1.58 \times 10^{-8} \text{ /s}$ . Substituting a value taken from a numerical simulation by Rudolph et al. (2011) ( $A = 6 \text{ m}^2$ ; Table 2) gives  $\lambda_- \sim 1.33 \times 10^{-6} \text{ /s}$  or a relaxation time of about 8.7 days, two orders of magnitude shorter than the observation. Eq. (21) suggests smaller  $A$ , smaller  $\mu_m$ , larger  $a$ , larger  $V_r$  or a combination of these are required to be consistent with the observation. Given the spatial extent of the observed LOS displacements,  $a$  and  $V_r$  may not be much larger than those currently assigned. Smaller  $A$ , smaller  $\mu_m$ , or both are thus required to match up with the observation. For example,  $\mu_m = 0.2 \text{ GPa}$  and  $A = 0.6 \text{ m}^2$ , both of which are an order of magnitude smaller than the previous values, give  $\lambda_- \sim 1.33 \times 10^{-8} \text{ /s}$  or a relaxation time of  $\sim 2.4$  years, more consistent with the observation. Although Istadi et al. (2009) derived the rigidity of the mud as  $\sim 2 \text{ GPa}$  from drilling samples, it might not represent the rigidity of the mud responsible for the eruption but represent the bulk property around the mud volcano. While visual inspection from satellite images suggests that the conduit has a diameter of about  $70 \text{ m}$  or  $A \sim 4 \times 10^3 \text{ m}^2$  at the surface, the conduit is probably, at least effectively, narrower at depth.

## 5. Conclusion

We derived the temporal evolution of ground deformation associated with the eruption of LUSI mud volcano between 2006 and 2011 from a time series analysis of SAR images from the ALOS satellite. Our results show that the marked subsidence is observed to the west of the eruption center as well as around the vent. The observed total LOS changes are up to  $200 \text{ mm}$  or more. We also inferred that the LOS changes decays exponentially after the middle of 2008 with a time constant of  $1.5\text{--}2.5$  years in the both areas. This short decay time indicates that the eruption won't last long. This observation also shows that the near-vent area and western part have been connected since the middle of 2008 with a stationary geometry. The creation of this system makes the mud extrusion controlled by a pressure gradient between the mud reservoir and surface. The time series we obtained also revealed that the onset of the exponential decay around the vent is earlier than the western part by about a half year. We also observed that the subsidence in the western part has been accelerated until 2007 when the subsidence around the vent had stopped accelerating. These observations suggest that the subsidence to the west has been triggered by the mud eruption with time delay.

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