Harmony Search: Current Studies and Uses on Healthcare Systems

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Abstract

One of the popular metaheuristic search algorithms is Harmony Search (HS). It has been verified that HS can find solutions to optimization problems due to its balanced exploratory and convergence behavior and its simple and flexible structure. This capability makes the algorithm preferable to be applied in several real-world applications in various fields, including healthcare systems, different engineering fields, and computer science. The popularity of HS urges us to provide a comprehensive survey of the literature on HS and its variants on health systems, analyze its strengths and weaknesses, and suggest future research directions. In this review paper, the current studies and uses of harmony search are studied in four main domains. (i) The variants of HS, including its modifications and hybridization. (ii) Summary of the previous review works. (iii) Applications of HS in healthcare systems. The main contribution of this review is intended to provide a thorough examination of HS in healthcare systems while also serving as a valuable resource for prospective scholars who want to investigate or implement this method.

Keywords

Harmony Search, Optimization, Evolutionary Algorithms, Meta-heuristics, Health Care, Medical Applications.

1. Background and Introduction

Before the year 2001, several search algorithms were already introduced and applied in different fields of applications. HS is one of the search algorithms that Zong Woo Geem has introduced. His vision was to develop a better-performing algorithm as an alternative to the other predefined algorithms. The intention of designing the algorithm is to have a generalized optimization technique for continuous, constrained, and discrete optimization in several types of optimization problems. Both the algorithm name and idea are inspired by the principle of the musician's improvisation; just like how musicians are always trying to choose the best and most potent harmony during their performances, this algorithm looks for the best solution (harmony) [1].

During the past years, the HS gained popularity, which can be observed through the diversified problems applied by the algorithm. HS's ability to solve various optimization problems attracted researchers and proved an effective optimization technique. Nowadays, the HS algorithm is still involved in engineering, computer science, industry, healthcare, construction, and robotics [2][3]. The factors that made the HS competitive with other algorithms are [3]:

- The ease of its mathematical model;
- No initial parameters are required to be set;
- The derivative information of the method is needless;
- The high flexibility of the algorithm;
- The fast and accurate nature of the method.

Many algorithms take the same path in finding inspiration to create their procedure ideas, such as Evolutionary Programming (EP), Particle Swarm Optimization (PSO), Evolution Strategies (ES), and Genetic Programming (GP), which are based on evolution. Some algorithms are based on some phenomena that can be seen in nature and the way living creatures think and act, such as Tabu Search (TS), Ant Colonies Optimization (ACO), and Neural Networks [2]. In contrast to the previously stated algorithms, the HS is based on an artificial phenomenon: the music improvisation process in which a given number of musicians seek to tune their instruments to achieve the best harmony (best state) [4][5].

In [6], Geem et al. developed the HS, a population-based meta-heuristic optimization method implemented in 2001. The HS mimics the construction of a unique harmony in musical composition

to handle an optimization challenge. HS has been used in many complex problems, and it has produced outstanding results almost every time. Common examples of these problems are healthcare systems [7], fuzzy controllers and benchmark functions [8][9], beam and ball controllers [10], power flow analysis [11], congestion management [12], data mining [13], job shop scheduling [14], water distribution [6], university timetables [15], structural design, renewable energy [16], data clustering [17], and neural networks [18].

The HS's primary advantages are its clarity in implementation, its track record of success, and its capacity to deal with a wide range of complicated issues at once. The HS can make trade-offs between convergent and divergent areas, which is the primary reason for its vitality, success, and enviable reputation in the industry. Exploitation is mainly regulated by the pitch adjustment rate (PAR) and the bandwidth (BW) in the HS rule [6,19]. At the same time, exploration is primarily controlled by the harmony memory considering rate (HMCR) in the HS rule [20][21].

In addition, numerous survey papers and monographs [22] have discussed the advancements of primary HS and its variants. However, as far as we are aware, there is no comprehensive study of HS from its use in healthcare systems. A question raised here that how HS and its variants are utilized for the application domains of health systems. To address this question, this study aims to provide a comprehensive review of HS on healthcare systems to create a valuable source for researchers to inspire ideas for developing medical technologies. Therefore, the main contribution of this work is to examine the current research and applications of HS in healthcare systems.

This paper discusses HS and its extensions in healthcare applications four-fold. These are as follows:

- 1) HS variations, including alterations and hybridizations, are discussed in detail;
- 2) A synopsis of earlier review materials;
- 3) The applications of HS in the healthcare sector are reviewed;
- 4) The last section of the paper proposes an operational framework for using HS in healthcare systems.

As a critical contribution, this study aims to give a comprehensive assessment of the usage of HS in healthcare systems while also acting as a beneficial resource for potential researchers who want to explore or adopt this approach. In brief, we will make every effort to incorporate as many of these advancements as possible.

In this paper, we will start to present the current trends of HS in Section 2. In the next section, we will summarize the previsou review works on HS, followed by introducing the procedure of the original algorithm in Section 4. Next, we will discuss the most common modification that occurred

to HS in Section 5; then, Section 6 will review the uses of HS in healthcare systems. In Section 7, we will propose an operational framework of HS variants to summarize their uses and procedures in healthcare problems. Finally, we will deliberate our conclusion and future trends in Section 8.

2. Current trends of HS

Since its first publication in a peer-reviewed journal, HS has established itself as a well-known population-based optimization method due to its broad adoption [23]. Since then, it has received widespread acceptance in various technical and medical sectors, as shown by many publications, as seen in Figure (1). As demonstrated by the number of papers on the technique's use since 2012 and the number of significant algorithm structure adjustments since 2006, there has been a sustained and rising interest in the HS and its variations [24]. Figure (2) depicts the number of issued articles, book chapters, conference papers, and other types of papers according to publisher types (ScienceDirect, IEEE, Springer, Wiley, and Taylor & Francis) since HS was proposed until December 2021. Figure (3) shows the number of published papers on each of the main variants of the HS, and Figure (4) presents the number of publications on applications of the HS to the healthcare sector.



Figure (1): Growing interest in the analysis and application of HS since 2001 (Source: Google Scholar; keyword search: "Harmony Search"; at 12: 40 Friday 31st December 2021)



Figure (2): Number of publications on the HS since it was proposed until December 2021, sorted by publisher and type (Source: ScienceDirect, Springer, IEEE, Wiley, and Taylor & Francis; keyword search: "Harmony Search"; at 12: 40 Friday 31st December 2021)



Figure (3): Number of publications on variants of the HS since it was proposed until December 2021 (Source: Google Scholar, keyword search: "Harmony Search", at 12: 40 Friday 31st December 2021)



Figure (4): Number of publications on healthcare applications of the HS since it was proposed until December 2021 (at 12: 40 Friday 31st December 2021)

3. Summary of Previous Reviews

This Section briefs the recent study surveys in HS and outlines their achievements and identified research holes. Yang X-S. published a book chapter on HS in 2009 [25]. This chapter aims to review and discuss the novel HS in metaheuristic algorithms. He began by outlining the basic steps of HS and demonstrating how it operates. Next, he attempted to characterize metaheuristics and explain why HS is an effective metaheuristic algorithm. He then briefly discussed other common metaheuristics, such as particle swarm optimization, to compare and contrast them with HS. Finally, He explored strategies for improving and developing new HS varieties and making recommendations for further studies, including open questions.

