

HADAMARD-TYPE INEQUALITIES FOR GENERALIZED CONVEX FUNCTIONS

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Abstract. In this paper we investigate (ω_1, ω_2) -convex functions and obtain characterization theorems and Hadamard-type inequalities for them.

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