

Handbook of 

# Formulas and Software for Plant Geneticists and Breeders



Manjit S. Kang • Editor

*Manjit S. Kang*  
*Editor*

## ***Handbook of Formulas and Software for Plant Geneticists and Breeders***



*Pre-publication  
REVIEWS,  
COMMENTARIES,  
EVALUATIONS . . .*

**"T**his is indeed a reference book that can help plant scientists identifying friendly software to analyze their experimental data. This book is a compendium of analytical tools that can save precious time and effort for plant geneticists and breeders, making their data analysis more efficient, accurate, and informative. It describes freely available software that could be time-consuming to develop by individual research programs. I value this book as a good teaching tool where students can become familiar with software and analytical methods and learn how to analyze experimental data."

**Javier Betran, PhD**  
*Assistant Professor,  
Corn Breeding and Genetics,  
Department of Soil and Crop Sciences,  
Texas A&M University*

**"T**he title of this book is a very concise and precise description of the contents; it is a great handbook for addressing many of the theoretical and applied aspects of plant genetics and breeding. There is something for everyone involved in these fields.

The general layout is very consistent, which makes it easy to find particular areas of interest. Most chapters contain useful examples and sample data which are quite helpful when working through some of the formulas for the first time, or in loading them into spreadsheets. The contributing authors have been selected for their expertise in their particular fields and for their ability to convey their messages effectively. The final chapter is typical of the clear, practical, and often classical examples in that it gives a single formula to determine the number of plants needed to recover a pre-determined number of individuals with a desired trait at a particular probability level when the genetic nature of the trait is known."

**Duane E. Falk, PhD**  
*Associate Professor and Cereal Breeder,  
Plant Agriculture Department,  
University of Guelph,  
Ontario*

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# Handbook of Formulas and Software for Plant Geneticists and Breeders

Manjit S. Kang  
Editor



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Dr. Kang is the editor, author, or co-author of hundreds of articles, books, and book chapters. He enjoys an international reputation in genetics and plant breeding. He serves on the editorial boards of *Crop Science*, *Agronomy Journal*, *Journal of New Seeds*, and the *Indian Journal of Genetics & Plant Breeding*, as well as The Haworth Food Products Press.

Dr. Kang is a member of Gamma Sigma Delta and Sigma Xi. He was elected a Fellow of the American Society of Agronomy and of the Crop Science Society of America. In 1999 he served as a Fulbright Senior Scholar in Malaysia.

Dr. Kang edited *Genotype-By-Environment Interaction and Plant Breeding* (1990), which resulted from an international symposium that he organized at Louisiana State University in February 1990. He is the author/publisher of *Applied Quantitative Genetics* (1994), which resulted from teaching a graduate-level course on Quantitative Genetics in Plant Improvement. Another book, *Genotype-By-Environment Interaction*, edited by Dr. Kang and Hugh Gauch Jr., was published by CRC Press in 1996. He edited *Crop Improvement for the 21st Century* in 1997 (Research Signpost, India). He recently co-authored *GGE Biplot Analysis: A Geographical Tool for Breeders, Geneticists, and Agronomists* (2002, CRC Press), and he edited *Crop Improvement: Challenges in the Twenty-First Century* (2002, The Haworth Press) and *Quantitative Genetics, Genomics, and Plant Breeding* (2002, CABI Publishing, U.K.).

Dr. Kang's research interests are: genetics of resistance to aflatoxin, weevils, and herbicides in maize; genetics of grain dry-down rate and stalk quality in maize; genotype-by-environment interaction and crop adaptation; interorganismal genetics, and conservation and utilization of plant genetic resources.

Dr. Kang taught Plant Breeding and Plant Genetics courses at Southern Illinois University–Carbondale (1972-1974). He has been teaching a graduate-level Applied Quantitative Genetics course at Louisiana State University since 1986. He developed and taught an intermediary plant genetics course in 1996 and team-taught an Advanced Plant Genetics course (1993-1995). He also taught an Advanced Plant Breeding course at LSU in 2000. He has directed six MS theses and six PhD dissertations. He has been a Full Professor in the Department of Agronomy at LSU since 1990. He has received many invitations to speak at international symposium relative to genetics and plant breeding.

Dr. Kang was recognized for his significant contributions to plant breeding and genetics by Punjab Agricultural University at Ludhiana at its 36th Foundation Day in 1997. He served as President (2000-2001) of the LSU Chapter of Sigma Xi—The Scientific Research Society. He was elected President of the Association of Agricultural Scientists of Indian Origin in 2001 for a two-year term. In addition, he serves as the Chairman of the American Society of Agronomy's Member Services and Retention Committee (2001-2004). Dr. Kang's biographical sketches have been included in *Marquis Who's Who in the South and Southwest*, *Who's Who in America*, *Who's Who in the World*, *Who's Who in Science and Engineering*, and *Who's Who in Medicine and Healthcare*.

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# Preface

Statistical techniques and formulas have been part and parcel of genetics and breeding programs. Some techniques and formulas are used routinely while others may be used only occasionally. The ones used frequently have been incorporated into popular statistical packages, such as the Statistical Analysis System (SAS), and are readily available. To meet their needs, researchers began developing specific software not found in statistical packages. For example, in the early 1980s, I began using in my research relative to genotype-by-environment interaction a formula for stability variance that Shukla (1972) developed and a formula for ecovariance that Wricke (1962) developed. Hand calculations for these formulas were tedious and time-consuming. Thus, in my necessitous circumstances I wrote a computer program in the matrix programming language of SAS (Kang, 1985). *The Journal of Heredity* published a description of the program, and I received several hundred requests for the program code from researchers around the world who were working with plants and animals, and I also received requests from those working with humans, e.g., psychiatrists (Kang, 1986). Having published several other programs since, I have realized that there is a need among researchers for special software programs for use in research. For example, geneticists working with many different crops requested the DIALLEL-SAS program (Zhang and Kang, 1997).

Software programs, or descriptions thereof, are occasionally published in international journals such as *The Journal of Heredity* and *Agronomy Journal*. Full-fledged codes for statistical and genetics-related software programs are rarely published in journals because they are generally not the main domain of these journals. I believe it would better serve the scientific community to have published or unpublished programs made more easily accessible in a handbook.

With the intent of making available to researchers and teachers of genetics and breeding a compendium devoted to such specialized programs as DIALLEL-SAS and those which others have created around the world, I



turned to Food Products Press, an imprint of The Haworth Press, Inc. ([www.haworthpressinc.com](http://www.haworthpressinc.com)), to undertake the publication of *Handbook of Formulas and Software for Plant Geneticists and Breeders*. A questionnaire was sent to some 2,300 members of the C1 Division (geneticists and breeders) of the Crop Science Society of America (CSSA) and many contributors were identified. The response was excellent as evidenced by the various contributions in this book.

This first edition of the handbook is an excellent start to meet the needs of the scientific community. I am sure as researchers, teachers, and students begin to realize the usefulness of this effort, additional contributions will follow, which can, hopefully, be included in a subsequent edition. In this handbook, most contributions of a specific software include program codes and practical examples on how to use the software or formula in question; others direct the reader where to get specific software. Due to the enormous effort devoted to linkage and mapping using molecular markers, I have also included a chapter that lists software on genetic linkage and mapping that can be accessed via the Internet (Chapter 26). Obviously, program codes are not printed for the software listed in that group. I trust the handbook will serve as an up-to-date, ready reference on genetic formulas and software for practicing geneticists/breeders, as well as for students. Please send any comments on this handbook or new contributions to this editor and author, via e-mail, at <[mKang@agctr.lsu.edu](mailto:mKang@agctr.lsu.edu)> or <[kang\\_majit@hotmail.com](mailto:kang_majit@hotmail.com)>.

I thank Dr. Amarjit S. Basra, Editor-in-Chief with Food Products Press, for his encouragement. This project could not have been accomplished without the participation and cooperation of the various authors and the publisher.

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## Chapter 1

# DIALLEL-SAS: A Program for Griffing's Diallel Methods

Yudong Zhang  
Manjit S. Kang

### *Importance*

Diallel mating designs are frequently used in plant breeding research to obtain genetic information, such as general combining ability (GCA) and specific combining ability (SCA), and possibly narrow-sense heritability. Griffing (1956) developed four methods to compute GCA and SCA. These methods have provided valuable information on various important traits in crops (Borges, 1987; Moffatt et al., 1990; Pixley and Bjarnason, 1993; Kang et al., 1995). To obtain more reliable genetic information, multi-environment data are generally needed. The following statistical models illustrate Griffing's methods for analyzing multi-environment data:

The general linear model for Methods 1 and 3 (reciprocal crosses) is:

$$Y_{ijklc} = \mu + \alpha_l + b_{kl} + v_{ij} + (\alpha v)_{ijl} + e_{ijklc},$$

where  $v_{ij} = g_i + g_j + s_{ij} + r_{ij}$ ,  $(\alpha v)_{ijl} = (\alpha g)_{il} + (\alpha g)_{jl} + (\alpha s)_{ijl} + (\alpha r)_{ijl}$ ,  
 $r_{ij} = m_i + m_j + n_{ij}$ , and  $(\alpha r)_{ijl} = (\alpha m)_{il} + (\alpha m)_{jl} + (\alpha n)_{ijl}$ .

The general linear model for Methods 2 and 4 is:

$$Y_{ijklc} = \mu + \alpha_l + b_{kl} + v_{ij} + (\alpha v)_{ijl} + e_{ijklc},$$

where  $v_{ij} = g_i + g_j + s_{ij}$  and  $(\alpha v)_{ijl} = (\alpha g)_{il} + (\alpha g)_{jl} + (\alpha s)_{ijl}$ .

In these models,  $Y_{ijklc}$  = observed value of each experimental unit,  $\mu$  = population mean,  $\alpha_l$  = environment effect,  $b_{kl}$  = block or replication effect in each environment,  $v_{ij} = F_1$  hybrid effect,  $(\alpha v)_{ijl}$  = interaction between environ-

ments and  $F_1$  hybrids,  $e_{ijklc}$  = residual effect,  $g_i$  = GCA effect for  $i$ th parent,  $g_j$  = GCA effect for  $j$ th parent,  $s_{ij}$  = SCA for  $ij$ th  $F_1$  hybrid,  $r_{ij}$  = reciprocal effect for  $ij$ th or  $ji$ th  $F_1$  hybrid,  $(\alpha g)_{il}$  = interaction between GCA effect for  $i$ th parent and environments,  $(\alpha g)_{jl}$  = interaction between GCA effect for  $j$ th parent and environments,  $(\alpha s)_{ijl}$  = interaction between SCA effect for  $ij$ th  $F_1$  hybrid and environments,  $(\alpha r)_{ijl}$  = interaction between reciprocal effect for  $ij$ th or  $ji$ th  $F_1$  hybrid and environments,  $m_i$  = maternal effect of parental line  $i$ ,  $m_j$  = maternal effect of parental line  $j$ ,  $n_{ij}$  = nonmaternal effect of  $ij$ th or  $ji$ th  $F_1$  hybrid,  $(\alpha m)_{il}$  = interaction between environments and maternal effect of parental line  $i$ ,  $(\alpha m)_{jl}$  = interaction between environments and maternal effect of parental inbred  $j$ , and  $(\alpha n)_{ijl}$  = interaction between environments and nonmaternal effect of  $ij$ th or  $ji$ th  $F_1$  hybrid.

### **Definitions**

**Diallel:** A mating design in which all possible two-way combinations are produced among a set of genetically different lines. It is used to estimate GCA (average performance of the progeny) of each parental line in crosses with a set of lines and to estimate SCA (progeny performance of a specific cross).

### **Program Description**

DIALLEL-SAS was developed using SAS (SAS Institute, 1995). It provides a partition of  $F_1$  hybrid (or cross)  $\times$  environment (E) interaction into GCA  $\times$  E, SCA  $\times$  E, and reciprocal  $\times$  E components for Griffing's Methods 1 and 3, and into GCA  $\times$  E and SCA  $\times$  E components for Griffing's Methods 2 and 4. DIALLEL-SAS can be run on any microcomputer with SAS as well as on mainframe computers installed with SAS, via UNIX or TSO. The DIALLEL-SAS output for Methods 1 and 3 includes (1) mean squares for environments,  $F_1$  hybrids,  $F_1$  hybrids  $\times$  E, GCA, SCA, reciprocal, maternal, nonmaternal, GCA  $\times$  E, SCA  $\times$  E, reciprocal  $\times$  E, maternal  $\times$  E, nonmaternal  $\times$  E; (2) estimates of GCA and maternal effects for each parental line; and (3) estimates of SCA, nonmaternal, and reciprocal effects for each  $F_1$  hybrid.

### **Originator**

Griffing, B. (1956). Concept of general and specific combining ability in relation to diallel crossing systems. *Australian Journal of Biological Science* 9:463-493.

## ***Software Availability***

Zhang, Y. and Kang, M.S. (1997). DIALLEL-SAS: A SAS program for Griffing's diallel analyses. *Agronomy Journal* 89:176-182.

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## ***EXAMPLE***

A fictitious diallel data set for Griffing's Method 1 with five parental lines, two environments, and two replications per environment is analyzed using DIALLEL-SAS.

## ***DIALLEL-SAS Method 1 Program Listing with Output***

```

OPTIONS PS=56 LS=78;
TITLE 'METHOD 1';
DATA METHOD1;
INPUT I J REP HYBRID YIELD ENV;
DROP N NI NJ P;
P=5;*NUMBER OF PARENTAL LINES;
ARRAY GCA(N) G1 G2 G3 G4;
DO N=1 TO (P-1);
GCA=(( I=N) - (I=P)) + ((J=N) - (J=P));
END;
ARRAY SCA(N) S11 S12 S13 S14 S22 S23 S24 S33 S34 S44;
N=0;
DO NI=1 TO (P-1);
DO NJ=NI TO (P-1);
N+1;
IF NI=NJ THEN DO;
SCA=(I=NI) * ((J=NJ) - (J=P)) + (I=P) * ((J=P) - (J=NI));END;
ELSE DO;

```

```

SCA=(I=NI) * (J=NJ) - (J=P) * ((I=NI) + (I=NJ) - (I=P) * 2) + (I=NJ) * (J=NI)
- (I=P) * ((J=NI) + (J=NJ));
END;END;END;
ARRAY REC(N) R12 R13 R14 R15 R23 R24 R25 R34 R35 R45;
N=0;
DO NI=1 TO (P-1);
DO NJ=(NI+1) TO P;
N+1;
REC=(I=NI) * (J=NJ) - (J=NI) * (I=NJ);
END;END;
ARRAY MAT (N) M1 M2 M3 M4;
DO N=1 TO (P-1);
MAT=(I=N) + (J=P) - (J=N) - (I=P);
END;
ARRAY NONM (N) N12 N13 N14 N23 N24 N34;
N=0;
DO NI=1 TO (P-2);
DO NJ=(NI+1) TO (P-1);
N+1;
NONM=((I=NI) * (J=NJ)) - (I=NJ) * (J=NI) - ((I=NI) * (J=P)) + (I=NJ) * (J=P)
+ ((I=P) * ((J=NI) - (J=NJ)));
END;END;
CARDS;
1 1 1 1 10.5 1
1 1 2 1 10.7 1
1 2 1 2 11.9 1
1 2 2 2 12.0 1
1 3 1 3 14.5 1
1 3 2 3 14.2 1
1 4 1 4 9.0 1
1 4 2 4 8.5 1
1 5 1 5 13.5 1
1 5 2 5 14.2 1
2 1 1 6 12.8 1
2 1 2 6 13.2 1
2 2 1 7 16.2 1
2 2 2 7 17.0 1
2 3 1 8 20.5 1
2 3 2 8 18.2 1
2 4 1 9 9.8 1
2 4 2 9 10.3 1
2 5 1 10 16.5 1
2 5 2 10 18.4 1
3 1 1 11 8.9 1
3 1 2 11 10.2 1
3 2 1 12 15.4 1
3 2 2 12 16.0 1
3 3 1 13 17.8 1
3 3 2 13 18.9 1
3 4 1 14 22.1 1
3 4 2 14 23.0 1
3 5 1 15 18.4 1
3 5 2 15 20.6 1
4 1 1 16 12.0 1
4 1 2 16 12.2 1
4 2 1 17 13.4 1
4 2 2 17 14.2 1

```

4	3	1	18	13.5	1
4	3	2	18	13.8	1
4	4	1	19	21.2	1
4	4	2	19	20.7	1
4	5	1	20	17.8	1
4	5	2	20	19.4	1
5	1	1	21	20.1	1
5	1	2	21	21.3	1
5	2	1	22	20.9	1
5	2	2	22	21.2	1
5	3	1	23	19.2	1
5	3	2	23	20.2	1
5	4	1	24	22.2	1
5	4	2	24	21.6	1
5	5	1	25	20.8	1
5	5	2	25	21.3	1
1	1	1	1	11.2	2
1	1	2	1	11.7	2
1	2	1	2	11.2	2
1	2	2	2	12.7	2
1	3	1	3	14.3	2
1	3	2	3	15.2	2
1	4	1	4	9.2	2
1	4	2	4	9.5	2
1	5	1	5	13.0	2
1	5	2	5	14.9	2
2	1	1	6	12.2	2
2	1	2	6	12.8	2
2	2	1	7	16.0	2
2	2	2	7	17.8	2
2	3	1	8	19.5	2
2	3	2	8	18.8	2
2	4	1	9	10.4	2
2	4	2	9	11.3	2
2	5	1	10	16.9	2
2	5	2	10	18.0	2
3	1	1	11	10.8	2
3	1	2	11	11.2	2
3	2	1	12	15.0	2
3	2	2	12	16.6	2
3	3	1	13	17.2	2
3	3	2	13	17.9	2
3	4	1	14	21.1	2
3	4	2	14	22.6	2
3	5	1	15	19.2	2
3	5	2	15	21.6	2
4	1	1	16	12.6	2
4	1	2	16	13.2	2
4	2	1	17	12.4	2
4	2	2	17	13.2	2
4	3	1	18	14.5	2
4	3	2	18	15.8	2
4	4	1	19	20.2	2
4	4	2	19	20.1	2
4	5	1	20	17.0	2
4	5	2	20	18.4	2
5	1	1	21	22.1	2

```

5 1 2 21 21.0 2
5 2 1 22 21.9 2
5 2 2 22 20.2 2
5 3 1 23 20.2 2
5 3 2 23 20.8 2
5 4 1 24 21.2 2
5 4 2 24 20.6 2
5 5 1 25 20.2 2
5 5 2 25 21.0 2
;
PROC SORT;BY REP ENV I J;
PROC GLM;CLASS REP ENV HYBRID;MODEL YIELD=ENV REP(ENV)
HYBRID HYBRID*ENV;TEST H=HYBRID E=HYBRID*ENV;
LSMEANS HYBRID;
RUN;
TITLE 'DIALLEL-SAS 1';PROC GLM;CLASS REP ENV HYBRID;
MODEL YIELD=ENV REP(ENV) G1 G2 G3 G4 S11 S12 S13 S14 S22 S23 S24 S33
S34 S44 R12 R13 R14 R15 R23 R24 R25 R34 R35 R45 G1*ENV G2*ENV G3*ENV
G4*ENV S11*ENV S12*ENV S13*ENV S14*ENV S22*ENV S23*ENV S24*ENV S33*ENV
S34*ENV S44*ENV R12*ENV R13*ENV R14*ENV R15*ENV R23*ENV R24*ENV R25*ENV
R34*ENV R35*ENV R45*ENV;
%MACRO GCASCA;
CONTRAST 'GCA' G1 1,G2 1,G3 1,G4 1;
CONTRAST 'SCA' S11 1,S12 1,S13 1,S14 1,S22 1,S23 1,S24 1,S33 1,S34
1,S44 1;
ESTIMATE 'G1' G1 1;ESTIMATE 'G2' G2 1;ESTIMATE 'G3' G3 1;
ESTIMATE 'G4' G4 1;
ESTIMATE 'G5' G1 -1 G2 -1 G3 -1 G4 -1;
ESTIMATE 'S11' S11 1; ESTIMATE 'S12' S12 1; ESTIMATE 'S13' S13 1;
ESTIMATE 'S14' S14 1; ESTIMATE 'S22' S22 1; ESTIMATE 'S23' S23 1;
ESTIMATE 'S24' S24 1; ESTIMATE 'S33' S33 1; ESTIMATE 'S34' S34 1;
ESTIMATE 'S44' S44 1;
ESTIMATE 'S15' S11 -1 S12 -1 S13 -1 S14 -1;
ESTIMATE 'S25' S12 -1 S22 -1 S23 -1 S24 -1;
ESTIMATE 'S35' S13 -1 S23 -1 S33 -1 S34 -1;
ESTIMATE 'S45' S14 -1 S24 -1 S34 -1 S44 -1;
ESTIMATE 'S55' S11 1 S12 2 S13 2 S14 2 S22 1 S23 2 S24 2 S33 1 S34 2
S44 1;
%MEND GCASCA;
%GCASCA
%MACRO INTERACT;
CONTRAST 'GCA*ENV' G1*ENV 1 -1,G2*ENV 1 -1,G3*ENV 1 -1,G4*ENV 1 -1;
CONTRAST 'SCA*ENV' S11*ENV 1 -1,S12*ENV 1 -1,S13*ENV 1 -1,S14*ENV 1 -
1,S22*ENV 1 -1,S23*ENV 1 -1,S24*ENV 1 -1,S33*ENV 1 -1,S34*ENV 1 -
1,S44*ENV 1 -1;
%MEND INTERACT;
%INTERACT
CONTRAST 'REC' R12 1, R13 1, R14 1, R15 1, R23 1, R24 1, R25 1, R34 1,
R35 1, R45 1;
ESTIMATE 'R12' R12 1; ESTIMATE 'R13' R13 1; ESTIMATE 'R14' R14 1;
ESTIMATE 'R15' R15 1; ESTIMATE 'R23' R23 1; ESTIMATE 'R24' R24 1;
ESTIMATE 'R25' R25 1; ESTIMATE 'R34' R34 1; ESTIMATE 'R35' R35 1;
ESTIMATE 'R45' R45 1;
CONTRAST 'REC*ENV' R12*ENV 1 -1,R13*ENV 1 -1,R14*ENV 1 -1,R15*ENV 1 -
1,R23*ENV 1 -1,R24*ENV 1 -1,R25*ENV 1 -1,R34*ENV 1 -1,R35*ENV 1 -
1,R45*ENV 1 -1;

```

```

CONTRAST 'MAT SS' R12 1 R13 1 R14 1 R15 1,R12 -1 R23 1 R24 1 R25 1,R13
-1 R23 -1 R34 1 R35 1,R14 -1 R24 -1 R34 -1 R45 1;
ESTIMATE 'MAT1' R12 1 R13 1 R14 1 R15 1/DIVISOR=4;
ESTIMATE 'MAT2' R12 -1 R23 1 R24 1 R25 1/DIVISOR=4;
ESTIMATE 'MAT3' R13 -1 R23 -1 R34 1 R35 1/DIVISOR=4;
ESTIMATE 'MAT4' R14 -1 R24 -1 R34 -1 R45 1/DIVISOR=4;
ESTIMATE 'MAT5' R15 -1 R25 -1 R35 -1 R45 -1/DIVISOR=4;
RUN;

TITLE 'DIALLEL-SAS 2';PROC GLM;CLASS REP ENV HYBRID;
MODEL YIELD=ENV REP(ENV) G1 G2 G3 G4 S11 S12 S13 S14 S22 S23 S24 S33
S34 S44 M1 M2 M3 M4 N12 N13 N14 N23 N24 N34 G1*ENV G2*ENV G3*ENV
G4*ENV S11*ENV S12*ENV S13*ENV S14*ENV S22*ENV S23*ENV S24*ENV S33*ENV
S34*ENV S44*ENV M1*ENV M2*ENV M3*ENV M4*ENV N12*ENV N13*ENV N14*ENV
N23*ENV N24*ENV N34*ENV;
%GCASCA
%INTERACT
CONTRAST 'MAT SS' M1 1,M2 1,M3 1,M4 1;
CONTRAST 'NONM SS' N12 1,N13 1,N14 1,N23 1,N24 1,N34 1;
CONTRAST 'MAT*ENV' M1*ENV 1 -1,M2*ENV 1 -1,M3*ENV 1 -1,M4*ENV 1 -1;
CONTRAST 'NONM*ENV' N12*ENV 1 -1,N13*ENV 1 -1,N14*ENV 1 -1,N23*ENV 1 -
1,N24*ENV 1 -1,N34*ENV 1 -1;
ESTIMATE 'M1' M1 1; ESTIMATE 'M2' M2 1; ESTIMATE 'M3' M3 1;
ESTIMATE 'M4' M4 1; ESTIMATE 'M5' M1 -1 M2 -1 M3 -1 M4 -1;
ESTIMATE 'N12' N12 1; ESTIMATE 'N13' N13 1; ESTIMATE 'N14' N14 1;
ESTIMATE 'N23' N23 1; ESTIMATE 'N24' N24 1; ESTIMATE 'N34' N34 1;
ESTIMATE 'N15' N12 -1 N13 -1 N14 -1;
ESTIMATE 'N25' N12 1 N23 -1 N24 -1;
ESTIMATE 'N35' N13 1 N23 1 N34 -1;
ESTIMATE 'N45' N14 1 N24 1 N34 1;
RUN;

```

## Output

```

METHOD 1
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The GLM Procedure
Class Level Information
Class Levels Values
REP          2 1 2
ENV          2 1 2
HYBRID       25 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21
                22 23 24 25
Number of observations    100
METHOD 1
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The GLM Procedure
Dependent Variable: YIELD

Source          DF          Sum of Squares      Mean Square      F Value      Pr > F
Model           51      1655.034800          32.451663         73.03      <.0001
Error           48          21.329600           0.444367
Corrected Total 99      1676.364400

R-Square          Coeff Var      Root MSE      YIELD Mean
0.987276          4.098170       0.666608       16.26600

```



Source	DF	Type I SS	Mean Square	F Value	Pr > F
ENV	1	0.384400	0.384400	0.87	0.3570
REP (ENV)	2	9.130400	4.565200	10.27	0.0002
HYBRID	24	1631.674400	67.986433	153.00	<.0001
ENV*HYBRID	24	13.845600	0.576900	1.30	0.2171

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ENV	1	0.384400	0.384400	0.87	0.3570
REP (ENV)	2	9.130400	4.565200	10.27	0.0002
HYBRID	24	1631.674400	67.986433	153.00	<.0001
ENV*HYBRID	24	13.845600	0.576900	1.30	0.2171

Tests of Hypotheses Using the Type III MS for ENV\*HYBRID as an Error

Source	DF	Type III SS	Mean Square	F Value	Pr > F
HYBRID	24	1631.674400	67.986433	117.85	<.0001
METHOD 1					3

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The GLM Procedure

Least Squares Means

HYBRID	YIELD LSMEAN
1	11.0250000
2	11.9500000
3	14.5500000
4	9.0500000
5	13.9000000
6	12.7500000
7	16.7500000
8	19.2500000
9	10.4500000
10	17.4500000
11	10.2750000
12	15.7500000
13	17.9500000
14	22.2000000
15	19.9500000
16	12.5000000
17	13.3000000
18	14.4000000
19	20.5500000
20	18.1500000
21	21.1250000
22	21.0500000
23	20.1000000
24	21.4000000
25	20.8250000

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The GLM Procedure

Class Level Information

Class Levels Values

REP	2	1	2																					
ENV	2	1	2																					
HYBRID	25	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	
			23	24	25																			

Number of observations 100

DIALLEL-SAS 1

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The GLM Procedure

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	51	1655.034800	32.451663	73.03	<.0001
Error	48	21.329600	0.444367		
Corrected Total	99	1676.364400			

R-Square	Coeff Var	Root MSE	YIELD Mean		
0.987276	4.098170	0.666608	16.26600		
Source	DF	Type I SS	Mean Square	F Value	Pr > F
ENV	1	0.3844000	0.3844000	0.87	0.3570
REP (ENV)	2	9.1304000	4.5652000	10.27	0.0002
G1	1	887.7781250	887.7781250	1997.85	<.0001
G2	1	9.6400417	9.6400417	21.69	<.0001
G3	1	50.0520833	50.0520833	112.64	<.0001
G4	1	0.0060500	0.0060500	0.01	0.9076
S11	1	10.0806250	10.0806250	22.69	<.0001
S12	1	10.6666667	10.6666667	24.00	<.0001
S13	1	12.5563021	12.5563021	28.26	<.0001
S14	1	27.3195312	27.3195312	61.48	<.0001
S22	1	6.2084028	6.2084028	13.97	0.0005
S23	1	9.9487674	9.9487674	22.39	<.0001
S24	1	52.2200104	52.2200104	117.52	<.0001
S33	1	2.1267361	2.1267361	4.79	0.0336
S34	1	61.6333333	61.6333333	138.70	<.0001
S44	1	115.8852250	115.8852250	260.79	<.0001
R12	1	1.2800000	1.2800000	2.88	0.0961
R13	1	36.5512500	36.5512500	82.25	<.0001
R14	1	23.8050000	23.8050000	53.57	<.0001
R15	1	104.4012500	104.4012500	234.94	<.0001
R23	1	24.5000000	24.5000000	55.13	<.0001
R24	1	16.2450000	16.2450000	36.56	<.0001
R25	1	25.9200000	25.9200000	58.33	<.0001
R34	1	121.6800000	121.6800000	273.83	<.0001
R35	1	0.0450000	0.0450000	0.10	0.7517
R45	1	21.1250000	21.1250000	47.54	<.0001
G1*ENV	1	1.5401250	1.5401250	3.47	0.0688
G2*ENV	1	0.5320417	0.5320417	1.20	0.2793
G3*ENV	1	0.0700833	0.0700833	0.16	0.6930
G4*ENV	1	0.9384500	0.9384500	2.11	0.1527
S11*ENV	1	0.0756250	0.0756250	0.17	0.6818
S12*ENV	1	0.5400000	0.5400000	1.22	0.2758

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The GLM Procedure

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
S13*ENV	1	0.0567187	0.0567187	0.13	0.7225
S14*ENV	1	1.4987813	1.4987813	3.37	0.0725
S22*ENV	1	0.3500694	0.3500694	0.79	0.3792
S23*ENV	1	0.5941840	0.5941840	1.34	0.2533
S24*ENV	1	0.1575938	0.1575938	0.35	0.5543
S33*ENV	1	1.8677778	1.8677778	4.20	0.0458
S34*ENV	1	0.3307500	0.3307500	0.74	0.3926
S44*ENV	1	0.2209000	0.2209000	0.50	0.4842
R12*ENV	1	0.1250000	0.1250000	0.28	0.5983

R13*ENV	1	0.5512500	0.5512500	1.24	0.2709
R14*ENV	1	0.0200000	0.0200000	0.05	0.8329
R15*ENV	1	0.2812500	0.2812500	0.63	0.4302
R23*ENV	1	0.0450000	0.0450000	0.10	0.7517
R24*ENV	1	1.6200000	1.6200000	3.65	0.0622
R25*ENV	1	0.0000000	0.0000000	0.00	1.0000
R34*ENV	1	2.4200000	2.4200000	5.45	0.0238
R35*ENV	1	0.0050000	0.0050000	0.01	0.9160
R45*ENV	1	0.0050000	0.0050000	0.01	0.9160

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ENV	1	0.3844000	0.3844000	0.87	0.3570
REP (ENV)	2	9.1304000	4.5652000	10.27	0.0002
G1	1	595.4700500	595.4700500	1340.04	<.0001
G2	1	25.9920500	25.9920500	58.49	<.0001
G3	1	47.1906125	47.1906125	106.20	<.0001
G4	1	0.0060500	0.0060500	0.01	0.9076
S11	1	17.2432562	17.2432562	38.80	<.0001
S12	1	0.7710118	0.7710118	1.74	0.1940
S13	1	22.2103059	22.2103059	49.98	<.0001
S14	1	48.4334235	48.4334235	108.99	<.0001
S22	1	23.1842250	23.1842250	52.17	<.0001
S23	1	11.3796735	11.3796735	25.61	<.0001
S24	1	157.5091882	157.5091882	354.46	<.0001
S33	1	0.4192563	0.4192563	0.94	0.3363
S34	1	13.5576735	13.5576735	30.51	<.0001
S44	1	115.8852250	115.8852250	260.79	<.0001
R12	1	1.2800000	1.2800000	2.88	0.0961
R13	1	36.5512500	36.5512500	82.25	<.0001
R14	1	23.8050000	23.8050000	53.57	<.0001
R15	1	104.4012500	104.4012500	234.94	<.0001
R23	1	24.5000000	24.5000000	55.13	<.0001
R24	1	16.2450000	16.2450000	36.56	<.0001
R25	1	25.9200000	25.9200000	58.33	<.0001
R34	1	121.6800000	121.6800000	273.83	<.0001
R35	1	0.0450000	0.0450000	0.10	0.7517

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The GLM Procedure

Dependent Variable: YIELD

Source	DF	Type III SS	Mean Square	F Value	Pr > F
R45	1	21.1250000	21.1250000	47.54	<.0001
G1*ENV	1	2.1632000	2.1632000	4.87	0.0322
G2*ENV	1	0.2592000	0.2592000	0.58	0.4488
G3*ENV	1	0.2485125	0.2485125	0.56	0.4582
G4*ENV	1	0.9384500	0.9384500	2.11	0.1527
S11*ENV	1	0.0175563	0.0175563	0.04	0.8433
S12*ENV	1	1.2274000	1.2274000	2.76	0.1030
S13*ENV	1	0.1751059	0.1751059	0.39	0.5331
S14*ENV	1	0.5539882	0.5539882	1.25	0.2697
S22*ENV	1	0.3364000	0.3364000	0.76	0.3886
S23*ENV	1	0.0860029	0.0860029	0.19	0.6620
S24*ENV	1	0.1106941	0.1106941	0.25	0.6200
S33*ENV	1	2.2725563	2.2725563	5.11	0.0283
S34*ENV	1	0.4920029	0.4920029	1.11	0.2980
S44*ENV	1	0.2209000	0.2209000	0.50	0.4842

R12*ENV	1	0.1250000	0.1250000	0.28	0.5983
R13*ENV	1	0.5512500	0.5512500	1.24	0.2709
R14*ENV	1	0.0200000	0.0200000	0.05	0.8329
R15*ENV	1	0.2812500	0.2812500	0.63	0.4302
R23*ENV	1	0.0450000	0.0450000	0.10	0.7517
R24*ENV	1	1.6200000	1.6200000	3.65	0.0622
R25*ENV	1	0.0000000	0.0000000	0.00	1.0000
R34*ENV	1	2.4200000	2.4200000	5.45	0.0238
R35*ENV	1	0.0050000	0.0050000	0.01	0.9160
R45*ENV	1	0.0050000	0.0050000	0.01	0.9160

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
GCA	4	947.4763000	236.8690750	533.05	<.0001
SCA	10	308.6456000	30.8645600	69.46	<.0001
GCA*ENV	4	3.0807000	0.7701750	1.73	0.1581
SCA*ENV	10	5.6924000	0.5692400	1.28	0.2678
REC	10	375.5525000	37.5552500	84.51	<.0001
REC*ENV	10	5.0725000	0.5072500	1.14	0.3527
MAT SS	4	112.5565000	28.1391250	63.32	<.0001

Parameter	Estimate	Standard		t Value	Pr >  t
		Error			
G1	-3.45100000	0.09427265		-36.61	<.0001
G2	-0.72100000	0.09427265		-7.65	<.0001
G3	0.97150000	0.09427265		10.31	<.0001
G4	-0.01100000	0.09427265		-0.12	0.9076
G5	3.21150000	0.09427265		34.07	<.0001
S11	1.66100000	0.26664333		6.23	<.0001

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The GLM Procedure  
Dependent Variable: YIELD

Parameter	Estimate	Standard		t Value	Pr >  t
		Error			
S12	0.25600000	0.19434806		1.32	0.1940
S13	-1.37400000	0.19434806		-7.07	<.0001
S14	-2.02900000	0.19434806		-10.44	<.0001
S22	1.92600000	0.26664333		7.22	<.0001
S23	0.98350000	0.19434806		5.06	<.0001
S24	-3.65900000	0.19434806		-18.83	<.0001
S33	-0.25900000	0.26664333		-0.97	0.3363
S34	1.07350000	0.19434806		5.52	<.0001
S44	4.30600000	0.26664333		16.15	<.0001
S15	1.48600000	0.19434806		7.65	<.0001
S25	0.49350000	0.19434806		2.54	0.0144
S35	-0.42400000	0.19434806		-2.18	0.0341
S45	0.30850000	0.19434806		1.59	0.1190
S55	-1.86400000	0.26664333		-6.99	<.0001
R12	-0.40000000	0.23568164		-1.70	0.0961
R13	2.13750000	0.23568164		9.07	<.0001
R14	-1.72500000	0.23568164		-7.32	<.0001
R15	-3.61250000	0.23568164		-15.33	<.0001
R23	1.75000000	0.23568164		7.43	<.0001
R24	-1.42500000	0.23568164		-6.05	<.0001
R25	-1.80000000	0.23568164		-7.64	<.0001
R34	3.90000000	0.23568164		16.55	<.0001
R35	-0.07500000	0.23568164		-0.32	0.7517
R45	-1.62500000	0.23568164		-6.89	<.0001

MAT1	-0.90000000	0.11784082	-7.64	<.0001
MAT2	-0.26875000	0.11784082	-2.28	0.0271
MAT3	-0.01562500	0.11784082	-0.13	0.8951
MAT4	-0.59375000	0.11784082	-5.04	<.0001
MAT5	1.77812500	0.11784082	15.09	<.0001

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The GLM Procedure

Class Level Information

Class Levels Values

REP	2	1	2																							
ENV	2	1	2																							
HYBRID	25	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21				
			22	23	24	25																				

Number of observations 100

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The GLM Procedure

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	51	1655.034800	32.451663	73.03	<.0001
Error	48	21.329600	0.444367		
Corrected Total	99	1676.364400			

R-Square	Coeff Var	Root MSE	YIELD Mean
0.987276	4.098170	0.666608	16.26600

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ENV	1	0.3844000	0.3844000	0.87	0.3570
REP (ENV)	2	9.1304000	4.5652000	10.27	0.0002
G1	1	887.7781250	887.7781250	1997.85	<.0001
G2	1	9.6400417	9.6400417	21.69	<.0001
G3	1	50.0520833	50.0520833	112.64	<.0001
G4	1	0.0060500	0.0060500	0.01	0.9076
S11	1	10.0806250	10.0806250	22.69	<.0001
S12	1	10.6666667	10.6666667	24.00	<.0001
S13	1	12.5563021	12.5563021	28.26	<.0001
S14	1	27.3195312	27.3195312	61.48	<.0001
S22	1	6.2084028	6.2084028	13.97	0.0005
S23	1	9.9487674	9.9487674	22.39	<.0001
S24	1	52.2200104	52.2200104	117.52	<.0001
S33	1	2.1267361	2.1267361	4.79	0.0336
S34	1	61.6333333	61.6333333	138.70	<.0001
S44	1	115.8852250	115.8852250	260.79	<.0001
M1	1	91.8061250	91.8061250	206.60	<.0001
M2	1	8.5503750	8.5503750	19.24	<.0001
M3	1	0.9187500	0.9187500	2.07	0.1570
M4	1	11.2812500	11.2812500	25.39	<.0001
N12	1	5.3204167	5.3204167	11.97	0.0011
N13	1	81.2500521	81.2500521	182.84	<.0001
N14	1	7.2902812	7.2902812	16.41	0.0002
N23	1	7.2226563	7.2226563	16.25	0.0002
N24	1	4.3605104	4.3605104	9.81	0.0030
N34	1	157.5520833	157.5520833	354.55	<.0001
G1*ENV	1	1.5401250	1.5401250	3.47	0.0688
G2*ENV	1	0.5320417	0.5320417	1.20	0.2793
G3*ENV	1	0.0700833	0.0700833	0.16	0.6930
G4*ENV	1	0.9384500	0.9384500	2.11	0.1527

S11*ENV	1	0.0756250	0.0756250	0.17	0.6818
S12*ENV	1	0.5400000	0.5400000	1.22	0.2758
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The GLM Procedure  
Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
S13*ENV	1	0.0567187	0.0567187	0.13	0.7225
S14*ENV	1	1.4987813	1.4987813	3.37	0.0725
S22*ENV	1	0.3500694	0.3500694	0.79	0.3792
S23*ENV	1	0.5941840	0.5941840	1.34	0.2533
S24*ENV	1	0.1575938	0.1575938	0.35	0.5543
S33*ENV	1	1.8677778	1.8677778	4.20	0.0458
S34*ENV	1	0.3307500	0.3307500	0.74	0.3926
S44*ENV	1	0.2209000	0.2209000	0.50	0.4842
M1*ENV	1	0.2101250	0.2101250	0.47	0.4950
M2*ENV	1	0.1450417	0.1450417	0.33	0.5705
M3*ENV	1	0.0440833	0.0440833	0.10	0.7542
M4*ENV	1	0.0612500	0.0612500	0.14	0.7121
N12*ENV	1	0.2604167	0.2604167	0.59	0.4477
N13*ENV	1	0.0713021	0.0713021	0.16	0.6905
N14*ENV	1	0.0300313	0.0300313	0.07	0.7960
N23*ENV	1	0.0689062	0.0689062	0.16	0.6955
N24*ENV	1	1.1412604	1.1412604	2.57	0.1156
N34*ENV	1	3.0400833	3.0400833	6.84	0.0119

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ENV	1	0.3844000	0.3844000	0.87	0.3570
REP (ENV)	2	9.1304000	4.5652000	10.27	0.0002
G1	1	595.4700500	595.4700500	1340.04	<.0001
G2	1	25.9920500	25.9920500	58.49	<.0001
G3	1	47.1906125	47.1906125	106.20	<.0001
G4	1	0.0060500	0.0060500	0.01	0.9076
S11	1	17.2432562	17.2432562	38.80	<.0001
S12	1	0.7710118	0.7710118	1.74	0.1940
S13	1	22.2103059	22.2103059	49.98	<.0001
S14	1	48.4334235	48.4334235	108.99	<.0001
S22	1	23.1842250	23.1842250	52.17	<.0001
S23	1	11.3796735	11.3796735	25.61	<.0001
S24	1	157.5091882	157.5091882	354.46	<.0001
S33	1	0.4192563	0.4192563	0.94	0.3363
S34	1	13.5576735	13.5576735	30.51	<.0001
S44	1	115.8852250	115.8852250	260.79	<.0001
M1	1	25.9200000	25.9200000	58.33	<.0001
M2	1	2.3112500	2.3112500	5.20	0.0271
M3	1	0.0078125	0.0078125	0.02	0.8951
M4	1	11.2812500	11.2812500	25.39	<.0001
N12	1	0.1470000	0.1470000	0.33	0.5679
N13	1	107.9203333	107.9203333	242.86	<.0001
N14	1	29.2053333	29.2053333	65.72	<.0001
N23	1	50.8300833	50.8300833	114.39	<.0001
N24	1	37.8563333	37.8563333	85.19	<.0001

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The GLM Procedure  
Dependent Variable: YIELD

Source	DF	Type III SS	Mean Square	F Value	Pr > F
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N34	1	157.5520833	157.5520833	354.55	<.0001
G1*ENV	1	2.1632000	2.1632000	4.87	0.0322
G2*ENV	1	0.2592000	0.2592000	0.58	0.4488
G3*ENV	1	0.2485125	0.2485125	0.56	0.4582
G4*ENV	1	0.9384500	0.9384500	2.11	0.1527
S11*ENV	1	0.0175563	0.0175563	0.04	0.8433
S12*ENV	1	1.2274000	1.2274000	2.76	0.1030
S13*ENV	1	0.1751059	0.1751059	0.39	0.5331
S14*ENV	1	0.5539882	0.5539882	1.25	0.2697
S22*ENV	1	0.3364000	0.3364000	0.76	0.3886
S23*ENV	1	0.0860029	0.0860029	0.19	0.6620
S24*ENV	1	0.1106941	0.1106941	0.25	0.6200
S33*ENV	1	2.2725563	2.2725563	5.11	0.0283
S34*ENV	1	0.4920029	0.4920029	1.11	0.2980
S44*ENV	1	0.2209000	0.2209000	0.50	0.4842
M1*ENV	1	0.2812500	0.2812500	0.63	0.4302
M2*ENV	1	0.1250000	0.1250000	0.28	0.5983
M3*ENV	1	0.0703125	0.0703125	0.16	0.6926
M4*ENV	1	0.0612500	0.0612500	0.14	0.7121
N12*ENV	1	0.8333333	0.8333333	1.88	0.1772
N13*ENV	1	0.6750000	0.6750000	1.52	0.2238
N14*ENV	1	0.0480000	0.0480000	0.11	0.7438
N23*ENV	1	0.3520833	0.3520833	0.79	0.3778
N24*ENV	1	2.5230000	2.5230000	5.68	0.0212
N34*ENV	1	3.0400833	3.0400833	6.84	0.0119

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
GCA	4	947.4763000	236.8690750	533.05	<.0001
SCA	10	308.6456000	30.8645600	69.46	<.0001
GCA*ENV	4	3.0807000	0.7701750	1.73	0.1581
SCA*ENV	10	5.6924000	0.5692400	1.28	0.2678
MAT SS	4	112.5565000	28.1391250	63.32	<.0001
NONM SS	6	262.9960000	43.8326667	98.64	<.0001
MAT*ENV	4	0.4605000	0.1151250	0.26	0.9027
NONM*ENV	6	4.6120000	0.7686667	1.73	0.1344

Parameter	Estimate	Standard Error	t Value	Pr >  t
G1	-3.45100000	0.09427265	-36.61	<.0001
G2	-0.72100000	0.09427265	-7.65	<.0001
G3	0.97150000	0.09427265	10.31	<.0001
G4	-0.01100000	0.09427265	-0.12	0.9076
G5	3.21150000	0.09427265	34.07	<.0001

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The GLM Procedure  
Dependent Variable: YIELD

Parameter	Estimate	Standard Error	t Value	Pr >  t
S11	1.66100000	0.26664333	6.23	<.0001
S12	0.25600000	0.19434806	1.32	0.1940
S13	-1.37400000	0.19434806	-7.07	<.0001
S14	-2.02900000	0.19434806	-10.44	<.0001
S22	1.92600000	0.26664333	7.22	<.0001
S23	0.98350000	0.19434806	5.06	<.0001
S24	-3.65900000	0.19434806	-18.83	<.0001
S33	-0.25900000	0.26664333	-0.97	0.3363

S34	1.07350000	0.19434806	5.52	<.0001
S44	4.30600000	0.26664333	16.15	<.0001
S15	1.48600000	0.19434806	7.65	<.0001
S25	0.49350000	0.19434806	2.54	0.0144
S35	-0.42400000	0.19434806	-2.18	0.0341
S45	0.30850000	0.19434806	1.59	0.1190
S55	-1.86400000	0.26664333	-6.99	<.0001
M1	-0.72000000	0.09427265	-7.64	<.0001
M2	-0.21500000	0.09427265	-2.28	0.0271
M3	-0.01250000	0.09427265	-0.13	0.8951
M4	-0.47500000	0.09427265	-5.04	<.0001
M5	1.42250000	0.09427265	15.09	<.0001
N12	0.10500000	0.18255821	0.58	0.5679
N13	2.84500000	0.18255821	15.58	<.0001
N14	-1.48000000	0.18255821	-8.11	<.0001
N23	1.95250000	0.18255821	10.70	<.0001
N24	-1.68500000	0.18255821	-9.23	<.0001
N34	3.43750000	0.18255821	18.83	<.0001
N15	-1.47000000	0.18255821	-8.05	<.0001
N25	-0.16250000	0.18255821	-0.89	0.3778
N35	1.36000000	0.18255821	7.45	<.0001
N45	0.27250000	0.18255821	1.49	0.1421

### ***DIALLEL-SAS Method 2 Program Listing***

```

DATA METHOD2; TITLE 'METHOD 2';
INPUT I J REP HYBRID YIELD ENV;
DROP N NI NJ P;
P=5; *NUMBER OF PARENTAL LINES;
ARRAY GCA(N) G1 G2 G3 G4;
DO N=1 TO (P-1);
  GCA=( (I=N) - (I=P) ) + ( (J=N) - (J=P) );
END;
ARRAY SCA(N) S11 S12 S13 S14 S22 S23 S24 S33 S34 S44;
N=0;
DO NI=1 TO (P-1);
DO NJ=NI TO (P-1);
N+1;
IF NI=NJ THEN DO;
SCA=(I=NI) * ( (J=NJ) - (J=P) * 2 ) + (I=P) * (J=P); END;
ELSE DO;
SCA=(I=NI) * (J=NJ) - (J=P) * ( (I=NI) + (I=NJ) - (I=P) );
END; END; END;
CARDS;

```

[Your data here]

```

;
PROC SORT; BY REP ENV I J;
PROC GLM; CLASS REP ENV HYBRID; MODEL YIELD=ENV REP(ENV)
HYBRID HYBRID*ENV; TEST H=HYBRID E=HYBRID*ENV;
LSMEANS HYBRID;
PROC GLM; CLASS REP ENV HYBRID;
MODEL YIELD=ENV REP(ENV) G1 G2 G3 G4 S11 S12 S13 S14 S22 S23 S24 S33

```



```

S34 S44 G1*ENV G2*ENV G3*ENV G4*ENV S11*ENV S12*ENV S13*ENV S14*ENV
S22*ENV S23*ENV S24*ENV S33*ENV S34*ENV S44*ENV;
CONTRAST 'GCA' G1 1,G2 1,G3 1,G4 1;
CONTRAST 'SCA' S11 1,S12 1,S13 1,S14 1,S22 1,S23 1,S24 1,S33 1,S34 1,
      S44 1;
ESTIMATE 'G1' G1 1;ESTIMATE 'G2' G2 1;ESTIMATE 'G3' G3 1;
ESTIMATE 'G4' G4 1;
ESTIMATE 'G5' G1 -1 G2 -1 G3 -1 G4 -1;
ESTIMATE 'S11' S11 1; ESTIMATE 'S12' S12 1; ESTIMATE 'S13' S13 1;
ESTIMATE 'S14' S14 1; ESTIMATE 'S22' S22 1; ESTIMATE 'S23' S23 1;
ESTIMATE 'S24' S24 1; ESTIMATE 'S33' S33 1; ESTIMATE 'S34' S34 1;
ESTIMATE 'S44' S44 1;
ESTIMATE 'S15' S11 -1 S12 -1 S13 -1 S14 -1;
ESTIMATE 'S25' S12 -1 S22 -1 S23 -1 S24 -1;
ESTIMATE 'S35' S13 -1 S23 -1 S33 -1 S34 -1;
ESTIMATE 'S45' S14 -1 S24 -1 S34 -1 S44 -1;
ESTIMATE 'S55' S11 1 S12 2 S13 2 S14 2 S22 1 S23 2 S24 2 S33 1 S34 2
      S44 1;
CONTRAST 'GCA*ENV' G1*ENV 1 -1,G2*ENV 1 -1,G3*ENV 1 -1,G4*ENV 1 -1;
CONTRAST 'SCA*ENV' S11*ENV 1 -1,S12*ENV 1 -1,S13*ENV 1 -1,S14*ENV 1 -
      1, S22*ENV 1 -1,S23*ENV 1 -1,S24*ENV 1 -1,S33*ENV 1 -1, S34*ENV 1
      -1,S44*ENV 1 -1;
RUN;

```

### ***DIALLEL Method 3 Program Listing***

```

TITLE 'METHOD 3';
DATA METHOD3;
INPUT I J REP HYBRID YIELD ENV;
DROP N NI NJ P;
P=5;*NUMBER OF PARENTAL LINES;
ARRAY GCA(N) G1 G2 G3 G4;
DO N=1 TO (P-1);
GCA=((I=N)-(I=P))+((J=N)-(J=P));
END;
ARRAY SCA(N) S12 S13 S14 S23 S24;
N=0;
DO NI=1 TO (P-3);
DO NJ=NI+1 TO (P-1);
N+1;
SCA=(I=NI)*(J=NJ)-((I=NI)+(I=NJ))*(J=P)+(J=NI)*(I=NJ)
-(I=P)*((J=NI)+(J=NJ));
IF ((I>=(P-2))&(J>=(P-1)))|((I>=(P-1))&(J>=(P-2))) THEN DO;
SCA=- (I=(P-2))*(J=(P-1))+(I>=(P-2))*(J=P)*(I NE NJ)-(J=(P-2))*(I=(P-
1))+(J>=(P-2))*(I=P)*(J NE NJ);
END;END;END;
ARRAY REC(N) R12 R13 R14 R15 R23 R24 R25 R34 R35 R45;
N=0;
DO NI=1 TO (P-1);
DO NJ=(NI+1) TO P;
N+1;
REC=(I=NI)*(J=NJ)-(J=NI)*(I=NJ);
END;END;
ARRAY MAT(N) M1 M2 M3 M4;
DO N=1 TO (P-1);

```

```

MAT=(I=N)+(J=P)-(J=N)-(I=P);
END;
ARRAY NONM(N) N12 N13 N14 N23 N24 N34;
N=0;
DO NI=1 TO (P-2);
DO NJ=(NI+1) TO (P-1);
N+1;
NONM=((I=NI)*(J=NJ))-(I=NJ)*(J=NI)+((I=NJ)-(I=NI))*(J=P)
+((I=P)*(J=NI)-(J=NJ));
END;END;
CARDS;

```

[Your data here]

```

;
PROC SORT;BY ENV REP I J;
PROC GLM;CLASS REP ENV HYBRID;MODEL YIELD=ENV REP(ENV) HYBRID
ENV*HYBRID;TEST H=HYBRID E=ENV*HYBRID;TEST H=ENV E=REP(ENV);
LSMEANS HYBRID;RUN;
TITLE 'DIALLEL-SAS 1';
PROC GLM;CLASS REP HYBRID ENV;
MODEL YIELD=ENV REP(ENV) G1 G2 G3 G4 S12 S13 S14 S23 S24 R12
R13 R14 R15 R23 R24 R25 R34 R35 R45 G1*ENV G2*ENV G3*ENV G4*ENV
S12*ENV S13*ENV S14*ENV S23*ENV S24*ENV R12*ENV R13*ENV R14*ENV
R15*ENV R23*ENV R24*ENV R25*ENV R34*ENV R35*ENV R45*ENV;
%MACRO GCASCA;
CONTRAST 'GCA' G1 1,G2 1,G3 1,G4 1;
CONTRAST 'SCA' S12 1,S13 1,S14 1,S23 1,S24 1;
ESTIMATE 'G1' G1 1;ESTIMATE 'G2' G2 1;ESTIMATE 'G3' G3 1;
ESTIMATE 'G4' G4 1;
ESTIMATE 'G5' G1 -1 G2 -1 G3 -1 G4 -1;
ESTIMATE 'S12' S12 1; ESTIMATE 'S13' S13 1; ESTIMATE 'S14' S14 1;
ESTIMATE 'S23' S23 1; ESTIMATE 'S24' S24 1;
ESTIMATE 'S15' S12 -1 S13 -1 S14 -1;ESTIMATE 'S25' S12 -1 S23 -1 S24 -
1;
ESTIMATE 'S34' S12 -1 S13 -1 S14 -1 S23 -1 S24 -1;
ESTIMATE 'S35' S12 1 S14 1 S24 1;ESTIMATE 'S45' S12 1 S13 1 S23 1;
%MEND GCASCA;
%GCASCA
CONTRAST 'REC' R12 1,R13 1,R14 1,R15 1,R23 1,R24 1,R25 1,R34 1,R35 1,
R45 1;
ESTIMATE 'R12' R12 1; ESTIMATE 'R13' R13 1; ESTIMATE 'R14' R14 1;
ESTIMATE 'R15' R15 1; ESTIMATE 'R23' R23 1; ESTIMATE 'R24' R24 1;
ESTIMATE 'R25' R25 1; ESTIMATE 'R34' R34 1; ESTIMATE 'R35' R35 1;
ESTIMATE 'R45' R45 1;
CONTRAST 'MAT SS' R12 1 R13 1 R14 1 R15 1,R12 -1 R23 1 R24 1 R25 1,
R13 -1 R23 -1 R34 1 R35 1,R14 -1 R24 -1 R34 -1 R45 1;
ESTIMATE 'MAT1' R12 1 R13 1 R14 1 R15 1/DIVISOR=4;
ESTIMATE 'MAT2' R12 -1 R23 1 R24 1 R25 1/DIVISOR=4;
ESTIMATE 'MAT3' R13 -1 R23 -1 R34 1 R35 1/DIVISOR=4;
ESTIMATE 'MAT4' R14 -1 R24 -1 R34 -1 R45 1/DIVISOR=4;
ESTIMATE 'MAT5' R15 -1 R25 -1 R35 -1 R45 -1/DIVISOR=4;
%MACRO INTERACT;
CONTRAST 'GCA*ENV' G1*ENV 1 -1,G2*ENV 1 -1,G3*ENV 1 -1,G4*ENV 1 -1;
CONTRAST 'SCA*ENV' S12*ENV 1 -1,S13*ENV 1 -1,S14*ENV 1 -1, S23*ENV 1 -
1,S24*ENV 1 -1;

```

```

%MEND INTERACT;
%INTERACT
CONTRAST 'REC*ENV' R12*ENV 1 -1,R13*ENV 1 -1,R14*ENV 1 -1, R15*ENV 1
-1,R23*ENV 1 -1,R24*ENV 1 -1, R25*ENV 1 -1,R34*ENV 1 -1,R35*ENV 1
-1, R35*ENV 1 -1,R45*ENV 1 -1;
RUN;
TITLE 'DIALLEL-SAS 2';
PROC GLM;CLASS REP HYBRID ENV;
MODEL YIELD=ENV REP(ENV) G1 G2 G3 G4 S12 S13 S14 S23 S24 M1 M2 M3
M4 N12 N13 N14 N23 N24 N34 G1*ENV G2*ENV G3*ENV G4*ENV
S12*ENV S13*ENV S14*ENV S23*ENV S24*ENV M1*ENV M2*ENV M3*ENV
M4*ENV N12*ENV N13*ENV N14*ENV N23*ENV N24*ENV N34*ENV;
%GCASCA
%INTERACT
CONTRAST 'MAT' M1 1,M2 1,M3 1,M4 1;
CONTRAST 'NONM' N12 1,N13 1,N14 1,N23 1,N24 1,N34 1;
ESTIMATE 'M1' M1 1; ESTIMATE 'M2' M2 1; ESTIMATE 'M3' M3 1;
ESTIMATE 'M4' M4 1; ESTIMATE 'M5' M1 -1 M2 -1 M3 -1 M4 -1;
ESTIMATE 'N12' N12 1;ESTIMATE 'N13' N13 1;ESTIMATE 'N14' N14 1;
ESTIMATE 'N23' N23 1;ESTIMATE 'N24' N24 1;ESTIMATE 'N34' N34 1;
ESTIMATE 'N15' N12 -1 N13 -1 N14 -1;
ESTIMATE 'N25' N12 1 N23 -1 N24 -1;
ESTIMATE 'N35' N13 1 N23 1 N34 -1;
ESTIMATE 'N45' N14 1 N24 1 N34 1;
CONTRAST 'MAT*ENV' M1*ENV 1 -1,M2*ENV 1 -1,M3*ENV 1 -1, M4*ENV 1 -1;
CONTRAST 'NONM*ENV' N12*ENV 1 -1,N13*ENV 1 -1,N14*ENV 1 -1, N23*ENV 1
-1,N24*ENV 1 -1,N34*ENV 1 -1;
RUN;

```

### ***DIALLEL Method 4 Program Listing***

```

DATA METHOD4;TITLE 'METHOD 4';
INPUT I J REP HYBRID YIELD ENV;
DROP N NI NJ P;
P=5;*NUMBER OF PARENTAL LINES;
ARRAY GCA(N) G1 G2 G3 G4;
DO N=1 TO (P-1);
GCA=((I=N)-(I=P))+((J=N)-(J=P));
END;
ARRAY SCA(N) S12 S13 S14 S23 S24;
N=0;
DO NI=1 TO (P-3);
DO NJ=NI+1 TO (P-1);
N+1;
SCA=(I=NI)*(J=NJ)-((I=NI)+(I=NJ))*(J=P);
IF ((I>=(P-2)) & (J>=(P-1))) | ((I>=(P-1)) & (J>=(P-2))) THEN DO;
SCA=- (I=(P-2))*(J=(P-1))+(I>=(P-2))*(J=P)*(I NE NJ);
END;END;END;
CARDS;

```

[Your data here]

```

;
PROC SORT;BY REP ENV I J;

```

```

PROC GLM;CLASS REP ENV HYBRID;MODEL YIELD=ENV REP(ENV) HYBRID
      HYBRID*ENV;TEST H=HYBRID E=HYBRID*ENV; LSMEANS HYBRID;
PROC GLM;CLASS REP ENV HYBRID;
MODEL YIELD=ENV REP(ENV) G1 G2 G3 G4 S12 S13 S14 S23 S24
G1*ENV G2*ENV G3*ENV G4*ENV S12*ENV S13*ENV S14*ENV S23*ENV S24*ENV;

CONTRAST 'GCA' G1 1,G2 1,G3 1,G4 1;
CONTRAST 'SCA' S12 1,S13 1,S14 1,S23 1,S24 1;
CONTRAST 'GCA*ENV' G1*ENV 1 -1,G2*ENV 1 -1,G3*ENV 1 -1,G4*ENV 1 -1;
CONTRAST 'SCA*ENV' S12*ENV 1 -1,S13*ENV 1 -1,S14*ENV 1 -1,S23*ENV 1 -
      1,S24*ENV 1 -1;
ESTIMATE 'G1' G1 1;ESTIMATE 'G2' G2 1;ESTIMATE 'G3' G3 1;
ESTIMATE 'G4' G4 1;
ESTIMATE 'G5' G1 -1 G2 -1 G3 -1 G4 -1;
ESTIMATE 'S12' S12 1; ESTIMATE 'S13' S13 1; ESTIMATE 'S14' S14 1;
ESTIMATE 'S23' S23 1; ESTIMATE 'S24' S24 1;
ESTIMATE 'S15' S12 -1 S13 -1 S14 -1;
ESTIMATE 'S25' S12 -1 S23 -1 S24 -1;
ESTIMATE 'S34' S12 -1 S13 -1 S14 -1 S23 -1 S24 -1;
ESTIMATE 'S35' S12 1 S14 1 S24 1;
ESTIMATE 'S45' S12 1 S13 1 S23 1;
RUN;

```

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## Chapter 2

# Diallel Analysis for a Seed and Endosperm Model with Genotype-by-Environment Interaction Effects

Jun Zhu

### *Purpose*

To analyze balanced or unbalanced data of diploid seed and triploid endosperm models for estimating components of variance, covariance, heritability, and selection response.

### *Definitions*

#### *Mating Design*

A set of inbred lines are sampled from a reference population. These parents are used to produce  $F_1$  and  $F_2$  seeds. Experiments with parents,  $F_1$ s, and  $F_2$ s are conducted in multiple environments using a randomized complete-block design.

#### *Genetic Model*

The genetic model for genetic entry of the  $k$ th type of generation derived from parents  $i$  and  $j$  in the  $l$ th block within the  $h$ th environment is

$$y_{ijkl} = \mu + E_h + G_{ijk} + GE_{hijk} + B_{hl} + e_{ijkl}$$

where  $\mu$  = population mean,  $E_h$  = environment effect,  $G_{ijk}$  = total genotypic effect,  $GE_{hijk}$  = genotype  $\times$  environment interaction effect,  $B_{hl}$  = block effect, and  $e_{hijkl}$  = residual effect.

Genetic partitioning for the diploid seed model (Zhu and Weir, 1994a; Zhu, 1996):

For parent ( $P_i, k = 0$ ):

$$G_{ii0} \quad GE_{hii0} \quad 2A_i \quad D_{ii} \quad C_i \quad 2Am_i \quad Dm_{ii} \quad 2AE_{hi} \quad DE_{hiii} \quad CE_{hi} \\ 2AmE_{hi} \quad DmE_{hii}$$

For  $F_1$  ( $P_i \times P_j, k = 1$ ):

$$G_{ij1} \quad GE_{hij2} \quad A_i \quad A_j \quad D_{ij} \quad C_i \quad 2Am_i \quad Dm_{ii} \quad AE_{hi} \quad AE_{hj} \quad DE_{hij} \\ CE_{hi} \quad 2AmE_{hi} \quad DmB_{hii}$$

For  $F_2$  ( $F_1 \otimes, k = 2$ ):

$$G_{ij2} \quad GE_{hij2} \quad A_i \quad A_j \quad \frac{1}{4}D_{ii} \quad \frac{1}{4}D_{jj} \quad \frac{1}{2}D_{ij} \quad C_i \quad Am_i \quad Am_j \quad Dm_{ij} \\ AE_{hi} \quad AE_{hj} \quad \frac{1}{4}DE_{hii} \quad \frac{1}{4}DE_{hjj} \quad \frac{1}{2}DE_{hij} \quad CE_{hi} \\ AmE_{hi} \quad AmE_{hj} \quad DmE_{hij}$$

Genetic partitioning for triploid endosperm model (Zhu and Weir, 1994b; Zhu, 1996):

For parent ( $P_i, k = 0$ ):

$$G_{ii0} \quad GE_{hii0} \quad 3A_i \quad 3D_{ii} \quad C_i \quad 2Am_i \quad Dm_{ii} \quad 3AE_{hi} \quad 3DE_{hii} \quad CE_{hi} \\ 2AmE_{hi} \quad DmE_{hii}$$

For  $F_1$  ( $P_i \times P_j, k = 1$ ):

$$G_{ij1} \quad GE_{hij1} \quad 2A_i \quad A_j \quad D_{ii} \quad 2D_{ij} \quad C_i \quad 2Am_i \quad Dm_{ii} \quad 2AE_{hi} \\ AE_{hj} \quad DE_{hii} \quad 2DE_{hij} \quad CE_{hi} \quad 2AmE_{hi} \quad DmE_{hii}$$

For  $F_2$  ( $F_1 \otimes$ ,  $k = 2$ ):

$$G_{ij2} \quad GE_{hij2} \quad \frac{1}{2}A_i \quad \frac{1}{2}A_j \quad D_{ii} \quad D_{jj} \quad D_{ij} \quad C_i \quad Am_i \quad Am_j \quad Dm_{ij} \\ \frac{1}{2}AE_{hi} \quad \frac{1}{2}AE_{hj} \quad DE_{hii} \quad DE_{hjj} \quad DE_{hij} \quad CE_{hi} \\ AmE_{hi} \quad AmE_{hj} \quad DmE_{hij}$$

where  $A$  = direct additive effect,  $D$  = direct dominance effect,  $C$  = cytoplasm effect,  $Am$  = maternal additive effect,  $Dm$  = maternal dominance effect,  $AE$  = direct additive by environment interaction effect,  $DE$  = direct dominance by environment interaction effect,  $CE$  = cytoplasm by environment interaction effect,  $AmE$  = maternal additive by environment interaction effect,  $DmE$  = maternal dominance by environment interaction effect.

Other generations, such as  $BC_1$ s and  $BC_2$ s and their reciprocals ( $RBC_1$ s and  $RBC_2$ s) can also be used for analyzing seed traits (Zhu and Weir, 1994a; Zhu, 1996).

### Analysis Methodology

#### Mixed Linear Model

The phenotypic mean of the seed genetic model can be expressed by a mixed linear model as

$$y \quad Xb \quad U_A e_A \quad U_D e_D \quad U_C e_C \quad U_{Am} e_{Am} \quad U_{Dm} e_{Dm} \quad U_{AE} e_{AE} \quad U_{DE} e_{DE} \\ U_{CE} e_{CE} \quad U_{AmE} e_{AmE} \quad U_{DmE} e_{DmE} \quad U_B e_B \quad e_e \\ Xb \quad U_u e_u \\ u$$

with variance-covariance matrix

$$\text{var}(y) \quad \sigma_A^2 V_1 \quad \sigma_D^2 V_2 \quad \sigma_C^2 V_3 \quad \sigma_{Am}^2 V_4 \quad \sigma_{Dm}^2 V_5 \quad \sigma_{AE}^2 V_6 \quad \sigma_{DE}^2 V_7 \\ \sigma_{CE}^2 V_8 \quad \sigma_{AmE}^2 V_9 \quad \sigma_{DmE}^2 V_{10} \quad \sigma_B^2 V_{11} \quad \sigma_{A.Am} V_{12} \quad \sigma_{D.Dm} V_{13} \\ \sigma_{AE.AmE} V_{14} \quad \sigma_{DE.DmE} V_{15} \quad \sigma_e^2 V_{16} \\ u \quad V_u \\ u \quad 1$$

where  $V_u = U_u U_u^T$  ( $u = 1, 2, \dots, 11$ ),  $V_{12} = U_1 U_4^T = U_4 U_1^T$ ,  $V_{13} = U_2 U_5^T = U_5 U_2^T$ ,  $V_{14} = U_6 U_9^T = U_9 U_6^T$ ,  $V_{15} = U_7 U_{10}^T = U_{10} U_7^T$ ,  $V_{16} = I$ .



*Variance Components*

Unbiased estimation of variances and covariances of the same trait can be obtained by the following MINQUE(0/1) equations (Zhu, 1992; Zhu and Weir, 1994a):

$$\text{tr } Q_{0/1} V_u Q_{0/1} V_v \hat{u} = y^T Q_{0/1} V_u Q_{0/1} y$$

where

$$Q_{0/1} = V_{0/1}^{-1} - V_{0/1}^{-1} X X^T V_{0/1}^{-1} X X^T V_{0/1}^{-1} X X^T V_{0/1}^{-1}$$

$$V_{0/1} = \sum_{u=1}^{11} U_u U_u^T I$$

For diploid seed of  $F_2$ , genetic variance and covariance components can be obtained by  $V_A = 2\sigma_A^2$ ,  $V_D = \frac{3}{8}\sigma_D^2$ ,  $V_C = \sigma_C^2$ ,  $V_{Am} = 2\sigma_{Am}^2$ ,  $V_{Dm} = \sigma_{Dm}^2$ ,  $V_{AE} = 2\sigma_{AE}^2$ ,  $V_{DE} = \frac{3}{8}\sigma_{DE}^2$ ,  $V_{CE} = \sigma_{CE}^2$ ,  $V_{AmE} = 2\sigma_{AmE}^2$ ,  $V_{DmE} = \sigma_{DmE}^2$ ,  $V_e = \sigma_e^2$ ,  $C_{A.Am} = 2\sigma_{A.Am}$ ,  $C_{D.Dm} = \frac{1}{2}\sigma_{D.Dm}$ ,  $C_{AE.AmE} = 2\sigma_{AE.AmE}$ ,  $C_{DE.DmE} = \frac{1}{2}\sigma_{DE.DmE}$ .

For triploid endosperm of  $F_2$ , genetic variance and covariance components can be obtained by  $V_A = 4\frac{1}{2}\sigma^2$ ,  $V_D = 3\sigma_D^2$ ,  $V_C = \sigma_C^2$ ,  $V_{AM} = 2\sigma_{Am}^2$ ,  $V_{Dm} = \sigma_{Dm}^2$ ,  $V_{AE} = 4\frac{1}{2}\sigma_{AE}^2$ ,  $V_{DE} = 3\sigma_{DE}^2$ ,  $V_{CE} = \sigma_{CE}^2$ ,  $V_{AmE} = 2\sigma_{AmE}^2$ ,  $V_{DmE} = \sigma_{DmE}^2$ ,  $V_e = \sigma_e^2$ ,  $C_{A.Am} = 3\sigma_{A.Am}$ ,  $C_{D.Dm} = \sigma_{D.Dm}$ ,  $C_{AE.AmE} = 3\sigma_{AE.AmE}$ ,  $C_{DE.DmE} = \sigma_{DE.DmE}$ .

The total phenotypic variance is  $V_P = V_A + V_D + V_C + V_{Am} + V_{Dm} + V_{AE} + V_{DE} + V_{CE} + V_{AmE} + V_{DmE} + 2C_{A.Am} + 2C_{D.Dm} + 2C_{AE.AmE} + 2C_{DE.DmE} + V_e$ , where  $C_{A.Am}$  and  $C_{D.Dm}$  are the covariances between direct effects ( $A$  and  $D$ ) and maternal effects ( $Am$  and  $Dm$ ) of the same trait,  $C_{AE.AmE}$  and  $C_{DE.DmE}$  are the covariances between direct by environment interaction effect ( $AE$  and  $DE$ ) and maternal by environment interaction effect ( $AmE$  and  $DmE$ ) of the same trait.

*Covariance Components and Correlation*

Unbiased estimation of covariances between two traits ( $y_1$  and  $y_2$ ) can be obtained by MINQUE(0/1) approaches (Zhu, 1992; Zhu and Weir, 1994a).

$$tr \mathbf{Q}_{0/1} \mathbf{V}_u \mathbf{Q}_{0/1} \mathbf{V}_v \hat{u/u} = y_1^T \mathbf{Q}_{0/1} \mathbf{V}_u \mathbf{Q}_{0/1} y_2$$

For diploid seed of  $F_2$ , genetic covariance components can be obtained by  $C_A$   $2\sigma_{A/A}$ ,  $C_D$   $\frac{3}{8}\sigma_{D/D}$ ,  $C_C$   $\sigma_{C/C}$ ,  $C_{Am}$   $2\sigma_{Am/Am}$ ,  $C_{Dm}$   $\sigma_{D/D}$ ,  $C_{AE}$   $2\sigma_{AE/AE}$ ,  $C_{DE}$   $\frac{3}{8}\sigma_{DE/DE}$ ,  $C_{CE}$   $\sigma_{CE/CE}$ ,  $C_{AmE}$   $2\sigma_{AmE/AmE}$ ,  $C_{DmE}$   $\sigma_{DE/DE}$ ,  $C_e$   $\sigma_{e/e}$ ,  $C_{A/Am}$   $2\sigma_{A/Am}$ ,  $C_{D/Dm}$   $\frac{1}{2}\sigma_{D/Dm}$ ,  $C_{AE/AmE}$   $2\sigma_{AE/AmE}$ ,  $C_{DE/DmE}$   $\frac{1}{2}\sigma_{DE/DmE}$ .

For triploid endosperm of  $F_2$ , genetic covariance components can be obtained by  $C_A$   $4\frac{1}{2}\sigma_{A/A}$ ,  $C_D$   $3\sigma_{D/D}$ ,  $C_C$   $\sigma_{C/C}$ ,  $C_{Am}$   $2\sigma_{Am/Am}$ ,  $C_{Dm}$   $\sigma_{D/D}$ ,  $C_{AE}$   $4\frac{1}{2}\sigma_{AE/AE}$ ,  $C_{DE}$   $3\sigma_{DE/DE}$ ,  $C_{CE}$   $\sigma_{CE/CE}$ ,  $C_{AmE}$   $2\sigma_{AmE/AmE}$ ,  $C_{DmE}$   $\sigma_{DE/DE}$ ,  $C_e$   $\sigma_{e/e}$ ,  $C_{A/Am}$   $3\sigma_{A/Am}$ ,  $C_{D/Dm}$   $\sigma_{D/Dm}$ ,  $C_{AE/AmE}$   $3\sigma_{AE/AmE}$ ,  $C_{DE/DmE}$   $\sigma_{DE/DmE}$ .

The total phenotypic covariance is  $C_P = C_A + C_D + C_C + C_{Am} + C_{Dm} + C_{AE} + C_{DE} + C_{CE} + C_{AmE} + C_{DmE} + 2C_{A/Am} + 2C_{D/Dm} + 2C_{AE/AmE} + 2C_{DE/DmE} + C_e$ . For trait 1 and trait 2, correlation coefficients of genetic components can be estimated by  $r_A$   $C_A / \sqrt{V_{A(1)}V_{A(2)}}$ ,  $r_D$   $C_D / \sqrt{V_{D(1)}V_{D(2)}}$ ,  $r_C$   $C_C / \sqrt{V_{C(1)}V_{C(2)}}$ ,  $r_{Am}$   $C_{Am} / \sqrt{V_{Am(1)}V_{Am(2)}}$ ,  $r_{Dm}$   $C_{Dm} / \sqrt{V_{Dm(1)}V_{Dm(2)}}$ ,  $r_{AE}$   $C_{AE} / \sqrt{V_{AE(1)}V_{AE(2)}}$ ,  $r_{DE}$   $C_{DE} / \sqrt{V_{DE(1)}V_{DE(2)}}$ ,  $r_{CE}$   $C_{CE} / \sqrt{V_{CE(1)}V_{CE(2)}}$ ,  $r_{AmE}$   $C_{AmE} / \sqrt{V_{AmE(1)}V_{AmE(2)}}$ ,  $r_{DmE}$   $C_{DmE} / \sqrt{V_{DmE(1)}V_{DmE(2)}}$ ,  $r_e$   $C_e / \sqrt{V_{e(1)}V_{e(2)}}$ .

### Heritability Components

The total heritability ( $h^2$ ) can be partitioned into general heritability ( $h_G^2$ ) and interaction heritability ( $h_{GE}^2$ ) with their components (Zhu, 1997),

$$h^2 = h_G^2 + h_{GE}^2$$

$$h_G^2 = h_O^2 + h_C^2 + h_M^2 + h_{OE}^2 + h_{CE}^2 + h_{ME}^2$$

where  $h_O^2 = V_A / V_P$  is direct general heritability,  $h_C^2 = V_C / V_P$  is cytoplasm general heritability, and  $h_M^2 = V_{Am} / V_P$  is maternal general heritability;  $h_{OE}^2 = V_{AE} / V_P$  is direct interaction heritability,  $h_{CE}^2 = V_{CE} / V_P$  is cytoplasm interaction heritability, and  $h_{ME}^2 = V_{AmE} / V_P$  is maternal interaction heritability.

### Selection Response

The total selection response ( $R = ih^2\sqrt{V_P}$ ) can be partitioned into several components (Zhu, 1997):

$$R = R_G + R_{GE} + R_O + R_C + R_M + R_{OE} + R_{CE} + R_{ME}$$

where  $R_G = ih_G^2\sqrt{V_P}$  is general response, which consists of direct general response ( $R_O = ih_O^2\sqrt{V_P}$ ), cytoplasm general response ( $R_C = ih_C^2\sqrt{V_P}$ ), and maternal general response ( $R_M = ih_M^2\sqrt{V_P}$ );  $R_{GE} = ih_{GE}^2\sqrt{V_P}$  is interaction response, which consists of direct interaction response ( $R_{OE} = ih_{OE}^2\sqrt{V_P}$ ), cytoplasm interaction response ( $R_{CE} = ih_{CE}^2\sqrt{V_P}$ ), and maternal interaction response ( $R_{ME} = ih_{ME}^2\sqrt{V_P}$ ).

### Heterosis Components

Prediction of genetic merits can be obtained using the linear unbiased prediction (LUP) method (Zhu, 1992; Zhu and Weir, 1996) or the adjusted unbiased prediction (AUP) method (Zhu, 1993a; Zhu and Weir, 1996). Predicted genotypic effects and  $GE$  interaction effects can be further used in analyzing heterosis of different generations (Zhu, 1997). Heterosis in specific environments consists of two components. General heterosis is due to genotypic effects and can be expected in overall environments, and interaction heterosis is a deviant of  $GE$  interaction relative to specific environments. The two components of heterosis relative to midparent or female parent can be calculated as ( $x = 1$  for diploid seed and  $x = 2$  for triploid endosperm):

General heterosis of  $F_n$  relative to midparent:

$$H_M = F_n \left[ \frac{H_{MO}}{2} + \frac{H_{MC}}{2} + \frac{H_{MM}}{2} \right]^{n-x}$$

Interaction heterosis of  $F_n$  relative to midparent:

$$H_{ME} F_n \quad H_{MOE} \quad H_{MCE} \quad H_{MME}$$

$$\frac{1}{2} \quad n^{-x} \quad OE \quad \frac{1}{2} \quad CE \quad \frac{1}{2} \quad n^{-2} \quad ME$$

General heterosis of  $F_n$  relative to female parent ( $P_i$ ):

$$H_F F_n \quad H_{FO} \quad H_{FM}$$

$$\frac{1}{2} \quad n^{-x} \quad O \quad -\frac{1}{2} \quad O \quad \frac{1}{2} \quad n^{-2} \quad M \quad -\frac{1}{2} \quad M$$

Interaction heterosis of  $F_n$  relative to female parent ( $P_i$ ):

$$H_{FE} F_n \quad H_{FOE} \quad H_{FME}$$

$$\frac{1}{2} \quad n^{-x} \quad OE \quad -\frac{1}{2} \quad OE \quad \frac{1}{2} \quad n^{-2} \quad ME \quad -\frac{1}{2} \quad ME$$

where  $O = D_{ij} - \frac{1}{2} D_{ii} - \frac{1}{2} D_{jj}$ ,  $M = Dm_{ij} - \frac{1}{2} Dm_{ii} - \frac{1}{2} Dm_{jj}$ ,  $OE = DE_{hij} - \frac{1}{2} DE_{hii} - \frac{1}{2} DE_{hjj}$ ,  $ME = DmE_{hij} - \frac{1}{2} DmE_{hii} - \frac{1}{2} DmE_{hjj}$ ,  $O = 2 A_i - A_j - D_{ii} - D_{jj}$  for diploid and  $O = 3 A_i - A_j - 3 D_{ii} - D_{jj}$  for triploid endosperm,  $C = C_i - C_j$ ,  $M = 2 Am_i - Am_j - Dm_{ii} - Dm_{jj}$ .

Heterosis based on population mean ( $H_{PM} = \frac{1}{\mu} H_M$ ,  $H_{PME} = \frac{1}{\mu} H_{ME}$ ,  $H_{PF} = \frac{1}{\mu} H_F$ , or  $H_{PFE} = \frac{1}{\mu} H_{FE}$ ) can be used to compare proportion of heterosis among different traits.

### Covariances Between Seed Quality Trait and Plant Agronomic Trait

In plant breeding, breeders usually want to improve seed quality traits while keeping the genetic merit of yield traits. Therefore, understanding the genetic relationship between seed quality traits and plant yield traits is of importance. Seed models and plant models have unequal design matrices. Zhu (1993b) developed a new method for estimating genetic covariance components between seed traits ( $\mathbf{y}_s$ ) and plant traits ( $\mathbf{y}_p$ ). For seed model:

$$y_s = Xb_{(S)} + U_A e_{A(S)} + U_D e_{D(S)} + U_C e_{C(S)} + U_{Am} e_{Am(S)} + U_{Dm} e_{Dm(S)} + U_{AE} e_{AE(S)} + U_{DE} e_{DE(S)} + U_{CE} e_{CE(S)} + U_{AmE} e_{AmE(S)} + U_{DmE} e_{DmE(S)} + U_B e_{B(S)} + e_{e(S)}$$

$$Xb_{(S)} = U_u e_{u(S)}$$

The corresponding plants bearing the seeds will have the following mixed linear model:

$$\begin{array}{r}
 y_p \\
 \begin{array}{r}
 Xb_{(P)} \\
 U_{CE}e_{CE(P)} \\
 U_Be_{B(P)} \\
 Xb_{(P)} \\
 \end{array} \\
 \begin{array}{r}
 U_Ce_{C(P)} \\
 U_{AmE}e_{AmE(P)} \\
 e_{e(P)} \\
 U_u e_{u(P)} \\
 \end{array} \\
 \begin{array}{r}
 U_{Am}e_{Am(P)} \\
 U_{DmE}e_{DmE(P)} \\
 \\
 U_u e_{u(P)} \\
 \end{array} \\
 \begin{array}{r}
 U_{Dm}e_{Dm(P)} \\
 \\
 \\
 U_u e_{u(P)} \\
 \end{array} \\
 \end{array}$$

There are covariances between random factors of seed traits and those of plant traits:  $\sigma_{A/Am}$  = covariance between seed direct additive effects and plant additive effects,  $\sigma_{D/Dm}$  = covariance between seed direct dominance effects and plant dominance effects,  $\sigma_{C/C}$  = covariance between seed cytoplasm effects and plant cytoplasm effects,  $\sigma_{Am/Am}$  = covariance between seed maternal additive effects and plant additive effects,  $\sigma_{Dm/Dm}$  = covariance between seed maternal dominance effects and plant dominance effects,  $\sigma_{AE/AmE}$  = covariance between seed  $AE$  effects and plant  $AmE$  effects,  $\sigma_{DE/DmE}$  = covariance between seed  $DE$  effects and plant  $DmE$  effects,  $\sigma_{CE/CE}$  = covariance between seed  $CE$  effects and plant  $CE$  effects,  $\sigma_{AmE/AmE}$  = covariance between seed  $AmE$  effects and plant  $AmE$  effects,  $\sigma_{DmE/DmE}$  = covariance between seed  $DmE$  effects and plant  $DmE$  effects,  $\sigma_{B/B}$  = covariance between seed block effects and plant block effects,  $\sigma_{e/e}$  = covariance between seed residual effects and plant residual effects.