In 2013, O. Abdel-Raouf and M. A.-B published an HS [1] survey to examine the distinctions between HS algorithms and their implementations. Additionally, some proposed potential enhancements are included, such as the deployment of HS on different applications. Manjarres D. et al. published another review article around the same time on the application of HS [26]. They comprehensively discussed and analyzed the main characteristics and implementation portfolio of HS. They claimed to review the most recent literature on the application of HS in several practical applications with the following three objectives: (i) to emphasize the excellent behavior of this modern meta-heuristic based on the increase in related contributions reported to date; (ii) to provide

a bibliographic foundation for future research trends focusing on its applicability to other areas; and (iii) to do an in-depth study of potential possible research directions based on this meta-heuristic solver.

In 2016, Assad A. and Deep K. [13] published a survey report on the applications of HS in data mining. The analytical review was expected to provide an overview of the use of HS in data mining, particularly for those researchers interested in delving into the algorithm's capabilities in this area.

In late 2018, updated analysis and review were published by [27] on HS for energy engineering systems. The particular emphasis of this work had two primary objectives. To begin, the improved versions of HS adopted in recent studies are discussed. Second, contributions to energy system analysis using HS analyzed.

In 2019, four review works were published on HS with different objectives: (1) In early 2019, Ala'a A. et al. [28] published a comprehensive survey on the development of HS and its applications. The review paper discussed HS and its derivatives from a variety of perspectives. First, they explained the HS algorithm and demonstrated how its parameters influence its efficiency. Second, they defined HS classifications based on well-known HS variants and hybrid algorithms and the implementations of these classifications. Finally, a review of the HS algorithm's strengths and disadvantages and potential improvements was held. By highlighting similar studies from various disciplines, this article piqued curiosity about the implementation of HS for a broad range of audiences. (2) afterward, Yi J. et al. [29] published another survey work on HS's current state-of-the-art and its applications to intelligent manufacturing. This article offered a comprehensive overview of the HS fundamental principle and a survey of its most recent variants for feature optimization. Additionally, it included a study of cutting-edge HS applications in intelligent manufacturing, focusing on approximately 40 recently published papers. This paper also analyzed and summarized several possible future study avenues for HS and its applications to intelligent manufacturing. (3) Then, another review paper was published by Zhang T. and Geem Z. W. [22] to emphasize the historical evolution of algorithm structure rather than its implementations. This article discussed the initial HS in detail and various adapted and hybrid HS methods: adaptation of the basic HS operators, parameter adaptation, hybrid methods, solving multi-objective optimization issues, and restriction handling. (4) Finally, Yusup N. et al. published [29] a survey on HS focused on the feature selection method for classification. This article aimed to explore the efficiency of the HS for classification in various applications. The review concluded that HS function selection outperforms other well-known nature-inspired metaheuristics algorithms.

In 2020, Abualigah L. et al. [24] issued a comprehensive review of HS in various practical applications. In the same work, they reviewed papers in which HS was extended to multiple uses, most of which were clustering-related, such as data clustering, evidence clustering, fuzzy clustering, text clustering, wireless sensor networks, and image processing. Meanwhile, they discussed the strengths and shortcomings of HS and its variants to provide recommendations for potential studies.

Our review paper is distinct from previous work in several areas outlined below: (i) The prior review works are outdated, and they do not focus on specification applications of HS, such as healthcare systems. This review examines the most recent developments in various HS on healthcare systems. (ii) The implementation of HS is explained by giving the step-by-step procedure of HS and a practical example. (iii) The state-of-the-art reviews on HS and its variants are also discussed. (iv) This article delves deeply into healthcare environments where HS is widely employed and highlights notable work to inspire scholars in the field of meta-heuristic algorithms. (v) An operational framework of HS is proposed to review the leading implementation of HS and its extensions on healthcare systems and find the relationships among these variants. (vi) It illustrates the challenges and offers alternative solutions. We discovered about 300 latest study articles using Google Scholar by feeding various variations of the term 'harmony search, HS, harmony search algorithm' into the search box. After critically analyzing the collected documents, we identified around 60 as the most important in HS and its variants on healthcare systems, which are addressed in this survey.

4. The Standard HS

Harmony composition in terms of music is when the musicians attempt to generate new harmony by combining notes emitted in sequence. The composition process changes the harmonies seeking improvement until they get a satisfactory result [5][30]. They made formalization on the three measurable optimization options, which are [31]:

- 1) Select and play any popular from the musician's memory;
- 2) Playing something similar to a tune that has been played before;
- 3) Composing some new notes, which can be a random note.

Following the same concept in HS, we will have three components that the HS utilizes to have an equivalent process to the harmony composition that we mentioned before. These components are HM, pitch adjusting, and randomization [31]. Also, it is noteworthy to note that there are two parameter rates in HS [32]:

 HM considering rate (HMCR): - this is used to define the set value (1.0-HMRC) in the HM (HM); 2) Pitch adjusting rate (PAR): this parameter is used only after choosing a value from the HM because it sets the pace of regulating the pitch selected from the HM (1-PAR).

These components and parameters are used in the HS variable decision where a value that follows one of the three rules as the following [21,30–33] :

- 1) HM: selecting any single weight from the HM;
- 2) Pitch adjusting: determining an adjacent value of one value from its memory;
- 3) Randomization: choosing a random value from the possible values range.

The HS has the following five steps [21,31–38]:

<u>Step 1:</u> initializing the parameters of the algorithm and the optimization problem, which is represented in Equation (1) as follows:

$$Min\{f(x) | x_i \in X_i\}, \ i = 1, 2, \dots, N$$
(1)

Where:

f(x): The objective function.

 x_i : decision variables set.

 X_i : The possible range of values for each decision variable (x_i) that is $X_i \in [L^{x_i}, U^{x_i}]$ where L^{x_i} And U^{x_i} are the minimum and maximum bound for x_i .

N: Number of decision variables.

In this step, the control parameters are quantified. These parameters are:

- HM Size (HMS): this parameter can be considered the equivalent to the size of the population in population-based algorithms;
- (2) The HM Consideration Rate: This is used to check if the decision variable value is selected from the stored solution in the HM;
- (3) The Pitch Adjustment Rate: this parameter determines whether or not the decision variables have been changed to a neighboring value;
- (4) The Distance Bandwidth (BW) value specifies the adjustment distance for the pitch adjustment operator;
- (5) The Number of Improvisations (NI).

<u>Step 2:</u> Initialize the HM; in this step, the HM is generated by filling the matrix with randomly generated solution vectors, as shown in Equation (3). The numbers are between the maximum and the minimum bound $[L^{x_i}, U^{x_i}]$ where $1 \le i \le N$. The values are generated by Equations (2) and (3).

$$x_i^j = L^{x_i} + rand(0,1) \times (U^{x_i} - L^{x_i})$$
where $j = 1,2,3, \dots HMS,$ (2)

$$HM = \begin{bmatrix} x_1^1 & x_2^1 & \dots & x_N^1 \\ x_1^2 & x_2^2 & \dots & x_H^2 \\ \dots & \dots & \dots & \dots \\ x_1^{HMS} & x_2^{HMS} & \dots & x_N^{HMS} \end{bmatrix}$$
(3)

<u>Step 3:</u> new harmony improvising from the HM, In this step, a new harmony vector is generated $\vec{x} = (\vec{x}_1, \vec{x}_2, \vec{x}_3, ..., \vec{x}_N)$ based on the three rules:

- 1) Harmony Memory (HM): The first variable decision $\dot{x_1}$, is selected from the HM range $[\dot{x_1} x_1^{HMS}]$ with probability (w.p): HMCR where HRMS $\in (0,1)$;
- Pitch adjusting: using PAR parameter: Each decision variable is examined to check if it should be pitch-adjusted with probability PAR, where PAR ∈ (0,1) is presented in Equation (4).
- Pitch adjusting decision for $\dot{x_1} \leftarrow \begin{cases} \dot{x_1} = \pm rand(0,1) \times BW & w.p \quad PAR, \\ \dot{x_1} & w.p \quad 1 PAR \end{cases}$ (4)
- 3) Randomization: the first variable decision $\dot{x_1}$, s selected from a random value that already exists in the current HS with a probability of (1 HRMS) as it is shown in Equation (5)

$$\dot{x_1} \leftarrow \begin{cases} \dot{x_1} \in \{x_i^1, x_i^2, x_i^3 \dots, x_i^{HMS}\} & w. p \ HMRC, \\ \dot{x_1} \in X_i & w. p \ 1 - HRMS \end{cases}$$
(5)

<u>Step 4:</u> Update the HM, checking if the New Harmony vector $\vec{x} = (\vec{x}_1, \vec{x}_2, \vec{x}_3, ..., \vec{x}_N)$ is better than the worst harmony in the HM; the HM will be updated by excluding the worst harmony and including the best one.

Step 5: Repeat the previous steps 3 and 4 to satisfy the termination criterion.

The pseudocode of the HS algorithm is presented in the algorithm (1).

- 1. Begin
- 2. Define objective function $\{f(x), | x=(x), X2 | \dots Xa\}$
- *3. Define (HMCR), (PAR) and the other parameters*
- 4. Generate (HM) with random harmonies
- 5. *While (t<max number of iterations)*

5.	while (i -max number of iterations)
6.	<i>While (i</i> <= <i>number of variables)</i>
7.	If (rand <hmcr),< td=""></hmcr),<>
8.	Choose a value from HM for the variable i
9.	If (rand <par).< td=""></par).<>
10.	Adjust the value by adding a certain amount
11.	End if
12.	Else
13.	Choose a random value
14.	End if
15.	End while
16.	Accept the new harmony (solution) if better
17.	End while
18.	Find the current best solution
19.	End

Algorithm (1): Pseudocode of HS

5. Variants of HS

Due to the popularity of the HS, various publications have been proposed, and some of them are applied in different applications to achieve better performance than the original HS [1]. Scholars were inspired to enhance the standard HS's efficiency due to its alleged deficiencies in respect to deficiency and convergence speed. Numerous scholars have proposed modifications to the original HS algorithm, although others have adapted it to several issues. This Section discusses the developments of HS variants and the current published work on them. These variants are classified into two main categories: modifications and hybridizations of HS. Figure (5) depicts a general framework of the main variants of HS.



Figure (5): Variants of HS

5.1. Modifications of HS

Scholars have updated it numerous times to enhance HS's efficacy and efficiency and make it more suitable for a particular application. This Section discusses five adjusted HS algorithms. The modified algorithms are HIS, GHS, NGHS, SAHS, and CHS. These algorithms are summarized in Table (1).

Algorithm	Reference,	Aim	Modification method	Performance	Concluding
	author(s)			index	remarks
iHS	[39] , M. Mahdavi et al	Solving practical problems	Tuning HS constant parameters	iHS > HS	iHS works better than HS and other heuristic methods and is an excellent search for many engineering optimization problems.
GHS	[40], M. G. H. Omran and M. Mahdavi	Improving the performance of HS	Borrowing swarm intelligence principles improve the efficiency of HS	HS performance was improved	GHS seems to be a viable solution for solving problems, including Integer Programming.
NGHS	[41], D. Zou et al.	Solving reliability problems	Performing two critical operations: location updating and low- probability genetic mutation	NGHS	NGHS can be a viable option for resolving reliability issues.
SAHS	[38], CM. Wang and YF. Huang	Tuning appropriate parameter values	Adjusting automatic parameter values	SAHS	SAHS has supremacy over the original HS and its newly evolved derivatives.
IHSCH	[42], O. Abdel- Raouf et al.	Solving assignments	Generating a candidate solution by disorderly action is comparable to acoustic monophony.	IHSCH > HS and IHS	IHSCH is a more reliable and more effective process than conventional approaches (HS and HIS).

Table (1): The modified HS algorithms

5.1.1. IHS. The objective of IHS is to enhance the performance by evaluating both pitch adjusting rate and distance bandwidth values because small values of PAR and large values of BW can reduce the performance of this method [43][39]. In the Original HS (OHS), these parameters were fixed [44], which made Mahdavi et al. add their modifications in 2007 [5] by applying a dynamic technique to archive their values dynamically [28]. The dynamic PAR is shown in Equation (6) as follows:

$$PAR(N) = PAR_{Min} + \frac{(PAR_{Max} - PAR_{Min})}{NI} * n.$$
(6)

Where [40]:

PAR(N) : the PAR value for n generation.

PAR Max: maximum adjustment value.

PAR Min maximum adjustment value.