If we define  $F_1 (U_A U_A^T, U_{Am} U_{Am}^T)$ ,  $F_2 (U_D U_D^T, U_{Dm} U_{Dm}^T)$ ,  $F_3 (2U_C U_C^T)$ ,  $F_4 (2U_{Am} U_{Am}^T)$ ,  $F_5 (2U_{Dm} U_{Dm}^T)$ ,  $F_6 (U_{AE} U_{AmE}^T, U_{AmE} U_{AE}^T)$ ,  $F_7 (U_{DE} U_{DmE}^T, U_{DmE} U_{DE}^T)$ ,  $F_8 (2U_{CE} U_{CE}^T)$ ,  $F_9 (2U_{AmE} U_{AmE}^T)$ ,  $F_{10} (2U_{DmE} U_{DmE}^T)$ ,  $F_{11} (2U_B U_B^T)$ , and  $F_{12} 2I$ , covariance components between a seed trait and a plant trait can then be estimated by the following equations:

$$tr(Q_{(0/1)} F_u Q_{(0/1)} F_v) \hat{\sigma}_{u/uv} = 2y_S^T Q_{(0/1)} F_u Q_{(0/1)} y_p$$

where

$$\begin{array}{r}
 Q_{(0/1)} \\
 V_{(0/1)} \\
 \begin{array}{r}
 V_{(0/1)}^{-1} - V_{(0/1)}^{-1} X(X^T V_{(0/1)}^{-1} X)^{-1} X^T V_{(0/1)}^{-1} \\
 2[U_C U_C^T \\
 U_{Am} U_{Am}^T \\
 U_B U_B^T \\
 I] \\
 U_{Dm} U_{Dm}^T \\
 U_{CE} U_{CE}^T \\
 U_{AmE} U_{AmE}^T \\
 U_{DmE} U_{DmE}^T \\
 \end{array} \\
 \end{array}$$

## Originators

- Zhu, J. (1992). Mixed model approaches for estimating genetic variances and covariances. *Journal of Biomathematics* 7(1):1-11.
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- Zhu, J. (1993b). Mixed model approaches for estimating covariances between two traits with unequal design matrices (Chinese). *Journal of Biomathematics* 8(3):24-30.
- Zhu, J. (1996). Analysis methods for seed models with genotype  $\times$  environment interactions (Chinese). *Acta Genetica Sinica* 23(1):56-68.
- Zhu, J. (1997). *Analysis Methods for Genetic Models*. Agricultural Publication House of China, Beijing.
- Zhu, J. and Weir, B.S. (1994a). Analysis of cytoplasmic and maternal effects. I. A genetic model for diploid plant seeds and animals. *Theoretical and Applied Genetics* 89:153-159.
- Zhu, J. and Weir, B.S. (1994b). Analysis of cytoplasmic and maternal effects. II. Genetic models for triploid endosperm. *Theoretical and Applied Genetics* 89:160-166.
- Zhu, J. and Weir, B.S. (1996). Diallel analysis for sex-linked and maternal effects. *Theoretical and Applied Genetics* 92(1):1-9.

## Software Available

Zhu, J. (1997). GENDIPLD.EXE for constructing seed model, GENVAR0.EXE for estimating components of variance and heritability, GENCOV0.EXE for estimating components of covariance and correlation, GENHET0.EXE for predicting genetic effects and components of heterosis. *Analysis Methods for Genetic Models* (pp. 256-278), Agricultural Publication House of China, Beijing (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.

## EXAMPLE

Unbalanced data (COTSEEDM.TXT) to be analyzed (Parent = 5, Year = 2, Generation = P, F<sub>1</sub>, F<sub>2</sub>, Blk = 1):

Year	Fema	Male	Gene	Blk	Pro%	Oil%
1	1	1	0	1	37.6	37.4
1	1	3	1	1	37.5	36.5
1	1	3	2	1	38.3	36.1
1	1	4	1	1	38.4	34.6
1	1	4	2	1	37.8	35.3
1	2	2	0	1	42.9	32.5
1	2	3	1	1	39.8	33.1

1	2	3	2	1	39.2	35.5
1	3	1	2	1	37.2	35.9
1	3	2	2	1	37.1	37.1
1	3	3	0	1	38	34.8
1	3	5	1	1	40.6	35.4
1	3	5	2	1	39.8	36.1
1	4	1	1	1	37.2	36.8
1	4	1	2	1	37	36.1
1	4	2	1	1	39.2	38.1
1	4	2	2	1	38.1	35.3
1	4	4	0	1	38.9	35.5
1	4	5	1	1	41	38.1
1	4	5	2	1	40.1	35.6
1	5	5	0	1	45.8	34.5
2	1	1	0	1	37.7	36.5
2	1	3	1	1	37.2	36.5
2	1	3	2	1	37.2	35.6
2	1	4	1	1	36	36.5
2	1	4	2	1	35.9	36.2
2	2	2	0	1	40.5	34.8
2	2	3	1	1	37.4	36.9
2	2	3	2	1	37	36.8
2	2	4	1	1	38.3	36.3
2	2	4	2	1	37.2	36.9
2	3	3	0	1	38.6	35.4
2	3	5	1	1	38.3	35.7
2	3	5	2	1	37.8	35.8
2	4	4	0	1	39.7	35.1
2	4	5	1	1	38.9	35.6
2	4	5	2	1	38.6	34.6
2	5	5	0	1	44	31.2

1. Use one of the following two programs for generating a mating design matrix and data:

GENDIPLD.EXE for traits of diploid seeds or animals.

GENTRIPL.EXE for traits of triploid endosperm.

Before running these programs, create a data file (COTSEEDM.TXT) for your analysis with five design columns followed by trait columns. The five design columns should be labeled (1) environment, (2) maternal, (3) paternal, (4) generation, and (5) replication. There is a limitation (<100 traits) for the number of trait columns.

2. Run programs for variance and covariance analyses. Standard errors of estimates are calculated by jackknifing over cell means.
3. You should always run GENVAR0C.EXE for estimating variance components and predicting genetic effects before estimating covariance and correlation. This program will allow you to choose the prediction methods (LUP or AUP). You also need to input coefficients (1, 0, or -1) for conducting linear contrasts for genetic effects.

4. After finishing variance analysis, run GENCOV0C.EXE for estimating covariance components and coefficients of correlation among all the traits analyzed.
5. If you want to predict heterosis and genotypic value for F<sub>2</sub> seed, you can run GENHET0C.EXE.
6. All results will be automatically stored in text files for later use or printing. Examples of result files are provided with the names COTSEEDM.VAR for analysis of variance and genetic effects, COTSEEDM.PRE for predicting genotype values and heterosis, and COTSEEDM.COR for analysis of covariances and correlation.

### ***Output 1 for Single Trait Test***

Traits = , 2  
 Variance components = , 15  
 Degree of freedom = , 37  
 File name is cotseedm.VAR  
 Date and Time for Analysis: Fri Jun 23 21:06:32 2000

Variance Components Estimated by MINQUE(0/1) with GENHET0C.EXE.  
 Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP)  
 Method.

Jackknifing Over Block Conducted for Estimating S.E.

NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Linear Contrasting Test:  
 + <1> + <2> + <3> - <4> - <5>

Genetic Analysis of 1 Trait, Pro%, Public Users.

Var Comp	Estimate	S. E.	P-value	
Direct Additive	4.22578	0.971094	5.11522e-005	S**
Direct Dominance	0.661729	0.187698	0.000572911	S**
Cytoplasm	0.979784	0.316941	0.00188757	S**
Maternal Additive	0	0	0.5	NS
Maternal Dominance	2.14103	0.491783	5.08401e-005	S**
D Add. × Env.	4.14108	1.08163	0.00024065	S**
D Dom. × Env.	0.226718	0.0427548	2.75864e-006	S**
Cyto × Env.	3.08077	0.725817	7.05334e-005	S**
M Add. × Env.	2.1	0.520779	0.000132504	S**
M Dom. × Env.	0	0	0.5	NS
A.Am	0	0.271806	1	NS
D.Dm	0.684771	0.400178	0.0954231	S+
AE.AmE	-2.45518	1.3901	1.91438	NS
DE.DmE	0	0	1	NS
Residual	1.56207	0.341266	2.58189e-005	S**
Var(Phenotype)	15.5781	2.49795	1.50314e-007	S**

Heritability	Estimate	S. E.	P-value	
General Heritability N(A)	0.271263	0.0372287	5.88087e-009	S**



General Heritability B(A+D)	0.357699	0.0380067	-1.37905e-011	S**
General Heritability N(C)	0.0628948	0.0226378	0.00426618	S**
General Heritability N(Am)	0	0	0.5	NS
General Heritability B(Am+Dm)	0.181395	0.0240944	2.80833e-009	S**
Interaction Heritability N(AE)	0.108222	0.0325895	0.00101347	S**
Interaction Heritability B(AE+DE)	0.28038	0.0788095	0.000523146	S**
Interaction Heritability N(CE)	0.197762	0.0388026	5.23056e-006	S**
Interaction Heritability N(AmE)	-0.0227996	0.0252744	0.186424	NS
Interaction Heritability B(AmE+DmE)	0.134804	0.0530296	0.00766977	S**

Genetic Predictor, S. E. , P-value of Two Tail t-test

<1>: Random Effect is Direct Additive

A1	-1.024558	0.602650	0.0975	S+
A2	0.849192	0.492454	0.093	S+
A3	-0.959033	0.579315	0.106	NS
A4	0.023544	0.447671	0.958	NS
A5	1.110611	0.833896	0.191	NS
Linear Contrast	-1.74484	1.15265	0.138582	NS

<2>: Random Effect is Direct Dominance

D1*1	0.430174	0.474310	0.37	NS
D2*2	2.060002	1.236368	0.104	NS
D3*3	0.896631	0.591905	0.138	NS
D4*4	1.637057	0.873815	0.0689	S+
D5*5	1.830764	0.882766	0.0451	S*
D1*3	-0.478229	0.456267	0.301	NS
D1*4	-2.177030	1.321475	0.108	NS
D2*3	-2.215217	1.325812	0.103	NS
D2*4	-0.755464	0.577872	0.199	NS
D3*5	-0.781604	0.580198	0.186	NS
D4*5	-0.447118	0.831929	0.594	NS
Heterosis <Delta>	-2.30767	1.86916	0.225	NS

<3>: Random Effect is Cytoplasm

C1	-0.278965	0.268528	0.306	NS
C2	0.125445	0.666036	0.852	NS
C3	-0.434191	1.217060	0.723	NS
C4	0.022447	0.667609	0.973	NS
C5	0.565182	1.479941	0.705	NS
Linear Contrast	-1.32754	4.23754	0.755827	NS

<4>: Random Effect is Maternal Additive

No Significant Effects.

<5>: Random Effect is Maternal Dominance

Dm1*1	0.328107	0.347168	0.351	NS
Dm2*2	1.334076	0.415525	0.00274	S**
Dm3*3	1.422192	0.519389	0.00944	S**
Dm4*4	1.798117	0.562728	0.00285	S**
Dm5*5	1.842966	0.707409	0.0131	S*
Dm1*3	0.355737	0.403627	0.384	NS
Dm1*4	-0.581557	0.660676	0.384	NS
Dm2*3	-1.434893	0.704201	0.0488	S*
Dm2*4	-1.937210	0.780548	0.0177	S*
Dm3*5	-1.322985	0.768254	0.0934	S+
Dm4*5	-1.804685	0.762519	0.0233	S*

Heterosis <Delta> -2.05554 0.153624 -5.09e-011 S\*\*

<6>: Random Effect is D Add. × Env.

AE1 in E1	-2.254065	0.889523	0.0156	S*
AE2 in E1	0.550176	0.647403	0.401	NS
AE3 in E1	-1.761268	0.848635	0.045	S*
AE4 in E1	0.449786	0.592606	0.453	NS
AE5 in E1	3.015095	1.252800	0.0212	S*
AE1 in E2	0.632488	0.575894	0.279	NS
AE2 in E2	0.874021	0.831909	0.3	NS
AE3 in E2	0.005609	0.629156	0.993	NS
AE4 in E2	-0.596792	0.806521	0.464	NS
AE5 in E2	-0.915384	0.884746	0.308	NS
Linear Contrast	-5.3845	1.32097	0.000233	S**

<7>: Random Effect is D Dom. × Env.

DE1*1 in E1	-0.159850	0.800087	0.843	NS
DE2*2 in E1	0.407181	1.084693	0.71	NS
DE3*3 in E1	-0.132742	0.696827	0.85	NS
DE4*4 in E1	0.001560	0.707096	0.998	NS
DE5*5 in E1	0.110871	0.599268	0.854	NS
DE1*3 in E1	-0.214554	0.706944	0.763	NS
DE1*4 in E1	-0.558690	0.675476	0.413	NS
DE2*3 in E1	-0.403386	1.054141	0.704	NS
DE2*4 in E1	0.075915	0.482125	0.876	NS
DE3*5 in E1	0.105371	1.002477	0.917	NS
DE4*5 in E1	0.768304	1.301119	0.558	NS
DE1*1 in E2	0.508888	1.015302	0.619	NS
DE2*2 in E2	0.623124	1.464434	0.673	NS
DE3*3 in E2	0.853831	1.248241	0.498	NS
DE4*4 in E2	0.310951	1.774209	0.862	NS
DE5*5 in E2	0.149658	1.260388	0.906	NS
DE1*3 in E2	-0.242427	0.585483	0.681	NS
DE1*4 in E2	-0.388505	2.125310	0.856	NS
DE2*3 in E2	-0.489308	1.570559	0.757	NS
DE2*4 in E2	-0.455681	0.679028	0.506	NS
DE3*5 in E2	-0.711946	1.394222	0.613	NS
DE4*5 in E2	-0.158580	1.360425	0.908	NS
Heterosis <Delta>	1.00932	2.70601	0.711	NS

<8>: Random Effect is Cyto × Env.

CE1 in E1	0.776034	0.458734	0.0991	S+
CE2 in E1	2.165781	1.241707	0.0894	S+
CE3 in E1	-1.300904	1.205518	0.288	NS
CE4 in E1	-1.491405	0.967790	0.132	NS
CE5 in E1	-0.149753	1.093888	0.892	NS
CE1 in E2	-1.444760	0.686140	0.0421	S*
CE2 in E2	-1.573186	0.812138	0.0604	S+
CE3 in E2	-0.538525	0.951240	0.575	NS
CE4 in E2	0.589799	1.194278	0.624	NS
CE5 in E2	2.966626	1.385019	0.0388	S*
Linear Contrast	2.09064	1.35549	0.131499	NS

<9> : Random Effect is M Add. × Env.

AmE1 in E1	0.164594	0.421542	0.698	NS
AmE2 in E1	-0.132997	0.439265	0.764	NS

AmE3 in E1	1.211076	0.516050	0.0244	S*
AmE4 in E1	-2.478739	1.117579	0.0328	S*
AmE5 in E1	1.235679	0.732488	0.1	NS
AmE1 in E2	-1.227880	0.750977	0.111	NS
AmE2 in E2	-1.586811	0.633135	0.0167	S*
AmE3 in E2	-0.309359	0.516714	0.553	NS
AmE4 in E2	-0.003356	0.573114	0.995	NS
AmE5 in E2	3.127315	1.394990	0.0311	S*
Linear Contrast	2.71224	3.94209	0.495730	NS

<10>: Random Effect is M Dom. × Env.  
No Significant Effects.

Results of Oil% are not presented.

Time Used (Hour) = 0.001389

## Output 2 for Covariance Analysis

Traits = , 2  
Variance components = , 15  
Degree of freedom = , 37  
File name is cotseedm.COV  
Date and Time for Analysis: Fri Jun 23 21:06:49 2000

Variance Components Estimated by MINQUE(0/1) with GENHET0C.EXE.  
Jackknifing Over Block Conducted for Estimating S.E.  
For statistical methods, see the following references:

NS = Not significant; S+ = Significant at 0.10 level.  
S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Covariances and Correlations Between, Pro% &, Oil% for, Public Users.:

Covariances	Estimates	S.E.	P-value	
Direct Additive Cov	-0.12332	0.785577	0.876	NS
Direct Dominance Cov	-0.18046	0.223768	0.425	NS
Cytoplasm Cov	-0.0560615	0.946456	0.953	NS
Maternal Additive Cov	-0.247106	0.497206	0.622	NS
Maternal Dominance Cov	-0.76196	0.363677	0.0431	S*
D Add. × Env. Cov	0.238753	1.25031	0.85	NS
D Dom. × Env. Cov	0.0696955	0.201047	0.731	NS
Cyto × Env. Cov	-0.748348	0.966985	0.444	NS
M Add. × Env. Cov	-0.567987	0.712327	0.43	NS
M Dom. × Env. Cov	0.139297	0.400729	0.73	NS
A.Am Cov	0.0209709	0.592716	0.972	NS
D.Dm Cov	-0.317895	0.181318	0.0878	S+
AE.AmE Cov	0.538553	0.864524	0.537	NS
DE.DmE Cov	-0.104535	0.150625	0.492	NS
Residual Cov	-0.125117	0.335582	0.711	NS

Cov <1=Genotypic>	Estimates	S.E.	P-value	
Cov <2=Phenotypic>				
Cov 2	-2.08843	1.00453	0.0446	S*
Cov 1	-1.96331	1.0037	0.058	S+

Correlation	Estimates	S.E.	P-value	
Direct Additive Cor	0.000000	0	1	NS
Direct Dominance Cor	-0.313393	0.0713042	8.97e-005	S**
Cytoplasm Cor	0.000000	0	1	NS
Maternal Additive Cor	0.000000	0	1	NS
Maternal Dominance Cor	-0.527223	0.0751039	2.66e-008	S**
D Add. × Env. Cor	0.064792	0.0855313	0.454	NS
D Dom. × Env. Cor	0.225062	0.0669711	0.00182	S**
Cyto × Env. Cor	-0.302136	0.0755769	0.000294	S**
M Add. × Env. Cor	-0.271364	0.0710278	0.000493	S**
M Dom. × Env. Cor	0.000000	0	1	NS
Residual Cor	-0.379882	0.0634317	6.5e-007	S**

Cor <1=Genotypic> <2=Phenotypic>	Estimates	S.E.	P-value	
Cor 2	-0.157513	0.0580681	0.0101	S*
Cor 1	-0.154315	0.0587436	0.0125	S*

Time Used (Hour) = 0.000556

### Output 3 for Heterosis Analysis

Traits =, 2  
 Variance components =, 15  
 Degree of freedom =, 37  
 File name is cotseedm.PRE  
 Date and Time for Analysis: Fri Jun 23 21:07:07 2000

Variance Components Estimated by MINQUE(0/1) with GENHET0C.EXE.  
 Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP)  
 Method.

Jackknifing Over Block Conducted for Estimating S.E.

NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Genetic Analysis of 1 Trait, Pro%, for Public Users.

Var Comp	Estimate	S. E.	P-value	
Direct Additive	4.22543	0.971079	5.12e-005	S**
Direct Dominance	0.661737	0.187698	0.000573	S**
Cytoplasm	0.979678	0.316932	0.00189	S**
Maternal Additive	0	0	0.5	NS
Maternal Dominance	2.141	0.491782	5.08e-005	S**
D Add. × Env.	4.14101	1.08162	0.000241	S**
D Dom. × Env.	0.226713	0.042754	2.76e-006	S**
Cyto × Env.	3.08084	0.725821	7.05e-005	S**
M Add. × Env.	2.10002	0.520781	0.000132	S**
M Dom. × Env.	0	0	0.5	NS
A.Am	0	0	1	NS
D.Dm	0.684787	0.400178	0.0954	S+
AE.AmE	-2.45513	1.3901	0.0856	S+
DE.DmE	0	0	1	NS

Residual	1.5621	0.341269	2.58e-005	S**
Var (Phenotype)	15.5779	2.49795	1.5e-007	S**

Genetic Advance (for 0.05)	Estimate	S. E.	P-value	
General Genetic Advance (A)	5.69401	0.844563	3.13324e-008	S**
General Genetic Advance (C)	1.32017	0.382756	0.000709897	S**
General Genetic Advance (Am)	0	0	0.5	NS
Interaction Genetic Advance (AE)	2.27182	0.576013	0.00017183	S**
Interaction Genetic Advance (CE)	4.15161	0.768543	2.0263e-006	S**
Interaction Genetic Advance (AmE)	0.478526	0.466339	0.155745	NS

Heterosis Analysis of Trait, Pro%, for F2 Seeds with total mean =, 38.731644

No.	Cro	G(T)	S.E.	Pv	Sig	G(O)	S.E.	Pv	Sig	G(C)	S.E.	Pv	Sig	G(M)	S.E.	Pv	Sig
Cro<1>	<1 * 3>	-1.810.71	0.01	S *	S *	-1.89	0.69	0.01	S**	-0.28	0.19	0.15	NS	0.36	0.34	0.30	NS
Cro<2>	<1 * 4>	-2.430.67	0.00	S**	S**	-1.57	0.59	0.01	S *	-0.28	0.19	0.15	NS	-0.58	0.40	0.16	NS
Cro<3>	<2 * 3>	-1.790.75	0.02	S *	S *	-0.48	0.37	0.21	NS	0.13	0.40	0.76	NS	-1.43	0.66	0.04	S *
Cro<4>	<2 * 4>	-0.390.99	0.69	NS	NS	1.42	0.57	0.02	S *	0.13	0.40	0.76	NS	-1.94	0.76	0.02	S *
Cro<5>	<3 * 5>	-1.311.39	0.35	NS	NS	0.44	0.32	0.18	NS	-0.43	0.89	0.63	NS	-1.32	0.76	0.09	S +
Cro<6>	<4 * 5>	0.001.04	1.00	NS	NS	1.78	0.58	0.00	S**	0.02	0.40	0.96	NS	-1.80	0.74	0.02	S *

No.	Cro	Hm(T)	S.E.	Pv	Sig	Hm(O)	S.E.	Pv	Sig	Hm(C)	S.E.	Pv	Sig	Hm(M)	S.E.	Pv	Sig
Cro<1>	<1 * 3>	-0.03	0.02	0.22	NS	-0.01	0.01	0.07	S +	0.00	0.01	0.83	NS	-0.01	0.01	0.33	NS
Cro<2>	<1 * 4>	-0.09	0.02	0.00	S**	-0.04	0.02	0.04	S *	0.00	0.00	0.24	NS	-0.04	0.02	0.02	S *
Cro<3>	<2 * 3>	-0.11	0.04	0.01	S *	-0.05	0.02	0.06	S +	0.01	0.02	0.66	NS	-0.07	0.02	0.00	S**
Cro<4>	<2 * 4>	-0.12	0.04	0.00	S**	-0.03	0.02	0.05	S *	0.00	0.01	0.89	NS	-0.09	0.03	0.00	S**
Cro<5>	<3 * 5>	-0.12	0.05	0.04	S *	-0.03	0.01	0.03	S *	-0.01	0.03	0.62	NS	-0.08	0.03	0.02	S *
Cro<6>	<4 * 5>	-0.13	0.05	0.01	S**	-0.03	0.01	0.00	S**	-0.01	0.02	0.73	NS	-0.09	0.03	0.00	S**

No.	Cro	Hf(T)	S.E.	Pv	Sig	Hf(O)	S.E.	Pv	Sig	Hf(M)	S.E.	Pv	Sig	Gen.	S.E.	Pv	Sig
Cro<1>	<1 * 3>	-0.01	0.02	0.75	NS	-0.01	0.01	0.60	NS	0.00	0.01	0.96	NS	0.00	0.00	2.00	NS
Cro<2>	<1 * 4>	-0.02	0.02	0.33	NS	0.00	0.02	0.95	NS	-0.02	0.02	0.15	NS	0.00	0.00	2.00	NS
Cro<3>	<2 * 3>	-0.18	0.06	0.01	S**	-0.11	0.05	0.03	S *	-0.07	0.02	0.00	S**	0.00	0.00	2.00	NS
Cro<4>	<2 * 4>	-0.14	0.05	0.01	S *	-0.06	0.04	0.11	NS	-0.08	0.03	0.00	S**	0.00	0.00	2.00	NS
Cro<5>	<3 * 5>	-0.03	0.03	0.33	NS	0.04	0.03	0.15	NS	-0.07	0.03	0.02	S *	0.00	0.00	2.00	NS
Cro<6>	<4 * 5>	-0.09	0.03	0.00	S**	0.00	0.02	0.90	NS	-0.09	0.03	0.00	S**	0.00	0.00	2.00	NS

Interaction Heterosis Analysis of Trait, Pro%, for F2 Seeds with total mean =, 38.731644

No.	Cro	GE(T)	S.E.	Pv	Sig	GE(O)	S.E.	Pv	Sig	GE(C)	S.E.	Pv	Sig	GE(M)	S.E.	Pv	Sig
Env.<1>	<1 * 3>	-2.04	1.06	0.06	S +	-4.20	1.25	0.00	S**	0.78	0.32	0.02	S *	1.38	0.50	0.01	S**
Env.<1>	<1 * 4>	-3.66	1.30	0.01	S**	-2.12	0.77	0.01	S**	0.78	0.43	0.08	S +	-2.31	1.12	0.05	S *
Env.<1>	<2 * 3>	1.90	1.69	0.27	NS	-1.34	0.87	0.13	NS	2.17	1.82	0.24	NS	1.08	0.98	0.28	NS
Env.<1>	<2 * 4>	0.70	1.99	0.73	NS	1.14	1.11	0.31	NS	2.17	1.82	0.24	NS	-2.61	1.03	0.02	S *
Env.<1>	<3 * 5>	2.45	1.57	0.13	NS	1.30	0.95	0.18	NS	-1.30	1.23	0.30	NS	2.45	0.91	0.01	S *
Env.<1>	<4 * 5>	1.14	1.06	0.29	NS	3.88	1.45	0.01	S *	-1.49	0.69	0.04	S *	-1.24	0.99	0.22	NS
Env.<2>	<1 * 3>	-2.12	1.11	0.06	S +	0.86	1.17	0.47	NS	-1.44	0.65	0.03	S *	-1.54	0.85	0.08	S +
Env.<2>	<1 * 4>	-2.63	1.41	0.07	S +	0.05	0.83	0.96	NS	-1.44	0.65	0.03	S *	-1.23	0.61	0.05	S +
Env.<2>	<2 * 3>	-2.47	1.47	0.10	NS	1.00	0.70	0.16	NS	-1.57	1.03	0.14	NS	-1.90	0.84	0.03	S *
Env.<2>	<2 * 4>	-2.88	1.55	0.07	S +	0.28	0.73	0.70	NS	-1.57	1.03	0.14	NS	-1.59	0.84	0.07	S +
Env.<2>	<3 * 5>	1.27	1.24	0.31	NS	-1.01	0.69	0.15	NS	-0.54	0.39	0.17	NS	2.82	1.24	0.03	S *
Env.<2>	<4 * 5>	2.24	1.67	0.19	NS	-1.48	0.83	0.08	S +	0.59	0.80	0.46	NS	3.12	1.48	0.04	S *

No.	Cro	HmE(T)	S.E.	Pv	Sig	HmE(O)	S.E.	Pv	Sig	HmE(C)	S.E.	Pv	Sig	HmE(M)	S.E.	Pv	Sig
Env.<1>	<1 * 3>	>0.03	0.01	0.02	S *	0.00	0.00	0.37	NS	0.03	0.01	0.01	S *	0.00	0.00	2.00	NS

Env.<1><1*4>0.02	0.04	0.59	NS	-0.01	0.03	0.81	NS	0.03	0.01	0.02	S*	0.00	0.00	2.00	NS
Env.<1><2*3>0.04	0.05	0.49	NS	-0.01	0.01	0.53	NS	0.04	0.04	0.28	NS	0.00	0.00	2.00	NS
Env.<1><2*4>0.05	0.03	0.18	NS	0.00	0.02	0.94	NS	0.05	0.03	0.13	NS	0.00	0.00	2.00	NS
Env.<1><3*5>-0.01	0.02	0.54	NS	0.00	0.01	0.85	NS	-0.01	0.02	0.38	NS	0.00	0.00	2.00	NS
Env.<1><4*5>-0.01	0.03	0.79	NS	0.01	0.02	0.62	NS	-0.02	0.01	0.11	NS	0.00	0.00	2.00	NS
Env.<2><1*3>-0.02	0.01	0.10	S+	-0.01	0.01	0.06	S+	-0.01	0.01	0.28	NS	0.00	0.00	2.00	NS
Env.<2><1*4>-0.04	0.05	0.48	NS	-0.01	0.04	0.78	NS	-0.03	0.02	0.14	NS	0.00	0.00	2.00	NS
Env.<2><1*3>-0.03	0.05	0.53	NS	-0.02	0.04	0.71	NS	-0.01	0.02	0.41	NS	0.00	0.00	2.00	NS
Env.<2><2*4>-0.04	0.05	0.47	NS	-0.01	0.03	0.71	NS	-0.03	0.02	0.24	NS	0.00	0.00	2.00	NS
Env.<2><3*5>-0.06	0.06	0.29	NS	-0.02	0.04	0.67	NS	-0.05	0.01	0.00	S**	0.00	0.00	2.00	NS
Env.<2><4*5>-0.04	0.05	0.45	NS	-0.01	0.03	0.84	NS	-0.03	0.01	0.00	S**	0.00	0.00	2.00	NS

No.	Cro HfE(T)	S.E.	Pv	Sig HfE(O)	S.E.	Pv	Sig HfE(C)	S.E.	Pv	Sig	HfE (M)	S.E.	Pv	Sig	
Env.<1><1*3>0.04	0.02	0.07	S+	0.01	0.02	0.47	NS	0.03	0.01	0.05	S+	0.00	0.00	2.00	NS
Env.<1><1*4>0.00	0.08	0.97	NS	0.07	0.09	0.47	NS	-0.07	0.04	0.09	S+	0.00	0.00	2.00	NS
Env.<1><2*3>-0.04	0.07	0.58	NS	-0.07	0.04	0.06	S+	0.03	0.05	0.50	NS	0.00	0.00	2.00	NS
Env.<1><2*4>-0.07	0.05	0.21	NS	-0.01	0.04	0.79	NS	-0.06	0.05	0.23	NS	0.00	0.00	2.00	NS
Env.<1><3*5>0.13	0.04	0.00	S**	0.13	0.04	0.00	S**	0.00	0.02	0.98	NS	-4.88	0.27	0.00	S**
Env.<1><4*5>0.17	0.04	0.00	S**	0.08	0.03	0.01	S**	0.10	0.05	0.09	S+	-2.54	0.25	0.00	S**
Env.<2><1*3>0.00	0.04	1.00	NS	-0.02	0.03	0.42	NS	0.02	0.02	0.23	NS	0.00	0.00	2.00	NS
Env.<2><1*4>-0.01	0.04	0.77	NS	-0.04	0.05	0.41	NS	0.03	0.03	0.24	NS	0.00	0.00	2.00	NS
Env.<2><2*3>0.00	0.05	0.97	NS	-0.04	0.06	0.55	NS	0.03	0.02	0.14	NS	0.00	0.00	2.00	NS
Env.<2><2*4>-0.01	0.05	0.80	NS	-0.05	0.06	0.36	NS	0.04	0.02	0.11	NS	0.00	0.00	2.00	NS
Env.<2><3*5>0.04	0.05	0.44	NS	-0.05	0.04	0.24	NS	0.09	0.04	0.04	S*	0.00	0.00	2.00	NS
Env.<2><4*5>0.07	0.05	0.19	NS	-0.02	0.02	0.53	NS	0.08	0.04	0.04	S*	0.00	0.00	2.00	NS

Results of Oil% are not presented.

Time Used (Hour) = 0.000278



## Chapter 3

# Diallel Analysis for an Additive-Dominance Model with Genotype-by-Environment Interaction Effects

Jun Zhu

### *Purpose*

To analyze balanced or unbalanced data of an additive x dominance (AD) genetic model for estimating components of variance, covariance, heritability, and selection response.

### *Definitions*

#### *Mating Design*

A set of inbred lines are sampled from a reference population. These parents are used to produce  $F_1$  crosses. If it is difficult to use  $F_1$  crosses for some crops,  $F_2$  crosses can be used as an alternative. Experiments with parents and  $F_1$ s (or  $F_2$ s) are conducted in multiple environments using a randomized complete block design.

#### *Genetic Model*

The genetic model for a genetic entry derived from parents  $i$  and  $j$  in the  $k$ th block within the  $h$ th environment is

$$y_{hijk} = \mu + E_h + G_{ij} + GE_{hij} + B_{hk} + e_{hijk}$$



where  $\mu$  = population mean,  $E_h$  = environment effect,  $G_{ij}$  = total genotypic effect,  $GE_{hij}$  = genotype  $\times$  environment interaction effect,  $B_{hk}$  = block effect, and  $e_{hijk}$  = residual effect.

For parent ( $P_i$ ):

$$G_{ii} \quad GE_{hii} \quad 2A_i \quad D_{ii} \quad 2AE_{hi} \quad DE_{hii}$$

For  $F_1$  ( $P_i \times P_j$ ):

$$G_{ij} \quad GE_{hij} \quad A_i \quad A_j \quad D_{ij} \quad AE_{hi} \quad AE_{hj} \quad DE_{hij}$$

For  $F_2$  ( $F_1 \otimes$ ):

$$G_{ij} \quad GE_{hij} \quad A_i \quad A_j \quad \frac{1}{4}D_{ij} \quad \frac{1}{4}D_{ii} \quad \frac{1}{2}D_{jj} \\ AE_{hi} \quad AE_{hj} \quad \frac{1}{4}DE_{hii} \quad \frac{1}{4}DE_{hjj} \quad \frac{1}{2}DE_{hij}$$

where  $A$  = additive effect,  $D$  = dominance effect,  $AE$  = additive by environment interaction effect,  $DE$  = dominance by environment interaction effect.

## ***Analysis Methodology***

### *Mixed Linear Model*

The phenotypic mean of the genetic model can be expressed by a mixed linear model as

$$y = Xb + \begin{matrix} U_A e_A \\ U_D e_D \\ U_{AE} e_{AE} \\ U_{DE} e_{DE} \\ U_B e_B \\ e_e \end{matrix} + \begin{matrix} U_u e_u \\ \end{matrix}$$

with variance-covariance matrix

$$\text{var}(y) = \begin{matrix} \sigma_A^2 U_A U_A^T & & & & & & \\ & \sigma_D^2 U_D U_D^T & & & & & \\ & & \sigma_{AE}^2 U_{AE} U_{AE}^T & & & & \\ & & & \sigma_{DE}^2 U_{DE} U_{DE}^T & & & \\ & & & & \sigma_B^2 U_B U_B^T & & \\ & & & & & \sigma_e^2 I & \\ & & & & & & \sigma_u^2 U_u U_u^T \\ & & & & & & & \sigma_u^2 V_u \end{matrix}$$

### Variance Components

Unbiased estimation of variances can be obtained by the following MINQUE(1) equations (Zhu, 1992; Zhu and Weir, 1996):

$$\text{tr } Q_{(1)} V_u Q_{(1)} V_v \quad \hat{\sigma}_u^2 \quad y^T Q_{(1)} V_u Q_{(1)} y$$

where

$$Q_{(1)} = V_{(1)}^{-1} - V_{(1)}^{-1} X (X^T V_{(1)}^{-1} X)^{-1} X^T V_{(1)}^{-1}$$

$$V_{(1)} = \begin{matrix} V_u & & & \\ & U_u & U_u^T & \\ & & U_u & \\ & & & V_e \end{matrix}$$

When experimental variances ( $\sigma_u^2$ ) are estimated, genetic variance components can be obtained by  $V_A$ ,  $2\sigma_A^2$ ,  $V_D$ ,  $\sigma_D^2$ ,  $V_{AE}$ ,  $2\sigma_{AE}^2$ ,  $V_{DE}$ ,  $\sigma_{DE}^2$ , and  $V_e$ ,  $\sigma_e^2$ . The total phenotypic variance is  $V_P = V_A + V_D + V_{AE} + V_{DE} + V_e$ .

### Covariance Components and Correlation

Unbiased estimation of covariances  $\sigma_{u/1u}$  between two traits ( $y_1$  and  $y_2$ ) can be obtained by MINQUE(1) approaches (Zhu, 1992; Zhu and Weir, 1996):

$$\text{tr } Q_{(1)} V_u Q_{(1)} V_v \quad \hat{\sigma}_{u/1u} \quad y_1^T Q_{(1)} V_u Q_{(1)} y_2$$

When experimental covariances ( $\sigma_{u/1u}$ ) are estimated, genetic covariance components can be obtained by  $C_A$ ,  $2\sigma_{A/A}$ ,  $C_D$ ,  $\sigma_{D/D}$ ,  $C_{AE}$ ,  $2\sigma_{AE/AE}$ ,  $C_{DE}$ ,  $\sigma_{DE/DE}$ , and  $C_e$ ,  $\sigma_{e/e}$ . The total phenotypic covariance is  $C_P = C_A + C_D + C_{AE} + C_{DE} + C_e$ . For trait 1 and trait 2, correlation coefficient of genetic components can be estimated by  $r_A = C_A / \sqrt{V_{A(1)} V_{A(2)}}$ ,  $r_D = C_D / \sqrt{V_{D(1)} V_{D(2)}}$ ,  $r_{AE} = C_{AE} / \sqrt{V_{AE(1)} V_{AE(2)}}$ ,  $r_{DE} = C_{DE} / \sqrt{V_{DE(1)} V_{DE(2)}}$ , and  $r_e = C_e / \sqrt{V_{e(1)} V_{e(2)}}$ .

### Heritability Components

For the genetic model with GE interaction effects, the total heritability ( $h^2$ ) can be partitioned into two components ( $h^2 = h_G^2 + h_{GE}^2$ ), where  $h_G^2 = V_A / V_P$  is general heritability and  $h_{GE}^2 = V_{AE} V_P$  is interaction heritability

(Zhu, 1997). General heritability is applicable to multiple environments whereas interaction heritability is applicable only to specific environments.

### Selection Response

The total selection response ( $R = ih^2\sqrt{V_p}$ ) can be partitioned into two components (Zhu, 1997):

$$R = R_G + R_{GE}$$

where  $R_G = ih_G^2\sqrt{V_p}$  is general response and  $R_{GE} = ih_{GE}^2\sqrt{V_p}$  is interaction response.

### Heterosis Components

Prediction of genetic merits can be obtained by using the linear unbiased prediction (LUP) method (Zhu, 1992; Zhu and Weir, 1996) or adjusted unbiased prediction (AUP) method (Zhu, 1993; Zhu and Weir, 1996). Predicted genotypic effects and  $GE$  interaction effects can be further used in analyzing heterosis of different generations (Zhu, 1997). Heterosis in specific environments consists of two components. General heterosis is due to genotypic effects and can be expected in overall environments, and interaction heterosis is a deviant of  $GE$  interaction relative to specific environments. The two components of heterosis based on midparent or better parent can be calculated as

General heterosis of  $F_n$  relative to midparent:  $H_M(F_n) = (\frac{1}{2})^{n-1} D$

Interaction heterosis of  $F_n$  relative to midparent:  $H_{ME}(F_n) = (\frac{1}{2})^{n-1} DE$

General heterosis of  $F_n$  relative to better parent ( $P_j$ ):

$$H_B(F_n) = (\frac{1}{2})^{n-1} D - \frac{1}{2} G$$

Interaction heterosis of  $F_n$  relative to better parent ( $P_j$ ):

$$H_{BE}(F_n) = (\frac{1}{2})^{n-1} DE - \frac{1}{2} GE$$

where  $D = D_{ij} - \frac{1}{2}(D_{ii} + D_{jj})$  is dominance heterosis,  $DE = DE_{hij} - \frac{1}{2}(DE_{hii} + DE_{hjj})$  is  $DE$  interaction heterosis,  $G = |G(P_i) - G(P_j)|$  is parental genotypic difference, and  $GE = |GE(P_i) - GE(P_j)|$  is parental interaction difference.

Heterosis based on population mean ( $H_{PM} - \frac{1}{\mu}H_M$ ,  $H_{PME} - \frac{1}{\mu}H_{ME}$ ,  $H_{PB} - \frac{1}{\mu}H_B$ , or  $H_{PBE} - \frac{1}{\mu}H_{BE}$ ) can be used to compare proportion of heterosis among different traits.

### Originators

- Zhu, J. (1992). Mixed model approaches for estimating genetic variances and covariances. *Journal of Biomathematics* 7(1):1-11.
- Zhu, J. (1993). Methods of predicting genotype value and heterosis for offspring of hybrids (Chinese). *Journal of Biomathematics* 8(1):32-44.
- Zhu, J. (1997). *Analysis Methods for Genetic Models*. Agricultural Publication House of China, Beijing.
- Zhu, J. and Weir, B.S. (1996). Diallel analysis for sex-linked and maternal effects. *Theoretical and Applied Genetics* 92(1):1-9.

### Software Available

Zhu, J. (1997). GENAD.EXE for constructing AD model, GENVAR1.EXE for estimating components of variance and heritability, GENCOV1.EXE for estimating components of covariance and correlation, GENHET1.EXE for predicting genetic effects and components of heterosis. *Analysis Methods for Genetic Models* (pp. 278-285), Agricultural Publication House of China, Beijing (program free of charge). Contact: Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.

## EXAMPLE

Unbalanced data (COTDATA.TXT) to be analyzed (Parent = 4, Year = 2, Blk = 2):

Env	Fem	Male	Cross	Blk	Bolls	Fiber	Yield
1	1	1	0	1	14.5	54.4	
1	1	1	0	2	11.2	29.7	
1	1	2	1	1	10.9	54.3	
1	1	2	1	2	12.4	55.1	
1	1	3	1	1	12.7	43.7	
1	1	3	1	2	10.4	51.2	
1	1	4	1	1	15.5	58.3	
1	1	4	1	2	14.3	38.5	
1	2	1	1	1	15.9	62.5	
1	2	1	1	2	14.0	56.8	
1	2	2	0	1	14.0	34.8	
1	2	2	0	2	14.9	35.0	
1	2	3	1	1	12.7	34.3	

1	2	3	1	2	10.0	24.1
1	2	4	1	1	14.7	34.9
1	2	4	1	2	18.2	34.1
1	3	1	1	1	10.0	26.9
1	3	1	1	2	11.4	28.1
1	3	2	1	1	13.9	23.9
1	3	2	1	2	11.1	33.5
1	3	3	0	1	6.3	12.5
1	3	3	0	2	9.1	22.3
1	3	4	1	1	11.4	19.8
1	3	4	1	2	11.0	21.4
1	4	1	1	1	13.3	43.8
1	4	1	1	2	12.0	42.0
1	4	2	1	1	15.9	31.5
1	4	2	1	2	16.7	40.2
1	4	3	1	1	13.6	39.9
1	4	3	1	2	14.9	19.6
1	4	4	0	1	10.0	28.5
1	4	4	0	2	15.0	28.1
2	1	1	0	1	19.4	55.1
2	1	1	0	2	24.1	56.3
2	1	2	1	1	21.7	69.2
2	1	2	1	2	25.1	79.5
2	1	3	1	1	15.1	76.8
2	1	3	1	2	16.6	42.7
2	1	4	1	1	22.9	72.7
2	1	4	1	2	19.2	62.7
2	2	2	0	1	17.2	60.6
2	2	2	0	2	19.6	71.6
2	2	3	1	1	18.9	36.8
2	2	3	1	2	17.2	47.8
2	2	4	1	1	32.8	61.9
2	2	4	1	2	30.7	78.3
2	3	3	0	1	13.6	27.8
2	3	3	0	2	8.4	19.1
2	3	4	1	1	16.8	37.9
2	3	4	1	2	17.0	34.2
2	4	4	0	1	21.5	49.5
2	4	4	0	2	19.9	57.1

1. Run GENAD.EXE to create mating design matrix files and data files for additive-dominance (AD) model. Before running this program, you should create a file for your analysis with five design columns followed by trait columns. The first five columns are: (1) environment, (2) maternal, (3) paternal, (4) generation, and (5) replication. There is a limitation (<100 traits) for the number of trait columns. An example of a data file is provided with the name COTDATA.TXT.
2. Run programs for variance and covariance analyses. Standard errors of estimates are calculated using jackknife procedures. If you have multiple blocks for your experiments, you can use GENVAR1R.EXE or GENCOV1R.EXE for jackknifing over blocks. Otherwise you can use

- GENVAR1C.EXE or GENCOV1C.EXE for jackknifing over cell means.
3. Run GENVAR1R.EXE or GENVAR1C.EXE for estimating variance components and predicting genetic effects before estimating covariance and correlation. These two programs will allow you to choose the parental type (inbred or outbred) and the prediction methods (LUP or AUP). You also need to input coefficients (1, 0, or -1) for conducting linear contrasts for genetic effects of parents.
  4. After you finish variance analysis, you can run GENCOV1R.EXE or GENCOV1C.EXE for estimating covariance components and coefficients of correlation among all the traits analyzed.
  5. If you want to predict heterosis and genotypic value for each  $F_1$  or  $F_2$  cross by an AD model, you can run GENHET1R.EXE or GENHET1C.EXE.
  6. The results from the analyses will be automatically stored in text files for later use or printing. Examples of result files are provided with the names COTDATA.VAR for analysis of variance and genetic effects, COTDATA.PRE for heterosis, and COTDATA.COR for analysis of covariances and correlation.

### ***Output 1 for Variance Analysis***

```
Traits =, 2
Variance components = , 6
Degree of freedom = , 3
File name is cotdata.VAR
Date and Time for Analysis: Thu Jun 22 21:43:19 2000

Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.
Jackknifing Over Block Conducted for Estimating S.E.
Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP)
Method.
```

NS = Not significant; S+ = Significant at 0.10 level.  
S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Linear Contrasts:  
+ <1> + <2> - <3> + <4>

Diallel Analysis of Trait 'Bolls' for Public Users

Var Comp	Estimate	S. E.	P-value	
(1): Additive Var	7.30438	1.4425	0.00743	S**
(2): Dominance Var	3.29038	0.935764	0.0195	S*
(3): Add. * Env. Var	0.866547	0.683906	0.147	NS
(4): Dom. * Env. Var	4.82384	1.71492	0.0336	S*
(6): Residual Var	4.18772	0.555651	0.00242	S**

(7): Var(Pheno.)	20.4729	2.79941	0.00264	S**
Proportion of Var(G)/Var(T)Estimate		S. E.	P-value	
(1): Additive Var/Vp	0.356783	0.0888328	0.0139	S*
(2): Dominance Var/Vp	0.160719	0.0275068	0.005	S**
(3): Add. * Env. Var/Vp	0.0423266	0.0244	0.0906	S+
(4): Dom. * Env. Var/Vp	0.235621	0.0667933	0.0194	S*
(6): Residual Var/Vp	0.20455	0.0209314	0.00114	S**
Heritability	Estimate	S. E.	P-value	
(7): Heritability(N)	0.356783	0.0888328	0.0139	S*
(8): Heritability(B)	0.517502	0.0661515	0.00217	S**
(9): Heritability(NE)	0.0423266	0.0244	0.0906	S+
(10): Heritability(BE)	0.277948	0.0575567	0.00846	S**
Genetic Predictor, S. E., P-value for Two-tail t-test				
(1): Random Effect is Additive Effect				
A1	0.392019	0.632218	0.579	NS
A2	1.326158	0.211643	0.0082	S**
A3	-2.917664	0.353084	0.00371	S**
A4	1.199422	0.548514	0.117	NS
Linear Contrast	3.05342	0.470211	0.00741	S**
(2): Random Effect is Dominance Effect				
D1*1	0.263665	0.437706	0.589	NS
D2*2	-2.176718	0.509854	0.0236	S*
D3*3	-1.244060	0.786988	0.212	NS
D4*4	-1.836773	0.495630	0.0341	S*
D1*2	0.388935	0.399988	0.403	NS
D1*3	-0.349309	0.311425	0.344	NS
D1*4	-0.273600	0.915662	0.785	NS
D2*3	0.210065	0.829160	0.816	NS
D2*4	4.888072	0.707825	0.00622	S**
D3*4	0.129694	0.666849	0.858	NS
Heterosis <Delta>	1.37653	0.337286	0.0266	S*
(3): Random Effect is Add. * Env. Effect				
AE1 in E1	0.089686	0.496245	0.868	NS
AE2 in E1	0.242420	0.070750	0.0416	S*
AE3 in E1	-0.079016	0.182773	0.695	NS
AE4 in E1	-0.253113	0.407134	0.578	NS
AE1 in E2	-0.136729	0.705758	0.859	NS
AE2 in E2	0.342004	0.648600	0.634	NS
AE3 in E2	-1.257717	1.654640	0.502	NS
AE4 in E2	1.052433	0.508793	0.13	NS
Linear Contrast	-1.76747e-005	6.70577e-006	0.0779	S+
(4): Random Effect is Dom. * Env. Effect				
DE11 in E1	-0.349740	0.559982	0.577	NS
DE22 in E1	2.063640	0.515148	0.0279	S*
DE33 in E1	-0.889553	1.186821	0.508	NS
DE44 in E1	-0.318622	1.006553	0.772	NS
DE12 in E1	-1.294414	0.520453	0.0887	S+
DE13 in E1	0.562069	0.405746	0.26	NS
DE14 in E1	1.114442	1.050572	0.367	NS
DE23 in E1	-0.217579	1.660683	0.904	NS
DE24 in E1	-2.368299	0.651167	0.0358	S*

DE34 in E1	1.698030	0.881687	0.15	NS
DE11 in E2	0.751202	0.780806	0.407	NS
DE22 in E2	-4.653504	1.121175	0.0254	S*
DE33 in E2	-0.744776	1.086469	0.542	NS
DE44 in E2	-1.890872	0.707435	0.0755	S+
DE12 in E2	1.815819	0.552480	0.0462	S*
DE13 in E2	-0.926615	0.698261	0.276	NS
DE14 in E2	-1.611676	1.678116	0.408	NS
DE23 in E2	0.437429	0.800245	0.623	NS
DE24 in E2	8.238749	1.841553	0.0208	S*
DE34 in E2	-1.415766	1.261023	0.343	NS
Heterosis <Delta>	0.971038	0.40929	0.0983	S+

Fixed Effect , 12.8719

Fixed Effect , 19.885

Results of Fiber Yield are not presented.

Time Used (Hour) = 0.001389

## Output 2 for Covariance Analysis

Traits =, 2

Variance components = , 6

Degree of freedom = , 3

File name is cotdata.COV

Date and Time for Analysis: Thu Jun 22 22:00:24 2000

Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.  
Jackknifing Over Block Conducted for Estimating S.E.

NS = Not significant; S+ = Significant at 0.10 level.

S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Covariances and Correlations Between Bolls & FibYield, for Public Users:

Covariances	Estimates	S.E.	P-value	
Additive Cov	26.4031	15.0422	0.177	NS
Dominance Cov	3.68996	4.09328	0.434	NS
Add. * Env. Cov	5.2684	5.4782	0.407	NS
Dom. * Env. Cov	0.725936	6.15727	0.914	NS
Residual Cov	5.74197	4.7088	0.31	NS

Cov 1=Genotypic

Cov2=Phenotypic

	Estimates	S.E.	P-value	
Cov 2	41.8294	20.9549	0.14	NS
Cov 1	36.0874	21.3383	0.189	NS

Correlation	Estimates	S.E.	P-value	
Additive Cor	0.905414	0.326942	0.0696	S+
Dominance Cor	0.275228	0.243147	0.34	NS
Add. * Env. Cor	1.000000	0.288675	0.0405	S*
Dom. * Env. Cor	0.000000	0	1	NS



Residual Cor                    0.318575            0.229826            0.26            NS

Cor 1=Genotypic  
 Cor2=Phenotypic                Estimates            S.E.                P-value

Cor 2                            0.556778            0.215421            0.0815            S+

Cor 1                            0.635333            0.26869             0.099             S+

Time Used (Hour) = 0.000000

### **Output 3 for Heterosis Analysis**

Traits = , 2  
 Variance components = , 6  
 Degree of freedom = , 3  
 File name is cot8185.  
 Date and Time for Analysis: Thu Jun 22 22:15:40 2000

Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.  
 Jackknifing Over Block Conducted for Estimating S.E.  
 Genetic Effects by Adjusted Unbiased Prediction (AUP) Method.

NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Diallel Analysis of Trait, Bolls, for Public Users.

Var Comp	Estimate	S. E.	P-value	
Additive Var	7.30429	1.4425	0.00743	S**
Dominance Var	3.29035	0.935764	0.0195	S*
Add. * Env. Var	0.866537	0.683909	0.147	NS
Dom. * Env. Var	4.82386	1.71492	0.0336	S*
Residual Var	4.18772	0.555651	0.00242	S**

Heterosis Analysis of Trait, Bolls, for F2 Seeds with total mean =, 15.312341

No.	Cro	(F <sub>1</sub> ) (GE)	S.E.	P- value	Sig- nif.	(F <sub>2</sub> ) (GE)	S.E.	P- value	Sig- nif.
Cro 1	<E1> <1 * 2>	-0.962	0.471	0.134	NS	0.113	0.578	0.857	NS
Cro 2	<E1> <1 * 3>	0.573	0.406	0.253	NS	-0.018	0.213	0.938	NS
Cro 3	<E1> <1 * 4>	0.951	1.020	0.420	NS	0.227	0.366	0.579	NS
Cro 4	<E1> <2 * 3>	-0.054	1.673	0.976	NS	0.348	0.530	0.558	NS
Cro 5	<E1> <2 * 4>	-2.379	0.984	0.094	S+	-0.759	0.930	0.474	NS
Cro 6	<E1> <3 * 4>	1.366	0.489	0.068	S+	0.215	0.630	0.756	NS
Cro 7	<E2> <1 * 2>	2.021	1.222	0.197	NS	0.138	1.488	0.932	NS
Cro 8	<E2> <1 * 3>	-2.321	0.646	0.037	S*	-1.856	0.366	0.015	S*
Cro 9	<E2> <1 * 4>	-0.696	1.562	0.686	NS	-0.175	0.708	0.821	NS
Cro 10	<E2> <2 * 3>	-0.478	1.110	0.696	NS	-2.047	0.629	0.047	S*
Cro 11	<E2> <2 * 4>	9.633	1.556	0.008	S**	3.878	0.469	0.004	S**
Cro 12	<E2> <3 * 4>	-1.621	0.806	0.138	NS	-1.572	0.610	0.082	S+

Significance of F1 or F2 is over Population Mean 15.312341

No.	Cro	(F <sub>1</sub> ) (G)	S.E.	P- value	Sig- nif.	(F <sub>2</sub> ) (G)	S.E.	P- value	Sig- nif.
Cro 1	<1 * 2>	17.420	1.118	0.156	NS	16.747	1.233	0.329	NS
Cro 2	<1 * 3>	12.437	0.868	0.045	S*	12.367	0.732	0.028	S*

Cro 3	<1 * 4>	16.630	1.075	0.308	NS	16.374	0.748	0.251	NS
Cro 4	<2 * 3>	13.931	1.064	0.285	NS	12.971	0.832	0.067	S+
Cro 5	<2 * 4>	22.726	0.625	0.001	S**	19.279	0.832	0.018	S*
Cro 6	<3 * 4>	13.724	0.814	0.146	NS	12.889	1.033	0.101	NS

No.	Cro	H <sub>pm</sub> (F <sub>1</sub> )	S.E.	P-value	Sig-nif.	H <sub>pm</sub> (F <sub>2</sub> )	S.E.	P-value	Sig-nif.
Cro 1 <E1>	<1 * 2>	-0.140	0.034	0.027	S*	-0.070	0.017	0.027	S*
Cro 2 <E1>	<1 * 3>	0.077	0.030	0.079	S+	0.039	0.015	0.079	S+
Cro 3 <E1>	<1 * 4>	0.095	0.087	0.355	NS	0.047	0.043	0.355	NS
Cro 4 <E1>	<2 * 3>	-0.053	0.140	0.733	NS	-0.026	0.070	0.733	NS
Cro 5 <E1>	<2 * 4>	-0.212	0.059	0.038	S*	-0.106	0.030	0.038	S*
Cro 6 <E1>	<3 * 4>	0.150	0.115	0.283	NS	0.075	0.058	0.283	NS
Mean for		-0.014	0.059	0.830	NS	-0.007	0.029	0.830	NS
Env. Cro No. = 6									

Cro 7 <E2>	<1 * 2>	0.246	0.052	0.018	S*	0.123	0.026	0.018	S*
Cro 8 <E2>	<1 * 3>	-0.061	0.056	0.361	NS	-0.030	0.028	0.361	NS
Cro 9 <E2>	<1 * 4>	-0.068	0.153	0.686	NS	-0.034	0.076	0.686	NS
Cro 10 <E2>	<2 * 3>	0.205	0.074	0.071	S+	0.102	0.037	0.071	S+
Cro 11 <E2>	<2 * 4>	0.752	0.200	0.033	S*	0.376	0.100	0.033	S*
Cro 12 <E2>	<3 * 4>	-0.006	0.113	0.958	NS	-0.003	0.057	0.958	NS

Significance of F1 or F2 is over Population Mean 15.312341									
No.	Cro	H <sub>pm</sub> (F <sub>1</sub> ) (G)	S.E.	P-value	Sig-nif.	H <sub>pm</sub> (F <sub>2</sub> ) (G)	S.E.	P-value	Sig-nif.
Cro 1	<1 * 2>	0.088	0.031	0.067	S+	0.044	0.016	0.067	S+
Cro 2	<1 * 3>	0.009	0.027	0.754	NS	0.005	0.013	0.754	NS
Cro 3	<1 * 4>	0.033	0.078	0.696	NS	0.017	0.039	0.696	NS
Cro 4	<2 * 3>	0.125	0.072	0.181	NS	0.063	0.036	0.181	NS
Cro 5	<2 * 4>	0.450	0.083	0.012	S*	0.225	0.042	0.012	S*
Cro 6	<3 * 4>	0.109	0.075	0.241	NS	0.055	0.037	0.241	NS

No.	Cro	H <sub>pb</sub> (F <sub>1</sub> )	S.E.	P-value	Sig-nif.	H <sub>pb</sub> (F <sub>2</sub> )	S.E.	P-value	Sig-nif.
Cro 1 <E1>	<1 * 2>	-0.229	0.003	0.000	S**	-0.159	0.019	0.004	S**
Cro 2 <E1>	<1 * 3>	0.049	0.012	0.025	S*	0.010	0.017	0.595	NS
Cro 3 <E1>	<1 * 4>	0.073	0.107	0.542	NS	0.026	0.069	0.732	NS
Cro 4 <E1>	<2 * 3>	-0.170	0.128	0.277	NS	-0.144	0.068	0.123	NS
Cro 5 <E1>	<2 * 4>	-0.322	0.077	0.025	S*	-0.216	0.054	0.029	S*
Cro 6 <E1>	<3 * 4>	0.143	0.114	0.297	NS	0.068	0.056	0.315	NS
Cro 7 <E2>	<1 * 2>	0.101	0.048	0.128	NS	-0.022	0.034	0.563	NS
Cro 8 <E2>	<1 * 3>	-0.183	0.118	0.219	NS	-0.152	0.095	0.206	NS
Cro 9 <E2>	<1 * 4>	-0.077	0.163	0.670	NS	-0.043	0.087	0.657	NS
Cro 10 <E2>	<2 * 3>	0.182	0.116	0.215	NS	0.079	0.126	0.573	NS
Cro 11 <E2>	<2 * 4>	0.615	0.151	0.027	S*	0.239	0.055	0.023	S*
Cro 12 <E2>	<3 * 4>	-0.120	0.165	0.520	NS	-0.117	0.111	0.369	NS

Significance of F1 or F2 is over Population Mean 15.312341									
No.	Cro	H <sub>pb</sub> (F <sub>1</sub> ) (G)	S.E.	P-value	Sig-nif.	H <sub>pb</sub> (F <sub>2</sub> ) (G)	S.E.	P-value	Sig-nif.
Cro 1	<1 * 2>	0.069	0.040	0.183	NS	0.025	0.029	0.445	NS
Cro 2	<1 * 3>	-0.256	0.081	0.050	S+	-0.261	0.091	0.064	S+
Cro 3	<1 * 4>	0.018	0.088	0.854	NS	0.001	0.049	0.987	NS
Cro 4	<2 * 3>	-0.121	0.092	0.278	NS	-0.184	0.071	0.081	S+
Cro 5	<2 * 4>	0.447	0.076	0.010	S**	0.222	0.036	0.008	S**
Cro 6	<3 * 4>	-0.140	0.082	0.184	NS	-0.195	0.050	0.030	S*

Significance of Heterosis is over Population Mean 15.312341

Pre (F <sub>1</sub> )	16.4871	0.580926	0.136	NS
Pre (F <sub>2</sub> )	15.4467	0.665146	0.853	NS
Hpm (F <sub>1</sub> )	0.135267	0.030647	0.0216	S*
Hpm (F <sub>2</sub> )	0.067634	0.015324	0.0216	S*
Hpb (F <sub>1</sub> )	-0.04533	0.042593	0.365	NS
Hpb (F <sub>2</sub> )	-0.11297	0.035282	0.0493	S*

Results of Fiber yield are not presented.

Time Used (Hour) = 0.000278

## Chapter 4

# Diallel Analysis for an Additive-Dominance-Epistasis Model with Genotype-by-Environment Interaction Effects

Jun Zhu

### *Purpose*

To analyze balanced or unbalanced data of an additive x dominance (AD) + additive x additive (AA) genetic model for estimating components of variance, covariance, heritability, and selection response.

### *Definitions*

#### *Mating Design*

A set of inbred lines is sampled from a reference population. Parents are used to produce  $F_1$  crosses and their  $F_2$ . Experiments with parents,  $F_1$ s, and  $F_2$ s are conducted in multiple environments using a randomized complete block design.

#### *Genetic Model*

The genetic model for genetic entry of the  $k$ th type of generation derived from parents  $i$  and  $j$  in the  $l$ th block within the  $h$ th environment is

$$y_{ijkl} = \mu + E_h + G_{ijk} + GE_{hijk} + B_{hl} + e_{ijkl}$$

where  $\mu$  = population mean,  $E_h$  = environment effect,  $G_{ijk}$  = total genotypic effect,  $GE_{hijk}$  = genotype x environment interaction effect,  $B_{hl}$  = block effect, and  $e_{ijkl}$  = residual effect.

For parent ( $P_i, k = 0$ ):

$$G_{ii0} \quad GE_{hii0} \quad 2A_i \quad D_{ii} \quad 4AA_{ii} \quad 2AE_{hi} \quad DE_{hii} \quad 4AAE_{hii}$$

For  $F_1$  ( $P_i \times P_j, k = 1$ ):

$$G_{ij1} \quad GE_{hij1} \quad A_i \quad A_j \quad D_{ij} \quad AA_{ii} \quad AA_{jj} \quad 2AA_{ij} \quad AE_{hi} \\ AE_{hj} \quad DE_{hij} \quad AAE_{hii} \quad AAE_{hjj} \quad 2AAE_{hij}$$

For  $F_2$  ( $F_1 \otimes, k = 2$ ):

$$G_{ij2} \quad GE_{hij2} \quad A_i \quad A_j \quad \frac{1}{4}D_{ij} \quad \frac{1}{4}D_{ii} \quad \frac{1}{2}D_{jj} \quad AA_{ii} \quad AA_{jj} \quad 2AA_{ij} \\ AE_{hi} \quad AE_{hj} \quad \frac{1}{4}DE_{hii} \quad \frac{1}{4}DE_{hjj} \quad \frac{1}{2}DE_{hij} \\ AAE_{hii} \quad AAE_{hjj} \quad 2AAE_{hij}$$

where  $A$  = additive effect,  $D$  = dominance effect,  $AA$  = additive by additive epistatic effect,  $AE$  = additive by environment interaction effect,  $DE$  = dominance by environment interaction effect, and  $AAE$  = epistasis by environment interaction effect.

## Analysis Methodology

### Mixed Linear Model

The phenotypic mean of the genetic model can be expressed by a mixed linear model as

$$y = Xb + \begin{matrix} U_A e_A \\ U_D e_D \\ U_{AA} e_{AA} \\ U_{AE} e_{AE} \\ U_{DE} e_{DE} \\ U_{AAE} e_{AAE} \\ U_B e_B \\ e_e \end{matrix} + \begin{matrix} U_u e_u \end{matrix}$$

with variance-covariance matrix

$$\text{var}(y) = \begin{matrix} \sigma^2 U_A U_A^T & \sigma^2 U_D U_D^T & \sigma^2 U_{AA} U_{AA}^T & \sigma^2 U_{AE} U_{AE}^T & & & & & \\ & \sigma^2 U_{DE} U_{DE}^T & \sigma^2 U_{AAE} U_{AAE}^T & \sigma^2 U_B U_B^T & \sigma^2 I & & & & \\ & & & & & \sigma^2 U_u U_u^T & & & \\ & & & & & & & & \end{matrix}$$

### Variance Components

Unbiased estimation of variances can be obtained by restricted maximum likelihood (REML) or MINQUE(1) approaches. When experimental variances ( $\sigma_u^2$ ) are estimated, genetic variance components can be obtained by  $V_A$ ,  $2\sigma_A^2$ ,  $V_D$ ,  $\sigma_D^2$ ,  $V_{AA}$ ,  $4\sigma_{AA}^2$ ,  $V_{AE}$ ,  $2\sigma_{AE}^2$ ,  $V_{DE}$ ,  $\sigma_{DE}^2$ ,  $V_{AAE}$ ,  $4\sigma_{AAE}^2$ ,  $V_e$ ,  $\sigma_e^2$ . The total phenotypic variance is  $V_P = V_A + V_D + V_{AA} + V_{AE} + V_{DE} + V_{AAE} + V_e$ .

### Covariance Components and Correlation

Unbiased estimation of covariances can be obtained by MINQUE(1) approaches (Zhu, 1992; Zhu and Weir, 1996). When experimental covariances ( $\sigma_{u/u}$ ) are estimated, genetic covariance components can be obtained by  $C_A$ ,  $2\sigma_{AA}$ ,  $C_D$ ,  $\sigma_{DD}$ ,  $C_{AA}$ ,  $4\sigma_{AA/AA}$ ,  $C_{AE}$ ,  $2\sigma_{AE/AE}$ ,  $C_{DE}$ ,  $\sigma_{DE/DE}$ ,  $C_{AAE}$ ,  $4\sigma_{AAE/AAE}$ ,  $C_e$ ,  $\sigma_{ee}$ . The total phenotypic covariance is  $C_P = C_A + C_D + C_{AA} + C_{AE} + C_{DE} + C_{AAE} + C_e$ . For trait 1 and trait 2, correlation coefficients of genetic components can be estimated by  $r_A = C_A / \sqrt{V_{A(1)}V_{A(2)}}$ ,  $r_D = C_D / \sqrt{V_{D(1)}V_{D(2)}}$ ,  $r_{AA} = C_{AA} / \sqrt{V_{AA(1)}V_{AA(2)}}$ ,  $r_{AE} = C_{AE} / \sqrt{V_{AE(1)}V_{AE(2)}}$ ,  $r_{DE} = C_{DE} / \sqrt{V_{DE(1)}V_{DE(2)}}$ ,  $r_{AAE} = C_{AAE} / \sqrt{V_{AAE(1)}V_{AAE(2)}}$ , and  $r_e = C_e / \sqrt{V_{e(1)}V_{e(2)}}$ .

### Heritability Components

The total heritability ( $h^2$ ) can be partitioned into two components ( $h^2 = h_G^2 + h_{GE}^2$ ), where  $h_G^2 = (V_A + V_{AA})/V_P$  is general heritability and  $h_{GE}^2 = (V_{AE} + V_{AAE})/V_P$  is interaction heritability (Zhu, 1997).

### Selection Response

The total selection response ( $R = ih^2\sqrt{V_P}$ ) can be partitioned into two components (Zhu, 1997):

$$R = R_G + R_{GE}$$

where  $R_G = ih_G^2\sqrt{V_P}$  is general response and  $R_{GE} = ih_{GE}^2\sqrt{V_P}$  is interaction response.

## Heterosis Components

Prediction of genetic merits can be obtained by use of the linear unbiased prediction (LUP) method (Zhu, 1992; Zhu and Weir, 1996) or the adjusted unbiased prediction (AUP) method (Zhu, 1993; Zhu and Weir, 1996). Predicted genotypic effects and  $GE$  interaction effects can be further used in analyzing heterosis of different generations (Zhu, 1997). Heterosis in specific environments consists of two components. General heterosis is due to genotypic effects and can be expected in overall environments, and interaction heterosis is a deviant of  $GE$  interaction relative to specific environments. The two components of heterosis relative to midparent or relative to better parent can be calculated as follows:

General heterosis of  $F_n$  relative to midparent:

$$H_M(F_n) = \left(\frac{1}{2}\right)^{n-1} D_D 2$$

Interaction heterosis of  $F_n$  relative to midparent:

$$H_{ME}(F_n) = \left(\frac{1}{2}\right)^{n-1} DE_{AAE} 2$$

General heterosis of  $F_n$  relative to better parent ( $P_i$ ):

$$H_B(F_n) = H_M(F_n) - \frac{1}{2} G_G$$

Interaction heterosis of  $F_n$  relative to better parent ( $P_i$ ):

$$H_{BE}(F_n) = H_{ME}(F_n) - \frac{1}{2} GE_{GE}$$

where  $D_D D_{ij} - \frac{1}{2}(D_{ii} + D_{jj})$  is dominance heterosis,  $DE_{DE} DE_{hij} - \frac{1}{2}(DE_{hii} + DE_{hjj})$  is  $DE$  interaction heterosis,  $G_G |G(P_i) - G(P_j)|$  is parental genotypic difference, and  $GE_{GE} |GE(P_i) - GE(P_j)|$  is parental interaction difference.

Heterosis based on population mean ( $H_{PM} = \frac{1}{\mu} H_M$ ,  $H_{PME} = \frac{1}{\mu} H_{ME}$ ,  $H_{PB} = \frac{1}{\mu} H_B$ , or  $H_{PBE} = \frac{1}{\mu} H_{BE}$ ) can be used to compare proportion of heterosis among different traits.

## Originators

- Zhu, J. (1992). Mixed model approaches for estimating genetic variances and covariances. *Journal of Biomathematics* 7(1):1-11.
- Zhu, J. (1993). Methods of predicting genotype value and heterosis for offspring of hybrids (Chinese). *Journal of Biomathematics* 8(1):32-44.
- Zhu, J. (1997). *Analysis Methods for Genetic Models*. Agricultural Publication House of China, Beijing.
- Zhu, J. and Weir, B.S. (1996). Diallel analysis for sex-linked and maternal effects. *Theoretical and Applied Genetics* 92(1):1-9.

## Software Available

Zhu, J. (1997). GENAD.EXE for constructing AD model, GENVAR1.EXE for estimating components of variance and heritability, GENCOV1.EXE for estimating components of covariance and correlation, GENHET1.EXE for predicting genetic effects and components of heterosis. *Analysis Methods for Genetic Models* (pp. 278-285). Agricultural Publication House of China, Beijing (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.

## EXAMPLE

Unbalanced data (COTADAA.TXT) to be analyzed (Parent = 10, Year = 2, Generation = P, F<sub>1</sub>, F<sub>2</sub>, Blk = 1):

Year	Male	Fem	Gen	Blk	Bolls	Lint%
1	1	1	0	1	10.39	37.16
1	1	6	1	1	16.69	39.29
1	1	6	2	1	15.05	37.68
1	1	7	1	1	18.27	40.92
1	1	7	2	1	14.44	38.35
1	1	9	1	1	13.36	36.43
1	1	9	2	1	12.37	36.1
1	1	10	1	1	14.57	33.45
1	1	10	2	1	11.52	34.81
1	2	2	0	1	18.06	34.95
1	2	6	1	1	16.65	38.28
1	2	6	2	1	15.43	39.5
1	2	7	1	1	17.67	39.27
1	2	7	2	1	18.82	38.43
1	2	8	1	1	19.89	38.22
1	2	8	2	1	12.65	35.44
1	2	9	1	1	18.03	34.57
1	2	9	2	1	15.45	35.51
1	2	10	1	1	17.08	33.69
1	2	10	2	1	16.1	29.89
1	3	3	0	1	11.03	39.53
1	3	7	1	1	17.52	42.46
1	3	7	2	1	13.99	39.38
1	3	9	1	1	14.56	37.04
1	3	9	2	1	12.28	38.27
1	3	10	1	1	13.27	37.83
1	3	10	2	1	16.42	39.14
1	4	4	0	1	16.54	40.8
1	4	6	1	1	17.11	40.34
1	4	6	2	1	14.58	40.77
1	4	8	1	1	16.7	40.92
1	4	8	2	1	14.7	39.72
1	4	9	1	1	17.1	38.7
1	4	9	2	1	17.34	38.41



1	4	10	1	1	14.14	36.54
1	4	10	2	1	13.86	36.99
1	5	5	0	1	13.89	40.49
1	5	7	1	1	18.57	41.6
1	5	7	2	1	14.53	41.53
1	5	8	1	1	17.27	40.33
1	5	8	2	1	16.1	39.9
1	5	9	1	1	16.31	39.16
1	5	9	2	1	14.82	39.92
1	5	10	1	1	16.98	37.65
1	5	10	2	1	12.22	37.3
1	6	6	0	1	16.66	39.1
1	7	7	0	1	18.35	42.04
1	8	8	0	1	13.49	38.81
1	9	9	0	1	12.91	35.98
1	10	10	0	1	11.52	30.89
2	1	1	0	1	10.09	37.69
2	1	6	1	1	10.82	41.92
2	1	6	2	1	11.13	38.06
2	1	7	1	1	7.97	40.53
2	1	7	2	1	11.08	41.2
2	1	9	1	1	8.22	37.49
2	1	9	2	1	9.85	37.45
2	1	10	1	1	7.26	33.81
2	1	10	2	1	8.52	33.53
2	2	2	0	1	9.87	39.3
2	2	6	1	1	12.31	40.64
2	2	6	2	1	11.95	41.35
2	2	7	1	1	11.3	42.04
2	2	7	2	1	9.98	40.17
2	2	8	1	1	13.5	39.85
2	2	8	2	1	11.47	37.64
2	2	9	1	1	11.93	37.71
2	2	9	2	1	10.83	37.45
2	2	10	1	1	8.23	34.59
2	2	10	2	1	11.1	34.01
2	3	3	0	1	6.4	39.44
2	3	7	1	1	8	42.68
2	3	7	2	1	9.09	43.29
2	3	9	1	1	11.49	37.92
2	3	9	2	1	10.78	38.9
2	3	10	1	1	7.32	34.76
2	3	10	2	1	10.9	38.42
2	4	4	0	1	8.83	42.65
2	4	6	1	1	11.37	42.67
2	4	6	2	1	11.77	41.45
2	4	8	1	1	13.07	41.84
2	4	8	2	1	11.18	42.27
2	4	9	1	1	10.63	38.12
2	4	9	2	1	11.47	41.08
2	4	10	1	1	10.43	39.06
2	4	10	2	1	11.84	37.58
2	5	5	0	1	11.37	42.86
2	5	7	1	1	12.03	42.65
2	5	7	2	1	10.69	44.69
2	5	8	1	1	10.2	40.36
2	5	8	2	1	10.09	39.53

2	5	9	1	1	10.47	40.31
2	5	9	2	1	10.89	40.03
2	5	10	1	1	10.33	38.78
2	5	10	2	1	8.95	39.09
2	6	6	0	1	11.24	38.6
2	7	7	0	1	10.67	43.22
2	8	8	0	1	10.77	40.74
2	9	9	0	1	6.87	37.43
2	10	10	0	1	11.69	35.05

1. Run GENADE.EXE to create mating design matrix files and data for additive-dominance-epistasis (AD+AA) models. The data files (COTADAA.TXT) should have five columns: (1) environment, (2) maternal, (3) paternal, (4) generation, and (5) replication. There is a limitation (<100 traits) for the number of trait columns. An example of a data file is provided under the name COTADAA.TXT.
2. Run programs for variance and covariance analyses. Standard errors of estimates are calculated using jackknife procedures. If you have multiple blocks for your experiments, you can use GENVAR1R.EXE or GENCOV1R.EXE for jackknifing over blocks. Otherwise you can use GENVAR1C.EXE or GENCOV1C.EXE for jackknifing over cell means.
3. Run GENVAR1R.EXE or GENVAR1C.EXE for estimating variance components and predicting genetic effects before estimating covariance and correlation. The two programs in Step 2 will allow you to choose the parental type (inbred or outbred) and the prediction methods (LUP or AUP). You also need to input coefficients (1, 0, or -1) for conducting linear contrasts for genetic effects of parents.
4. After you finish variance analysis, you can run GENCOV1R.EXE or GENCOV1C.EXE for estimating covariance components and coefficients of correlation among all the traits analyzed.
5. If you want to predict heterosis and genotypic value for each  $F_1$  or  $F_2$  cross by an AD model, you can run GENHET1R.EXE or GENHET1C.EXE.
6. All results are automatically stored in text files for later use or printing. Examples of output files are provided with the names COTADAA.VAR for analysis of variance and genetic effects, COTADAA.PRE for heterosis, and COTADAA.COR for analysis of covariances and correlation.

**Output 1 for Variance Analysis**

Traits =, 2  
 Variance components = , 7  
 Degree of freedom = , 99  
 File name is COTADAA.VAR  
 Date and Time for Analysis: Fri Jun 23 08:33:02 2000

Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.  
 Jackknifing Over Block Conducted for Estimating S.E.  
 Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP)  
 Method.

NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Linear Contrast Test:

+<1> +<2> +<3> +<4> +<5> -<6> -<7> -<8> -<9> -<10>

Diallel Analysis of Trait, Bolls, for Public Users.

Var Comp	Estimate	S. E.	P-value	
(1): Additive Var	2.36714	0.474734	1.31e-006	S**
(2): Dominance Var	12.4508	2.25708	1.39e-007	S**
(3): Add.*Add. Var	3.48369	0.502654	1.9e-010	S**
(4): Add. * Env. Var	3.59761	0.745664	2.55e-006	S**
(5): Dom. * Env. Var	16.8931	2.83894	2.03e-008	S**
(6): (AA) * Env. Var	0	0	1	NS
(7): Residual Var	3.12779	0.712819	1.43e-005	S**
(8): Var(Pheno.)	41.9202	4.31614	2.55e-011	S**

Proportion of Var(G)/Var(T)	Estimate	S. E.	P-value	
(1): Additive Var/Vp	0.0564678	0.0211358	0.00441	S**
(2): Dominance Var/Vp	0.297013	0.0369701	2.44e-011	S**
(3): Add.*Add. Var/Vp	0.0831029	0.0214262	9.46e-005	S**
(4): Add. * Env. Var/Vp	0.0858205	0.0120405	5.86e-011	S**
(5): Dom. * Env. Var/Vp	0.402983	0.0341788	2.55e-011	S**
(6): (AA) * Env. Var/Vp	0	0	1	NS
(7): Residual Var/Vp	0.0746131	0.0151876	1.78e-006	S**

Heritability	Estimate	S. E.	P-value	
(8): Heritability(N)	0.139571	0.0266373	4.55e-007	S**
(9): Heritability(B)	0.436584	0.0348678	2.55e-011	S**
(10): Heritability(NE)	0.0858205	0.0120405	5.86e-011	S**
(11): Heritability(BE)	0.488803	0.03613	-2.55e-011	S**

Genetic Predictor, S.E., P-value for Two-tail t-test

(1): Random Effect is Additive Effects				
A1	0.020391	1.046932	0.984	NS
A2	-0.172118	0.865219	0.843	NS
A3	0.243015	0.933404	0.795	NS
A4	0.024512	0.610581	0.968	NS
A5	-0.198413	0.284266	0.487	NS
A6	-0.045113	0.559257	0.936	NS
A7	-0.006029	0.525715	0.991	NS

A8	-0.242755	0.336519	0.472	NS
A9	0.177528	0.247130	0.474	NS
A10	0.197105	0.780527	0.801	NS
Linear Contrast	-0.237404	11.14	0.983	NS

## (2): Random Effect is Dominance Effects

D1*1	-1.985631	1.605723	0.219	NS
D2*2	-4.853828	3.095245	0.12	NS
D3*3	-0.293169	0.924650	0.752	NS
D4*4	-1.707263	1.061605	0.111	NS
D5*5	-7.790652	3.617237	0.0337	S*
D6*6	-2.681446	1.218021	0.03	S*
D7*7	-4.154995	2.393013	0.0856	S+
D8*8	-7.236830	3.889634	0.0658	S+
D9*9	-3.026015	1.713898	0.0806	S+
D10*10	1.364409	1.417177	0.338	NS
D1*6	1.844893	1.020188	0.0736	S+
D1*7	0.088293	2.692258	0.974	NS
D1*9	-2.270995	1.155729	0.0522	S+
D1*10	2.668295	1.548696	0.088	S+
D2*6	1.351880	0.655828	0.0419	S*
D2*7	-1.297874	1.003310	0.199	NS
D2*8	9.815433	5.523754	0.0786	S+
D2*9	5.188726	2.350358	0.0296	S*
D2*10	-4.090970	1.895508	0.0333	S*
D3*7	3.495850	2.000000	0.0836	S+
D3*9	4.970930	2.262232	0.0303	S*
D3*10	-9.112045	4.458072	0.0436	S*
D4*6	2.946256	1.541041	0.0588	S+
D4*8	5.140935	2.364873	0.0321	S*
D4*9	-1.798652	0.660681	0.00766	S**
D4*10	-1.958099	0.910923	0.034	S*
D5*7	6.710816	3.253640	0.0418	S*
D5*8	-0.368711	0.290930	0.208	NS
D5*9	0.235750	0.576913	0.684	NS
D5*10	8.804042	3.903617	0.0263	S*
Heterosis <Delta>	2.90056	12.8407	0.822	NS

## (3): Random Effect is Add.\*Add. Effects

AA1*1	-1.827866	0.885620	0.0416	S*
AA2*2	1.857440	0.692252	0.00855	S**
AA3*3	-3.923112	1.819274	0.0335	S*
AA4*4	-0.427958	0.372799	0.254	NS
AA5*5	1.095843	0.431401	0.0126	S*
AA6*6	1.074095	0.485307	0.0292	S*
AA7*7	2.010456	0.866196	0.0223	S*
AA8*8	0.866474	0.254778	0.00097	S**
AA9*9	-2.618613	1.297275	0.0462	S*
AA10*10	-1.434506	0.678498	0.037	S*
AA1*6	1.127468	0.554236	0.0446	S*
AA1*7	0.260405	0.142121	0.0699	S+
AA1*9	-0.626353	0.353682	0.0796	S+
AA1*10	-2.892538	1.389233	0.0399	S*
AA2*6	-0.039485	0.150785	0.794	NS
AA2*7	0.997226	0.482695	0.0414	S*
AA2*8	-2.373975	1.062655	0.0277	S*
AA2*9	0.916657	0.551207	0.0995	S+

AA2*10	0.966337	0.475264	0.0447	S*
AA3*7	-1.240906	0.602029	0.0419	S*
AA3*9	0.736135	0.560053	0.192	NS
AA3*10	3.882660	1.687257	0.0235	S*
AA4*6	-0.333696	0.292460	0.257	NS
AA4*8	0.232070	0.281352	0.411	NS
AA4*9	3.758026	1.714850	0.0308	S*
AA4*10	0.453800	0.251847	0.0746	S+
AA5*7	-1.360470	0.556477	0.0163	S*
AA5*8	0.698657	0.311950	0.0274	S*
AA5*9	1.219364	0.571954	0.0355	S*
AA5*10	-3.054544	1.399209	0.0314	S*
Heterosis <Delta>	1.12761	5.66678	0.843	NS

## (4): Random Effect is Add. \* Env. Effects

AE1 in E1	-1.871303	1.336265	0.165	NS
AE2 in E1	1.679535	1.500118	0.266	NS
AE3 in E1	-0.899398	0.974282	0.358	NS
AE4 in E1	0.355846	0.398988	0.375	NS
AE5 in E1	0.613201	0.505110	0.228	NS
AE6 in E1	-0.319194	0.433700	0.463	NS
AE7 in E1	3.154071	2.503520	0.211	NS
AE8 in E1	-1.709535	0.955588	0.0767	S+
AE9 in E1	-1.004626	0.705371	0.158	NS
AE10 in E1	0.000037	0.749113	1	NS
AE1 in E2	-0.687704	0.654509	0.296	NS
AE2 in E2	0.130732	0.339243	0.701	NS
AE3 in E2	-1.165105	0.703354	0.101	NS
AE4 in E2	1.212089	0.914817	0.188	NS
AE5 in E2	-0.818562	0.501433	0.106	NS
AE6 in E2	1.647312	1.146417	0.154	NS
AE7 in E2	-2.111514	1.652810	0.204	NS
AE8 in E2	1.666313	1.018155	0.105	NS
AE9 in E2	1.460007	0.882265	0.101	NS
AE10 in E2	-1.334250	0.692084	0.0567	S+
Linear Contrast	-0.000322198	0.00010415	0.00257	S**

## (5): Random Effect is Dom. \* Env. Effects

DE11 in E1	-7.339941	3.362180	0.0314	S*
DE22 in E1	-5.544965	3.293144	0.0954	S+
DE33 in E1	-1.685938	2.763209	0.543	NS
DE44 in E1	-1.592941	1.468080	0.281	NS
DE55 in E1	-6.919656	3.156330	0.0307	S*
DE66 in E1	-2.769618	1.534016	0.074	S+
DE77 in E1	-5.708889	3.470978	0.103	NS
DE88 in E1	-6.906281	3.149161	0.0306	S*
DE99 in E1	-3.155495	1.695257	0.0657	S+
DE1010 in E1	-4.448080	3.583114	0.217	NS
DE16 in E1	1.945276	1.444322	0.181	NS
DE17 in E1	6.019940	4.117258	0.147	NS
DE19 in E1	0.953192	0.789965	0.23	NS
DE110 in E1	5.306395	3.178059	0.0981	S+
DE26 in E1	0.018365	0.840712	0.983	NS
DE27 in E1	-4.879109	2.046507	0.019	S*
DE28 in E1	11.874683	6.855778	0.0864	S+
DE29 in E1	2.481694	2.213078	0.265	NS
DE210 in E1	1.704185	1.338270	0.206	NS

DE37 in E1	5.935123	3.679177	0.11	NS
DE39 in E1	2.916905	2.004578	0.149	NS
DE310 in E1	-5.481360	3.413565	0.112	NS
DE46 in E1	3.541911	2.501341	0.16	NS
DE48 in E1	1.163906	1.499863	0.44	NS
DE49 in E1	-1.462106	0.664229	0.03	S*
DE410 in E1	0.093319	0.547534	0.865	NS
DE57 in E1	5.091230	3.513362	0.15	NS
DE58 in E1	0.249648	0.907277	0.784	NS
DE59 in E1	1.192191	1.072943	0.269	NS
DE510 in E1	7.405446	4.610249	0.111	NS
DE11 in E2	6.233934	2.649984	0.0206	S*
DE22 in E2	0.070564	1.631085	0.966	NS
DE33 in E2	2.860760	1.834532	0.122	NS
DE44 in E2	0.496960	1.260403	0.694	NS
DE55 in E2	0.762586	0.976264	0.437	NS
DE66 in E2	0.750042	0.589078	0.206	NS
DE77 in E2	2.513161	1.959827	0.203	NS
DE88 in E2	-0.681558	1.133328	0.549	NS
DE99 in E2	1.396232	1.222769	0.256	NS
DE1010 in E2	6.754486	3.043240	0.0287	S*
DE16 in E2	-0.782136	0.571314	0.174	NS
DE17 in E2	-6.286620	3.932846	0.113	NS
DE19 in E2	-2.727444	1.812851	0.136	NS
DE110 in E2	-2.626815	1.660283	0.117	NS
DE26 in E2	0.500294	0.497259	0.317	NS
DE27 in E2	2.695619	1.378225	0.0533	S+
DE28 in E2	0.710618	1.939384	0.715	NS
DE29 in E2	1.408633	0.928007	0.132	NS
DE210 in E2	-5.416844	3.370826	0.111	NS
DE37 in E2	-2.775914	1.748225	0.116	NS
DE39 in E2	1.697015	1.049894	0.109	NS
DE310 in E2	-4.892908	3.552561	0.172	NS
DE46 in E2	-0.956358	0.906075	0.294	NS
DE48 in E2	2.794023	1.735292	0.111	NS
DE49 in E2	-1.011061	1.141284	0.378	NS
DE410 in E2	-1.635955	1.322434	0.219	NS
DE57 in E2	0.749728	1.094644	0.495	NS
DE58 in E2	-1.851171	0.743874	0.0145	S*
DE59 in E2	-1.672750	0.952113	0.082	S+
DE510 in E2	0.922233	1.377869	0.505	NS

(6): Random Effect is (AA) \* Env. Effects  
No Significant Effects.

Fixed Effect <1>, 15.345  
Fixed Effect <2>, 10.3648

Results of Lint% are not presented.

Time Used (Hour) = 0.004722

## ***Output 2 for Covariance Analysis***

Traits =, 2

Covariance components = , 7  
 Degree of freedom = , 99  
 File name is COTADAA.COV  
 Date and Time for Analysis: Fri Jun 23 08:33:35 2000

Covariance Components Estimated by MINQUE(1) with GENCOV1C.EXE.  
 Jackknifing Over Cell Mean Conducted for Estimating S.E.

NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Covariances and Correlations Between, Bolls, , &, Lint%, for Public Users.:

Covariances	Estimates	S.E.	P-value	
Additive Cov	-0.165704	0.968417	0.864	NS
Dominance Cov	0.802175	2.31849	0.73	NS
Add.*Add. Cov	0.52236	0.79344	0.512	NS
Add. * Env. Cov	-0.585695	0.668664	0.383	NS
Dom. * Env. Cov	1.44656	2.09928	0.492	NS
(AA) * Env. Cov	-0.116658	1.07689	0.914	NS
Residual Cov	0.192467	0.376523	0.61	NS

Cov<1=Genotypic>	Estimates	S.E.	P-value	
Cov <2=Phenotypic>	2.09551	1.35407	0.125	NS
Cov 1	1.90304	1.35435	0.163	NS

Correlation	Estimates	S.E.	P-value	
Additive Cor	-0.043057	0.0498808	0.39	NS
Dominance Cor	0.100186	0.0495757	0.046	S *
Add.*Add. Cor	0.174520	0.0516629	0.00104	S **
Add. * Env. Cor	-0.207088	0.0362769	1.19e-007	S **
Dom. * Env. Cor	0.000000	0	1	NS
(AA) * Env. Cor	0.000000	0	1	NS
Residual Cor	0.079717	0.0377952	0.0375	S *

Cor <1=Genotypic>	Estimates	S.E.	P-value	
Cor <2=Phenotypic>	0.073183	0.0448333	0.106	NS
Cor 1	0.072636	0.0500355	0.15	NS

Time Used (Hour) = 0.003056

### ***Output 3 for Heterosis Analysis***

Traits = , 2  
 Variance components = , 7  
 Degree of freedom = , 99  
 File name is COTADJM.PRE  
 Date and Time for Analysis: Fri Jun 23 08:34:07 2000

Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.  
 Jackknifing Over Block Conducted for Estimating S.E.

Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP)  
Method.

NS = Not significant; S+ = Significant at 0.10 level.

S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Var Comp, Estimate, S. E. , P-value of One Tail t-test of, Bolls, for  
Public Users.

Additive Var	2.36728	0.474749	1.31e-006	S **
Dominance Var	12.4508	2.25708	1.39e-007	S **
Add.*Add. Var	3.48381	0.502665	1.9e-010	S **
Add. * Env. Var	3.59769	0.745673	2.54e-006	S **
Dom. * Env. Var	16.893	2.83894	2.03e-008	S **
(AA) * Env. Var	0	0	0.5	NS
Residual Var	3.12783	0.712823	1.43e-005	S **

Heterosis Analysis of Trait, Bolls, for F<sub>2</sub> Seeds with total mean =,  
12.854884

No.	Cross	F1 (GE)	S.E.	P-value	Sig.	F2 (GE)	S.E.	P-value	Sig.
Cro 1 <E1>	<1 * 6>	-0.25	1.85	0.90	NS	-3.75	1.57	0.02	S *
Cro 2 <E1>	<1 * 7>	7.30	4.14	0.08	S +	1.03	1.39	0.46	NS
Cro 3 <E1>	<1 * 9>	-1.92	1.60	0.23	NS	-5.02	1.88	0.01	S **
Cro 4 <E1>	<1 * 10>	3.44	3.50	0.33	NS	-2.17	2.05	0.29	NS
Cro 5 <E1>	<2 * 6>	1.38	1.17	0.24	NS	-0.71	1.26	0.57	NS
Cro 6 <E1>	<2 * 7>	-0.04	3.21	0.99	NS	-0.42	2.55	0.87	NS
Cro 7 <E1>	<2 * 8>	11.84	6.84	0.09	S +	2.79	2.30	0.23	NS
Cro 8 <E1>	<2 * 9>	3.16	2.41	0.19	NS	-0.26	1.40	0.85	NS
Cro 9 <E1>	<2 * 10>	3.38	1.63	0.04	S *	0.03	1.43	0.98	NS
Cro 10 <E1>	<3 * 7>	8.19	4.09	0.05	S *	3.37	1.89	0.08	S +
Cro 11 <E1>	<3 * 9>	1.01	2.25	0.65	NS	-1.66	1.67	0.32	NS
Cro 12 <E1>	<3 * 10>	-6.38	3.52	0.07	S +	-5.17	2.04	0.01	S *
Cro 13 <E1>	<4 * 6>	3.58	2.53	0.16	NS	0.72	0.98	0.47	NS
Cro 14 <E1>	<4 * 8>	-0.19	1.73	0.91	NS	-2.90	1.47	0.05	S +
Cro 15 <E1>	<4 * 9>	-2.11	0.82	0.01	S *	-2.57	0.89	0.00	S **
Cro 16 <E1>	<4 * 10>	0.45	0.81	0.58	NS	-1.11	1.39	0.43	NS
Cro 17 <E1>	<5 * 7>	8.86	4.38	0.05	S *	3.16	2.50	0.21	NS
Cro 18 <E1>	<5 * 8>	-0.85	1.20	0.48	NS	-4.43	1.51	0.00	S **
Cro 19 <E1>	<5 * 9>	0.80	1.22	0.51	NS	-2.31	1.20	0.06	S +
Cro 20 <E1>	<5 * 10>	8.02	4.80	0.10	S +	1.47	1.73	0.40	NS
Cro 21 <E2>	<1 * 6>	0.18	0.77	0.82	NS	2.31	0.92	0.01	S *
Cro 22 <E2>	<1 * 7>	-9.09	4.23	0.03	S *	-3.76	1.82	0.04	S *
Cro 23 <E2>	<1 * 9>	-1.95	1.88	0.30	NS	1.32	0.89	0.14	NS
Cro 24 <E2>	<1 * 10>	-4.65	1.97	0.02	S *	-0.09	1.17	0.94	NS
Cro 25 <E2>	<2 * 6>	2.28	0.97	0.02	S *	2.23	1.05	0.04	S *
Cro 26 <E2>	<2 * 7>	0.72	1.80	0.69	NS	0.01	1.27	0.99	NS
Cro 27 <E2>	<2 * 8>	2.51	1.99	0.21	NS	2.00	1.12	0.08	S +
Cro 28 <E2>	<2 * 9>	3.00	1.18	0.01	S *	2.66	1.00	0.01	S **
Cro 29 <E2>	<2 * 10>	-6.62	3.59	0.07	S +	-2.21	1.30	0.09	S +
Cro 30 <E2>	<3 * 7>	-6.05	2.55	0.02	S *	-3.32	1.71	0.05	S +
Cro 31 <E2>	<3 * 9>	1.99	1.19	0.10	S +	2.21	0.94	0.02	S *
Cro 32 <E2>	<3 * 10>	-7.39	3.97	0.07	S +	-2.54	1.53	0.10	NS
Cro 33 <E2>	<4 * 6>	1.90	1.64	0.25	NS	2.69	1.44	0.06	S +
Cro 34 <E2>	<4 * 8>	5.67	2.21	0.01	S *	4.23	1.49	0.01	S **
Cro 35 <E2>	<4 * 9>	1.66	1.61	0.31	NS	2.64	1.29	0.04	S *
Cro 36 <E2>	<4 * 10>	-1.76	1.31	0.18	NS	0.87	0.94	0.35	NS
Cro 37 <E2>	<5 * 7>	-2.18	2.04	0.29	NS	-1.74	1.67	0.30	NS
Cro 38 <E2>	<5 * 8>	-1.00	0.91	0.27	NS	-0.06	0.76	0.94	NS
Cro 39 <E2>	<5 * 9>	-1.03	1.05	0.33	NS	0.35	0.65	0.60	NS



Cro 40 <E2> <5 \* 10> -1.23 1.67 0.46 NS 0.19 1.10 0.87 NS

Significance of F1 or F2 is over Population Mean 12.854884

Number	Cross	F1(G)	S.E.	P-value	Sig.	F2(G)	S.E.	P-value	Sig.
Cro 1	<1 * 6>	16.18	1.01	0.00	S **	14.09	0.98	0.21	NS
Cro 2	<1 * 7>	13.66	2.81	0.78	NS	12.08	1.30	0.55	NS
Cro 3	<1 * 9>	5.08	1.77	0.00	S **	4.96	1.64	0.00	S **
Cro 4	<1 * 10>	6.69	3.39	0.07	S +	5.20	2.95	0.01	S *
Cro 5	<2 * 6>	16.84	1.27	0.00	S **	14.28	1.52	0.35	NS
Cro 6	<2 * 7>	17.24	1.85	0.02	S *	15.64	2.33	0.24	NS
Cro 7	<2 * 8>	20.23	5.09	0.15	NS	12.30	2.58	0.83	NS
Cro 8	<2 * 9>	19.12	2.07	0.00	S **	14.56	1.07	0.12	NS
Cro 9	<2 * 10>	11.15	1.91	0.37	NS	12.32	1.42	0.71	NS
Cro 10	<3 * 7>	12.19	2.39	0.78	NS	9.33	1.62	0.03	S *
Cro 11	<3 * 9>	13.18	2.73	0.91	NS	9.86	1.89	0.12	NS
Cro 12	<3 * 10>	6.59	4.32	0.15	NS	11.41	2.81	0.61	NS
Cro 13	<4 * 6>	15.76	1.80	0.11	NS	13.19	1.32	0.80	NS
Cro 14	<4 * 8>	18.68	1.98	0.00	S **	13.87	0.86	0.24	NS
Cro 15	<4 * 9>	15.73	1.49	0.06	S +	15.45	1.71	0.13	NS
Cro 16	<4 * 10>	10.16	0.76	0.00	S **	11.06	0.67	0.01	S **
Cro 17	<5 * 7>	19.75	2.59	0.01	S **	13.41	0.98	0.58	NS
Cro 18	<5 * 8>	15.40	0.84	0.00	S **	11.83	1.97	0.61	NS
Cro 19	<5 * 9>	13.99	0.64	0.08	S +	11.16	1.12	0.13	NS
Cro 20	<5 * 10>	15.21	4.39	0.59	NS	9.20	2.55	0.16	NS

No.	Cross	H <sub>pm</sub> (F <sub>1</sub> ) (GE)	S.E.	P-value	Sig.	H <sub>pm</sub> (F <sub>2</sub> ) (GE)	S.E.	P-value	Sig.
Cro 1	<E1> <1 * 6>	0.54	0.25	0.03	S *	0.27	0.12	0.03	S *
Cro 2	<E1> <1 * 7>	0.98	0.54	0.07	S +	0.49	0.27	0.07	S +
Cro 3	<E1> <1 * 9>	0.48	0.19	0.01	S *	0.24	0.10	0.01	S *
Cro 4	<E1> <1 * 10>	0.87	0.45	0.06	S +	0.44	0.23	0.06	S +
Cro 5	<E1> <2 * 6>	0.32	0.15	0.03	S *	0.16	0.07	0.03	S *
Cro 6	<E1> <2 * 7>	0.06	0.28	0.84	NS	0.03	0.14	0.84	NS
Cro 7	<E1> <2 * 8>	1.41	0.77	0.07	S +	0.70	0.38	0.07	S +
Cro 8	<E1> <2 * 9>	0.53	0.27	0.05	S +	0.27	0.13	0.05	S +
Cro 9	<E1> <2 * 10>	0.52	0.24	0.04	S *	0.26	0.12	0.04	S *
Cro 10	<E1> <3 * 7>	0.75	0.46	0.11	NS	0.37	0.23	0.11	NS
Cro 11	<E1> <3 * 9>	0.42	0.26	0.12	NS	0.21	0.13	0.12	NS
Cro 12	<E1> <3 * 10>	-0.19	0.43	0.67	NS	-0.09	0.22	0.67	NS
Cro 13	<E1> <4 * 6>	0.45	0.29	0.13	NS	0.22	0.15	0.13	NS
Cro 14	<E1> <4 * 8>	0.42	0.20	0.03	S *	0.21	0.10	0.03	S *
Cro 15	<E1> <4 * 9>	0.07	0.12	0.55	NS	0.04	0.06	0.55	NS
Cro 16	<E1> <4 * 10>	0.24	0.15	0.10	S +	0.12	0.07	0.10	S +
Cro 17	<E1> <5 * 7>	0.89	0.46	0.06	S +	0.44	0.23	0.06	S +
Cro 18	<E1> <5 * 8>	0.56	0.19	0.00	S **	0.28	0.10	0.00	S **
Cro 19	<E1> <5 * 9>	0.48	0.20	0.02	S *	0.24	0.10	0.02	S *
Cro 20	<E1> <5 * 10>	1.02	0.57	0.08	S +	0.51	0.29	0.08	S +
Cro 21	<E2> <1 * 6>	-0.33	0.13	0.01	S *	-0.17	0.06	0.01	S *
Cro 22	<E2> <1 * 7>	-0.83	0.46	0.08	S +	-0.41	0.23	0.08	S +
Cro 23	<E2> <1 * 9>	-0.51	0.24	0.04	S *	-0.25	0.12	0.04	S *
Cro 24	<E2> <1 * 10>	-0.71	0.30	0.02	S *	-0.35	0.15	0.02	S *
Cro 25	<E2> <2 * 6>	0.01	0.08	0.93	NS	0.00	0.04	0.93	NS
Cro 26	<E2> <2 * 7>	0.11	0.16	0.51	NS	0.05	0.08	0.51	NS
Cro 27	<E2> <2 * 8>	0.08	0.22	0.72	NS	0.04	0.11	0.72	NS
Cro 28	<E2> <2 * 9>	0.05	0.12	0.66	NS	0.03	0.06	0.66	NS
Cro 29	<E2> <2 * 10>	-0.69	0.39	0.08	S +	-0.34	0.19	0.08	S +
Cro 30	<E2> <3 * 7>	-0.42	0.23	0.06	S +	-0.21	0.11	0.06	S +

Cro 31	<E2><3 * 9>	-0.03	0.12	0.77	NS	-0.02	0.06	0.77	NS
Cro 32	<E2><3 * 10>	-0.75	0.43	0.08	S +	-0.38	0.22	0.08	S +
Cro 33	<E2><4 * 6>	-0.12	0.12	0.29	NS	-0.06	0.06	0.29	NS
Cro 34	<E2><4 * 8>	0.22	0.20	0.26	NS	0.11	0.10	0.26	NS
Cro 35	<E2><4 * 9>	-0.15	0.14	0.29	NS	-0.08	0.07	0.29	NS
Cro 36	<E2><4 * 10>	-0.41	0.20	0.04	S *	-0.20	0.10	0.04	S *
Cro 37	<E2><5 * 7>	-0.07	0.13	0.59	NS	-0.03	0.06	0.59	NS
Cro 38	<E2><5 * 8>	-0.15	0.09	0.09	S +	-0.07	0.04	0.09	S +
Cro 39	<E2><5 * 9>	-0.21	0.12	0.08	S +	-0.11	0.06	0.08	S +
Cro 40	<E2><5 * 10>	-0.22	0.20	0.26	NS	-0.11	0.10	0.26	NS

Significance of F1 or F2 is over Population Mean 12.854884

No.	Cro	H <sub>pm</sub> (F <sub>1</sub> ) (G)	S.E.	P- value	Sig.	H <sub>pm</sub> (F <sub>2</sub> ) (G)	S.E.	P- value	Sig.
Cro 1	<1 * 6>	0.56	0.12	0.00	S **	0.40	0.08	0.00	S **
Cro 2	<1 * 7>	0.27	0.31	0.39	NS	0.15	0.16	0.35	NS
Cro 3	<1 * 9>	0.27	0.10	0.01	S *	0.26	0.08	0.00	S **
Cro 4	<1 * 10>	0.04	0.19	0.85	NS	-0.08	0.12	0.50	NS
Cro 5	<2 * 6>	0.16	0.20	0.42	NS	-0.04	0.13	0.78	NS
Cro 6	<2 * 7>	0.10	0.18	0.56	NS	-0.02	0.10	0.84	NS
Cro 7	<2 * 8>	0.65	0.62	0.30	NS	0.04	0.37	0.92	NS
Cro 8	<2 * 9>	0.91	0.26	0.00	S **	0.56	0.13	0.00	S **
Cro 9	<2 * 10>	-0.07	0.17	0.70	NS	0.03	0.10	0.80	NS
Cro 10	<3 * 7>	0.40	0.21	0.06	S +	0.18	0.11	0.09	S +
Cro 11	<3 * 9>	1.14	0.21	0.00	S **	0.88	0.19	0.00	S **
Cro 12	<3 * 10>	0.27	0.52	0.61	NS	0.65	0.40	0.11	NS
Cro 13	<4 * 6>	0.30	0.18	0.10	NS	0.10	0.11	0.36	NS
Cro 14	<4 * 8>	0.75	0.28	0.01	S **	0.38	0.14	0.01	S *
Cro 15	<4 * 9>	0.87	0.24	0.00	S **	0.84	0.25	0.00	S **
Cro 16	<4 * 10>	0.08	0.12	0.53	NS	0.15	0.10	0.14	NS
Cro 17	<5 * 7>	0.53	0.43	0.22	NS	0.04	0.26	0.88	NS
Cro 18	<5 * 8>	0.51	0.23	0.03	S *	0.23	0.11	0.04	S *
Cro 19	<5 * 9>	0.75	0.16	0.00	S **	0.53	0.10	0.00	S **
Cro 20	<5 * 10>	0.49	0.42	0.25	NS	0.02	0.26	0.94	NS

No.	Cross	H <sub>pb</sub> (F <sub>1</sub> ) (GE)	S.E.	P- value	Sig.	H <sub>pb</sub> (F <sub>2</sub> ) (GE)	S.E.	P- value	Sig.
Cro 1	<E1><1 * 6>	0.25	0.23	0.28	NS	-0.03	0.13	0.85	NS
Cro 2	<E1><1 * 7>	0.52	0.56	0.35	NS	0.03	0.31	0.91	NS
Cro 3	<E1><1 * 9>	0.25	0.16	0.13	NS	0.01	0.10	0.92	NS
Cro 4	<E1><1 * 10>	0.61	0.45	0.17	NS	0.18	0.23	0.45	NS
Cro 5	<E1><2 * 6>	0.28	0.18	0.13	NS	0.11	0.15	0.44	NS
Cro 6	<E1><2 * 7>	-0.05	0.27	0.86	NS	-0.08	0.19	0.68	NS
Cro 7	<E1><2 * 8>	1.09	0.75	0.15	NS	0.39	0.37	0.30	NS
Cro 8	<E1><2 * 9>	0.42	0.31	0.18	NS	0.15	0.20	0.46	NS
Cro 9	<E1><2 * 10>	0.43	0.31	0.17	NS	0.17	0.23	0.45	NS
Cro 10	<E1><3 * 7>	0.59	0.50	0.24	NS	0.22	0.29	0.46	NS
Cro 11	<E1><3 * 9>	0.35	0.30	0.25	NS	0.14	0.19	0.45	NS
Cro 12	<E1><3 * 10>	-0.23	0.42	0.60	NS	-0.13	0.22	0.56	NS
Cro 13	<E1><4 * 6>	0.35	0.31	0.27	NS	0.12	0.17	0.46	NS
Cro 14	<E1><4 * 8>	0.05	0.22	0.81	NS	-0.16	0.17	0.36	NS
Cro 15	<E1><4 * 9>	-0.10	0.13	0.46	NS	-0.13	0.09	0.16	NS
Cro 16	<E1><4 * 10>	0.10	0.20	0.60	NS	-0.02	0.15	0.91	NS
Cro 17	<E1><5 * 7>	0.64	0.44	0.15	NS	0.20	0.22	0.38	NS
Cro 18	<E1><5 * 8>	0.38	0.23	0.11	NS	0.10	0.19	0.61	NS
Cro 19	<E1><5 * 9>	0.46	0.20	0.02	S *	0.22	0.13	0.08	S +
Cro 20	<E1><5 * 10>	0.97	0.59	0.11	NS	0.46	0.32	0.15	NS
Cro 21	<E2><1 * 6>	-0.36	0.19	0.06	S +	-0.20	0.14	0.16	NS

Cro 22	<E2><1 * 7>	-1.08	0.48	0.03	S *	-0.67	0.25	0.01	S **
Cro 23	<E2><1 * 9>	-0.53	0.27	0.05	S +	-0.28	0.17	0.10	S +
Cro 24	<E2><1 * 10>	-0.74	0.34	0.03	S *	-0.38	0.21	0.07	S +
Cro 25	<E2><2 * 6>	-0.14	0.11	0.21	NS	-0.14	0.08	0.08	S +
Cro 26	<E2><2 * 7>	0.03	0.23	0.90	NS	-0.02	0.16	0.88	NS
Cro 27	<E2><2 * 8>	-0.01	0.24	0.96	NS	-0.05	0.14	0.71	NS
Cro 28	<E2><2 * 9>	-0.10	0.14	0.48	NS	-0.13	0.10	0.19	NS
Cro 29	<E2><2 * 10>	-0.83	0.40	0.04	S *	-0.49	0.22	0.03	S *
Cro 30	<E2><3 * 7>	-0.51	0.26	0.05	S +	-0.30	0.16	0.06	S +
Cro 31	<E2><3 * 9>	-0.18	0.14	0.21	NS	-0.16	0.10	0.11	NS
Cro 32	<E2><3 * 10>	-0.89	0.44	0.05	S *	-0.52	0.23	0.03	S *
Cro 33	<E2><4 * 6>	-0.17	0.11	0.13	NS	-0.11	0.07	0.13	NS
Cro 34	<E2><4 * 8>	0.21	0.22	0.33	NS	0.10	0.13	0.43	NS
Cro 35	<E2><4 * 9>	-0.21	0.14	0.15	NS	-0.13	0.09	0.14	NS
Cro 36	<E2><4 * 10>	-0.45	0.22	0.04	S *	-0.25	0.14	0.07	S +
Cro 37	<E2><5 * 7>	-0.10	0.18	0.57	NS	-0.07	0.13	0.60	NS
Cro 38	<E2><5 * 8>	-0.28	0.12	0.02	S *	-0.21	0.09	0.03	S *
Cro 39	<E2><5 * 9>	-0.42	0.13	0.00	S **	-0.31	0.09	0.00	S **
Cro 40	<E2><5 * 10>	-0.41	0.24	0.09	S +	-0.30	0.15	0.05	S +

Significance of F1 or F2 is over Population Mean 12.854884

No.	Cro	H <sub>pb</sub> (F <sub>1</sub> ) (G)	S.E.	P- value	Sig.	H <sub>pb</sub> (F <sub>2</sub> ) (G)	S.E.	P- value	Sig.
Cro 1	<1 * 6>	0.14	0.17	0.43	NS	-0.02	0.15	0.88	NS
Cro 2	<1 * 7>	-0.24	0.31	0.44	NS	-0.36	0.18	0.05	S *
Cro 3	<1 * 9>	0.12	0.14	0.42	NS	0.11	0.13	0.42	NS
Cro 4	<1 * 10>	-0.17	0.21	0.42	NS	-0.29	0.15	0.05	S +
Cro 5	<2 * 6>	0.14	0.20	0.49	NS	-0.06	0.13	0.63	NS
Cro 6	<2 * 7>	0.04	0.20	0.85	NS	-0.08	0.13	0.53	NS
Cro 7	<2 * 8>	0.40	0.64	0.53	NS	-0.22	0.39	0.58	NS
Cro 8	<2 * 9>	0.31	0.24	0.19	NS	-0.04	0.16	0.80	NS
Cro 9	<2 * 10>	-0.31	0.25	0.22	NS	-0.22	0.20	0.28	NS
Cro 10	<3 * 7>	-0.35	0.23	0.14	NS	-0.58	0.20	0.00	S **
Cro 11	<3 * 9>	1.05	0.21	0.00	S **	0.79	0.21	0.00	S **
Cro 12	<3 * 10>	-0.18	0.53	0.74	NS	0.20	0.40	0.63	NS
Cro 13	<4 * 6>	0.11	0.18	0.55	NS	-0.09	0.11	0.41	NS
Cro 14	<4 * 8>	0.72	0.27	0.01	S **	0.34	0.15	0.03	S *
Cro 15	<4 * 9>	0.49	0.25	0.05	S +	0.46	0.26	0.08	S +
Cro 16	<4 * 10>	0.05	0.17	0.76	NS	0.12	0.16	0.44	NS
Cro 17	<5 * 7>	0.23	0.44	0.60	NS	-0.26	0.27	0.34	NS
Cro 18	<5 * 8>	0.49	0.23	0.04	S *	0.22	0.13	0.10	S +
Cro 19	<5 * 9>	0.38	0.19	0.05	S *	0.16	0.18	0.36	NS
Cro 20	<5 * 10>	0.48	0.39	0.23	NS	0.01	0.25	0.96	NS

Significance of Heterosis is over Population Mean 12.854884

Pre (F1)	13.987	0.730276	0.124	NS
Pre (F2)	12.6895	0.306025	0.59	NS
Hpm (F1)	0.147004	0.136824	0.285	NS
Hpm (F2)	0.0457101	0.0706352	0.519	NS
Hpb (F1)	-0.837894	0.143119	6.23e-008	S **
Hpb (F2)	-0.939187	0.0983169	-5.09e-011	S **
Generation n	0.569721	0.0534007	-5.09e-011	S **
0.5 Omega(AA)	0.673029	0.0727739	-5.09e-011	S **
2Delta(AA)	-0.0555835	0.0447671	0.217	NS

Results of Lint% are not presented.

Time Used (Hour) = 0.003056

## Chapter 5

# Diallel Analysis for an Animal Model with Sex-Linked and Maternal Effects Along with Genotype-by-Environment Interaction Effects

Jun Zhu

### *Purpose*

To analyze balanced or unbalanced data of an animal genetic model for estimating components of variance, covariance, heritability, and selection response.

### *Definitions*

#### *Mating Design*

A set of inbred lines is sampled from a reference population. Parents are used to produce  $F_1$  crosses. Experiments with parents and their  $F_1$ s are conducted in multiple environments.

#### *Genetic Model*

The genetic model for the phenotypic mean ( $y_{ijks}$ ) of sex  $s$  in block  $k$  within environment  $h$  from the cross between maternal line  $i$  and paternal line  $j$  is

$$y_{hijks} = \mu + E_h + G_{ijs} + GE_{hijks} + e_{hijks}$$

where  $\mu$  = population mean,  $E_h$  = environment effect,  $G_{ijs}$  = genotype effect,  $GE_{hij_s}$  = genotype-environment effect, and  $e_{hij_{sk}}$  = residual effect.

The total genotype effect  $G_{ijs}$  and genotype  $\times$  environment interaction effect  $GE_{hij_s}$  can be further partitioned into different components for heterogametic progeny (XY or ZW,  $s = 1$ ) and for homogametic progeny (XX or ZZ,  $s = 2$ ):

$$\begin{array}{r}
 G_{ij1}^{XY} \quad GE_{hij1}^{XY} \quad A_i \quad A_j \quad D_{ij} \quad L_{i1} \quad M_i \quad AE_{hi} \quad AE_{hj} \quad DE_{hij} \quad LE_{hi1} \quad ME_{hi} \\
 \text{or } G_{ij1}^{ZW} \quad GE_{hij1}^{ZW} \quad A_i \quad A_j \quad D_{ij} \quad L_{j1} \quad M_i \quad AE_{hi} \quad AE_{hj} \quad DE_{hij} \quad LE_{hj1} \quad ME_{hi} \\
 G_{ij2}^{XX/ZZ} \quad GE_{hij2}^{XX/ZZ} \quad A_i \quad A_j \quad D_{ij} \quad \frac{1}{2}L_{i2} \quad \frac{1}{2}L_{j2} \quad M_i \quad AE_{hi} \quad AE_{hj} \quad DE_{hij} \quad \frac{1}{2}LE_{hi2} \\
 \qquad \qquad \qquad \frac{1}{2}LE_{hj2} \quad ME_{hi}
 \end{array}$$

where  $A_i$  (or  $A_j$ )  $\sim (0, \sigma_A^2)$  is the additive effect of autosomal genes;  $D_{ij} \sim (0, \sigma_D^2)$  is the dominance effect of autosomal genes;  $L_{i1}$  (or  $L_{j1}$ ) and  $L_{i2}$  (or  $L_{j2}$ )  $\sim (0, \sigma_L^2)$  is the additive effect of sex-linked genes;  $M_i \sim (0, \sigma_M^2)$  is the maternal effect of dam  $i$ ;  $AE_{hi}$  (or  $AE_{hj}$ )  $\sim (0, \sigma_{AE}^2)$  is the additive  $\times$  environment interaction effect of autosomal genes;  $DE_{hij} \sim (0, \sigma_{DE}^2)$  is the dominance  $\times$  environment interaction effect of autosomal genes;  $L_{i1}$  (or  $L_{j1}$ ),  $L_{i2}$  (or  $L_{j2}$ )  $\sim (0, \sigma_{LE}^2)$  is the sex-linked additive  $\times$  environment interaction effect; and  $ME_{hi} \sim (0, \sigma_M^2)$  is the maternal  $\times$  environment interaction effect of dam  $i$ .

## Analysis

### Mixed Linear Model

The phenotypic mean of the genetic model can be expressed by a mixed linear model as

$$\begin{array}{r}
 y \quad Xb \quad U_A e_A \quad U_D e_D \quad U_L e_L \quad U_M e_M \quad U_{AE} e_{AE} \quad U_{DE} e_{DE} \quad U_{LE} e_{LE} \\
 \quad U_{ME} e_{ME} \quad e_e \\
 \quad Xb \quad U_u e_u \\
 \quad \quad u
 \end{array}$$

with variance-covariance matrix

$$\text{var}(y) \begin{matrix} \sigma_A^2 U_A U_A^T & \sigma_D^2 U_D U_D^T & \sigma_L^2 U_L U_L^T & \sigma_M^2 U_M U_M^T & \sigma_{AE}^2 U_{AE} U_{AE}^T \\ & \sigma_{DE}^2 U_{DE} U_{DE}^T & \sigma_{LE}^2 U_{LE} U_{LE}^T & \sigma_{ME}^2 U_{ME} U_{ME}^T & \sigma_e^2 I \\ & & & & \end{matrix}$$

9  
 $\sigma_u^2 V_u$   
u 1

*Variance Components*

Unbiased estimation of variances can be obtained by REML or MINQUE(1) approaches. When experimental variances are estimated, genetic variance components can be obtained by  $V_A$ ,  $2\sigma_A^2$ ,  $V_D$ ,  $\sigma_D^2$ ,  $V_L$ ,  $\sigma_L^2$ ,  $V_M$ ,  $\sigma_M^2$ ,  $V_{AE}$ ,  $2\sigma_{AE}^2$ ,  $V_{DE}$ ,  $\sigma_{DE}^2$ ,  $V_{LE}$ ,  $\sigma_{LE}^2$ ,  $V_M$ ,  $\sigma_M^2$ ,  $V_e$ ,  $\sigma_e^2$ . The total phenotypic variance is  $V_P = V_A + V_D + V_L + V_M + V_{AE} + V_{DE} + V_{LE} + V_M + V_e$ .

*Covariance Components and Correlation*

Unbiased estimation of covariances can be obtained by MINQUE(1) approaches (Zhu, 1997; Zhu and Weir, 1996). When experimental covariances are estimated, genetic covariance components can be obtained by  $C_A$ ,  $2\sigma_{AA}$ ,  $C_D$ ,  $\sigma_{D/D}$ ,  $C_L$ ,  $\sigma_{L/L}$ ,  $C_M$ ,  $\sigma_{M/M}$ ,  $C_{AE}$ ,  $\sigma_{AE/AE}$ ,  $C_{DE}$ ,  $\sigma_{DE/DE}$ ,  $C_{LE}$ ,  $\sigma_{LE/LE}$ ,  $C_{ME}$ ,  $\sigma_{ME/ME}$ ,  $C_e$ ,  $\sigma_{e/e}$ . The total phenotypic covariance is  $C_P = C_A + C_D + C_L + C_M + C_{AE} + C_{DE} + C_{LE} + C_{ME} + C_e$ . For trait 1 and trait 2, correlation coefficients of genetic components can be estimated by

$$\begin{aligned} r_A &= C_A / \sqrt{V_{A(1)} V_{A(2)}}, \\ r_D &= C_D / \sqrt{V_{D(1)} V_{D(2)}}, \\ r_L &= C_L / \sqrt{V_{L(1)} V_{L(2)}}, \\ r_M &= C_M / \sqrt{V_{M(1)} V_{M(2)}}, \\ r_{AE} &= C_{AE} / \sqrt{V_{AE(1)} V_{AE(2)}}, \\ r_{LE} &= C_{LE} / \sqrt{V_{LE(1)} V_{LE(2)}}, \\ r_{ME} &= C_{ME} / \sqrt{V_{ME(1)} V_{ME(2)}}, \text{ and} \\ r_{eE} &= C_e / \sqrt{V_{e(1)} V_{e(2)}}. \end{aligned}$$

### Heritability Components

The total heritability ( $h^2$ ) can be partitioned into two components ( $h^2 = h_G^2 + h_{GE}^2$ ), where  $h_G^2 = V_A / V_P$  is general heritability and  $h_{GE}^2 = V_{AE} / V_P$  is interaction heritability (Zhu, 1997).

### Selection Response

The total selection response ( $R = ih^2 \sqrt{V_P}$ ) can be partitioned into two components (Zhu, 1997):

$$R = R_G + R_{GE}$$

where  $R_G = ih_G^2 \sqrt{V_P}$  is general response and  $R_{GE} = ih_{GE}^2 \sqrt{V_P}$  is interaction response.

### Originators

Zhu, J. (1997). *Analysis Methods for Genetic Models*. Agricultural Publication House of China, Beijing.

Zhu, J. and Weir, B.S. (1996). Diallel analysis for sex-linked and maternal effects. *Theoretical and Applied Genetics*, 92(1):1-9.

### Software Available

Zhu, J. (1997). GENSEX.EXE for constructing animal models, GENVAR1R.EXE or GENVAR1C.EXE for estimating components of variance and heritability, GENCOV1R.EXE or GENCOV1C.EXE for estimating components of covariance and correlation, GENHET1R.EXE or GENHET1C.EXE for predicting genetic effects and components of heterosis. *Analysis Methods for Genetic Models* (pp. 278-285), Agricultural Publication House of China, Beijing (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.

**EXAMPLE**

Balanced mice data (provided by William R. Atchley, Department of Genetics, North Carolina State University, Raleigh, NC) to be analyzed (Parent = 1, Year = 1, Sex = 1 & 2, Blk = 1):

Year	Fem	Male	Cross	Rep	Sex	35BW	35TL
1	1	1	0	1	1	20.23	79.78
1	1	1	0	1	2	17.71	78.93
1	1	2	1	1	1	22.01	84.79
1	1	2	1	1	2	19.44	82.87
1	1	3	1	1	1	22.48	93.66
1	1	3	1	1	2	18.34	88.74
1	1	4	1	1	1	22.80	85.48
1	1	4	1	1	2	20.41	85.09
1	1	5	1	1	1	22.57	82.83
1	1	5	1	1	2	19.25	81.83
1	1	6	1	1	1	25.11	86.36
1	1	6	1	1	2	21.79	84.54
1	1	7	1	1	1	22.67	89.44
1	1	7	1	1	2	19.80	87.06
1	2	1	1	1	1	22.91	88.60
1	2	1	1	1	2	19.14	86.39
1	2	2	0	1	1	20.94	83.13
1	2	2	0	1	2	18.50	82.40
1	2	3	1	1	1	22.09	91.83
1	2	3	1	1	2	18.28	88.57
1	2	4	1	1	1	22.37	81.91
1	2	4	1	1	2	20.30	82.42
1	2	5	1	1	1	23.61	86.13
1	2	5	1	1	2	20.16	83.73
1	2	6	1	1	1	26.45	88.73
1	2	6	1	1	2	22.01	86.77
1	2	7	1	1	1	22.86	87.86
1	2	7	1	1	2	19.85	86.45
1	3	1	1	1	1	23.73	85.75
1	3	1	1	1	2	19.86	84.80
1	3	2	1	1	1	24.18	84.48
1	3	2	1	1	2	19.75	82.55
1	3	3	0	1	1	23.72	87.41
1	3	3	0	1	2	19.09	84.93
1	3	4	1	1	1	25.36	87.27
1	3	4	1	1	2	20.00	85.20
1	3	5	1	1	1	21.98	79.03
1	3	5	1	1	2	18.77	77.21
1	3	6	1	1	1	26.48	85.66
1	3	6	1	1	2	21.85	83.52
1	3	7	1	1	1	24.99	86.89
1	3	7	1	1	2	20.41	85.06
1	4	1	1	1	1	23.33	84.48
1	4	1	1	1	2	20.77	83.14
1	4	2	1	1	1	23.18	81.61
1	4	2	1	1	2	19.47	79.41
1	4	3	1	1	1	22.50	88.10
1	4	3	1	1	2	18.90	84.24



1	4	4	0	1	1	24.24	85.97
1	4	4	0	1	2	20.91	84.16
1	4	5	1	1	1	23.22	83.22
1	4	5	1	1	2	19.33	82.19
1	4	6	1	1	1	24.01	83.07
1	4	6	1	1	2	20.62	81.25
1	4	7	1	1	1	24.86	86.73
1	4	7	1	1	2	20.70	85.19
1	5	1	1	1	1	22.07	87.14
1	5	1	1	1	2	19.37	87.90
1	5	2	1	1	1	21.05	82.04
1	5	2	1	1	2	18.78	82.88
1	5	3	1	1	1	21.32	84.22
1	5	3	1	1	2	18.19	82.25
1	5	4	1	1	1	23.31	90.07
1	5	4	1	1	2	20.18	89.91
1	5	5	0	1	1	23.79	84.50
1	5	5	0	1	2	20.48	84.69
1	5	6	1	1	1	24.48	87.04
1	5	6	1	1	2	21.15	87.06
1	5	7	1	1	1	21.41	81.79
1	5	7	1	1	2	19.18	82.03
1	6	1	1	1	1	22.28	87.39
1	6	1	1	1	2	18.81	85.55
1	6	2	1	1	1	18.86	75.66
1	6	2	1	1	2	15.75	74.44
1	6	3	1	1	1	21.68	87.52
1	6	3	1	1	2	16.24	83.10
1	6	4	1	1	1	23.01	85.38
1	6	4	1	1	2	18.64	85.04
1	6	5	1	1	1	22.97	84.62
1	6	5	1	1	2	18.69	82.70
1	6	6	0	1	1	25.60	84.43
1	6	6	0	1	2	20.88	83.36
1	6	7	1	1	1	22.91	84.57
1	6	7	1	1	2	18.81	82.43
1	7	1	1	1	1	22.59	91.29
1	7	1	1	1	2	17.91	88.00
1	7	2	1	1	1	22.48	86.97
1	7	2	1	1	2	17.50	83.04
1	7	3	1	1	1	21.71	86.41
1	7	3	1	1	2	17.54	83.27
1	7	4	1	1	1	24.23	92.60
1	7	4	1	1	2	19.88	89.00
1	7	5	1	1	1	23.79	86.83
1	7	5	1	1	2	18.93	84.83
1	7	6	1	1	1	25.07	89.44
1	7	6	1	1	2	20.21	87.38
1	7	7	0	1	1	24.31	90.48
1	7	7	0	1	2	19.81	86.65

1. Run GENSEX.EXE to create mating design matrix files and AD+L+M model data. Before running this program, create a data file (MICEDATA.TXT) for your analysis with six design columns fol-

- lowed by trait columns. The six design columns are (1) environment, (2) maternal, (3) paternal, (4) generation, (5) replication, and (6) sex. There is a limitation (<100 traits) for the number of trait columns. An example of the data file is provided with the name MICEDATA.TXT.
2. Run programs for variance and covariance analyses. Standard errors of estimates are calculated by the jackknife procedures. If you have multiple blocks for your experiments, you can use GENVAR1R.EXE or GENCOV1R.EXE for jackknifing over blocks. Otherwise you can use GENVAR1C.EXE or GENCOV1C.EXE for jackknifing over cell means.
  3. Run GENVAR1R.EXE or GENVAR1C.EXE for estimating variance components and predicting genetic effects before estimating covariance and correlation. These two programs will allow you to choose the parental type (inbred or outbred) and the prediction methods (LUP or AUP). You also need to input coefficients (1, 0, or -1) for conducting linear contrasts for genetic effects of parents.
  4. After finishing variance analysis, run GENCOV1R.EXE or GENCOV1C.EXE to estimate covariance components and coefficients of correlation among all analyzed traits.
  5. Results will automatically be stored in text files for later use or printing.

### ***Output 1 for Variance Analysis***

```
Traits =, 2
Variance components = , 5
Degree of freedom = , 48
File name is micedata.VAR
Date and Time for Analysis: Sat Jun 24 20:03:15 2000
```

```
Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.
Jackknifing Over Block Conducted for Estimating S.E.
Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP) Method.
```

```
NS = Not significant; S+ = Significant at 0.10 level.
S* = Significant at 0.05 level; S** = Significant at 0.01 level.
```

```
Linear Contrasts:
+<1> +<2> +<3> +<4> -<5> -<6> -<7>
```

Diallel Analysis of Trait, 35BW, for Public Users.

Var Comp	Estimate	S. E.	P-value	
(1): Additive Var	4.05678	0.914491	2.67e-005	S**
(2): Dominance Var	0.447741	0.114861	0.00015	S**
(3): Sex-linked Var	4.82177	0.332787	2.87e-017	S**

(4): Maternal Var	3.16826	0.912454	0.000551	S**
(5): Residual Var	0.979275	0.309302	0.00134	S**
(6): Var(Pheno.)	13.4738	1.91195	3.11e-009	S**

Proportion of Var(G)/Var(T)Estimate	S. E.	P-value	
(1): Additive Var/Vp	0.301086	0.0251507	2.53e-016 S**
(2): Dominance Var/Vp	0.0332304	0.011576	0.00304 S**
(3): Sex-linked Var/Vp	0.357862	0.032024	2.98e-015 S**
(4): Maternal Var/Vp	0.235142	0.0202444	7.84e-016 S**
(5): Residual Var/Vp	0.0726798	0.0271762	0.0051 S**

Heritability	Estimate	S. E.	P-value	
(6): Heritability(N)	0.301086	0.0251507	2.53e-016	S**
(7): Heritability(B)	0.334316	0.0236245	3.21e-017	S**

## Genetic Predictor, S. E. , P-value

## (1): Random Effect is Additive Effects

A1	-1.163629	0.383414	0.00388	S**
A2	-1.622929	0.534681	0.00387	S**
A3	-1.099644	0.273847	0.000208	S**
A4	0.535614	0.274989	0.0573	S+
A5	0.188242	0.412984	0.651	NS
A6	2.638442	0.623674	0.000104	S**
A7	0.517437	0.316664	0.109	NS
Linear Contrast	-6.21749	1.79317	0.00112	S**

## (2): Random Effect is Dominance Effects

D1*1	-1.575254	1.171944	0.185	NS
D2*2	-0.823010	0.741883	0.273	NS
D3*3	0.161857	0.293363	0.584	NS
D4*4	0.306696	0.310885	0.329	NS
D5*5	1.089396	0.790779	0.175	NS
D6*6	1.449270	1.100055	0.194	NS
D7*7	0.697693	0.513080	0.18	NS
D1*2	0.719177	0.566455	0.21	NS
D1*3	0.433285	0.376514	0.256	NS
D1*4	0.532937	0.514004	0.305	NS
D1*5	0.105613	0.398419	0.792	NS
D1*6	0.617389	0.608657	0.316	NS
D1*7	-0.008952	0.420072	0.983	NS
D2*3	0.292272	0.710588	0.683	NS
D2*4	0.047317	0.659437	0.943	NS
D2*5	0.062535	0.567660	0.913	NS
D2*6	-0.378167	2.358942	0.873	NS
D2*7	-0.164429	0.355381	0.646	NS
D3*4	-0.129561	0.270304	0.634	NS
D3*5	-1.016032	0.950404	0.29	NS
D3*6	-0.268319	0.703458	0.705	NS
D3*7	-0.256718	0.609336	0.675	NS
D4*5	-0.370931	0.502767	0.464	NS
D4*6	-0.697666	0.733653	0.346	NS
D4*7	0.261144	0.349548	0.459	NS
D5*6	-0.182574	0.462678	0.695	NS
D5*7	-0.609768	0.793060	0.446	NS
D6*7	-0.298528	0.437983	0.499	NS
Heterosis <Delta>	-0.738068	1.8011	0.684	NS

(3): Random Effect is Sex-linked Effects

L1 for Sex1	1.619670	0.268733	2.28e-007	S**
L2 for Sex1	1.950941	0.409804	1.81e-005	S**
L3 for Sex1	2.545023	0.396915	5.87e-008	S**
L4 for Sex1	1.998426	0.326978	1.69e-007	S**
L5 for Sex1	1.194290	0.283566	0.000111	S**
L6 for Sex1	2.173739	0.465039	2.42e-005	S**
L7 for Sex1	3.040606	0.367137	8.28e-011	S**
L1 for Sex2	-1.468479	0.283005	4.22e-006	S**
L2 for Sex2	-1.416539	0.315276	4.42e-005	S**
L3 for Sex2	-2.789509	0.420796	2.73e-008	S**
L4 for Sex2	-1.799656	0.408109	5.82e-005	S**
L5 for Sex2	-2.015034	0.390778	4.72e-006	S**
L6 for Sex2	-2.912965	0.350283	7.36e-011	S**
L7 for Sex2	-2.124706	0.288782	2.09e-009	S**
Linear Contrast	4.99948	0.147414	5.87e-017	S**

(4): Random Effect is Maternal Effects

M1	0.532529	0.235722	0.0285	S*
M2	1.445810	0.744384	0.058	S+
M3	1.947175	0.459670	0.000102	S**
M4	0.036886	0.341978	0.915	NS
M5	0.198565	0.396981	0.619	NS
M6	-3.214121	0.790225	0.000176	S**
M7	-0.950092	0.338411	0.0072	S**
Linear Contrast	5.89251	1.83518	0.00236	S**

Fixed Effect <1>, 21.2871

Results of Tail Length are not presented.

Time Used (Hour) = 0.001389

### ***Output 2 for Covariance Analysis***

Traits = , 2  
 Covariance components = , 5  
 Degree of freedom = , 48  
 File name is micedata.COV  
 Date and Time for Analysis: Sat Jun 24 20:03:33 2000

Covariance Components Estimated by MINQUE(1) with GENCOV1C.EXE.  
 Jackknifing Over Cell Mean Conducted for Estimating S.E.

NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.

Covariances and Correlations Between, 35BW, , &, 35TL, for Public Users.:

Covariances	Estimates	S.E.	P-value	
Additive Cov	1.2739	1.40446	0.369	NS
Dominance Cov	-0.279037	0.886415	0.754	NS
Sex-linked Cov	2.07233	0.465324	5.04e-005	S**
Maternal Cov	0.848917	1.69412	0.619	NS

Residual Cov	1.76704	0.698536	0.0148	S*
Cov <1=Genotypic>				
Cov <2=Phenotypic>	Estimates	S.E.	P-value	
Cov 2	5.68315	2.84705	0.0516	S+
Cov 1	3.91611	2.85586	0.177	NS
Correlation	Estimates	S.E.	P-value	
Additive Cor	0.190211	0.07873	0.0195	S*
Dominance Cor	-0.169791	0.0696301	0.0185	S*
Sex-linked Cor	0.589663	0.0588193	2.33e-013	S**
Maternal Cor	0.138456	0.0704558	0.0552	S+
Residual Cor	0.664416	0.0763856	1.98e-011	S**
Cor <1=Genotypic>				
Cor <2=Phenotypic>	Estimates	S.E.	P-value	
Cor 2	0.248755	0.0830793	0.00434	S**
Cor 1	0.197347	0.0879154	0.0294	S*

Results of Tail Length are not presented.

Time Used (Hour) = 0.000556

## Chapter 6

# Generation Means Analysis

Michael M. Kenty  
David S. Wofford

### *Importance*

Development of elite varieties or germplasm often involves quantitatively inherited traits, such as insect resistance in soybeans. In these instances, it is advantageous for the breeder/geneticist to utilize methodology that allows not only the selection of desirable genotypes but also a determination of the underlying genetic effects contributing to the expression of the desired trait.

### *Definitions*

Using Hayman's (1958) methodology and Gamble's (1962) notation, the models for the generation means analysis are as follows:

$$\begin{array}{rcllclclcl} P_1 & = & m & + & a & - & d/2 & + & aa & - & ad & + & dd/4 \\ P_2 & = & m & - & a & - & d/2 & + & aa & + & ad & + & dd/4 \\ F_1 & = & m & & & & + & d/2 & & & & & + & dd/4 \\ F_2 & = & m & & & & & & & & & & & \\ BC_1 & = & m & + & a/2 & & & & + & aa/4 & & & & \\ BC_2 & = & m & - & a/2 & & & & + & aa/4 & & & & \\ F_3 & = & m & & & - & d/4 & & & & & & + & dd/16 \\ BS_1 & = & m & + & a/2 & - & d/4 & + & aa/4 & - & ad/8 & + & dd/16 \\ BS_2 & = & m & - & a/2 & - & d/4 & + & aa/4 & + & ad/8 & + & dd/16 \end{array}$$

where  $m$  = overall mean,  $a$  = additive genetic effects,  $d$  = dominance genetic effects,  $aa$  = additive  $\times$  additive genetic effects,  $ad$  = additive  $\times$  dominance genetic effects,  $dd$  = dominance  $\times$  dominance genetic effects.

## Originators

- Gamble, E.E. (1962). Gene effects in corn (*Zea mays* L.) I. Separation and relative importance of gene effects for yield. *Canadian Journal of Plant Science* 42:339-348.
- Hayman, B.I. (1958). The separation of epistatic from additive and dominance variation in generation means. *Heredity* 12:371-390.

## Software Available

- Kenty, M.M. (1994). Inheritance of resistance to the soybean looper in soybean. Doctoral dissertation. University of Florida, Gainesville.

## Key References

- Kenty, M.M., Hinson, K., Quesenberry, K.H., and Wofford, D.S. (1996). Inheritance of resistance to the soybean looper in soybean. *Crop Science* 36:1532-1537.
- Meredith, W.R., Jr. and Bridge, R.R. (1972). Heterosis and gene action in cotton, *Gossypium hirsutum* L. *Crop Science* 12:304-310.
- Scott, G.E., Hallauer, A.R., and Dicke, F.F. (1964). Types of gene action conditioning resistance to European corn borer leaf feeding. *Crop Science* 4:603-605.

## Contacts

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## EXAMPLE

The data are presented in this order: generation, plant no., rating 1 (top 1/3 plant), rating 2 (middle 1/3 plant), and rating 3 (bottom 1/3 plant).

Data to be analyzed (insect defoliation, 1 = 0-10%, 10 = 91-100%):

P1 1121	P2 4778	F2 2678	F3 5224
P1 2131	P2 5788	F2 3455	BC1 1112
P1 3222	F1 1233	F2 4223	BC1 2223
P1 4121	F1 2333	F2 5566	BC1 3121
P1 5121	F1 3234	F3 1112	BC1 4112
P2 1788	F1 4244	F3 2334	BC1 5233
P2 2789	F1 5334	F3 3556	BC2 1111
P2 3889	F2 1121	F3 4233	BC2 2122

BC2 3223	F3 10223	P1 12111	P2 19678
BC2 4222	BS1 6667	P1 13223	P2 20779
BC2 5333	BS1 7789	P1 14112	BC1 16123
BS1 1677	BS1 8889	P1 15223	BC1 17122
BS1 2789	BS1 9777	P2 11677	BC1 18112
BS1 3889	BS1 10677	P2 12789	BC1 19223
BS1 4788	BC1 6111	P2 13889	BC1 20233
BS1 5677	BC1 7223	P2 14778	BS1 16667
BS2 1667	BC1 8121	P2 15888	BS1 17889
BS2 2777	BC1 9122	BC1 11121	BS1 18777
BS2 3899	BC1 10223	BC1 12233	BS1 19678
BS2 4789	BC2 6112	BC1 13233	BS1 20889
BS2 5889	BC2 7223	BC1 14123	F1 16233
P2 6888	BC2 8222	BC1 15222	F1 17334
P2 7778	BC2 9333	BS1 11677	F1 18445
P2 8678	BC2 10123	BS1 12778	F1 19223
P2 9779	BS2 6677	BS1 13889	F1 20122
P2 10889	BS2 7778	BS1 14667	F2 16121
F1 6233	BS2 8889	BS1 15777	F2 17445
F1 7334	BS2 9789	BS2 11667	F2 18667
F1 8234	BS2 10678	BS2 12778	F2 19223
F1 9233	F1 11233	BS2 13888	F2 20123
F1 10333	F1 12222	BS2 14789	F3 16113
P1 6121	F1 13234	BS2 15677	F3 17122
P1 7122	F1 14334	BC2 11111	F3 18334
P1 8133	F1 15233	BC2 12223	F3 19556
P1 9123	F2 11121	BC2 13121	F3 20678
P1 10112	F2 12678	BC2 14112	BC2 16112
F2 6678	F2 13556	BC2 15123	BC2 17121
F2 7334	F2 14778	P1 16111	BC2 18223
F2 8223	F2 15223	P1 17212	BC2 19234
F2 9566	F3 11112	P1 18223	BC2 20122
F2 10112	F3 12334	P1 19122	BS2 16677
F3 6223	F3 13445	P1 20121	BS2 17778
F3 7112	F3 14567	P2 16678	BS2 18678
F3 8556	F3 15778	P2 17889	BS2 19899
F3 9667	P1 11121	P2 18899	BS2 20789

## Program

```

/*This is a Generation Means Analysis based on Hayman's methodology,
Heredity 12:371-390 */
DATA;
INFILE 'A:Cage1.dat';
/* The INPUT statement will vary according to the data set, you need
generation ("GEN") and a dependent variable */
INPUT row plant gen $ fc $ rating1 rating2 rating3;
MEANRATE = (rating1+rating2+rating3)/3;
PROC SORT; BY GEN;
PROC MEANS; BY GEN; VAR MEANRATE;
OUTPUT OUT=NE MEAN=Y VAR=V STDERR=S;
DATA NEW; SET NE; RS=1/S; IF GEN='D' OR GEN='BD' THEN DELETE;
PROC PRINT;
/* You need a minimum of 6 generations to conduct this analysis, if
the number of generations used are different than the amount (9)

```



in this example, refer to Gamble's paper (*Canadian Journal of Plant Science* 42:339-348) to obtain the proper coefficients. Another source of information is Jennings et al. (*Iowa State Journal of Research* 48:267-280) \*/

DATA COEFCNTS;

INPUT GEN \$ X1 X2 X3 X4 X5;  
CARDS;

BC1	0.5	0.0	0.25	0.0	0.0
BC2	-0.5	0.0	0.25	0.0	0.0
BS1	0.5	-0.25	0.25	-0.125	0.0625
BS2	-0.5	-0.25	0.25	0.125	0.0625
F1	0.0	0.5	0.0	0.0	0.25
F2	0.0	0.0	0.0	0.0	0.0
F3	0.0	-0.25	0.0	0.0	0.0625
P1	1.0	-0.5	1.0	-0.5	0.25
P2	-1.0	-0.5	1.0	0.5	0.25

DATA FINAL; MERGE NEW COEFCNTS;

PROC PRINT;

/\* This model tests the significance of the additive (X1) and the dominance (X2) effects \*/

TITLE 'PROC REG WEIGHTED';

PROC REG;

MODEL Y = X1 X2;

WEIGHT RS;

/\* The model must be weighted to account for the unequal population sizes among the generations. See Rowe and Alexander (*Crop Science* 20:109-110) for further details. The next model tests for the epistatic effects, additive-additive (X3), additive-dominance (X4), and dominance-dominance (X5), as well as the additive (X1) and dominance (X2) effects. \*/

PRO REG;

MODEL Y = X1 X2 X3 X4 X5;

WEIGHT RS;

RUN;

/\* This next set of models are tested with PROC GLM instead of PROC REG \*/

TITLE 'PROC GLM WEIGHTED';

PROC GLM;

MODEL Y = X1 X2;

WEIGHT RS;

PROC GLM;

MODEL Y = X1 X2 X3 X4 X5;

WEIGHT RS;

RUN;

/\* The next series of models are the same as the previous models, except that they assume equal population size among the generations, and are, therefore, not weighted. \*/

TITLE 'PROC REG NOWEIGHT';

PROC REG;

MODEL Y = X1 X2;

PROC REG;

MODEL Y = X1 X2 X3 X4 X5;

RUN;

```
TITLE 'PROC GLM NOWEIGHT';
MODEL Y = X1 X2;
PROC GLM; MODEL Y = X1 X2 X3 X4 X5;
RUN;
/* Depending on whether or not the population sizes among the generations are equal, report the model that has the most significant effects from either PROC GLM or PROC REG. */
```

**SAS Output File**

The SAS System 15:21 Thursday, March 16, 2000 1

The MEANS Procedure

gen=BC1

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	1.9166667	0.5606492	1.0000000	2.6666667

gen=BC2

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	1.9166667	0.6386664	1.0000000	3.0000000

gen=BS1

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	7.3166667	0.7683429	6.3333333	8.3333333

gen=BS2

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	7.4833333	0.7606937	6.3333333	8.6666667

gen=F1

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	2.9000000	0.5629912	1.6666667	4.3333333

gen=F2

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	4.0166667	2.2412272	1.3333333	7.3333333

gen=F3  
Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	3.7166667	2.0008039	1.3333333	7.3333333

gen=P1  
Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	1.6333333	0.4445906	1.0000000	2.3333333

gen=P2  
The MEANS Procedure

Analysis Variable : MEANRATE

N	Mean	Std Dev	Minimum	Maximum
20	7.7166667	0.5543554	6.6666667	8.6666667

Obs	gen	TYPE	FREQ	Y	V	S	RS
1	BC1	0	20	1.91667	0.31433	0.12536	7.9767
2	BC2	0	20	1.91667	0.40789	0.14281	7.0023
3	BS1	0	20	7.31667	0.59035	0.17181	5.8205
4	BS2	0	20	7.48333	0.57865	0.17010	5.8790
5	F1	0	20	2.90000	0.31696	0.12589	7.9435
6	F2	0	20	4.01667	5.02310	0.50115	1.9954
7	F3	0	20	3.71667	4.00322	0.44739	2.2352
8	P1	0	20	1.63333	0.19766	0.09941	10.0590
9	P2	0	20	7.71667	0.30731	0.12396	8.0673

PROC REG WEIGHTED

Obs	gen	TYPE	FREQ	V	S	RS	X1	X2	X3	X4	X5	
1	BC1	0	20	1.91667	0.31433	0.12536	7.9767	0.5	0.00	0.25	0.00	0.0000
2	BC2	0	20	1.91667	0.40789	0.14281	7.0023	-0.5	0.00	0.25	0.00	0.0000
3	BS1	0	20	7.31667	0.59035	0.17181	5.8205	0.5	-0.25	0.25	-0.25	0.0625
4	BS2	0	20	7.48333	0.57865	0.17010	5.8790	-0.5	-0.25	0.25	0.25	0.0625
5	F1	0	20	2.90000	0.31696	0.12589	7.9435	0.0	0.50	0.00	0.00	0.2500
6	F2	0	20	4.01667	5.02310	0.50115	1.9954	0.0	0.00	0.00	0.00	0.0000
7	F3	0	20	3.71667	4.00322	0.44739	2.2352	0.0	-0.25	0.00	0.00	0.0625
8	P1	0	20	1.63333	0.19766	0.09941	10.0590	1.0	-0.50	1.00	-1.00	0.2500
9	P2	0	20	7.71667	0.30731	0.12396	8.0673	-1.0	-0.50	1.00	1.00	0.2500

PROC REG WEIGHTED

The REG Procedure  
Model: MODEL1  
Dependent Variable: Y

Weight: RS

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	2	177.56093	88.78047	2.67	0.1485

Generation Means Analysis

Error 6 199.86954 33.31159  
 Corrected Total 8 377.43047

Root MSE 5.77162 R-Square 0.4704  
 Dependent Mean 4.09505 Adj R-Sq 0.2939  
 Coeff Var 140.94121

Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t
Intercept	1	3.75399	0.84226	4.46	0.0043
X1	1	-2.32644	1.16302	-2.00	0.0924
X2	1	-2.93086	2.34026	-1.25	0.2570

PROC REG WEIGHTED

The REG Procedure  
 Model: MODEL1  
 Dependent Variable: Y

Weight: RS

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	301.20716	60.24143	2.37	0.2542
Error	3	76.22331	25.40777		
Corrected Total	8	377.43047			

Root MSE 5.04061 R-Square 0.7980  
 Dependent Mean 4.09505 Adj R-Sq 0.4615  
 Coeff Var 123.09023

Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t
Intercept	1	4.42225	1.11945	3.95	0.0289
X1	1	0.38757	2.39420	0.16	0.8817
X2	1	-10.68980	4.64427	-2.30	0.1048
X3	1	-8.61894	4.64304	-1.86	0.1604
X4	1	3.35783	2.74842	1.22	0.3091
X5	1	14.76576	9.56113	1.54	0.2202

PROC GLM WEIGHTED

Number of observations 9  
 The GLM Procedure  
 Dependent Variable: Y

Weight: RS

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	2	177.5609302	88.7804651	2.67	0.1485

Error	6	199.8695384	33.3115897
Corrected			
Total	8	377.4304686	

R-Square	Coeff Var	Root MSE	Y Mean
0.470447	140.9412	5.771619	4.095055

Source	DF	Type I SS	Mean Square	F Value	Pr > F
X1	1	125.3143256	125.3143256	3.76	0.1005
X2	1	52.2466046	52.2466046	1.57	0.2570

Source	DF	Type III SS	Mean Square	F Value	Pr > F
X1	1	133.2929249	133.2929249	4.00	0.0924
X2	1	52.2466046	52.2466046	1.57	0.2570

Parameter	Estimate	Standard Error	t Value	Pr >  t
Intercept	3.753994272	0.84225532	4.46	0.0043
X1	-2.326444874	1.16301923	-2.00	0.0924
X2	-2.930859648	2.34025761	1.25	0.2570

PROC GLM WEIGHTED

The GLM Procedure  
 Number of observations 9  
 Dependent Variable: Y

Weight: RS

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	301.2071567	60.2414313	2.37	0.2542
Error	3	76.2233119	25.4077706		
Corrected Total	8	377.4304686			

R-Square	Coeff Var	Root MSE	Y Mean
0.798047	123.0902	5.040612	4.095055

Source	DF	Type I SS	Mean Square	F Value	Pr > F
X1	1	125.3143256	125.3143256	4.93	0.1130
X2	1	52.2466046	52.2466046	2.06	0.2470
X3	1	29.6732521	29.6732521	1.17	0.3590
X4	1	33.3748169	33.3748169	1.31	0.3349
X5	1	60.5981574	60.5981574	2.39	0.2202

Source	DF	Type III SS	Mean Square	F Value	Pr > F
X1	1	0.6657960	0.6657960	0.03	0.8817
X2	1	134.6078535	134.6078535	5.30	0.1048
X3	1	87.5525268	87.5525268	3.45	0.1604
X4	1	37.9243276	37.9243276	1.49	0.3091
X5	1	60.5981574	60.5981574	2.39	0.2202

Parameter	Estimate	Standard Error	t Value	Pr >  t
Intercept	4.42225240	1.11945357	3.95	0.0289
X1	0.38756832	2.39420301	0.16	0.8817
X2	-10.68980183	4.64427294	-2.30	0.1048
X3	-8.61894129	4.64304465	-1.86	0.1604
X4	3.35782810	2.74841807	1.22	0.3091
X5	14.76576243	9.56113494	1.54	0.2202

PROC REG NOWEIGHT

The REG Procedure

Model: MODEL1

Dependent Variable: Y

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	2	20.79725	10.39863	2.02	0.2141
Error	6	30.96170	5.16028		
Corrected Total	8	51.75895			

Root MSE 2.27163 R-Square 0.4018  
 Dependent Mean 4.29074 Adj R-Sq 0.2024  
 Coeff Var 52.94251

Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t
Intercept	1	3.83788	0.83885	4.58	0.0038
X1	1	-2.05556	1.31152	-1.57	0.1681
X2	1	-3.26061	2.59909	-1.25	0.2563

PROC REG NOWEIGHT

The REG Procedure

Model: MODEL1

Dependent Variable: Y

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	32.17318	6.43464	0.99	0.5404
Error	3	19.58577	6.52859		
Corrected Total	8	51.75895			

Root MSE 2.55511 R-Square 0.6216  
 Dependent Mean 4.29074 Adj R-Sq -0.0091  
 Coeff Var 59.54940

## Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t
Intercept	1	3.91960	1.23483	3.17	0.0503
X1	1	0.51587	3.25117	0.16	0.8840
X2	1	-7.22098	5.05505	-1.43	0.2485
X3	1	-4.82188	4.94994	-0.97	0.4018
X4	1	3.42857	3.86296	0.89	0.4402
X5	1	9.36501	12.09879	0.77	0.4953

PROC GLM NOWEIGHT

The REG Procedure

Model: MODEL2

Dependent Variable: Y

## Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	2	20.79725	10.39863	2.02	0.2141
Error	6	30.96170	5.16028		
Corrected Total	8	51.75895			
Root MSE	2.27163		R-Square	0.4018	
Dependent Mean	4.29074		Adj R-Sq	0.2024	
Coeff Var	52.94251				

## Parameter Estimates

Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t
Intercept	1	3.83788	0.83885	4.58	0.0038
X1	1	-2.05556	1.31152	-1.57	0.1681
X2	1	-3.26061	2.59909	-1.25	0.2563

PROC GLM NOWEIGHT

The GLM Procedure

Number of observations 9

Dependent Variable: Y

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	32.17318074	6.43463615	0.9	0.5404
Error	3	19.58576988	6.52858996		
Corrected Total	8	51.75895062			
R-Square		Coeff Var	Root MSE	Y Mean	
0.621596		59.54940	2.555111	4.290741	

Source	DF	Type I SS	Mean Square	F Value	Pr > F
X1	1	12.67592593	12.67592593	1.94	0.2578

X2	1	8.12132435	8.12132435	1.24	0.3460
X3	1	2.32149174	2.32149174	0.36	0.5930
X4	1	5.14285714	5.14285714	0.79	0.4402
X5	1	3.91158158	3.91158158	0.60	0.4953

Source	DF	Type III SS	Mean Square	F Value	Pr > F
X1	1	0.16437130	0.16437130	0.03	0.8840
X2	1	13.32175859	13.32175859	2.04	0.2485
X3	1	6.19514901	6.19514901	0.95	0.4018
X4	1	5.14285714	5.14285714	0.79	0.4402
X5	1	3.91158158	3.91158158	0.60	0.4953

Parameter	Estimate	Standard Error	t Value	Pr >  t
Intercept	3.919597315	1.23482719	3.17	0.0503
X1	0.515873016	3.25116872	0.16	0.8840
X2	-7.220984340	5.05504842	-1.43	0.2485
X3	-4.821879195	4.94994238	-0.97	0.4018
X4	3.428571429	3.86296406	0.89	0.4402
X5	9.365011186	12.09878615	0.77	0.4953

Type-3 tests of estimates of fixed effects

Genetic effect	Numerator df	Denominator df	F value	Pr > F
Additive (a)	1	175	4.08	0.0450
Dominance (d)	1	175	7.49	0.0068
Epistatic effects				
aa	1	175	0.33	0.5693
dd	1	175	18.34	<.0001
ad	1	175	18.19	<.0001

Additive, dominance, additive x dominance, and dominance x dominance effects are significant.





## Chapter 7

# PATHSAS: Path Coefficient Analysis of Quantitative Traits

Christopher S. Cramer  
Todd C. Wehner  
Sandra B. Donaghy

### *Purpose*

To calculate path coefficients (direct effects) and indirect effects between independent (x) and dependent (y) variables.

### *Definitions*

Path coefficient analysis: the correlation between two traits is a function of the direct relationship between two traits and the indirect relationships of related traits (Wright, 1934).

$$r_{10} = \rho_{01} + \rho_{02}r_{12} + \rho_{03}r_{13} + \rho_{04}r_{14}$$

where  $r_{10}$  = the correlation between  $X_1$  and  $Y$ ;  $\rho_{01}$  = the path coefficient between  $X_1$  and  $Y$ ;  $\rho_{02}$  = the path coefficient between  $X_2$  and  $Y$ ;  $r_{12}$  = the correlation between  $X_1$  and  $X_2$ ;  $\rho_{02}r_{12}$  = the indirect effect of  $X_2$  on the correlation between  $X_1$  and  $Y$ ;  $\rho_{03}$  = the path coefficient between  $X_3$  and  $Y$ ;  $r_{13}$  = the correlation between  $X_1$  and  $X_3$ ;  $\rho_{03}r_{13}$  = the indirect effect of  $X_3$  on the correlation between  $X_1$  and  $Y$ ;  $\rho_{04}$  = the path coefficient between  $X_4$  and  $Y$ ;  $r_{14}$  = the correlation between  $X_1$  and  $X_4$ ;  $\rho_{04}r_{14}$  = the indirect effect of  $X_4$  on the correlation between  $X_1$  and  $Y$ .

**Originator**

Wright, S. (1934). The method of path coefficients. *Annals of Mathematical Statistics* 5:161-215.

**Software Available**

Cramer, C.S., Wehner, T.C., and Donaghy, S.B. (1999). PATHSAS: A SAS computer program for path coefficient analysis of quantitative data. *Journal of Heredity* 90:260-262 (free of charge).

**Some References Where the Software Has Been Used**

Cramer, C.S. and Wehner, T.C. (1998). Fruit yield and yield component means and correlations of four slicing cucumber populations improved through six to ten cycles of recurrent selection. *Journal of American Society of Horticulture Science* 123:388-395.

Cramer, C.S. and Wehner, T.C. (1999). Little heterosis for yield and yield components in hybrids of six cucumber inbreds. *Euphytica* 110:101-110.

Cramer, C.S. and Wehner, T.C. (2000). Path analysis of the correlation between fruit number and plant traits of cucumber populations. *HortScience* 35(4):708-711.

**Contact**

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**EXAMPLE**

Data to be analyzed:

Plot	Replication	Cycle	Plant number	Pistillate flowers	Branch number	Leaf number	Total fruit number	Culled fruit number	Early fruit number
001	01	1	29	022	040	0240	01	00	00
002	02	1	21	017	034	0120	17	02	01
003	03	1	31	052	032	0440	29	15	03
004	04	1	30	049	077	0550	25	09	05
005	04	3	30	058	071	0810	30	10	05

006	03	3	23	039	040	0460	32	03	13
007	02	3	26	044	047	0460	27	07	08
008	01	3	22	023	027	0330	12	04	00
009	01	2	19	025	054	0510	27	05	04
010	02	2	27	035	038	0510	34	03	05
011	03	2	23	050	027	0290	01	00	00
012	04	2	32	035	055	0560	47	10	08
013	05	1	28	088	140	1315	58	13	27
014	06	1	28	162	105	0986	39	09	14
015	07	1	25	026	070	0741	36	05	10
016	08	1	31	074	125	0803	55	08	35
017	08	2	33	048	127	0870	57	11	13
018	07	2	25	069	038	0639	26	04	09
019	06	2	32	041	105	0878	31	04	13
020	05	2	30	021	098	0982	53	02	06
021	05	3	26	012	064	0622	31	03	09
022	06	3	31	024	111	1133	26	01	07
023	07	3	24	046	082	0879	33	04	04
024	08	3	28	048	161	1122	63	05	07

### ***SAS Program***

```

DATA DST1;
INPUT PLOT REP CYC PLANTNO PISTFLOW BRANCHNO LEAFNO TOTALNO CULLNO
      EARLYNO;
MARK=TOTALNO-CULLNO;
BRANPLAN=BRANCHNO/PLANTNO;
NODEBRAN=LEAFNO/(BRANCHNO+PLANTNO);
TOTFEMND=PISTFLOW+TOTALNO;
PERFENOD=(TOTFEMND/LEAFNO);
FRTSET=TOTALNO/PISTFLOW;
FRTPLANT=TOTALNO/PLANTNO;
MARKPLAN=MARK/PLANTNO;
EARPLAN=EARLYNO/PLANTNO;
CARDS;
001 01 1 29 022 040 0240 01 00 00
002 02 1 21 017 034 0120 17 02 01
003 03 1 31 052 032 0440 29 15 03
004 04 1 30 049 077 0550 25 09 05
005 04 3 30 058 071 0810 30 10 05
006 03 3 23 039 040 0460 32 03 13
007 02 3 26 044 047 0460 27 07 08

```

```

008 01 3 22 023 027 0330 12 04 00
009 01 2 19 025 054 0510 27 05 04
010 02 2 27 035 038 0510 34 03 05
011 03 2 23 050 027 0290 01 00 00
012 04 2 32 035 055 0560 47 10 08
013 05 1 28 088 140 1315 58 13 27
014 06 1 28 162 105 0986 39 09 14
015 07 1 25 026 070 0741 36 05 10
016 08 1 31 074 125 0803 55 08 35
017 08 2 33 048 127 0870 57 11 13
018 07 2 25 069 038 0639 26 04 09
019 06 2 32 041 105 0878 31 04 13
020 05 2 30 021 098 0982 53 02 06
021 05 3 26 012 064 0622 31 03 09
022 06 3 31 024 111 1133 26 01 07
023 07 3 24 046 082 0879 33 04 04
024 08 3 28 048 161 1122 63 05 07

```

```
;
```

```
%macro path(data,indep,dep0,dep,bylist,printreg,printout);
```

```
/*
```

```
Parameters to macro are:
```

```
data =name of dataset to analyze
```

```
indep=list of independent variables
```

```
dep0=primary dependent variable
```

```
dep=other dependent variables
```

```
bylist=by variable list
```

```
printreg=print regression? ( value is either yes or no)
```

```
printout=print results(direct,indirect effects)?
```

```
(value is either yes or no)
```

```
*/
```

```
%local noind word nodep noby bylast printr;
```

```
/* create noind macro variable
```

```
*/
```

```
/* noind is the number of independent variables in &indep
```

```
*/
```

```
%let noind=0;
```

```
%if &indep ne %then %do;
```

```
%let word=%scan(&indep,1);
```

```
%do %while (&word ne );
```

```
%let noind=%eval(&noind+1);
```

```
%let word=%scan(&indep,&noind+1);
```

```
%end;
```

```
%end;
```

```
/* create nodep macro variable
```

```
*/
```

```
/* nodep is the number of dependent variables in &dep
```

```
*/
```

```
%let nodep=0;
```

```
%if &dep ne %then %do;
```

```
%let word=%scan(&dep,1);
```

```
%do %while (&word ne );
```

```
%let nodep=%eval(&nodep+1);
```

```
%let word=%scan(&dep,&nodep+1);
```

```
%end;
```

```
%end;
```

```
/* create noby macro variable
```

```
*/
```

```

/* noby is the number of by variables in &bylist          */
%let noby=0;
%if &bylist ne %then %do;
  %let word=%scan(&bylist,1);
  %do %while (&word ne );
    %let noby=%eval(&noby+1);
    %let word=%scan(&bylist,&noby+1);
  %end;
%let bylast=%scan(&bylist,&noby);

/* create printr macro variable                          */
/* printr has a blank value or the value NOPRINT        */
/* specifies whether to print regression output or not  */
%if %upcase(&printreg)=YES %then %let printr=;
%else %let printr=noprintr;

data data1; set &data;
  keep &bylist &dep0 &dep &indep;
run;

proc sort data=data1;
  by &bylist;
proc standard data=data1 mean=0 std=1 out=sdata2;
  by &bylist;
  var &indep &dep0 &dep;
run;

proc reg data=sdata2 &printr
  outsscp=sscp(keep=&bylist intercep _type_)
  outest=estdep(drop=_model_ _type_ _rmse_ intercep);
  by &bylist;
  model &dep0=&indep;
run;

/*
_type_='N' is the number of obs in the dataset;
nobs, number of obs., is created
needed for checking that there are enough obs.
if not, the reg. coefficients are biased, and need to set to miss-
ing
*/
data sscp; set sscp;
  if _type_='N';
  rename intercep=nobs;
  drop _type_;

/* if no. of obs. is <= the no. of indep. variables, then
   set the regression coefficients to missing          */
data estdep; merge sscp estdep;
  by &bylist;
  array v &indep;
  look='no ';
  if nobs<=&noindep then do;
    look='yes';
    do over v;
      v=.;

```

```

        end;
    end;
run;

proc print data=estdep;
    where look='yes';
    var &bylist nob;
title3
'The following identification levels do not have enough obs. for anal-
    ysis';
title4 ' ' and the regression coefficients were set to missing
    ';
    run;
title3 ' ' ;

proc reg data=sdata2 &printr
    outest=estindep(drop=_model_ _type_ _rmse_ intercep);
    by &bylist;
    model &dep=&dep0;
    run;

data estind2; set estindep;
    by &bylist;
    array r regc1-regc&nodep;
    retain regc1-regc&nodep;
    if first.&bylast then _i_=0;
    _i_+1;
    r=&dep0;
    if last.&bylast then do;
        output;
        do over r;
            r=.;
            end;
        end;
    drop &dep0 &dep _depvar_;
    run;

proc corr data=data1 outp=corr noprint;
    by &bylist;
    var &indep;
    run;

data corr; set corr;
    if _type_='CORR';
    drop _type_;
    run;

data estdep; set estdep;
    array reg &indep;
    array r2 reg1-reg&noind;
    do over reg;
        r2=reg;
        end;
    drop &indep;
    run;

data tog;
    merge corr estdep;

```

```

by &bylist;
array dir &indep;
array corr &indep;
array r2 reg1-reg&noind;
if first.&bylast then do;
  totc=0;
  n=0;
end;
n+1;
&dep0=.;
do over dir;
  if n=_i_ then dir= r2;
  else dir=r2*corr;
  &dep0 + dir;
end;
drop n;
keep &bylist--_name_ &indep &dep0 _depvar_ nob;
format &indep &dep0_5.2;
run;

data tog2; merge tog estind2; by &bylist;
array r regc1-regc&nodep;
array t &dep;
do over r;
  t=&dep0 * r;
end;
format &dep &dep0 5.2;
format regc1-regc&nodep 5.2;
* drop regc1-regc&nodep;
drop _depvar_;
run;

%if %upcase(&printout)=YES %then
  %str(proc print data=tog2(drop=regc1-regc&nodep); run);

%mend path;

%path(data=dst1,
  indep=branplan nodebran perfenod frtset,
  dep0=frtplant,
  dep=markplan earplan,
  bylist=cyc,
  printreg=no,
  printout=yes
);

RUN;

```

## SAS Output

	B	N	P		F	M	
	R	O	E		T	A	E
	A	D	R	F	T	R	A
$\bar{N}$	N	E	F	R	P	K	R
A	P	B	E	T	N	L	P



	O	C	M	L	R	N	S	O	A	L	L
	B	Y	E	A	A	O	E	B	N	A	A
	S	C		N	N	D	T	S	T	N	N
001	1	BRAN	PLAN	0.72	0.18	-0.06	0.03	8	0.87	0.80	0.78
002	1	NODE	BRAN	0.37	0.34	-0.10	0.04	8	0.65	0.61	0.59
003	1	PERF	ENOD	-0.17	-0.15	0.23	0.01	8	-0.08	-0.07	-0.07
004	1	FRT	SET	0.07	0.05	0.01	0.30	8	0.42	0.39	0.38
005	2	BRAN	PLAN	0.72	-0.13	-0.41	0.42	8	0.61	0.54	0.31
006	2	NODE	BRAN	-0.26	0.34	0.01	-0.01	8	0.08	0.07	0.04
007	2	PERF	ENOD	-0.58	0.01	0.50	-0.53	8	-0.60	-0.53	-0.30
008	2	FRT	SET	0.40	-0.01	-0.34	0.77	8	0.82	0.72	0.41
009	3	BRAN	PLAN	1.06	-0.03	-0.37	0.12	8	0.78	0.75	0.28
010	3	NODE	BRAN	-0.15	0.20	-0.31	-0.10	8	-0.36	-0.35	-0.13
011	3	PERF	ENOD	-0.46	-0.07	0.86	-0.22	8	0.10	0.09	0.04
012	3	FRT	SET	0.28	-0.04	-0.42	0.46	8	0.28	0.26	0.10

## Chapter 8

# Restricted Maximum Likelihood Procedure to Estimate Additive and Dominance Genetic Variance Components

Agron Collaku

### *Purpose*

To estimate narrow-sense heritability without any restriction in mating design.