Furthermore, the update of the BW will be based on the Bwmax and Bwmin value of BW as follows in Equation (7) [40]:

$$BW(N) = bw_{max} Exp\left(\left(\frac{Ln\left(\frac{BW_{Min}}{BW_{Max}}\right)}{NI}\right) * n\right)$$
(7)

Where:

BW(N) = the bandwidth of the generation n.

Bwmax = the maximum BW value.

Bwmin = The minimum BW value.

The IHS was applied to solve many complex problems such as (minimization of the weight of spring, welded beam design disjoints feasible region, etc.) [39]. It is also used to solve the distribution network problems [45]. Consequently, it provides better performance than the OHS regarding noise and high dimensions [1]. Similarly, IHS generated a new solution vector that increases the accuracy and enhancement rate of the HS [5][46]. However, the main issue of IHS is the difficulty in choosing the minimum and maximum values of the bandwidth within a wide range (0-infinity) [25]. Similarly, the values of bwmax and bwmin can be introduced to other problems by determining and guessing them by the user because they are not independent [47].

5.1.2. GHS. After the presence of the IHS, M. Omran and M. Mahdavi proposed another modified algorithm called the Global-best HS (GHS) while they were trying to compare their study of applying the IHS algorithm to designing water-network problems with the other stochastic algorithms [28,47]. The authors noticed the limitations of IHS, which has the struggle of finding the upper and lower

bandwidth bounds (BW). Therefore, they worked to overcome this problem by integrating the concept of PSO. The PSO in GHA deals with particles defined as a swarm of individuals where each of these particles represents a candidate solution. The only difference between the HS and GHS is this approach, which changes the pitch-adjusting step whereby the BW is replaced with the best HM value. This step adds a more social dimension to the algorithm. Equation (8) demonstrated how GHS utilizes the excellent result in HM to substitute BW values [40].

If $rand(0,1) \le PAR(t)$, then Produce a random number $k \in U(1,..D)$ (8)

The GHS gives more successful results than HS and IHS concerning high dimensions and noise problems. It is the best choice to apply in applications, such as water network design rather than HS in minor and medium-scale issues; however, the GHS performance is worse in large-scale problems than HS [40].

5.1.3. NGHS. In 2010, Zou et al. Intended to update GHS to make it able to solve complex reliability problems [41]. They proposed a modified algorithm called Novel NGHS, which has two additional operations: position updating and genetic. The advantage of NGHS is its ability to turn the worst harmony in the HM into a global best harmony in each iteration rapidly. However, convergence problems may appear; therefore, the genetic mutation operator should solve this problem [48][49]. The pseudocode of NGHS is available in [41].

5.1.4. SAHS. The authors of [38] proposed a modified algorithm in 2010 that is also concerned with the pitch adjustment since the BW and PAR parameters impact the value of the final solution. Their proposed method was the parameters self-adapting based on the best experience. The concept of the randomized number is replaced with the low-discrepancy sequences in the HS initialization represented by Equations (9) and (10) so that the latest harmony is revised by the HM's maximum and minimum values.

$$trial^{i} + [\max(HM^{i} - trila^{i})] \times rand[0,1)$$
(9)

$$trial^{i} - min (HM)^{i}] \times rand[0,1)$$
⁽¹⁰⁾

Where:

 $trial^i$ = the pitch adjusted that is chosen from the HM.

 $Max(HM^i)$ & min (HM^i) = the maximum and minimum values of the HM [38].

5.1.5. IHSCH. The improved version of a harmony metaheuristic algorithm with different chaotic maps (IHSCH) is another version of HS used to solve linear assignment problems, considered one of the main optimization problems. This problem can be found in many scheduling applications such as planes and crews. These kinds of applications have many tasks and agents, and each agent should be

assigned to one task so that the total assignment cost is reduced. This problem can be presented in Equation (11).

$$Min f(x) = \sum_{i=1}^{n} \sum_{j=1}^{n} c_{ij} x_{ij}$$
(11)

Subject to:

$$\sum_{j=1}^{n} x_{ij} = 1, \ i = 1, 2, 3, \dots, n \tag{12}$$

$$\sum_{i=1}^{n} x_{ij} = 1, \ j = 1, 2, 3, \dots, n \tag{13}$$

An improvement has been presented in the HS algorithm to overcome this problem, embedding the nature of chaos with HS to find a solution. Testing the algorithm with three problems takes less time than traditional algorithms, and optimal solutions are obtained. The modified algorithms' foremost step is to generate long and consistent sequences to simulate complex problems quickly. After testing the modified algorithm with different linear assignment problems, the results show that total time is reduced beside the total cost [42].

5.2. Hybridizations of HS

Hybridization is a widespread and successful technique to improve an algorithm. Hybrid algorithms combine or merge two existing algorithms, resulting in a new and robust algorithm with enhanced capabilities. The hybrid HS algorithms have proved their efficiency in performance optimization to a higher level [28]. This enhancement can be represented in global search ability and/or exploration, the quality of the solutions, computational cost, and convergence speed. Several types of research used the concept of merging other algorithms with HS. However, we can categorize this hybridization into two main categories [50]:

- 1) The first category is the incorporation of HS with algorithms: In this case, the researchers will attempt to improve the HS by exploiting the advantages of another algorithm or using it to overcome some drawbacks in HS [50]. For instance, Niu et al. borrowed the arithmetic crossover operation from GA to increase the range of HS solutions, which will solve the premature convergence problem [51].
- 2) The second category is incorporating other algorithms into HS: in such cases, the HS is used as a component to improve the different algorithms, just like how Kaveh et al. introduced a new hybrid algorithm (HPSACO) based on PSOPC, ACO, and HS. They employed HS to control variable constraints in truss structure design [28][52].

6. Applications of HS in healthcare systems

A comprehensive overview of the HS and its variants was explained in the previous sections. The HS algorithm is an optimization algorithm for comparing solutions to achieve the optimum result for issues in different applications, including the biological and medical fields. There are many problems in this area that the HS algorithm can be used to determine its optimal result, especially since the most essential characteristics of this algorithm are its simplicity and ease of code and its fast results. In this section, we will examine what medical problems HS can be utilized by giving ideas that have been proposed in different academic publications. HS's use in healthcare systems includes image segmentation, disease detection and prediction, future selection and classification, force control, COVID-19, therapeutic medical physics, distribution of healthcare units, rostering and scheduling problems, and miscellaneous. The applicability of HS and its variants in different research domains of healthcare systems are shown in Figure (6).



Figure (6): Applications of HS and its variants in the healthcare domain

6.1. Medical image segmentation

One of the applications of HS is to find the optimum value of clustering numbers in medical image segmentation. Table (2) summarizes the applications of HS and its variants in medical image segmentation.