### *Definitions*

Estimation of genetic variance components for additive and dominance effects is important in plant breeding for estimating narrow-sense heritability and predicting the results of selection. Quantitative genetic methods used to estimate genetic variance components are based on strict mating designs with a number of restrictions for the way genotypes are produced. Many of the restrictions are untenable in common breeding programs. The restricted maximum likelihood (REML) method is advantageous because it provides genetic variance estimates without any restriction in mating design not only for balanced data but also for unbalanced data. REML estimates of additive and dominance variance components using a mixed-model approach are obtained based on the following formulas.

### *Additive Variance*

The additive genetic variance component measures the expected mean genotypic effect in the selected material and can be estimated from the equation

$$COV_{HS} = 2r_{xy}\sigma_A^2$$

where  $COV_{HS}$  is the covariance among half-sib families,  $r_{xy}$  is the coancestry coefficient that measures the relationship among parents of half-sib families, and  $\sigma_A^2$  is additive genetic variance component.

### Dominance Variance

The dominance genetic variance component measures deviations of genotypic values from their additive effects due to interaction between alleles at the same locus. It can be estimated from the equation

$$COV_{FS} = 2r_{xy}\sigma_A^2 + u_{xy}\sigma_D^2$$

where  $COV_{FS}$  is the covariance among full-sib families,  $u_{xy}$  is the double coancestry coefficient that measures the relationship among parents of full-sib families, and  $\sigma_D^2$  is dominance genetic variance component.

The preceding equations assume no epistatic interaction of any kind.

The mixed model fitted to obtain additive and dominance genetic variances is

$$y = X\beta + Z_1\alpha + Z_2\gamma + Z_3\delta + \epsilon$$

where  $y$  is a vector of  $n \times 1$  observations;  $n$  is the number of observations for each entry in each year and each environment;  $X$  is the design matrix of fixed effects, and  $\beta$  is a  $b \times 1$  vector of fixed effects,  $Z_1$  is the design matrix of additive effects, and  $\alpha$  is a  $a \times 1$  vector;  $a$  is the number of populations or crosses in the genetic design;  $Z_2$  is the design matrix of dominance effects, and  $\gamma$  is a  $d \times 1$  vector, and  $d$  is the number of populations;  $Z_3$  is the design matrix of entry-by-environment interaction (GE) effects, and  $\delta$  is a  $g \times 1$  vector;  $g$  is the cross combination of entries with environments; and  $\epsilon$  is the vector of experimental error effects.

Random effects (additive, dominance, GE, and error) have the following variance-covariance matrix:

$$\text{Var} \begin{pmatrix} \alpha \\ \delta \end{pmatrix} = \begin{pmatrix} A\sigma_A^2 & 0 & 0 & 0 \\ 0 & D\sigma_D^2 & 0 & 0 \\ 0 & 0 & I\sigma_{GE}^2 & 0 \\ 0 & 0 & 0 & I\sigma^2 \end{pmatrix}$$

where  $A$  is a matrix of  $n \times n$ . The diagonal elements of  $A$  are equal to 1 and the off-diagonal elements are equal to the coancestry coefficient times two ( $2r_{xy}$ ) between  $n$  entries in the study. The matrix of coancestry coefficients can be obtained by using PROC INBREED of SAS (see example).  $D$  is a matrix of  $n \times n$  with diagonal elements equal to 1/4, i.e., double coancestry coefficients within full-sib entries and off-diagonal elements are double coancestry coefficients among full-sib entries.  $I$  is an identity matrix.

Mixed model equations are used to obtain estimates of  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$ . REML estimates for genetic variance components (additive and dominance) as well as for other components are obtained by running PROC MIXED in SAS, in which  $A$  and  $D$  matrices are appended (see example).

## References

These key references used maximum likelihood estimators to estimate additive and dominance genetic variance components:

- Bernardo, R. (1994). Prediction of maize single-cross performance using RFLPs and information from related hybrids. *Crop Science* 34(1):20-25.
- Collaku, A. (2000). Heritability of waterlogging tolerance in wheat (pp. 53-78). Doctoral dissertation, Louisiana State University, Baton Rouge, Louisiana.

## Contact

- A. Collaku, Department of Pharmacogenomics, Johnson & Johnson Research and Development, Raritan, New Jersey 08869.

## EXAMPLE

Four  $F_2$  populations (crosses) of soft red winter wheat were studied:

- Cross No. 1 - Tchere/savannah//GA 85240
- Cross No. 2 - Tchere/savannah//PION 2643
- Cross No. 3 - Tchere/DS 2368//GA 85240
- Cross No. 4 - Tchere/DS 2368//PION 2691

Five random full-sib families from each cross totaling twenty entries were studied in a randomized complete block design with three replications. The experiment was conducted for two years. Double coancestry co-

efficients between entries 6-15=0.0625. Diagonal elements of  $D$  matrix = 0.25 which represented double coancestry coefficients of within full-sib families. All other elements of  $D$  matrix were zero. Based on these elements, a matrix was constructed and appended to the data analyzed using PROC MIXED.

Data to be analyzed (Yield):

LINE	YEAR	REP	CROSS	YIELD
1	1	1	1	150.0
1	1	2	1	130.0
1	1	3	1	141.3
2	1	1	1	178.0
2	1	2	1	172.6
2	1	3	1	167.0
3	1	1	1	148.0
3	1	2	1	120.0
3	1	3	1	.
4	1	1	1	108.5
4	1	2	1	113.0
4	1	3	1	123.0
5	1	1	1	89.0
5	1	2	1	90.0
5	1	3	1	92.0
6	1	1	2	93.8
6	1	2	2	121.5
6	1	3	2	86.0
7	1	1	2	113.0
7	1	2	2	107.0
7	1	3	2	.
8	1	1	2	113.0
8	1	2	2	111.4
8	1	3	2	109.8
9	1	1	2	68.0

9	1	2	2	47.0
9	1	3	2	56.0
10	1	1	2	100.0
10	1	2	2	68.0
10	1	3	2	94.0
11	1	1	3	159.0
11	1	2	3	151.3
11	1	3	3	.
12	1	1	3	172.0
12	1	2	3	139.0
12	1	3	3	.
13	1	1	3	127.0
13	1	2	3	.
13	1	3	3	92.0
14	1	1	3	109.0
14	1	2	3	138.0
14	1	3	3	119.2
15	1	1	3	159.0
15	1	2	3	152.0
15	1	3	3	137.0
16	1	1	4	152.6
16	1	2	4	147.0
16	1	3	4	.
17	1	1	4	134.0
17	1	2	4	184.3
17	1	3	4	125.0
18	1	1	4	134.0
18	1	2	4	146.3
18	1	3	4	186.4
19	1	1	4	107.0
19	1	2	4	90.0
19	1	3	4	124.0
20	1	1	4	77.0

20	1	2	4	113.0
20	1	3	4	96.7

LINE	YEAR	REP	CROSS	YIELD
1	2	1	1	118.6
1	2	2	1	98.2
1	2	3	1	108.9
2	2	1	1	80.9
2	2	2	1	119.5
2	2	3	1	76.0
3	2	1	1	112.6
3	2	2	1	96.5
3	2	3	1	99.3
4	2	1	1	80.3
4	2	2	1	73.2
4	2	3	1	72.2
5	2	1	1	65.3
5	2	2	1	54.3
5	2	3	1	58.4
6	2	1	2	61.7
6	2	2	2	81.3
6	2	3	2	66.0
7	2	1	2	65.5
7	2	2	2	95.8
7	2	3	2	88.2
8	2	1	2	.
8	2	2	2	103.0
8	2	3	2	103.9
9	2	1	2	60.3
9	2	2	2	79.8
9	2	3	2	70.2
10	2	1	2	137.8

10	2	2	2	128.4
10	2	3	2	.
11	2	1	3	82.5
11	2	2	3	74.3
11	2	3	3	78.5
12	2	1	3	132.4
12	2	2	3	128.7
12	2	3	3	116.1
13	2	1	3	87.0
13	2	2	3	88.9
13	2	3	3	61.8
14	2	1	3	121.9
14	2	2	3	98.4
14	2	3	3	112.3
15	2	1	3	84.7
15	2	2	3	105.0
15	2	3	3	98.2
16	2	1	4	113.4
16	2	2	4	105.7
16	2	3	4	101.3
17	2	1	4	114.8
17	2	2	4	131.2
17	2	3	4	117.7
18	2	1	4	71.3
18	2	2	4	41.8
18	2	3	4	45.2
19	2	1	4	.
19	2	2	4	100.6
19	2	3	4	115.0
20	2	1	4	129.1
20	2	2	4	113.6
20	2	3	4	139.7

data c;



```
input F $ M $ Cross $ Line $ Gene;
datalines;
```

TCH.	SAV	P1	P1	1
P1	GA	1	1	2
P1	GA	1	2	2
P1	GA	1	3	2
P1	GA	1	4	2
P1	GA	1	5	2
P1	P.2643	2	6	2
P1	P.2643	2	7	2
P1	P.2643	2	8	2
P1	P.2643	2	9	2
P1	P.2643	2	10	2
TCH.	DS	P2	P2	1
P2	GA	3	11	2
P2	GA	3	12	2
P2	GA	3	13	2
P2	GA	3	14	2
P2	GA	3	15	2
P2	P.2691	4	16	2
P2	P.2691	4	17	2
P2	P.2691	4	18	2
P2	P.2691	4	19	2
P2	P.2691	4	20	2

```
;
```

```
proc inbreed data=c covar outcov=matrix;
var line f m;
data matrix;
set matrix;
if substr(line,1,1)>0;
drop OBS _TYPE_ _PANEL_ LINE F M;
proc print data=matrix;
run;
data two;
```

```
retain row (0);
parm=1;
set matrix(drop=_col_ col1-col4 col10 col16 col17 col23);
if substr(line,1,1)>0;
drop _type_ _panel_ line f m;
array old col5--col28;
array new ncol1-ncol20;
do over old;
  new=old;
end;
drop col5--col28;
row+1;
run;
data two;
set two;
array old ncol1-ncol20;
array new col1-col20;
do over old;
  new=old;
end;
drop ncol1-ncol20;
run;
data three;
row=1;
parm=2;
array dmat{20} col1-col20;
do j=1 to 20;
  dmat{j}=0;
end;
do i=1 to 5;
  do j=1 to 5;
    dmat{j}=0.25;
  end;
  parm=2;
  row=i;
  output;
end;
do j=1 to 20;
  dmat{j}=0;
end;
do i=6 to 10;
```

```

do j=6 to 10;
  dmat{j}=0.25;
  dmat{j+5}=0.0625;
end;
parm=2;
row=i;
output;
end;
do j=1 to 20;
  dmat{j}=0;
end;
do i=11 to 15;
  do j=11 to 15;
    dmat{j}=0.0625;
    dmat{j+5}=0.25;
  end;
  parm=2;
  row=i;
  output;
end;
do j=1 to 20;
  dmat{j}=0;
end;
do i=16 to 20;
  do j=16 to 20;
    dmat{j}=0.25;
  end;
  parm=2;
  row=i;
  output;
end;
drop i j;
run;
data mat20;
set two three;
run;
data varcomp;
input line year rep cross yield;
cards;

```

1	1	1	1	150.0
1	1	2	1	130.0

1	1	3	1	141.3
2	1	1	1	178.0
2	1	2	1	172.6
.	.	.	.	.
.	.	.	.	.
18	2	1	4	71.3
18	2	2	4	41.8
18	2	3	4	45.2
19	2	1	4	.
19	2	2	4	100.6
19	2	3	4	115.0
20	2	1	4	129.1
20	2	2	4	113.6
20	2	3	4	139.7

```

;
Proc Mixed covtest;
class l yr rep cr;
model yield = yr rep(yr);
random l/type=Lin(2) ldata=mat80 ;
random yr*l(cr);
parms (110) (100) (700) (200);
run;

```

### SAS Output

#### Covariance Parameter Estimates (REML)

Cov Parm	Estimate	Std Error	Z	Pr> Z
LIN (1)	111.66689661	19.28580197	5.79	0.0001
LIN(2)	386.10778285	592.07749876	0.65	0.5143
ENTRY*YEAR(CROSS)	577.41756955	156.55363443	3.69	0.0002
Residual	203.03072111	35.06509448	5.79	0.0001

## Tests of Fixed Effects

Source	NDF	DDF	Type III	F Pr>F
YEAR	1	19	11.91	0.0027
REP(YEAR)	4	67	0.31	0.8707

In the previous output,

Lin(1) is  $\hat{\sigma}_A^2$  – the estimate of additive variance component, and

Lin(2) is  $\hat{\sigma}_D^2$  – the estimate of dominance variance component.

Changes needed in this program:

- Calculate double coancestry coefficients among a group of full-sib families and then construct matrix D as shown in the program.
- When appending matrices A and D, use the number of columns corresponding to each set of full-sib families included in the study.

## Chapter 9

# Calculating Additive Genetic Correlation Using ANOVA and the Sum Method of Estimating Covariance

Blair L. Waldron

### *Importance*

Genetic correlations allow breeders to predict the correlated response due to pleiotropy and/or linkage in unselected traits. For this reason, they are often required in many selection indices.

### *Definitions*

#### *Additive Genetic Correlations*

Estimated as

$$r_{A(xy)} = \sigma_{A(xy)} / \sqrt{(\sigma^2_{A(x)}\sigma^2_{A(y)})}$$

where  $\sigma_{A(xy)}$  is the additive genetic covariance of means for traits  $x$  and  $y$ , and  $\sigma_{A(x)}$  and  $\sigma_{A(y)}$  are the additive genetic standard deviations for traits  $x$  and  $y$ , respectively. Approximate standard errors for genetic correlations can be calculated as described by Falconer (1989). This assumes an appropriate family structure exists within the population of interest such that additive genetic variance ( $\sigma^2_A$ ) can be derived. Most often, half-sib families (HSFs) are used where it is assumed that the variance among HSFs =  $\frac{1}{4}\sigma^2_A$ .

*Sum Method of Estimating Covariance*

The sum method is based on the statistical property of the sum of two random variables, which states:

$$\text{Var}(X + Y) = \text{Var}(X) + \text{Var}(Y) + 2\text{Cov}(X, Y)$$

This can be rearranged and written as

$$\text{Cov}(X, Y) = [\text{Var}(X + Y) - \text{Var}(X) - \text{Var}(Y)] / 2.$$

In this case,  $X$  and  $Y$  refer to two different traits evaluated within the same population.

Using ANOVA we get an estimate (mean square) for  $\text{Var}(X)$ ,  $\text{Var}(Y)$ , and  $\text{Var}(X+Y)$  (most often referred to as the mean cross product, or MCP). The  $\text{Var}(X+Y)$  (e.g., MCP) is obtained by running ANOVA on a new variable created by summing the plot mean values for trait  $X$  and trait  $Y$  for each level of observation within each HSF ( $X_{ij} + Y_{ij}$ ).

*Additive Genetic Variance and Covariance*

Standard procedures for isolating appropriate variance components, based on expected mean squares, are used to estimate additive genetic variances and covariances where, as previously stated, it is assumed that

$$\sigma^2_{HSF(x)} = \frac{1}{4}\sigma^2_{A(x)}; \sigma^2_{HSF(y)} = \frac{1}{4}\sigma^2_{A(y)}; \text{ and}$$

$$\sigma_{HSF(xy)} \text{ (e.g., covariance among HSFs for } x \text{ and } y) = \frac{1}{4}\sigma_{A(xy)} \text{ (e.g., additive genetic covariance between traits } x \text{ and } y).$$

The appropriate linear combination of mean squares or mean cross products is used to solve for  $\sigma^2_{HSF(x)}$ ,  $\sigma^2_{HSF(y)}$ , and  $\sigma^2_{HSF(xy)}$ , respectively (see the following example).

*Important Considerations*

a. Because the additive genetic correlation is a function of two mathematical equations (i.e., the linear combination of mean squares or mean cross products to solve for variance components, and the statistical prop-

erty that  $Cov(X, Y) = [Var(X + Y) - Var(X) - Var(Y)] / 2$ , all components will contribute to the standard error of the correlation. In some cases, this can lead to large standard errors for the correlation estimate, resulting in correlations greater than 1.

b. As is the case with the estimation of all genetic parameters, consideration should be given as to how many HSFs are needed to obtain reliable estimates. In general, the more heritable a character, the fewer HSFs needed to obtain good genetic correlation estimates. Fifteen to twenty HSFs is the minimal acceptable range that can be used.

c. Traits  $X$  and  $Y$  may differ widely in overall scale due to differences in concentration and/or units of measurement. For example, for a particular forage quality study, mean neutral detergent fiber (NDF) may equal 508 g·kg<sup>-1</sup> (range: 478 to 539), whereas mean magnesium concentration may equal 2.18 g·kg<sup>-1</sup> (range: 1.56 to 2.69). The sum of the average NDF and magnesium concentrations would equal 510.18 and is heavily weighted toward NDF. In such a case, the sum method could produce misleading results. When these types of data are used, they should first be standardized, such that traits  $X$  and  $Y$  are both on the same scale. One standardization method that effectively cancels scaling differences is to divide each trait's raw data by its mean standard deviation prior to creating the  $X + Y$  variable (Frey and Horner, 1957).

### ***Originator***

The sum method of estimating additive genetic covariances originated at North Carolina State University during the theoretical development and application of mating designs I and II. This method was taught by Dr. Robert E. Stucker (a North Carolina State University graduate) at the University of Minnesota in the Statistical Topics in Plant Sciences course.

### ***Key References Using the Formula***

Waldron, B.L., Ehlke, N.J., Wyse, D.L., and Vellekson, D.J. (1998). Genetic variation and predicted gain from selection for winterhardiness and turf quality in a perennial ryegrass topcross population. *Crop Science* 38:817-822.

### ***Contact***

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**EXAMPLE**

Traits  $X$  and  $Y$  are visual scores where the range is 1-9; HSFs were evaluated in multiple locations for one year using a randomized complete block (RCB) design. All variables are assumed to be random.

**Step 1. Creating  $X + Y$  Variable**

HSF	Trait $X$	Trait $Y$	Trait $X + Y$
1	9	8	17
2	8	3	11
3	5	4	9
.	.	.	.
.	.	.	.
.	.	.	.
$n$	$X_n$	$Y_n$	$X_n + Y_n$

**Step 2. ANOVA for Traits  $X$  and  $Y$** 

Source	DF	Mean Square	Expected Mean Square
Location	$l-1$	$MS_{L(x \text{ or } y)}$	$\sigma^2_{E(x \text{ or } y)} + r \sigma^2_{HL(x \text{ or } y)} + h \sigma^2_{RL(x \text{ or } y)} + rh \sigma^2_{L(x \text{ or } y)}$
Rep in Loc	$l(r-1)$	$MS_{RL(x \text{ or } y)}$	$\sigma^2_{E(x \text{ or } y)} + h \sigma^2_{RL(x \text{ or } y)}$
HSF	$h-1$	$MS_{H(x \text{ or } y)}$	$\sigma^2_{E(x \text{ or } y)} + r \sigma^2_{HL(x \text{ or } y)} + rl \sigma^2_{H(x \text{ or } y)}$
HSF $\times$ Loc	$(h-1)(l-1)$	$MS_{HL(x \text{ or } y)}$	$\sigma^2_{E(x \text{ or } y)} + r \sigma^2_{HL(x \text{ or } y)}$
Error	$l(r-1)(h-1)$	$MS_{E(x \text{ or } y)}$	$\sigma^2_{E(x \text{ or } y)}$

**Step 3. ANOVA for Traits  $X + Y$** 

Source	DF	MCP	Expected Mean Cross Product
Location	$l-1$	$MCP_{L(x+y)}$	$\sigma_{E(x+y)} + r \sigma_{HL(x+y)} + h \sigma_{RL(x+y)} + rh \sigma_{L(x+y)}$
Rep in Loc	$l(r-1)$	$MCP_{RL(x+y)}$	$\sigma_{E(x+y)} + h \sigma_{RL(x+y)}$
HSF	$h-1$	$MCP_{H(x+y)}$	$\sigma_{(x+y)} + r \sigma_{HL(x+y)} + rl \sigma_{H(x+y)}$

$$\begin{array}{l} \text{HSF} \times \text{Loc} \quad (h-1)(l-1) \quad \text{MCP}_{HL(x+y)} \quad \sigma_{E(x+y)} + r \sigma_{HL(x+y)} \\ \text{Error} \quad \quad \quad 1(r-1)(h-1) \quad \text{MCP}_{E(x+y)} \quad \quad \quad E(x+y) \end{array}$$

MCP is the the mean square value resulting from ANOVA on the new variable  $X+Y$ .

**Step 4. Solving for Appropriate Variance Components**

$$\begin{aligned} \sigma^2_{A(x)} &= ((\text{MS}_{H(x)} - \text{MS}_{HL(x)}) / rl) \\ \sigma^2_{A(y)} &= ((\text{MS}_{H(y)} - \text{MS}_{HL(y)}) / rl) \\ \sigma^2_{A(x+y)} &= ((\text{MCP}_{H(x+y)} - \text{MCP}_{HL(x+y)}) / rl) \end{aligned}$$

**Step 5. Solving for Additive Genetic Covariance Between Traits X and Y**

$$\sigma_{A(xy)} = (\sigma^2_{A(x+y)} - \sigma^2_{A(x)} - \sigma^2_{A(y)}) / 2$$

**Step 6. Calculating Additive Genetic Correlation Between Traits X and Y**

$$r_{A(xy)} = \sigma_{A(xy)} / \sqrt{(\sigma^2_{A(x)} \sigma^2_{A(y)})}$$

REFERENCES

Falconer, D.S. (1989). *Introduction to quantitative genetics*, Third edition. John Wiley & Sons, Inc., New York, p. 317.  
 Frey, K.J. and Horner, T. (1957). Heritability in standard units. *Agronomy Journal* 49: 59-62.



## Chapter 10

# Developmental Analysis for Quantitative Traits

Jun Zhu

### *Purpose*

To analyze developmental quantitative traits.

### *Definitions*

#### *Genetic Model*

For time-dependent traits, the phenotypic data observed at time  $t$  ( $t=1, 2, \dots$ ) have the following mixed linear model:

$$y_{(t)} = \mathbf{X}b_{(t)} + \sum_{u=1}^m \mathbf{U}_u e_{u(t)} \\ \sim N(\mathbf{X}b_{(t)}, \mathbf{V}_{(t)} + \sum_{u=1}^m \sigma_{u(t)}^2 \mathbf{U}_u \mathbf{U}_u^T)$$

Variance at time  $t$ ,  $\sigma_{u(t)}^2$ , can measure genetic variation accumulated from the initial time to time  $t$ . Given the observed phenotype vector  $y_{(t-1)}$  measured at time  $(t-1)$ , the conditional random variables of  $y_{(t)} | y_{(t-1)}$  at time  $t$  have conditional distribution:

$$y_{(t)} | y_{(t-1)} = \mathbf{X}b_{(t|t-1)} + \sum_{u=1}^m \mathbf{U}_u e_{u(t|t-1)} \\ \sim N(\mathbf{X}b_{(t|t-1)}, \mathbf{V}_{(t|t-1)} + \sum_{u=1}^m \sigma_{u(t|t-1)}^2 \mathbf{U}_u \mathbf{U}_u^T)$$

Since conditional  $y_{(t)} | y_{(t-1)}$  is independent of  $y_{(t-1)}$ , conditional random effects,  $e_{(t|t-1)}$ , and conditional variance components,  $\sigma_{u(t|t-1)}^2$  contain extra variation from time  $t-1$  to time  $t$ , which is not explainable by the accumulated effects of the initial time to time  $t-1$ .

### **Analysis**

With observed phenotypic data at time  $t-1$  ( $y_{(t-1)}$ ) and time  $t$  ( $y_{(t)}$ ), a new random vector  $y_{(*)}$  can be obtained using mixed model approaches (Zhu, 1995):

$$y_{(*)} = y_{(t)} - C_{(t-1,t)} V_{(t-1)}^{-1} (y_{(t-1)} - Xb_{(t-1)})$$

The new random vector has variance,

$$\text{var}(y_{(*)}) = V_{(t)} - C_{(t-1,t)} V_{(t-1)}^{-1} C_{(t,t-1)},$$

which is identical to the conditional variance-covariance matrix of  $V_{(t|t-1)}$ . It can be proved that  $y_{(*)}$  is independent of  $y_{(t-1)}$ .

When the new data ( $y_{(*)}$ ) are used to fit the genetic model,

$$\begin{aligned} y_{(*)} &= Xb_{(*)} + \sum_{u=1}^m \sigma_{u^{(*)}}^2 U_u U_u^T \\ &\sim N(Xb_{(*)}, V_{(*)} + \sum_{u=1}^m \sigma_{u^{(*)}}^2 U_u U_u^T) \end{aligned}$$

unbiased estimation of variances,  $\sigma_{u^{(*)}}^2$ , can be obtained by REML or MINQUE(1) approaches (Zhu, 1995). Prediction of random effects,  $e_{u^{(*)}}$ , can be obtained by the linear unbiased prediction (LUP) method (Zhu, 1992; Zhu and Weir, 1996) or the adjusted unbiased prediction (AUP) method (Zhu, 1993; Zhu and Weir, 1996). Since  $\sigma_{u^{(*)}}^2$  is equivalent to the conditional variance  $\sigma_{u(t|t-1)}^2$ , genetic effects  $e_{u^{(*)}}$  also have an equivalency to the conditional genetic effects  $e_{u(t|t-1)}$ .

### **Originator**

Zhu, J. (1992). Mixed model approaches for estimating genetic variances and covariances. *Journal of Biomathematics* 7(1):1-11.

- Zhu, J. (1993). Methods of predicting genotype value and heterosis for offspring of hybrids. *Journal of Biomathematics* 8(1):32-44.
- Zhu, J. (1995). Analysis of conditional effects and variance components in developmental genetics *Genetics* 141(4):1633-1639.
- Zhu, J. and Weir, B.S. (1996). Diallel analysis for sex-linked and maternal effects. *Theoretical and Applied Genetics* 92(1):1-9.

### **Software Available**

- Zhu, J. (1997). GENCOND1.EXE a computer software for calculating conditional phenotypic data. *Analysis Methods for Genetic Models* (pp. 278-285), Agricultural Publication House of China, Beijing (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.

### **EXAMPLE**

Unconditional data (BOL8/4 and BOL8/9) to be analyzed (file: COTBOLM.TXT) (Parent = 4, Year = 2, Blk = 1):

Env	Fem	Male	Cross	BLK	BOL8/4	BOL8/9
1	1	1	0	1	6.46	8.14
1	1	2	1	1	5.77	7.85
1	1	3	1	1	8.64	9.01
1	1	4	1	1	8.33	10.30
1	2	1	1	1	6.70	8.74
1	2	2	0	1	5.65	7.90
1	2	3	1	1	7.94	9.13
1	2	4	1	1	8.47	11.24
1	3	1	1	1	8.72	9.29
1	3	2	1	1	9.32	10.36
1	3	3	0	1	4.98	5.35
1	3	4	1	1	8.90	10.14
1	4	1	1	1	7.58	9.74
1	4	2	1	1	8.74	11.08
1	4	3	1	1	9.34	11.49
1	4	4	0	1	7.02	8.90
2	1	1	0	1	8.06	11.63
2	1	2	1	1	11.36	15.18
2	1	3	1	1	9.31	10.58
2	1	4	1	1	13.30	15.76
2	2	2	0	1	8.09	12.39

2	2	3	1	1	10.87	13.50
2	2	4	1	1	15.60	20.45
2	3	3	0	1	5.05	5.78
2	3	4	1	1	12.76	14.26
2	4	4	0	1	12.29	15.86

Conditional data (BOL8/9|BOL8/4) produced and to be analyzed (Parent = 4, Year = 2, Blk = 1):

Year	Fem	Male	Cross	Blk	BOL8/9 BOL8/4
1	1	1	0	1	9.75974
1	1	2	1	1	10.0186
1	1	3	1	1	8.54954
1	1	4	1	1	9.42577
1	2	1	1	1	9.98357
1	2	2	0	1	10.3079
1	2	3	1	1	9.30607
1	2	4	1	1	10.1621
1	3	1	1	1	8.74997
1	3	2	1	1	9.16348
1	3	3	0	1	8.62587
1	3	4	1	1	8.8201
1	4	1	1	1	9.61174
1	4	2	1	1	9.73354
1	4	3	1	1	9.73246
1	4	4	0	1	8.86123
2	1	1	0	1	14.6502
2	1	2	1	1	14.8385
2	1	3	1	1	12.6994
2	1	4	1	1	12.6991
2	2	2	0	1	14.9987
2	2	3	1	1	13.9182
2	2	4	1	1	14.949
2	3	3	0	1	12.5327
2	3	4	1	1	12.0607
2	4	4	0	1	12.8132

1. Run GENAD.EXE to create mating design matrix files and unconditional data for the additive-dominance (AD) model. Before running these programs, create a data file (e.g., COTBOLM.TXT) for your analysis of unconditional data with five design columns followed by trait columns, which are (1) environment, (2) maternal, (3) paternal, (4) generation, and (5) replication. There is a limitation (<100 traits)

- for the number of trait columns. The data file COTBOLM.TXT contains phenotypic data of two traits (BOL8/4 and BOL8/9).
2. Run the program GENCOND1.EXE for constructing conditional data. The conditional data will have five design columns and will be stored in a file with the name COTBOLM.CON. Afterward, run GENAD.EXE again using the conditional data file COTBOLM.CON to create files for mating design matrix and conditional data by the AD model.
  3. Conditional variances and conditional genetic effects can be obtained by running programs for variance analyses. Standard errors of estimates are calculated by jackknife procedures. If you have multiple blocks for your experiments, you can use GENVAR1R.EXE for jackknifing over blocks. Otherwise, you can use GENVAR1C.EXE or GENCOV1C.EXE for jackknifing over cell means. These two programs will allow you to choose the parental type (inbred or outbred) and the prediction methods (LUP or AUP). You also need to input coefficients (1, 0, or -1) for conducting linear contrasts for genetic effects of parents.
  4. The results will be automatically stored in text files for later use or printing. An example of results is provided in a file named COTBOLM.VAR (output 1) for analysis of conditional variance and conditional genetic effects.
  5. Developmental genetic analysis can also be conducted for other genetic models, such as GENADM.EXE for additive, dominance, and maternal models with  $G = A + D + M$ ; GENADE.EXE for additive, dominance, and epistatic models with  $G = A + D + AA$ ; GENSEX.EXE for additive, dominance, sex-linked, and maternal models with  $G = A + D + L + M$ ; GENDIPLD.EXE for traits of diploid seeds or animals; GENTRIPL.EXE for traits of triploid endosperm.

### ***Output 1 for Conditional Variance Analysis***

```
Traits =, 1
Variance components = , 5
Degree of freedom = , 25
File name is cotbolm.VAR
Date and Time for Analysis: Sat Jun 24 19:07:06 2000
```

```
Variance Components Estimated by MINQUE(1) with GENVAR1R.EXE.
Jackknifing Over Block Conducted for Estimating S.E.
Predicting Genetic Effects by Adjusted Unbiased Prediction (AUP)
Method.
```



NS = Not significant; S+ = Significant at 0.10 level.  
 S\* = Significant at 0.05 level; S\*\* = Significant at 0.01 level.  
 Linear Contrast Test:  
 +<1> +<2> -<3> +<4>

Diallel Analysis of Trait, BOL8/9|BOL8/4, for Public Users.

Var Comp	Estimate	S. E.	P-value	
(1): Additive Var	0.665074	0.120759	5.04e-006	S**
(2): Dominance Var	0.180163	0.0462009	0.00032	S**
(3): Add. * Env. Var	0.193749	0.0588614	0.00148	S**
(4): Dom. * Env. Var	0.331579	0.0779674	0.000129	S**
(5): Residual Var	0.189768	0.0819921	0.0146	S*
(6): Var(Pheno.)	1.56033	0.209525	4.22e-008	S**

Proportion of Var(G)/Var(T)	Estimate	S. E.	P-value	
(1): Additive Var/Vp	0.426239	0.0429252	1.59e-010	S**
(2): Dominance Var/Vp	0.115464	0.0393502	0.00353	S**
(3): Add. * Env. Var/Vp	0.124172	0.0301349	0.000182	S**
(4): Dom. * Env. Var/Vp	0.212505	0.0386894	5.24e-006	S**
(5): Residual Var/Vp	0.12162	0.0341315	0.000753	S**

Heritability	Estimate	S. E.	P-value	
(6): Heritability(N)	0.426239	0.0429252	1.59e-010	S**
(7): Heritability(B)	0.541703	0.0394694	2.53e-011	S**
(8): Heritability(NE)	0.124172	0.0301349	0.000182	S**
(9): Heritability(BE)	0.336677	0.0399954	4.56e-009	S**

Genetic Predictor, S. E., P-value

(1): Random Effect is Additive Effects				
A1,	0.223513,	0.155049,	0.162,	NS
A2,	0.677601,	0.121236,	8.19e-006,	S**
A3,	-0.562930,	0.091853,	2.09e-006,	S**
A4,	-0.338327,	0.119019,	0.00878,	S**
Linear Contrast,	1.95226,	0.371664,	1.94e-005,	S**

(2): Random Effect is Dominance Effects

D1*1	0.798935	0.436678	0.0793	S+
D2*2	0.018615	0.066023	0.78	NS
D3*3	0.072842	0.101742	0.481	NS
D4*4	-0.412087	0.328823	0.222	NS
D1*2	0.425023	0.229382	0.0757	S+
D1*3	-1.004059	0.598641	0.106	NS
D1*4	-0.661568	0.375175	0.0901	S+
D2*3	-0.076713	0.091950	0.412	NS
D2*4	1.092527	0.629749	0.0951	S+
D3*4	-0.253545	0.321869	0.438	NS

Heterosis <Delta>	-0.563434	0.767809	0.47	NS
-------------------	-----------	----------	------	----

(3): Random Effect is Add. \* Env. Effects

AE1 in E1	-0.022308	0.102366	0.829	NS
AE2 in E1	0.036740	0.088970	0.683	NS
AE3 in E1	-0.011993	0.081400	0.884	NS
AE4 in E1	-0.002428	0.153184	0.987	NS
AE1 in E2	0.158196	0.194168	0.423	NS
AE2 in E2	0.357913	0.255052	0.173	NS

AE3 in E2	-0.305599	0.174689	0.0925	S+
AE4 in E2	-0.210610	0.188787	0.275	NS
Linear Contrast	1.58114e-005	1.77345e-005	0.381	NS

(4): Random Effect is Dom. \* Env. Effects

DE1 in E1	-0.320161	0.196316	0.115	NS
DE2 in E1	0.368241	0.179784	0.0512	S+
DE3 in E1	-0.184366	0.161795	0.265	NS
DE4 in E1	-0.541939	0.380790	0.167	NS
DE1 in E2	-0.053143	0.150489	0.727	NS
DE2 in E2	-0.057755	0.290609	0.844	NS
DE3 in E2	0.687891	0.349814	0.0604	S+
DE4 in E2	-0.303718	0.189203	0.121	NS
DE1 in E3	-0.340375	0.372988	0.37	NS
DE2 in E3	0.745340	0.610413	0.233	NS
DE3 in E3	0.927552	0.534879	0.0952	S+
DE4 in E3	-0.569171	0.246751	0.0296	S*
DE1 in E4	0.343324	0.197179	0.0939	S+
DE2 in E4	0.301441	0.324563	0.362	NS
DE3 in E4	0.139931	0.334570	0.679	NS
DE4 in E4	-0.560693	0.344209	0.116	NS
DE1 in E5	-1.175256	0.700765	0.106	NS
DE2 in E5	0.311932	0.239635	0.205	NS
DE3 in E5	1.167883	0.778234	0.146	NS
DE4 in E5	-0.887039	0.664529	0.194	NS
Heterosis <Delta>	0	0	1	NS

Fixed Effect <1>, 9.42573

Fixed Effect <2>, 13.616

Time Used (Hour) = 0.000556



## Chapter 11

# Ecovalence and Stability Variance

Manjit S. Kang

### *Purpose*

To identify and select genotypes with consistent (stable) performance across diverse environments (broad adaptation).

### *Definitions*

#### *Ecovalence*

Ecovalence is the sum of squares contributed by a genotype to a genotype-by-environment interaction:

$$W_i = \sum_j (u_{ij} - \bar{u}_i)^2$$

where  $W_i = \text{ecovalence}$  for  $i$ th genotype,  $u_{ij} = x_{ij} - \bar{x}_{.j}$ ,  $x_{ij}$  = observed trait value for the  $i$ th genotype in  $j$ th environment,  $\bar{x}_{.j}$  = mean of all genotypes in  $j$ th environment;  $\bar{u}_i = \sum_j u_{ij} / s$ ,  $s$  = number of environments.

#### *Originator*

Wricke, G. (1962). Über eine Methode zur Erfassung der ökologischen Streubreite. *Zeitschrift für Pflanzenzüchtung* 47:92-96.

#### *Stability Variance*

Stability variance measures the consistency of performance of a genotype across a set of diverse environments. The smaller the value, the greater the stability:

$$\sigma_i^2 = 1 / (s-1)(t-1)(t-2) \times t(t-1) \sum_j (u_{ij} - \bar{u}_i.)^2 - \sum_i \sum_j (u_{ij} - \bar{u}_i.)^2,$$

where,  $\sigma_i^2$  = stability variance for the  $i$ th genotype, and  $t$  = total number of genotypes evaluated.

When genotype-by-environment interaction is significant, it is desirable to know the factor(s) responsible for the interaction. Technically, factors are used as covariates and their linear effects, which represent heterogeneity or nonadditivity, are removed. Following the removal of heterogeneity, the remainder of the genotype-by-environment interaction is examined for significance. If heterogeneity is significant, the contribution of each genotype ( $s_i^2$ ) to the residual genotype-by-environment interaction can be determined using the following formula provided by Shukla (1972):

$$s_i^2 = t / (t-2)(s-2)(s-2) \times S_i - \sum_i S_i / t(t-1),$$

where  $S_i = \sum_j (u_{ij} - \bar{u}_i. - b_i Z_j)^2$ , and  $b_i = \sum_j (u_{ij} - \bar{u}_i. Z_j) / \sum_j Z_j$ , and  $Z_j = \bar{x}_{.j} - \bar{x}_{..}$ .

### **Originator**

Shukla, G. K. (1972). Some statistical aspects of partitioning genotype-environmental components of variability. *Heredity* 29:237-245.

### **Software Available**

Kang, M.S. (1989). A new SAS program for calculating stability-variance parameters. *Journal of Heredity* 80:415. (software is free of charge).

### **Key Reference(s) Using the Concept/Software/Formula**

Kang, M.S. (1993). Simultaneous selection for yield and stability in crop performance trials: Consequences for growers. *Agronomy Journal* 85:754-757.

Pazdernick, D.L., Hardman, L.L., and Orf, J.H. (1997). Agronomic performance and stability of soybean varieties grown in three maturity zones of Minnesota. *Journal of Production Agriculture* 10:425-430.

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**EXAMPLE**

**Data to be analyzed (Yield):**

Environments	Env1	Env2	Env3	Env4	Env5	Env6
Genotypes						
Genotype1	161.7 <sup>†</sup>	247.0	185.4	218.7	165.3	154.6
Genotype2	187.7	257.5	182.4	183.3	138.9	143.8
Genotype3	200.1	262.9	194.9	220.2	165.8	146.3
Genotype4	196.9	339.2	271.2	266.3	151.2	193.6
Genotype5	182.5	253.8	219.2	200.5	184.4	190.1
Zj	-16.41	69.93	8.43	15.63	-41.07	-36.51

<sup>†</sup>Each cell represents summation of six observations (six replications).

**Case 1: Using Totals Across Replications**

Since each cell in the above data represents a “total” of six observations, the value for *N* in the computer program provided in this chapter will be 6, and that for *REP* will be 1 (*N* = 6; *REP* = 1); For the given data set,  $\bar{x}_{..}$  = 202.18 (grand mean), and

$$Z_j \quad \bar{x}_{.j} - \bar{x}_{..} \quad -16.41 \quad 69.93 \quad 8.43 \quad 15.63 \quad -41.07 \quad -36.51$$

Note: *Z<sub>j</sub>* represents a covariate.

**Program Listing for Case 1**

```
DATA GENETIC;
INPUT X1 - X6;
CARDS;
161.7 247.0 185.4 218.7 165.3 154.6
187.7 257.5 182.4 183.3 138.9 143.8
200.1 262.9 194.9 220.2 165.8 146.3
196.9 339.2 271.2 266.3 151.2 193.6
182.5 253.8 219.2 200.5 184.4 190.1
;
PROC IML; USE GENETIC;
READ ALL VAR _ALL_ INTO X;
N=6; REP=1;
ZJ={-16.41 69.93 8.43 15.63 -41.07 -36.51};
P=NROW(X); Q=NCOL(X);
```

```

CMEAN=X(|+,|)/P;
GENO=J(P,Q); START;
DO I=1 TO P; GENO(|I,|)=CMEAN(|1,1:Q|); END;
FINISH; RUN;
U=X - GENO; UM=U/Q;
ENV=J(P,Q); START;
DO K=1 TO Q;
ENV(|,K|)=UM(|,+|); END;
FINISH; RUN;
DIFF=U-ENV; SSDIFF=(DIFF#DIFF)(|,+|);
SUMSS=SUM(SSDIFF); ECOV=SSDIFF/N;
L=P*(P-1); E=(Q-1)*(P-1)*(P-2);
LSSDIFF=(SSDIFF*L)/N;
D=J(P,1,(SUMSS/N));
SIG=LSSDIFF-D; SIGMA=SIG/E;
SUMSQZJ=SUM(ZJ#ZJ); HAT=J(P,Q);
START; DO R=1 TO P;
HAT(|R,|)=ZJ(|1,1:Q|); END;
FINISH; RUN;
NEW=DIFF#HAT; BETA=(NEW/SUMSQZJ)(|,+|);
GP=J(P,Q); START;
DO C=1 TO Q; GP(|,C|)=BETA(|1:P,1|); END;
FINISH; RUN;
BIZJ=HAT#GP; NEWDIFF=(DIFF-BIZJ);
SI=(NEWDIFF#NEWDIFF)(|,+|); TS=P/((P-2)*(Q-2));
TOTSI=SUM(SI)/L; SP=((SI-TOTSI)*TS)/N;
F=D(|1,1|); START;
IF N=1 THEN DO; ECOV=ECOV*REP;
F=F*REP; SIGMA=SIGMA*REP; SP=SP*REP; END;
FINISH; RUN;
TITLE 'STABILITY-VARIANCE';
TITLE2 'X MATRIX REPRESENTS INPUT DATA';
TITLE3 'ECOV MATRIX REPRESENTS GXE SS FOR EACH GENOTYPE';
TITLE4 'F MATRIX REPRESENTS TOTAL GXE SS';
TITLE5 'SIGMA MATRIX REPRESENTS STABILITY VARIANCE FOR EACH GENOTYPE';
TITLE6 'SP MATRIX REPRESENTS SMALL S-SQUARE SUB-I';
PRINT X, ECOV, F, SIGMA, SP; RUN;

```

### Case 1 Output

```

X MATRIX REPRESENTS INPUT DATA
ECOV MATRIX REPRESENTS GXE SS FOR EACH GENOTYPE
TITLE4 'F MATRIX REPRESENTS TOTAL GXE SS';
SIGMA MATRIX REPRESENTS STABILITY VARIANCE FOR EACH GENOTYPE
SP MATRIX REPRESENTS SMALL S-SQUARE SUB-I

```

X	COL1	COL2	COL3	COL4	COL5	COL6
ROW1	161.7	247.0	185.4	218.7	165.3	154.6
ROW2	187.7	257.5	182.4	183.3	138.9	143.8
ROW3	200.1	262.9	194.9	220.2	165.8	146.3
ROW4	196.9	339.2	271.2	266.3	151.2	193.6
ROW5	182.5	253.8	219.2	200.5	184.4	190.1

ECOV	COL1
ROW1	151.5

ROW2	132.7
ROW3	142.1
ROW4	750.5
ROW5	300.9
F	COL1
ROW1	1477.7
SIGMA	COL1
ROW1	25.8791
ROW2	19.5998
ROW3	22.7305
ROW4	225.5
ROW5	75.6800
SP	COL1
ROW1	34.1065
ROW2	40.4848
ROW3	42.8052
ROW4	79.6618
ROW5	23.2671

NOTE: EXIT FROM IML

## ***Case 2: Using Means Across Replications***

Differences when running the program using means across replications:

- After the *CARDS* statement, enter the means instead of totals across replications.
- Calculate *ZJ* using means instead of totals.
- $N = 1$ ;  $REP = 6$ .





## Chapter 12

# Genotype-by-Environment Interaction Variance

Robert Magari  
Manjit S. Kang

### ***Purpose***

To estimate genotype-by-environment interaction and evaluate performance across a range of environments.

### ***Definitions***

Genotype-by-environment variance (GE variance) program is a restricted maximum likelihood estimator of Shukla's (1972) stability variance.

### ***Originator***

Shukla, G.K. (1972). Some statistical aspects of partitioning genotype-environment components of variability. *Heredity* 29:237-245.

### ***Software Available***

Magari, R. and Kang, M.S. (1997). SAS\_STABLE: Analysis of balanced and unbalanced data. *Agronomy Journal* 89:929-932. The software is provided free of charge.

### ***Key References***

Kang, M.S. and Magari, R. (1996). New developments in selecting for phenotypic stability in crop breeding. In Kang, M.S. and Gauch, H.G. (Eds.), *Genotype by Environment Interaction* (pp. 1-14). CRC Press, Boca Raton, FL.

Magari, R., Kang, M.S., and Zhang, Y. (1997). Genotype by environment interaction for ear moisture loss in corn. *Crop Science* 37:774-779.

### Contact

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### EXAMPLE

Replicated data of several genotypes in different environments are entered in SAS format. The solutions to the parameters are obtained as follows:

$$\begin{array}{rcccccc}
 \hat{\beta} & X X & X Z_1 & X Z_2 & X Z_{3k} &^{-1} X y \\
 \hat{\alpha} & Z_1 X & Z_1 Z_1 & I \frac{\hat{\sigma}_\delta^2}{\hat{\sigma}^2_E} & Z_1 R^{-1} Z_2 & Z_1 Z_{3k} & Z_1 y \\
 \hat{\cdot} & Z_2 X & Z_2 Z_1 & Z_2 Z_2 & I \frac{\hat{\sigma}^2}{\hat{\sigma}^2_E} & Z_2 Z_{3k} & Z_2 y \\
 \\ 
 \hat{\delta K} & Z_{3k} X & & Z_{3k} Z_2 & Z_{3k} Z_{3k} & I \frac{\hat{\sigma}^2}{\hat{\sigma}_{EG(k)}} & Z_{3k} y
 \end{array}$$

where  $\mathbf{y}$  is vector of observations,  $\hat{\beta}$ ,  $\hat{\alpha}$ ,  $\hat{\cdot}$ , and  $\hat{\delta}_k$  are the vector of estimates for genotypes, environments, replicates within environments, and each GEI, respectively.  $\mathbf{X}$  is the design matrix of the fixed effects (genotypes),  $\mathbf{Z}_1$  is the design matrix for environments,  $\mathbf{Z}_2$  is the design matrix for replications-within-environments, and  $\mathbf{Z}_{3k}$  is the design matrix for GEI of the  $k$ th genotype.

Variance components are defined and calculated as follows:

Environmental variance

$$\hat{\sigma}^2_E = \frac{\hat{a} \hat{a} \text{ tr } \mathbf{C}_{22} \hat{\sigma}^2}{a}$$

Replications-within-environment variance

$$\hat{\sigma}_{R/E}^2 = \frac{\hat{\mathbf{I}} \text{tr } \mathbf{C}_{33} \hat{\sigma}^2}{b}$$

Genotype-by-environment interaction variance

$$\hat{\sigma}_{GE(k)}^2 = \frac{\hat{\delta}_k \hat{\mathbf{I}} \hat{\delta}_k \text{tr } \mathbf{C}_{(3\ k)(3\ k)} \hat{\sigma}^2}{\text{no. columns of } \mathbf{Z}_{3k}}$$

Experimental error variance

$$\hat{\sigma}^2 = \frac{\mathbf{y} \mathbf{y} - \hat{\beta} \mathbf{X} \mathbf{y} - \hat{\mathbf{u}} \mathbf{Z} \mathbf{y}}{n - c}$$

where  $\mathbf{I}$  represents identity matrix,  $\mathbf{C}$  represents corresponding blocks of inverse of the aforementioned (large) matrix, where solutions of parameters are obtained,  $a$  is the number of environments,  $b$  is the number of replicates,  $c$  is the number of genotypes, and  $n$  is the dimension of the  $\mathbf{y}$  vector.

### ***Program Listing***

```
proc iml;
use early;

/* Read data into vectors*/;
read all var{earwt} into y;
read all var{hybrid} into X;
read all var{date} into ZE;
read all var{rep} into r;

/* Set up design matrices */;
R=design(r);
X=design(X);
ZE=design(ZE);
U=hdir(X,ZE);
RE=hdir(R,ZE);
nr=ncol(RE);
W=X||ZE||U||RE;
dim=ncol(W);
t=nrow(y);
a=ncol(X);
b=ncol(ZE);
yy=y`*y;
wy=W`*y;
ww=W`*W;
bb=ncol(U);
```

```

/* Starting values for iterations */;
lambda=0.4;
lambda1=0.4;
lambda2=0.4;

/* Set up matrices and start iterations */;
block1=j(a,a,0);
do iter=1 to 1000;
block2=I(b)*lambda;
block3=I(bb)*lambda1;
block4=I(nr)*lambda2;
addon=block(block1,block2,block3,block4);
M=ww+addon;
invM=inv(M);

/* Solutions for vector of effects (BLUE and BLUP) */;
solution=invM*wy;

/* Variance components */;
sigmae=(yy-solution`*wy)/(t-a);
ue=solution[a+1:a+b];
ue1=solution[a+1+b:a+2*b];
ue2=solution[a+1+2*b:a+3*b];
ue3=solution[a+1+3*b:a+4*b];
ue4=solution[a+1+4*b:a+5*b];
ue5=solution[a+1+5*b:a+6*b];
ue6=solution[a+1+6*b:a+7*b];
ue7=solution[a+1+7*b:a+8*b];
ue8=solution[a+1+8*b:a+9*b];
ur=solution[a+1+9*b:a+9*b+nr];

true=trace(invM[a+1:a+b,a+1:a+b]);
sigmaue=(ue`*ue>true*sigmae)/b;
true1=trace(invM[a+1+b:a+2*b,a+1+b:a+2*b]);
s1=(ue1`*ue1>true1*sigmae)/b;
true2=trace(invM[a+1+2*b:a+3*b,a+1+2*b:a+3*b]);
s2=(ue2`*ue2>true2*sigmae)/b;
true3=trace(invM[a+1+3*b:a+4*b,a+1+3*b:a+4*b]);
s3=(ue3`*ue3>true3*sigmae)/b;
true4=trace(invM[a+1+4*b:a+5*b,a+1+4*b:a+5*b]);
s4=(ue4`*ue4>true4*sigmae)/b;
true5=trace(invM[a+1+5*b:a+6*b,a+1+5*b:a+6*b]);
s5=(ue5`*ue5>true5*sigmae)/b;
true6=trace(invM[a+1+6*b:a+7*b,a+1+6*b:a+7*b]);
s6=(ue6`*ue6>true6*sigmae)/b;
true7=trace(invM[a+1+7*b:a+8*b,a+1+7*b:a+8*b]);
s7=(ue7`*ue7>true7*sigmae)/b;
true8=trace(invM[a+1+8*b:a+9*b,a+1+8*b:a+9*b]);
s8=(ue8`*ue8>true8*sigmae)/b;
truer=trace(invM[a+b+bb+1:a+b+bb+nr,a+b+bb+1:a+b+bb+nr]);
sigmar=(ur`*ur+truer*sigmae)/nr;

if(mod(iter,10)=0) then print iter sigmae sigmaue sigmar;
if(mod(iter,10)=0) then print iter s1 s2 s3 s4 s5 s6 s7 s8;
sig=(s1+s2+s3+s4+s5+s6+s7+s8)/a;
lambda=sigmae/sigmaue;
lambda1=sigmae/sig;

```

```

lambda2=sigmae/sigmar;
if(mod(iter,10)=0) then print iter sig;
end;

/* Set up of Fisher's information matrix */;
e1={1,0,0,0,0,0,0,0,0,0};
e2={0,1,0,0,0,0,0,0,0,0};
e3={0,0,1,0,0,0,0,0,0,0};
e4={0,0,0,1,0,0,0,0,0,0};
e5={0,0,0,0,1,0,0,0,0,0};
e6={1,0,0,0,0,0,1,0,0,0};
e7={1,0,0,0,0,0,0,1,0,0};
e8={1,0,0,0,0,0,0,0,1,0};
a=ncol(X);
k=I(b);
ee1=e1@k;
ee2=e2@k;
ee3=e3@k;
ee4=e4@k;
ee5=e5@k;
ee6=e6@k;
ee7=e7@k;
ee8=e8@k;
Z1=U*ee1;
Z2=U*ee2;
Z3=U*ee3;
Z4=U*ee4;
Z5=U*ee5;
Z6=U*ee6;
Z7=U*ee7;
Z8=U*ee8;
fi=j(11,11,0);
V=ZE*ZE`*sigmae+RE*RE`*sigmar+U*U`*sig+I(t)*sigmae;
vi=inv(V);
p=vi-vi*X*inv(X`*vi*X)*X`*vi;
fi[1,1]=0.5*trace(p*ZE*ZE`*p*ZE*ZE`);
fi[1,2]=0.5*trace(p*ZE*ZE`*p*RE*RE`);
fi[1,3]=0.5*trace(p*ZE*ZE`*p*Z1*Z1`);
fi[1,4]=0.5*trace(p*ZE*ZE`*p*Z2*Z2`);
fi[1,5]=0.5*trace(p*ZE*ZE`*p*Z3*Z3`);
fi[1,6]=0.5*trace(p*ZE*ZE`*p*Z4*Z4`);
fi[1,7]=0.5*trace(p*ZE*ZE`*p*Z5*Z5`);
fi[1,8]=0.5*trace(p*ZE*ZE`*p*Z6*Z6`);
fi[1,9]=0.5*trace(p*ZE*ZE`*p*Z7*Z7`);
fi[1,10]=0.5*trace(p*ZE*ZE`*p*Z8*Z8`);
fi[1,11]=0.5*trace(p*ZE*ZE`*p);

fi[2,1]=fi[1,2]; fi[2,2]=0.5*trace(p*RE*RE`*p*RE*RE`);
fi[2,3]=0.5*trace(p*RE*RE`*p*Z1*Z1`);
fi[2,4]=0.5*trace(p*RE*RE`*p*Z2*Z2`);
fi[2,5]=0.5*trace(p*RE*RE`*p*Z3*Z3`);
fi[2,6]=0.5*trace(p*RE*RE`*p*Z4*Z4`);
fi[2,7]=0.5*trace(p*RE*RE`*p*Z5*Z5`);
fi[2,8]=0.5*trace(p*RE*RE`*p*Z6*Z6`);
fi[2,9]=0.5*trace(p*RE*RE`*p*Z7*Z7`);
fi[2,10]=0.5*trace(p*RE*RE`*p*Z8*Z8`);

```

```

fi[2,11]=0.5*trace(p*RE*RE`*p);
fi[3,1]=fi[1,3]; fi[3,2]=fi[2,3];
fi[3,3]=0.5*trace(p*Z1*Z1`*p*Z1*Z1`);
fi[3,4]=0.5*trace(p*Z1*Z1`*p*Z2*Z2`);
fi[3,5]=0.5*trace(p*Z1*Z1`*p*Z3*Z3`);
fi[3,6]=0.5*trace(p*Z1*Z1`*p*Z4*Z4`);
fi[3,7]=0.5*trace(p*Z1*Z1`*p*Z5*Z5`);
fi[3,8]=0.5*trace(p*Z1*Z1`*p*Z6*Z6`);
fi[3,9]=0.5*trace(p*Z1*Z1`*p*Z7*Z7`);
fi[3,10]=0.5*trace(p*Z1*Z1`*p*Z8*Z8`);
fi[3,11]=0.5*trace(p*Z1*Z1`*p);

fi[4,1]=fi[1,4]; fi[4,2]=fi[2,4];
fi[4,3]=fi[3,4]; fi[4,4]=0.5*trace(p*Z2*Z2`*p*Z2*Z2`);
fi[4,5]=0.5*trace(p*Z2*Z2`*p*Z3*Z3`);
fi[4,6]=0.5*trace(p*Z2*Z2`*p*Z4*Z4`);
fi[4,7]=0.5*trace(p*Z2*Z2`*p*Z5*Z5`);
fi[4,8]=0.5*trace(p*Z2*Z2`*p*Z6*Z6`);
fi[4,9]=0.5*trace(p*Z2*Z2`*p*Z7*Z7`);
fi[4,10]=0.5*trace(p*Z2*Z2`*p*Z8*Z8`);
fi[4,11]=0.5*trace(p*Z2*Z2`*p);

fi[5,1]=fi[1,5]; fi[5,2]=fi[2,5];
fi[5,3]=fi[3,5]; fi[5,4]=fi[4,5];
fi[5,5]=0.5*trace(p*Z3*Z3`*p*Z3*Z3`);
fi[5,6]=0.5*trace(p*Z3*Z3`*p*Z4*Z4`);
fi[5,7]=0.5*trace(p*Z3*Z3`*p*Z5*Z5`);
fi[5,8]=0.5*trace(p*Z3*Z3`*p*Z6*Z6`);
fi[5,9]=0.5*trace(p*Z3*Z3`*p*Z7*Z7`);
fi[5,10]=0.5*trace(p*Z3*Z3`*p*Z8*Z8`);
fi[5,11]=0.5*trace(p*Z3*Z3`*p);

fi[6,1]=fi[1,6]; fi[6,2]=fi[2,6];
fi[6,3]=fi[3,6]; fi[6,4]=fi[4,6];
fi[6,5]=fi[5,6]; fi[6,6]=0.5*trace(p*Z4*Z4`*p*Z4*Z4`);
fi[6,7]=0.5*trace(p*Z4*Z4`*p*Z5*Z5`);
fi[6,8]=0.5*trace(p*Z4*Z4`*p*Z6*Z6`);
fi[6,9]=0.5*trace(p*Z4*Z4`*p*Z7*Z7`);
fi[6,10]=0.5*trace(p*Z4*Z4`*p*Z8*Z8`);
fi[6,11]=0.5*trace(p*Z4*Z4`*p);

fi[7,1]=fi[1,7]; fi[7,2]=fi[2,7];
fi[7,3]=fi[3,7]; fi[7,4]=fi[4,7];
fi[7,5]=fi[5,7]; fi[7,6]=fi[6,7];
fi[7,7]=0.5*trace(p*Z5*Z5`*p*Z5*Z5`);
fi[7,8]=0.5*trace(p*Z5*Z5`*p*Z6*Z6`);
fi[7,9]=0.5*trace(p*Z5*Z5`*p*Z7*Z7`);
fi[7,10]=0.5*trace(p*Z5*Z5`*p*Z8*Z8`);
fi[7,11]=0.5*trace(p*Z5*Z5`*p);

fi[8,1]=fi[1,8]; fi[8,2]=fi[2,8];
fi[8,3]=fi[3,8]; fi[8,4]=fi[4,8];
fi[8,5]=fi[5,8]; fi[8,6]=fi[6,8];
fi[8,7]=fi[7,8]; fi[8,8]=0.5*trace(p*Z6*Z6`*p*Z6*Z6`);
fi[8,9]=0.5*trace(p*Z6*Z6`*p*Z7*Z7`);
fi[8,10]=0.5*trace(p*Z6*Z6`*p*Z8*Z8`);
fi[8,11]=0.5*trace(p*Z6*Z6`*p);

```

```

fi[9,1]=fi[1,9]; fi[9,2]=fi[2,9];
fi[9,3]=fi[3,9]; fi[9,4]=fi[4,9];
fi[9,5]=fi[5,9]; fi[9,6]=fi[6,9];
fi[9,7]=fi[7,9]; fi[9,8]=fi[8,9];
fi[9,9]=0.5*trace(p*Z7*Z7`*p*Z7*Z7`);
fi[9,10]=0.5*trace(p*Z7*Z7`*p*Z8*Z8`);
fi[9,11]=0.5*trace(p*Z7*Z7`*p);

fi[10,1]=fi[1,10]; fi[10,2]=fi[2,10];
fi[10,3]=fi[3,10]; fi[10,4]=fi[4,10];
fi[10,5]=fi[5,10]; fi[10,6]=fi[6,10];
fi[10,7]=fi[7,10]; fi[10,8]=fi[8,10];
fi[10,9]=fi[9,10]; fi[10,10]=0.5*trace(p*Z8*Z8`*p*Z8*Z8`);
fi[10,11]=0.5*trace(p*Z8*Z8`*p);

fi[11,1]=fi[1,11]; fi[11,2]=fi[2,11];
fi[11,3]=fi[3,11]; fi[11,4]=fi[4,11];
fi[11,5]=fi[5,11]; fi[11,6]=fi[6,11];
fi[11,7]=fi[7,11]; fi[11,8]=fi[8,11];
fi[11,9]=fi[9,11]; fi[11,10]=fi[10,11];
fi[11,11]=0.5*trace(p*p);

/* Inverse of Fisher's information matrix */;
asvc=inv(fi);

/* Standard errors */;
erruel=j(a,1,0);
errue=sqrt(asvc[1,1]);
errar=sqrt(asvc[2,2]);
erruel[1]=sqrt(asvc[3,3]);
erruel[2]=sqrt(asvc[4,4]);
erruel[3]=sqrt(asvc[5,5]);
erruel[4]=sqrt(asvc[6,6]);
erruel[5]=sqrt(asvc[7,7]);
erruel[6]=sqrt(asvc[8,8]);
erruel[7]=sqrt(asvc[9,9]);
erruel[8]=sqrt(asvc[10,10]);
errae=sqrt(asvc[11,11]);

/* Testing */;
zerror=sigmaae/errae;

zenv=sigmaae/errue;
zrepenv=sigmar/errar;
perror=(1-probnorm(zerror))*2;
penv=(1-probnorm(zenv))*2;
prepenv=(1-probnorm(zrepenv))*2;
s=j(a,1,0);
z=j(a,1,0);
pge=j(a,1,0);

s[1]=s1;
s[2]=s2;
s[3]=s3;
s[4]=s4;
s[5]=s5;
s[6]=s6;

```



```

s[7]=s7;
s[8]=s8;
ii=j(a,1,1);
z=s/erruel;
pge=(ii-probnorm(z))*2;
gen=j(a,1,0);
do i=1 to a;
gen[i]=i;
end;
print 'Fisher's information matrix';
print fi;
print 'Inverse of Fisher's information matrix';
print asvc;
print 'Individual GxE variance components';
print gen      s      erruel      z      pge;
print 'Error';
print sigmae      errae      perror;
print 'Environment';
print sigmaue      errue      penv;
print 'Replications within environment';
print sigmar      errar      prepenv;

```

## Output

### ITERATION HISTORY OF STABILITY VARIANCES

```

ITER      S
  10 0.0034962
      0.0030041
      0.003348
      0.0044955

```

```

ITER      S
  20 0.0027947
      0.0024548
      0.0026893
      0.0035634

```

```

ITER      S
 100 0.002327
      0.0020955
      0.0022605
      0.0029363

```

SOURCE	GENOTYPE	MEAN	VARIANCE	ERROR	Z	PROB
ENV	.	.	0.025184	0.021807	1.15486	0.24815
GXE	1	4.15499	0.002327	0.001933	1.20366	0.22872
GXE	2	4.16907	0.002095	0.001933	1.08388	0.27842
GXE	3	4.14078	0.002261	0.001880	1.20265	0.22911
GXE	4	4.18702	0.002936	0.001880	1.56219	0.11824
REP/ENV	.	.	0.000643	0.001527	0.42118	0.67363
ERROR	.	.	0.008739	0.002464	3.54657	0.00039

## Chapter 13

# Code for Simulating Degrees of Freedom for the Items in a Principal Components Analysis of Variance

Walter T. Federer  
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### *Purpose*

To provide simulations required to approximate degrees of freedom for such items as principal components, autoregressions, smoothing, kriging, and the like.

### *Data*

The experiment design is a balanced lattice square in which  $v = 16$  insecticide treatments and  $r = 5$  replicates (complete blocks). The measurement  $y$  is the mean of three counts of plants infected with boll weevil. The variable `grad` in the input statement of the following program listing is the linear polynomial regression coefficients of count on column order in each row of a replicate.

For each simulation using random unit normal deviates, the randomization plan of the experiment for which degrees of freedom are being estimated, is utilized. Then, the sum of squares for a line in the analysis of variance is an estimate of the degrees of freedom since the expected value of each mean square is one.

### *Originator*

Cochran, W.G. and Cox, G.M. (1957). *Experimental Designs*, John Wiley & Sons, New York.

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```

/* Here the data are included, but an infile statement may be used to
   input the plan of the experiment to be simulated. */
data original;
input y rep row col grad treat;
      label row='incomplete block';
      datalines;
  9.0  1  1  1 -3 10
20.3  1  1  2 -1 12
17.7  1  1  3  1  9
26.3  1  1  4  3 11
  4.7  1  2  1 -3  2
  9.0  1  2  2 -1  4
  7.3  1  2  3  1  1
  8.3  1  2  4  3  3
  9.0  1  3  1 -3 14
  6.7  1  3  2 -1 16
11.7  1  3  3  1 13
  4.3  1  3  4  3 15
  4.0  1  4  1 -3  6
  5.0  1  4  2 -1  8
  5.7  1  4  3  1  5
14.3  1  4  4  3  7
19.0  2  1  1 -3  5
  8.7  2  1  2 -1 12
13.0  2  1  3  1 15
15.7  2  1  4  3  2
12.0  2  2  1 -3 10
  6.0  2  2  2 -1  7
15.3  2  2  3  1  4
12.0  2  2  4  3 13
12.7  2  3  1 -3 16
  6.3  2  3  2 -1  1
  1.7  2  3  3  1  6
13.0  2  3  4  3 11
  3.7  2  4  1 -3  3
  3.7  2  4  2 -1 14
  8.0  2  4  3  1  9
13.3  2  4  4  3  8
17.0  3  1  1 -3 10
  7.0  3  1  2 -1 15
10.3  3  1  3  1  8
  1.3  3  1  4  3  1
11.3  3  2  1 -3  9
12.3  3  2  2 -1 16
  3.0  3  2  3  1  7
  5.3  3  2  4  3  2
12.3  3  3  1 -3 12
  8.7  3  3  2 -1 13
  8.0  3  3  3  1  6
  9.3  3  3  4  3  3

```

```

30.3  3 4 1 -3 11
22.3  3 4 2 -1 14
11.0  3 4 3  1  5
12.7  3 4 4  3  4
 5.0  4 1 1 -3 16
10.3  4 1 2 -1 12
 5.7  4 1 3  1  8
12.7  4 1 4  3  4
 2.7  4 2 1 -3 11
 6.7  4 2 2 -1 15
10.3  4 2 3  1  3
 5.7  4 2 4  3  7
 1.0  4 3 1 -3  1
10.3  4 3 2 -1  5
11.3  4 3 3  1  9
11.7  4 3 4  3 13
11.0  4 4 1 -3  6
19.0  4 4 2 -1  2
20.7  4 4 3  1 14
29.7  4 4 4  3 10
 2.0  5 1 1 -3  3
 5.0  5 1 2 -1 16
 4.0  5 1 3  1  5
13.7  5 1 4  3 10
 9.3  5 2 1 -3  6
 1.7  5 2 2 -1  9
 6.3  5 2 3  1  4
12.3  5 2 4  3 15
16.7  5 3 1 -3 12
 4.3  5 3 2 -1  7
18.7  5 3 3  1 14
 8.7  5 3 4  3  1
16.7  5 4 1 -3 13
30.0  5 4 2 -1  2
25.7  5 4 3  1 11
14.0  5 4 4  3  8
run;
/* data sets for the pc analysis */
proc sort data=original;
  by rep row col;
run;
%let nsim=2; /* nsim=2 is for 2 simulations. Usually nsim will be
  large. */
%let seed=2834701; /* Any random seed may be specified. */
data sim;
  set original;
  do k=1 to &nsim;
    y = rannor(&seed); /* This statement says that unit normal ran-
      dom deviates are to be used in the simulation. */
    output;
  end;
run;
/* principal component analysis, by k, i. e. for each simulated analy-
  sis, and rep */
proc sort data=sim;
  by k rep col row;
proc transpose data=sim prefix=row out=simr(drop=_name_);

```

```

    by k rep col;
    var y;
proc princomp data=simr prefix=rpc n=2 out=rowvar noprint;
    by k rep;
    var row1-row4; /* Four rows in the design. */
proc sort data=sim;
    by k rep row col;
proc transpose data=sim prefix=col out=simc(drop=_name_);
    by k rep row;
    var y;
proc princomp data=simc prefix=cpc n=2 out=colvar noprint;
    by k rep;
    var col1-col4; /* Four columns in the design. */
/* expand data sets and merge */
data cc;
    set colvar;
    array colv{4} col1-col4;
    do col = 1 to 4;
        y = colv{col};
        output;
    end;
    drop col1-col4;
data rr;
    set rowvar;
    array rowv{4} row1-row4;
    do row = 1 to 4;
        y = rowv{row};
        output;
    end;
    drop row1-row4;
proc sort data=rr;
    by k rep row col;
data ana;
    merge sim cc rr;
    by k rep row col;
/* analysis of variance using the principal components, non-nested */
proc glm data=ana outstat=o1 noprint;
    by k;
    class rep treat;
    model y=rep treat cpc1 cpc2 rpc1 rpc2 cpc1*rpc1 cpc1*rpc2
        cpc2*rpc1 cpc2*rpc2 ;
proc print data=o1;
run;
/* using the principal components, nested */
proc glm data=ana outstat=o2 noprint;
    by k;
    class rep treat;
    model y=rep treat cpc1(rep) cpc2(rep) rpc1(rep) rpc2(rep)
        cpc1*rpc1(rep) cpc1*rpc2(rep) cpc2*rpc1(rep) cpc2*rpc2(rep) ;
proc print data=o2;
run;
/* using the textbook analysis of the design as in Cochran and Cox
(1957), page 493, and as given above. This provides a check on
the simulations as the sums of squares are the degrees of free-
dom. */
proc glm data=ana outstat=o3 noprint;
    by k;

```

```

class rep row col treat;
model y=rep treat row(rep) col(rep);
lsmean treat;
proc print data=o3;
run;

```

Output from this program follows. SS1 is type I sum of squares; SS3 is type III sum of squares; and the sum of squares is the degrees of freedom as the expected value of each mean square in the table is one.

## Unnested PCTA ANOVA - run 1

OBS	K	_NAME_	_SOURCE_	_TYPE_	DF	SS	F	PROB
1	1	Y	ERROR	ERROR	52	41.0582	.	.
2	1	Y	REP	SS1	4	10.6315	3.3662	0.01594
3	1	Y	TREAT	SS1	15	16.8648	1.4239	0.17144
4	1	Y	CPC1	SS1	1	9.5108	12.0454	0.00105
5	1	Y	CPC2	SS1	1	0.0890	0.1127	0.73848
6	1	Y	RPC1	SS1	1	5.9200	7.4976	0.00844
7	1	Y	RPC2	SS1	1	1.1131	1.4097	0.24049
8	1	Y	CPC1*RPC1	SS1	1	0.4601	0.5828	0.44869
9	1	Y	CPC1*RPC2	SS1	1	2.9147	3.6915	0.06018
10	1	Y	CPC2*RPC1	SS1	1	0.0440	0.0558	0.81427
11	1	Y	CPC2*RPC2	SS1	1	0.0642	0.0813	0.77664
12	1	Y	REP	SS3	4	10.6315	3.3662	0.01594
13	1	Y	TREAT	SS3	15	5.6731	0.4790	0.94084
14	1	Y	CPC1	SS3	1	9.0891	11.5113	0.00133
15	1	Y	CPC2	SS3	1	0.3867	0.4898	0.48715
16	1	Y	RPC1	SS3	1	6.1529	7.79260	0.00732
17	1	Y	RPC2	SS3	1	0.9345	1.18358	0.28165
18	1	Y	CPC1*RPC1	SS3	1	0.6489	0.82188	0.36881
19	1	Y	CPC1*RPC2	SS3	1	2.9887	3.78517	0.05712
20	1	Y	CPC2*RPC1	SS3	1	0.0470	0.05948	0.80827
21	1	Y	CPC2*RPC2	SS3	1	0.0642	0.08133	0.77664

## Unnested PCTA ANOVA - run 2

OBS	K	_NAME_	_SOURCE_	_TYPE_	DF	SS	F	PROB
22	2	Y	ERROR	ERROR	52	38.1947	.	.
23	2	Y	REP	SS1	4	1.9787	0.67346	0.61338
24	2	Y	TREAT	SS1	15	19.1134	1.73479	0.07252
25	2	Y	CPC1	SS1	1	1.7968	2.44618	0.12388
26	2	Y	CPC2	SS1	1	1.8594	2.53141	0.11766
27	2	Y	RPC1	SS1	1	6.0489	8.23524	0.00593
28	2	Y	RPC2	SS1	1	1.1192	1.52375	0.22260
29	2	Y	CPC1*RPC1	SS1	1	5.9688	8.12616	0.00624
30	2	Y	CPC1*RPC2	SS1	1	0.0026	0.00354	0.95277
31	2	Y	CPC2*RPC1	SS1	1	0.09327	0.12699	0.72302
32	2	Y	CPC2*RPC2	SS1	1	0.74168	1.00975	0.31962
33	2	Y	REP	SS3	4	1.97867	0.67346	0.61338
34	2	Y	TREAT	SS3	15	4.41711	0.40091	0.97267
35	2	Y	CPC1	SS3	1	3.54125	4.82123	0.03260
36	2	Y	CPC2	SS3	1	1.62114	2.20710	0.14341
37	2	Y	RPC1	SS3	1	6.56799	8.94197	0.00425
38	2	Y	RPC2	SS3	1	1.24960	1.70127	0.19787
39	2	Y	CPC1*RPC1	SS3	1	5.87599	7.99984	0.00663
40	2	Y	CPC1*RPC2	SS3	1	0.01225	0.01668	0.89773

41	2	Y	CPC2*RPC1	SS3	1	0.06838	0.09310	0.76149
42	2	Y	CPC2*RPC2	SS3	1	0.74168	1.00975	0.31962

## Nested PCTA ANOVA - run 1

OBS	K	NAME	SOURCE	TYPE	DF	SS	F	PROB
1	1	Y	ERROR	ERROR	20	4.7282	.	.
2	1	Y	REP	SS1	4	10.6315	11.2427	0.00006
3	1	Y	TREAT	SS1	15	16.8648	4.7558	0.00076
4	1	Y	CPC1 (REP)	SS1	5	15.5141	13.1248	0.00001
5	1	Y	CPC2 (REP)	SS1	5	2.7152	2.2970	0.08381
6	1	Y	RPC1 (REP)	SS1	5	10.0044	8.4637	0.00020
7	1	Y	RPC2 (REP)	SS1	5	4.7658	4.0318	0.01080
8	1	Y	CPC1*RPC1 (REP)	SS1	5	7.5124	6.3554	0.00110
9	1	Y	CPC1*RPC2 (REP)	SS1	5	4.6495	3.9335	0.01203
10	1	Y	CPC2*RPC1 (REP)	SS1	5	8.2553	6.9839	0.00064
11	1	Y	CPC2*RPC2 (REP)	SS1	5	3.0294	2.5628	0.06004
12	1	Y	REP	SS3	4	10.6315	11.2427	0.00006
13	1	Y	TREAT	SS3	15	3.1950	0.9010	0.57497
14	1	Y	CPC1 (REP)	SS3	5	13.1371	11.1139	0.00003
15	1	Y	CPC2 (REP)	SS3	5	2.6241	2.2200	0.09243
16	1	Y	RPC1 (REP)	SS3	5	8.5463	7.2301	0.00052
17	1	Y	RPC2 (REP)	SS3	5	4.3279	3.6614	0.01630
18	1	Y	CPC1*RPC1 (REP)	SS3	5	3.5137	2.9726	0.03638
19	1	Y	CPC1*RPC2 (REP)	SS3	5	3.0198	2.5547	0.06065
20	1	Y	CPC2*RPC1 (REP)	SS3	5	5.8240	4.9271	0.00423
21	1	Y	CPC2*RPC2 (REP)	SS3	5	3.0294	2.5628	0.06004

## Nested PCTA ANOVA - run 2

22	2	Y	ERROR	ERROR	20	4.3221	.	.
23	2	Y	REP	SS1	4	1.9787	2.2890	0.09551
24	2	Y	TREAT	SS1	15	19.1134	5.8963	0.00018
25	2	Y	CPC1 (REP)	SS1	5	9.1962	8.5108	0.00019
26	2	Y	CPC2 (REP)	SS1	5	3.9972	3.6993	0.01562
27	2	Y	RPC1 (REP)	SS1	5	8.7444	8.0927	0.00026
28	2	Y	RPC2 (REP)	SS1	5	0.8850	0.8190	0.55043
29	2	Y	CPC1*RPC1 (REP)	SS1	5	15.2570	14.1200	0.00001
30	2	Y	CPC1*RPC2 (REP)	SS1	5	6.2267	5.7626	0.00188
31	2	Y	CPC2*RPC1 (REP)	SS1	5	3.81879	3.53420	0.01883
32	2	Y	CPC2*RPC2 (REP)	SS1	5	3.37785	3.12611	0.03029
33	2	Y	REP	SS3	4	1.97867	2.28901	0.09551
34	2	Y	TREAT	SS3	15	1.79833	0.55477	0.87591
35	2	Y	CPC1 (REP)	SS3	5	6.68211	6.18412	0.00128
36	2	Y	CPC2 (REP)	SS3	5	3.52047	3.25810	0.02592
37	2	Y	RPC1 (REP)	SS3	5	8.15456	7.54683	0.00040
38	2	Y	RPC2 (REP)	SS3	5	1.92512	1.78165	0.16248
39	2	Y	CPC1*RPC1 (REP)	SS3	5	8.04745	7.44771	0.00043
40	2	Y	CPC1*RPC2 (REP)	SS3	5	7.22510	6.68665	0.00082
41	2	Y	CPC2*RPC1 (REP)	SS3	5	4.65856	4.31137	0.00799
42	2	Y	CPC2*RPC2 (REP)	SS3	5	3.37785	3.12611	0.03029

## Textbook ANOVA - run 1

OBS	K	NAME	SOURCE	TYPE	DF	SS	F	PROB
1	1	Y	ERROR	ERROR	30	25.6177	.	.
2	1	Y	REP	SS1	4	10.6315	3.11254	0.02958
3	1	Y	TREAT	SS1	15	16.8648	1.31665	0.25255
4	1	Y	ROW (REP)	SS1	15	19.6950	1.53760	0.15374
5	1	Y	COL (REP)	SS1	15	15.8615	1.23832	0.29886

6	1	Y	REP	SS3	4	10.6315	3.11254	0.02958
7	1	Y	TREAT	SS3	15	9.8877	0.77194	0.69613
8	1	Y	ROW(REP)	SS3	15	15.7929	1.23297	0.30227
9	1	Y	COL(REP)	SS3	15	15.8615	1.23832	0.29886
Textbook ANOVA - run 2								
10	2	Y	ERROR	ERROR	30	29.5471	.	.
11	2	Y	REP	SS1	4	1.9787	0.50225	0.73428
12	2	Y	TREAT	SS1	15	19.1134	1.29376	0.26542
13	2	Y	ROW(REP)	SS1	15	16.4413	1.11289	0.38676
14	2	Y	COL(REP)	SS1	15	9.8368	0.66584	0.79576
15	2	Y	REP	SS3	4	1.9787	0.50225	0.73428
16	2	Y	TREAT	SS3	15	9.3513	0.63298	0.82440
17	2	Y	ROW(REP)	SS3	15	13.8467	0.93726	0.53691
18	2	Y	COL(REP)	SS3	15	9.8368	0.66584	0.79576





## Chapter 14

# Principal Components (PC) and Additive Main Effects and Multiplicative Interaction (AMMI) Trend Analyses for Incomplete Block and Lattice Rectangle-Designed Experiments

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### *Importance*

A principal component (PC) is a linear combination of data that has a maximum sum of squares. No other linear combination can be associated with a larger sum of squares. Therefore, the analyses outlined in this chapter could prove useful when describing spatial variation found in field experiments. PC and additive main effects and multiplicative interaction (AMMI) analyses have been used in genotype-by-environment studies. The problem is that the degrees of freedom for these linear combinations need to be obtained via simulations. A program for doing this is given in Chapter 13 of this book. The SAS code allocates a single degree of freedom for each PC, but this is not correct. In such a case, if the F-value associated with a PC is less than the F-value at the 25 percent level, the PC sum of squares is pooled with the residual sum of squares. Rather than applying this rule, one may use a SAS/MIXED procedure to eliminate all effects from the model that has variance components estimated as zero; however, the two procedures do not give the same result in general. Since the properties of this procedure have not been established, it is not recommended.

## References

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- Moreno-Gonzales, J. and Crossa, J. (1998). Combining environments, genotypes, and attribute variables in regression models for predicting the cell-means of multi-environment trials. *Theoretical and Applied Genetics* 96:803-811.
- Zobel, R.W. (1990). A powerful statistical tool for understanding genotype-by-environment interaction. In Kang, M.S. (Ed.), *Genotype-by-Environment Interaction and Plant Breeding* (pp. 126-140). Louisiana State University, Baton Rouge, Louisiana.

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## Data

The example used to illustrate the SAS code is a balanced lattice square-designed experiment. By altering the program appropriately, the code can also be used for incomplete block and row-column-designed experiments. Also, PCs can be computed using the correlation matrix or the variance-covariance matrix. The SAS default uses the correlation matrix.

## Originator

Cochran, W.G. and Cox, G.M. (1957). *Experimental Designs*, John Wiley & Sons, New York.