Reference, author(s)	Proposed algorithm	Aim	Performance	Concluding remarks
			index	
[53], Srikanth R, and	The proposed	Image segmentation	The proposed	The proposed method
Bikshalu K	algorithm	of the tongue	algorithm was	is superior to
			more efficient	histogram-based
			than the other	methods.
			compared	
			techniques	
[54], Fachrurrozi M	Hybrid multilevel	Image segmentation	HSA (medium	The minimal distance
et al.	thresholding and HS	of the tongue	level parameter)	classifier, the k-NN
	(HSA)			classifier, and the
				SVM classifier are
				employed for
				classification, and
				HHS achieves an
				average classification
				accuracy of 98.19
				percent, 98.34 percent,
				and 97.18 percent,
				respectively, with the
				fewest features.
[55], M. S. H. Lipu et	Improved HS (HIS)	Magnetic resonance	IHS	IHS was superior to
al.		imaging (MRI) brain		the fuzzy clustering
		image segmentation		algorithm for MRI
				image segmentation.

Table (2): Applications of HS and its variants in medical image segmentation

6.2. Disease detection and prediction

The use of HS for detecting and predicting diseases has gained more importance in the medical decision support systems. Referring to Table (3), HS has been used to predict, detect, and diagnose several diseases.

Reference, author(s)	Proposed algorithm	Aim	Performance	Concluding remarks
			index	
[56], Tuo S et al.	MP-HS-DHSI	Detecting high-order	MP-HS-DHSI	The suggested strategy
		single nucleotide	outperformed	may significantly be
		polymorphism (SNP)	four state-of-the-	improved the search
		interactions	art algorithms	speed and
				discriminating ability
				of a variety of epistasis
				models
[57], Koti P et al.	Hybrid HS (HM-L)	Predicting kidney	HM-L algorithm	Sensitivity of 96,
	method combined	diseases	outperformed	specificity of 93.33,
	with the Levi		other state-of-	the accuracy of 95, F-
	distribution		the-art methods	score of 96, and kappa
				value of 0.89 were
				obtained with the
				provided HM-L model
[58], Tuo S et al.	Niche HS	Detecting complex	Niche HS	Niche HS showed
		disease-associated	outperformed	promise in discovering
		high-order SNP	several	high-order disease-
		combinations	traditional	causing models when
			algorithms in	applied to age-related
			detection power	macular degeneration
			and CPU runtime	(AMD).
			for all of these	
			datasets.	
[59], Hickmann KS et	The forecasting	Forecasting the 2013-	N/A	For the 2013-2014 ILI
al.	model	2014 influenza season		observations, the
				forecasting approach
				yielded 50 percent and
				95 percent credible
				intervals that
				encompassed the
				actual observations for
				most weeks in the
				prediction.
[60], Gandhi TK et al.	DHS-MD	Detecting epileptic	DHS-MD	DHS-MD detection
		seizure activity with	compared to	was 100% accurate
			others	with the same degree

Table (3): Applications of HS and its variants in disease detection and prediction

		very fast and highest		of sensitivity and
		accuracy		specificity.
[61], P. Koti et al.	Hybrid HS with Levi	Predicting heart	Hybrid HS	The accuracy of
	Distribution (HM-L)	diseases		disease diagnosis was
				improved with less
				time.

6.3. Feature selection and classification

HS has been used for several medical classification tasks. Table (4) reviews the use of HS in different feature selection and classification applications.

Reference, author(s)	Algorithm	Aim	Performance	Concluding remarks
			index	
[62], Sarkar SS et al.	Proposed HS	Categorizing	Proposed HS	HS method achieved a
		microstructure image		higher agreement
		datasets		between feature
				selection and
				classification accuracy
				than the other
				methods.
[63], Dash R.	Adaptive HS	Gene selection and	Adaptive HS	Adaptive HS was
		classification of high		competent compared
		dimensional medical		to other considered
		data		approaches.
[64], Bae JH et al.	Z-FS-KM-MHS	Classifying colorectal	Z-FS-KM-MHS	The suggested model
		cancer patients from	was more	achieved an accuracy
		healthy people	accurate than the	of up to 94.36 percent
			other compared	in classifying objects.
			methods	
[65], Mousavi SM et	OFHS	Classifying medical	OFHS was more	OFHS was robust in
al.		datasets	efficient than the	data analysis and
			other compared	classification of
			algorithms	clinical datasets.
[66], S. Kar et al.	Group improvised HS	Lung nodule	GrIHS had a	Provision of high
	(GrIHS)	classification	sensitivity of	accuracy for ling
			97.59% and	nodule blind testing.
			accuracy of	
			97.78%	

 Table (4): Applications of HS and its variants in feature selection and classification

[67], Sudha MN, and	Hybrid of cuckoo	breast tumor	HHS was more	The minimal distance,
Selvarajan S.	search and (HHS)	classification	accurate than a	the k-NN, and the
			genetic algorithm	SVM classifier were
			(GA) and particle	employed for
			swarm algorithm	classification. With
			(PSO)	the fewest features,
				HHS achieved an
				average classification
				accuracy of 98.19
				percent, 98.34 percent,
				and 97.18 percent,
				respectively.
[68], E. Alexandre et	HS	Sound classification	HS	HS has outperformed
al.				its competitors in
				respect of error rate
				and execution time.
[69], Alexandre E et	Music-inspired HS	Classifying sounds in	Music-inspired	Music-inspired HS
al.		hearing aids	HS	was compared with
				sequential search
				algorithms or random
				search on 74 different
				features to test its
				performance.

6.4. Force control in bone drilling surgeries

For several years ago, bone drilling in surgeries has been used and different surgeries. This requires the prediction of increasing and minimizing the thrust force. Vibration-Assisted Drilling (VAD) was presented [71] to achieve this aim. This research used IFSHS. In the same study, a drilling algorithm developed results in an optimal cutting state. The optimal solution is achieved by applying evaluation information feedback, optimization parameters, and dynamic searching parameters. Experiments showed that VAD reduces the force by 18.4% to 33.2% compared to CD. Compared to the original VAD, the drilling force decreased by 20.19%. The way the HS algorithm works has been presented previously in this work. IFSHS operates using self-adaptive parameters that consist of a dynamic parameter and feedback factors.

6.5. COVID-19

HS and its variants have been used for different purposes in COVID-19, such as image enhancement for Coronavirus detection and social network contact tracing. Table (5) recaps the use of HS in Coronavirus.

Reference, author(s)	Proposed algorithm	Aim	Performance	Concluding remarks
			index	
[70], Al-Shaikh A et	Hybrid harmony	Social network	HHS showed its	HHS improved run
al.	search (HHS)	contact tracing of	superiority over	time by 77.18 percent
		COVID-19	these algorithms	and had an excellent
				average error rate of
				1.7 percent compared
				to other current
				algorithms for locating
				tightly coupled
				components (SCCs).
[71], V. Rajinikanth	HS and Otsu based	COVID-19 disease	The proposed	HS was beneficial in
et al.	System	detection	method extracted	preventing the
			the diseased	diagnostic burden
			portion more	associated with mass
			precisely	screening processing.

Table (5): Applications of HS and its variants in COVID-19

6.6. Therapeutic medical physics

Medical physics is almost as essential as medicine because it involves radiation for medicinal and diagnostic purposes. This analysis compared HS and GA in optimization simulations for HDR brachytherapy for prostate cancer, where the optimum treatment strategy is determined by analyzing radiation dose-based optimization constraints. Since therapeutic radiation plays a critical role in cancer care, it is possible to use optimization techniques such as HS to provide a hefty dose of radiation to cancer cells in this situation. The HS has several benefits that make it ideal for these uses, one of which is that it is quicker than the GA, which is vital for patients to improve in medical physics. Additionally, the HS can be highly effective in HDR prostate brachytherapy and is well-suited for mixing its parameters with optimum parameters to achieve a considerably shorter treatment period. This capability is critical for time-consuming clinic procedures such as IMRT, tomotherapy, brachytherapy, and beam angle optimization. The simulation environment was constructed using

various methods, including wxpython, Matplotlib, NumPy, and Python. - of these resources is free and open-source [72].

6.7. Distribution of the healthcare units

The two major problems are targeted, such as smart re-location and distribution of healthcare units. Table (6) presents the two main applications of HS and its variants in the distribution of healthcare units.

Reference, author(s)	Proposed algorithm	Aim	Performance	Concluding remarks
			index	
[73], M. Alinaghian	CPLEX	Locating the	CPLEX	CPLEX provided a
et al.		healthcare centers		reasonable solution for
		based on their		locating healthcare
		facilities		centers based on their
				facilities.
[74], Landa-Torres I	Multi-objective	Distribution of	MOGHS	The encouraging
et al.	grouping HS	medical emergency		findings open the way
	(MOGHS)	units		for the proposed
				technique to be used in
				real-world
				circumstances.

Table (6): Applications of HS and its variants in the distribution of healthcare units

6.8. Rostering and scheduling problems

The Nurse Rostering Problems (NRPs) is a management study for finding an ideal way for scheduling nurses for their shift and patient admission with a set of restraints. The uses of HS and its variants in rostering and scheduling problems are reviewed in Table (7).

				-
Reference, author(s)	Proposed algorithm	Aim	Performance	Concluding remarks
			index	
[75], Doush IA et al.	Novel HS	Patient admission	The novel HS	The suggested HS was
		scheduling (PAS)	algorithm was	a highly efficient
			capable of	solution to the PAS
			producing	problem that may
			comparably	address various
			competitive	scheduling issues
			results when	involving enormous
			compared with	amounts of data.
			nine state-of-the-	
			art algorithms	

 Table (7): Applications of HS and its variants in rostering and scheduling problems

[76], Yagmur EC,	Opposition-based	Nurse scheduling	Opposition-based	The proposed
and Sarucan A.	parallel HSA	problem	parallel HSA >	approach had achieved
			HS	better results than the
				standard HS in all
				eight different
				situations
[77], Hadwan M. et	Enhanced HS with	Solving nurse	DHSA > the	DHSA performed
al.	great deluge	rostering problems	hybridization of	much better than
	algorithm (GD),		enhanced HS	CHSA in solution
	called DHSA		with hill climbing	quality, with a slightly
			(HC) (CHSA)	higher execution time
				in all instances.
[78], Hadwan M et al.	CHSA	Addressing the nurse	CHSA > HS	This hybridization
		rostering problem by		process aided in
		combining an		achieving a balance
		enhanced HS with a		between exploration
		regular hill-climbing		and exploitation
		algorithm (HC)		throughout the search
				phase.
[79], M. Hadwan	HS	Nurse rostering	HS	HS obtained
		problems		reasonable results in
				addition to other
				algorithms available in
				the literature.
[80], M. Ayob et al.	Enhanced HS (EHS)	Nurse rostering	EHS	EHS showed better
		problems		results compared to
				HS.
[81], Awadallah MA	HS (improved)	Nurse rostering	HS (improved)	The findings achieved
et al.				by HS were
				reasonably equivalent
				to those acquired by
				the five INRC2010
				winners' approaches.
[82], Awadallah MA	Adaptive HS	Nurse scheduling	Adaptive HS in	Adaptive HS was
et al.		problem	comparison with	capable of solving
			the previously	nurse scheduling
			reported results	problems.
[83], Awadallah MA	Modified HS	Nurse rostering	MHSA	The MHSA built a
et al.	(MHSA)			realistic roster with
				competitively similar
				outcomes by using the

					International Nurse
					Rostering Competition
					2010 (INRC2010)
					dataset.
[84], Awadallah MA	Hybrid HS (HHSA)	Nurse	rostering	HHSA	The experimental
et al.		problem			findings demonstrated
					that HHSA was
					capable of producing
					high-quality solutions
					within the specified
					time constraints.

6.9. Miscellaneous

HS has been used in other healthcare systems application areas, such as pressure vessels, diet dwells time optimization, predicting protein structure, medical image enhancement, and finding motifs of biological data. These applications are designed by using either HS or enhanced HS. Table (8) summarizes the main applications of HS and its variants in different areas of healthcare systems.

Reference, author(s)	Proposed algorithm	Aim	Performance	Concluding remarks
			index	
[85], Alomoush AA	HS (improvised)	Designing a	HS performed	The EHS variant
et al.		simulation software	better than other	provided the best-
		for pressure vessel	HS hybridized	obtained results
			algorithms	both with and without
				the OBL technique.
[86], Firmansyah E et	An expert system	Developing an expert	N/A	The proposed expert
al.	inspired by HS	method to determine		system worked well
		the optimal diet		for people with normal
				body metabolism.
[87], Gupta B et al.	Linearly quantile	Improving the	The proposed	The proposed
	separated	contrast of r	approach works	approach showed that
	histogram	mammogram image	better than state-	basic breast-region
	equalization-grey		of-the-art.	segmentation may
	relational analysis			have provided decent
				results if the input
				picture has adequate
				contrast and can
				comprehend hidden
				features.