```
/* Here the data are included, but an infile statement may be used to
   input data. */
data original;
  input y rep row col grad treat; /* grad is the linear regression
    coefficient on column order. */
  label row='incomplete block';
  datalines;
  9.0  1  1  1  -3  10
  20.3 1  1  2  -1  12
  17.7 1  1  3   1   9
  26.3 1  1  4   3  11
   4.7 1  2  1  -3   2
   9.0 1  2  2  -1   4
```

7.3	1	2	3	1	1
8.3	1	2	4	3	3
9.0	1	3	1	-3	14
6.7	1	3	2	-1	16
11.7	1	3	3	1	13
4.3	1	3	4	3	15
4.0	1	4	1	-3	6
5.0	1	4	2	-1	8
5.7	1	4	3	1	5
14.3	1	4	4	3	7
19.0	2	1	1	-3	5
8.7	2	1	2	-1	12
13.0	2	1	3	1	15
15.7	2	1	4	3	2
12.0	2	2	1	-3	10
6.0	2	2	2	-1	7
15.3	2	2	3	1	4
12.0	2	2	4	3	13
12.7	2	3	1	-3	16
6.3	2	3	2	-1	1
1.7	2	3	3	1	6
13.0	2	3	4	3	11
3.7	2	4	1	-3	3
3.7	2	4	2	-1	14
8.0	2	4	3	1	9
13.3	2	4	4	3	8
17.0	3	1	1	-3	10
7.0	3	1	2	-1	15
10.3	3	1	3	1	8
1.3	3	1	4	3	1
11.3	3	2	1	-3	9
12.3	3	2	2	-1	16
3.0	3	2	3	1	7
5.3	3	2	4	3	2
12.3	3	3	1	-3	12
8.7	3	3	2	-1	13
8.0	3	3	3	1	6
9.3	3	3	4	3	3
30.3	3	4	1	-3	11
22.3	3	4	2	-1	14
11.0	3	4	3	1	5
12.7	3	4	4	3	4
5.0	4	1	1	-3	16
10.3	4	1	2	-1	12
5.7	4	1	3	1	8
12.7	4	1	4	3	4
2.7	4	2	1	-3	11
6.7	4	2	2	-1	15
10.3	4	2	3	1	3
5.7	4	2	4	3	7
1.0	4	3	1	-3	1
10.3	4	3	2	-1	5
11.3	4	3	3	1	9
11.7	4	3	4	3	13
11.0	4	4	1	-3	6
19.0	4	4	2	-1	2
20.7	4	4	3	1	14

```

29.7 4 4 4 3 10
2.0 5 1 1 -3 3
5.0 5 1 2 -1 16
4.0 5 1 3 1 5
13.7 5 1 4 3 10
9.3 5 2 1 -3 6
1.7 5 2 2 -1 9
6.3 5 2 3 1 4
12.3 5 2 4 3 15
16.7 5 3 1 -3 12
4.3 5 3 2 -1 7
18.7 5 3 3 1 14
8.7 5 3 4 3 1
16.7 5 4 1 -3 13
30.0 5 4 2 -1 2
25.7 5 4 3 1 11
14.0 5 4 4 3 8
run;

```

```

/* principal component analysis. */
proc sort data=original;
  by rep col row;
proc transpose data=original prefix=row out=origr(drop=_name_);
  by rep col;
  var y;
/* The SAS default option is the correlation matrix. If it is desired
   to use the variance-covariance matrix, simply add COV at the end
   of the following statement and also in the next PROC PRINCOMP
   statement.*/
proc princomp data=origr prefix=rpc out=rowvar noprint;
  by rep;
  var row1-row4; /* Four rows in the design. */
proc sort data=original;
  by rep row col;
proc transpose data=original prefix=col out=origc(drop=_name_);
  by rep row;
  var y;
proc princomp data=origc prefix=cpc out=colvar noprint;
  by rep;
  var col1-col4; /* Four columns in the design. */

/* expand data sets and merge */
data cc;
  set colvar;
  array colv{4} col1-col4;
  do col = 1 to 4;
    y = colv{col};
    output;
  end;
  drop col1-col4;
data rr;
  set rowvar;
  array rowv{4} row1-row4;
  do row = 1 to 4;
    y = rowv{row};
    output;
  end;

```

```

    drop row1-row4;
proc sort data=rr;
  by rep row col;
data ana;
  merge original cc rr;
  by rep row col;

/* analysis of variance, fixed principal component effects, non-nested
  */
proc glm data=ana;
  class rep treat;
  model y=rep treat cpc1 cpc2 rpcl rpc2 cpc1*rpcl cpc1*rpc2
    cpc2*rpcl cpc2*rpc2 ;
run;

/* fixed principal component effects, nested */
proc glm data=ana;
  class rep treat;
  model y=rep treat cpc1(rep) cpc2(rep) rpcl(rep) cpc1*rpcl(rep)
    cpc1*rpc2(rep)
    cpc2*rpcl(rep) cpc2*rpc2(rep) ;
run;

/* random principal component effects, nested */
proc mixed data = ana;
  class rep treat row col;
  model y = treat;
  random rep cpc1(rep) cpc2(rep) rpcl(rep) cpc1*rpcl(rep)
    cpc1*rpc2(rep)
    cpc2*rpcl(rep) cpc2*rpc2(rep);
  lsmeans treat;
run;

/* fixed effects textbook analysis of the design as in Cochran and Cox
  (1957), page 493. */
proc glm data=ana;
  class rep row col treat;
  model y=rep treat row(rep) col(rep);
run;

/* fixed AMMI trend analysis, PC within row within replicate */
proc glm data = ana;
  class rep treat row col;
  model y = rep treat row(rep) rpcl*row(rep);
run;

/* random AMMI effect within row and random row and rep effects */
proc mixed data = ana;
  class rep treat row col;
  model y = treat;
  random rep row(rep) rpcl*row(rep);
  lsmeans treat;
run;

```

An abbreviated form of the output from this program is given here.

```

/*fixed effect un-nested PC analysis */

```

Dependent Variable: Y

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	27	2723.926541	100.886168	5.93	0.0001
Error	52	884.611459	17.011759		
Corrected Total	79	3608.538000			

R-Square	C.V.	Root MSE	Y Mean
0.754856	37.82239	4.124531	10.90500

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.563000	7.890750	0.46	0.7619
TREAT	15	1244.202000	82.946800	4.88	0.0001
CPC1	1	937.165951	937.165951	55.09	0.0001
CPC2	1	28.780965	28.780965	1.69	0.1991
RPC1	1	465.277940	465.277940	27.35	0.0001
RPC2	1	7.694324	7.694324	0.45	0.5042
CPC1*RPC1	1	1.186538	1.186538	0.07	0.7927
CPC1*RPC2	1	7.642424	7.642424	0.45	0.5057
CPC2*RPC1	1	0.325597	0.325597	0.02	0.8905
CPC2*RPC2	1	0.087801	0.087801	0.01	0.9430

Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	4	31.5630000	7.8907500	0.46	0.7619
TREAT	15	371.7330707	24.7822047	1.46	0.1571
CPC1	1	913.7729632	913.7729632	53.71	0.0001
CPC2	1	75.9641822	75.9641822	4.47	0.0394
RPC1	1	466.8813930	466.8813930	27.44	0.0001
RPC2	1	8.7776829	8.7776829	0.52	0.4758
CPC1*RPC1	1	1.8655460	1.8655460	0.11	0.7419
CPC1*RPC2	1	7.7122489	7.7122489	0.45	0.5037
CPC2*RPC1	1	0.3476938	0.3476938	0.02	0.8869
CPC2*RPC2	1	0.0878007	0.0878007	0.01	0.9430

/\* Random PC effects, nested analysis\*/

Dependent Variable: Y

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	54	3503.080701	64.871865	15.38	0.0001
Error	25	105.457299	4.218292		
Corrected Total	79	3608.538000			

R-Square	C.V.	Root MSE	Y Mean
0.970776	18.83400	2.053848	10.90500

General Linear Models Procedure

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.563000	7.890750	1.87	0.1470
TREAT	15	1244.202000	82.946800	19.66	0.0001
CPC1 (REP)	5	1034.531257	206.906251	49.05	0.0001
CPC2 (REP)	5	46.108785	9.221757	2.19	0.0879
RPC1 (REP)	5	480.204652	96.040930	22.77	0.0001

CPC1*RPC1 (REP)	5	262.322233	52.464447	12.44	0.0001
CPC1*RPC2 (REP)	5	71.654226	14.330845	3.40	0.0177
CPC2*RPC1 (REP)	5	117.938209	23.587642	5.59	0.0014
CPC2*RPC2 (REP)	5	214.556340	42.911268	10.17	0.0001
Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	4	31.563000	7.890750	1.87	0.1470
TREAT	15	84.006127	5.600408	1.33	0.2576
CPC1 (REP)	5	1145.198035	229.039607	54.30	0.0001
CPC2 (REP)	5	56.156010	11.231202	2.66	0.0462
RPC1 (REP)	5	401.390987	80.278197	19.03	0.0001
CPC1*RPC1 (REP)	5	197.143931	39.428786	9.35	0.0001
CPC1*RPC2 (REP)	5	67.960365	13.592073	3.22	0.0222
CPC2*RPC1 (REP)	5	138.518519	27.703704	6.57	0.0005
CPC2*RPC2 (REP)	5	214.556340	42.911268	10.17	0.0001

The MIXED Procedure

Least Squares Means

Effect	TREAT	LSMEAN	Std Error	DF	t	Pr >  t
TREAT	1	7.54548158	1.72555784	29	4.37	0.0001
TREAT	2	10.37683195	1.75725118	29	5.91	0.0001
TREAT	3	9.37048456	1.56493910	29	5.99	0.0001
TREAT	4	12.34206915	1.57505850	29	7.84	0.0001
TREAT	5	11.45961200	1.61696971	29	7.09	0.0001
TREAT	6	9.11047013	1.69326123	29	5.38	0.0001
TREAT	7	7.86631476	1.75974765	29	4.47	0.0001
TREAT	8	11.11913803	1.67931870	29	6.62	0.0001
TREAT	9	12.18761611	1.64388978	29	7.41	0.0001
TREAT	10	14.08160555	1.92299755	29	7.32	0.0001
TREAT	11	13.13295404	1.92869896	29	6.81	0.0001
TREAT	12	11.40375822	1.67381535	29	6.81	0.0001
TREAT	13	10.59779026	1.54426804	29	6.86	0.0001
TREAT	14	12.13599166	1.70542148	29	7.12	0.0001
TREAT	15	9.18610407	1.62649961	29	5.65	0.0001
TREAT	16	12.56377795	1.63547347	29	7.68	0.0001

/\* textbook analysis, fixed effects \*/

Dependent Variable: Y

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	49	2928.370083	59.762655	2.64	0.0029
Error	30	680.167917	22.672264		
Corrected Total	79	3608.538000			

R-Square	C.V.	Root MSE	Y Mean
0.811511	43.66382	4.761540	10.90500

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.563000	7.890750	0.35	0.8433
TREAT	15	1244.202000	82.946800	3.66	0.0012
ROW (REP)	15	1093.015500	72.867700	3.21	0.0032
COL (REP)	15	559.589583	37.305972	1.65	0.1197

Source	DF	Type III SS	Mean Square	F Value	Pr > F
--------	----	-------------	-------------	---------	--------



REP	4	31.563000	7.890750	0.35	0.8433
TREAT	15	319.452083	21.296806	0.94	0.5350
ROW (REP)	15	1026.755833	68.450389	3.02	0.0049
COL (REP)	15	559.589583	37.305972	1.65	0.1197

... ..

/\* treatment means from random effects AMMI analysis \*/

Effect	TREAT	LSMEAN	Std Error	DF	t	Pr >  t
TREAT	1	6.37311825	2.38292075	25	2.67	0.0130
TREAT	2	10.61497350	2.15761108	25	4.92	0.0001
TREAT	3	7.93436160	2.06059560	25	3.85	0.0007
TREAT	4	12.28827249	1.99475730	25	6.16	0.0001
TREAT	5	10.76991952	1.97476997	25	5.45	0.0001
TREAT	6	8.24325882	2.17029859	25	3.80	0.0008
TREAT	7	5.71709277	2.38681041	25	2.40	0.0244
TREAT	8	10.24396596	2.09650099	25	4.89	0.0001
TREAT	9	12.25845651	2.11969951	25	5.78	0.0001
TREAT	10	14.74535577	2.35708086	25	6.26	0.0001
TREAT	11	15.30490826	2.42463576	25	6.31	0.0001
TREAT	12	13.57092699	2.14533617	25	6.33	0.0001
TREAT	13	11.45714987	2.01082282	25	5.70	0.0001
TREAT	14	13.94971794	2.10372824	25	6.63	0.0001
TREAT	15	8.62267164	2.09619203	25	4.11	0.0004
TREAT	16	12.38585010	2.14469670	25	5.78	0.0001

## Chapter 15

# A Method for Classifying Observations Using Categorical and Continuous Variables

Jorge Franco  
José Crossa

### *Purpose*

Classifying observations into homogeneous subpopulations or groups using categorical and continuous variables is important in various fields of research, such as genetic resource conservation, genetics, plant breeding, biotechnology, agronomy, and ecology.

The program outlined in this chapter uses a statistical method for classifying observations into homogeneous groups.

### *Definitions*

The objective is to classify  $n$  observations using the statistical technique known as the mixture of a finite number of distributions. The model assumes a statistical distribution for variables. The probability of membership of each observation in each subpopulation or group is computed. The program allows use of continuous variables (Gaussian Model, GM) (McLachlan and Basford, 1988) or of continuous and categorical variables (Modified Location Model, MLM) (Franco et al., 1998). Homogeneity of variance-covariance matrices within subpopulations is also assumed.

The GM model assumes that each vector  $\mathbf{y}_j$  ( $j = 1, \dots, n$ ), formed with  $p$  continuous variables is distributed as a mixture of  $g$  multivariate, a multivariate normal with  $p$  variables, each corresponding to a subpopulation. Thus, assuming homogeneity of variance-covariance matrices within subpopulations, its probability density function (PDF) is

$$f(y_j; \Theta) = \prod_{i=1}^g \alpha_i (2)^{-p/2} | \Sigma_i |^{-1/2} \exp \left\{ -(1/2)(y_j - \mu_i) \Sigma_i^{-1} (y_j - \mu_i) \right\}$$

where the vector  $\Theta$  contains the parameters of the model;  $\alpha_i$  ( $i = 1, 2, \dots, g$ ) is the proportion of observations in each subpopulation (cluster) of the mixture;  $\Sigma_i$  is the common variance-covariance matrix within a subpopulation; and  $\mu_i$  represents vectors of means of the  $i$ th subpopulation.

The MLM model transforms the vector formed with  $p$  continuous and  $q$  categorical variables into a  $p + 1$  vector in which all the categorical values are transformed into a unique multinomial variable  $W$  that takes values  $s = 1, 2, \dots, m$ , where  $m$  is the number of combinations observed or multinomial cells. The vector of  $p + 1$  variables ( $x_{sj}$ ) is assumed to be distributed as a mixture of the product of the multinomial and multinormal variables. The model assumes that the dispersion matrices and mean vectors are equal for all of the multinomial cells within each subpopulation; thus, its probability density function is

$$f(x_{sj}; \Theta) = \prod_{i=1}^g \alpha_i p_{is} (2)^{-p/2} | \Sigma_i |^{-1/2} \exp \left\{ -(1/2)(y_{sj} - \mu_i) \Sigma_i^{-1} (y_{sj} - \mu_i) \right\}$$

where the vector  $\Theta$  contains the parameters of the model;  $\alpha_i$  ( $i = 1, 2, \dots, g$ ) is the proportion of observations in each subpopulation (cluster) of the mixture;  $p_{is}$  is the proportion of observations in the  $s$ th multinomial cell of the  $i$ th subpopulation;  $\Sigma_i$  is the common variance-covariance matrix within a subpopulation; and  $\mu_i$  are the vectors of means of the  $i$ th subpopulation.

The program uses the expectation maximization (EM) algorithm (Dempster et al., 1977) to estimate parameters (maximization) and to calculate the probability of membership for each observation (expectation).

The likelihood function corresponding to the matrix of the whole sample data,  $X$ , is the objective function for the maximization. For the MLM model, this function is

$$L(\Theta; X) = \prod_{s=1}^m \prod_{j=1}^{n_s} f(x_{sj}; \Theta) = \prod_{s=1}^m \prod_{j=1}^{n_s} \prod_{i=1}^g \alpha_i p_{is} (2)^{-p/2} | \Sigma_i |^{-1/2} \exp \left\{ -(1/2)(y_{sj} - \mu_i) \Sigma_i^{-1} (y_{sj} - \mu_i) \right\} .$$

### Originator

Franco, J., Crossa, J., Villaseñor, J., Taba, S., and Eberhart, S.A. (1998). Classifying genetic resources by categorical and continuous variables. *Crop Science* 38(6):1688-1696.

## Software Available

Franco, J. and Crossa, J. (2001). SAS program for classifying observations using categorical and continuous attributes. Centro Internacional de Mejoramiento de Maiz y Trigo (CIMMYT, INT), access online: <<http://www.cimmyt.org/biometrics>>.

## Key References

- Dempster, A.P., Laird, N.M., and Rubin, D.B. (1977). Maximum likelihood from incomplete data via the EM algorithm. *Journal of Royal Society, Series B*, 39:1-38.
- Franco, J., Crossa, J., Ribaut, J.M., Betran, J., Warbuton, M.L., and Khairallah, M. (2001). A method for combining molecular markers and phenotypic attributes for classifying plant genotypes. *Theoretical and Applied Genetics* 103(6/7):944-952.
- Franco, J., Crossa, J., Villaseñor, J., Taba, S., and Eberhart, S.A. (1998). Classifying genetic resources by categorical and continuous variables. *Crop Science* 38(6):1688-1696.
- McLachlan, G.J. and Basford, K.E. (1988). *Mixture models: Inference and applications to clustering*. Marcel Dekker, New York.

## Contacts

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## Modifications to the Program

Lines that can be modified begin with **/\***, end with **\*/**, and are in bold. The program starts with a data file called DATA0 (this name can be changed) with the following characteristics:

1. Observations are rows; variables are columns.
2. The variable showing initial subpopulations must be called CLASS0 (CLASS zero); the discrete variables must be called Q1, Q2,..., Qq. If the GM model (only continuous variables) is required, use a unique discrete variable (Q1) with all values equal to 1.
3. Names for continuous variables can be any valid SAS name no longer than eight characters and should not begin with a number.

4. Any other variable (not included in the analysis) must be dropped from line L2.

The next lines that can be modified are:

1. L3: The TABLES statement must be followed by a list of discrete variables Q1\*Q2\*...\*Qq joined by an asterisk (\*).
2. L4, L5, L6: The statements must be Q1-Qq, where q is the subindex for the last discrete variable.
3. L8, L9: These lines can be modified to allow more than fifty iterations or a lesser value of convergence.
4. L10, L11, L12: In these lines you must write the names of continuous variables.

The program produces a file (SAS file) called FINAL that contains the following information:

1. All the initial information plus the number of group to which each observation was assigned (named FINGROUP)
2. Membership probabilities for each observation in each group (named GROUP1,...,GROUPg)
3. Starting group (called INIGROUP)
4. Results from the canonical analysis

The program performs a canonical analysis on the continuous variables to observe the separation of the groups on the first two canonical variables and to allow characterization of the groups relative to the continuous variables.

### ***EXAMPLE***

The example comes from Franco et al. (2001). Fifteen maize genotypes are classified using five continuous variables (days to anthesis and silking, plant and ear height, and grain weight) and fifteen discrete variables (restriction fragment length polymorphism [RFLP] markers). There are five initial subpopulations (or groups). Note that categorical variables can be binary, ordinal, or multistate. The data T0 is created from the original and

five initial groups are defined to form data set DATA0. Lines for forming the data set DATA0 are shown in bold.

### SAS Program

```

OPTIONS LS=132 PS=9000 NODATE NOCENTER;
TITLE Modified Location Model, Franco et al. 1998;
TITLE2 Example, Table 6, Franco et al. 2001;
DATA T0;INPUT NOBS ad sd ph eh grw Q1-Q15;
LABEL NOBS='ENTRY';
CARDS;
  1  87.61 91.37  97.00 36.36 286.07 0 1 1 0 0 1 0 1 0 0 1 0 1 1 1
  2  89.96 96.20 110.00 38.42 292.08 0 0 1 0 0 0 0 1 0 1 0 1 0 0 1
  3  87.49 94.91 119.33 56.36 169.67 1 1 1 0 0 1 0 1 0 0 1 0 1 1 0
  4  92.97 96.77 100.33 35.77 290.78 0 0 0 1 0 0 1 0 1 0 0 1 1 0 0
  5  90.73 91.36 120.33 50.48 702.64 1 0 1 1 1 0 1 0 1 0 0 1 0 0 1
  6  90.85 94.33 117.33 50.16 427.10 1 0 1 1 1 1 1 0 0 1 0 1 0 0 0
  7  83.85 88.02 101.67 41.91 263.24 0 0 1 0 1 0 1 0 1 0 1 0 1 1 1
  8  84.93 87.09 113.67 41.53 498.19 0 0 0 1 0 0 0 0 1 0 1 0 0 1 0
  9  91.30 92.32 119.33 37.26 522.76 1 0 1 1 1 1 1 0 0 1 0 1 0 0 0
 10  87.95 88.04 115.00 53.76 505.95 0 0 0 1 0 0 0 1 0 1 0 1 0 1 0
 11  91.51 92.37 106.67 36.64 451.09 0 0 0 0 1 0 1 0 1 0 1 0 1 1 1
 12  83.33 84.72 103.67 31.66 316.84 1 1 0 1 0 0 0 0 0 1 0 0 1 0 1
 13  89.43 91.59 113.67 42.55 572.25 0 1 0 1 1 0 0 0 1 0 1 0 1 1 0
 14  86.19 87.82  97.33 40.15 581.17 0 1 0 0 0 0 0 1 0 1 0 1 1 0 1
 15  86.88 87.75 126.67 47.99 518.48 1 0 1 1 1 1 1 0 1 0 0 1 0 0 0
DATA T6;INPUT G6 @@;CARDS;
  1  2  1  3  4  4  5  3  4  5  5  6  2  2  4
;
DATA T5;INPUT G5 @@;CARDS;
  1  2  1  3  4  4  5  3  4  5  5  2  2  2  4
;
DATA T4;INPUT G4 @@;CARDS;
  1  2  1  3  4  4  3  3  4  3  3  2  2  2  4
;
DATA T3;INPUT G3 @@;CARDS;
  1  1  1  2  3  3  2  2  3  2  2  1  1  1  3
;
DATA T2;INPUT G2 @@;CARDS;
  1  1  1  1  2  2  1  1  2  1  1  1  1  1  2
;
/*L1*/ DATA DATA0; MERGE T0 T2 T3 T4 T5 T6;
/*L2*/ DATA DATA1;SET DATA0; CLAS0 = G5; DROP G2-G6;
/*L3*/ PROC FREQ; TABLES
Q1*Q2*Q3*Q4*Q5*Q6*Q7*Q8*Q9*Q10*Q11*Q12*Q13*Q14*Q15 / LIST;
/*L4*/ PROC SORT DATA=DATA1;BY Q1-Q15 NOBS;
/*L5*/ DATA T1;SET DATA1;DROP Q1-Q15;
/*L6*/ DATA T2;SET DATA1;KEEP Q1-Q15;

PROC IML;
REMOVE ALL;
USE T1;
NAM1=CONTENTS(T1);
READ ALL INTO A;
/* GENERATING VARIABLE W */

```

```

READ ALL VAR{CLAS0} INTO CLAS0;
G=CLAS0[];
VARCUA=CONTENTS(T2);
USE DATA1;
READ ALL VAR VARCUA INTO Q;
N=NROW(Q);
NQ=NCOL(Q);
P=NCOL(A)-2;
W=J(N,1,1);
DO I=2 TO N;
  IF Q[I,] = Q[I-1,] THEN W[I]=W[I-1];
  ELSE W[I] = W[I-1] + 1;
END;
M=W[];
D1=A||W;
NAM2=NAM1`||{W};
CREATE D1 FROM D1 [COLNAME=NAM2];
APPEND FROM D1;
STORE N NQ P G M;
QUIT;
PROC SORT DATA=D1; BY W CLAS0 NOBS;
PROC IML;
LOAD N P G M;
NAM1=CONTENTS(D1);
USE D1;
READ ALL INTO D1;
READ ALL VAR {W CLAS0} INTO M0;
MI=J(M,G,0); M1=J(1,2,0);
DO S=1 TO M;
  DO I=1 TO G;
    M1[1,1]=S;M1[1,2]=I;
    DO J=1 TO N;
      IF M0[J,] = M1 THEN MI[S,I] = 1;
    END;
  END;
END;
STORE MI;
QUIT;

DATA T1;SET D1;DROP NOBS W CLAS0;
DATA T2;SET D1;KEEP NOBS W CLAS0;

PROC IML;
LOAD N P G M MI;

START CERO;
VARCLAS=CONTENTS(T2);
VARCONT=CONTENTS(T1);
T={GROUP};
IG=INT(G/10);
VARTAO=CHAR(J(G,1,0));
XX=1;
DO X=0 TO IG;
  DO Y=0 TO 9;
    IF (0 < (10*X+Y) & (10*X+Y) <= G) THEN DO;
      VARTAO[XX]=CONCAT(T,CHAR(X,1),CHAR(Y,1));
      XX=XX+1;
    END;
  END;
END;

```

```

    END;
  END;
END;
ENE=J(M,G,0);
USE D1;
CONT=0;
DO S=1 TO M;
  DO I=1 TO G;
    IF MI[S,I] = 1 THEN DO;
      READ ALL WHERE(W=S & CLAS0=I) VAR VARCONT INTO B;
      ENE[S,I]=NROW(B);
    END;
  END;
END;
ENEI=ENE[+, ]` ; ENES=ENE[, +] ; N=SUM(ENE);
PRINT VARCLAS VARCONT M G P VARTAO;
PRINT ENE N ENEI ENES [FORMAT=5.0];
FINISH CERO;

START UNO;
/* INITIAL ESTIMATIONS */
/* MEANS AND SUM OF SQUARES BY GROUP */
USE D1;
MEDI=J(G,P,0); SC=J(P,P,0);
DO I=1 TO G;
  READ ALL WHERE(CLAS0=I) VAR VARCONT INTO B;
  MEDI[I, ]=J(1,NROW(B),1/NROW(B))*B;
  SC=SC+B`*(I(NROW(B))-J(NROW(B),NROW(B),1/NROW(B)))*B;
END;
V=SC/N;
SINV=INV(V);
DETS=DET(V);
/* ALPHA AND P ESTIMATION */
ALFA=ENEI/N;
PE=J(M,G,0);
DO S=1 TO M;
  DO I=1 TO G;
    IF MI[S,I] = 1 THEN PE[S,I] = ENE[S,I] / ENEI[I];
    ELSE PE[S,I] = 1E-04;
  END;
END;
DO I=1 TO G;
  NCERO=0;
  DO S=1 TO M;
    IF PE[S,I] <= 1E-04 THEN NCERO=NCERO+1;
  END;
  DO S=1 TO M;
    IF PE[S,I] > 1E-04 THEN PE[S,I] =
      PE[S,I] - NCERO*1E-04 / (M - NCERO);
  END;
END;
PRINT V [FORMAT=9.4];
PRINT DETS;
PRINT MEDI [FORMAT=9.4];
PRINT ALFA [FORMAT=7.5];
PRINT PE [FORMAT=7.5];
PRINT "LOG LIKELIHOOD :";
FINISH UNO;

```



```

START DOS;          /* LIKELIHOOD AND POSTERIOR PROBABILITY ESTIMATION*/
CONT3=0; TAO=J(N,G,0); L=J(N,G+1,0); ID=J(N,3,0); B1=J(N,P,0);
DO S=1 TO M;
  DO I=1 TO G;
    IF MI[S,I] = 1 THEN DO;
      READ ALL WHERE(W=S & CLAS0=I) VAR(NOBS CLAS0 W) INTO ID0;
      READ ALL WHERE(W=S & CLAS0=I) VAR VARCONT INTO B;
      L0=J(ENE[S,I],G,0);
      DO K=1 TO G;
        IF PE[S,K] <= 1E-04 THEN PE[S,K] = 1E-04;
        L0[,K]=LOG(ALFA[K])+LOG(PE[S,K])-0.5*
          VECDIAG((B-REPEAT(MEDI[K,],ENE[S,I],1))*SINV*
            (B-REPEAT(MEDI[K,],ENE[S,I],1)))`);
      END;
      L1=-(P/2)*1.83788-0.5*LOG(DETS)+L0;
      L2=EXP(L1);
      L3=LOG(L2[,+]);
      L[(CONT3+1:CONT3+ENE[S,I]),(1:G+1)] = L1||L3;
      TAO1=EXP(L1-(REPEAT(L3,1,G)));
      ID[(CONT3+1:CONT3+ENE[S,I]),(1:3)] = ID0;
      TAO[(CONT3+1:CONT3+ENE[S,I]),(1:G)] = TAO1;
      B1[(CONT3+1:CONT3+ENE[S,I]),(1:P)] = B;
      CONT3=CONT3+ENE[S,I];
    END;
  END;
END;
GROUP=TAO[,<:>]; MAXP=TAO[,];
C=ID||B1||TAO||GROUP||MAXP;
C1=J(N,P+G+5,0);
DO I=1 TO N;
  T1=TAO[I,];
  IF (T1[,] < 0.75) THEN C1[I,]=C[I,];
END;
LOGLTOT=SUM(L[,G+1]);
RESET NONAME;
PRINT LOGLTOT [FORMAT=20.5];
RESET NAME;
FINISH DOS;

START TRES;          /* MAXIMUM LIKELIHOOD ESTIMATORS (MAXIMIZATION) */
DO I=1 TO G;
  ALFA[I]=SUM(TAO[,I])/N;
END;
MED=J(M*G,P,0); TOT=J(G,P,0); MEDI=J(G,P,0); DIV=J(G,1,0);
CONT=0; CONT3=0;
DO S=1 TO M;
  DO I=1 TO G;
    TT=TAO[(CONT3+1:CONT3+ENES[S]),I];
    BB= B1[(CONT3+1:CONT3+ENES[S]),];
    PE[S,I]=SUM(TT)/(N*ALFA[I]);
    IF PE[S,I] > 0 THEN DO;
      CONT=CONT+1;
      MED[CONT,]=TT`*BB/(N*PE[S,I]*ALFA[I]);
    END;
  END;
END;
CONT3=CONT3+ENES[S];

```

```

END;
CONT=0;
DO S=1 TO M;
  DO I=1 TO G;
    IF PE[S,I] > 0 THEN DO;
      CONT=CONT+1;
      TOT[I,]=TOT[I,] + MED[CONT,] * N * PE[S,I] * ALFA[I];
      DIV[I]=DIV[I] + N * PE[S,I] * ALFA[I];
    END;
  END;
END;
DO I=1 TO G;
MEDI[I,] = TOT[I,] * (1/DIV[I]);
END;
SC=J(P,P,0);CONT3=0;
DO S=1 TO M;
  DO I=1 TO G;
    TT=TAO[(CONT3+1:CONT3+ENES[S]),I];
    BB= B1[(CONT3+1:CONT3+ENES[S]),];
    IF PE[S,I] > 0 THEN DO;
      SC=SC+(TT#(BB-REPEAT(MEDI[I,],NROW(BB),1)))`*
        (BB-REPEAT(MEDI[I,],NROW(BB),1)));
    END;
  END;
  CONT3=CONT3+ENES[S];
END;
V=SC/N;
SINV=INV(V);
DETS=DET(V);
FINISH TRES;

START EM;                                     /* LOOP UNTIL LOG-LIKELIHOOD CONVERGE */
DO WHILE ((ABS(LOGLTOT-LOGLTOT0)/ABS(LOGLTOT0)) > CRIT);
  ITERA=ITERA+1;
  LOGLTOT0=LOGLTOT;
/*L8*/ IF ITERA = 50 THEN CRIT=10;
/*L9*/ ELSE CRIT = 1E-8;
  RUN TRES;
  RUN DOS;
END;
FINISH EM;

*****                                     RUNNING                                     ***** ;

RUN CERO;
RUN UNO;
RUN DOS;
LOGLTOT0 = LOGLTOT - 1;
CRIT=0;
ITERA=1;
RUN EM;
TAOM=TAO[,]; CALI=TAOM[:];
FINGROUP={FINGROUP}; MAXPN={MAXPROB};
NAMES=VARCLAS`||VARCONT`||VARTAO`||FINGROUP||MAXPN;
CREATE FINAL FROM C [COLNAME=NAMES];
APPEND FROM C;
CREATE BAJAS FROM C1 [COLNAME=NAMES];

```

```

APPEND FROM C1;
PRINT "FINAL RESULTS:" ;
RESET NONAME;
PRINT LOGLTOT "          FINAL LOG-LIKELIHOOD";
RESET NAME;
PRINT PE [FORMAT=7.5];
PRINT V [FORMAT=9.4];
PRINT DETS;
PRINT MEDI [FORMAT=9.4];
PRINT ITERA "          NUMBER OF ITERATIONS";
PRINT "          AVERAGE OF THE MAXIMA OF THE PROBABILITIES:";
RESET NONAME;
PRINT CALI [FORMAT=8.4];
RESET NAME;
QUIT;

DATA T1;SET FINAL;
INIGROUP=CLAS0; DROP CLAS0;
TITLE2 'INITIAL AND FINAL CLASSIFICATIONS';
PROC FREQ; TABLES INIGROUP*FINGROUP / NOCOL NOPERCENT;
PROC FREQ; TABLES W*FINGROUP / NOPERCENT;
PROC PRINT; VAR NOBS W INIGROUP FINGROUP MAXPROB;
DATA T2;SET BAJAS;
INIGROUP=CLAS0;DROP CLAS0 MAXPROB;
IF INIGROUP EQ 0 THEN DELETE;
TITLE2 'OBSERVATIONS CLASSIFIED WITH LEAST THAN 75% OF PROBABILITY';
PROC PRINT;
RUN;
TITLE '          ';
RUN;

PROC SORT DATA=DATA0 OUT=T1;BY NOBS;
PROC SORT DATA=FINAL OUT=T2;BY NOBS;
DATA FIN;MERGE T1 T2;BY NOBS;
PROC SORT DATA=FIN OUT=C1; BY FINGROUP;
PROC MEANS NOPRINT DATA=C1;BY FINGROUP;
/*L10*/      VAR ad sd ph eh grw;
/*L11*/ OUTPUT OUT=C2 MEAN= ad sd ph eh grw;
DATA MED;SET C2;SIZE=_FREQ_;DROP _FREQ_ _TYPE_;
PROC PRINT;
/*L12/ proc candisc data=fin mah;var ad sd ph eh grw; class fingroup;
RUN;

```

## Results

### 1. Frequency analysis showing the formation of each value of the *W* variable:

The FREQ Procedure

Cumulative		Cumulative													Per-	Cum.	Per-	
Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10	Q11	Q12	Q13	Q14	Q15	Freq.	cent	Freq.	cent

0	0	0	0	1	0	0	0	1	0	1	0	1	0	1	1	6.67	1	6.67
0	0	0	0	1	0	1	0	1	0	1	0	1	1	1	1	6.67	2	13.33
0	0	0	1	0	0	0	0	1	0	1	0	0	1	0	1	6.67	3	0.00
0	0	0	1	0	0	1	0	1	0	0	1	1	0	0	1	6.67	4	6.67
0	0	1	0	0	0	0	1	0	1	0	1	0	0	1	1	6.67	5	33.33
0	0	1	0	1	0	1	0	1	0	1	0	1	1	1	1	6.67	6	40.00
0	1	0	0	0	0	0	1	0	1	0	1	1	0	1	1	6.67	7	46.67
0	1	0	1	1	0	0	1	0	1	0	1	1	0	1	1	6.67	8	53.33
0	1	1	0	0	1	0	1	0	0	1	0	1	1	1	1	6.67	9	60.00
1	0	1	1	1	0	1	0	1	0	0	1	0	0	1	1	6.67	10	66.67
1	0	1	1	1	1	1	0	0	1	0	1	0	0	0	2	13.33	12	80.00
1	0	1	1	1	1	1	0	1	0	0	1	0	0	0	1	6.67	13	86.67
1	1	0	1	0	0	0	0	0	1	0	0	1	0	1	1	6.67	14	93.33
1	1	1	0	0	1	0	1	0	0	1	0	1	1	0	1	6.67	15	100.00

- Names of the categorical (VARCLAS) and continuous (VARCONT) variables; number of levels of the *W* variable (M), number of groups (G), and number of continuous variables (P); numbers of observations by cell (ENE), total number of observations (N), number of observations by group (ENEI); and number of observations by multinomial cell (ENES):

VARCLAS	VARCONT	M	G	P	VARTAO	ENE	N	ENEI	ENES
NOBS	ad	14	5	5	GROUP01	0	15	2	1
CLAS0	sd				GROUP02	0		4	1
W	ph				GROUP03	0		2	1
	eh				GROUP04	0		4	1
	grw				GROUP05	0		3	1
0	0	0	0	1		0			
0	0	0	0	1		0			
0	0	1	0	0		0			
0	0	1	0	0		0			
0	1	0	0	0		0			
0	0	0	0	1		0			
0	1	0	0	0		0			
0	1	0	0	0		0			
1	0	0	0	0		0			
0	0	0	1	0		0			
0	0	0	2	0		0			
0	0	0	1	0		0			
0	1	0	0	0		0			
1	0	0	0	0		0			

- Description of the initial grouping: variance-covariance matrix (V),  $\det(V) = \text{DETS}$ , vectors of means by group (MEDI), proportion of observations by group (ALFA), and proportion of observations by cell (PE):

## V

6.8643	7.5542	-0.7639	-1.2623	13.8824
7.5542	10.7997	0.3649	0.6961	-110.3075
-0.7639	0.3649	42.2084	26.2318	88.4037
-1.2623	0.6961	26.2318	36.8485	157.3504
13.8824	-110.3075	88.4037	157.3504	11672.031

## DETS

44954302

## MEDI

87.5500	93.1400	108.1650	46.3600	227.8700
87.2275	90.0825	106.1675	38.1950	440.5850
88.9500	91.9300	107.0000	38.6500	394.4850
89.9400	91.4400	120.9150	46.4725	542.7450
87.7700	89.4767	107.7800	44.1033	406.7600

## ALFA

0.13333  
0.26667  
0.13333  
0.26667  
0.20000

## PE

0.00010	0.00010	0.00010	0.00010	0.33297
0.00010	0.00010	0.00010	0.00010	0.33297
0.00010	0.00010	0.49940	0.00010	0.00010
0.00010	0.00010	0.49940	0.00010	0.00010
0.00010	0.24975	0.00010	0.00010	0.00010
0.00010	0.00010	0.00010	0.00010	0.33297
0.00010	0.24975	0.00010	0.00010	0.00010
0.00010	0.24975	0.00010	0.00010	0.00010
0.49940	0.00010	0.00010	0.00010	0.00010
0.00010	0.00010	0.00010	0.24963	0.00010
0.00010	0.00010	0.00010	0.49963	0.00010
0.00010	0.00010	0.00010	0.24963	0.00010
0.00010	0.24975	0.00010	0.00010	0.00010
0.49940	0.00010	0.00010	0.00010	0.00010

## 4. Convergence of the log-likelihood:

LOG LIKELIHOOD :

-277.82415  
-277.79638  
-277.69873  
-276.90376

-271.46840  
 -262.19260  
 -258.50714  
 -258.50701  
 -258.50701

### 5. Final results: Description of the resulting groups:

-258.507                      FINAL LOG-LIKELIHOOD

V

4.0629	5.5976	0.5649	-0.2552	0.3318
5.5976	9.1068	4.0598	2.7156	-81.5348
0.5649	4.0598	37.4202	24.9494	-78.6771
-0.2552	2.7156	24.9494	36.7351	89.2941
0.3318	-81.5348	-78.6771	89.2941	8410.8310

DETS

3426193.4                      MEDI

86.3166	91.4333	106.0000	44.8765	239.6610
86.7680	89.4840	107.6680	38.8621	452.1069
92.9700	96.7700	100.3300	35.7700	290.7808
89.9400	91.4400	120.9150	46.4725	542.7451
89.7300	90.2050	110.8350	45.2000	478.5200

ITERA

9                      NUMBER OF ITERATIONS

AVERAGE OF THE MAXIMUM PROBABILITIES:

1.0000

INITIAL AND FINAL CLASSIFICATIONS

The FREQ Procedure

### 6. Two-way tables of the observed changes produced by the MLM and the distribution of the W variable into the final groups:

Table of INIGROUP by FINGROUP

INIGROUP	FINGROUP						
Frequency							
Row Pct	1	2	3	4	5	Total	
-----+-----+-----+-----+-----+-----+-----	1	2	0	0	0	0	2
100.00	0.00	0.00	0.00	0.00	0.00		
-----+-----+-----+-----+-----+-----+-----	2	0	4	0	0	0	4

	0.00	100.00	0.00	0.00	0.00	
3	0	1	1	0	0	2
	0.00	50.00	50.00	0.00	0.00	
4	0	0	0	4	0	4
	0.00	0.00	0.00	100.00	0.00	
5	1	0	0	0	2	3
	33.33	0.00	0.00	0.00	66.67	
Total	3	5	1	4	2	15

Table of W by FINGROUP

W	FINGROUP					Total
Frequency	1	2	3	4	5	
Row Pct						
Col Pct						
1	0	0	0	0	1	1
	0.00	0.00	0.00	0.00	100.00	
	0.00	0.00	0.00	0.00	50.00	
2	0	0	0	0	1	1
	0.00	0.00	0.00	0.00	100.00	
	0.00	0.00	0.00	0.00	50.00	
3	0	1	0	0	0	1
	0.00	100.00	0.00	0.00	0.00	
	0.00	20.00	0.00	0.00	0.00	
4	0	0	1	0	0	1
	0.00	0.00	100.00	0.00	0.00	
	0.00	0.00	100.00	0.00	0.00	
5	0	1	0	0	0	1
	0.00	100.00	0.00	0.00	0.00	
	0.00	20.00	0.00	0.00	0.00	
6	1	0	0	0	0	1
	100.00	0.00	0.00	0.00	0.00	
	33.33	0.00	0.00	0.00	0.00	
7	0	1	0	0	0	1
	0.00	100.00	0.00	0.00	0.00	
	0.00	20.00	0.00	0.00	0.00	
8	0	1	0	0	0	1
	0.00	100.00	0.00	0.00	0.00	
	0.00	20.00	0.00	0.00	0.00	
9	1	0	0	0	0	1
	100.00	0.00	0.00	0.00	0.00	
	33.33	0.00	0.00	0.00	0.00	

10	0	0	0	1	0	1
	0.00	0.00	0.00	100.00	0.00	
	0.00	0.00	0.00	25.00	0.00	
11	0	0	0	2	0	2
	0.00	0.00	0.00	100.00	0.00	
	0.00	0.00	0.00	50.00	0.00	
12	0	0	0	1	0	1
	0.00	0.00	0.00	100.00	0.00	
	0.00	0.00	0.00	25.00	0.00	
13	0	1	0	0	0	1
	0.00	100.00	0.00	0.00	0.00	
	0.00	20.00	0.00	0.00	0.00	
14	1	0	0	0	0	1
	100.00	0.00	0.00	0.00	0.00	
	33.33	0.00	0.00	0.00	0.00	
Total	3	5	1	4	2	15

7. Initial (INIGROUP) and final (FINGROUP) classification by observation (NOBS), and probability of membership of each observation into the final group:

INITIAL AND FINAL CLASSIFICATIONS

Obs	NOBS	W	INIGROUP	FINGROUP	MAXPROB
1	10	1	5	5	1.00000
2	11	2	5	5	1.00000
3	8	3	3	2	1.00000
4	4	4	3	3	1.00000
5	2	5	2	2	1.00000
6	7	6	5	1	1.00000
7	14	7	2	2	1.00000
8	13	8	2	2	1.00000
9	1	9	1	1	1.00000
10	5	10	4	4	1.00000
11	6	11	4	4	1.00000
12	9	11	4	4	1.00000
13	15	12	4	4	1.00000
14	12	13	2	2	0.99996
15	3	14	1	1	1.00000

8. Description of the observations classified in a group with membership probability less than or equal to 0.75. *In this example, there were no observations classified with 0.75 or less probability.*



## 9. Means of the continuous variables by FINGROUP:

Obs	FINGROUP	ad	sd	ph	eh	grw	SIZE
1	1	86.3167	91.4333	106.000	44.8767	239.660	3
2	2	86.7680	89.4840	107.668	38.8620	452.106	5
3	3	92.9700	96.7700	100.330	35.7700	290.780	1
4	4	89.9400	91.4400	120.915	46.4725	542.745	4
5	5	89.7300	90.2050	110.835	45.2000	478.520	2

## 10. Canonical analysis:

The CANDISC Procedure

Observations	15	DF Total	14
Variables	5	DF Within Classes	10
Classes	5	DF Between Classes	4

Class Level Information

FINGROUP	Variable Name	Frequency	Weight	Proportion
1	_1	3	3.0000	0.200000
2	_2	5	5.0000	0.333333
3	_3	1	1.0000	0.066667
4	_4	4	4.0000	0.266667
5	_5	2	2.0000	0.133333

## 11. Mahalanobis distances between groups:

Pairwise Squared Distances Between Groups

$$D^2(i|j) = \bar{X}_i - \bar{X}_j \text{ COV}^{-1} \bar{X}_i - \bar{X}_j$$

Squared Distance to FINGROUP

From FINGROUP	1	2	3	4	5
1	0	9.69890	31.89182	32.03905	53.71280
2	9.69890	0	47.17016	25.33743	64.65959
3	31.89182	47.17016	0	21.83177	11.25790
4	32.03905	25.33743	21.83177	0	16.44569
5	53.71280	64.65959	11.25790	16.44569	0

## 12. Canonical analysis:

Eigenvalues of Inv(E)\*H  
= CanRsq/(1-CanRsq)

Test of H0: The canonical  
correlations in the current  
row and all that follow are zero

Eigenvalue		Cumulative		Likelihood			Pr > F	
Eigenvalue	Difference	Proportion	Cumulative	Likelihood Ratio	Approx. F Value	Num DF	Den DF	Pr > F
13.0060	9.4873	0.7566	0.7566	0.00896176	3.28	20	20.85	0.0048
3.5187	3.0719	0.2047	0.9613	0.12551810	1.87	12	18.812	0.1089
0.4468	0.2281	0.0260	0.9873	0.56717249	0.87	6	16	0.5349
0.2187		0.0127	1.0000	0.82057834	0.98	2	9	0.4107

## 13. Correlations between the canonical and the original variables:

Pooled Within Canonical Structure

Variable	Can1	Can2	Can3	Can4
ad	0.237833	0.038504	-0.573316	0.675213
sd	0.066067	-0.143236	-0.342918	0.869577
ph	0.130221	0.426431	0.662903	0.598061
eh	0.077913	0.038632	0.779939	0.275478
grw	0.130604	0.581677	-0.090215	-0.512354

## 14. Class means on canonical variables:

FINGROUP	Can1	Can2	Can3	Can4
1	-2.195407354	-2.087516850	0.619110701	0.208971868
2	-2.871781847	0.763304861	-0.330874168	-0.251208708
3	2.982907431	-2.512395225	-1.568231850	0.543463597
4	2.006569437	1.682283872	0.234528031	0.361097995
5	4.967973060	-0.885357009	0.213579232	-0.679363820



## Chapter 16

# Mixed Linear Model Approaches for Quantitative Genetic Models

Jixiang Wu  
Jun Zhu  
Johnie N. Jenkins

### *Purpose*

Computer software for estimating variance and covariance components, correlations, and predicting genetic effects.

### *Software Description*

We describe a suite of genetic software that employs mixed linear model approaches. The various components relate to three categories, viz, genetic models for diallel crosses (Table 16.1), seed traits (Table 16.2), and developmental traits (Table 16.3). It can also be used to analyze regional agronomic trials.

This software has several features:

1. Handles complicated genetic models for agronomic traits, seed traits, and developmental traits
2. Analyzes unbalanced data
3. Utilizes jackknifing techniques to test the significance of each genetic parameter
4. Provides some important references containing results
5. Fast computation

## ***System Requirements***

*Hardware:* PC 486 or above; 16MB RAM, or more; 10 MB or more available hard disk space

*Operating System:* Microsoft Windows 95/98, Microsoft Windows NT 3.5 or above.

## ***Installing***

The software suite is available upon request to the author or from the Web site: <<http://msa.ars.usda.gov/ms/msstate/csrl/jenkins.htm>>.

All related files are compressed into RUNWIN32.EXE, a self-extracting file. To install the software,

1. Copy RUNWIN32.ZIP to a subdirectory (e.g. *c:\WIN32*) on hard disk using Windows Explorer or Windows NT Explorer.
2. Double click RUNWIN32.ZIP and all files will be extracted into the current subdirectory WinZip 6.3 extraction software.

## ***Tasks Performed by the Software***

This software performs analyses on agronomic traits for diallel cross models; seed models; developmental models; and regional trials.

### ***A. Programs for Diallel Cross Models***

Table 16.1 shows programs for diallel crosses.

This software can be used to estimate genetic variance components and genetic covariance components and to predict genetic effects and heterosis for AD, ADM, and ADAA models.

### ***B. Programs for Seed Models***

Table 16.2 includes programs for seed models. These programs can also be used to estimate genetic variance components, genetic covariance components, and to predict genetic effects of diploid seed and triploid seed models.

TABLE 16.1. Diallel Crosses

Genetic Models	Jackknife by cell	Jackknife by block
AD <sup>1</sup>	GENAD	GENAD
	GENVAR1C	GENVAR1R
	GENCOV1C	GENCOV1R
	GENHET1C	GENHET1R
ADM <sup>2</sup>	GENADM	GENADM
	GENVAR1C	GENVAR1R
ADAA <sup>3</sup>	GENADAA	GENADAA
	GENVAR1C	GENVAR1R
	GENCOV1C	GENCOV1R

<sup>1</sup>Additive-dominance models

<sup>2</sup>Additive-dominance maternal models

<sup>3</sup>Additive-dominance additive × additive epistasis models

TABLE 16.2. Seed Models

Genetic models	Jackknife by cell	Jackknife by block
Diploid	GENDIPLD	GENDIPLD
	GENVAR0C	GENVAR0R
	GENCOV0C	GENCOV0R
	GENHET0C	GENHET0R
Triploid	GENTRIPL	GENTRIPL
	GENVAR0C	GENVAR0R
	GENCOV0C	GENCOV0R
	GENHET0C	GENHET0R

### *C. Programs for Developmental Genetic Models*

Table 16.3 includes programs for developmental traits. These programs can be used to create conditional data files, to estimate conditional genetic variance components, and to predict conditional genetic effects for AD, ADM, ADAA for diploid or triploid seed models. Some programs have appeared in Tables 16.1 and 16.2.

TABLE 16.3. Developmental Traits

Genetic Models	Jackknife by cells	Jackknife by block
AD	GENAD	GENAD
	GENCOND1	GENCOND1
	GENVAR1C	GENVAR1R
ADM	GENADM	GENADM
	GENCOND1	GENCOND1
	GENVAR1C	GENVAR1R
ADAA	GENADAA	GENADAA
	GENCOND1	GENCOND1
	GENVAR1C	GENVAR1R
Diploid	GENDIPLD	GENDIPLD
	GENCOND0	GENCOND0
	GANVAR0C	GENVAR0R
Triploid	GENTRIPL	GENTRIPL
	GENCOND0	GENCOND0
	GENVAR0C	GENVAR0R

## *Use of the Software Package*

### *A. Diallel Model Analysis*

*Step 1.* Build a data file. The arrangement of data is shown in file diall1.txt. on the Web page. The first five columns in this file represent environment (e.g., year or location), female, male, generation, and block. In column 1, enter environment number (1...e); in column 2 and 3, enter female and male number, respectively (1...p); and in column 5 enter block number (1...b). The data identifiers should be consecutive positive integers, each beginning with 1. The generation codes for column 4 are 0 for parents, 1 for  $F_1$ , and 2 for  $F_2$ . Enter data in columns 6 to  $n$ .

*Step 2.* Create an information matrix based on genetic models. Run GENAD for AD model, GENADM for ADM model, and GENADE for ADAA model. For example, when GENAD is chosen, prompts will automatically appear on screen as follows:

Input name of your data file: (e.g., dial 1.txt)

Do you have block effects within location (or environment)? Y/N

When running GENADM, you will see an extra prompt:

Do you analyze triploid endosperm? Y/N

Two files will be automatically created, e.g., *dial1.dat*, *dial1.mat*, where, *dial1.mat* contains matrix information, and *dial1.dat* contains the data of traits to be analyzed.

*Step 3.* Estimate the variance components and predict genetic effects. For example, when GENVAR1C or GENVAR1R is selected on the screen you will see the following prompts:

Input name of your data file: (input the data file name as given in Step 2).

What kind of parents did you use? Input 1 for inbred or 0 for outbred.

Choose prediction method. Do you want to use LUP or AUP? Input L for LUP and O for AUP.

Input coefficients for each parent: 1 for first group, -1 for second group, 0 for others.

Input sampling number for the jackknife procedure if running GENVAR1C.

The results are automatically stored in a file named, for example, *dial1.var*.

*Step 4.* Estimate covariance components and correlation coefficients. After finishing step 3, you can run GENCOV1C or GENCOV1R, and you will see the following prompts:

Input name of your data file: (the name given in Step 2);

What kind of parents did you use? Input 1 for inbred or 0 for outbred;

Input sampling number for the jackknife procedure: if running GENCOV1C.

The results are automatically stored in a file named, for example, *dial1.cor*.

*Step 5.* Predict heterosis. After running step 2, you can run GENHET1C or GENHET1R. Follow the prompts that automatically appear on the screen after you have chosen to run either model:

Input name of your data file: (input the name used in Step 2);

What kind of parents did you use? Input 1 for inbred or 0 for outbred;



Input sampling number for the jackknife procedure: if running GENHET1C.

The results are automatically stored in a file named, for example, *dial1.pre*. Note: During the process, other temporary files such as *matrix.var*, *matrix.uq2*, *matrix.uq3*, *matrix.uq4*, *matrix.uq5*, or *matdjc.var* will be created. The user should delete these files after finishing all analyses.

### B. Seed Model Analysis

*Step 1.* Build a data file. The arrangement of data is shown in file *ctseed.txt*. The first five columns in this data file represent environment (e.g., year, location), female, male, generation, and block. In column 1, enter environment number (1 . . . e), in column 2, female number, in column 3, male number (1 . . . p), and in column 5, block number (1 . . . b). The data identifiers should be consecutive integers, each beginning with 1. The generation codes for column 4 are 0 for parent, 1 for  $F_1$ , 2 for  $F_2$ , 3 for  $BC1 = (F_1 \times P_1)$ , 4 for  $BC2 = (F_1 \times P_2)$ , 5 for  $RBC1 = (P_1 \times F_1)$ , and 6 for  $RBC2 = (P_2 \times P_2)$ . Enter data in columns 6 to *n*.

*Step 2.* Construct an information matrix based on genetic models; GENDIPLD for diploid seed model and GENTRIPL for triploid seed model. When GENDIPLD is run, the following prompts appear on the screen:

Input name of your data file: (for example, enter *ctseed.txt*)  
Do you have block effect within location? Y/N

Note: Two files will be automatically created, *ctseed.dat*, *ctseed.mat*, where *ctseed.mat* contains matrix information, and *ctseed.dat* contains data on traits to be analyzed.

*Step 3.* Estimate variance components and predict genetic effects. For example, for GENVAR0C or GENVAR0R, the following prompts will appear on the screen:

Input name of your data file: (name given in Step 2)  
Choose prediction method. Do you want to use LUP or AUP? For LUP, input L, for AUP input O.  
Input coefficients for each parent: 1 for first group, -1 for second group, and 0 for others;

Input sampling number for the jackknife procedure: if running GENVAR0C.

The results are automatically stored in the *ctseed.var* file.

*Step 4.* Estimate covariance components and correlation coefficients. For example, run GENCOV0C or GENCOV0R. When running this program, on-screen prompts include:

Input name of your data file: (name given in Step 2)

Input sampling number for the jackknife procedure: if running GENCOV0C.

The results are automatically stored in the *ctseed.cov* file. Note: The user should delete temporary files created during the execution of the program, after finishing all analyses.

### *C. Developmental Genetic Model Analysis*

*Step 1.* Construct the file. The file format is the same as for the diallel and seed models.

*Step 2.* Convert traits to conditional traits.

(a) Construct information matrix based on genetic models.

For example, for AD model run GENAD and follow the on-screen prompts.

Input name of your data file: filename.txt

Do you have blocks within location? Y/N

(b) Run GENCOND1 or GENCOND0, where GENCOND1 is for AD, ADM, and ADAA models; and GENCOND0 is for diploid and triploid seed models.

*Step 3.* Now run steps 2 through 5 from A (diallel models) or B (seed models), the only difference being the change in the name of input file from *filename.txt* to *filename.doc* (the latter is a conditional data file).

### *D. Crop Regional Trial Analysis*

Software included: GENTEST, GENETESTM, and GENTESTW. These programs can be used to estimate variance components, compare

the significance of differences among varieties, and to evaluate the stability of each variety.

*Step 1.* Build the data file. The arrangement of data is shown in the file *msbean.txt*. The four columns represent variety, year, location, and replication. In the first column, enter variety number (check variety should be the highest number; this is important if you choose to transform data relative to the check). In the second column, enter year number. In the third column, location number; and in the fourth column enter replication number. The data identifiers should be consecutive positive integers beginning with 1.

*Step 2.* Construct an information matrix based on chosen genetic models.

For example, run GENTEST and follow these on-screen prompts:  
Input name of your data file:

*Step 3.* Estimate stability for a single trait.

For example, run GENTESTM and follow the on-screen prompts:  
Input name of your data file: (from Step 1).

Do you want to transform data relative to check genotype? Y/N

How many linear contrasts do you want?

Input coefficients for each variety: 1 for first group, -1 for second group, 0 for others.

The results are automatically stored in the *region.var* file. The results include variance components, linear contrasts among different genotypes, and stability of each genotype for each trait.

*Step 4.* Estimate stability for multiple traits.

For example, run GENTESTW and follow on-screen prompts:

Input name of your data file: (from Step 1).

Input weight or values for each trait (sum of these weights = 1.0).

How many linear contrasts do you want?

Input coefficients for each variety: 1 for first group, -1 for second group, 0 for others.

The results are automatically stored in the *region.cov* file. These results include variance and covariance components and stability of each genotype for multiple traits.

The following references may help the reader to understand the use of software packages and Internet sites.

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## Chapter 17

# Best Linear Unbiased Prediction (BLUP) for Genotype Performance

Mónica Balzarini  
Scott Milligan

### *Importance*

Whenever the examined genotypes (varieties, clones, cultivars, etc.) in an experiment can be regarded as random samples from larger sets or populations, genotype effects should also be considered random in the model. Commonly, random genotype effects are assumed to broaden inferences, i.e., to allow inference about a reference population. Moreover, pairwise comparisons between specific genotypes that have been examined will also be feasible. In addition to estimating genotype variance components, which are of intrinsic interest with random genotype effects, genotypes can be compared by calculating best linear unbiased predictors (BLUPs) of genotype effects. In this context, “best” means minimum mean squared prediction error (MSPE). The smaller the MSPE, the greater the relationship between the dependent and independent variables.

BLUPs are used to predict random effects in mixed models. The predictable function,  $\mu + G_i$ ,  $i = 1, \dots, g$ , allows inference about the performance of the  $i$ th genotype from a trial involving  $g$  randomly selected varieties (broad inference). Thus, the BLUPs of  $\mu + G_i$  in a mixed model have a similar role as the genotype mean in a fixed-effect model. BLUPs are called *shrinkage estimators* because they are obtained by regression toward the overall mean based on the variance components of the model effects. A simple version of BLUP to estimate genetic performance of the  $i$ th genotype, in a model containing unrelated genotypes as random effects, is

$$\text{BLUP}(\mu + G_i) = \bar{Y}_{..} - F^G (\bar{Y}_i - \bar{Y}_{..})$$

where  $F^G$  is the shrinkage factor that =

$$\frac{\sigma_G^2}{\sigma_G^2 + \frac{\sigma_e^2}{n}},$$

where  $\sigma_G^2$  is genetic variance or variance among genotypes,  $\sigma_e^2$  is the error variance or variance within genotype, and  $n$  is the number of observations per genotype. Thus, for this simple model, the estimator moves the genotype mean toward the overall mean depending on the magnitude of a trait's heritability. A large heritability value implies little shrinkage or more reliability of genotype means, and in such a case, genotype BLUPs resemble genotype means. Therefore, the smaller the heritability value, the larger the shrinkage of extreme genotype means toward  $\mu$  with a reduction in the risk of misinterpretation.

The BLUP for the predictable function,  $\mu$   $G_i$   $E_j$   $G \times E_{ij}$ ,  $i = 1, \dots, g$  and  $j = 1, \dots, l$ , in a model also involving environment and genotype-by-environment interaction (GE) random effects, assuming independent and equal variance random effects, is

$$\text{BLUP } \mu \quad G_i \quad E_j \quad G \times E_{ij} \quad \bar{Y} \dots \quad F^G \quad \bar{Y}_{i..} - \bar{Y} \dots \\ F^{GE} \quad \bar{Y} \dots - \bar{Y}_{i..} - \bar{Y}_{.j.} - \bar{Y}_{ij.}$$

where  $F^G$ ,  $F^E$ , and  $F^{GE}$  are the following shrinkage factors:

$$F^G = \frac{\sigma_G^2}{\sigma_G^2 + \frac{\sigma_e^2}{nl}} \quad F^E = \frac{\sigma_E^2}{\sigma_E^2 + \frac{\sigma_e^2}{ng}} \quad F^{GE} = \frac{\sigma_{GE}^2}{\sigma_{GE}^2 + \frac{\sigma_e^2}{n}}$$

where  $\sigma_{GE}^2$  represents the  $GE$  variance component,  $\sigma_E^2$  is the variance component associated with environment effects, and  $g$  and  $l$  are the number of environments and genotypes in the experiment, respectively.

A general form of BLUP of random effects can be obtained by expressing them as a solution of the mixed model equation (extended normal equations). In matrix form, a normal mixed model is

$$y = X\beta + Zu + e$$

where  $y$  is an  $n$  vector of observable random variables (data),  $X$  and  $Z$  are known design matrices,  $\beta$  is a  $p$  vector of fixed effects, and  $u$  (random effects) and  $e$  (error term) are unobservable normal random  $m$  and  $n$  vectors with covariance matrices  $G$  and  $R$ , respectively. The variance-covariance matrix is  $V = ZGZ' + R$ . Estimates of  $\beta$  and  $u$  can be written as follows:

$$\hat{\beta} = (X'V^{-1}X)^{-1}X'V^{-1}y$$

$$\hat{u} = GZ'V^{-1}(y - X\hat{\beta})$$

Since variance components are usually unknown, estimated covariance matrices are used in place of true matrices. Thus, the vector  $\hat{u}$  is better referred to as an empirical BLUP (EBLUP) to indicate that it is approximated from the data. The vector  $\hat{u}$  can be interpreted as a weighted deviation of genotype means from the overall mean after adjusting for fixed effects. Provided that  $G$  is nonsingular, the estimated covariance matrix of  $\hat{\beta}$  and  $\hat{u}$  can be written as follows:

$$\hat{C} = \begin{bmatrix} \hat{C}_{11} & \hat{C}_{21}' \\ \hat{C}_{21} & \hat{C}_{22} \end{bmatrix}, \text{ where}$$

$$\begin{aligned} \hat{C}_{11} &= (X'V^{-1}X)^{-1} \\ \hat{C}_{21} &= -GZ'V^{-1}X\hat{C}_{11} \\ \hat{C}_{22} &= (Z'R^{-1}Z + G^{-1})^{-1} - \hat{C}_{21}X'V^{-1}ZG \end{aligned}$$

The elements of  $\hat{C}_{22}$  provide the estimated prediction error variances that allow comparisons of BLUPs. A predictable function  $K\beta + Mu$  is estimated by  $K'\hat{\beta} + M'\hat{u}$ . Thus, the BLUP of  $\mu + G_i$  is  $\hat{\mu} + \hat{G}_i$ . As a linear combination of fixed and random model effects, its prediction error variance can be easily derived from  $\hat{C}$ . These estimates address the objective of assessing and comparing genotype performance in a mixed model context. The square root of the prediction error variance (a standard error analog) can be used to approximate Prediction Intervals for the pairwise BLUP differences.

If the genotypes were genetically related, a matrix of genetic relationships,  $A$ , may be used to adjust the matrix  $G$  and, in turn, the BLUPs. These relationships may be computed from pedigree or molecular-based analyses. The covariance matrix for the genetic effects is commonly written as  $G = \sigma_c^2 A$ , where elements in  $A$  are used to represent genetic related-



ness between any two genotypes, and it is expressed as a proportion of genetic variance. Note that  $A = I$  represents the special case of unrelated genotypes. Several covariance structures for  $G$  and  $R$  may be reasonable. Likewise, following the aforementioned procedure, different BLUP versions can be obtained.

A SAS macro was developed to obtain BLUPs of genotype effects, prediction errors, BLUPs of the predictable functions  $\mu + G_i$ , and pairwise, approximated prediction intervals for the differences between the BLUPs of two genotypes. The macro uses restricted maximum likelihood (REML) variance component estimates obtained from PROC MIXED of SAS (SAS, 1997). It calls for an IML module to obtain and compare the BLUPs derived with or without (Model = GGR) (model = GI), assuming a given genetic relationship among the examined genotypes.

### **EXAMPLE**

Two sample data sets, one with a large genotypic variance and the other with a small genotypic variance, are provided to show how a simple (assuming genotypes are not related) version of BLUP for genotypes (broad inference) works. Each data set contains four genotypes and four replicates per genotype.

<pre>data AltaH2; input genotype y; datalines; 1 28.41 1 27.35 1 27.25 1 28.42 2 19.90 2 18.93 2 19.52 2 19.61 3 19.65 3 18.79 3 18.86 3 19.45 4 21.80 4 18.61 4 22.37 4 22.52</pre>	<pre>data BajaH2; input genotype y; datalines; 1 18.41 1 17.35 1 17.25 1 18.42 2 19.90 2 18.93 2 19.52 2 19.61 3 19.45 3 19.65 3 21.86 3 20.79 4 21.80 4 18.61 4 22.52 4 17.37</pre>
--	--

Assuming the macro file is being retrieved from a floppy disk, write:

```
%include 'a:BLUP GP.sas' ;
%BLUP_GP (Model=GI, Workds=AltaH2, Ldata=, S2_G=, S2_A=, S2_E=,
          Class=, Fixed=, C_matrix=, PredRes=);
```

The macro arguments that can be modified by the user are:

```
Model :enter GI for Independent or unrelated Genotypes
        enter GR for Related Genotypes
Workds:work data set name
Ldata :name for the data set containing a Genetic
        relationship coefficient matrix. Required if model=GR
S2_G  :enter a known Genetic VarianceValue (otherwise it is estimated)
S2_A  :enter a known Additive Variance Value (optional)
S2_E  : enter a known Error Variance Value (otherwise it is estimated)
Class : classification variables excluding genotype (optional)
Fixed : model fixed effects separated by blanks (optional)
C_Matrix :YES to print mixed model parameter covariance matrix
PredRes : YES to print Predicted and Residual Values
```

If the model GI (unrelated genotypes) is fitted to both data sets, the BLUPs of genotype effects and the BLUPs of  $\mu + G_i$  shown in the output will be as follows:

AltaH2 data set		BajaH2 data set	
BLUP ( $G_i$ )	BLUP ( $\mu + G_i$ )	BLUP ( $G_i$ )	BLUP ( $\mu + G_i$ )
5.799	27.764 A	-0.992	18.473 B
-2.435	19.529 C	0.015	19.480 A
-2.733	19.231 C	0.600	20.065 A
-0.630	21.335 B	0.376	19.841 A

The BLUP differences among the ten possible pairwise comparisons of genotype versus a 95 percent prediction interval column containing either 1 or 0 for each contrast are shown. The zeros indicate that the prediction interval for the BLUP difference contains a zero value, which can be interpreted as not different in genotypic performance. For the AltaH2 data set, all BLUP differences, except those between genotypes 2 and 3, are significant. For the BajaH2 data set, only the difference between genotype 1 and 3 is significant. Here we show the traditional genotype means and least

significant difference (LSD) for both sample data sets to compare BLUP performance against ordinary mean performance:

AltaH2 data set		BajaH2 data set	
Genotype Mean	LSD significance	Genotype Mean	LSD significance
27.858	A	17.856	B
19.490	C	19.490	AB
19.187	C	20.438	A
21.325	B	20.075	A

Note: For a large trait heritability, BLUPs closely resemble means, but a small genotype variance component shrinks genotype performances toward the overall mean, yielding different significances in the BajaH2 data set. In a real data set (large number of genotypes and probably different genotype sample sizes), shrinkage might provide significant improvement over genotype means.

The data GR is a sample data set to enter the covariance coefficient matrix for a set of four genotypes. The columns parm (equal to 1) and row (from 1 to g) should be in the data set to conform with SAS PROC MIXED requirements for using the covariance structure type = LIN(1). This structure indicates that the covariance parameters in  $G$  are a linear combination of variance components. This variance component may be the additive variance (entered as macro argument) to obtain BLUPs with shrinkage factors based on the narrow-sense heritability (matrix coefficients should be  $2*r_{ij}$ , where  $r_{ij}$  is the coancestry coefficient between genotypes  $i$  and  $j$ ). The variance component might also be a genetic variance, entered as a macro argument or estimated from the data. The sample data GR shows a covariance coefficient (0.5) between genotypes 2 and 3.

```
Data GR;
input parm row coll-col4;
datalines;
1 1 1 0 0 0
1 2 0 1 0.5 0
1 3 0 0.5 1 0
1 4 0 0 0 1
```

The relationship coefficient matrix data set should be indicated in the macro argument LDATA, whenever model GGR is required. The output interpretation is the same as before, but BLUPs have been calculated assuming the given genetic relationship among the genotypes.