 Table (8): Applications of HS and its variants in different areas of healthcare systems

[88], Haridoss R, and	Opposition	based	Reducing the	OIHSA	The proposed
Punniyakodi S	improved	HS	computational time of	performed well	algorithm with
	(OIHSA)		compressing and	in reducing	Shannon entropy
			enhancing medical	execution time	undisputedly
			images		performed well
[89], Taghipour S et	Proposed	а	Predicting protein	N/A	The proposed
al.	methodology		structure		methodology
					established a novel
					way to predict protein
					complexes with a high
					degree of confidence,
					backed by functional
					investigations and
					literature mining.
[90], Dongardive J et	A novel HS		finding motifs	N/A	Experimental
al.			of biological data		validation of the
					suggested approach
					was performed using
					sequences of Human
					Papillomavirus strains
					acquired from certified
					and approved sources.
[91], Panchal A, and	HS		Optimizing dwell	HS > GA	HS was a feasible
Tom B			times for high dose-		alternative to currently
			rate (HDR) prostate		available algorithms
			brachytherapy		for optimizing HDR
					prostate
					brachytherapy.

7. Discussion

As described in the previous Section, HS and its extensions have been used in several healthcare systems applications. Every use of the HS variant has a unique procedure and different performance indicators. Similarly, different HS variants might be deployed for a specific problem, or several issues can be dealt with using the same HS variants. Concerning its performance, HS has been expanded into several versions to solve healthcare problems and has demonstrated excellent performance, with each variant utilizing a unique technique to maintain a high update success rate for HS. However, several forms of HS are thriving in various settings within healthcare systems.

Meanwhile, the HS made an implausible assumption, and its analysis of the update success rate is insufficiently accurate. On this premise, we propose an operational framework of HS variants to summarize their uses and procedures in healthcare problems. The suggested framework is depicted in Figure (7).

The significant expansions of HS in the healthcare systems are the primary HS, HHS, HIS, and multiobjective HS. Each enhancement of HS has been used in several healthcare applications. For example, standard HS and IHS have been used for classification (sound classification and lung nodule classification) and rostering and scheduling problems. In contrast, basic and multi-objective HS have been utilized for smart healthcare unit distributions. Meanwhile, the standard HS has been solely applied to therapeutic medical physics. In addition to that, IHS is the only algorithm deployed for image segmentation and enhancement for COVID-19 detection. On the other hand, heart disease has been predicted using HHS. Other application areas of healthcare systems, such as pressure vessels, diet dwell time optimization, predicting protein structure, medical image enhancement, and finding motifs of biological data, are designed by either HS or improved HS.



Figure (7): The proposed operational framework of HS in healthcare systems

Furthermore, several scholars have made significant efforts to apply HS in healthcare settings, and a system containing the algorithm's operating knowledge is open to other researchers. All these researches proved the popularity of HS, which was gained due to the following advantages:

- 1) The absence of complex mathematical operations to find the optimum solution;
- 2) Using a random search, which makes constructive information unnecessary;
- 3) Simple structure, which enables it to be combined with other meta-heuristic algorithms easily;
- 4) The speed in finding solutions;
- 5) Easily applicable in a variety of healthcare applications.

Despite these advantages, it does not prevent the existence of some challenges that mainly revolve around:

- 1) The static parameters;
- 2) The freedom to balance local and global search, as it becomes trapped in a local search as extended to numerical applications;
- 3) Another criticism about the HS is its limited work done mathematically [92,93].

Over the past several decades, scholars have conducted an extensive study on the control parameters of HS. Moreover, several scholars have changed the HS fundamental structure by integrating notions from various metaheuristics. However, there are a few areas in HS that remain unexplored. We believe that the above shortcomings of HS in healthcare applications can be improved in four directions. The most pertinent improvement area of HS is parameter tuning. The most critical phase in every metaheuristic method is parameter tuning. Additional research is necessary to establish the ideal HS parameter setting relevant to healthcare applications. The issue of parameter tuning is seen as an optimization problem. Automatic approaches are needed to determine the optimum parameters for the given health problem. Another exciting enhancement area of HS in health applications is considering the theoretical analysis of HS. The majority of research publications omitted any theoretical consideration of the modification and improvement processes used in HS. There is a need to research the HS and explain why it works better than others. It is necessary to do a theoretical investigation of fitness parameters, structure, and landscapes. The final possible improvement of HS in health systems can be in the scope of multi-objective optimization. Numerous methods for multi-objective harmony search have been developed.

Nonetheless, there is considerable room for expansion in the foreseeable future. Previously used algorithms made use of the idea of the archive. Many other methods and multi-objective operators available in the literature may be used to solve multi-objective issues.

8. Conclusion and Future Trends

This review article discussed the HS optimization algorithm, its variations, uses, and implementations in different areas of healthcare systems. As a critical contribution, this study aimed to give a comprehensive assessment of the usage of HS in healthcare systems while also acting as a beneficial resource for potential researchers who want to explore or adopt this approach. Since its inception, the algorithm garnered tremendous attention due to its capability to balance discovery and extraction and its versatility in various research areas due to its simplicity. In recent years, HS had been applied to multiple optimization issues, proving its superiority over other heuristic algorithms and meta-mathematical optimization approaches. The algorithm's continuous evolution and diverse applications to new sorts of healthcare issues demonstrated that HS was an excellent option. As a result, several types of research had been conducted to improve its efficiency. However, other further efforts were possible, including the following:

- Investigation into how to prevent being trapped in a local solution, since the majority of suggested HS had this issue;
- 2) Use HS to solve dynamic issues;
- 3) Create and evaluate methods for an ensemble of HS operators;
- 4) Propose a novel adaptive approach for parameter updating in the HS;
- 5) Address more real-world issues, such as the traveling salesman dilemma and time series forecasting;
- 6) Use HS to tackle difficulties with machine learning;
- 7) Investigate how well HS performs when confronted with confined issues;
- 8) Analyze the impact of hybridizing HS with additional EAs.

For additional research in the future, HS can be hybridized with several algorithms for healthcare problems to further validate its efficiency, such as the backtracking search optimization algorithm [94–96], the variants of evolutionary clustering algorithm star [97–100], chaotic sine cosine firefly algorithm [101], shuffled frog leaping algorithm [102] and hybrid artificial intelligence algorithms [103]. Furthermore, HS can be applied to more complex and real-world applications to explore more deeply the advantages and drawbacks of the algorithm or improve its efficiencies, such as engineering application problems [101], wind speed prediction [104–110], traffic flow prediction [111], laboratory management [112], e-organization and e-government services [113], online analytical processing [114], web science [115], and the Semantic Web ontology learning [116].