```
/*
/*SAMPLE DATA SET FOR OBTAINING BLUPS FOR GENOTYPE PERFORMANCE */
/*Data ALTAH2 shows a larger genotype variance than data BAJAH2 */
/*Data GR shows how to input a genetic relationship matrix */
/*The following variable names should be the same in your data set:*/
/*genotype, y (for trait values),Parm (equals 1),row (from 1 to g) */
/*Coll to Colg to indicate the g columns of the relationship matrix*/
```

```
data AltaH2;
input genotype y bl;
datalines;
1 28.41 1
1 27.35 2
1 27.25 3
1 28.42 4
2 19.90 1
2 18.93 2
2 19.52 3
2 19.61 4
3 19.65 1
3 18.79 2
3 18.86 3
3 19.45 4
4 21.80 1
4 18.61 2
4 22.37 3
4 22.52 4
data BajaH2;
input genotype y;
datalines;
1 18.41
1 17.35
1 17.25
1 18.42
2 19.90
2 18.93
2 19.52
2 19.61
3 19.45
3 19.65
3 21.86
3 20.79
4 21.80
4 18.61
4 22.52
4 17.37
Data GR;
input parm row coll-col4;
datalines;
1 1 1 0 0 0
1 2 0 1 0.5 0
1 3 0 0.5 1 0
1 4 0 0 0 1
;
```

```

/*                                                                    */
/*Macro BLUP_GP produces Genotype Performance BLUPs for models with */
/*only genotype effects as random. Two versions of genotype BLUPs  */
/*can be obtained (with or without relationship among genotypes)    */
/*The macro arguments are:                                           */
/*Model :enter GI for Independent or unrelated Genotypes            */
/*       enter GR for Related Genotypes                             */
/*Workds:work data set name                                          */
/*Ldata :name for the data set containing a Genetic                  */
/*       relationship coefficient matrix. Required if model=GR        */
/*S2_G   :enter a known Genetic Variance (otherwise it is estimated) */
/*S2_A   :enter a known Additive Variance (optional)                 */
/*S2_E   :enter a known Error Variance (otherwise it is estimated)  */
/*Class :classification variables excluding genotype (optional)    */
/*Fixed :model fixed effects separated by blanks (optional)        */
/*C_matrix:YES to print mixed model parameter covariance matrix     */
/*PredRes :YES to print Predicted and Residual Values               */
/*                                                                    */

options nodate nocenter;
%macro BLUP_GP(Model=GI,Workds=BajaH2,Ldata=GR,S2_G=,S2_A=,S2_E=,
              Class=,Fixed=, C_matrix=Yes,PredRes=);

proc mixed data=&workds noclprint noitprint covtest;
class genotype &class;
model y=&Fixed/pm p;

%if (&model=GI) %then %do;
  random Genotype/s ;
%end;

%if (&model=GGR) %then %do;
  random Genotype/ldata=&ldata type=lin(1) s ;
%end;

  make 'solutionR' noprint out=BLUP&model;
  make 'covparms' out=V&model;
  make 'predmeans' noprint out=L&model;
  make 'predicted' noprint out=Pred&model;

/*                                                                    */
/*Calculate the Predictable Function Mu+Genotype effect              */
/*                                                                    */

Data BLUPs;
set BLUP&model;
Keep Genotype BLUP P_Error P_value;
BLUP=_EST_;
P_Error=_SEPREDE_;
P_Value=_PT_;

%if (&S2_G<0) %then %do;
%if (&S2_A<0) %then %do;

proc print;

```

```

title1 'Genotype effect BLUPs, Prediction Error and P-Value for
      H0:BLUP=0';
run;
%end;
%end;
title1 '  ';

%if (&model=GGR) %then %do;
data AR;
set &ldata;
drop parm row;
%end;

data level;
set &workds;
keep genotype;

data VarComp;
set V&model;
if covparm='Residual' or Covparm='GENOTYPE' or covparm='LIN(1)';

data Y;
set &workds;
keep Y;

proc iml;
use Y;
read all into Y;
use L&model var{_resid_};
read all into ya;
use level;
read all into level;
use VarComp;
read all into VC;

Z=design(level);
yp=inv(Z`*Z)*Z`*ya;

S2e=VC(|2,1|);
S2u=VC(|1,1|);

%if (&S2_E>0) %then %do; S2e=&S2_E; print S2e;%end;
%if (&S2_G>0) %then %do; S2u=&S2_G; print S2u;%end;
%if (&S2_A>0) %then %do; S2u=&S2_A; print S2u;%end;

%if (&model=GI) %then %do;
  AR=I(nrow(Z`));
  V=inv(Z`*Z)*Z`*(S2u*Z*AR*Z`+S2e*I(nrow(Z)))*Z*inv(Z`*Z)`;
%end;

%if (&model=GGR) %then %do;
  use AR;
  read all into AR;
  V=inv(Z`*Z)*Z`*(S2u*Z*AR*Z`+S2e*I(nrow(Z)))*Z*inv(Z`*Z)`;
%end;

```

```

C=VC(|1,1|)*AR;
BLUPg=C*inv(V)*yp;

X=J(nrow(level),1);
G=S2u*AR;
R=S2e*I(nrow(Z));
V=Z*G*Z`+R;
Beta=inv(X`*X)*X`*Y;

K=J(nrow(Z`),1)`;
M=I(nrow(Z`));

PF=K`*Beta+M`*BLUPg;

/*
/*Calculate Prediction Error Variances
/*
*/

C11=Ginv(X`*inv(V)*X);
C21=-G*Z`*inv(V)*X*C11;
C22=inv(Z`*inv(R)*Z+inv(G))-C21*X`*inv(V)*Z*G;
COV_BU=(C11|C21`)/(C21|C22);

VarPF=K`*C11*K+M`*C22*M+2*M*C21*K;

ncon=Nrow(PF)*(Nrow(PF)-1)/2;
row=0;
LPF=shape(0,ncon,nrow(BLUPG));
Gi=shape(0,ncon,1);
Gj=shape(0,ncon,1);

do i=1 to nrow(BLUPG);
  do j=1 to nrow(BLUPG);
    If i<j then do;
      row=row+1;
      LPF[row,i]=1;
      LPF[row,j]=-1;
      Gi[row,1]=i;
      Gj[row,1]=j;
    end;
  end;
end;

Con_PF=LPF*PF;
Var_C=LPF*VarPF*LPF`;
PF_Diff=Con_PF;
Con_PF=Con_PF@j(1,nrow(LPF));
CValue=2*SQRRT(Diag(Var_C));
LS_IC=Diag(Con_PF+CValue);
LI_IC=Diag(Con_PF-CValue);

Pred_Int=J(nrow(LPF),1);
do i=1 to nrow(LPF);
  If LS_IC[i,i]>0 then do;If LI_IC[i,i]<0 then Pred_Int[i]=0;end;
end;

```

```
/*                                                    */
/*Printing Results                                    */
/*                                                    */
print 'Predictable Functions and Pairwise Differences';
print  BLUPg PF Gi GJ PF_Diff Pred Int;
print  'Pred_Int=0 means no different BLUPs';

%if (&C_matrix=YES) %then %do;
    print COV_BU;
%end;

%if (&PredRes=YES) %then %do;
    proc print data=Pred&model;
%end;

%mend BLUP_GP;

%BLUP_GP;

run;
```





## Chapter 18

# Graphing GE and GGE Biplots

Juan Burgueño  
 José Crossa  
 Mateo Vargas

### *Purpose*

- To analyze multienvironment trials and to study genotype  $\times$  environment interaction (GEI) using linear/bilinear AMMI or SREG models.
- To graph biplots to describe GEI and to identify megaenvironments and cultivars with best performance.

### *Definitions*

The linear/bilinear AMMI model is

$$\bar{y}_{ij} = \mu + \tau_i + \delta_j + \sum_{k=1}^t \alpha_{ik} \alpha_{jk} + \bar{\epsilon}_{ij}$$

and the linear/bilinear SREG model is

$$\bar{y}_{ij} = \mu + \delta_j + \sum_{k=1}^t \alpha_{ik} \alpha_{jk} + \bar{\epsilon}_{ij}$$

where  $\bar{y}_{ij}$  is mean of the  $i$ th cultivar in the  $j$ th environment;  $\mu$  is the overall mean,  $\tau_i$  is the genotypic effect;  $\delta_j$  is the site effect;  $\alpha_{k1}, \alpha_{k2}, \dots, \alpha_{kt}$  represents the singular values (scaling constants);  $\alpha_{1k}, \dots, \alpha_{gk}$  and  $\alpha_{jk}, \dots, \alpha_{ek}$  are the singular vectors for cultivars and environment, respectively, with  $\sum_i \alpha_{ik}^2 = \sum_j \alpha_{jk}^2 = 1$  and  $\sum_i \alpha_{ik} \alpha_{jk} = 0$  for  $k \neq k'$ ;  $\bar{\epsilon}_{ij}$ : residual error with NID  $(0, \sigma^2 / r)$  ( $\sigma^2$  is pooled error variance and  $r$  is number of replicates).

### *Originators*

Gollob, H.F. (1968). A statistical model which combines features of factor analytic and analysis of variance. *Psychometrika* 33:73-115.

Mandel, J. (1961). Non-additivity in two-way analysis of variance. *Journal of the American Statistical Association* 56:878-888.

### *Biplot*

Biplots graph scores of sites and genotypes of the first bilinear term against scores of sites and genotypes of the second bilinear term.

### *Originators*

Gabriel, K. R. (1971). The biplot graphic display of matrices with application to principal component analysis. *Biometrika* 58:453-467.

Yan, W., Hunt, L.A., Sheng, Q., and Szlavncics, Z. (2000). Cultivar evaluation and mega-environment investigation based on the GGE biplot. *Crop Science* 40:597-605.

### *Software Available*

Burgueño, J., Crossa, J., and Vargas, M. (2001). SAS PROGRAMS for graphing GE and GGE biplots. Centro Internacional de Mejoramiento de Maiz y Trigo (CIMMYT), INT, accessed online <<http://www.cimmyt.org/biometrics>>.

### *Key References*

Burgueño, J., Crossa, J., and Vargas, M. (2001). SAS PROGRAMS for graphing GE and GGE biplots. Centro Internacional de Mejoramiento de Maiz y Trigo (CIMMYT), INT, accessed online <<http://www.cimmyt.org/biometrics>>.

Vargas, M. and Crossa, J. (2000). The AMMI analysis and the graph of the biplot in SAS. Centro Internacional de Mejoramiento de Maiz y Trigo (CIMMYT) INT. México, p. 42.

Yan, W., Hunt, L.A., Sheng, Q., and Szlavncics, Z. (2000). Cultivar evaluation and mega-environment investigation based on the GGE biplot. *Crop Science* 40:597-605.

### *Contact*

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**Data to Be Analyzed**

Yield (kg·ha<sup>-1</sup>), obtained from individual analysis by year:

year genotype	1990	1991	1992	1993	1994	1995
1	5991.67	6640.33	5518.67	6657.67	6701.67	5280.67
2	7160.67	6081.00	5638.00	6688.67	7280.33	5869.67
3	7793.00	6954.33	5399.67	7553.33	7196.00	6041.00
4	7715.00	7170.00	6536.00	6530.67	7610.67	6284.00
5	8082.67	7224.67	6229.00	8087.67	7092.33	5891.00
6	8179.00	7467.33	6680.00	7296.00	8510.33	6901.67
7	7780.00	7095.67	7175.00	8385.67	8579.33	6931.67
8	7864.00	7632.33	7075.00	8529.67	8591.67	7012.33

**Case 1**

Using the AMMI model for obtaining the GE biplot:

```

/* setup output */
OPTIONS PS = 5000 LS=78 NODATE;
FILENAME BIPLLOT 'EXAMPLE1.CGM';
GOPTIONS DEVICE=CGMMWVC GSFNAME=BIPLLOT GSFMODE=REPLACE;

/* read data file */
DATA RAW;
      INFILE 'c:\cimmyt\ami\EXAMPLE1.DAT';
      INPUT ENV $ GEN $ YIELD;
      YLD=YIELD/1000;

/* analysis linear-bilinear model */
PROC GLM DATA=RAW OUTSTAT=STATS ;
      CLASS ENV GEN;
      MODEL YLD = ENV GEN ENV*GEN/SS4;
DATA STATS2;
SET STATS ;
DROP _NAME_ _TYPE_ ;
IF _SOURCE_ = 'ERROR' THEN DELETE;

/* values obtained from previous analysis */
MSE=0.1580245;
DFE=94;
NREP=3;
SS=SS*NREP;
MS=SS/DF;
F=MS/MSE;
PROB=1-PROBF(F,DF,DFE) ;
PROC PRINT DATA=STATS2 NOOBS;
      VAR _SOURCE_ DF SS MS F PROB;

/* define AMMI model */
PROC GLM DATA=RAW NOPRINT;
      CLASS ENV GEN;
      MODEL YLD = ENV GEN / SS4 ;
      OUTPUT OUT=OUTRES R=RESID;
PROC SORT DATA=OUTRES;

```

```

        BY GEN ENV;
PROC TRANSPOSE DATA=OUTRES OUT=OUTRES2;
        BY GEN;
        ID ENV;
        VAR RESID;

PROC IML;
USE OUTRES2;
READ ALL INTO RESID;
NGEN=NROW (RESID) ;
NENV=NCOL (RESID) ;
USE STATS2;
READ VAR {MSE} INTO MSEM;
READ VAR {DFE} INTO DFEM;
READ VAR {NREP} INTO NREP;
CALL SVD (U,L,V,RESID) ;
MINIMO=MIN (NGEN,NENV) ;
L=L[1:MINIMO,] ;
SS=(L##2)*NREP;
SUMA=SUM(SS) ;
PERCENT=((1/SUMA)#SS)*100;
MINIMO=MIN (NGEN,NENV) ;
PERCENTA=0;

        DO I = 1 TO MINIMO;
                DFA=(NGEN-1)+(NENV-1)-(2*I-1) ;
                DFA=DFA/DFE;
                PORCEACU=PERCENT[I,] ;
                PERCENTA=PERCENTA+PORCEACU;
                PERCENAC=PERCENAC//PERCENTA;

        END;
DFE=J (MINIMO,1,DFEM) ;
MSE=J (MINIMO,1,MSEM) ;
SSDF=SS||PERCENT||PERCENAC||DFA||DFE||MSE;
L12=L##0.5;
SCOREG1=U[,1]#L12[1,];
SCOREG2=U[,2]#L12[2,];
SCOREG3=U[,3]#L12[3,];
SCOREE1=V[,1]#L12[1,];
SCOREE2=V[,2]#L12[2,];
SCOREE3=V[,3]#L12[3,];
SCOREG=SCOREG1||SCOREG2||SCOREG3;
SCOREE=SCOREE1||SCOREE2||SCOREE3;
SCORES=SCOREG//SCOREE;
CREATE SUMAS FROM SSDF;
APPEND FROM SSDF;
CLOSE SUMAS;
CREATE SCORES FROM SCORES;
APPEND FROM SCORES ;
CLOSE SCORES;

/* obtaining the biplot's polygon and its perpendiculars */
d1=scoreg[1,1:2][cvexhull(scoreg[1,2]) [loc(cvexhull(scoreg[1,2])>0),],];
d=d1//d1[1,];
xxx=J(nrow(d)-1,1,0);
yyy=J(nrow(d)-1,1,0);
ppp={0 1,1 0};
        do i=1 to nrow(d)-1 ;
                dd=d[i:i+1,];
                if dd[1,1]>dd[2,1] then ddd=ppp*dd;
                else ddd=dd;
                p=(ddd[2,2]-ddd[1,2])/(ddd[2,1]-ddd[1,1]) ;

```

```

                if p<0 then ss=1 ;
                else ss=-1 ;
                r=tan((180-90-
abs(atan(p)*180/3.14156))*3.14156/180)*ss ;
                aa=(ddd[1,2]+ddd[2,2])/2-p*(ddd[1,1]+ddd[2,1])/2;
                xx=aa/(r-p) ;
                if abs(r)<1 then xxx[i,]=1;
                else xxx[i,]=1/abs(r);
                if xx<0 then xxx[i,]=-xxx[i,] ;
                else xxx[i,]=xxx[i,];
                yyy[i,]=xxx[i,]*r;
            end;
kk=xxx||yyy;
xx1={V1 V2};
create pol from d[colNAME=xx1];
append from d ;
close pol;
xx2={V3 V4};
create perp from kk[colNAME=xx2];
append from kk ;
close perp;
data pol; set pol; TYPE="pol";
data perp; set perp; TYPE="per";
DATA SSAMMI;
SET SUMAS;
SSAMMI =COL1;
PERCENT =COL2;
PERCENAC=COL3;
DFAMMI =COL4;
DFE =COL5;
MSE =COL6;
DROP COL1 - COL6;
MSAMMI=SSAMMI/DFAMMI;
F_AMMI=MSAMMI/MSE;
PROBF=1-PROBF(F_AMMI,DFAMMI,DFE);
PROC PRINT DATA=SSAMMI NOOBS;
        VAR SSAMMI PERCENT PERCENAC DFAMMI MSAMMI F_AMMI PROBF;

/* prepare data for plotting */

PROC SORT DATA=RAW;
        BY GEN;
PROC MEANS DATA = RAW NOPRINT;
        BY GEN ;
        VAR YLD;
        OUTPUT OUT = MEDIAG MEAN=YLD;
DATA NAMEG;
        SET MEDIAG;
        TYPE = 'GEN';
        NAME = GEN;
        KEEP TYPE NAME YLD;
PROC SORT DATA=RAW;
        BY ENV;
PROC MEANS DATA = RAW NOPRINT;
        BY ENV ;
        VAR YLD;
        OUTPUT OUT = MEDIAE MEAN=YLD;
DATA NAMEE;
        SET MEDIAE;
        TYPE = 'ENV';

```

```

NAME1 = 'S' || ENV;
NAME = COMPRESS(NAME1);
KEEP TYPE NAME YLD;
DATA NAMETYPE;
  SET NAMEG NAMEE;
DATA BILOT0 ;
  MERGE NAMETYPE SCORES;
  DIM1=COL1;
  DIM2=COL2;
  DIM3=COL3;
  DROP COL1-COL3;
data biplot ;
  set biplot0 pol perp;
PROC PRINT DATA=BILOT NOOBS;
  VAR TYPE NAME YLD DIM1 DIM2 DIM3;
Data labels;
  set biplot ;
  retain xsys '2' ysys '2' ;
  length function text $8 ;
  text = name ;
      if type = 'GEN' then do;
        color='black ' ;
        size = 0.6;
        style = 'hwcm001';
        x = dim1;
        y = dim2;
          if dim1 >=0
            then position='5';
          else position='5';
        function = 'LABEL';
        output;
      end;
      if type = 'ENV' then DO;
        color='black ' ;
        size = 0.6;
        style = 'hwcm001';
        x = 0.0;
        y = 0.0;
        function='MOVE';
        output;
        x = dim1;
        y = dim2;
        function='DRAW' ;
        output;
          if dim1 >=0
            then position='5';
          else position='5';
        function='LABEL';
        output;
      end;
      if type = "per" then do;
        color='red';
        line=2;
        size = 0.6;
        style = 'hwcm001';
        x=0.0;
        y=0.0;
        function='MOVE';
        output;
        x=v3;

```

```

                                y=v4;
                                function='DRAW';
                                output;
                                end;

/* graphing the biplot */
Proc gplot data=biplot;
Plot dim2*dim1 v2*v1 / overlay Annotate=labels frame
    Vref=0.0 Href = 0.0
    cvref=black chref=black
    lvref=3 lhref=3
    vaxis=axis2 haxis=axis1
    vminor=1 hminor=1 nolegend;
    symbol1 v=none c=black h=0.7 ;
    symbol2 v=none c=blue i=j line=3 ;
    axis2
        length = 6.0 in
        order = (-1.0 to 1.0 by 0.2)
        label=(f=hwcm001 h=1.2 a=90 r=0 'Factor 2')
        value=(h=0.8)
        minor=none;
    axis1
        length = 6.0 in
        order = (-1.0 to 1.0 by 0.2)
        label=(f=hwcm001 h=1.2 'Factor 1')
        value=(h=0.8)
        minor=none;
run;

```

## Output

The SAS System  
 General Linear Models Procedure  
 Class Level Information

Class	Levels	Values
ENV	6	90 91 92 93 94 95
GEN	8	1 2 3 4 5 6 7 8

Number of observations in data set = 48

General Linear Models Procedure

Dependent Variable:YLD

Source	DF	Sum of Squares	Mean Square	FValue	Pr>F
Model	47	36.27979794	0.77191059	.	.
Error	0	.	.		
Corrected Total	47	36.27979794			

R-Square	C.V.	RootMSE	YLDMean
1.000000	0	0	7.053890

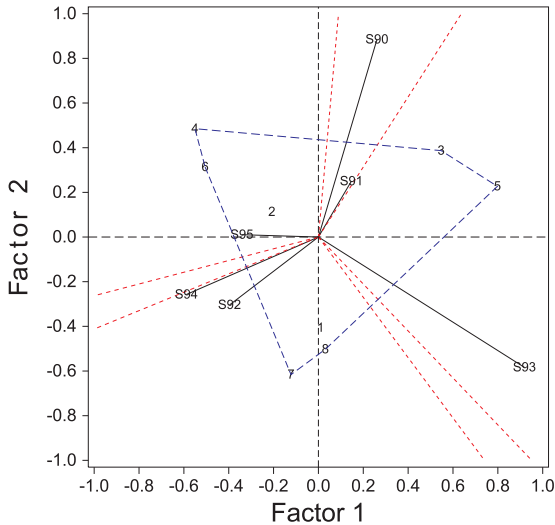


Source	DF	TypeIVSS	Mean Square	FValue	Pr>F
ENV	5	16.39991745	3.27998349	.	.
GEN	7	14.25289126	2.03612732	.	.
ENV*GEN	35	5.62698924	0.16077112	.	.

_SOURCE_	DF	SS	MS	F	PROB
ENV	5	49.1998	9.83995	62.2685	.0000000000
GEN	7	42.7587	6.10838	38.6547	.0000000000
ENV*GEN	35	16.8810	0.48231	3.0521	.0000096813

SSAMMI	PERCENT	PERCENAC	DFAMMI	MSAMMI	F_AMMI	PROBF
7.24287	42.9055	42.906	11	0.65844	4.16671	0.00005
5.42327	32.1265	75.032	9	0.60259	3.81324	0.00039
2.96965	17.5917	92.624	7	0.42424	2.68462	0.01403
1.19061	7.0530	99.677	5	0.23812	1.50686	0.19509
0.05457	0.3233	100.000	3	0.01819	0.11511	0.95106

TYPE	NAME	YLD	DIM1	DIM2	DIM3
GEN	1	6.13178	0.00956	-0.40614	0.71637
GEN	2	6.45306	-0.20785	0.11243	-0.42252
GEN	3	6.82289	0.54723	0.38688	-0.17175
GEN	4	6.97439	-0.55039	0.48510	0.32201
GEN	5	7.10122	0.79807	0.22696	0.09611
GEN	6	7.50572	-0.50527	0.31346	-0.10796
GEN	7	7.65789	-0.12223	-0.61605	-0.38304
GEN	8	7.78417	0.03088	-0.50265	-0.04923
ENV	S90	7.57075	0.26094	0.88469	-0.35836
ENV	S91	7.03321	0.14700	0.24992	0.80484
ENV	S92	6.28142	-0.39629	-0.30402	0.23481
ENV	S93	7.46617	0.91858	-0.58360	-0.19014
ENV	S94	7.69529	-0.58882	-0.25741	-0.30403
ENV	S95	6.27650	-0.34140	0.01041	-0.18713



0.00000 0.0000 100.0000 1 0.00000 0.00000 1.00000

### Case 2

Using the SREG model for obtaining the GGE biplot (required changes to the previous program are highlighted in bold):

AMMI Model	SREG Model
PROC GLM DATA=RAW NOPRINT;	PROC GLM DATA=RAW NOPRINT;
CLASS ENV <b>GEN</b> ;	CLASS ENV;
MODEL YLD = ENV <b>GEN</b> /SS4;	MODEL YLD = ENV/SSR;
OUTPUT OUT=OUTRES R=RESID;	OUTPUT OUT=OUTRES R=RESID;

The range of the scores should be changed.

Previous codes

Axis2

length = 6.0 in order = (-1 to 1 by 10)

label=(f=hwcgm001 h=1.2 a=90 r=0  
'Factor 2')

value=(h=0.8)

minor=none;

Modified codes

Axis 2

length = 6.0 in order = (-1.2 to 1.2 by 10)

label=(f=hwcgm001 h=1.2 a=90 r=0  
'Factor2')

value=(h=0.8)

minor=none;

axis 1

length = 6.0 in order = (-1 to 1 by 10)

label=(f=hwcgm001 h=1.2 'Factor 1')

value=(h=0.8)

minor=none;

axis1

length = 6.0 in order = (-1.2 to 1.2 by 10)

label=(f=hwcgm001 h=1.2 'Factor 1')

value=(h=0.6)

minor=none;

Previous codes

if abs(r)&lt;1 then xxx[i,]=1;

else xxx[i,]=1/abs(r);

Modified codes

if abs(r)&lt;1 then xxx[i,]=1.2;

else xxx[i,]=1.2/abs(r);

## Output

General Linear Models Procedure  
Class Level Information

Class	Levels	Values
ENV	6	90 91 92 93 94 95
GEN	8	1 2 3 4 5 6 7 8

Number of observations in data set = 48

General Linear Models Procedure

Dependent Variable: YLD

Source	DF	Sum of Squares	Mean Square	FValue	Pr>F
Model	47	36.27979794	0.77191059	.	.
Error	0	.	.	.	.
Corrected Total	47	36.27979794			

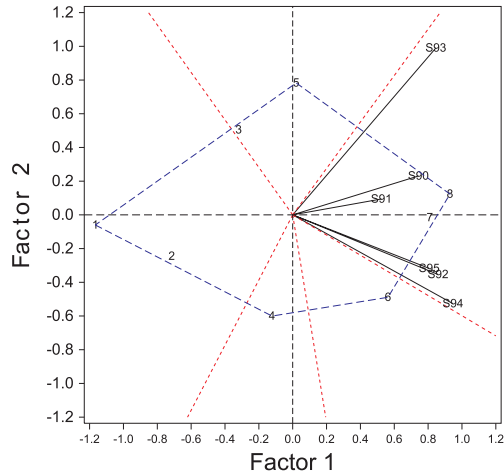
R-Square	C.V.	RootMSE	YLDMean
1.000000	0	0	7.053890

Source	DF	TypeIVSS	MeanSquare	FValue	Pr>F
ENV	5	16.39991745	3.27998349	.	.
GEN	7	14.25289126	2.03612732	.	.
ENV*GEN	35	5.62698924	0.16077112	.	.

_SOURCE_	DF	SS	MS	F	PROB
ENV	5	49.1998	9.83995	62.2685	.0000000000
GEN	7	42.7587	6.10838	38.6547	.0000000000
ENV*GEN	35	16.8810	0.48231	3.0521	.0000096813

SSAMMI	PERCENT	PERCENAC	DFAMMI	MSAMMI	F_AMMI	PROBF
43.8940	73.5988	73.599	11	3.99037	25.2516	0.00000
7.1690	12.0206	85.619	9	0.79656	5.0407	0.00002

5.1750	8.6771	94.296	7	0.73929	4.6783	0.00016
2.2756	3.8156	98.112	5	0.45513	2.8801	0.01830
1.0970	1.8394	99.951	3	0.36567	2.3140	0.08092
0.0289	0.0485	100.000	1	0.02894	0.1832	0.66965
TYPE	NAME	YLD	DIM1	DIM2	DIM3	
GEN	1	6.13178	-1.16627	-0.05995	-0.64719	
GEN	2	6.45306	-0.71482	-0.24510	0.06686	
GEN	3	6.82289	-0.31952	0.50436	0.40386	
GEN	4	6.97439	-0.12234	-0.60031	0.39015	
GEN	5	7.10122	0.02080	0.78280	0.28332	
GEN	6	7.50572	0.56288	-0.48905	0.35601	
GEN	7	7.65789	0.81001	-0.01615	-0.47082	
GEN	8	7.78417	0.92925	0.12340	-0.38218	
ENV	S90	7.57075	0.74276	0.23078	0.98338	
ENV	S91	7.03321	0.52365	0.09414	0.12375	
ENV	S92	6.28142	0.85870	-0.35358	-0.30693	
ENV	S93	7.46617	0.84586	0.99020	-0.44343	
ENV	S94	7.69529	0.94654	-0.52657	-0.19706	
ENV	S95	6.27650	0.80649	-0.31772	0.03713	





## Chapter 19

# Analysis for Regional Trials with Unbalanced Data

Jun Zhu

### *Purpose*

To analyze unbalanced data of regional trials for comparing varieties by linear contrast tests.

### *Definitions*

#### *Statistical Model*

Analysis of experimental data from regional trials is based on the following linear model, which regards the genotypic effects ( $G$ ) as fixed and further partitions the random  $E$  ( $E = Y + L + YL$ ) and  $GE$  interaction effects ( $GE = GY + GL + GYL$ ) ( $h = 1, 2, \dots, g$ ;  $i = 1, 2, \dots, n_h$ ;  $j = 1, 2, \dots, n_{hj}$ ;  $k = 1, 2, \dots, r$ ):

$$y_{hijk} = G_h + Y_i + L_j + YL_{ij} + GY_{hi} + GL_{hj} + GYL_{hij} + B_{k(ij)} + e_{hijk}$$

where,  $Y$  = year effect,  $L$  = location effect,  $YL$  = year  $\times$  location interaction effect,  $GY$  = genotype  $\times$  year effect,  $GL$  = genotype  $\times$  location effect,  $GYL$  = genotype  $\times$  year  $\times$  location interaction effect,  $B$  = block effect, and  $e$  = residual effect.

### *Analysis*

Balanced data of regional trials can be easily analyzed using ANOVA methods. The experimental data of regional trials, however, are quite often unbalanced because of missing genotype records in specific locations and



$$C_W = \sum_{h=1}^g c_h \sum_{f=1}^t w_f \hat{G}_{h(f)} \sum_{f=1}^t w_f C_{(f)}$$

with sampling variance

$$\sigma^2(C_W) = \sum_{f=1}^t w_f^2 \sigma^2(C_{(f)}) + 2 \sum_{f=1}^{t-1} \sum_{f'=1}^t w_f w_{f'} \sigma(C_{(f)}, C_{(f')})$$

where,  $\hat{\sigma}(C_{(f)}, C_{(f')}) = c^T (X^T \hat{C}_{(f,f)}^{-1} X)^{-1} c$  is the covariance between  $C_{(f)}$  and  $C_{(f')}$ .

If  $|C_W / \hat{\sigma}(C_W)| > z_{(\alpha/2)}$ , reject the null hypothesis  $H_0: \sum_{h=1}^g c_h \sum_{f=1}^t w_f G_{h(f)} = 0$  and accept the alternative hypothesis  $H_1: \sum_{h=1}^g c_h \sum_{f=1}^t w_f G_{h(f)} \neq 0$  at a significant level  $= \alpha$ .

## Originators

- Zhu, J. (1992). Mixed model approaches for estimating genetic variances and covariances. *Journal of Biomathematics* 7(1):1-11.
- Zhu, J., Lai, M.G., and Xu, F.H. (1993). Analysis methods for unbalanced data from regional trial of crop variety: Analysis for multiple traits (Chinese). *Journal of Zhejiang Agricultural University* 19(3):241-247.
- Zhu, J. and Weir, B.S. (1996). Diallel analysis for sex-linked and maternal effects. *Theoretical and Applied Genetics* 92(1):1-9.
- Zhu, J., Xu, F.H., and Lai, M.G. (1993). Analysis methods for unbalanced data from regional trials of crop variety: Analysis for single trait (Chinese). *Journal of Zhejiang Agricultural University* 19(1):7-13.

## Software Available

Zhu, J. (1997). GENTEST.EXE a computer software for constructing regional test models, GENTESTM.EXE for analyzing single traits of regional tests, and GENTESTW.EXE for analyzing multiple traits of regional tests. *Analysis Methods for Genetic Models* (pp. 285-292), Agricultural Publication House of China, Beijing (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.



**EXAMPLE**

Unbalanced data (COTTEST.TXT) to be analyzed (Variety = 3, Year = 2, Location = 8, Blk = 1):

Var	Year	Loca	Blk	Yield	Lint%
1	1	1	1	65.7	40.6
1	1	2	1	55.9	40.0
1	1	3	1	83.3	39.5
1	1	4	1	47.0	38.3
1	1	5	1	63.0	40.7
1	1	6	1	26.1	37.6
1	2	1	1	64.7	39.3
1	2	2	1	61.9	40.5
1	2	3	1	58.2	40.0
1	2	4	1	45.3	38.6
1	2	5	1	56.7	38.8
1	2	6	1	44.8	37.3
1	2	7	1	46.7	40.2
1	2	8	1	52.1	39.0
2	1	1	1	64.3	44.0
2	1	2	1	64.2	42.7
2	1	3	1	69.7	43.8
2	1	4	1	34.3	40.3
2	1	5	1	59.4	43.9
2	1	6	1	63.3	42.3
2	1	7	1	59.1	43.3
2	1	8	1	76.2	44.5
2	2	1	1	65.7	42.7
2	2	2	1	78.4	44.5
2	2	3	1	66.6	43.5
2	2	4	1	48.6	41.4
2	2	5	1	70.0	42.3
2	2	6	1	61.0	40.4
2	2	7	1	63.0	45.1
2	2	8	1	73.6	45.0
3	1	1	1	61.4	41.9
3	1	2	1	75.9	38.8
3	1	3	1	75.3	40.0
3	1	4	1	61.3	37.6
3	1	5	1	64.1	40.4
3	1	6	1	57.8	38.2
3	1	7	1	86.8	40.5
3	1	8	1	64.8	40.4
3	2	3	1	72.3	40.0

3	2	4	1	50.7	38.1
3	2	5	1	52.7	38.8
3	2	6	1	63.3	37.8
3	2	7	1	72.0	40.3
3	2	8	1	73.2	40.0

1. Use GENTEST.EXE for generating mating design matrix and data. Before running these programs, create a file for your analysis with four design columns, followed by trait columns. The four design columns are: variety, year, location, and block. There is a limitation (<100 traits) for the number of trait columns.
2. Run GENTESTM.EXE for analyzing each trait. Standard errors of estimates are calculated by jackknifing over locations for stability testing. Always run GENTESTM.EXE before analyzing multiple traits. This program will allow you to choose data transformation based on check variety. You will also need to input coefficients (1, 0, or -1) for conducting linear contrasts for different varieties. The results will be automatically stored in a file named COTTEST.VAR for analysis of single traits.
3. After you finish analysis for each trait, run GENTESTW.EXE for combining analysis of all traits studied. This program will allow you to choose weight coefficients for each trait. The results will be automatically stored in a file named COTTEST.VAR for analysis of multiple traits.

### ***Output 1 for Single Trait Test***

```

Traits =, 2
Variance components =, 6
File name is cottest.VAR
Date and Time for Analysis: Thu Jun 22 20:36:15 2000

Variance Components Estimated by MINQUE(1) with GENTESTW.EXE.
Contrast 1:  +  +  -
Contrast 2:  +  -
Contrast 3:  +  -  -

Analysis of trait Yield
Estimate of Var(Y) =, 0
Estimate of Var(L) =, 43.7906
Estimate of Var(YL) =, 0
Estimate of Var(GY) =, 1.79863
Estimate of Var(GL) =, 31.5667
Estimate of Var(e) =, 55.9106

```

Mean of Variety:,	Mean,	S.E.
Mean of Variety 1 =,	55.1,	3.86105
Mean of Variety 2 =,	63.5875,	3.71664
Mean of Variety 3 =,	66.5429,	3.86105

( 3),	V 1 ,	55.1000,	A
( 2),	V 2 ,	63.5875,	a AB
( 1),	V 3 ,	66.5429,	a B

Contrast,	C-value,	S.E.,	Standard Normal z-value
(1) This Linear Contrast Test Is for Varieties: (V1, V2) vs. (V3)	Contrast 1,	-14.398222,	7.480348, 1.924806
(2) This Linear Contrast Test Is for Varieties: (V1) vs. (V2)	Contrast 2,	-8.487495,	4.215852, 2.013234
(3) This Linear Contrast Test Is for Varieties: (V1) vs. (V2, V3)	Contrast 3,	-19.930346,	7.480348, 2.664361

Stability Analysis for Variety  
Estimates and S.E. are obtained by Jackknifing over environments.

Stability Analysis for Variety 1:  
a = -25.4509, S.E. = 24.3941, 0.95 C.I. is < -73.2633 & 22.3616 >  
b = 1.32148, S.E. = 0.3862, 0.95 C.I. is < 0.564532 & 2.07844 >  
r = 0.83176, S.E. = 0.0856267, 0.95 C.I. is < 0.663932 & 0.999588 >

Stability Analysis for Variety 2:  
a = 8.36712, S.E. = 25.0719, 0.95 C.I. is < -40.7739 & 57.5081 >  
b = 0.879325, S.E. = 0.386812, 0.95 C.I. is < 0.121172 & 1.63748 >  
r = 0.718145, S.E. = 0.157704, 0.95 C.I. is < 0.409044 & 1.02725 >

Stability Analysis for Variety 3:  
a = 16.9362, S.E. = 13.7335, 0.95 C.I. is < -9.98134 & 43.8538 >  
b = 0.804752, S.E. = 0.227599, 0.95 C.I. is < 0.358659 & 1.25085 >  
r = 0.740325, S.E. = 0.104486, 0.95 C.I. is < 0.535531 & 0.945118 >

Stability in Order for Variety  
Order by b ( 3), V 3 , a = 16.9362 , b = 0.8048 , r = 0.7403  
Order by b ( 2), V 2 , a = 8.3671 , b = 0.8793 , r = 0.7181  
Order by b ( 1), V 1 , a = -25.4509 , b = 1.3215 , r = 0.8318

Analysis of trait Lint%  
Estimate of Var(Y) =, 0  
Estimate of Var(L) =, 0.812176  
Estimate of Var(YL) =, 0.495318  
Estimate of Var(GY) =, 0  
Estimate of Var(GL) =, 0.175569  
Estimate of Var(e) =, 0.244097

Mean of Variety:,	Mean,	S.E.
Mean of Variety 1 =,	39.3143,	0.428769
Mean of Variety 2 =,	43.1063,	0.411924
Mean of Variety 3 =,	39.4857,	0.428769

( 3),	V 1 ,	39.3143,	a A
( 2),	V 3 ,	39.4857,	a A
( 1),	V 2 ,	43.1063,	

Contrast, C-value, S.E., Standard Normal z-value  
 (1) This Linear Contrast Test Is for Varieties: (V1, V2) vs. (V3)  
 Contrast 1, 3.449110, 0.552117, 6.247059  
 (2) This Linear Contrast Test Is for Varieties: (V1) vs. (V2)  
 Contrast 2, -3.791962, 0.297600, 12.741823  
 (3) This Linear Contrast Test Is for Varieties: (V1) vs. (V2, V3)  
 Contrast 3, -3.963402, 0.552117, 7.178548

Stability Analysis for Variety  
 Estimates and S.E. are obtained by Jackknifing over environments.

Stability Analysis for Variety 1:  
 a = 7.89727, S.E. = 4.23156, 0.95 C.I. is < -0.396587 & 16.1911 >  
 b = 0.772582, S.E. = 0.103208, 0.95 C.I. is < 0.570295 & 0.974869 >  
 r = 0.905533, S.E. = 0.0482835, 0.95 C.I. is < 0.810898 & 1.00017 >

Stability Analysis for Variety 2:  
 a = 0.177973, S.E. = 4.68567, 0.95 C.I. is < -9.00594 & 9.36189 >  
 b = 1.05051, S.E. = 0.115322, 0.95 C.I. is < 0.824481 & 1.27654 >  
 r = 0.917149, S.E. = 0.0463384, 0.95 C.I. is < 0.826326 & 1.00797 >

Stability Analysis for Variety 3:  
 a = 2.71998, S.E. = 4.52641, 0.95 C.I. is < -6.15178 & 11.5917 >  
 b = 0.902994, S.E. = 0.113154, 0.95 C.I. is < 0.681213 & 1.12478 >  
 r = 0.937269, S.E. = 0.0332955, 0.95 C.I. is < 0.87201 & 1.00253 >

Stability in Order for Variety  
 Order by b ( 3), V 1, a = 7.8973, b = 0.7726, r = 0.9055  
 Order by b ( 2), V 3, a = 2.7200, b = 0.9030, r = 0.9373  
 Order by b ( 1), V 2, a = 0.1780, b = 1.0505, r = 0.9171

Time Used (Hour) = 0.009722

## ***Output 2 for Multiple Trait Test***

Traits =, 2  
 Variance components =, 6  
 File name is cottest.COV  
 Date and Time for Analysis: Thu Jun 22 20:38:33 2000

Variance Components Estimated by MINQUE(1) with GENTESTW.EXE.

<W1>: 0.6, <W2>: 0.4,

Analysis for Public Users

Estimated Var for <Yield>  
 Estimate for Var(Y) =, -7.04805  
 Estimate for Var(L) =, 98.8959  
 Estimate for Var(YL) =, -1.89563  
 Estimate for Var(GY) =, 4.06199  
 Estimate for Var(GL) =, 71.2897  
 Estimate for Var(e) =, 126.267

Estimated Cov for <Yield> & <Lint%>  
 Estimate for Cov (Y) =, -0.0680642  
 Estimate for Cov (L) =, 29.2247  
 Estimate for Cov (YL) =, -2.47928  
 Estimate for Cov (GY) =, 1.12331  
 Estimate for Cov (GL) =, 1.57541  
 Estimate for Cov (e) =, 4.52009

Estimated Var for <Lint%>  
 Estimate for Var(Y) =, -0.280077  
 Estimate for Var(L) =, 5.20919  
 Estimate for Var(YL) =, 3.1769  
 Estimate for Var(GY) =, -0.097269  
 Estimate for Var(GL) =, 1.12607  
 Estimate for Var(e) =, 1.56561

Analysis for multiple traits:

Combined Variety Mean:

Mean of Variety:	Mean,	S.E.
Mean of Variety 1 =,	89.5086,	3.82078
Mean of Variety 2 =,	101.003,	3.68336
Mean of Variety 3 =,	100,	3.82078

( 3),	V 1 ,	89.5086,	a	A
( 2),	V 3 ,	100.0000,	a	A
( 1),	V 2 ,	101.0029,	a	A

Contrast, C-value, S.E. , Standard Normal z-value

(1) This Linear Contrast Test Is for Varieties:

Cont. 1, -9.488488, 49.575051, 0.191396

(2) This Linear Contrast Test Is for Varieties:

Cont. 2, -11.494320, 15.667476, 0.733642

(3) This Linear Contrast Test Is for Varieties:

Cont. 3, -21.985739, 49.575054, 0.443484

Stability Analysis for Variety

Estimates and S.E. are obtained by Jackknifing over environments.

Stability Analysis for Variety 1:

a = -28.7855, S.E. = 34.6409, 0.95 C.I. is < -96.6817 & 39.1106 >

b = 1.23013, S.E. = 0.351782, 0.95 C.I. is < 0.540642 & 1.91963 >

r = 0.827958, S.E. = 0.0706079, 0.95 C.I. is < 0.689566 & 0.966349 >

Stability Analysis for Variety 2:

a = 11.0869, S.E. = 35.9274, 0.95 C.I. is < -59.3307 & 81.5045 >

b = 0.917704, S.E. = 0.35883, 0.95 C.I. is < 0.214397 & 1.62101 >

r = 0.753344, S.E. = 0.1381, 0.95 C.I. is < 0.482668 & 1.02402 >

Stability Analysis for Variety 3:

a = 21.659, S.E. = 19.4541, 0.95 C.I. is < -16.4711 & 59.7891 >

b = 0.808956, S.E. = 0.204255, 0.95 C.I. is < 0.408615 & 1.2093 >

r = 0.781107, S.E. = 0.0871521, 0.95 C.I. is < 0.610289 & 0.951926 >

Stability in Order for Variety

Order of b ( 3), V 3 , a = 21.6590 , b = 0.8090 , r = 0.7811

Order of b ( 2), V 2 , a = 11.0869 , b = 0.9177 , r = 0.7533

Order of b ( 1), V 1 , a = -28.7855 , b = 1.2301 , r = 0.8280

Time Used (Hour) = 0.006667

## Chapter 20

# Conditional Mapping of QTL with Epistatic Effects and QTL-by-Environment Interaction Effects for Developmental Traits

Jun Zhu

### *Purpose*

To map quantitative trait loci (QTL) for net effects due to gene expression from time  $t - 1$  to  $t$ .

### *Definitions*

#### *Genetic Model*

For multiple-environment data of doubled haploid (DH) or recombinant inbred line (RIL) populations, the conditional phenotypic value of the  $j$ th genetic entry in environment  $h$  at time  $t$ , given phenotypic value at time  $t - 1$ , can be expressed as the following conditional genetic model:

$$\begin{aligned}
 y_{hj(t|t-1)} = & \mu_{(t|t-1)} + a_{1(t|t-1)}x_{A_1j} + a_{2(t|t-1)}x_{A_2j} + aa_{(t|t-1)}x_{AAj} \\
 & + u_{E_{hj}}e_{E_{h(t|t-1)}} + u_{A_1E_{hj}}e_{A_1E_{h(t|t-1)}} + u_{A_2E_{hj}}e_{A_2E_{h(t|t-1)}} + u_{AAE_{hj}}e_{AAE_{h(t|t-1)}} \\
 & + u_{M_{fj}}e_{M_{f(t|t-1)}} + u_{MM_{lj}}e_{MM_{l(t|t-1)}} + u_{ME_{hpj}}e_{ME_{hp(t|t-1)}} \\
 & + u_{MME_{hij}}e_{MME_{hij(t|t-1)}} + \epsilon_{hj(t|t-1)}
 \end{aligned}$$

where  $\mu_{(t|t-1)}$  is the conditional population mean;  $a_{1(t|t-1)}$  and  $a_{2(t|t-1)}$  are the conditional additive effects of loci  $Q_1$  and  $Q_2$ , respectively;  $aa_{(t|t-1)}$  is the

conditional additive  $\times$  additive epistatic effect of loci  $Q_1$  and  $Q_2$ ;  $x_{A_1j}$ ,  $x_{A_2j}$ , and  $x_{AA_j}$  are coefficients of these conditional genetic main effects;  $e_{E_{h(t|t-1)}}$  is the conditional random effect of environment  $h$  with coefficient  $u_{E_{hj}}$ ;  $e_{A_1E_{h(t|t-1)}}$  (or  $e_{A_2E_{h(t|t-1)}}$ ) is the conditional additive  $\times$  environment interaction effect with coefficient  $u_{A_1E_{hj}}$  (or  $u_{A_2E_{hj}}$ ) for  $Q_1$  (or  $Q_2$ );  $e_{AAE_{h(t|t-1)}}$  is the conditional epistasis  $\times$  environment interaction effect with coefficient  $u_{AAE_{hj}}$ ;  $e_{M_f}$  is the conditional marker main effect with coefficient  $u_{M_f}$ ;  $e_{MM_{l(t|t-1)}}$  is the conditional marker  $\times$  marker interaction effect with coefficient  $u_{MM_{l_1}}$ ;  $e_{ME_{hp(t|t-1)}}$  is the conditional marker  $\times$  environment interaction effect with coefficient  $u_{ME_{hpj}}$ ;  $e_{MME_{hq(t|t-1)}}$  is the marker  $\times$  marker  $\times$  environment interaction effect with coefficient  $u_{MME_{qbj}}$ ; and  $e_{hj(t|t-1)}$  is the conditional residual effect.

### Mixed Linear Model

The conditional epistasis QTL model can be expressed in the matrix form as follows:

$$\begin{aligned}
 \mathbf{y}_{(t|t-1)} &= \mathbf{X}\mathbf{b}_{(t|t-1)} + \mathbf{U}_E \mathbf{e}_{E(t|t-1)} + \mathbf{U}_{A_1E} \mathbf{e}_{A_1E(t|t-1)} + \mathbf{U}_{A_2E} \mathbf{e}_{A_2E(t|t-1)} \\
 &\quad + \mathbf{U}_{AAE} \mathbf{e}_{AAE(t|t-1)} + \mathbf{U}_M \mathbf{e}_{M(t|t-1)} + \mathbf{U}_{MM} \mathbf{e}_{MM(t|t-1)} \\
 &\quad + \mathbf{U}_{ME} \mathbf{e}_{ME(t|t-1)} + \mathbf{U}_{MME} \mathbf{e}_{MME(t|t-1)} + \mathbf{e}_{(t|t-1)} \\
 &\sim N(\mathbf{X}\mathbf{b}_{(t|t-1)}, \mathbf{V}_{(t|t-1)})
 \end{aligned}$$

where  $\mathbf{y}_{(t|t-1)}$  is the conditional phenotype vector;  $\mathbf{b}_{(t|t-1)}$  is the conditional fixed parameter vector for conditional population mean and QTL effects;  $\mathbf{X}$  is the known incidence matrix of the fixed parameters;  $\mathbf{e}_{1(t|t-1)} \dots \mathbf{e}_{E(t|t-1)} \sim N(0, \sigma_{E(t|t-1)}^2 \mathbf{I})$  is the vector of conditional environment effects;  $\mathbf{e}_{2(t|t-1)} \mathbf{e}_{A_1E(t|t-1)} \sim N(0, \sigma_{A_1E(t|t-1)}^2 \mathbf{I})$  is the vector of conditional  $A_1 \times E$  interaction effects;  $\mathbf{e}_{3(t|t-1)} \mathbf{e}_{A_2E(t|t-1)} \sim N(0, \sigma_{A_2E(t|t-1)}^2 \mathbf{I})$  is the vector of conditional  $A_2 \times E$  interaction effects;  $\mathbf{e}_{4(t|t-1)} \mathbf{e}_{AAE(t|t-1)} \sim N(0, \sigma_{AAE(t|t-1)}^2 \mathbf{R}_{AAE})$  is the vector of conditional  $AA \times E$  interaction effects;  $\mathbf{e}_{5(t|t-1)} \mathbf{e}_{M(t|t-1)} \sim N(0, \sigma_{M(t|t-1)}^2 \mathbf{R}_M)$  is

the vector of conditional marker main effects;  $e_{6(t|t-1)} \quad e_{MM(t|t-1)} \sim N(0, \alpha_{MM(t|t-1)}^2 R_{MM})$  is the vector of conditional interaction marker main effects;  $e_{7(t|t-1)} \quad e_{ME(t|t-1)} \sim N(0, \sigma_{MM(t|t-1)}^2 R_{ME})$  is the vector of conditional  $M \times E$  interaction effects;  $e_{8(t|t-1)} \quad e_{MME(t|t-1)} \sim N(0, \sigma_{MME(t|t-1)}^2 R_{MME})$  is the vector of conditional  $MM \times E$  interaction effects;  $e_{9(t|t-1)} \quad e_{(t|t-1)} \sim N(0, \sigma_{(t-1)}^2 \mathbf{I})$  is the vector of conditional residual effects;  $U_u (u=1, 2, \dots, 8)$  is the known incidence matrix of the conditional random effects, and  $U, \mathbf{I}$ .

### Analysis Methodology

With observed phenotypic data at time  $t-1$  ( $y_{(t-1)}$ ) and time  $t$  ( $y_{(t)}$ ), conditional phenotypic data  $y_{(t|t-1)}$  can be obtained via mixed model approaches (Zhu, 1995). Then a mixed-model-based composite interval mapping (MCIM) can be used for mapping QTLs with conditional epistatic effects and QTL  $\times$  environment interaction effects (Zhu, 1998; Zhu and Weir, 1998; Wang et al., 1999). The likelihood function ( $L$ ) for the parameters of conditional fixed effects  $b_{(t|t-1)}$  and conditional variance components [ $\sigma_{u(t|t-1)}^2$ ] is

$$L(b_{(t|t-1)}, V_{(t|t-1)}) = 2^{-\frac{n}{2}} |V_{(t|t-1)}|^{-\frac{1}{2}} \times \exp \left\{ -\frac{1}{2} (y_{(t|t-1)} - Xb_{(t|t-1)})^T V_{(t|t-1)}^{-1} (y_{(t|t-1)} - Xb_{(t|t-1)}) \right\}$$

with the log of the likelihood function ( $l$ )

$$l(b_{(t|t-1)}, V_{(t|t-1)}) = -\frac{n}{2} \ln(2) - \frac{1}{2} \ln |V_{(t|t-1)}| - \frac{1}{2} (y_{(t|t-1)} - Xb_{(t|t-1)})^T V_{(t|t-1)}^{-1} (y_{(t|t-1)} - Xb_{(t|t-1)}).$$

For searching QTL, null hypothesis for genetic parameters (conditional QTL main effects and  $QE$  interaction effects) can be tested by the likelihood ratio statistic ( $LR$ ):

$$LR = 2l_1(\hat{b}_{(t|t-1)1}, V_{(t|t-1)1}) - 2l_0(\hat{b}_{(t|t-1)0}, V_{(t|t-1)0}).$$

The maximum likelihood estimates of QTL effects in  $b_{(t|t-1)}$  can be obtained by



$$\hat{b}_{(t|t-1)} = X^T V_{(t|t-1)}^{-1} X^{-1} X^T V_{(t|t-1)}^{-1} y_{(t|t-1)}$$

with variance-covariance matrix

$$\text{var}(\hat{b}_{(t|t-1)}) = X^T V_{(t|t-1)}^{-1} X^{-1}.$$

Conditional *QE* interaction effects (conditional additive  $\times$  environment interaction  $e_{A_i E(t|t-1)}$  and  $e_{A_j E(t|t-1)}$ , conditional epistasis  $\times$  environment interaction  $e_{AA_{ij} E(t|t-1)}$ ) can be obtained by the best linear unbiased prediction (BLUP) method:

$$\hat{e}_{u(t|t-1)} = \sigma_{u(t|t-1)}^2 U_u^T Q_{(t|t-1)} y_{(t|t-1)}$$

with variance-covariance matrix

$$\text{var}(\hat{e}_{u(t|t-1)}) = \sigma_{u(t|t-1)}^4 U_u^T Q_{(t|t-1)} U_u$$

where  $Q_{(t|t-1)} = V_{(t|t-1)}^{-1} - V_{(t|t-1)}^{-1} X (X^T V_{(t|t-1)}^{-1} X)^{-1} X^T V_{(t|t-1)}^{-1}$ .

## **Originators**

- Wang, D., Zhu, J., Li, Z.K., and Paterson, A.H. (1999). Mapping QTLs with epistatic effects and QTL  $\times$  environment interactions by mixed linear model approaches. *Theoretical and Applied Genetics* 99:1255-1264.
- Zhu, J. (1995). Analysis of conditional effects and variance components in developmental genetics. *Genetics* 141(4):1633-1639.
- Zhu, J. (1998). Mixed model approaches of mapping genes for complex quantitative traits. In Wang, L.Z. and Dai J.R. (Eds.), *Proceedings of Genetics and Crop Breeding of China* (pp.19-20). Chinese Agricultural Science and Technology Publication House, Beijing.
- Zhu, J. and Weir, B.S. (1998). Mixed model approaches for genetic analysis of quantitative traits. In Chen, L.S., Ruan, S.G., and Zhu, J. (Eds.), *Advanced Topics in Biomathematics: Proceedings of International Conference on Mathematical Biology* (pp. 321-330). World Scientific Publishing Co., Singapore.

### ***Software Available***

- Wang, D., Zhu, J., Li, Z.K., and Paterson, A.H. (1999). QTLMapper Version 1.0: A computer software for mapping quantitative trait loci (QTLs) with additive effects, epistatic effects and QTL  $\times$  environment interactions. *User Manual for QTLMapper Version 1.0* (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.
- Zhu, J. (1997). GENCONDI.EXE, a computer software for calculating conditional phenotypic data. *Analysis Methods for Genetic Models* (pp. 278-285), Agricultural Publication House of China, Beijing (program free of charge).



## Chapter 21

# Mapping QTL with Epistatic Effects and QTL-by-Environment Interaction Effects

Jun Zhu

### *Purpose*

To map quantitative trait loci (QTL) with additive, epistatic, and QTL-by-environment interaction effects for doubled haploid (DH) or recombinant inbred line (RIL) populations.

### *Definitions*

#### *Genetic Model*

If multiple-environment data of DH or RIL populations are used for mapping QTL, the phenotypic value of the  $j$ th genetic entry in environment  $h$  can be expressed as shown in the genetic model

$$y_{hj} = \mu + a_1 x_{A_1j} + a_2 x_{A_2j} + aa x_{AAj} + u_{E_{hj}} e_{E_h} + u_{A_1 E_{hj}} e_{A_1 E_h} + u_{A_2 E_{hj}} e_{A_2 E_h} + u_{AAE_{hj}} e_{AAE_h} + u_{M_{fj}} e_{M_f} + u_{MM_{lj}} e_{MM_l} + u_{ME_{hpj}} e_{ME_{hp}} + u_{MME_{hbj}} e_{MME_{hq}} + \epsilon_{bj}$$

where  $\mu$  is the population mean;  $a_1$  and  $a_2$  are the additive effects of loci  $Q_1$  and  $Q_2$ , respectively;  $aa$  is the additive  $\times$  additive epistatic effect of loci  $Q_1$  and  $Q_2$ ;  $x_{A_1j}$ ,  $x_{A_2j}$ , and  $x_{AAj}$  are coefficients of these genetic main effects;  $e_{E_h}$  is the random effect of environment  $h$  with coefficient  $u_{E_{hj}}$ ;  $e_{A_1 E_h}$  (or  $e_{A_2 E_h}$ ) is the additive  $\times$  environment interaction effect with coefficient  $u_{A_1 E_{hj}}$

(or  $u_{A_2E_{hj}}$ ) for  $Q_1$  (or  $Q_2$ );  $e_{AAE_h}$  is the epistasis  $\times$  environment interaction effect with coefficient  $u_{AAE_{hj}}$ ;  $e_{M_f}$  is the marker main effect with coefficient  $u_{M_f}$ ;  $e_{MM_1}$  is the marker  $\times$  marker interaction effect with coefficient  $u_{MM_1}$ ;  $e_{ME_{hp}}$  is the marker  $\times$  environment interaction effect with coefficient  $u_{ME_{hp}}$ ;  $e_{MME_{hq}}$  is the marker  $\times$  marker  $\times$  environment interaction effect with coefficient  $u_{MME_{hq}}$ ; and  $e_{hj}$  is the residual effect.

### *Mixed Linear Model*

The epistatic QTL model can be expressed in matrix form as

$$\mathbf{y} = \mathbf{X}\mathbf{b} + \mathbf{U}_E\mathbf{e}_E + \mathbf{U}_{A_1E}\mathbf{e}_{A_1E} + \mathbf{U}_{A_2E}\mathbf{e}_{A_2E} + \mathbf{U}_{AAE}\mathbf{e}_{AAE} + \mathbf{U}_M\mathbf{e}_M + \mathbf{U}_{MM}\mathbf{e}_{MM} + \mathbf{U}_{ME}\mathbf{e}_{ME} + \mathbf{U}_{MME}\mathbf{e}_{MME} + \mathbf{e}$$

$$\mathbf{X}\mathbf{b} = \mathbf{U}_u\mathbf{e}_u$$

$$\sim N(\mathbf{X}\mathbf{b}, \mathbf{V} = \sigma_u^2 \mathbf{U}_u \mathbf{R}_u \mathbf{U}_u^T)$$

where  $\mathbf{y}$  is the phenotype vector;  $\mathbf{b}$  is the fixed parameter vector for population mean and QTL effects;  $\mathbf{X}$  is the known incidence matrix of the fixed parameters;  $\mathbf{e}_1 = \mathbf{e}_E \sim N(0, \sigma_E^2 \mathbf{I})$  is the vector of environment effects;  $\mathbf{e}_2 = \mathbf{e}_{A_1E} \sim N(0, \sigma_{A_1E}^2 \mathbf{I})$  is the vector of  $A_1 \times E$  interaction effects;  $\mathbf{e}_3 = \mathbf{e}_{A_2E} \sim N(0, \sigma_{A_2E}^2 \mathbf{I})$  is the vector of  $A_2 \times E$  interaction effects;  $\mathbf{e}_4 = \mathbf{e}_{AAE} \sim N(0, \sigma_{AAE}^2 \mathbf{R}_{AAE})$  is the vector of  $AA \times E$  interaction effects;  $\mathbf{e}_5 = \mathbf{e}_M \sim N(0, \sigma_M^2 \mathbf{R}_M)$  is the vector of marker main effects;  $\mathbf{e}_6 = \mathbf{e}_{MM} \sim N(0, \sigma_{MM}^2 \mathbf{R}_{MM})$  is the vector of interaction marker main effects;  $\mathbf{e}_7 = \mathbf{e}_{ME} \sim N(0, \sigma_{ME}^2 \mathbf{R}_{ME})$  is the vector of  $M \times E$  interaction effects;  $\mathbf{e}_8 = \mathbf{e}_{MME} \sim N(0, \sigma_{MME}^2 \mathbf{R}_{MME})$  is the vector of  $MM \times E$  interaction effects;  $\mathbf{e}_9 = \mathbf{e} \sim N(0, \sigma^2 \mathbf{I})$  is the vector of residual effects;  $\mathbf{U}_u (u = 1, 2, \dots, 8)$  is the known incidence matrix of the random effects, and  $\mathbf{U}_9 = \mathbf{I}$ .

### Analysis Methodology

An approach of mixed-model-based composite interval mapping (MCIM) can be constructed for handling epistatic effects and QTL  $\times$  environment interaction effects. The likelihood function ( $L$ ) for the parameters of fixed effects  $b$  and variance components  $[\sigma_u^2]$  is

$$L(b, V) = (2\pi)^{-\frac{n}{2}} |V|^{-\frac{1}{2}} \exp \left\{ -\frac{1}{2} (y - Xb)^T V^{-1} (y - Xb) \right\}$$

with the log of the likelihood function ( $l$ )

$$l(b, V) = -\frac{n}{2} \ln(2\pi) - \frac{1}{2} \ln |V| - \frac{1}{2} (y - Xb)^T V^{-1} (y - Xb).$$

For searching QTL, the null hypothesis for genetic parameters (QTL main effects and Q  $\times$  E interaction effects) can be tested by the likelihood ratio statistic ( $LR$ ):

$$LR = 2l_1(\hat{b}_1, v_1) - 2l_0(\hat{b}_0, v_0).$$

The maximum likelihood estimates of QTL effects in  $b$  can be obtained by

$$\hat{b} = (X^T V^{-1} X)^{-1} X^T V^{-1} y$$

with variance-covariance matrix

$$\text{var}(\hat{b}) = (X^T V^{-1} X)^{-1}.$$

Q  $\times$  E interaction effects (additive  $\times$  environment interaction  $e_{A,E}$  and  $e_{A,E}$ , epistasis  $\times$  environment interaction  $e_{AA,E}$ ) can be obtained by the best linear unbiased prediction (BLUP) method:

$$\hat{e}_u = \sigma_u^2 U_u^T Q y$$

with variance-covariance matrix

$$\text{var}(\hat{e}_u) = \sigma_u^4 U_u^T Q U_u$$

where  $Q = V^{-1} - V^{-1}X(X^T V^{-1}X)^{-1}X^T V^{-1}$ .

### ***Originators***

- Wang, D., Zhu, J., Li, Z.K., and Paterson, A.H. (1999). Mapping QTLs with epistatic effects and QTL  $\times$  environment interactions by mixed linear model approaches. *Theoretical and Applied Genetics* 99:1255-1264.
- Zhu, J. (1998). Mixed model approaches of mapping genes for complex quantitative traits. In Wang, L.Z. and Dai, J.R. (Eds.), *Proceedings of Genetics and Crop Breeding in China* (pp. 19-20). Chinese Agricultural Science and Technology Publication House, Beijing.
- Zhu, J. and Weir, B.S. (1998). Mixed model approaches for genetic analysis of quantitative traits. In Chen, L.S., Ruan, S.G., and Zhu, J. (Eds.), *Advanced Topics in Biomathematics: Proceedings of International Conference on Mathematical Biology* (pp. 321-330). World Scientific Publishing Co., Singapore.

### ***Software Available***

- Wang, D., Zhu, J., Li, Z.K., and Paterson, A.H. (1999). *User Manual for QTLMapper Version 1.0: A Computer Software for Mapping Quantitative Trait Loci (QTLs) with Additive Effects, Epistatic Effects and QTL  $\times$  Environment Interactions* (program free of charge). Contact Dr. Jun Zhu, Department of Agronomy, Zhejiang University, Hangzhou, China. E-mail: <jzhu@zju.edu.cn>.

## ***EXAMPLE***

Data of DH population with ninety-six lines and fifty-four markers on three chromosomes (provided by Drs. N. Huang and P. Wu). Data analysis method is described in detail in the user manual for QTLMapper Version 1.0 (Wang et al., 1999).

Data file (ckge.map) for map information:

```
_Chromosomes 3
_MarkerNumbers 18 15 21
_DistanceUnit cM
```

```
*MapBegin*
Marker#      ch1          ch2          ch3
1             0            0            0
2            19.236       12.9949      7.7618
3            16.2488      5.3402       13.2518
4             4.8552       22.2875      6.9239
5             4.8047       27.7327      9.8037
```

6	15.3881	6.3438	2.7929
7	15.5969	29.4517	17.5239
8	15.0048	10.2825	41.7545
9	3.8375	8.9339	37.3036
10	3.2747	12.824	15.8394
11	34.4392	8.4598	18.7639
12	2.5322	5.1683	2.5121
13	23.7979	10.1262	5.0168
14	8.2644	5.2896	28.9405
15	13.3483	13.2089	1.9109
16	33.5319		22.7256
17	2.5622		15.2455
18	9.2129		32.48
19			7.1483
20			9.4924
21			18.718

\*MapEnd\*

Data file for marker and trait information:

```

_Population DH
_Genotypes 96
_Observations 192
_Environments yes
_Replications no
_TraitNumber 5
_TotalMarker 54
_MarkerCode P1=1 P2=2 F1=3 F1P1=4 F1P2=5

```

\*MarkerBegin\*

Ind	M1	M2	M3	M4	M5	M6	M7	M8	M9	M10	M11	M12	M13	M14	M15	M16	M17	M18	M19	M20	M21	M22	M23	M24	M25	M26	M27
1	2	1	1	1	1	1	1	2	2	2	2	2	2	2	2	1	1	1	2	2	2	2	1	1	2	2	2
2	1	1	1	1	1	1	1	2	2	2	2	1	1	1	1	1	1	1	2	2	2	2	2	2	1	1	1
3	1	1	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	1	2	2	2	1	1	1	1	1	1
4	2	2	2	2	2	2	2	2	2	1	.	1	1	1	2	2	2	2	2	2	2	1	1	2	2	2	2
5	2	2	1	.	1	1	1	2	2	2	2	.	.	2	.	1	1	1	2	2	2	2	.	2	2	2	2
6	1	1	2	2	2	2	2	2	2	1	1	.	1	1	2	2	2	2	2	2	1	1	1	1	1	2	2
7	1	1	2	.	2	2	2	2	2	2	2	2	2	1	1	1	1	1	2	2	2	2	2	2	1	2	2
8	1	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2
9	2	2	2	.	2	2	2	2	2	2	1	1	1	1	1	1	1	1	2	2	2	2	2	1	1	1	1
10	1	2	2	.	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	2	2	2
11	2	2	2	.	2	2	2	2	2	2	1	1	.	1	2	2	2	2	2	2	2	2	1	1	1	1	1
12	1	1	1	1	1	1	1	1	1	1	1	2	2	2	1	1	1	1	1	2	2	2	2	2	2	2	1
13	2	2	.	2	2	2	2	2	2	2	2	2	.	1	1	1	1	2	2	2	2	2	2	2	2	2	2
14	2	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	2	2	1	1	2	1	1	1	2	2	2
15	2	2	2	2	2	2	2	2	2	2	2	1	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2
16	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	2	2	2	2	2
17	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2	2
18	1	1	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	2	2	2	2	2	1	1	1	1	1
19	1	1	.	1	1	1	1	2	2	2	1	.	.	2	2	1	1	1	1	1	.	2	.	2	1	1	1
20	1	1	2	2	2	2	2	2	2	2	2	2	2	2	1	2	2	2	2	2	2	2	1	1	2	2	2
21	2	2	2	2	2	1	2	2	2	2	2	2	2	2	2	1	1	1	2	2	2	2	1	1	1	2	2
22	1	2	2	2	2	2	1	1	1	1	1	.	1	1	1	1	1	1	1	2	2	2	2	2	2	1	1
23	1	1	1	.	1	2	2	2	2	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	2	2	2
24	2	2	2	.	.	2	2	2	1	2	1	1	1	1	2	2	1	2	1	1	1	.	2	2	2	2	.
25	2	2	2	2	2	2	2	2	2	2	1	1	.	1	1	1	1	1	1	1	1	1	1	1	2	2	2





83	1	1	2	2	2	2	2	2	2	2	2	2	2	2	1	.	.	1	1	2	2	2	1	2	2	1	1	1	2	2	2	
84	1	1	1	1	1	2	2	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	2	2
85	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	2	2	2	2	2	2	2	2	1	1	
86	2	2	2	1	1	1	2	2	2	2	2	2	2	2	2	2	2	1	1	1	2	2	2	2	2	2	2	2	2	2	2	
87	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	.	.	2	2	2	2	2	2	2	1	1	1	1	1	1	
88	1	1	1	1	1	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	
89	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	2	2	2	2	1	1	1	2	2	2		
90	1	1	2	.	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	.	2	2	2	2		
91	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	.	1	2	2	2		
92	2	2	2	.	2	2	2	2	.	2	1	1	.	2	.	2	2	2	1	1	1	1	1	1	.	2	2	2	2	2		
93	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	.	2	2	2	1	1	1	1	1	1	1	1	1	1	1		
94	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	2	2		
95	1	1	1	1	1	2	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	2	2	2		
96	1	1	1	1	1	1	1	2	2	.	2	2	1	1	1	1	1	1	1	2	2	.	2	2	2	2	2	1	1	1		

M28	M29	M30	M31	M32	M33	M34	M35	M36	M37	M38	M39	M40	M41	M42	M43	M44	M45	M46	M47	M48	M49	M50	M51	M52	M53	M54		
2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	2	1	1	1	1	1	1	1	2	2	.	2	;	
1	1	1	1	1	1	2	1	1	1	1	1	2	2	1	1	1	1	1	1	1	1	1	1	1	1	1	;	
1	1	1	1	1	.	1	1	1	1	1	1	2	2	2	.	2	2	2	2	2	2	2	2	2	.	2	;	
1	2	2	2	2	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	.	2	;		
2	.	.	2	.	1	.	2	2	.	2	2	.	2	2	1	2	.	2	2	2	2	2	.	2	.	1	;	
1	1	1	1	1	.	2	2	2	2	2	2	2	1	2	2	2	2	2	1	1	1	.	1	1	.	1	;	
2	2	2	2	2	2	1	1	1	2	2	2	2	1	1	2	1	1	1	1	1	1	1	.	1	1	.	1	;
2	2	2	1	2	1	1	1	2	2	2	2	2	2	.	2	2	2	1	1	1	1	1	1	2	2	2	;	
1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	1	2	2	2	2	2	1	1	1	1	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	2	2	;	
1	1	1	1	1	1	1	1	1	1	1	1	2	1	1	2	1	1	1	1	1	1	1	1	1	1	1	;	
2	2	2	1	1	1	1	1	1	2	2	2	2	2	1	1	2	1	1	1	2	1	1	1	1	1	1	;	
1	1	1	1	1	1	2	2	2	2	2	2	2	2	1	1	.	1	1	1	2	2	2	2	1	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	.	2	2	2	2	2	2	2	2	1	1	;	
1	1	1	1	1	1	1	1	1	1	1	1	2	1	.	1	1	1	1	1	1	1	1	1	1	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	.	2	2	2	2	2	2	2	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	.	1	1	1	1	2	2	1	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	;	
1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	;	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	;	
1	.	1	1	1	1	2	2	2	2	2	2	1	.	1	1	1	1	1	1	1	2	2	2	.	2	.	;	
1	1	1	2	2	2	1	1	1	2	2	2	2	1	1	1	1	1	1	1	2	2	2	2	1	1	1	;	
2	2	2	.	2	.	1	1	1	1	.	1	2	1	1	1	1	1	1	1	2	2	2	2	2	.	2	;	
1	2	1	1	2	2	2	2	2	2	2	2	2	1	1	.	1	1	2	2	2	2	2	2	2	2	2	;	
1	.	1	1	1	1	1	1	1	.	2	2	2	.	1	1	1	1	1	2	2	2	.	2	2	.	1	;	
1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	1	2	2	.	2	;	
1	2	2	2	2	2	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	;	
2	2	2	2	2	.	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	;	
1	1	1	1	1	1	1	2	2	2	2	1	1	1	1	1	1	1	.	1	1	1	2	2	.	2	;		
1	1	1	1	1	1	1	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	2	2	;	



\*TraitBegin\*

Env#	Ind#	SH5 ;	Env#	Ind#	SH5 ;	Env#	Ind#	SH5 ;	Env#	Ind#	SH5 ;
1	1	52.5 ;	1	49	77.6 ;	2	1	43.8 ;	2	49	66.7 ;
1	2	62.5 ;	1	50	50.4 ;	2	2	39.5 ;	2	50	50.1 ;
1	3	77.9 ;	1	51	60.0 ;	2	3	57.8 ;	2	51	56.7 ;
1	4	57.2 ;	1	52	68.6 ;	2	4	44.9 ;	2	52	56.4 ;
1	5	51.7 ;	1	53	58.0 ;	2	5	41.9 ;	2	53	53.3 ;
1	6	62.5 ;	1	54	67.2 ;	2	6	44.2 ;	2	54	58.4 ;
1	7	56.0 ;	1	55	65.2 ;	2	7	46.8 ;	2	55	60.1 ;
1	8	62.7 ;	1	56	66.7 ;	2	8	51.4 ;	2	56	57.2 ;
1	9	62.1 ;	1	57	67.1 ;	2	9	46.4 ;	2	57	53.1 ;
1	10	76.2 ;	1	58	59.6 ;	2	10	65.6 ;	2	58	54.9 ;
1	11	69.1 ;	1	59	67.5 ;	2	11	53.0 ;	2	59	56.0 ;
1	12	68.4 ;	1	60	67.7 ;	2	12	58.4 ;	2	60	52.6 ;
1	13	45.4 ;	1	61	60.3 ;	2	13	40.2 ;	2	61	52.0 ;
1	14	68.4 ;	1	62	70.9 ;	2	14	59.1 ;	2	62	57.0 ;
1	15	83.9 ;	1	63	78.8 ;	2	15	67.7 ;	2	63	65.0 ;
1	16	81.5 ;	1	64	70.9 ;	2	16	67.7 ;	2	64	59.0 ;
1	17	74.4 ;	1	65	52.2 ;	2	17	63.7 ;	2	65	46.3 ;
1	18	73.9 ;	1	66	70.7 ;	2	18	68.0 ;	2	66	55.3 ;
1	19	58.7 ;	1	67	66.3 ;	2	19	48.7 ;	2	67	58.4 ;
1	20	64.5 ;	1	68	55.0 ;	2	20	51.8 ;	2	68	48.9 ;
1	21	61.2 ;	1	69	75.3 ;	2	21	49.9 ;	2	69	59.6 ;
1	22	48.5 ;	1	70	75.5 ;	2	22	41.1 ;	2	70	56.8 ;
1	23	48.2 ;	1	71	57.5 ;	2	23	34.1 ;	2	71	43.4 ;
1	24	83.5 ;	1	72	49.7 ;	2	24	71.4 ;	2	72	42.5 ;
1	25	55.2 ;	1	73	75.5 ;	2	25	44.6 ;	2	73	66.5 ;
1	26	49.6 ;	1	74	52.5 ;	2	26	47.0 ;	2	74	40.1 ;
1	27	77.3 ;	1	75	64.6 ;	2	27	62.3 ;	2	75	57.3 ;
1	28	78.5 ;	1	76	57.2 ;	2	28	60.8 ;	2	76	52.8 ;
1	29	71.0 ;	1	77	52.1 ;	2	29	64.1 ;	2	77	43.4 ;
1	30	67.2 ;	1	78	53.9 ;	2	30	62.3 ;	2	78	46.8 ;
1	31	80.9 ;	1	79	72.0 ;	2	31	67.6 ;	2	79	63.1 ;
1	32	88.4 ;	1	80	70.0 ;	2	32	77.3 ;	2	80	57.8 ;
1	33	79.2 ;	1	81	52.3 ;	2	33	66.1 ;	2	81	43.2 ;
1	34	77.1 ;	1	82	55.5 ;	2	34	58.6 ;	2	82	43.3 ;
1	35	72.7 ;	1	83	63.7 ;	2	35	57.9 ;	2	83	48.3 ;
1	36	78.6 ;	1	84	62.1 ;	2	36	60.3 ;	2	84	57.5 ;
1	37	65.1 ;	1	85	61.0 ;	2	37	55.1 ;	2	85	50.2 ;
1	38	48.8 ;	1	86	71.8 ;	2	38	44.3 ;	2	86	59.9 ;
1	39	65.5 ;	1	87	76.6 ;	2	39	47.1 ;	2	87	58.6 ;
1	40	79.3 ;	1	88	55.4 ;	2	40	71.4 ;	2	88	44.1 ;
1	41	81.8 ;	1	89	60.9 ;	2	41	70.1 ;	2	89	43.6 ;
1	42	63.8 ;	1	90	58.9 ;	2	42	57.4 ;	2	90	44.7 ;
1	43	96.6 ;	1	91	44.4 ;	2	43	76.0 ;	2	91	37.0 ;
1	44	67.2 ;	1	92	73.6 ;	2	44	56.7 ;	2	92	56.3 ;
1	45	55.5 ;	1	93	73.8 ;	2	45	46.1 ;	2	93	63.6 ;
1	46	44.2 ;	1	94	82.4 ;	2	46	28.3 ;	2	94	69.8 ;
1	47	80.1 ;	1	95	53.7 ;	2	47	67.7 ;	2	95	41.8 ;
1	48	75.9 ;	1	96	64.2 ;	2	48	66.7 ;	2	96	55.4 ;

\*TraitEnd\*

How to use the software:

1. Run QTLMAPPER.EXE to analyze QTL positions and effects. First create two files: one is a map file (ckge.map) and the other is a marker and trait file (ckge.txt). Choose run from submenu and map epistatic QTL.
2. After finishing the general analysis, choose output submenu and screen putative additive-effect QTL or epistatic QTL. The results are presented in Output 1.
3. Run jackknife test in output submenu for detecting significant additive and epistatic effects. The results are presented in Output 2.

### ***Output 1 for Contribution of QTL Effects***

```
// Result file created by QTLMapper V 1.0
// Data file name:      D:\QTLSOURCE\ckge.txt
// Marker map file name: D:\QTLSOURCE\ckge.map
// Environments:       yes
// Replications:       no
// Contents: relative contributions (H^2) for putative main-effect
//                  QTLs/epistatic QTLs
// Calculations based on: D:\QTLSOURCE\ckge.jke
// BGV control method: A (control marker main & interaction ef-
//                  fects)
# Date: 2000-07-04      Time: 14:05:56
```

```
Trait 1: SH5
Ch-Inj  Int.Namei  Sitei(M)  Ch-Inj  Int.Namej  Sitej(M)  H^2(Ai)  H^2(Aj)  H^2(AAij)  H^2(AEi)  H^2(AEj)  H^2(AAEij)
1-5    M5-M6    0.00     1-17   M17-M18   0.04     0.0000  0.0714  0.0000    0.0000  0.0001  0.0000
1-9    M9-M10   0.00     1-15   M15-M16   0.12     0.0000  0.2532  0.0000    0.0000  0.0001  0.0011
2-6    M24-M25  0.28     3-18   M51-M52   0.06     0.0000  0.0727  0.0000    0.0000  0.0001  0.0000
2-9    M27-M28  0.02     3-16   M49-M50   0.00     0.0625  0.0000  0.0000    0.0000  0.0001  0.0000
```

General contributions:

```
Additive (A): H^2 (A)=0.6131;   Epistasis: H^2 (AA)=0.0000
QE Interactions: H^2 (AE)=0.0003; H^2 (AAE)=0.0011
```

End

### ***Output 2 for QTL A and AA Effects***

```
// Result file created by QTLMapper V 1.0
// Data file name:      D:\QTLSOURCE\ckge.txt
// Marker map file name: D:\QTLSOURCE\ckge.map
// Environments:       yes
// Replications:       no
// Contents: Jackknife test results for epistatic QTLs
// Jackknife based on: D:\QTLSOURCE\ckge.fle
// BGV control method: A (control marker main & interaction effects)
// Threshold probability: 0.005000
```

```
# Date: 2000-07-04 Time: 13:48:12
```

```
Trait 1: SH5
```





## Chapter 22

# Gene Segregation and Linkage Analysis

Jinsheng Liu  
Todd C. Wehner  
Sandra B. Donaghy

### *Purpose*

To calculate single-gene goodness-of-fit testing to analyze gene linkage relationships, including calculations of chi-square, probability value, and two-locus-combined phases, for all gene pairs in segregation for the  $F_2$ ,  $BC_{1P1}$ , and  $BC_{1P2}$  generations. Recombination frequency and standard error are calculated according to the linkage phase.

### *Genetic Analysis*

Linkage is estimated using the chi-square method, a widely used standard for genetic data analysis (although it may produce inaccurate results in some cases). Recombination frequency (RF) and standard error (SE) are calculated according to phase (coupling or repulsion), using the following formulas (Sinnott and Dunn, 1939; Weir, 1994).

### *Definitions*

$F_2$  (repulsion):

$$RF = \frac{p}{\sqrt{\frac{-(bc - ad) + \sqrt{(bc - ad)^2 + ad(bc - ad)}}{(bc - ad)}}}$$



F<sub>2</sub> (coupling):

$$RF = 1 - p$$

$$SE = \sqrt{(1 - p^2)(2 - p^2) / 2n(1 - 2p^2)}$$

BC<sub>1</sub> (only coupling accepted):

$$RF = (b - c) / n$$

$$SE = \sqrt{RF(1 - RF) / n}$$

where  $a$  ( $A\_B\_$ ),  $b$  ( $A\_bb$ ),  $c$  ( $aaB\_$ ) and  $d$  ( $aabb$ ) are genotype segregation ratios in F<sub>2</sub> or BC<sub>1</sub>.

### ***Originators***

Sinnott, E.W. and Dunn, L.C. (1939). *Principles of Genetics*. McGraw-Hill, New York.  
Weir, B.S. (1994). *Genetic Data Analysis: Methods for Discrete Population Data*.  
Sinauer, Sunderland, MA.

### ***Software Available***

Files can be found on the World Wide Web at <<http://cuke.hort.ncsu.edu/cucurbit/Wehner/software.html>>. Or, send a 3.5" floppy disk to Todd C. Wehner, Department of Horticultural Science, North Carolina State University, Raleigh, NC 27695-7609.

### ***Publication***

Liu, J.S., Wehner, T.C., and Donaghy, S.B. (1997). SASGENE: A SAS computer program for genetic analysis of gene segregation and linkage. *Journal of Heredity* 88: 253-254.

### ***Some References Using the Software***

Wehner, T.C., Liu, J.S., Staub, J.E., and Fazio, G. (2003). Segregation and linkage of 14 loci in cucumber. *Journal of American Society of Horticulture Science*.

### ***Contact***

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**Revisions That Have Been Made**

SASGene1.0 and 1.1 had an error in the formula for calculation of SE for RF in coupling. F<sub>2</sub> (coupling):

$$RF = 1-p$$

$$SE = \frac{\sqrt{(1-p^2)(1-p^2)/2n(1-2p^2)}}{1-2p^2}$$

SASGene1.2 has been corrected F<sub>2</sub> (coupling):

$$RF = 1-p$$

$$SE = \frac{\sqrt{(1-p^2)(2-p^2)/2n(1-2p^2)}}{1-2p^2}$$

**EXAMPLE**

Data to be analyzed:

Plot	Rep	Fam	Gen	Plnt	Bi	Rc	Dv	Sp	Ll	Df	F	B	D	U	Tu
1	1	28	1	1	B	N	N	N	L	N	M	W	D	N	W
2	1	28	1	2	B	N	N	N	L	N	M	W	D	N	W
3	1	28	1	3	B	N	N	N	L	N	M	W	D	N	W
4	1	28	1	4	B	N	N	N	L	N	M	W	D	N	W
5	1	28	1	5	B	N	N	N	L	N	M	W	D	N	W
6	1	28	2	1	N	N	N	N	N	D	G	W	D	U	S
7	1	28	2	2	N	N	N	N	N	D	G	W	S	U	S
8	1	28	2	3	N	N	N	N	N	D	G	W	S	U	S
9	1	28	2	4	N	N	N	N	N	D	G	W	S	U	S
10	1	28	2	5	N	N	N	N	N	D	G	W	S	U	S
11	1	28	3	1	B	N	N	N	N	N	G	W	D	N	W
12	1	28	3	2	B	N	N	N	N	N	G	W	D	N	W
13	1	28	3	3	B	N	N	N	N	N	G	W	D	N	W
14	1	28	3	4	B	N	N	N	N	N	G	W	D	N	W
15	1	28	3	5	B	N	N	N	N	N	M	W	D	N	W
16	1	28	3	6	B	N	N	N	N	N	G	W	D	N	W
17	1	28	4	1	B	.	N	N	N	D	G	W	D	U	S
18	1	28	4	2	N	.	N	N	L	D	G	W	.	U	S
19	1	28	4	3	B	N	N	N	N	D	0	W	.	U	S
20	1	28	4	4	B	N	N	N	N	N	G	W	D	N	W
21	1	28	4	5	B	N	N	N	N	N	M	W	D	N	W
22	1	28	4	6	B	N	N	N	N	N	G	W	D	N	W
23	1	28	4	7	B	N	N	N	L	N	G	W	D	N	W
24	1	28	4	8	B	N	N	N	N	N	G	W	D	U	W
25	1	28	4	9	B	N	N	N	N	D	G	W	D	N	W
26	1	28	4	10	N	N	N	N	N	D	G	W	D	U	S
27	1	28	4	11	N	N	N	N	N	N	G	W	D	N	W

28	1	28	4	12	B	N	N	N	N	N	G	W	D	N	W
29	1	28	4	13	B	N	N	N	L	N	G	W	D	.	W
30	1	28	4	14	N	3	N	N	N	N	G	W	D	N	W
31	1	28	4	15	B	N	N	N	N	N	G	W	D	N	W
32	1	28	4	16	N	N	N	N	N	N	G	W	D	N	W
33	1	28	4	17	B	N	.	.	.	.	.	.	.	.	.
34	1	28	4	18	B	N	.	.	.	.	.	.	.	.	.
35	1	28	5	1	B	N	N	N	L	N	G	W	D	N	W
36	1	28	5	2	B	N	N	N	N	N	G	W	D	N	W
37	1	28	5	3	B	N	N	N	L	N	M	W	D	N	W
38	1	28	5	4	B	N	N	N	L	N	M	W	D	N	W
39	1	28	5	5	B	N	N	N	N	N	G	W	D	N	W
40	1	28	5	6	B	N	N	N	N	N	G	W	D	N	W
41	1	28	5	7	B	N	N	N	L	N	M	W	D	N	W
42	1	28	5	8	B	N	N	N	N	N	G	W	D	N	W
43	1	28	5	9	B	N	N	N	L	N	G	W	D	N	W
44	1	28	6	1	B	N	N	N	N	N	G	W	D	N	S
45	1	28	6	2	B	N	N	N	N	D	G	W	D	U	S
46	1	28	6	3	N	N	N	N	N	D	G	W	D	U	S
47	1	28	6	4	B	N	N	N	N	D	G	W	D	U	S
48	1	28	6	5	N	N	N	N	N	D	G	W	D	U	S
49	1	28	6	6	N	N	N	N	N	D	G	W	D	U	S
50	1	28	6	7	N	N	N	N	N	D	G	W	D	U	S
51	1	28	6	8	N	N	N	N	N	N	G	W	D	N	W
52	1	28	6	9	N	N	N	N	N	N	G	W	D	N	W
53	1	28	1	1	B	N	N	N	L	N	M	W	D	N	W
54	1	28	1	2	B	N	N	N	L	N	M	W	D	N	W
55	1	28	1	3	B	N	N	N	L	N	M	W	D	N	W
56	1	28	1	4	B	N	N	N	L	N	M	W	D	N	W
57	1	28	1	5	B	N	N	N	L	N	M	W	D	N	W
58	1	28	2	1	N	N	N	N	N	D	G	W	S	U	S
59	1	28	2	2	N	N	N	N	N	D	G	W	S	U	S
60	1	28	2	3	N	N	N	N	N	D	G	W	S	U	S
61	1	28	2	4	N	N	N	N	N	D	G	W	S	U	S
62	1	28	2	5	N	N	N	N	N	D	G	W	S	U	S
63	1	28	3	1	B	N	N	N	N	N	G	W	D	N	W
64	1	28	3	2	B	N	N	N	N	N	G	W	D	N	W
65	1	28	3	3	B	N	N	N	N	N	G	W	D	N	W
66	1	28	3	4	B	N	N	N	N	N	G	W	D	N	W
67	1	28	3	5	B	N	N	N	N	N	G	W	D	N	W
68	1	28	3	6	B	N	N	N	N	N	G	W	D	N	W
.															
.															
.															
469	5	30	1	1	N	R	N	S	N	N	M	B	D	U	W
470	5	30	1	2	N	R	N	S	N	N	M	B	D	N	W
471	5	30	1	3	N	R	N	S	N	N	M	B	D	N	W
472	5	30	1	4	N	R	N	S	N	N	G	B	D	N	W
473	5	30	1	5	N	R	N	S	N	N	G	B	D	U	W
474	5	30	2	1	N	N	N	N	N	N	G	W	S	U	S
475	5	30	2	2	N	N	N	N	N	D	G	W	S	U	W
476	5	30	2	3	N	N	N	N	N	D	G	W	S	U	S
477	5	30	2	4	N	N	N	N	N	N	G	W	S	U	S
478	5	30	2	5	N	N	N	N	N	D	G	W	S	U	S
479	5	30	3	1	B	N	N	N	N	D	M	B	D	N	W
480	5	30	3	2	B	N	N	N	N	N	G	B	D	N	W
481	5	30	3	3	B	N	N	N	N	D	G	B	D	N	W

482	5	30	3	4	B	N	N	N	N	D	G	B	D	N	W
483	5	30	3	5	B	N	N	N	N	N	G	B	D	N	W
484	5	30	3	6	B	N	N	N	N	D	G	B	D	N	W
485	5	30	4	1	B	N	N	N	N	N	G	B	D	N	W
486	5	30	4	2	B	N	N	N	N	N	G	W	D	U	S
487	5	30	4	3	N	R	N	S	N	N	G	W	D	U	W
488	5	30	4	4	B	N	N	N	N	D	G	B	S	U	W
489	5	30	4	5	B	N	N	N	N	D	G	B	S	U	W
490	5	30	4	6	B	N	N	N	N	N	G	B	D	N	W
491	5	30	4	7	B	N	N	N	N	N	G	W	D	U	S
492	5	30	4	8	B	N	N	N	N	D	G	B	D	N	W
493	5	30	4	9	N	N	N	N	N	N	G	W	D	N	S
494	5	30	4	10	N	N	N	N	N	D	G	B	D	N	S
495	5	30	4	11	B	N	N	N	N	N	G	B	D	N	W
496	5	30	4	12	B	N	N	N	N	D	G	B	D	U	S
497	5	30	4	13	B	N	N	N	N	D	G	W	S	U	W
498	5	30	4	14	B	N	N	N	N	D	G	B	D	N	W
499	5	30	4	15	N	N	N	N	N	N	G	B	D	N	W
500	5	30	4	16	N	N	N	N	N	N	G	W	D	U	S
501	5	30	4	17	N	N	N	N	N	N	G	B	D	N	W
502	5	30	4	18	N	N	N	N	N	N	G	B	D	N	W
503	5	30	5	1	B	N	N	N	N	D	G	B	D	N	W
504	5	30	5	2	N	R	N	S	N	N	G	B	D	U	W
505	5	30	5	3	B	N	N	N	N	D	N	B	D	U	W
506	5	30	5	4	N	R	N	S	N	N	M	.	.	.	.
507	5	30	5	5	B	N	N	N	N	N	G	B	D	N	W
508	5	30	5	6	B	N	N	N	N	D	G	B	D	N	W
509	5	30	5	7	B	N	N	N	N	N	G	B	D	N	W
510	5	30	5	8	B	R	N	S	N	N	M	B	D	N	W
511	5	30	5	9	N	R	N	S	N	N	M	.	.	.	.
512	5	30	6	1	B	N	N	N	N	D	G	B	D	N	W
513	5	30	6	2	N	N	N	N	N	D	G	B	D	U	S
514	5	30	6	3	B	N	N	N	N	D	G	B	D	U	W
515	5	30	6	4	B	N	N	N	N	D	G	W	D	U	S
516	5	30	6	5	N	N	N	N	N	D	G	B	D	N	W
517	5	30	6	6	B	N	N	N	N	D	G	W	D	N	W
518	5	30	6	7	N	N	N	N	N	D	G	W	D	U	W
519	5	30	6	8	N	N	N	N	N	D	M	W	D	U	S
520	5	30	6	9	B	N	N	N	N	D	G	W	D	N	S
.															
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## SAS Program (Five Files)

### File 1: readme.txt

SASGENE 1.1  
 Program for Analysis of  
 Gene Segregation and Linkage  
 November 5, 1997

### Instructions for Running SASGENE Macros

The SASGENE program for gene segregation and linkage analysis is written in SAS macro language. There are four SAS files. Three are macro files and one is an example. The first macro, SGENE, is for single-gene goodness-of-fit tests. The second macro, LINKAGE, is for analysis of gene linkage relationships. The third macro, CONVERT, is optional and converts gene values to “D” for dominant and “R” for recessive. STARTUP.SAS illustrates how to use the macros. The STARTUP.SAS file can easily be modified for other experiments of interest to the user.

The macros are written for version six and later versions of SAS. The amount of disk space required increases as the number of genes for the linkage analysis increases.

To use the macros, the user must create an input data file that will record data for the following fields: plot number, replication number, plant number, family number, generation number, and gene (or trait) names. Note that plot number, replication number, and plant number are used only for collecting data and are not used by the program for computing statistics. The user may specify any value for the family variable, but the macro requires values of 1, 2, 3, 4, 5, or 6 for the GNR (generation) variable (1 for P1, 2 for P2, 3 for F1, 4 for F2, 5 for BC1P1, 6 for BC1P2). Valid SAS variable names are used for the gene names. The genes (or traits) are variables (columns) and their values are observations (rows). Family and generation are identification variables. In the data file, the values of P1, P2, and F1 should not be omitted or the results may be incorrect.

The SGENE and LINKAGE macros require gene values to be coded as “D” for dominant, “R” for recessive, and “.” or blank for a missing value. An optional macro, CONVERT, converts the original gene values to “D,” “R,” or missing. For each gene and family, the most frequent value for F1 is the dominant gene. Any other nonmissing values are treated as recessive, and any missing values are counted as missing.

An example of a SAS data set follows:

```
data orig;
  input PLOT REP FAMILY GNR BI $ RC $ DV $ SP $
  LL $ DF $ F $ B $ D $ U $ TU $;
  cards;
  1 1 20 1 N R N S N N M B D N W
  2 1 20 1 N R N S N N M B D N W
  3 1 20 1 N R N S N N M B D N W
  4 1 20 1 N R N S N N M B D N W
  .
  .
run;
```

Either the macro code or a %INCLUDE (also known as %INC) statement is needed to define the macro to the SAS system. The user may include the macro into the program editor or use a %INC statement, such as %inc 'sgene.sas'. The %INC statement specifies the physical name of the external file where the macro is stored. The physical name is the name by which the host system recognizes the file. Depending on the host system and location of the file, the entire file name may need to be specified.

Examples:

```
%inc 'c:\mysas\sgene.sas';
%inc '~/sasmacro/sgene.sas';
```

The file, SGENE.SAS, contains the SAS macro, SGENE. File names, such as SGENE.SAS, usually carry the *sas* extension if the file is a SAS program or a SAS macro.

Once the macro is defined to SAS, the macro can be invoked. To invoke the macro, specify the %, the macro name (either SGENE, LINKAGE, or CONVERT), and the required parameters in parenthesis.

The SGENE macro has three parameters:

- DS—name of the SAS data set to analyze
- GENES—gene names from the SAS data set
- P1—critical value for about half of the frequency of one parent to determine the expected segregation ratio (1:1 or 1:0) in BC1 generation

Example:

```
%sgene (ds=new,
        genes=BI RC DV SP LL DF F B D U TU,
        p1=9);
```

The linkage macro has four parameters:

- DS—name of the SAS data set to analyze
- GENES—gene names from the SAS data set
- P1, P2—critical value for about half of the frequency of the parents to determine if the phase is coupling or repulsion

**Example:**

```
%linkage (ds=new,
          genes=BI RC DV SP LL DF F  B D U TU,
          p1=9,
          p2=9);
```

The convert macro has three parameters:

**DS**—name of the SAS data set to convert  
**GENES**—list of the desired gene names from the SAS data set  
**DSOUT**—name of the SAS data set after conversion

**Example**

```
%convert (ds=orig,
          genes=BI RC DV SP LL DF F  B D U TU,
          dsout=new);
```

Several additional files are stored in the same location as the introduction:

**STARTUP.SAS**—example that illustrates how to use the macros  
**ORIG.DAT**—sample data for the startup.sas file  
**CONVERT.SAS**—file that contains the SAS macro convert  
**SGENE.SAS**—file that contains the SAS macro sgene  
**LINKAGE.SAS**—file that contains the SAS macro linkage

*File 2: STARTUP.SAS*

```
*****
*
* SASGENE 1.1
* Program for Analysis of
* Gene Segregation and Linkage
* November 5, 1997
*
* Example of Invoking SASGENE macros
*
*****;

*****
*
* Specify file names and include macros.
*
* 1. Specify the name of the file where the data are stored.
* The name is enclosed in single quotes.
```

```

*      example: filename in 'orig.dat' ;
*
* 2.  Include the macros with the %INCLUDE (%inc) statement.
*      Specify the physical name of the external file where the macro
*      is stored. The physical name is enclosed in single quotes.
*      example: %inc 'convert.sas';
*               %inc 'sgene.sas';
*               %inc 'linkage.sas';
*
*      Summary:
*      The user only needs to change the information inside the
*      quotes on the FILENAME and %INCLUDE statements below.
*      The information inside the quotes specifies the name of the
*      external file where the data or macros are stored. It may be
*      necessary to specify the entire file name inside the quotes.
*      example: %inc 'c:\sasmacro\convert.sas';
*****;

filename in 'example.dat'; /* name and location of data file */
%inc 'convert.sas'; /* name and location of SAS macro CONVERT */
%inc 'sgene.sas'; /* name and location of SAS macro SGENE */
%inc 'linkage.sas'; /* name and location of SAS macro LINKAGE */

*****
*      include any desired titles and options
*****;
title 'Cucumber Gene Linkage Example';
options nodate pageno=1;
options linesize=80 pagesize=500;

*****
*      Create SAS dataset
*      The user will need to modify the INPUT statement to specify
*      the gene names from their experiment. If list input is used,
*      then missing values should be coded with a "."
*
*      Macros are expecting the following variable names:
*      family = family code
*      gnr     = generation code
*
*      Macros are expecting the following values for GNR variable:
*      1 for P1
*      2 for P2
*      3 for F1
*      4 for F2
*      5 for BC1P1
*      6 for BC1P2
*
*      P1, P2 and F1 generations must be included
*      for program to run (1 plant each is sufficient)
*****;
data original;
  infile in missover pad; /* MISSOEVER & PAD are options on INFILE */
  input plot rep family gnr plnt bi $ rc $ dv $ sp $ ll $ df $
        f $ b $ d $ u $ tu $ ;
run;

```





```
genes=BI RC DV SP LL DF F B D U TU,
p1=9,
p2=9);
```

### File 3: CONVERT.SAS

```
*****
*
* SASGENE 1.1
* Program for Analysis of
* Gene Segregation and Linkage
* November 5, 1997
*
*****;

%macro convert
(ds=_last_, /* SAS dataset to analyze(default:uses last one)*/
genes=, /* gene variable names */
dsout= /* name of new SAS dataset after conversion */
);

*****
* Name: CONVERT
*
* Purpose: Converts gene values to Dominant or Recessive
*
* Written: 09/14/95
*
* Modified: 10/02/95
* 03/05/97
*
* Products: Base SAS
*
* Example: %convert(ds=save.orig,
genes=BI RC DV SP LL DF F B D U TU SS NS,
dsout=new);
*****;

proc format;
value _gnrx
1='P1'
2='P2'
3='F1'
4='F2'
5='BC1P1'
6='BC1P2'
;
run;

title2 'Gene Segregation and Linkage Analysis';
%local nogene word geneid i;

/* create nogenes macro variable */
/* nogenes is the number of genes listed in &genes */
%let nogenes=0;
%if &genes ne %then %do;
%let word=%scan(&genes,1);
```

```

%do %while (&word ne );
    %let nogenes=%eval(&nogenes+1);
    %let word=%scan(&genes,&nogenes+1);
    %end;
/* create geneid macro variable */
/* geneid is the names of the genes in quotes */
/* used in array for identification in output */
%let word=%scan(&genes,1);
%let geneid=%str('%&word%');
%do i=2 %to &nogenes;
    %let word=%scan(&genes,&i);
    %let geneid=%str(&geneid,'%&word%');
%end;

proc sort data=&ds out=_orig; by family; run;
data _generat; set _orig;
    length id 3;
    array y{*} &genes;
    array yc{*} $ n1-n&nogenes (%unquote(&geneid));
    id=0;
    do _i_=1 to dim(y);
        id+1;
        code= y{ _i_ };
        gene=yc{ _i_ };
        output;
    end;
    keep family id gene gnr code;
run;
proc sort data=_generat; by family id; run;

proc freq noprint;
    by family id gene;
    where code not=' ';
    tables code / out=_count;
run;
proc means noprint; by family id ;
    var count;
    output out=_nocode n=n;
run;
data _look; merge _count _nocode; by family id;
    if n>2;
run;
proc print label;
title3 'Observed frequencies for each gene locus and allele code';
title4 'These genes in this table have more than 2 codes:';
title5 ' some codes may have been misentered ';
title6 'WARNING!!! Program will convert to 2 codes (D and R)
';
title7 ' Dominant will be assigned,
';
title8 ' other non-missing codes will be set to Recessive
';
var family gene code count;
label count='FREQUENCY';
run;

```

```

/* delete gene-family ids that do not make sense for analysis */
/* delete when the phenotype of P1 is the same as the      */
/* phenotype of P2                                         */
title3 ' ';
proc freq          data=_generat noprint;
  by family id gene;
  tables code*gnr / out=_gnrcode(drop=percent) ;
run;
data _gnrcode; set _gnrcode;
  if code=' ' then delete;
proc sort data=_gnrcode; by family id gene gnr descending count;
run;
data _delete(keep=family id gene); set _gnrcode;
  by family id gene gnr;
  retain d1;
  if first.id then do;
    d1='          ';
    d2='          ';
  end;
  if first.gnr then do;
    if gnr=1 then d1=code;
    else if gnr=2 then do;
      d2=code;
      if d1=d2 then output _delete;
    end;
  end;
run;
proc print data=_delete(drop=id);
  title3 'These gene-family combinations will be deleted ';
  title4 'since the phenotype for P1 and P2 are the same ';
  title5 'and do not fit the assumptions of the analysis.';
run;
data _generat _look; merge _generat _delete(in=yes);
  by family id gene;
  if yes then output _look;
  else output _generat;
run;
proc freq          data=_look;
  by family id gene;
  tables code*gnr / missprint nocum nopercnt norow nocol;
  label gnr='GENERATION';
  format gnr _gnrx.;
run;

/* find the dominant gene by looking at generation 3 (F1) */
title3 ' ';
proc freq noprint data=_generat;
  by family id gene;
  where gnr=3;
  tables code / out=_count;
run;
proc sort; by family id count; run;

data _dom; set _count;
  by family id;

```

```

array c $ c1-c&nogenes;
retain c1-c&nogenes;
length c1-c&nogenes $8;
if first.family then do;
  do _i_=1 to &nogenes;
    c{ _i_ }=' ';
  end;
end;

if last.id then c{id}=code;
if last.family then output;
keep family c1-c&nogenes;
run;

data &dsout; merge _orig _dom;
by family;
array genes{*} &genes;
array dom{*} $ c1-c&nogenes;

do _i_=1 to dim(genes);
  if dom{ _i_ }=' ' then genes{ _i_ }=' ' /*useless data- no domi-
nant*/
  else do;
    if genes{ _i_ }=dom{ _i_ } then genes{ _i_ }='D';
    else if genes{ _i_ }=' ' then genes{ _i_ }=' ';
    else genes{ _i_ }='R';
  end;
end;
drop c1-c&nogenes _i_;
run;

data _check; merge _orig _dom;
by family;
array genes &genes;
array dom $ c1-c&nogenes;
array yc{*} $ n1-n&nogenes (%unquote(&geneid));
id=0;
do _i_=1 to dim(genes);
  id+1;
  gene=yc{ _i_ };
  old_code=genes{ _i_ };
  if dom{ _i_ }=' ' then new_code=' ' /*useless data- no dominant
*/
  else do;
    if genes{ _i_ }=dom{ _i_ } then new_code='D';
    else if genes{ _i_ }=' ' then new_code=' ';
    else new_code='R';
  end;
  output;
end;
drop c1-c&nogenes n1-n&nogenes &genes;
run;

title4 "Conversion to 'D' or 'R' for each gene and family";
proc freq;
  tables id*gene*family*new_code*old_code/list nopercnt nocum
  nofreq;

```

```

run;
proc datasets library=work memtype=data nolist;
  delete _check_count_dom_generat_look_nocode_orig
        _delete_gnrancode;
quit;
%mend convert;

```

#### File 4: SGENE.SAS

```

*****
*
*       SASGENE 1.1
*       Program for Analysis of
*       Gene Segregation and Linkage
*       November 5, 1997
*
*****;

%macro sgene
  (ds=_last_, /* SAS dataset to analyze(default:uses last one)*/
   genes=,    /* gene variable names */
   p1=       /* freq of parent(P1) to determine Dom. or Rec. */
  );

*****
* Name:      SGENE
*
* Purpose:   Single Locus Goodness of Fit Test
*
* Written:   06/22/95
*
* Modified:  10/03/95
*           03/05/97
*
* Example:   %sgene(ds=dst,
*               genes=BI RC DV SP LL DF F B D U TU ,
*               p1=9);
*****;

%local nogene word geneid i;
title2 'Gene Segregation and Linkage Analysis';
title3 'Single Locus Goodness of Fit Test';
title4 'Probability >.05 is accepted as Single Locus';
options missing=' ';
proc format;
  picture _prob
    low-0.05   ='9.999*'
    0.05<-<0.06='9.999 '
    0.06-high  ='9.99  '
    .          ='      '
  ;
  value _gnrx
    1='P1'
    2='P2'
    3='F1'

```

```

4='F2'
5='BC1P1'
6='BC1P2'
;
run;

/* create nogenes macro variable */
/* nogenes is the number of genes listed in &genes */
%let nogenes=0;
%if &genes ne %then %do;
  %let word=%scan(&genes,1);
  %do %while (&word ne );
    %let nogenes=%eval(&nogenes+1);
    %let word=%scan(&genes,&nogenes+1);
  %end;
%end;

/* create geneid macro variable */
/* geneid is the names of the genes in quotes */
/* used in array for identification in output */
%let word=%scan(&genes,1);
%let geneid=%str('%&word%');
%do i=2 %to &nogenes;
  %let word=%scan(&genes,&i);
  %let geneid=%str(&geneid,'%&word%');
%end;

data _gent(keep=id family gnr a gene aa bb ee)
  _look(keep=obs family gnr &genes);
  set &ds;
  length id aa bb ee 3
         obs 4
         a $ 1;
  array y{*} &genes;
  array yc{*} $ n1-n&nogenes (%unquote(&geneid)) ;

/* create an obs. for each gene */
/* a will be the response variable for phenotype of individual */
/* of each gene */
/* gene will be the character id of each gene name */
/* id will be the numeric id of the gene -used for sorting */

  obs+1;
  id=0;
  do _i_=1 to dim(y);
    id+1;
    a=y{_i_}; gene=yc{_i_};
    a=upcase(a);
/* ensure all values are in upper case */
/* if the phenotype is dominant, then aa=1 */
/* if the phenotype is recessive, then bb=1 */
    aa=0; bb=0; ee=0;
    if a ='D' then aa=1;
    else if a ='R' then bb=1;
    else if a =' ' then ee=1;
    else do;

```

```

        put '***** ERROR ***** '
            'Invalid value for gene ' gene
            ' (' gene '='a ') at obs=' obs;
        output _look;
    end;
    output _gent;
end;

run;
/* print any invalid data values for gene to notify user */
title4 'Invalid data value for at least one gene'
      ' (value is not D, R, or missing)';
proc print data=_look;
    id obs;

run;
proc datasets library=work nolist;
    delete _look;
run;

title4 'Probability >.05 is accepted as Single Locus';
/* compute the sums for number of dominant and recessive */
/* individuals in 6 generations */
proc means data=_gent noprint nway;
    class id family gnr;
    id gene;
    var aa bb ee;
    output out =_sum sum=d r missing;
run;

/* compute chi square and probability */
data _chisq; set _sum;
    by id family;
    retain g1 omit;
    if first.family then do;
                                g1=' ';
                                omit='no ';
                                end;
    gltext=' ';

/* determine if the genotype of recurrent parent is dominant or */
/* recessive; this information is needed to choose */
/* expected 1:1 or 1:0 for chisq in BC1 and BC2 */
if gnr =1 then do;
    t=sum(d,r);
    if t<=0 then omit='yes';
    if 0<d<&p1 then g1='REC';
        else if d>=&p1 then g1='DOM';
        else g1=' ';
    end;

if omit='yes' then delete;

if gnr >3 then do;
    t=d+r;
    chisq=0; df=0;

```



```

/* expected is 3:1 for chisq in F2 */
if gnr=4 then do;
  glttext='3:1';
  /*chisq for 3:1 */
  chisq=(d-t*0.75)**2/ (t*0.75) + (r-t*0.25)**2/(t*0.25);
end;

/* choose expected 1:1 or 1:0 for chisq in BC1 and BC2 */
/* according to dominant or recessive recurrent parent */
else if gnr =5 then do;
  if gl='DOM' then do;
    glttext='1:0';
    chisq=((d-t)**2)/ t ;
  end;
  else if gl='REC' then do;
    glttext='1:1';
    chisq=(d-t*0.5)**2/(t*0.5) +
      (r-t*0.5)**2/(t*0.5);
  end;
end;
else if gnr =6 then do;
  if gl='DOM' then do;
    glttext='1:1';
    chisq=(d-t*0.5)**2/(t*0.5) + (r-t*0.5)**2/(t*0.5);
  end;
  if gl='REC' then do;
    glttext='1:0';
    chisq=((d-t)**2)/ t ;
  end;
end;
df=1;
prob=probchi(chisq,df);
prob=1-prob;
end;
drop omit;
drop id _type_ t gl;
run;

proc datasets library=work nolist;
  delete _gent _sum;
run;

proc print noobs label uniform data=_chisq;
  by notsorted gene family;
  pageby gene;
  format chisq 8.2 prob _prob. gnr _gnrx.;
  label gnr='GENERATION';
  label d='DOMINANT';
  label r='RECESSIVE';
  label glttext='EXPECTED';
  label _freq_='N';
run;
%mend sgene;

```

## File 5: LINKAGE.SAS

```

*****
*
*   SASGENE 1.2
*   Program for Analysis of
*   Gene Segregation and Linkage
*   March 2, 1999
*
*
*   linkage.sas of SASGENE 1.2 differs from SASGENE 1.1
*   because there was an error in the calculation of
*   the SE for the F2 (coupling) as follows:
*   in SASGENE 1.1 the formula was:
*       se=( (1-p*p)*(1+p*p)/(2*t*(1+2*p*p)) )**0.5;
*   in SASGENE 1.2 the formula is now:
*       se=( (1-p*p)*(2+p*p)/(2*t*(1+2*p*p)) )**0.5;
*
*****;

%macro linkage
(ds=_last_, /* SAS dataset to analyze(default:uses last one) */
genes=, /* gene variable names */
p1=, /* freq of P1 to determine Coupling or Repulsion */
p2= /* freq of P2 to determine Coupling or Repulsion */
);

*****
* Name: LINKAGE
*
* Purpose: Linkage Analysis for
* Recombination Frequency Data in F2, BC1P1 & BC2P2 Pop.
*
* Written: 06/22/95
*
* Modified: 10/03/95
* 03/05/97
*
* Example: %linkage(ds=dst,
genes=BI RC DV SP LL DF F B D U TU ,
p1=9
p2=9
);
*
* Note: The number of genes listed affects the amount of
time the program takes to execute. The resources for
your platform will determine the number of genes you
can use. Increasing the number of genes increases
the work space that is needed.
*****;

%local genes word geneid i;
title2 'Gene Segregation and Linkage Analysis';
title3 'Recombination Frequency Data in F2, BC1P1 & BC1P2 Population';
title4 'Prob with * indicates gene pair might be linked';
options missing= ' ';

```

```

proc format;
  picture _prob
    low-0.05   ='9.999*'
    0.05<-<0.06='9.999 '
    0.06-high  ='9.99  '
    .          ='      '
  ;
  value _gnrx
    4='F2'
    5='BC1P1'
    6='BC1P2';
run;
/* create nogenes macro variable                               */
/* nogenes is the number of genes listed in &genes           */
%let nogenes=0;
%if &genes ne %then %do;
  %let word=%scan(&genes,1);
  %do %while (&word ne );
    %let nogenes=%eval(&nogenes+1);
    %let word=%scan(&genes,&nogenes+1);
  %end;
%end;

/* create geneid macro variable                               */
/* geneid is the names of the genes in quotes                */
/*   used in array for identification of output              */
%let word=%scan(&genes,1);
%let geneid=%str('%&word%');
%do i=2 %to &nogenes;
  %let word=%scan(&genes,&i);
  %let geneid=%str(&geneid,'%&word%');
%end;

data _gent;
  set &ds;
  length id aa bb cc dd ee 3
         m n                $ 1;
  array y{*}      &genes;
  array yc{*} $ n1-n&nogenes (%unquote(&geneid)) ;

/* create an obs. for each pair of genes                       */
/* m   will be the response variable for gene1                 */
/* n   will be the response variable for gene2                 */
/* id  will be the numeric id of the (i,j)th combination of gene pair*/
/* gene1 character id of the i-th part of (i,j) pair          */
/* gene2 character id of the j-th part of (i,j) pair          */

obs+1;
id=0;
do _i=1 to dim(y)-1;
  do _j=_i+1 to dim(y);
    id+1;
    m=y{ _i }; n=y{ _j };
    m=upcase(m);
    n=upcase(n);
    gene1=yc{ _i }; gene2=yc{ _j };
    aa=0; bb=0; cc=0; dd=0; ee=0;
  end;
end;

```

```

        if      m ='D' and n ='D' then aa=1;
        else if m ='D' and n ='R' then bb=1;
        else if m ='R' and n ='D' then cc=1;
        else if m ='R' and n ='R' then dd=1;
        else if m =' ' or n =' ' then ee=1;
        else put '*****ERROR***** '
                'Invalid data value on obs=' obs ' for '
                yc{ _i_ }=' m ' or ' yc{ _j_ }=' n ;

    output;
end;
end;
keep id family gnr m n gene1 gene2 aa bb cc dd ee;
run;

/* compute the sums of dominant and recessive individuals */
/* a=AABB b=AAbb c=aaBB d=aabb */
proc means data= _gent noprint nway;
    class id family gnr;
    id gene1 gene2;
    var aa bb cc dd ee;
    output out =_sum(drop=_type_ ) sum=a b c d missing ;
run;

data _P12; set _sum;
    by id family;
    retain phase
           pldd pldr plrd plrr
           p2dd p2dr p2rd p2rr
           omit;
    if first.family then do;
        pldd=.; pldr=.; plrd=.; plrr=.;
        p2dd=.; p2dr=.; p2rd=.; p2rr=.;
        phase=' ';
        omit='no ';
    end;

    if gnr=1 then do;
        t=sum(a,b,c,d);
        if t<=0 then omit='yes';
        if a->&p1 then pldd=1;
        if b->&p1 then pldr=1;
        if c->&p1 then plrd=1;
        if d->&p1 then plrr=1;
    end;
    else if gnr=2 then do;
        if a->&p2 then p2dd=1;
        if b->&p2 then p2dr=1;
        if c->&p2 then p2rd=1;
        if d->&p2 then p2rr=1;
    end;

/* determine if phase= "C"(coupling),          */
/*                                     "R"(repulsion), or          */
/*                                     " "(useless phase).          */

    if      pldd=1 and p2rr=1 then phase='C';
    else if plrr=1 and p2dd=1 then phase='C';

```

```

        else if p1dr=1 and p2rd=1 then phase='R';
        else if p1rd=1 and p2dr=1 then phase='R';
    end;

    if omit='yes' then delete;

/* compute the chisq, probability, recombination frequencies (rf) */
/* and standard error (se). */
if phase not= ' ' and gnr>3 then do;
    t=sum(a,b,c,d);
    chisq=0; df=0;
    if gnr=4 then do;
        chisq=( a**2)/(t*9/16)+( b**2)/(t*3/16)+( c**2)/(t*3/16)
            +( d**2)/(t*1/16) -t ;

        div=b*c-a*d;
        if div ne 0 then do;
            p=( -(b*c+a*d)+((b*c+a*d)**2+a*d*(b*c-a*d))**0.5 )/div
                **0.5;
            se=( (1-p*p)*(2+p*p)/(2*t*(1+2*p*p))) **0.5;
        end;
        if phase='C' then rf=1-p;
        else if phase='R' then rf=p;
    end;

    else if 5<=gnr <=6 then do;
        chisq= (a-t*0.25)**2/(t*0.25)+(b-t*0.25)**2/(t*0.25)
            + (c-t*0.25)**2/(t*0.25)+ (d-t*0.25)**2/(t*0.25);
        rf= (b+c)/t;
        se=(rf*(1-rf)/t)**0.5;
    end;
    df=3;
    prob=probchi(chisq,df);
    prob=1-prob;
end;

drop omit;
drop pldd p1dr p1rd p1rr p2dd p2dr p2rd p2rr    div p;
run;

/* only print for good phases and generations 4, 5, and 6 */
data _gnr4to6;
    set _p12;
    if phase= ' ' then delete;
    if gnr >3;
run;

proc sort; by gnr phase id family; run;

proc print noobs label split='*' uniform data=_gnr4to6;
    by gnr;
    pageby gnr;
    var gene1 gene2    family phase _freq_ a b c d missing chisq df prob
        rf se;
    format chisq 5.1    rf se 6.3    prob _prob. gnr _gnrx.;
    label gnr='GENERATION';
    label family='FAM';
    label _freq_='N';
    label missing='MISS*-ING';

```

```

label se='STD *ERROR';
run;
%mend linkage;

```

### ***SAS Output: Single-Gene Goodness-of-Fit***

```

Cucumber Gene Linkage Example
Single Locus Goodness of Fit Test
Probability >.05 is accepted as Single Locus
GENE=SS FAMILY=44

```

GENERATION	N	DOMINANT	RECESSIVE	MISSING	EXPECTED	CHISQ	DF	PROB
P1	45	45	0	0				
P2	45	1	40	4				
F1	54	49	5	0				
F2	162	103	55	4	3:1	8.11	1	0.004*
BC1P1	81	78	3	0	1:0	0.11	1	0.73
BC1P2	81	38	42	1	1:1	0.20	1	0.65

### ***SAS Output: Linkage Analysis***

```

Cucumber Gene Linkage Example
Recombination Frequency (RF) Data in F2, & BC1 Population
Prob with * indicates gene pair might be linked
GENERATION=F2

```

GENE1	GENE2	FAM	PHASE	N	A	B	C	D	MISS-	STD	RF	ERROR
									ING	CHISQ	DF	PROB
U	SS	30	C	162	69	27	24	36	6	75.8	3	0.000*
U	SS	44	C	162	77	27	26	28	4	35.5	3	0.000*
U	NS	28	C	162	89	16	18	21	16	24.3	3	0.000*
U	NS	30	C	162	74	22	33	27	6	35.0	3	0.000*
RC	NS	30	R	162	83	34	24	15	6	4.8	3	0.18



## Chapter 23

# Mapping Functions

M. Humberto Reyes-Valdés

### ***Purpose***

To map genes and markers and to predict recombination frequencies.

### ***Definitions***

*Mapping function:* A mathematical function that relates map distances to recombination frequencies.

*Genetic map distance (in morgans):* The average number of crossovers per meiotic event between two loci. Genetic distance relates to physical distance, but they are not equivalent.

*Morgan unit:* A unit for expressing the distance between chromosome loci based on recombination. Haldane (1919) named it after T. H. Morgan.

*Coincidence:* Actual double recombinations/number expected with no interference. Each mapping function is based on an assumption about coincidence.

### ***Originators***

Carter, T.C. and Falconer, D.S. (1951). Stocks for detecting linkage in the mouse, and the theory of their design. *Journal of Genetics* 50:307-323.

Haldane, J.B.S. (1919). The combination of linkage values, and the calculation of distances between the loci of linked factors. *Journal of Genetics* 8:299-309.

Kosambi, D.D. (1944). The estimation of map distances from recombination values. *Annals of Eugenics* 12:172-175.

Pascoe, L. and Morton, N.E. (1987). The use of map functions in multipoint mapping. *American Journal of Human Genetics* 40:174-183.



**Software Available**

Reyes-Valdés, M.H. *GenMath* (a Mathematica application for genetics).

**Key References Using the Formulas**

Haley, C.S. and Knott, S.A. (1992). A simple regression method for mapping quantitative trait loci in line crosses using flanking markers. *Heredity* 69:315-324.

Reyes-Valdés, M.H. (2000). A model for marker-based selection in gene introgression breeding programs. *Crop Science* 40:91-98.

**Contact**

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**EXAMPLES****Example 1**

Convert the following recombination frequencies to map distances using the various mapping functions in Table 23.1:

[0.05, 0.10, 0.15, 0.20, 0.25]

TABLE 23.1. Mapping Functions

Author	Function	Coincidence
Haldane (1919)	$m = -\frac{1}{2} \log_e(1-2y)$	1
Kosambi (1944)	$m = \frac{1}{2} \tanh^{-1}(2y)$	2y
Pascoe and Morton (1987)	$m = \frac{\log_e \left[ \frac{(1-2y)^2}{(1-2y-4y^2)} \right] - \frac{\sqrt{3} \tan^{-1} \left[ \frac{(1-4y)/\sqrt{3}}{6} \right]}{6}}{12}$	0.15115 (2y) <sup>2</sup>
Carter and Falconer (1951)	$m = \frac{1}{4} [\tanh^{-1}(2y) - \tan^{-1}(2y)]$	(2y) <sup>3</sup>

*Note:* Where  $m$  = genetic map distance in morgans;  $y$  = recombination frequency;  $\tan$ ,  $\tan^{-1}$  = tangent and inverse tangent, respectively;  $\tanh$ ,  $\tanh^{-1}$  = hyperbolic tangent and inverse hyperbolic tangent, respectively.

The formulas in Table 23.1 can be used manually, but a computer program greatly facilitates calculations. Although the development of GenMath—a genetics package—is not fully complete, it can be used, at this time, for several applications, including mapping functions. The program runs in Mathematica software by Wolfram Research. With GenMath, proceed as follows:

1. Load GenMath in a Mathematica notebook. The prompts *In* and *Out* represent input and output, respectively.

```
In: <C:\genmath.m
```

2. To know the commands available in the package, type:

```
In: ?Global`Genmath`*
```

The output will be:

```
Out:
Abo          GenDis      Iden        PathAnalysis
Avef         HFun       IHFun       PMFun
CFun         Hw         IKFun       ReadConv
ChiTest      HwAbo      IPMFun      Ssd
Comp         Hwmean     KFun        Varc
Eftab       ICFun      Nsim
```

3. To know how a command works, e.g., HFun, type:

```
In: ?HFun
```

The output will be:

```
Out:
HFun[r] gives genetic distance in morgans for a given
recombination fraction r, based on Haldane mapping
function
```

4. You can convert each value, one by one, as follows:

```
In: HFun[0.05]
Out: 0.0526803
```

## 5. Or you can convert the entire vector in one step.

```
In: Map[HFun, {0.05, 0.1, 0.15, 0.2, 0.25}]
Out: {0.0526803, 0.111572, 0.178337, 0.255413, 0.346574}
```

## 6. Since units in the output are in morgans, multiply by 100 to get centimorgans.

```
In: Map[HFun, {0.05, 0.1, 0.15, 0.2, 0.25}]100
Out: {5.26803, 11.1572, 17.8337, 25.5413, 34.6574}
```

## 7. To obtain the whole matrix of map distances in centimorgans with the use of the four functions, combine the commands: HFun (Haldane), KFun (Kosambi), PMFun (Pascoe and Morton), and CFun (Carter and Falconer).

```
In:
TableForm[{Map[HFun, {0.05, 0.1, 0.15, 0.2, 0.25}],
Map[KFun, {0.05, 0.1, 0.15, 0.2, 0.25}],
Map[PMFun, {0.05, 0.1, 0.15, 0.2, 0.25}],
Map[CFun, {0.05, 0.1, 0.15, 0.2, 0.25}]}100]
Out:
5.26803    11.1572    17.8337    25.5413    34.6574
5.01677    10.1366    15.476     21.1824    27.4653
5.00125    10.0201    15.1028    20.3322    25.8425
5.0001     10.0032    15.0244    20.1039    25.3238
```

Each row in this output corresponds to a given mapping function, in the same order depicted in Table 23.1. Notice that for low recombination frequencies (e.g., 0.05), map distances are similar with the use of all the mapping functions. However, as the recombination frequencies increase, map distances diverge. Thus, Haldane's mapping function is not a good choice for high recombination frequencies.

**Example 2**

Convert the following map distances, given in centimorgans, to recombination frequencies using the four mapping functions:

[10, 20, 30, 40, 50, 200]

One way to convert them is to find the analytical inverse of the mapping functions, i.e., to write  $y$  as a function of  $m$ , which may prove difficult when using the last two formulas in Table 23.1. With GenMath, use the commands for inverse mapping functions: IHFun, IKFun, IPMFun,

ICFun. To convert a single value, e.g., 10, with a given inverse mapping function, proceed as follows:

```
In: IPMFun[.1]
Out: 0.0998006
```

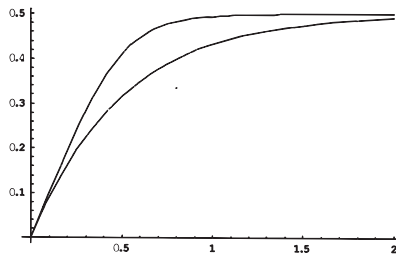
Notice that the map distance was divided by 100 to convert it to morgans before applying the command IPMFun.

To perform all the conversions and present them in table form, you can proceed as follows:

```
In:
TableForm[{Map[IHFun, {0.1, 0.2, 0.3, 0.4, .5, 2}],
Map[iKFun, {.1, .2, .3, .4, .5, 2}],
Map[IPMFun, {.1, .2, .3, .4, .5, 2}],
Map[ICFun, {.1, .2, .3, .4, .5, 2}]}]//N
Out:
0.0906346    0.16484    0.225594    0.275336    0.31606    0.490842
0.0986877    0.189974    0.268525    0.332018    0.380797    0.499665
0.0998006    0.196886    0.285161    0.357854    0.41152    0.499987
0.0999684    0.198987    0.292644    0.372168    0.42959    0.5
```

### Example 3

Plot recombination frequencies against map distances between 0 and 2 morgans using the functions of Haldane and Pascoe and Morton. With the use of GenMath, both plots can be combined as follows:



```
In:
Plot[{IHFun[x], IPMFun[x]}, {x, 0, 2}, PlotPoints->100]
Out:
```

The upper line corresponds to the function of Haldane, and the lower one to the function of Pascoe and Morton.

***Final Remarks***

All the formulas presented in this chapter assume coincidence =  $(2y)^k$ , where  $k$  is a constant that depends on a mapping function. The formulas include the most widely used mapping functions, but several other functions have also been developed. For an excellent account of this topic, the reader is referred to:

Crow, J.F. (1990). *Mapping functions*. *Genetics* 125:669-671.

## Chapter 24

# Bootstrap and Jackknife for Genetic Diversity Parameter Estimates

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### *Purpose*

Bootstrap and jackknife are resampling (sample from a sample) techniques. Whenever distributional properties of parameter estimates cannot be analytically derived due to complex structures of sample data or statistics, bootstrap and jackknife procedures can provide empirical parameter estimates.

### *Definitions*

#### *Bootstrap for Mean and Standard Error*

An original sample of size  $n$  should be available to obtain bootstrap samples. A bootstrap sample is a random sample of size  $n$  drawn with replacement from the original sample. The process is as follows:

1. Obtain a bootstrap sample and calculate the desired parameter estimator, say  $\hat{\theta}$ , from it.
2. Repeat step 1  $K$  times. The bootstrap mean is the mean across all  $K$  runs of the estimator values,

$$\bar{\theta}^B = \frac{1}{K} \sum_{i=1}^K \hat{\theta}_i,$$

and the bootstrap standard error of the estimator is

$$SE^B = \sqrt{\frac{1}{K-1} \sum_{i=1}^K (\bar{\theta}_i - \bar{\theta}^B)^2}$$

### *Jackknife for Mean and Standard Error*

An original sample of size  $n$  should be available to obtain jackknife samples. A jackknife sample is newly obtained from the original sample by leaving out one sample unit or object. The  $i$ th jackknife sample is the original data set with the  $i$ th object removed. The process is as follows:

1. Obtain a jackknife sample and calculate the desired parameter estimator, say  $\bar{\theta}_i$ , from it.
2. Repeat step 1 leaving out a different sample unit each time. For an original sample of size  $n$ , the total number of jackknife samples will be  $n$ . The jackknife mean is the mean across  $n$  estimator values,

$$\bar{\theta}^J = \frac{1}{n} \sum_{i=1}^n \bar{\theta}_i,$$

and the jackknife standard error of the estimator is

$$SE^J = \sqrt{\frac{n-1}{n} \sum_{i=1}^n (\bar{\theta}_i - \bar{\theta}^J)^2}$$

The coefficient multiplying the sample variance is an inflation factor used to account for a smaller variation among jackknife samples than among bootstrap samples.

### *Application for Genetic Diversity Parameters*

These computationally intensive techniques can be used to extract mean and standard errors of genetic diversity parameters from genomic data. With genotypes as sample units and several loci examined, the following multilocus statistics estimate genetic diversity:

1. Proportion of polymorphic loci (P) = the total number of polymorphic loci divided by the total number of loci examined. A locus is considered polymorphic if two or more alleles are detected.

2. Average number of alleles ( $A_a$ ) = the total number of alleles counted in the sample divided by the total number of loci examined.
3. Effective number of alleles ( $A_e$ ) = the reciprocal of the sum across all alleles.
4. Nei's expected heterozygosity ( $H_e$ ),

$$H_e = \frac{1}{L} \sum_{j=1}^L \frac{2n}{2n-1} \left(1 - \sum_{i=1}^a x_i^2\right),$$

where  $n$  is the sample size,  $a$  is the number of alleles,  $x_i$  is the frequency of the  $i$ th allele at the  $j$ th locus, and  $L$  is the number of loci examined.

5. Nei's biased expected heterozygosity ( $BH_e$ ),

$$BH_e = \frac{1}{L} \sum_{j=1}^L \left(1 - \sum_{i=1}^a x_i^2\right)$$

A computer program (*Genetic\_Diversity.exe*) was developed to calculate bootstrap and jackknife means and standard errors of multilocus statistics. It may be obtained free of charge from <<http://www.infostat.com.ar>> Web page. It is a user-friendly program that allows reading of text files structured with genotypes and loci as row and column factors, respectively. By opening the program, a default file of five genotypes and thirteen loci is automatically loaded. The user may select either the bootstrap or jackknife procedure to calculate genetic diversity measures and their standard errors. If jackknife is chosen, an output sample size other than one (default value for the number of sample units left out each time) can be obtained. If bootstrap is chosen, the number of bootstrap replications,  $K$ , can be specified. The default value for  $K$  is 250. There is no maximum number of alleles that can be specified, but the limitation may be the number of different symbols available to identify them. The program does not distinguish between upper- and lowercase letters.

Jackknife and bootstrap routines can be easily adapted to other sample functions (not necessarily genetic diversity statistics). For questions, please contact Dr. Balzarini <[mbalzari@agro.uncor.edu](mailto:mbalzari@agro.uncor.edu)>.





## Chapter 25

# Software on Genetic Linkage and Mapping Available Through the Internet

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### *Purpose*

With the increasing use of Internet resources in all scientific fields, it becomes necessary to compile a meaningful list of software relative to mapping of markers and quantitative trait loci (QTL) that can be accessed through the Internet. Geneticists are now heavily engaged in mapping QTL for important plant and animal traits. Thus, they can benefit from such a list. The list assembled in this chapter, with modifications, is patterned after one that already exists at <http://linkage.rockefeller.edu/soft/> (attributed to Dr. Wentian Li of Rockefeller University). This list contains only those software programs that have a functional Web site. The Weizmann Institute of Science, Genome, and Bioinformatics also has a listing of some of the linkage and mapping-related software at the following Web site: [http://bioinformatics.weizmann.ac.il/repository/mapping\\_software.html](http://bioinformatics.weizmann.ac.il/repository/mapping_software.html). Table 25.1 contains more than 100 such entries and a brief statement about the intended purpose of each software and its important features.

The reader should note that listed Web sites can change location without notice. No guarantee is made that they will remain operational. This list, or any other such list, should be regarded as informational in nature.

The reader is encouraged to check the Web sites listed in Table 25.1 to obtain additional information about software(s) of interest. Although many can be downloaded free of charge, others may require a fee.

TABLE 25.1. An Abbreviated Listing of Software on Genetic Linkage and Mapping

Name of Software	Features/Purpose	Web Site
ACT: Analysis of Complex Traits	Various modules can do the following: Calculate the proportion of genes which are identical by descent, shared in a nuclear family, assess increased allele sharing between all pairs of affected relatives, perform multivariate analysis of complex traits, estimate variance components using maximum likelihood and quasi-likelihood, and generate first-degree relationship coefficients for extended families.	<a href="http://www.epigenetic.org/Linkage/act.html">http://www.epigenetic.org/Linkage/act.html</a>
ALLASS: ALLele ASSociation	Nonparametric linkage and association mapping of disease genes. The ALLASS program implements a model for localizing disease genes by allelic association in a set of disease and normal haplotypes. The program can also model linkage disequilibrium between pairs of SNPs where SNP haplotypes are available.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/ALLASS">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/ALLASS</a>
ALP: Automated Linkage Preprocessor	ALP, a Microsoft Windows application, is designed to analyze microsatellite DNA fragments separated on an automated laser fluorescence sequencer (ALF, Pharmacia Biotech). ALP sizes DNA fragments, removes PCR stutter and other artifacts, if provided with pedigree data it performs genotyping checks to ensure a Mendelian inheritance pattern is followed, and formats data for Lathrop's linkage program package.	<a href="http://www.hgu.mrc.ac.uk/Softdata/ALP/">http://www.hgu.mrc.ac.uk/Softdata/ALP/</a>
Analyze	Simplifies the performance of a large array of parametric and nonparametric tests for linkage and association on data entered in linkage format pedigree and parameter files.	<a href="ftp://ftp.ebi.ac.uk/pub/software/linkage_and_mapping/linkage_cpmc_columbia/analyze/">ftp://ftp.ebi.ac.uk/pub/software/linkage_and_mapping/linkage_cpmc_columbia/analyze/</a>
APM: Affected Pedigree-member Method Arlequin	Linkage analysis.  An exploratory population genetics software environment able to handle large samples of molecular data (RFLPs, DNA sequences, microsatellites).	<a href="http://watson.hgen.pitt.edu/register/docs/apm.html">http://watson.hgen.pitt.edu/register/docs/apm.html</a>  <a href="http://lgb.unige.ch/arlequin/">http://lgb.unige.ch/arlequin/</a>
ASPEX: Affected Sibling Pairs EXclusion map	Performs multipoint exclusion mapping of affected sibling pair data for discrete traits. Allows genome-wide scan.	<a href="ftp://lahmed.stanford.edu/pub/aspeX/">ftp://lahmed.stanford.edu/pub/aspeX/</a>

Autoscan	Helps automate the tedious process of creating input files from genotype data of genome-wide scans.	<a href="http://www.genetics.ucla.edu/software/autoscan/">http://www.genetics.ucla.edu/software/autoscan/</a>
Beta	Performs nonparametric linkage analysis using allele sharing in sibling pairs.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/BETA">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/BETA</a>
BLOCK: BLOCKing Gibbs sampler for pedigree analysis	Perform general pedigree analysis on a general pedigree. Performs two-point linkage analysis on a general pedigree with an arbitrary number of alleles. Employs Markov chain Monte Carlo and Gibb's sampling.	<a href="http://www.cs.auc.dk/~claus/block.html">http://www.cs.auc.dk/~claus/block.html</a>
Borel (see also PANGAEA)	Programs for inference of genealogical relationships from genetic data, including sibship inference.	<a href="ftp://ftp.u.washington.edu/pub/user-supported/pangaea/PANGAEA/BOREL/">ftp://ftp.u.washington.edu/pub/user-supported/pangaea/PANGAEA/BOREL/</a>
CarthaGene	CarthaGene is a genetic/radiated hybrid mapping software. Uses multipoint maximum likelihood estimations of distances. Handles data made up of several distinct populations, which may each be either F2 backcross, recombinant inbred lines, F2 intercross, phase known outbreds, and/or radiated hybrids. Keeps best maps.	<a href="http://www.inra.fr/bia/T/CarthaGene/">http://www.inra.fr/bia/T/CarthaGene/</a>
CASPAR: Computerized Affected Sibling Pair Analyzer and Reporter	An exploratory program to study the genetics of complex (polygenic) diseases. Helps perform conditional linkage analyses, in which the population can be subdivided according to criteria at some loci and analyzed for linkage at other loci. Uses simulation to overcome the problems inherent in multiple testing.	<a href="http://www.ncbi.nlm.nih.gov/CBBresearch/Schaffer/caspar.html">http://www.ncbi.nlm.nih.gov/CBBresearch/Schaffer/caspar.html</a>
Ceph2Map	Constructs linkage maps. Developed from CRI-MAP v2.4.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/ceph2map">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/ceph2map</a>
Clump	Utilizes the Monte Carlo method for assessing significance of a case-control association study with multiallelic markers. Useful for any $2 \times N$ contingency table, especially when N is large.	<a href="http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html">http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html</a>
Combin	A software package developed for constructing ultradense linkage maps. Handles RFLP, SSR, and AFLP marker data.	<a href="http://www.dpw.wau.nl/pv/pub/combin/">http://www.dpw.wau.nl/pv/pub/combin/</a>
COMDS: COMBined Segregation and linkage analysis	Combined segregation and linkage analysis, incorporating severity and diathesis.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/comds">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/comds</a>

TABLE 25.1 (continued)

Name of Software	Features/Purpose	Web Site
CoPE: Collaborative Pedigree drawing Environment	A JAVA program for drawing pedigrees and a standardized system for pedigree storage. Intended for epidemiologists and statisticians to share their familial data through networks.	<a href="http://www.infobiogen.fr/services/CoPE/">http://www.infobiogen.fr/services/CoPE/</a>
CRI-MAP	Allows automated construction of multilocus linkage maps.	<a href="http://compngen.rutgers.edu/multimap/crimap/index.html">http://compngen.rutgers.edu/multimap/crimap/index.html</a>
CRI-MAP-PVM: CRI-MAP with Parallel Virtual Machine	A version of the CRI-MAP program for genetic likelihood computations that runs CRI-MAP's FLIPS and ALL functions in parallel on a distributed network of work stations.	<a href="http://compngen.rutgers.edu/multimap/crimappvm.html">http://compngen.rutgers.edu/multimap/crimappvm.html</a>
Cyrillic	A program for drawing pedigrees and for linking their data to programs for calculating genetic risks, analyzing linkage to DNA markers, and aligning haplotypes.	<a href="http://www.cyrillicsoftware.com/">http://www.cyrillicsoftware.com/</a>
dGene	A simple dBASE III program for the management of pedigree and locus data. Permits easy extraction of genetic data for use with Mendel and Fisher.	<a href="http://www.biomath.medsch.ucla.edu/faculty/klange/software.html">http://www.biomath.medsch.ucla.edu/faculty/klange/software.html</a>
DMap: Disequilibrium Map	Uses information from all disease locus-marker pairs while modeling the variability in disequilibrium values due to the evolutionary dynamics of the population.	<a href="http://lib.stat.cmu.edu/~bdevlin/">http://lib.stat.cmu.edu/~bdevlin/</a>
ECLIPSE (see also PANGAEA): Error Correcting Likelihoods In Pedigree Structure Estimation	It is a set of three programs (preproc, eclipse2, and eclipse3). Analyzes genetic-marker data for genotypic errors and pedigree errors.	<a href="http://stat.washington.edu/thompson/Genepi/pangea.shtml">http://stat.washington.edu/thompson/Genepi/pangea.shtml</a>
EH (EH+): Estimating Haplotype-frequencies	Estimates haplotype frequencies. Also provides log likelihood, chi-squares, and the degrees of freedom under $H_0$ (no allelic association) and $H_1$ (allelic association) hypotheses.	<a href="ftp://linkage.rockefeller.edu/software/eh/">ftp://linkage.rockefeller.edu/software/eh/</a>
ERPA: Extended Relative Pair Analysis	Performs nonparametric linkage analysis.	<a href="ftp://ftp.ebi.ac.uk/pub/software/linkage_and_mapping/statgen/dcurtis/">ftp://ftp.ebi.ac.uk/pub/software/linkage_and_mapping/statgen/dcurtis/</a>

ETDT: Extended Transmission/Disequilibrium Test	Performs TDT on markers with more than two alleles using a logistic regression analysis.	<a href="ftp://ftp.ebi.ac.uk/pub/software/linkage_and_mapping/statgen/dcurtis/">ftp://ftp.ebi.ac.uk/pub/software/linkage_and_mapping/statgen/dcurtis/</a>
FASTLINK (see also LINKAGE): faster version of LINKAGE	Maps disease genes and their approximate locations.	<a href="http://www.ncbi.nlm.nih.gov/CBBresearch/Schaffer/fastlink.html">http://www.ncbi.nlm.nih.gov/CBBresearch/Schaffer/fastlink.html</a>
FAST-MAP: Fluorescent Allele-calling Software Toolkit: Microsatellite Automation Package	A pattern recognition program that facilitates fully automated genotyping of microsatellite markers.	<a href="http://www-2.cs.cmu.edu/~genome/FAST-MAP.html">http://www-2.cs.cmu.edu/~genome/FAST-MAP.html</a>
FASTSLINK (see also SLINK): faster SLINK	Conditional simulation of genetic data on pedigrees.	<a href="http://watson.hgen.pitt.edu/register/soft_doc.html">http://watson.hgen.pitt.edu/register/soft_doc.html</a>
FBAT: Family-Based Association Test	A program for implementing a broad class of family-based association tests that are adjusted for population admixture.	<a href="http://www.biostat.harvard.edu/~fbat/fbat.htm">http://www.biostat.harvard.edu/~fbat/fbat.htm</a>
Firstord	A method for preliminary ordering of loci based on two-point LOD scores.	<a href="http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html">http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html</a>
Fisher	A program for genetic analysis of biometric traits that are controlled by a combination of polygenic inheritance and complex environmental factors.	<a href="http://www.biomath.medsch.ucla.edu/faculty/klange/software.html">http://www.biomath.medsch.ucla.edu/faculty/klange/software.html</a>
GAP: Genetic Analysis Package	A comprehensive package for the management and analysis of pedigree data. Provides powerful database management tools specifically designed for family data. Automatic pedigree drawing. Segregation and linkage analysis, based on traditional maximum likelihood methods and newer, more powerful, Monte Carlo methods that can model both genetic and environmental factors.	<a href="http://icarus2.hsc.usc.edu/epicenter/gap.html">http://icarus2.hsc.usc.edu/epicenter/gap.html</a>
GAS: Genetic Analysis System	An integrated computer program designed to automate and accelerate the acquisition and analysis of genomic data.	<a href="http://users.ox.ac.uk/~ayoung/gas.html">http://users.ox.ac.uk/~ayoung/gas.html</a>
GASP: Genometric Analysis Simulation Program	Generates samples of family data based on user-specified genetic models. Verifies analysis algorithms relative to the underlying theory. Tests the statistical validity of newly developed methods of genetic segregation and linkage analysis and investigates the statistical properties of test statistics. Determines the power and robustness of these methods. Allows application of insights gained from these simulation experiments to ongoing collaborative genetic analyses.	<a href="http://www.nhgri.nih.gov/DIR/IDRB/GASP/">http://www.nhgri.nih.gov/DIR/IDRB/GASP/</a>

TABLE 25.1 (continued)

Name of Software	Features/Purpose	Web Site
GASSOC: Genetic ASSOCIation analysis software	Statistical methods for genetic associations using cases and their parents. Include TDT for multiple marker alleles.	<a href="http://www.mayo.edu/statgen/">http://www.mayo.edu/statgen/</a>
Genehunter	Used for multipoint linkage analysis and nonparametric linkage analysis.	<a href="http://www.fhcrc.org/labs/kruglyak/Downloads/index.html">http://www.fhcrc.org/labs/kruglyak/Downloads/index.html</a>
Genehunter-Imprinting	In German. Parametric (LOD score) analysis of traits conditioned by imprinted genes.	<a href="http://www.meb.uni-bonn.de/imbie/mitarbeiter/strauch/">http://www.meb.uni-bonn.de/imbie/mitarbeiter/strauch/</a>
GenoCheck	Identifies genotypes likely to be errors. Based on Fastlink.	<a href="http://www.crpc.rice.edu/softlib/geno.html">http://www.crpc.rice.edu/softlib/geno.html</a>
GenoDB: GENOtype DataBase	Manipulates large amounts of genotype data generated with fluorescently labeled dinucleotide markers.	<a href="http://osteoporosis.creighton.edu/">http://osteoporosis.creighton.edu/</a>
GGT: Graphical Geno-Typing package	Enables representation of molecular marker data by simple chromosome drawings in several ways. Commonly used marker file types that contain marker information serve as input for this program.	<a href="http://www.dpw.wau.nl/pv/PUB/ggt/">http://www.dpw.wau.nl/pv/PUB/ggt/</a>
GRR: Graphical Representation of Relationships	Designed for detection of relationship specification errors in general pedigrees by use of genome scan marker data.	<a href="http://qtl.well.ox.ac.uk/GRR/">http://qtl.well.ox.ac.uk/GRR/</a>
GSCAN: Genomic Software for Complex Analysis of Nucleotides	Linkage program based on a semiparametric method. Allows semiparametric two-point linkage, linkage disequilibrium, and combined linkage/linkage-disequilibrium analysis of general pedigree data for discrete traits, including pedigree consistency checks and pedigree drawing, gene-gene and gene-environment interaction incorporation, and Z-score computation.	<a href="http://cougar.fhcrc.org/~filq/html/main.htm">http://cougar.fhcrc.org/~filq/html/main.htm</a>
Haplo	Haplotyping with computation of conditional probabilities.	<a href="http://watson.hgen.pitt.edu/register/soft_doc.html">http://watson.hgen.pitt.edu/register/soft_doc.html</a>
HAPPY: reconstructing HAPlotypes	Two-stage analysis: ancestral haplotype reconstruction using dynamic programming followed by QTL testing by linear regression.	<a href="http://www.well.ox.ac.uk/~rmott/happy.html">http://www.well.ox.ac.uk/~rmott/happy.html</a>

Hardy (see also PANGAEA)	Hardy contains program and documentation for Monte Carlo estimation of P values in sparse, two-dimensional contingency tables, or for Hardy Weinberg equilibrium.	<a href="http://www.stat.washington.edu/thompson/Genepi/Hardy.shtml">http://www.stat.washington.edu/thompson/Genepi/Hardy.shtml</a>
JoinMap	Software for the calculation of genetic linkage maps. Can handle many common types of mapping populations (BC1, F2, RILs, [doubled] haploids, full-sib family of outbreeders). Can combine (join) data derived from several sources into an integrated map.	<a href="http://www.plant.wageningen-ur.nl/default.asp?section=products&amp;page=/products/mapping/joinmap/jmintro.htm">http://www.plant.wageningen-ur.nl/default.asp?section=products&amp;page=/products/mapping/joinmap/jmintro.htm</a>
KINDRED	A program that stores and maintains data on families and members of families, and automatically draws pedigrees in a format suitable for presentation/publication.	<a href="http://icarus2.hsc.usc.edu/epicenter/kindred.html">http://icarus2.hsc.usc.edu/epicenter/kindred.html</a>
LDB: Location DataBase	Gives locations for expressed sequences and polymorphic markers. Locations are obtained by integrating data of different types (genetic linkage maps, radiation hybrid maps, physical maps, cytogenetic data, and mouse homology) and constructing a single summary map. Integrates genetic linkage map and physical map.	<a href="ftp://cedar.genetics.soton.ac.uk/public_html/ldb.html">ftp://cedar.genetics.soton.ac.uk/public_html/ldb.html</a>
Linkage: general pedigrees (see also FASTLINK)	The core of the Linkage package is a series of programs for maximum likelihood estimation of recombination rates, calculation of LOD score tables, and analysis of genetic risks.	<a href="ftp://linkage.rockefeller.edu/software/linkage/">ftp://linkage.rockefeller.edu/software/linkage/</a>
Linkbase	An easy and practical tool for connecting the genotype data produced by automatic sequencers (ABI Prism 377 [Perkin Elmer] and ALF [Pharmacia]) to linkage and sib-pair programs.	<a href="http://www.ktl.fi/molbio/software/linkbase/newintro.html">http://www.ktl.fi/molbio/software/linkbase/newintro.html</a>
Loki (see also PANGAEA)	Analyzes quantitative traits observed on large pedigrees using Monte Carlo multipoint linkage and segregation analysis.	<a href="ftp://ftp.u.washington.edu/pub/user-supported/pangaea/PANGAEA/Loki/">ftp://ftp.u.washington.edu/pub/user-supported/pangaea/PANGAEA/Loki/</a>
Map/Map+/Map+H	Performs multiple pairwise linkage analysis and incorporates interference.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/map+;">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/map+;</a> <a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/map+h">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/map+h</a>



TABLE 25.1 (continued)

Name of Software	Features/Purpose	Web Site
MAPL: MAPping and QTL analysis	Provides segregation ratio, linkage test, recombination value, grouping of markers, ordering of markers by metric multidimensional scaling, drawing maps, and graphical genotypes, as well as QTL analysis by interval mapping and ANOVA.	<a href="http://peach.ab.a.u-tokyo.ac.jp/~ukai/mapl98.html">http://peach.ab.a.u-tokyo.ac.jp/~ukai/mapl98.html</a>
Mapmaker/Exp	Constructs genetic linkage maps.	<a href="http://www-genome.wi.mit.edu/genome_software">http://www-genome.wi.mit.edu/genome_software</a>
Mapmaker/HOMOZ: HOMOZygoty mapping	Calculates multipoint LOD scores in pedigrees with inbreeding loops.	<a href="ftp://ftp-genome.wi.mit.edu/distribution/software/homoz/">ftp://ftp-genome.wi.mit.edu/distribution/software/homoz/</a>
Mapmaker/QTL	Helps map genes controlling quantitative traits.	<a href="ftp://ftp-genome.wi.mit.edu/distribution/software/newqtl/">ftp://ftp-genome.wi.mit.edu/distribution/software/newqtl/</a>
Map Manager Classic	A program for Apple Macintosh personal computer that helps analyze the results of genetic mapping experiments using backcrosses, intercrosses, or recombinant inbred strains.	<a href="http://mapmgr.roswellpark.org/classic.html">http://mapmgr.roswellpark.org/classic.html</a>
Map Manager QT	A version of Map Manager with additional functions for analyzing quantitative traits. A graphic, interactive program to map quantitative trait loci by regression methods.	<a href="http://mapmgr.roswellpark.org/mmQT.html">http://mapmgr.roswellpark.org/mmQT.html</a>
Map Manager QTX	A version of Map Manager that combines the cross-platform design of Map Manager XP with enhanced QT analysis from Map Manager QT. Allows detection and localization of quantitative trait loci by fast regression-based single locus association, simple interval mapping, and composite interval mapping. Calculates empirical significance values by permutation tests. Allows a choice of Haldane, Kosambi, and Morgan mapping functions. Supports advanced backcross and advanced intercross designs.	<a href="http://mapmgr.roswellpark.org/mmQTX.html">http://mapmgr.roswellpark.org/mmQTX.html</a>
MapPop	For selective mapping and bin mapping.	<a href="http://www.bio.unc.edu/faculty/vision/lab/mappop/">http://www.bio.unc.edu/faculty/vision/lab/mappop/</a>

Mapqtl	For calculation of QTL positions on genetic maps via interval mapping, composite interval mapping, or a nonparametric method.	<a href="http://www.plant.dlo.nl/default.asp?section=products&amp;page=products/mapping/mapqtl/mqintro.htm">http://www.plant.dlo.nl/default.asp?section=products&amp;page=products/mapping/mapqtl/mqintro.htm</a>
MCLEEPS: Monte Carlo Likelihood Estimation of Effective Population Size	For estimating effective population size from temporal changes in allele frequencies.	<a href="http://www.stat.washington.edu/thompson/Genepi/Mcleeps.shtml">http://www.stat.washington.edu/thompson/Genepi/Mcleeps.shtml</a>
MEGA2: Manipulation Environment for Genetic Analyses	A data-handling program for facilitating genetic linkage and association analyses.	<a href="http://watson.hgen.pitt.edu/mega2.html">http://watson.hgen.pitt.edu/mega2.html</a>
Mendel	For genetic analysis of human pedigree data involving a small number of loci. Useful for segregation analysis, linkage calculations, genetic counseling, and allele frequency estimation.	<a href="http://www.biomath.medsch.ucla.edu/faculty/klange/software.html">http://www.biomath.medsch.ucla.edu/faculty/klange/software.html</a>
MFLINK: Model Free Linkage analysis	Performs (nearly) model-free linkage analysis.	<a href="http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html">http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html</a>
MIM: Multipoint Identical-by-descent Method	For partitioning genetic variance of quantitative traits to specific chromosome regions using data on nuclear families.	<a href="ftp://morgan.med.utah.edu/pub/Mim/">ftp://morgan.med.utah.edu/pub/Mim/</a>
Mld	A shuffling version of conditional tests for different combinations of allelic and genotypic disequilibrium on haploid and diploid data.	<a href="ftp://statgen.ncsu.edu/pub/zaykin/">ftp://statgen.ncsu.edu/pub/zaykin/</a>
MORGAN:MONte CaRlo Genetic Analysis (see also PANGAEA)	For segregation and linkage analysis, using Markov chain and Monte Carlo methods. Includes MCMC methods for multilocus gene identity by descent and homozygosity mapping.	<a href="http://www.stat.washington.edu/thompson/Genepi/Morgan.shtml">http://www.stat.washington.edu/thompson/Genepi/Morgan.shtml</a>
MultiMap	For automated construction of genetic maps. Developed for large-scale linkage mapping of markers genotyped in reference pedigrees. Adapted for automated construction of radiation hybrid maps.	<a href="http://compgen.rutgers.edu/multimap/index.shtml">http://compgen.rutgers.edu/multimap/index.shtml</a>
NOPAR	Nonparametric linkage and association tests for quantitative traits.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/nopar/">http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/nopar/</a>

TABLE 25.1 (continued)

Name of Software	Features/Purpose	Web Site
PANGAEA: Pedigree Analysis for Genetics And Epidemiological Attributes	A nine-program package for genetic analyses including: Borel, Hardy, MORGAN, Pedpack, InSegT, Loki, MCLEEPS, Pedfiddler, and Eclipse.	<a href="http://www.stat.washington.edu/thompson/Genepi/pangaea.shtml">http://www.stat.washington.edu/thompson/Genepi/pangaea.shtml</a>
PAP: Pedigree Analysis Package	Computes the likelihood of specified parameter values; provides the probability of each genotype for pedigree members; simulates phenotypes for output into files; maximizes the likelihood over specified parameters (with or without standard errors); computes the standard errors of parameters for unknown estimates; simulates phenotypes and estimates parameter values; estimates expected LOD scores; and computes a grid of likelihood over one or two parameters. Also does TDT.	<a href="http://hasstedt.genetics.utah.edu/">http://hasstedt.genetics.utah.edu/</a>
PED: PEdigree Drawing software	A tool for fast and standardized drawing of pedigrees.	<a href="http://www.medgen.de/ped/index.htm">http://www.medgen.de/ped/index.htm</a>
PedCheck	Detects marker-typing incompatibilities in pedigree data.	<a href="http://watson.hgen.pitt.edu/register/docs/pedcheck.html">http://watson.hgen.pitt.edu/register/docs/pedcheck.html</a>
Pedfiddler	A set of programs to manipulate pedigree graphs. Can be used as a stand-alone version of the graphics facilities found in Pedpack. Pedfiddler is not fully compatible with Pedpack because it is not intended for analysis but for graphical purposes only.	<a href="http://www.stat.washington.edu/thompson/Genepi/Pedfiddler.shtml">http://www.stat.washington.edu/thompson/Genepi/Pedfiddler.shtml</a>
PedHunter	A software package that facilitates creation and verification of pedigrees within large genealogies.	<a href="http://www.ncbi.nlm.nih.gov/CBBresearch/Schaffer/pedhunter.html">http://www.ncbi.nlm.nih.gov/CBBresearch/Schaffer/pedhunter.html</a>
Pedigree/Draw	For creation, editing, and drawing of pedigrees of human or non-human families. The package consists of applications, example files, and a user's guide.	<a href="http://www.sfbr.org/sfbr/public/software/pedraw/peddrw.html">http://www.sfbr.org/sfbr/public/software/pedraw/peddrw.html</a>
PedJava	Uses browser technology to enter pedigrees into a database.	<a href="http://cooke.gsf.de/wjst/download.cfm">http://cooke.gsf.de/wjst/download.cfm</a>

PedPlot: PEDigree PLOTting program	Helps view a family structure by generating a plot from a pedfile/datafile pair.	<a href="http://www.chg.duke.edu/software/pedplot.html">http://www.chg.duke.edu/ software/pedplot.html</a>
PEDRAW/WPEDRAW: PEDigree DRAWing/Windows PEDigree DRAWing	A pedigree drawing program using LINKAGE or LINKSYS data files.	<a href="http://www.mds.qmw.ac.uk/statgen/dcurtis/software.html">http://www.mds.qmw.ac.uk/ statgen/dcurtis/software.html</a>
PEDSYS: PEDigree database system	For management of genetic, pedigree, and demographic data. Designed principally for use with pedigree analysis of either human or nonhuman subjects.	<a href="http://www.sfbr.org/sfbr/public/software/pedsys/pedsys.html">http://www.sfbr.org/sfbr/ public/ software/pedsys/pedsys.html</a>
Pointer	For complex segregation analysis with mixed models.	<a href="http://cedar.genetics.soton.ac.uk/pub/PROGRAMS/pointer">http://cedar.genetics. soton.ac. uk/pub/PROGRAMS/pointer</a> <a href="http://www.progeny2000.com/">http://www.progeny2000.com/</a>
Progeny	Provides a method of tracking, managing, and viewing genetic data using the most advanced pedigree drawing and database technology.	<a href="http://www.progeny2000.com/">http://www.progeny2000.com/</a>
QTDT: Quantitative (trait) Transmission/Dis- equilibrium Test	Provides a convenient one-stop interface for family-based tests of linkage disequilibrium.	<a href="http://www.sph.umich.edu/csg/abecasis/QTDT">http://www.sph.umich.edu/ csg/abecasis/QTDT</a>
QTL Cartographer	A suite of programs to map quantitative traits using a map of molecular markers.	<a href="http://statgen.ncsu.edu/qtlcart/cartographer.html">http://statgen.ncsu.edu/qtlcart /cartographer.html</a>
QUGENE: QUantitative GENETics	A flexible platform for investigation of the characteristics of genetic models. The architecture of the software has two main levels: (1) the genotype-environment system engine and (2) the application modules. The engine is the platform on which the different systems for investigation are generated and the modules are used to conduct the simulation experiments.	<a href="http://pig.ag.uq.edu.au/qu-gene/">http://pig.ag.uq.edu.au/ qu-gene/</a>
Relative	For relationship estimation, in particular between putative siblings when parents are untyped.	<a href="ftp://linkage.rockefeller.edu/software/relative/">ftp://linkage.rockefeller.edu/ software/relative/</a>
RelCheck	For verifying relationships between all pairs of individuals in a linkage study. Allows for the presence of genotyping errors.	<a href="http://biosun01.biostat.jhsph.edu/~kbroman/software/">http://biosun01.biostat.jhsph. edu/~kbroman/software/</a>
RHMAPPER: Radiation Hybrid MAPPER	An interactive program for radiation hybrid mapping. Uses a hidden Markov model for calculating maximum likelihood.	<a href="http://www-genome.wi.mit.edu/ftp/pub/software/rhmapper/">http://www-genome.wi.mit. edu/ftp/pub/software/ rhmapper/</a>

TABLE 25.1 (continued)

Name of Software	Features/Purpose	Web Site
SAGE: Statistical Analysis for Genetic Epidemiology	A software package containing more than twenty programs for use in genetic analysis of family and pedigree data.	<a href="http://darwin.cwru.edu/octance/sage/sage.php">http://darwin.cwru.edu/octance/sage/sage.php</a>
Sib-Pair	For simple nonparametric genetic analysis of family data.	<a href="http://www2.qimr.edu.au/davidD/">http://www2.qimr.edu.au/davidD/</a>
Simibd	For performing nonparametric linkage analysis.	<a href="http://watson.hgen.pitt.edu/register/soft_doc.html">http://watson.hgen.pitt.edu/register/soft_doc.html</a>
SimWalk2	For haplotype, parametric and nonparametric linkage, identity by descent, and mistyping analyses, using Markov chain, Monte Carlo, and simulated annealing algorithm.	<a href="http://watson.hgen.pitt.edu/register/soft_doc.html">http://watson.hgen.pitt.edu/register/soft_doc.html</a>
SOLAR: Sequential Oligogenic Linkage Analysis Routines	A software package for genetic variance components analysis, including linkage analysis, quantitative genetic analysis, and covariate screening.	<a href="http://www.sfbr.org/sfbr/public/software/solar/index.html">http://www.sfbr.org/sfbr/public/software/solar/index.html</a>
SPERM	For the analysis of sperm typing data.	<a href="http://www.biomath.medsch.ucla.edu/faculty/klange/software.html">http://www.biomath.medsch.ucla.edu/faculty/klange/software.html</a>
SPERMSEG	For analysis of segregation in single-sperm data.	<a href="http://galton.uchicago.edu/~mcpeek/software/spermseg/">http://galton.uchicago.edu/~mcpeek/software/spermseg/</a>
SPLINK: Affected Sib Pairs LINKage Analysis	A program for sibling pair linkage analysis. Maximum likelihood subject to possible triangle restriction. Marker haplotypes based on several closely linked markers. Haplotype frequencies are estimated from the data.	<a href="http://www-gene.cimr.cam.ac.uk/clayton/software/">http://www-gene.cimr.cam.ac.uk/clayton/software/</a>
TDT-PC: Transmission Disequilibrium Test Power Calculator	To compute the statistical power of the Transmission/Disequilibrium Test (TDT), which is a powerful test for linkage in the presence of association.	<a href="http://biosun01.biostat.jhsph.edu/~wmchen/pc.html">http://biosun01.biostat.jhsph.edu/~wmchen/pc.html</a>
TDT/S-TDT: Transmission Disequilibrium Test and Sibling-Transmission Disequilibrium Test	Provides separate results for TDT, S-TDT, and the combined (overall) test.	<a href="http://genomics.med.upenn.edu/spielman/TDT.htm">http://genomics.med.upenn.edu/spielman/TDT.htm</a>

Transmit	For transmission disequilibrium testing. Marker haplotypes based on several closely linked markers. Parental genotype and/or haplotype phase may be missing.	<a href="http://www.gene.cimr.cam.ac.uk/clayton/software">http://www.gene.cimr.cam.ac.uk/clayton/software</a>
2DMAP: 2-Dimensional Crossover-based MAP	For constructing two-dimensional crossover-based maps.	<a href="http://www.genlink.wustl.edu/software/">http://www.genlink.wustl.edu/software/</a>
Typenext	To simulate marker data for untyped individuals to determine how much information each untyped individual would contribute if typed.	<a href="ftp://linkage.rockefeller.edu/software/typenext/">ftp://linkage.rockefeller.edu/software/typenext/</a>
Vitesse	For likelihood calculation on pedigrees.	<a href="http://watson.hgen.pitt.edu/register/soft_doc.html">http://watson.hgen.pitt.edu/register/soft_doc.html</a>
Web-Prelink	Prepares data files for Linkage using web interface.	<a href="http://linkage.rockefeller.edu/gui/webprelink.html">http://linkage.rockefeller.edu/gui/webprelink.html</a>

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*Note:* AFLP = Amplified fragment length polymorphism; LOD = Logarithm of odds; the odds are the likelihood that linkage exists relative to the likelihood that linkage does not exist; QTL = quantitative trait loci; RIL = recombinant inbred line; RFLP = restriction fragment length polymorphism; SNP = single nucleotide polymorphism; SSR = simple sequence repeat.



## Chapter 26

# Gregor

Todd Krone

### *Importance*

An easy to use and valuable simulation tool to help plant breeders create population scenarios and subsequently observe the effects of selection via phenotype and/or genotype.

### *Originators*

Dr. Nick Tinker and Dr. Diane E. Mather

Tinker, N.A. and Mather, D.E. (1993). GREGOR: Software for genetic simulation. *Journal of Heredity* 84:237.

### *Summary of One Scientist's Use of Gregor*

This software program was found to be very useful when planning and executing backcrossing and breeding programs in maize. Its simplicity allows quick and efficient testing of various breeding questions. Many options and applications can be utilized in this program, but this brief summary does not allow complete coverage. I used Gregor for:

1. Testing the effects of varying assumptions on a backcrossing and breeding program. Many assumptions are made in a plant breeding program based on an understanding of the principles of plant breeding theory. Although theory gives an understanding of the effects that may result from varying assumptions, simulating a wide array of assumptions in Gregor provides a much deeper understanding of the effects. The many assumptions that can be tested using Gregor are



- number of genes affecting a trait,
- magnitude of gene effects,
- gene action,
- heritability,
- population size, and
- population type (e.g., F<sub>2</sub>, doubled haploids, recombinant inbred lines [RILs], etc.).

Gregor gives several options for evaluation of the simulation, such as viewing graphical genotypes and summary statistics for any given trait. It is also very simple to export data to Microsoft Excel or other programs to evaluate the results more deeply. This process helps one understand the assumptions that are critical to the success of a program.

2. Testing the effect of varying assumptions on the effectiveness of gene mapping. The variables can be varied, as in the breeding program simulations (point number 1), along with marker number, distribution of markers, and marker dominance/additivity. Although Gregor can give summary statistics for markers of interest, it is found to be most useful when exporting data to Excel or Mapmaker for analysis. Theories can lead to good assumptions, but testing them in Gregor is a fast and inexpensive way to verify them.
3. Testing the effect of varying assumptions on selection for a trait via molecular markers. Once a breeding program is established, and molecular marker associations have been determined for a trait of interest, marker-assisted selection can be applied. This is a subheading of the breeding program as marker-assisted selection is simply another tool that can be used in a breeding program. In Gregor, molecular markers are listed as separate menu options from population and trait. The use of markers in breeding programs is not generally accepted as a common tool. Rather, it is seen as a developing tool. Thus, it is listed as a separate application. In many applications, marker-assisted selection may be appropriate. Prior to executing a selection scheme, it should be run through Gregor first to determine the appropriate marker number and distribution. This has been particularly useful in developing marker-assisted selection for backcross breeding.

Gregor is limited in that it is DOS based and restricts population size. However, other publicly available simulation software that can simulate breeding situations in such an effective and easy way are not known. Overall, the primary benefit of Gregor is that you can easily tailor simulations for any breeding scenario. In addition to having a sound knowledge of principles of genetics and breeding, the breeder should benefit from a virtual run of the breeding program. The software allows wise testing of practices prior to expending large sums of money and time executing a breeding program.

### ***Software Available***

Dr. Diane E. Mather, Department of Plant Science, McGill University, 21111 Lakeshore Road, Ste-Anne-de-Bellevue, Québec H9X 3V9, Canada. FAX: 514-398-7897. E-mail: <dianemather@mcgill.ca>. For a link to a Web site that describes Gregor, set your browser to <<http://gnome.agrenv.mcgill.ca>>.

Dr. Nicholas A. Tinker, Agriculture and Agri-Food, Canada, Biometrics and Bioproducts, ECORC, K. W. Neatby Building, Floor 2, Room 2056, 960 Carling Avenue, Ottawa, Ontario, K1A 0C6, CANADA.



## Chapter 27

# Analysis for an Experiment Designed As Augmented Lattice Square Design

Walter T. Federer

### *Importance*

Augmented experiment designs are used internationally for screening large numbers of new genotypes used in early generations of plant-breeding programs. Any experiment design (complete block, incomplete block, row-column, or other) may be selected for the standard treatments replicated  $r$  times each. The blocks, incomplete blocks, or rows and columns are enlarged to accommodate the new treatments usually included only once in the experiment. The lattice square experiment design controls variation within each complete block in two directions (rows and columns). Augmented lattice square designs (ALSDs) are easily constructed as described by Federer, W. T. (2002) in “Construction and Analysis of an Augmented Lattice Square Design,” *Biometrical Journal* 44(2):251-257. ALSDs can accommodate  $c = 2k$  or  $3k$  check or standard cultivars in  $r = k$  complete blocks and  $n = k^2(k - 2)$  or  $k^2(k - 3)$  new genotypes. An ALSD with  $k = 4 = r$ ,  $c = 8$ , and  $n = 32$  illustrates a statistical analysis. A trend analysis using polynomial regression is used. The following data are presented for all sixty-four responses.

```
/*The infile for the data is auglsd8. The five columns of the data set
below represent, respectively, Rep, Row, Col, Trt, and Yield. In
the Trt column, checks are numbered 33-40 and new treatments are
numbered 1-32*/
```

```
1 1 1 33 17
1 1 2 1 9
1 1 3 2 9
1 1 4 40 23
1 2 1 37 21
1 2 2 34 18
```

1	2	3	3	9
1	2	4	4	9
1	3	1	5	9
1	3	2	38	22
1	3	3	35	19
1	3	4	6	9
1	4	1	7	9
1	4	2	8	19
1	4	3	39	23
1	4	4	36	20
2	1	1	33	17
2	1	2	9	8
2	1	3	10	8
2	1	4	39	25
2	2	1	40	22
2	2	2	34	18
2	2	3	11	18
2	2	4	12	18
2	3	1	13	18
2	3	2	37	23
2	3	3	35	19
2	3	4	14	17
2	4	1	15	16
2	4	2	16	21
2	4	3	38	25
2	4	4	36	20
3	1	1	33	24
3	1	2	17	17
3	1	3	18	17
3	1	4	38	18
3	2	1	39	22
3	2	2	34	12
3	2	3	19	17
3	2	4	20	16
3	3	1	21	17
3	3	2	40	25
3	3	3	35	15
3	3	4	22	17
3	4	1	23	17
3	4	2	24	17
3	4	3	37	15
3	4	4	36	15
4	1	1	33	28
4	1	2	25	20
4	1	3	26	20
4	1	4	37	25
4	2	1	38	29
4	2	2	34	22
4	2	3	27	26
4	2	4	28	26
4	3	1	29	16
4	3	2	39	32
4	3	3	35	25
4	3	4	30	26
4	4	1	31	16
4	4	2	32	16
4	4	3	40	25
4	4	4	36	30

The SAS/GLM and SAS/MIXED codes for this data set are as follows:

```

options ls = 76;
proc iml;
  opn3= orpol(1:4,2); /* The 4 is the number of columns and 2 indi-
    cates that
    linear and quadratic polynomial regression coefficients are desired.
    */
  opn3[,1]= (1:4)`;
  op3 =opn3 ;    print op3; /* Print-out of coefficients. */
  create opn3 from opn3[colname ={'COL' 'C1' 'C2'}]; append from opn3;
  close opn3;run;
  opn4 =orpol(1:4,2); /* There are 4 rows and two regressions. */
  opn4[,1]=(1:4)` ;
  op4 =opn4;          print op4;
  create opn4 from opn4[colname ={'ROW' 'R1' 'R2'}]; append from opn4;
  close opn4; run;
data auglsd8;
  infile 'auglsd8.dat';
  input rep row col trt yield;
  if (trt>32) then new = 0; else new = 1;
  /* This divides the 40 entries into 32 new treatments which are
  considered as random effects and 8 checks which are fixed effects. */
  if (new) then trtn = 999; else trtn = trt;
data augbig;set auglsd8;
  /* The regression coefficients are added to the data set. */
  idx = _n_; run;
proc sort data = augbig;
  by COL; run;data augbig; merge augbig opn3; by COL; run;
proc sort data = augbig;
  by ROW; run; data augbig; merge augbig opn4; by ROW; run;
proc sort data = augbig; by idx; run;
proc glm  data = augbig;
  class row col trt trtn rep;
  model yield = rep trt C1*rep R1*rep C1*R1*rep;
  lsmeans trt/out = lsmeans noprint; run;
proc sort data = lsmeans; by descending lsmean;
  /* n is usually quite large and this statement arranges the fixed
  effect means in descending order for viewing. */
proc print; run;
proc mixed data = augbig;
  class rep row col trt trtn;
  model yield = trtn/solution;
  random rep C1*rep R1*rep C1*R1*rep trt*new/solution;
  /* These two statements obtain solutions for the various effects. */
  lsmeans trtn; make 'solutionr' out = sr noprint; run;
proc sort data = sr;
  by descending _est_;
  /*The effect solutions are arranged from largest to smallest. */
proc print; run;
quit;

```

The output in the preceding example and program is presented in a modified version of the actual output. Following are the linear and quadratic coefficients:

OP3		
1	-0.67082	0.5
2	-0.223607	-0.5
3	0.2236068	-0.5
4	0.6708204	0.5

OP4		
1	-0.67082	0.5
2	-0.223607	-0.5
3	0.2236068	-0.5
4	0.6708204	0.5

## Class Level Information

Class Levels	Values
ROW	4 1 2 3 4
COL	4 1 2 3 4
TRT	40 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40
TRTN	9 33 34 35 36 37 38 39 40 999 /* Checks numbered 33-40.*/
REP	4 1 2 3 4

Number of observations in data set = 64

Dependent Variable: YIELD	Sum of	Mean			
Source	DF	Squares	Square	F Value	Pr > F
Model	54	2022.63549	37.45621	5.73	0.0041
Error	9	58.84888	6.53876		
Corrected Total	63	2081.48438			

R-Square	C.V.	Root MSE	YIELD Mean
0.971727	13.62652	2.55710	18.7656

## Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	3	634.92188	211.64063	32.37	0.0001
TRT	39	1284.68750	32.94071	5.04	0.0070
C1*REP	4	52.76528	13.19132	2.02	0.1755
R1*REP	4	3.38948	0.84737	0.13	0.9677
C1*R1*REP	4	46.87135	11.71784	1.79	0.2145
Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	3	240.67132	80.22377	12.27	0.0016
TRT	39	1066.10112	27.33593	4.18	0.0137
C1*REP	4	37.86878	9.46720	1.45	0.2953
R1*REP	4	23.77297	5.94324	0.91	0.4985
C1*R1*REP	4	46.87135	11.71784	1.79	0.2145

Fixed effect means:OBS	NAME	TRT	LSMEAN	STDERR
1	YIELD	36	28.5625	3.98587
2	YIELD	22	27.5443	3.87268
3	YIELD	33	26.5625	3.98587
4	YIELD	30	24.3923	3.87268
5	YIELD	39	24.1171	1.67939
6	YIELD	20	23.9249	3.40407
7	YIELD	28	23.0745	3.40407
8	YIELD	40	23.0142	1.67939
9	YIELD	38	22.9711	1.67939
10	YIELD	19	22.3609	2.89414

11	YIELD	27	22.2280	2.89414
12	YIELD	18	22.0455	3.40407
13	YIELD	14	21.9964	3.87268
14	YIELD	17	21.7855	3.87268
15	YIELD	37	20.8976	1.67939
16	YIELD	35	20.5625	1.41148
17	YIELD	12	20.0757	3.40407
18	YIELD	11	19.6544	2.89414
19	YIELD	34	17.8125	1.41148
20	YIELD	25	17.2728	3.87268
21	YIELD	26	16.5147	3.40407
22	YIELD	24	15.8193	5.01784
23	YIELD	6	14.5671	3.87268
24	YIELD	1	14.3972	3.87268
25	YIELD	9	14.0444	3.87268
26	YIELD	8	13.7216	5.01784
27	YIELD	21	12.9400	5.01784
28	YIELD	16	12.6102	5.01784
29	YIELD	4	11.6749	3.40407
30	YIELD	2	11.5900	3.40407
31	YIELD	3	11.2568	2.89414
32	YIELD	10	10.5998	3.40407
33	YIELD	13	10.1342	5.01784
34	YIELD	23	8.6472	8.44815
35	YIELD	32	7.5988	5.01784
36	YIELD	29	7.0391	5.01784
37	YIELD	5	3.6367	5.01784
38	YIELD	31	3.5431	8.44815
39	YIELD	15	-0.5431	8.44815
40	YIELD	7	-3.1472	8.44815

REML Estimation Iteration History

Iteration	Evaluations	Objective	Criterion
0	1	245.77696870	
1	3	218.84012634	0.00762773
2	2	218.34805379	0.00012725
3	2	218.33482743	0.00000093
4	1	218.33472566	0.00000000

Convergence criteria met.

Covariance Parameter Estimates (REML)

Cov Parm	Estimate
REP	11.99469629
C1*REP	1.88018116
R1*REP	3.98577174
C1*R1*REP	4.69746155
NEW*TRT	5.87662721
Residual	8.41233535

Solution for Fixed Effects

Effect	TRTN	Estimate	Std Error	DF	t	Pr >  t
INTERCEPT		15.84932467	1.85872722	3	8.53	0.0034
Effect	TRTN	Estimate	Std Error	DF	t	Pr >  t
TRTN	33	6.02505345	1.80689098	9	3.33	0.0087



TRTN	34	1.78104271	1.61807612	9	1.10	0.2996
TRTN	35	3.51473327	1.61757976	9	2.17	0.0578
TRTN	36	4.97612515	1.80199562	9	2.76	0.0221
TRTN	37	5.08850236	1.67222656	9	3.04	0.0140
TRTN	38	7.28885283	1.67222656	9	4.36	0.0018
TRTN	39	9.63215629	1.67222656	9	5.76	0.0003
TRTN	40	8.35433917	1.67222656	9	5.00	0.0007
TRTN	999	0.00000000	.	.	.	.

## Least Squares Means (Check, fixed effect means.)

Effect	TRTN	LSMEAN	Std Error	DF	t	Pr >  t
TRTN	33	21.87437812	2.39139410	9	9.15	0.0001
TRTN	34	17.63036738	2.26946107	9	7.77	0.0001
TRTN	35	19.36405795	2.26934312	9	8.53	0.0001
TRTN	36	20.82544982	2.38836997	9	8.72	0.0001
TRTN	37	20.93782703	2.31267932	9	9.05	0.0001
TRTN	38	23.13817750	2.31267932	9	10.00	0.0001
TRTN	39	25.48148096	2.31267932	9	11.02	0.0001
TRTN	40	24.20366385	2.31267932	9	10.47	0.0001
TRTN	999	15.84932467	1.85872722	9	8.53	0.0001

(Solutions for random effects arranged in descending order. To obtain the means, add the intercept value to each of the effects below.)

OBS	EFFECT_	REP	TRT	EST	SEPRE	DF	T	PT
1	REP	4		4.85091339	1.86295604	9	2.60	0.0286
2	R1*REP	2		2.51920549	1.33546047	9	1.89	0.0919
3	NEW*TRT		8	2.16475642	1.94313336	9	1.11	0.2941
4	NEW*TRT		27	2.01517588	1.90869357	9	1.06	0.3186
5	NEW*TRT		28	1.85527717	1.93230928	9	0.96	0.3621
6	NEW*TRT		30	1.81072275	1.93311801	9	0.94	0.3734
7	C1*R1*REP	4		1.73101272	1.85245416	9	0.93	0.3745
8	NEW*TRT		16	1.54679253	1.94313336	9	0.80	0.4465
9	NEW*TRT		22	1.54645580	1.93311801	9	0.80	0.4443
10	C1*REP	4		1.25643193	1.09118038	9	1.15	0.2792
11	NEW*TRT		24	1.25209662	1.94313336	9	0.64	0.5354
12	NEW*TRT		11	1.23086038	1.90869357	9	0.64	0.5351
13	NEW*TRT		19	1.17618212	1.90869357	9	0.62	0.5530
14	NEW*TRT		12	1.11283909	1.93230928	9	0.58	0.5788
15	NEW*TRT		18	1.01457415	1.94260482	9	0.52	0.6141
16	R1*REP	1		1.01019332	1.33546047	9	0.76	0.4687
17	NEW*TRT		23	1.00479517	1.99102006	9	0.50	0.6259
18	NEW*TRT		20	0.93494169	1.93230928	9	0.48	0.6400
19	NEW*TRT		21	0.92045869	1.93273116	9	0.48	0.6452
20	NEW*TRT		17	0.88317994	1.94374142	9	0.45	0.6603
21	NEW*TRT		13	0.83974581	1.93273116	9	0.43	0.6742
22	NEW*TRT		14	0.40203254	1.93311801	9	0.21	0.8399
23	C1*REP	2		0.34480113	1.09118038	9	0.32	0.7592
24	C1*R1*REP	1		0.28936528	1.85245416	9	0.16	0.8793
25	NEW*TRT		33	0.00000000	2.42417557	9	0.00	1.0000
26	NEW*TRT		34	0.00000000	2.42417557	9	0.00	1.0000
27	NEW*TRT		35	0.00000000	2.42417557	9	0.00	1.0000
28	NEW*TRT		36	0.00000000	2.42417557	9	0.00	1.0000
29	NEW*TRT		37	0.00000000	2.42417557	9	0.00	1.0000
30	NEW*TRT		38	0.00000000	2.42417557	9	0.00	1.0000
31	NEW*TRT		39	0.00000000	2.42417557	9	0.00	1.0000
32	NEW*TRT		40	0.00000000	2.42417557	9	0.00	1.0000
33	C1*REP	1		-0.02662262	1.09118038	9	-0.02	0.9811
34	REP	2		-0.42232220	1.86295604	9	-0.23	0.8257
35	C1*R1*REP	3		-0.46971222	1.85245416	9	-0.25	0.8055
36	NEW*TRT		25	-0.53275905	1.94374142	9	-0.27	0.7902
37	NEW*TRT		26	-0.55027490	1.94260482	9	-0.28	0.7834

38	NEW*TRT		15	-0.60995214	1.99102006	9	-0.31	0.7663
39	R1*REP	3		-0.77362810	1.33546047	9	-0.58	0.5766
40	R1*REP	4		-0.91895723	1.33546047	9	-0.69	0.5087
41	NEW*TRT		31	-1.01254232	1.99102006	9	-0.51	0.6233
42	C1*REP	3		-1.02947994	1.09118038	9	-0.94	0.3701
43	C1*R1*REP	2		-1.32767888	1.85245416	9	-0.72	0.4917
44	NEW*TRT		2	-1.38564933	1.94260482	9	-0.71	0.4937
45	NEW*TRT		29	-1.39513647	1.93273116	9	-0.72	0.4887
46	NEW*TRT		1	-1.42624812	1.94374142	9	-0.73	0.4818
47	NEW*TRT		32	-1.45720674	1.94313336	9	-0.75	0.4724
48	NEW*TRT		4	-1.56655327	1.93230928	9	-0.81	0.4384
49	NEW*TRT		3	-1.58335059	1.90869357	9	-0.83	0.4282
50	REP	3		-1.67547560	1.86295604	9	-0.90	0.3919
51	NEW*TRT		5	-1.76704354	1.93273116	9	-0.91	0.3844
52	NEW*TRT		6	-1.78805600	1.93311801	9	-0.92	0.3791
53	NEW*TRT		7	-1.91714185	1.99102006	9	-0.96	0.3608
54	NEW*TRT		9	-2.24587207	1.94374142	9	-1.16	0.2777
55	NEW*TRT		10	-2.47310037	1.94260482	9	-1.27	0.2349
56	REP	1		-2.75311559	1.86295604	9	-1.48	0.1736



## Chapter 28

# Augmented Row-Column Design and Trend Analyses

Walter T. Federer  
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### *Purpose*

To obtain estimates of augmented treatments under a mixed model.

### *Data*

The fifteen-row by twelve-column designed data set, as outlined in Federer (1998), is used in this chapter. There are two checks repeated  $r = 30$  times each and 120 new or augmented treatments each included once. Since the row-column design was not connected, in the sense that not all row, column, and treatment effects have solutions, it was necessary to use functions of row and column effects. Orthogonal polynomial regressions up to tenth degree for columns and up to twelfth degree for rows were computed. Those regressions with F-values lower than the 25 percent level were omitted from the model. Since row-column orientation may not be in the same direction as gradients in the experiment, interactions of row and column regressions were employed to account for the variation.

The treatments are divided into fixed effects (checks) and random effects (augmented treatments). An ordering of treatment effects from highest to lowest is useful since large numbers of augmented treatments are usually encountered in this type of screening experiment. The following SAS program constructs orthogonal polynomial coefficients.

## References

- Federer, W.T. (1998). Recovery of interblock, intergradient, and intervariety information in incomplete block and lattice rectangle designed experiments. *Biometrics* 54(2):471-481.
- Wolfinger, R.D., Federer, W.T., and Cordero-Brana, O. (1997). Recovering information in augmented designs, using SAS PROC GLM and PROC MIXED. *Agronomy Journal* 89:856-859.

## SAS Code

```

/* ---Create orthogonal polynomial regression coefficients.---*/
proc iml;
  opn12=orpol(1:12,10); /*---12 rows and up to tenth degree coeffi-
    cients---*/
  opn12[,1] = (1:12) `;
  op12=opn12;
  create opn12 from opn12[colname={'COL' 'C1' 'C2' 'C3' 'C4' 'C5'
  'C6' 'C7' 'C8' 'C9' 'C10'}]; append from opn12;
  close opn12; run;
  opn15 = orpol(1:15,12); /*---15 columns , up to 12th degree coeffi-
    cients---*/
  opn15[,1]=(1:15) `;
  op15 = opn15;
  create opn15 from opn15[colname={'ROW' 'R1' 'R2' 'R3' 'R4' 'R5'
  'R6' 'R7' 'R8' 'R9' 'R10' 'R11' 'R12'}]; append from opn15;
  close opn15;
run;
/* The data set augmercl.dat contained responses for grain weight and
  eight other characteristics of the 122 wheat genotypes (treat-
  ments) and comes from site number 1. */
data augsitel;
  infile 'augmercl.dat';
  input site col row trt grainwt ca cb cc cd ra rb rc rd;
/* The following statements partition the 122 treatments into two
  sets, checks (fixed) and new (treated as random). */
  if (trt>120) then new = 0; else new = 1; if (new) then trtn= 999;
  else trtn=trt;
/* The following steps create the data set augbig for analyses. */
data augbig; set augsitel;
  idx = _n_;
run;
proc sort data = augbig;
  by col; run;
data augbig;
  merge augbig opn12;
  by col; run;
proc sort data = augbig;
  by row; run;
data augbig;
  merge augbig opn15;
  by row; run;
proc sort data = augbig;

```

```

by idx;
run;
/* Exploratory model selection resulted in the following model for
   this data set. Residuals may also be obtained. */
proc glm data = augbig;
  class row col trt trtn;
  model grainwt =C1 C2 C3 C4 C6 C8 R1 R2 R4 R8 R10 R1*C1
  R1*C2 R1*C3 trt;
  output out = subres R = resid; proc print; /*---Printed in augbig---
  -*/
run;
/* "info nobound" may be included in the following statement if this
   type of solution for variance components is desired. Also, if
   ANOVA solutions for the variance components are desired, the
   PARMS procedure statement may be used after the random statement
   in PROC MIXED. REML solutions may not be appropriate for mean
   squares with few degrees of freedom. The trt*new in the random
   statement is used when augmented treatments are treated as random
   effects. */
proc mixed data = augbig;
  class row col trt trtn;
  model grainwt = trtn/solution;
  random R1 R2 R4 R8 R10 C1 C2 C3 C4 C6 C8 R1*C1 R1*C2 R1*C3
  trt*new / solution;
  lsmeans trtn;
  make 'solutionr' out = sr noprint;
run;
/* The following statements arrange the solutions in descending order.
   */
proc sort data = sr;
  by descending _EST_ ;
proc print;
run;

```

Using the data and program described above, an abbreviated output is given below:

```

Class Levels      Values
ROW      15      1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
COL      12      1 2 3 4 5 6 7 8 9 10 11 12
TRT     122      1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22
                23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41
                42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60
                61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79
                80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98
                99 100 101 102 103 104 105 106 107 108 109 110 111 112
                113 114 115 116 117 118 119 120 121 122

```

```
TRTN      3      121 122 999 /* Checks are number 121 and 122. */
```

Dependent Variable: GRAINWT

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	135	1685564.291	12485.661	3.62	0.0001
Error	44	151761.820	3449.132		
Corrected Total	179	1837326.111			
	R-Square	C.V.	Root MSE	GRAINWT Mean	
	0.917401	6.664109	58.72931	881.2778	

Dependent Variable: GRAINWT

Source	DF	Type I SS	Mean Square	F Value	Pr > F
C1	1	7.053	7.053	0.00	0.9641
C2	1	78620.049	78620.049	22.79	0.0001
C3	1	31357.514	31357.514	9.09	0.0043
C4	1	35185.066	35185.066	10.20	0.0026
C6	1	15954.687	15954.687	4.63	0.0370
C8	1	88778.180	88778.180	25.74	0.0001
R1	1	130227.001	130227.001	37.76	0.0001
R2	1	3182.964	3182.964	0.92	0.3420
R4	1	34117.771	34117.771	9.89	0.0030
R8	1	20274.909	20274.909	5.88	0.0195
R10	1	16821.594	16821.594	4.88	0.0325
C1*R1	1	138479.979	138479.979	40.15	0.0001
C2*R1	1	61605.531	61605.531	17.86	0.0001
C3*R1	1	13248.961	13248.961	3.84	0.0564
TRT	121	1017703.032	8410.769	2.44	0.0005

Source	DF	Type III SS	Mean Square	F Value	Pr > F
C1	1	12952.986	12952.986	3.76	0.0591
C2	1	48712.489	48712.489	14.12	0.0005
C3	1	42867.475	42867.475	12.43	0.0010
C4	1	22613.228	22613.228	6.56	0.0140
C6	1	31220.232	31220.232	9.05	0.0043
C8	1	77300.177	77300.177	22.41	0.0001
R1	1	28677.708	28677.708	8.31	0.0061
R2	1	12832.205	12832.205	3.72	0.0602
R4	1	4992.843	4992.843	1.45	0.2354
R8	1	20170.221	20170.221	5.85	0.0198
R10	1	15068.496	15068.496	4.37	0.0424
C1*R1	1	52885.122	52885.122	15.33	0.0003
C2*R1	1	24976.581	24976.581	7.24	0.0100
C3*R1	1	7998.357	7998.357	2.32	0.1350
TRT	121	1017703.032	8410.769	2.44	0.0005

## The MIXED Procedure

## Covariance Parameter Estimates (REML)

Cov Parm	Estimate
R1	9685.7206435
R2	147.76385914
R4	2382.8694456
R8	1165.7087131
R10	1055.8582605
C1	0.00000000
C2	5739.9404029
C3	2401.8203763
C4	1702.2868779
C6	1375.7002135
C8	6678.6086902
R1*C1	125150.99858
R1*C2	62327.029930
R1*C3	7191.3342088
NEW*TRT	2880.2792533
Residual	4385.0838420

## Solution for Fixed Effects

Effect	TRTN	Estimate	Std Error	DF	t	Pr >  t
INTERCEPT		887.85653363	7.78342790	44	114.07	0.0001
TRTN	121	22.56422549	14.52418333	44	1.55	0.1275
TRTN	122	-62.03676062	14.42385015	44	-4.30	0.0001

Least Squares Means						
Effect	TRTN	LSMEAN	Std Error	DF	t	Pr >  t
TRTN	121	910.42075912	12.23674167	44	74.40	0.0001
TRTN	122	825.81977301	12.15736600	44	67.93	0.0001
TRTN	999	887.85653363	7.78342790	44	114.07	0.0001

15 highest new treatment effects

OBS	EFFECT	TRT	EST	SEPRD	DF	T	PT
1	R1*C1		345.50045585	76.02914755	44	4.54	0.0001
2	R1		95.98535922	21.73762881	44	4.42	0.0001
3	NEW*TRT	60	86.34108807	42.34708520	44	2.04	0.0475
4	C8		79.38460062	19.40852139	44	4.09	0.0002
5	NEW*TRT	21	62.77643482	43.26254487	44	1.45	0.1539
6	R1*C3		62.42608658	57.39674225	44	1.09	0.2827
7	NEW*TRT	11	58.69112792	43.23892480	44	1.36	0.1816
8	NEW*TRT	99	56.51372478	42.26198657	44	1.34	0.1880
9	NEW*TRT	2	54.08461760	42.75771851	44	1.26	0.2126
10	NEW*TRT	35	49.26910001	42.25202699	44	1.17	0.2499
11	NEW*TRT	118	49.05376892	42.18955585	44	1.16	0.2512
12	NEW*TRT	58	48.88460726	42.12266951	44	1.16	0.2521
13	NEW*TRT	111	46.12302563	42.56352985	44	1.08	0.2844
14	C3		45.39408465	18.47150180	44	2.46	0.0180
15	R4		44.40038633	20.28481411	44	2.19	0.0340
16	NEW*TRT	46	44.15378862	42.18922373	44	1.05	0.3010
17	NEW*TRT	120	44.13816913	42.42913604	44	1.04	0.3039
18	NEW*TRT	61	42.88822110	42.53422618	44	1.01	0.3188
19	NEW*TRT	38	39.16602034	42.24545264	44	0.93	0.3589
20	NEW*TRT	82	38.75002538	42.56505326	44	0.91	0.3676
21	NEW*TRT	90	37.87336561	42.33458245	44	0.89	0.3759

.....Random effects 21 to 119 deleted.

15 lowest new treatment effects.

120	NEW*TRT	5	-36.65859703	42.24564023	44	-0.87	0.3902
121	NEW*TRT	23	-36.94625121	43.22631392	44	-0.85	0.3973
122	NEW*TRT	107	-40.26108079	42.27021281	44	-0.95	0.3461
123	NEW*TRT	55	-40.71903829	42.17831063	44	-0.97	0.3396
124	NEW*TRT	42	-40.77369290	42.69072074	44	-0.96	0.3447
125	NEW*TRT	56	-41.41021039	42.21331886	44	-0.98	0.3320
126	NEW*TRT	28	-41.70085605	42.31372687	44	-0.99	0.3298
127	NEW*TRT	17	-49.15984900	42.44192942	44	-1.16	0.2530
128	NEW*TRT	6	-52.33527614	42.15283284	44	-1.24	0.2210
129	NEW*TRT	51	-57.85952344	42.47160123	44	-1.36	0.1800
130	C2		-73.26618742	19.28735943	44	-3.80	0.0004
131	NEW*TRT	52	-75.09659823	42.62419762	44	-1.76	0.0850
132	NEW*TRT	43	-80.06306299	42.56340110	44	-1.88	0.0666
133	NEW*TRT	44	-80.23408721	42.42893008	44	-1.89	0.0652
134	NEW*TRT	81	-85.99507895	42.43715136	44	-2.03	0.0488
135	NEW*TRT	50	-91.58752547	42.56624934	44	-2.15	0.0370
136	R1*C2		-238.5012759	73.78434826	44	-3.23	0.0023





## Chapter 29

# PROC GLM and PROC MIXED Codes for Trend Analyses for Row-Column-Designed Experiments

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Russell D. Wolfinger

### *Purpose*

The program outlined in this chapter may be used for a variety of response models in row-column experiments. The example used to illustrate the steps in this program is a randomized complete block design (RCBD) that was laid out as an eight-row by seven-column field experiment. The experiment with data is described in Federer and Schlotfeldt (1954). The data include twenty plant heights in centimeters for seven different treatments. Since the experiment was planted as an eight-row by seven-column arrangement, an RCBD analysis may not be appropriate. The SAS code is written to compare five different response models that account for the spatial variation present. Variation orientation was different than the row-column layout.

SAS PROC GLM and PROC MIXED codes are presented for standard textbook analyses of variance for RCBD and for row-column design. These are followed by codes for trend analyses using standardized orthogonal polynomial regressions for rows and columns and for interaction of row and column regressions. A trend model using row, column, and interactions of row and column regressions appears to control the variation for this experiment. A PROC GLM analysis of variance and residuals is useful in exploratory model selection that takes account of spatial variation in the experiment. A PROC MIXED analysis is then used to recover information from the random effects (Federer, 1998; Federer and Wolfinger, 1998).

## References

- Federer, W.T. (1998). Recovery of interblock, intergradient, and intervariety information in incomplete block and lattice rectangle designed experiments. *Biometrics* 54(2):471-481.
- Federer, W.T. and Schlotfeldt, C.S. (1954). The use of covariance to control gradients in experiments. *Biometrics* 10:282-290.
- Federer, W.T. and Wolfinger, R.D. (1998). SAS PROC GLM and PROC MIXED code for recovering inter-effect information. *Agronomy Journal* 90:545-551.

## SAS Code

```

/*---input the data---*/
data colrow;
  input height row col trt;
  /*---rescale data for stability---*/
  y = height/1000;
  datalines;
1299.2 1 1 6
 875.9 1 2 7
 960.7 1 3 4
1004.0 1 4 3
1173.2 1 5 1
1031.9 1 6 2
1421.1 1 7 5
1369.2 2 1 2
 844.2 2 2 5
 968.7 2 3 6
 975.5 2 4 7
1322.4 2 5 3
1172.6 2 6 1
1418.9 2 7 4
1169.5 3 1 1
 975.8 3 2 5
 873.4 3 3 3
 797.8 3 4 7
1069.7 3 5 2
1093.3 3 6 6
1169.6 3 7 4
1219.1 4 1 6
 971.7 4 2 1
 607.6 4 3 7
1000.0 4 4 4
1343.3 4 5 2
 999.4 4 6 5
1181.3 4 7 3
1120.0 5 1 6
 827.0 5 2 7
 671.9 5 3 4
 972.2 5 4 3
1083.7 5 5 1
1146.9 5 6 2

```

```

993.8 5 7 5
1031.5 6 1 7
846.5 6 2 2
667.8 6 3 4
853.6 6 4 3
1087.1 6 5 1
990.2 6 6 5
1021.9 6 7 6
1076.4 7 1 2
917.9 7 2 1
627.6 7 3 5
776.4 7 4 6
960.4 7 5 3
852.4 7 6 7
1006.2 7 7 4
1099.6 8 1 4
947.4 8 2 5
787.1 8 3 2
898.3 8 4 1
1174.9 8 5 3
1003.3 8 6 6
947.6 8 7 7
run;

/*---code to construct orthogonal polynomials---*/
proc iml;
  /*---7 columns and up to 6th degree polynomials---*/
  opn4=orpol(1:7,6);
  opn4[,1] = (1:7)`;
  op4= opn4;
  create opn4 from opn4[colname={'col' 'c1' 'c2' 'c3' 'c4' 'c5'
    'c6'}];
  append from opn4;
  close opn4;
  /*---8 rows and up to 7th degree polynomials---*/
  opn3=orpol(1:8,7);
  opn3[,1] = (1:8)`;
  op3 = opn3;
  create opn3 from opn3[colname={'row' 'r1' 'r2' 'r3' 'r4' 'r5'
    'r6' 'r7'}];
  append from opn3;
  close opn3;
run;
/*---merge in polynomial coefficients---*/
data rcbig;
  set colrow;
  idx = _n_;
proc sort data=rcbig;
  by col;
data rcbig;
  merge rcbig opn4;
  by col;
proc sort data=rcbig;
  by row;
data rcbig;
  merge rcbig opn3;
  by row;

```

```

proc sort data = rcbig;
  by idx;
run;
/*---3d plot of data, one can also substitute row and column variables
as well as residuals for
  y to see how they model the trend---*/
proc g3d data=rcbig;
  plot row*col=y / rotate=20;
run;
/*---standard rcbd analysis with rows as blocks; treatments are not
significantly different---*/
/*---fixed-effects row model for RCBD---*/
proc glm data=rcbig;
  class row col trt;
  model y = row trt;
  output out=subres r=resid;
run;
/*---standard row-column analysis fits much better than RBCD, and now
treatment 7 is significantly different---*/
/*---fixed-effects row-column model---*/
proc glm data=rcbig;
  class row col trt;
  model y = row col trt;
  output out=subres r=resid;
run;
/*---model for random differential gradients within rows; does not fit
as well as row-column model, but results are similar---*/
/*---fixed-effects model for gradients within rows ---*/
proc glm data=rcbig;
  class row col trt;
  model y = trt row c2*row c3*row c4*row;
  output out=subres r=resid;
run;
/*---Fixed-effects polynomial model; it may be that a trend and analy-
sis is desired in that only certain polynomial regressions are
needed to explain the row and column variation. Also, since spa-
tial variation may not be in the row-column orientation of the
experiment, interactions of regressions may be needed to account
for this type of spatial variation. Of the 13 polynomial regres-
sions for rows and columns and the 16 interactions ci*rj, for i,
j = 1, 2, 3, and 4, those that had F-values greater than F at the
25% level were retained in the response model.---*/
proc glm data=rcbig;
  class row col trt;
  model y = trt c1 c2 c3 c5 r1 r2 r3 r5 r6 r7 c1*r1 c2*r1 c2*r3 c3*r2
  c4*r1 c4*r2;
  output out=subres r=resid;
run;
/*---random polynomial coefficient model---*/
proc mixed data=rcbig;
  class row col trt;
  model y = trt / ddfm=res;
  random c1 c2 c3 c5 r1 r2 r3 r5 r6 r7 c1*r1 c2*r1 c2*r3 c3*r2 c4*r1
  c4*r2;
  lsmeans trt / diff adjust=tukey;
run;

```

```

/*---Since the row and column variations were quite un-patterned,
   i.e., only c4, c6, and r4 were not in the model, the following
   analysis may be more appropriate for this data set.---*/
proc glm data=rcbig;
  class row col trt;
  model y = row col trt c1*r1 c2*r1 c2*r3 c3*r2 c4*r1 c4*r2;
run;
/*---combination model---*/
proc mixed data=rcbig;
  class row col trt;
  model y = trt / ddfm=res;
  random row col c1*r1 c2*r1 c2*r3 c3*r2 c4*r1 c4*r2
  repeated / type=sp(exp)(row col) subject=intercept;
  lsmeans trt / diff adjust=tukey;
run;

```

An abbreviated output from this code is presented below:

*RCBD ANOVA*

Dependent Variable:	Y	Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	13	0.66219035	0.05093772	1.69	0.1004
Error	42	1.26958627	0.03022824		
Corrected Total	55	1.93177662			
	R-Square	C.V.	Root MSE		Y Mean
	0.342788	17.17205	0.173863		1.012475

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ROW	7	0.38831490	0.05547356	1.84	0.1056
TRT	6	0.27387545	0.04564591	1.51	0.1985
Source	DF	Type III SS	Mean Square	F Value	Pr > F
ROW	7	0.38831490	0.05547356	1.84	0.1056
TRT	6	0.27387545	0.04564591	1.51	0.1985

*Row-column ANOVA*

Dependent Variable:	Y	Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	19	1.66711058	0.08774266	11.93	0.0001
Error	36	0.26466604	0.00735183		
Corrected Total	55	1.93177662			
	R-Square	C.V.	Root MSE		Y Mean
	0.862993	8.468638	0.085743		1.012475

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ROW	7	0.38831490	0.05547356	7.55	0.0001
COL	6	1.15907213	0.19317869	26.28	0.0001
TRT	6	0.11972355	0.01995392	2.71	0.0281
Source	DF	Type III SS	Mean Square	F Value	Pr > F
ROW	7	0.38831490	0.05547356	7.55	0.0001
COL	6	1.00492023	0.16748671	22.78	0.0001
TRT	6	0.11972355	0.01995392	2.71	0.0281

*Gradients within rows ANOVA*

Dependent Variable:	Y	Sum of	Mean		
Source	F	Squares	Square	F Value	Pr > F
Model	37	1.72819875	0.04670807	4.13	0.0011
Error	18	0.20357788	0.01130988		
Corrected Total	55	1.93177662			

R-Square	C.V.	Root MSE	Y Mean
0.894616	10.50376	0.106348	1.012475

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
TRT	6	0.27387545	0.04564591	4.04	0.0098
ROW	7	0.38831490	0.05547356	4.90	0.0030
C2*ROW	8	0.60283912	0.07535489	6.66	0.0004
C3*ROW	8	0.32440799	0.04055100	3.59	0.0116
C4*ROW	8	0.13876129	0.01734516	1.53	0.2142
Source	DF	Type III SS	Mean Square	F Value	Pr > F
TRT	6	0.25638292	0.04273049	3.78	0.0130
ROW	7	0.38831490	0.05547356	4.90	0.0030
C2*ROW	8	0.59754712	0.07469339	6.60	0.0004
C3*ROW	8	0.32649657	0.04081207	3.61	0.0113
C4*ROW	8	0.13876129	0.01734516	1.53	0.2142

Trend ANOVA

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	22	1.79302842	0.08150129	19.38	0.0001
Error	33	0.13874820	0.00420449		
Corrected Total	55	1.93177662			

R-Square	C.V.	Root MSE	Y Mean
0.928176	6.404311	0.064842	1.012475

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
TRT	6	0.27387545	0.04564591	10.86	0.0001
C1	1	0.09681321	0.09681321	23.03	0.0001
C2	1	0.53598746	0.53598746	127.48	0.0001
C3	1	0.22278336	0.22278336	52.99	0.0001
C5	1	0.13314475	0.13314475	31.67	0.0001
R1	1	0.27808763	0.27808763	66.14	0.0001
R2	1	0.02147675	0.02147675	5.11	0.0305
R3	1	0.04373966	0.04373966	10.40	0.0028
R5	1	0.02033078	0.02033078	4.84	0.0350
R6	1	0.01185195	0.01185195	2.82	0.1026
R7	1	0.01086024	0.01086024	2.58	0.1175
C1*R1	1	0.00973558	0.00973558	2.32	0.1376
C2*R3	1	0.01107563	0.01107563	2.63	0.1141
C3*R2	1	0.04705541	0.04705541	11.19	0.0021
R1*C4	1	0.04578624	0.04578624	10.89	0.0023
R2*C4	1	0.00916801	0.00916801	2.18	0.1492
C2*R1	1	0.02125631	0.02125631	5.06	0.0313

Source	DF	Type III SS	Mean Square	F Value	Pr > F
TRT	6	0.16044158	0.02674026	6.36	0.0002
C1	1	0.06777963	0.06777963	16.12	0.0003
C2	1	0.44309828	0.44309828	105.39	0.0001
C3	1	0.24999420	0.24999420	59.46	0.0001
C5	1	0.13222351	0.13222351	31.45	0.0001
R1	1	0.27808763	0.27808763	66.14	0.0001
R2	1	0.02147675	0.02147675	5.11	0.0305
R3	1	0.04373966	0.04373966	10.40	0.0028
R5	1	0.02033078	0.02033078	4.84	0.0350
R6	1	0.01185195	0.01185195	2.82	0.1026
R7	1	0.01086024	0.01086024	2.58	0.1175
C1*R1	1	0.00914040	0.00914040	2.17	0.1498
C2*R3	1	0.01580043	0.01580043	3.76	0.0611
C3*R2	1	0.04870965	0.04870965	11.59	0.0018
R1*C4	1	0.04431490	0.04431490	10.54	0.0027
R2*C4	1	0.01028565	0.01028565	2.45	0.1273
C2*R1	1	0.02125631	0.02125631	5.06	0.0313

Covariance Parameter Estimates (REML)

Cov Parm	Estimate
C1	0.00843481
C2	0.06534973
C3	0.03944736
C5	0.01928089
R1	0.03912510
R2	0.00246616
R3	0.00564660
R5	0.00230245
R6	0.00109118
R7	0.00094951
C1*R1	0.00559139
C2*R1	0.01769383
C2*R3	0.01540992
C3*R2	0.04762647
R1*C4	0.04172363
R2*C4	0.00559275
Residual	0.00421378

Least Squares Means

Effect	TRT	LSMEAN	Std Error	DF	t	Pr >  t
TRT	1	1.03145832	0.02506657	33	41.15	0.0001
TRT	2	1.03632328	0.02409811	33	43.00	0.0001
TRT	3	1.08344910	0.02517848	33	43.03	0.0001
TRT	4	1.06286153	0.02574839	33	41.28	0.0001
TRT	5	0.95488139	0.02447435	33	39.02	0.0001
TRT	6	1.01891389	0.02524623	33	40.36	0.0001
TRT	7	0.89943749	0.02437852	33	36.89	0.0001

Row-column and interaction of regressions or combination ANOVA

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	25	1.79923177	0.07196927	16.29	0.0001
Error	30	0.13254485	0.00441816		
Corrected Total	55	1.93177662			

R-Square	C.V.	Root MSE	Y Mean
0.931387	6.565027	0.066469	1.012475

Dependent Variable: Y

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ROW	7	0.38831490	0.05547356	12.56	0.0001
COL	6	1.15907213	0.19317869	43.72	0.0001
TRT	6	0.11972355	0.01995392	4.52	0.0023
C1*R1	1	0.00957865	0.00957865	2.17	0.1513
R1*C2	1	0.01825578	0.01825578	4.13	0.0510
C2*R3	1	0.00785874	0.00785874	1.78	0.1923
C3*R2	1	0.04166095	0.04166095	9.43	0.0045
R1*C4	1	0.04499265	0.04499265	10.18	0.0033
R2*C4	1	0.00977442	0.00977442	2.21	0.1473

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ROW	7	0.38831490	0.05547356	12.56	0.0001
COL	6	1.01906239	0.16984373	38.44	0.0001
TRT	6	0.11791625	0.01965271	4.45	0.0025
C1*R1	1	0.00939749	0.00939749	2.13	0.1551
R1*C2	1	0.02030565	0.02030565	4.60	0.0403



C2*R3	1	0.01290053	0.01290053	2.92	0.0978
C3*R2	1	0.04269878	0.04269878	9.66	0.0041
R1*C4	1	0.04417127	0.04417127	10.00	0.0036
R2*C4	1	0.00977442	0.00977442	2.21	0.1473

## Covariance Parameter Estimates (REML)

Cov Parm	Subject	Estimate
ROW		0.00729090
COL		0.02179930
C1*R1		0.00584283
R1*C2		0.01598859
C2*R3		0.01084891
C3*R2		0.04046662
R1*C4		0.04157133
R2*C4		0.00474734
SP (EXP) INTERCEPT		-0.00000000
Residual		0.00443729

## Least Squares Means

Effect	TRT	LSMEAN	Std Error	DF	t	Pr >  t
TRT	1	1.03279947	0.06849923	49	15.08	0.0001
TRT	2	1.04085965	0.06827608	49	15.24	0.0001
TRT	3	1.07188050	0.06898348	49	15.54	0.0001
TRT	4	1.05156492	0.06912807	49	15.21	0.0001
TRT	5	0.96546152	0.06879786	49	14.03	0.0001
TRT	6	1.02168355	0.06853511	49	14.91	0.0001
TRT	7	0.90307540	0.06835031	49	13.21	0.0001

## Differences of Least Squares Means

Effect	TRT	TRT	Difference	Std Error	DF	t	Pr >  t
TRT	1	2	-0.00806018	0.03504670	49	-0.23	0.8191
TRT	1	3	-0.03908103	0.03618394	49	-1.08	0.2854
TRT	1	4	-0.01876545	0.03958021	49	-0.47	0.6375
TRT	1	5	0.06733794	0.03740107	49	1.80	0.0780
TRT	1	6	0.01111592	0.03811781	49	0.29	0.7718
TRT	1	7	0.12972407	0.03761943	49	3.45	0.0012
TRT	2	3	-0.03102085	0.03841115	49	-0.81	0.4232
TRT	2	4	-0.01070527	0.03929203	49	-0.27	0.7864
TRT	2	5	0.07539812	0.03608589	49	2.09	0.0419
TRT	2	6	0.01917610	0.03569990	49	0.54	0.5936
TRT	2	7	0.13778425	0.03651435	49	3.77	0.0004
TRT	3	4	0.02031558	0.03754102	49	0.54	0.5909
TRT	3	5	0.10641897	0.04097063	49	2.60	0.0124
TRT	3	6	0.05019695	0.03892509	49	1.29	0.2033
TRT	3	7	0.16880510	0.03807134	49	4.43	0.0001
TRT	4	5	0.08610340	0.03927030	49	2.19	0.0331
TRT	4	6	0.02988137	0.03847642	49	0.78	0.4411
TRT	4	7	0.14848952	0.03787633	49	3.92	0.0003
TRT	5	6	-0.05622202	0.03756983	49	-1.50	0.1409
TRT	5	7	0.06238613	0.03639929	49	1.71	0.0929
TRT	6	7	0.11860815	0.03565169	49	3.33	0.0017

## Differences of Least Squares Means

Adjustment	Adj P
Tukey-Kramer	1.0000
Tukey-Kramer	0.9310
Tukey-Kramer	0.9991

Tukey-Kramer	0.5541
Tukey-Kramer	0.9999
Tukey-Kramer	0.0187
Tukey-Kramer	0.9831
Tukey-Kramer	1.0000
Tukey-Kramer	0.3749
Tukey-Kramer	0.9981
Tukey-Kramer	0.0074
Tukey-Kramer	0.9980
Tukey-Kramer	0.1492
Tukey-Kramer	0.8534
Tukey-Kramer	0.0010
Tukey-Kramer	0.3182
Tukey-Kramer	0.9862
Tukey-Kramer	0.0048
Tukey-Kramer	0.7455
Tukey-Kramer	0.6103
Tukey-Kramer	0.0260



## Chapter 30

# SAS/GLM and SAS/MIXED for Trend Analyses Using Fourier and Polynomial Regression for Centered and Noncentered Variates

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### *Purpose*

Spatial variations that are cyclic in nature should have statistical procedures to account for their occurrence. Since Fourier polynomial regression is a procedure that fits cyclic variations, a code is given in this chapter for such analyses. The data set used to illustrate the code's application is an eight-row, seven-column experiment on tobacco plant heights by Federer and Schlottfeldt (1954). The experiment was designed as a randomized complete block design, but was laid out as an eight-row by seven-column design instead. The laying out of an RCBD in a row-column arrangement is appropriate. However, the analysis needs to take the layout and any other type of variation into account. The spatial variation in the experimental area was noncyclical and not entirely row-column oriented. The Fourier regression model would not be expected to perform well with this data set because the variation was not cyclic. If it is desired to use noncentered polynomial regression, a code for this is also given in this chapter. Note that which regressions to retain in the model will need to be determined from a Type I rather than a Type III or IV analysis.

Codes for trend analyses are presented in the following order: Fourier regression trend analysis (FRTA), noncentered variate polynomial regression trend analysis (NPRTA), randomized complete block design (RCBD),

row-column design (RCD), orthogonal polynomial (centered variates) regression trend analysis (PRTA), and a mixture of row-column and orthogonal polynomial regression trend analyses. The last is considered to be the appropriate model for this data set. Since only three orthogonal polynomials—degrees 4 and 6 in columns and degree 4 in rows, c4, c6, and r4—were omitted in the next to last analysis, it was decided to use the last analysis listed as an appropriate model to explain the spatial variation. For this model, the blocking effect parameters were taken to be random for the SAS/MIXED procedure and treatment estimates and means were obtained. The code is useful for exploratory model selection in patterning spatial variation.

## References

- Federer, W.T. (1998). Recovery of interblock, intergradient, and intervariety information in incomplete block and lattice rectangle designed experiments. *Biometrics* 54(2):471-481.
- Federer, W.T. and Schlotfeldt, C.S. (1954). The use of covariance to control gradients in experiments. *Biometrics* 10:282-290 [Errata, *Biometrics* 11:251, 1955].

## SAS Codes

```

/--The SAS codes for obtaining standard textbook RCBD and RCD analy-
sis, FRTA, NPRTA, and PRTA analyses are given below:-- */
data colrow;
  infile 'colrow.dat';
  input Yield row col Trt;

/--code for Fourier polynomials, FRTA--*/
  NTrt = 7; Nrow = 8; Ncol = 7;
  Frc1 = Sin(2*3.14159*col/Ncol)      ;
  Frc2 = Cos(2*3.14159*col/Ncol)     ;
  Frr1 = Sin(2*3.14159*row/Nrow)     ;
  Frr2 = Cos(2*3.14159*row/Nrow)     ;
/--code for non-centered polynomials, NPRTA--*/
  pc1= col; pc2=col**2;pc3=col**3;pc4=col**4;pc5=col**5;pc6=col**6;
  pr1= row; pr2=row**2;pr3=row**3;pr4=row**4;pr5=row**5;
  pr6=row**6; pr7 = row**7 ;
  run;
/--code for ANOVA using Fourier series, FRTA--*/
proc glm data = colrow ;
  class Trt row col ;
  model Yield = Trt Frc1 Frc2 Frr1 Frr2 Frc1*Frr1 Frc1*Frr2
    Frc2*Frr1 Frc2*Frr2;
run;
/--code for ANOVA using non-centered polynomials, NPRTA--*/
proc glm data = colrow;

```

```

class Trt row col ;
model Yield = Trt pc1 pc2 pc3 pc4 pc5 pc6 pr1 pr2 pr3 pr4 pr5 pr6
pr7 pc1*pr1 pc2*pr1 pc2*pr3 pc3*pr2 pc4*pr1 pc4*pr2; run;

/*--code to construct orthogonal polynomials--*/
Proc iml;
/*--7 columns and up to 6th degree polynomials--*/
opn4=orpol(1:7,6);
opn4[,1]=(1:7)`;
op4=opn4;
create opn4 from opn4[colname={'col' 'c1' 'c2' 'c3' 'c4' 'c5' 'c6'}];
append from opn4;
close opn4;
/*--8 rows and up to 7th degree polynomials--*/
opn3=orpol(1:8,7);
opn3[,1]=(1:8)`;
op3=opn3;
create opn3 from opn3[colname={'row' 'r1' 'r2' 'r3' 'r4' 'r5'
'r6' 'r7'}] ;
append from opn3;
close opn3; run;
/*--merge in polynomial coefficients--*/
data rcbig;
set colrow;
idx = _n_;
proc sort data = rcbig;
by col ;
data rcbig ;
merge rcbig opn4;
by col ;
proc sort data = rcbig;
by row ;
data rcbig ;
merge rcbig opn3;
by row ;
proc sort data = rcbig ;
by idx ;
run;
/*--ANOVA for randomized complete blocks (rows), RCBD--*/
Proc Glim data = rcbig ;
Class row Trt ;
Model Yield = row Trt ;
run ;
/*--ANOVA for row-column design, RCD--*/
Proc Glim data = rcbig ;
Class row col Trt ;
Model Yield = row col Trt ;
run;

/*--ANOVA using orthogonal polynomials after omitting regressors
which had an F-value less than the 25% level, PRTA--*/
Proc Glim data = rcbig;
Class Trt row col ;
Model Yield = Trt c1 c2 c3 c5 r1 r2 r3 r5 r6 r7 c1*r1 c2*r1
c2*r3 c3*r2 c4*r1 c4*r2;
run ;

```

```

/*--ANOVA for mixture of row-column and orthogonal polynomial
regression trend analysis--this is the preferred analysis--*/
Proc Glm data = rcbig ; ;
  Class row col Trt ;
  Model Yield = row col Trt c1*r1 c2*r1 c2*r3 c3*r2 c4*r1 c4*r2 ;
Run ;
/*--random blocking effects and fixed Trt effects--*/
Proc Mixed data = rcbig ;
  Class row col Trt ;
  Model Yield = Trt/solution ;
  Random row col c1*r1 c2*r1 c2*r3 c3*r2 c4*r1 c4*r2 ;
  Lsmeans Trt ;
run ;

```

## SAS Program Output (Abbreviated)

### General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value
Model	14	1363645.120	97403.223	7.03
Error	41	568131.505	13856.866	
Corrected Total	55	1931776.625		

R-Square	C.V.	Root MSE	YIELD Mean
0.705902	11.62648	117.7152	1012.475

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
TRT	6	273875.4500	45645.9083	3.29	0.0097
FRC1	1	48018.4941	48018.4941	3.47	0.0698
FRC2	1	702583.1192	702583.1192	50.70	0.0001
FRR1	1	301163.4604	301163.4604	21.73	0.0001
FRR2	1	7263.2834	7263.2834	0.52	0.4732
FRC1*FRR1	1	2486.5375	2486.5375	0.18	0.6741
FRC1*FRR2	1	26380.3457	26380.3457	1.90	0.1751
FRC2*FRR1	1	107.9593	107.9593	0.01	0.9301
FRC2*FRR2	1	1766.4703	1766.4703	0.13	0.7229

Source	DF	Type III SS	Mean Square	F Value	Pr > F
TRT	6	233771.3341	38961.8890	2.81	0.0220
FRC1	1	17663.3134	17663.3134	1.27	0.2655
FRC2	1	718308.7485	718308.7485	51.84	0.0001
FRR1	1	301163.4356	301163.4356	21.73	0.0001
FRR2	1	7263.2583	7263.2583	0.52	0.4732
FRC1*FRR1	1	1924.3838	1924.3838	0.14	0.7113
FRC1*FRR2	1	26805.6766	26805.6766	1.93	0.1718
FRC2*FRR1	1	62.7531	62.7531	0.00	0.9467
FRC2*FRR2	1	1766.4703	1766.4703	0.13	0.7229

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	25	1727731.702	69109.268	10.16	0.0001
Error	30	204044.923	6801.497		
Corrected Total	55	1931776.625			

R-Square	C.V.	Root MSE	YIELD Mean
0.894374	8.145504	82.47119	1012.475

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
TRT	6	273875.4500	45645.9083	6.71	0.0001
PC1	1	96813.2065	96813.2065	14.23	0.0007
PC2	1	535987.4627	535987.4627	78.80	0.0001
PC3	1	222783.3577	222783.3577	32.76	0.0001
PC4	1	17076.3332	17076.3332	2.51	0.1236
PC5	1	130081.1699	130081.1699	19.13	0.0001
PC6	1	2178.7015	2178.7015	0.32	0.5756
PR1	1	278087.6327	278087.6327	40.89	0.0001
PR2	1	21476.7478	21476.7478	3.16	0.0857
PR3	1	43739.6582	43739.6582	6.43	0.0167
PR4	1	1967.8963	1967.8963	0.29	0.5946
PR5	1	20330.7758	20330.7758	2.99	0.0941
PR6	1	11851.9481	11851.9481	1.74	0.1968
PR7	1	10860.2508	10860.2508	1.60	0.2161
PC1*PR1	1	9578.6523	9578.6523	1.41	0.2446
PC2*PR1	1	18255.7824	18255.7824	2.68	0.1118
PC2*PR3	1	518.4962	518.4962	0.08	0.7844
PC3*PR2	1	64.3080	64.3080	0.01	0.9232
PC4*PR1	1	27989.2845	27989.2845	4.12	0.0515
PC4*PR2	1	4214.5876	4214.5876	0.62	0.4374

Source	DF	Type III SS	Mean Square	F Value	Pr > F
TRT	6	99655.69428	16609.28238	2.44	0.0483
PC1	1	98.68785	98.68785	0.01	0.9049
PC2	1	23.75368	23.75368	0.00	0.9533
PC3	1	67.88482	67.88482	0.01	0.9211
PC4	1	561.62765	561.62765	0.08	0.7758
PC5	1	1513.16254	1513.16254	0.22	0.6406
PC6	1	2820.59147	2820.59147	0.41	0.5245
PR1	1	17782.73420	17782.73420	2.61	0.1164
PR2	1	16210.23452	16210.23452	2.38	0.1331
PR3	1	14741.72628	14741.72628	2.17	0.1514
PR4	1	13480.96650	13480.96650	1.98	0.1695
PR5	1	12426.54810	12426.54810	1.83	0.1866
PR6	1	11559.77509	11559.77509	1.70	0.2023
PR7	1	10860.25084	10860.25084	1.60	0.2161
PC1*PR1	1	3426.85586	3426.85586	0.50	0.4833
PC2*PR1	1	6236.00944	6236.00944	0.92	0.3460
PC2*PR3	1	1843.47705	1843.47705	0.27	0.6065
PC3*PR2	1	633.86885	633.86885	0.09	0.7623
PC4*PR1	1	20811.22981	20811.22981	3.06	0.0905



PC4\*PR2 1 4214.58759 4214.58759 0.62 0.4374  
 Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	13	662190.3521	50937.7194	1.69	0.1004
Error	42	1269586.2729	30228.2446		
Corrected Total	55	1931776.6250			

R-Square	C.V.	Root MSE	YIELD Mean
0.342788	17.17205	173.8627	1012.475

## General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ROW	7	388314.9021	55473.5574	1.84	0.1056
TRT	6	273875.4500	45645.9083	1.51	0.1985

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ROW	7	388314.9021	55473.5574	1.84	0.1056
TRT	6	273875.4500	45645.9083	1.51	0.1985

## General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	19	1667110.584	87742.662	11.93	0.0001
Error	36	264666.041	7351.834		
Corrected Total	55	1931776.625			

R-Square	C.V.	Root MSE	YIELD Mean
0.862993	8.468638	85.74284	1012.475

## General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ROW	7	388314.902	55473.557	7.55	0.0001
COL	6	1159072.132	193178.689	26.28	0.0001
TRT	6	119723.549	19953.925	2.71	0.0281

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ROW	7	388314.902	55473.557	7.55	0.0001
COL	6	1004920.232	167486.705	22.78	0.0001
TRT	6	119723.549	19953.925	2.71	0.0281

## General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	22	1793028.425	81501.292	19.38	0.0001
Error	33	138748.200	4204.491		
Corrected Total	55	1931776.625			

R-Square	C.V.	Root MSE	YIELD Mean
----------	------	----------	------------

0.928176    6.404311    64.84205    1012.475  
 General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
TRT	6	273875.4500	45645.9083	10.86	0.0001
C1	1	96813.2065	96813.2065	23.03	0.0001
C2	1	535987.4627	535987.4627	127.48	0.0001
C3	1	222783.3577	222783.3577	52.99	0.0001
C5	1	133144.7539	133144.7539	31.67	0.0001
R1	1	278087.6327	278087.6327	66.14	0.0001
R2	1	21476.7478	21476.7478	5.11	0.0305
R3	1	43739.6582	43739.6582	10.40	0.0028
R5	1	20330.7758	20330.7758	4.84	0.0350
R6	1	11851.9481	11851.9481	2.82	0.1026
R7	1	10860.2434	10860.2434	2.58	0.1175
C1*R1	1	9735.5843	9735.5843	2.32	0.1376
C2*R1	1	20003.6652	20003.6652	4.76	0.0364
C2*R3	1	11087.8978	11087.8978	2.64	0.1139
C3*R2	1	47865.7583	47865.7583	11.38	0.0019
R1*C4	1	45098.6300	45098.6300	10.73	0.0025
R2*C4	1	10285.6523	10285.6523	2.45	0.1273

Source	DF	Type III SS	Mean Square	F Value	Pr > F
TRT	6	160441.5837	26740.2639	6.36	0.0002
C1	1	67779.6280	67779.6280	16.12	0.0003
C2	1	443098.2755	443098.2755	105.39	0.0001
C3	1	249994.1996	249994.1996	59.46	0.0001
C5	1	132223.5073	132223.5073	31.45	0.0001
R1	1	278087.6327	278087.6327	66.14	0.0001
R2	1	21476.7478	21476.7478	5.11	0.0305
R3	1	43739.6582	43739.6582	10.40	0.0028
R5	1	20330.7758	20330.7758	4.84	0.0350
R6	1	11851.9481	11851.9481	2.82	0.1026
R7	1	10860.2434	10860.2434	2.58	0.1175
C1*R1	1	9140.3988	9140.3988	2.17	0.1498
C2*R1	1	21256.3073	21256.3073	5.06	0.0313
C2*R3	1	15800.4345	15800.4345	3.76	0.0611
C3*R2	1	48709.6471	48709.6471	11.59	0.0018
R1*	1	44314.8960	44314.8960	10.54	0.0027
R2*C4	1	10285.6523	10285.6523	2.45	0.1273

General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	25	1799231.771	71969.271	16.29	0.0001
Error	30	132544.854	4418.162		
Corrected Total	55	1931776.625			

R-Square    C.V.    Root MSE    YIELD Mean  
 0.931387    6.565027    66.46925    1012.475

General Linear Models Procedure

Dependent Variable: YIELD

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ROW	7	388314.902	55473.557	12.56	0.0001
COL	6	1159072.132	193178.689	43.72	0.0001

TRT	6	119723.549	19953.925	4.52	0.0023
C1*R1	1	9578.652	9578.652	2.17	0.1513
R1*C2	1	18255.782	18255.782	4.13	0.0510
C2*R3	1	7858.737	7858.737	1.78	0.1923
C3*R2	1	41660.946	41660.946	9.43	0.0045
R1*C4	1	44992.650	44992.650	10.18	0.0033
R2*C4	1	9774.420	9774.420	2.21	0.1473
Source	DF	Type III SS	Mean Square	F Value	Pr > F
ROW	7	388314.902	55473.557	12.56	0.0001
COL	6	1019062.385	169843.731	38.44	0.0001
TRT	6	117916.250	19652.708	4.45	0.0025
C1*R1	1	9397.488	9397.488	2.13	0.1551
R1*C2	1	20305.653	20305.653	4.60	0.0403
C2*R3	1	12900.535	12900.535	2.92	0.0978
C3*R2	1	42698.784	42698.784	9.66	0.0041
R1*C4	1	44171.272	44171.272	10.00	0.0036
R2*C4	1	9774.420	9774.420	2.21	0.1473

## Covariance Parameter Estimates (REML)

Cov Parm	Estimate
ROW	7290.8987058
COL	21799.310745
C1*R1	5842.8474878
R1*C2	15988.580408
C2*R3	10848.115411
C3*R2	40466.589248
R1*C4	41571.338509
R2*C4	4747.3414225
Residual	4437.2974998

## Solution for Fixed Effects

Effect	TRT	Estimate	Std Error	DF	t	Pr >  t
INTERCEPT		903.07551781	68.35032779	6	13.21	0.0001
TRT	1	129.72384541	37.61944012	30	3.45	0.0017
TRT	2	137.78424774	36.51437318	30	3.77	0.0007
TRT	3	168.80483626	38.07134440	30	4.43	0.0001
TRT	4	148.48914899	37.87631974	30	3.92	0.0005
TRT	5	62.38611199	36.39931336	30	1.71	0.0969
TRT	6	118.60818492	35.65171322	30	3.33	0.0023
TRT	7	0.00000000	.	.	.	.

## Tests of Fixed Effects

Source	NDF	DDF	Type III F	Pr > F
TRT	6	30	4.64	0.0019

## Least Squares Means

Effect	TRT	LSMEAN	Std Error	DF	t	Pr >  t
TRT	1	1032.7993632	68.49924871	30	15.08	0.0001
TRT	2	1040.8597656	68.27610042	30	15.24	0.0001
TRT	3	1071.8803541	68.98349917	30	15.54	0.0001
TRT	4	1051.5646668	69.12808466	30	15.21	0.0001
TRT	5	965.46162980	68.79788141	30	14.03	0.0001
TRT	6	1021.6837027	68.53512010	30	14.91	0.0001
TRT	7	903.07551781	68.35032779	30	13.21	0.0001

## Chapter 31

# PROC GLM and PROC MIXED for Trend Analysis of Incomplete Block- and Lattice Rectangle-Designed Experiments

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### *Purpose*

For resolvable row-column or lattice rectangle designs, a variety of analysis options are given in this chapter. These programs are for randomized complete block designs, incomplete block designs with rows (columns) as blocks, standard textbook analysis, differential gradients within rows (columns), and trend analysis using orthogonal polynomial regression functions of the rows and columns and their interactions. The example used in this chapter pulls data from Table 12.5 of W. G. Cochran and G. M. Cox's 1957 book *Experimental Designs*.

There are sixteen insecticide treatments arranged in four rows and four columns within each of the five complete blocks (replicates) to form a balanced lattice square. The data are means of three counts of plants infected with boll weevil. The trend analysis is the most appropriate analysis for these data. The code can also be used for incomplete block design by either deleting the row or the column category.

### *SAS Code*

```
options ls = 76;
proc iml;
  opn4=orpol(1:4,3); /* 4 columns and 3 regressions. */
  opn4[,1] = (1:4) `;
  op4= opn4;      print op4;
  create opn4 from opn4[colname={'COL' 'C1' 'C2' 'C3'}];
  append from opn4;
```

```

close opn4;
run;
opn3=orpol(1:4,3); /* 4 rows and 3 regressions. */ opn3[,1] =
(1:4) `;
op3 = opn3; print op3;
create opn3 from opn3[colname={'ROW' 'R1' 'R2' 'R3'}];
append from opn3;
close opn3;
run;
data lsgr;
infile 'lsgr1645.dat'; /* Name of data file. */
input count rep ROW COL treat;
data lsbig; /* Name of lsgr after adding 6 polynomial regressions. */
set lsgr;
idx = _n_; run;
proc sort data= lsbig;
by COL; run;
data lsbig;
merge lsbig opn4;
by COL; run;
proc sort data = lsbig;
by ROW; run;
data lsbig;
merge lsbig opn3;
by ROW; run;
proc sort data = lsbig; by idx; run;
proc print; run;

/*In the codes below, a fixed-effects model is given first using PROC
GLM; this is followed by a code for a random-effects mode using
PROC MIXED. */
/* Randomized complete block design analysis. */
proc glm data = lsbig; class rep row col treat;
model count = rep treat;
run;
proc mixed data = lsbig;
class rep row col treat;
model count = treat;
random rep;
lsmeans treat;
run;

/* Incomplete block (row) analysis. */
proc glm data = lsbig; class rep row col treat;
model yield = rep row(rep) treat;
run;
proc mixed data = lsbig;
class rep row col treat;
model count = treat;
random rep row(rep);
lsmeans treat;
run;

/* Standard textbook lattice square analysis. */
proc glm data = lsbig; class rep row col treat;
model count = rep treat row(rep) col(rep);
run;

```

```

proc mixed data = lsbig;
  class rep row col treat;
  model count = treat;
  random rep row(rep) col(rep);
  lsmeans treat;
run;

/* Differential linear gradients within rows analysis. Quadratic and
cubic gradients did not appear to be present for these data.
This analysis is deemed appropriate for the data in Table 12.3 of
W. G/ Cochran and G. M. Cox's 1957 book entitled Experimental De-
signs, but not for this example. */
proc glm data = lsbig;  class rep row col treat;
  model count = rep treat row(rep) C1*row(rep);
run;
proc mixed data = lsbig;
  class rep row col treat;
  model count = treat/solution;
  random rep row(rep) C1*row(rep);
  lsmeans treat;run;/* Trend analysis using polynomial regressions
and their interactions. */
proc glm data = lsbig;  class rep row col treat;
  model count = rep treat r1*rep r2*rep c1*rep c1*r1*rep
  c2*r1*rep c2*r2*rep c3*r2*rep;run;
proc mixed data = lsbig;  class rep row col treat;
  model count = treat/solution;
  random rep r1*rep r2*rep c1*rep c1*r1*rep c2*r1*rep c2*r2*rep
  c3*r2*rep;
  lsmeans treat;
run;

```

An abbreviated part of the output of the previous code follows.

```

/* Linear, quadratic, and cubic polynomial regression coefficients. */

```

OP3					
1	-0.67082	0.5	-0.223607		
2	-0.223607	-0.5	0.6708204		
3	0.2236068	-0.5	-0.67082		
4	0.6708204	0.5	0.2236068		

```

/* Randomized complete block analysis. */
Dependent Variable: COUNT

```

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	19	1275.76500	67.14553	1.73	0.0564
Error	60	2332.77300	38.87955		
Corrected Total	79	3608.53800			

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.20	0.9358
TREAT	15	1244.20200	82.94680	2.13	0.0200

Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.20	0.9358
TREAT	15	1244.20200	82.94680	2.13	0.0200

```

/*Standard textbook analysis. */
Dependent Variable: COUNT

```

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	49	2928.37008	59.76265	2.64	0.0029
Error	30	680.16792	22.67226		
Corrected Total	79	3608.53800			

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.35	0.8433
TREAT	15	1244.20200	82.94680	3.66	0.0012
ROW (REP)	15	1093.01550	72.86770	3.21	0.0032
COL (REP)	15	559.58958	37.30597	1.65	0.1197

Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.35	0.8433
TREAT	15	319.45208	21.29681	0.94	0.5350
ROW (REP)	15	1026.75583	68.45039	3.02	0.0049
COL (REP)	15	559.58958	37.30597	1.65	0.1197

*/\* Differential linear gradients within rows and replicates. This is an appropriate analysis for the data in Table 12.3 of Cochran and Cox (1957). Experimental Designs but not for this data set. \*/*

Dependent Variable: COUNT

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	54	3134.27638	58.04216	3.06	0.0016
Error	25	474.26162	18.97046		
Corrected Total	79	3608.53800			

R-Square	C.V.	Root MSE	COUNT Mean
0.868572	39.94048	4.35551	10.9050

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.42	0.7955
TREAT	15	1244.20200	82.94680	4.37	0.0006
ROW (REP)	15	1093.01550	72.86770	3.84	0.0015
C1*ROW (REP)	20	765.49588	38.27479	2.02	0.0488

Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.42	0.7955
TREAT	15	347.188383	23.145892	1.22	0.3202
ROW (REP)	15	884.112744	58.940850	3.11	0.0060
C1*ROW (REP)	20	765.495883	38.274794	2.02	0.0488

*/\* Polynomial regression trend analysis considered appropriate for this example.\*/*

Dependent Variable: COUNT

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	54	3384.66411	62.67896	7.00	0.0001
Error	25	223.87389	8.95496		
Corrected Total	79	3608.53800			

R-Square	C.V.	Root MSE	COUNT Mean
0.937960	27.44139	2.99248	10.9050

Source	DF	Type I SS	Mean Square	F Value	Pr > F
REP	4	31.56300	7.89075	0.88	0.4893
TREAT	15	1244.20200	82.94680	9.26	0.0001
R1*REP	5	845.22838	169.04568	18.88	0.0001
R2*REP	5	246.02137	49.20427	5.49	0.0015
C1*REP	5	434.80006	86.96001	9.71	0.0001
R1*C1*REP	5	118.25808	23.65162	2.64	0.0475
R1*C2*REP	5	174.90489	34.98098	3.91	0.0094

R2*C2*REP	5	156.38244	31.27649	3.49	0.0157
R2*C3*REP	5	133.30389	26.66078	2.98	0.0305
Source	DF	Type III SS	Mean Square	F Value	Pr > F
REP	4	31.563000	7.890750	0.88	0.4893
TREAT	15	421.496008	28.099734	3.14	0.0056
R1*REP	5	809.864820	161.972964	18.09	0.0001
R2*REP	5	177.016456	35.403291	3.95	0.0089
C1*REP	5	352.057631	70.411526	7.86	0.0001
R1*C1*REP	5	96.281349	19.256270	2.15	0.0923
R1*C2*REP	5	204.368728	40.873746	4.56	0.0043
R2*C2*REP	5	138.464513	27.692903	3.09	0.0262
R2*C3*REP	5	133.303894	26.660779	2.98	0.0305

Cov Parm	Estimate
REP	0.00000000
R1*REP	53.23803826
R2*REP	9.80562147
C1*REP	23.76781000
R1*C1*REP	9.98969710
R1*C2*REP	45.69858595
R2*C2*REP	31.54099937
R2*C3*REP	21.49617387
Residual	9.00079394

Tests of Fixed Effects

Source	NDF	DDF	Type III F	Pr > F
TREAT	15	25	3.41	0.0033

Least Squares Means

Effect	TREAT	LSMEAN	Std Error	DF	t	Pr >  t
TREAT	1	5.10314265	1.63982935	25	3.11	0.0046
TREAT	2	13.43151284	1.75595605	25	7.65	0.0001
TREAT	3	9.78194530	1.71248681	25	5.71	0.0001
TREAT	4	11.59100160	1.70310420	25	6.81	0.0001
TREAT	5	12.04012050	1.77463190	25	6.78	0.0001
TREAT	6	6.46087629	1.71679001	25	3.76	0.0009
TREAT	7	4.87293305	1.65381037	25	2.95	0.0069
TREAT	8	11.43810953	1.88342899	25	6.07	0.0001
TREAT	9	9.89142127	1.65449886	25	5.98	0.0001
TREAT	10	15.19391731	1.92490202	25	7.89	0.0001
TREAT	11	15.29420036	1.80297734	25	8.48	0.0001
TREAT	12	11.46771203	1.69521361	25	6.76	0.0001
TREAT	13	10.39896987	1.63737478	25	6.35	0.0001
TREAT	14	15.23542928	1.71894217	25	8.86	0.0001
TREAT	15	8.54488157	1.66229114	25	5.14	0.0001
TREAT	16	13.73382654	1.67968857	25	8.18	0.0001





## Chapter 32

# Partitioning Crop Yield into Genetic Components

Vasilias A. Fasoula  
Dionysia A. Fasoula

### *Importance*

To increase efficiency in plant breeding by selecting for high yield and stability from the early generations of selection. Partitioning crop yield into genetic components increases efficiency and offers the following advantages: (1) yield and stability genes are selected early in the program, rather than late-generation testing where most genes are irretrievably lost; (2) breeders can identify and cross, in early generations, complementary lines for genes that control the three components of crop yield and combine them in one line; and (3) breeders can develop density-independent cultivars especially favored by farmers.

### *Genetic Components of Crop Yield*

1. *Genes controlling yield potential per plant.* These genes contribute to the production of density-independent cultivars by expanding the lower limit of the optimal productivity density range.
2. *Genes conferring tolerance to biotic and abiotic stresses.* These genes enhance the production of density-independent cultivars by expanding the upper limit of the optimal productivity density range.
3. *Genes controlling responsiveness to inputs.* These genes enable cultivars to exploit optimal growing conditions.

### ***Parameters That Determine the Genetic Components***

1. *The progeny mean yield per plant* ( $\bar{x}$ ) evaluates and selects genes contributing to higher yield.
2. *The progeny standardized mean* ( $\bar{x}/s$ ) evaluates and selects genes contributing to stability of performance.
3. *The progeny standardized selection differential* ( $(\bar{x}_{sel} - \bar{x})/s$ ) evaluates and selects genes that exploit nonstress environments, where  $\bar{x}$  is the progeny mean,  $s$  is the progeny phenotypic standard deviation, and  $\bar{x}_{sel}$  is the mean yield of the selected plants at a predetermined selection pressure.

### ***Conditions of Selection***

To partition crop yield into genetic components, it is essential to perform selection under the following conditions:

1. *Absence of competition.* This condition increases response to selection by reducing the masking effect of competition on single-plant heritability and by optimizing the range of phenotypic expression.
2. *Enhanced gene fixation.* This condition is essential for (1) reducing the masking effect of heterozygosity on single-plant heritability, (2) exploiting additive alleles, and (3) increasing genetic advance through selection.
3. *Multiple environment evaluation.* This condition exposes progenies to the environmental diversity encountered over the target area of adaptation and improves heritability by allowing selection for reduced genotype-by-environment interaction and increased responsiveness to inputs.
4. *Utilization of the honeycomb selection designs.* Comparable evaluation of progenies across the target area of adaptation requires designs that fulfill four conditions: (1) effective sampling of environmental diversity, (2) concurrent selection among and within progenies, (3) joint selection for broad as well as specific adaptation, and (4) application of high selection pressures.
5. *Nonstop selection.* This condition refers to the constant improvement of the crop yield and quality of released and adapted cultivars. Continuous selection after the release of cultivars is imposed by the con-

stant need to eliminate undesirable mutations while exploiting desirable ones.

### ***Originators***

Fasoula, V.A. and Fasoula, D.A. (2000). Honeycomb breeding: Principles and applications. *Plant Breeding Reviews* 18:177-250.

### ***Software Available***

Batzios, D.P. and Roupakias, D.G. (1997). HONEY: A microcomputer program for plant selection and analysis of the honeycomb designs. *Crop Science* 37:744-747 (program free of charge).

For software distribution, contact Dimitrios P. Batzios, Variety Research Institute, 57400 Sindos, Greece. Tel. + 302310796-264. FAX + 302310796-343. E-mail: <Varinst@spark.net.gr>. The software refers to honeycomb breeding as it appears in Fasoula and Fasoula (1995) and Fasoula and Fasoula (2000).

### ***Contact***

Vasilias A. Fasoula, Center for Applied Genetic Technologies, 111 Riverbend Road, University of Georgia, Athens, GA 30602-6810, USA. E-mail: <vfasoula@uga.edu>.

## ***EXAMPLE***

The following example (Table 32.1) demonstrates the partitioning of crop yield into genetic components and shows the evaluation of twenty F<sub>4</sub> cotton lines plus one check tested in a replicated-honeycomb trial (Fasoulas and Fasoula, 1995) across two locations with a total of 100 replications (fifty replications per location). This example is included in the available software and utilizes data from Batzios (1997).

Lines were evaluated in the absence of competition in two locations for the three genetic components of crop yield: (1) yield per plant, (2) tolerance to stresses, and (3) responsiveness to inputs. The check (line 21) represents the cotton cultivar Sindos 80 developed in Greece. The three ge-

TABLE 32.1. Evaluation of 20 F<sub>4</sub> cotton lines selected for high yield per plant

Progeny lines	Mean yield per plant (g)		Tolerance to stresses		Responsiveness to inputs	
	( $\bar{x}$ )	(%)*	( $\bar{x} / s$ )	(%)*	( $\bar{x}_{sel} - \bar{x}$ ) / $s$	(%)*
15	315.0	100	2.42	100	1.86	91
11	305.8	97	2.08	86	1.67	82
3	298.1	95	2.22	92	1.71	83
5	272.2	86	1.59	66	1.71	84
12	259.9	82	1.72	71	1.69	82
17	250.1	79	1.90	79	1.70	83
18	245.5	78	2.36	97	1.71	85
7	236.8	75	2.07	86	1.75	85
1	235.5	75	1.62	67	1.76	86
13	235.4	75	1.54	64	1.69	83
6	235.4	75	1.54	64	1.69	83
14	216.6	69	2.03	84	1.62	79
19	215.5	68	2.07	86	1.67	81
2	208.3	66	1.71	71	1.44	70
8	199.7	63	1.20	50	1.58	77
21(ck)	198.0	63	1.64	68	1.83	89
16	184.5	58	1.61	67	1.93	94
20	179.4	57	1.81	75	1.74	85
9	169.6	54	1.18	49	1.58	77
4	167.9	53	1.23	51	2.05	100
10	159.3	51	1.25	52	1.82	89
	130.4	41	1.29	53	1.78	87

\*Percent of highest value

netic components of crop yield were calculated from 100 values of single plants representative of each progeny line grown in the honeycomb experiments.

### **Conclusions**

An analysis of Table 32.1 data leads to several conclusions that are relevant to the benefits of partitioning crop yield into genetic components:

1. Percent range of expression: 41 to 100 for the first component, 49 to 100 for the second component, and 70 to 100 for the third component. Thus, in this genetic material, genes controlling yield per plant and tolerance to stresses showed the largest variation.
2. The check cultivar (21) has the following relative values compared to the best line: 58 percent for the first component, 67 percent for the second component, and 94 percent for the third. Evidently, for the check cultivar, the genetic components of crop yield ranks in relative importance as: responsiveness to inputs → tolerance to stresses → yield per plant.
3. The best  $F_4$  line on the basis of the component evaluation is line 15. Three best plants were selected from line 15 and seven other plants were selected from the most superior lines of Table 32.1, and their progenies were tested as  $F_{4:6}$  lines in evaluation trials. These 10 best  $F_{4:6}$  lines derived by the honeycomb methodology, along with the 10 best  $F_{4:6}$  lines derived by the conventional methodology, were evaluated in randomized complete block (RCB) trials. The lines derived from honeycomb breeding outperformed the lines derived from conventional breeding (Batzios, 1997; Batzios et al., 2001). More specifically, in the RCB trials, the three best  $F_{4:6}$  lines (15-1, 15-2, and 15-3), derived from line 15, produced the following yield superiority in percent of the check cultivar Sindos 80.

The best $F_{4:6}$	Yield (%)
15-1	154
15-2	141
15-3	128
Sindos 80	100

Lines 15-1 and 15-2 ranked first and outyielded the other eighteen lines. This indicates that honeycomb selection for superior component and quality performance across the target area of adaptation can be a safe and efficient way to exploit desirable genes in every generation to substantially increase efficiency.

4. Selection for the three crop yield components and quality across the target area of adaptation at all stages of the breeding program makes regional testing unnecessary and halves the time required to release a cultivar.

5. Given that selection is based on genetic components of crop yield, the developed cultivars are density independent, an advantage favored greatly by farmers since density-independent cultivars perform well at a greater range of plant densities.
6. If during evaluation and selection no lines show satisfactory relative superiority, promising lines that complement each other for the three components of crop yield and quality are crossed to obtain desirable recombinant lines.

### ***A Noteworthy Relation***

When evaluation is performed in the absence of competition, an important relation is revealed between the genetic components of crop yield and the parameters of the general response equation. Thus, starting from the general response equation

$$R = i h^2 \sigma_p \quad (\text{Falconer, 1989})$$

and substituting heritability by its equivalent  $\sigma_g^2 / \sigma_p^2$ , the equation becomes

$$R = i \frac{\sigma_g}{\sigma_p} \sigma_g \quad (\text{Falconer, 1989})$$

where  $i$  is the intensity of selection or the standardized selection differential,  $h^2$  is the heritability,  $\sigma_p$  is the phenotypic standard deviation, and  $\sigma_g$  is the genotypic standard deviation.

Iliadis (1998) estimated the correlation coefficient between  $\sigma_g$  and  $\bar{x}$  (progeny mean yield per plant) in chickpea grown in the absence of competition. This correlation coefficient ( $r = 0.95$ ) was high. This suggests that when evaluation is practiced in the absence of competition that maximizes both  $\bar{x}$  and  $\sigma_g$ ,  $\bar{x}$  may replace  $\sigma_g$  and the equation becomes

$$R = i \frac{\bar{x}}{\sigma_p} \bar{x}.$$

The new formula is a product of (1) the progeny standardized selection differential, (2) the progeny standardized mean, and (3) the progeny mean, i.e., the product of the three genetic components of crop yield (Fasoula and Fasoula, 2000), described in detail previously.

## REFERENCES

- Batzios, D.P. (1997). Effectiveness of selection methods in cotton (*Gossypium hirsutum* L.) breeding. Doctoral thesis, Department of Genetics and Plant Breeding, Aristotelian University, Thessaloniki, Greece.
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- Iliadis, C.G. (1998). Evaluation of a breeding methodology for developing germplasm in chick-pea (*Cicer arietinum* L.). Doctoral thesis, Department of Genetics and Plant Breeding, Aristotelian University, Thessaloniki, Greece.





## Short Note 1

# Inbreeding Coefficient in Mass Selection in Maize

Fidel Márquez-Sánchez

### *Importance*

To know how much inbreeding is being generated through the course of mass selection.

### *Definitions*

Inbreeding coefficient at generation  $t$ : the amount of inbreeding that has been accumulated up to cycle  $t$  of selection.

$$F(MS)_t = 1/2nm \left[ 1 - 2m(n-1)F_{t-1} - 2(m-1)F_{t-2} - F_{t-3} \right]$$

where  $F(MS)_t$  = inbreeding coefficient at cycle  $t$  of mass selection;  $n$  = number of open-pollinated ears that make the seed balanced composite from where the population under selection originates;  $m$  = number of seeds per open-pollinated ear.

### *Originator*

Márquez-Sánchez, F. (1998). Expected inbreeding with recurrent selection in maize: I. Mass selection and modified ear-to-row selection. *Crop Science* 38(6):1432-1436.

### *Contact*

Dr. Fidel Márquez-Sánchez. E-mail: <fidelmqz@hotmail.com>.

**Observations**

$n$  and  $m$  must be adjusted by the variance effective number,

$$N_{e(v)} = N[4s / (1 - 2s)],$$

where  $N = nm$ , and  $s$  is the selection pressure (Crossa and Venkovsky, 1997). The adjustment is made as follows:

$$n = [N_{e(v)}Q]^{\frac{1}{2}}$$

$$m = [N_{e(v)} / Q]^{\frac{1}{2}}, \text{ where } Q = n/m.$$

In the case of modified ear-to-row selection the actual number of plants ( $N$ ) in the selection plot must first be adjusted by the inbreeding effective number,

$$N_{e(f)} = 4N_{fr}N_{mr} / (N_{fr} + N_{mr}),$$

where  $N_{fr}$  and  $N_{mr}$  are the numbers of female and male rows, respectively, of the detasseling-selection plot (Falconer, 1961).

**REFERENCES**

- Crossa, J. and Venkovsky, R. (1997). Variance effective population size for two-stage sampling of monoecious species. *Crop Science* 37:14-26.
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## Short Note 2

# Regression of Forage Yield Against a Growth Index As a Tool for Interpretation of Multiple Harvest Data

Jeffery F. Pedersen

### *Purpose*

Concise representation of multiple harvest forage data and as a graphical aid in assessing the value of a forage variety across an entire growing season.

### *Originator*

Pedersen, J.F., Moore, K.J., and van Santen, E. (1991). Interpretive analyses for forage yield trial data. *Agronomy Journal* 83:774-776.

### *Contact*

Dr. J. F. Pedersen, USDA-ARS, 344 Keim Hall, University of Nebraska, Lincoln, NE 68583-0937, USA. E-mail: <jfp@unlserve.unl.edu>.

### **EXAMPLE**

```
DATA ONE;  
INPUT REP YEAR MONTH $ LINE $ KGHA;  
CARDS;  
1          87          Apr          AUVigor          2487  
1          87          May          AUVigor          1228  
1          87          Jun          AUVigor          407  
1          87          Dec          AUVigor          78
```

1	87	Apr	Johnston	793
1	87	May	Johnston	985
1	87	Jun	Johnston	514
1	87	Dec	Johnston	0
2	87	Apr	AUVigor	2491
2	87	May	AUVigor	1232
2	87	Jun	AUVigor	411
2	87	Dec	AUVigor	82
2	87	Apr	Johnston	797
2	87	May	Johnston	989
2	87	Jun	Johnston	518
2	87	Dec	Johnston	0;

```
PROC SORT;
BY MONTH YEAR LINE;
RUN;
```

\* The following PROC GLM does not contribute directly to the stability analysis. It tests for differences due to MONTH\*YEAR (environment) LINE and the LINE\*MONTH\*YEAR interaction \*;

```
PROC GLM;
CLASS MONTH YEAR REP LINE;
MODEL KGHA=MONTH*YEAR REP(MONTH*YEAR) LINE LINE*MONTH*YEAR;
MEANS LINE MONTH*YEAR LINE*MONTH*YEAR;
RUN;
```

\* The following PROC MEANS outputs a data set named TWO with KGHA means across reps \*;

```
PROC MEANS NOPRINT;
BY MONTH YEAR LINE;
VARIABLES KGHA;
OUTPUT OUT=TWO MEAN=KGHA;
RUN;
```

```
PROC PRINT DATA=TWO;
RUN;
```

\* The following PROC GLM is used to put MONTH\*YEAR (environmental) means onto the data set. MONTH\*YEAR mean=COLM. The new data set is named THREE. The ANOVA generated is not otherwise used for data interpretation\*;

```
PROC GLM;
CLASS MONTH YEAR;
MODEL KGHA=MONTH*YEAR;
OUTPUT OUT=THREE PREDICTED=COLM;
RUN;
```

\* The following PROC GLM puts the grand mean (YBAR) and the value for the environmental mean minus the grand mean(COLEF) on a data set named FOUR. COLEF is the environmental index for the stability analysis \*;

```
PROC GLM;
MODEL COLM=;
```

```
OUTPUT OUT=FOUR PREDICTED=YBAR RESIDUAL=COLEF;
RUN;
```

```
PROC PRINT;
RUN;
```

```
* The following PROC GLM calculates the regression coefficient for
  KGHA on COLEF (the environmental index) for each line. Estimates
  of XBAR and b are given for each line in the ANOVA. Predicted
  values=YHAT and residuals=RY. Outputted data set= FIVE. *;
```

```
* To test H0: b=1, t= (estimate - 1) / SE
  df= df shown for COLEF*LINE in ANOVA *;
```

```
PROC GLM;
CLASSES LINE;
MODEL KGHA=LINE COLEF*LINE / P NOINT SOLUTION;
OUTPUT OUT=FIVE PREDICTED=YHAT RESIDUAL=RY;
RUN;
```

```
PROC PLOT;
PLOT YHAT*COLEF=LINE;
RUN;
```

```
PROC SORT;
BY LINE;
RUN;
```

```
PROC PLOT;
BY LINE;
PLOT KGHA*COLEF='*' YHAT*COLEF=LINE/OVERLAY;
RUN;
```

```
* The following PROC MEANS generates the raw sum of squares (USS) for
  deviations of the means from regression on environment index.
  Variance of deviation from regression can be calculated as USS /
  n-2 *;
```

```
* To test H0: F=1
```

```

r (USS/#obs-2) (#lines/#lines-1)
-----
Error MS (#lines/#lines-1)
```

```
where r = #replications
#lines/#lines-1 = correction factor
Error MS = error ms from last ANOVA
df= df #obs-2, pooled error df (from 1st PROC GLM) *;
```

```
PROC MEANS USS;
BY LINE;
VARIABLES RY;
RUN;
```



## Short Note 3

# Tolerance Index

Lajos Bona

### ***Purpose***

To identify the tolerance level of tested cereal (or other plant) cultivars/entries. The simple formula outlined in this chapter was applied for evaluation of small-grain cereal entries for acid soil tolerance, but it can serve as a useful tool for other traits as well. Among and within species, ranking and numerical evaluation of a range of entries will be reliable based on tolerance index ( $Ti$ ).

### ***Definitions***

*Tolerance index* refers to the characteristic production (grain yield, biomass, root or shoot length, etc.) of a genotype in a given stress environment (e.g., acid soil) relative to a nonstress environment (e.g., improved or limed acid soil).

$$Ti_{GY} = ALRL_{(-L)} / ALRL_{(+L)}$$

where,  $Ti$  = tolerance index (for grain yield) for a certain genotype,  $ALRL_{(-L)}$  = calculated mean longest root length of a genotype in unlimed (-L) acid soil (production in stress environment),  $ALRL_{(+L)}$  = calculated mean longest root length of a genotype in limed (+L) acid soil (production in nonstress environment).

or

$$Ti_{GY} = AGY_{(-L)} / AGY_{(+L)}$$



where,  $T_i$  = tolerance index (for grain yield) for a certain genotype,  $AGY_{(-L)}$  = observed grain yield of a genotype in unlimed (-L) acid soil (production in stressed environment),  $AGY_{(+L)}$  = observed grain yield of a genotype in limed (+L) acid soil (production in nonstressed environment).

### ***Originator***

Bona, L., Wright, R.J., and Baligar, V.C. (1991). A rapid method for screening cereals for acid soil tolerance. *Cereal Research Communications* 19:465-468.

## Short Note 4

# Computer Program to Calculate Population Size

Leví M. Mansur

### *Purpose*

To calculate population size necessary to recover any number of individuals exhibiting a trait.

### *Definitions*

Sedcole (1977) provided four methods to calculate the total number of plants needed to obtain one or more segregants with desired genes for a given probability of success. The following formula gives an accurate result:

$$n = \frac{2(r-0.5)z^2(1-q) + z^2(1-q)^2 + 4(1-q)(r-0.5)^{1/2}}{2q}$$

where  $n$  = total number of plants needed,  $r$  = required number of plants with desired genes,  $q$  = frequency of plants with desired genes,  $p$  = value that is function of ( $p$ ).

### *Originator*

Sedcole, J.R. (1977). Number of plants necessary to recover a trait. *Crop Science* 17:667-668.

### ***Software Available***

Mansur, L.M., Hadder, K., and Suárez, J.C. (1990). Computer program to calculate population size necessary to recover any number of individuals exhibiting a trait. *Journal of Heredity* 81:407-440 (software free of charge). E-mail: Leví Mansur at <levi@entelchile.net>.

### ***Example***

Data to be analyzed  $r = 10$ ,  $P = 0.95$ ,  $q = 0.25$ , germination rate = 0.8.  
The number of progenies that must be grown is  $N = 75$ .

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