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References

- [1] Abdel-Raouf O, Metwally MA-B. A survey of harmony search algorithm. Int J Comput Appl 2013;70.
- [2] Geem ZW, Tseng C-L, Park Y. Harmony search for generalized orienteering problem: best touring in China. Int. Conf. Nat. Comput., Springer; 2005, p. 741–50.
- [3] Patil SA, Patel DA. An overview: Improved harmony search algorithm and its applications in mechanical engineering. Int J Eng Sci Innov Technol 2013;2:433–44.
- [4] Kougias I, Theodosiou N. A new music-inspired harmony based optimization algorithm. Theory and applications. Int. Conf. Prot. Restor. Environ. X, 2010.
- [5] Askarzadeh A, Rashedi E. Harmony search algorithm: Basic concepts and engineering applications. Intell. Syst. Concepts, Methodol. Tools, Appl., IGI Global; 2018, p. 1–30.
- [6] Geem ZW. Optimal cost design of water distribution networks using harmony search. Eng Optim 2006;38:259–77.
- [7] Lin C-C, Hung L-P, Liu W-Y, Tsai M-C. Jointly rostering, routing, and rerostering for home health care services: A harmony search approach with genetic, saturation, inheritance, and immigrant schemes. Comput Ind Eng 2018;115:151–66.
- [8] Castillo O, Valdez F, Peraza C, Yoon JH, Geem ZW. High-Speed Interval Type-2 Fuzzy Systems for Dynamic Parameter Adaptation in Harmony Search for Optimal Design of Fuzzy Controllers. Mathematics 2021;9:758.
- [9] Valdez F, Castillo O, Peraza C. Fuzzy logic in dynamic parameter adaptation of harmony search optimization for benchmark functions and fuzzy controllers. Int J Fuzzy Syst 2020;22:1198–211.
- [10] Peraza C, Valdez F, Castro JR, Castillo O. Fuzzy dynamic parameter adaptation in the harmony search algorithm for the optimization of the ball and beam controller. Adv Oper Res 2018;2018.
- [11] Pandiarajan K, Babulal CK. Fuzzy harmony search algorithm based optimal power flow for power system security enhancement. Int J Electr Power Energy Syst 2016;78:72–9.
- [12] Jalili A, Ghadimi N. Hybrid harmony search algorithm and fuzzy mechanism for solving congestion management problem in an electricity market. Complexity 2016;21:90–8.
- [13] Assad A, Deep K. Applications of harmony search algorithm in data mining: a survey. Proc. Fifth Int. Conf. Soft Comput. Probl. Solving, Springer; 2016, p. 863–74.
- [14] Gao K-Z, Suganthan PN, Pan Q-K, Chua TJ, Cai TX, Chong C-S. Discrete harmony search

algorithm for flexible job shop scheduling problem with multiple objectives. J Intell Manuf 2016;27:363–74.

- [15] Al-Betar MA, Khader AT. A harmony search algorithm for university course timetabling. Ann Oper Res 2012;194:3–31.
- [16] Geem ZW, Yoon Y. Harmony search optimization of renewable energy charging with energy storage system. Int J Electr Power Energy Syst 2017;86:120–6.
- [17] Abualigah LM, Khader AT, AlBetar MA, Hanandeh ES. A new hybridization strategy for krill herd algorithm and harmony search algorithm applied to improve the data clustering. 1st EAI Int. Conf. Comput. Sci. Eng., European Alliance for Innovation (EAI); 2016, p. 54.
- [18] Saadat J, Moallem P, Koofigar H. Training echo state neural network using harmony search algorithm. Int J Artif Intell 2017;15:163–79.
- [19] Geem ZW. Music-inspired harmony search algorithm: theory and applications. vol. 191. Springer; 2009.
- [20] Lee KS, Geem ZW. A new structural optimization method based on the harmony search algorithm. Comput Struct 2004;82:781–98.
- [21] Lee KS, Geem ZW. A new meta-heuristic algorithm for continuous engineering optimization: harmony search theory and practice. Comput Methods Appl Mech Eng 2005;194:3902–33.
- [22] Zhang T, Geem ZW. Review of harmony search with respect to algorithm structure. Swarm Evol Comput 2019;48:31–43.
- [23] Geem ZW, Kim JH, Loganathan GV. A new heuristic optimization algorithm: harmony search. Simulation 2001;76:60–8.
- [24] Abualigah L, Diabat A, Geem ZW. A comprehensive survey of the harmony search algorithm in clustering applications. Appl Sci 2020;10:3827.
- [25] Yang X-S. Harmony search as a metaheuristic algorithm. Music. Harmon. search algorithm, Springer; 2009, p. 1–14.
- [26] Manjarres D, Landa-Torres I, Gil-Lopez S, Del Ser J, Bilbao MN, Salcedo-Sanz S, et al. A survey on applications of the harmony search algorithm. Eng Appl Artif Intell 2013;26:1818–31.
- [27] Nazari-Heris M, Mohammadi-Ivatloo B, Asadi S, Kim J-H, Geem ZW. Harmony search algorithm for energy system applications: an updated review and analysis. J Exp Theor Artif Intell 2019;31:723–49.
- [28] Ala'a A, Alsewari AA, Alamri HS, Zamli KZ. Comprehensive review of the development of the harmony search algorithm and its applications. IEEE Access 2019;7:14233–45.
- [29] Yusup N, Zain AM, Latib AA. A review of Harmony Search algorithm-based feature selection method for classification. J. Phys. Conf. Ser., vol. 1192, IOP Publishing; 2019, p. 12038.
- [30] Kim JH, Lee HM. Investigating the convergence characteristics of harmony search. Harmon. Search Algorithm, Springer; 2016, p. 3–10.
- [31] Portilla-Flores EA, Sánchez-Márquez Ál, Flores-Pulido L, Vega-Alvarado E, Yañez MBC,

Aponte-Rodríguez JA, et al. Enhancing the harmony search algorithm performance on constrained numerical optimization. IEEE Access 2017;5:25759–80.

- [32] Al-Betar MA, Doush IA, Khader AT, Awadallah MA. Novel selection schemes for harmony search. Appl Math Comput 2012;218:6095–117.
- [33] Das S, Mukhopadhyay A, Roy A, Abraham A, Panigrahi BK. Exploratory power of the harmony search algorithm: analysis and improvements for global numerical optimization. IEEE Trans Syst Man, Cybern Part B 2010;41:89–106.
- [34] Ammar M, Bouaziz S, Alimi AM, Abraham A. Hybrid harmony search algorithm for global optimization. 2013 World Congr. Nat. Biol. Inspired Comput., IEEE; 2013, p. 69–75.
- [35] Shahemabadi AR, Noor SBM, Alizadeh M, Isa MM. A New Harmony Memory Updating Technique for Harmony Search Optimization Algorithm. Open Int J Informatics 2012;1:1– 14.
- [36] Geem ZW. Novel derivative of harmony search algorithm for discrete design variables. Appl Math Comput 2008;199:223–30.
- [37] Geem ZW, Tseng C-L. New Methodology, Harmony Search, its Robustness. GECCO Late Break. Pap., 2002, p. 174–8.
- [38] Wang C-M, Huang Y-F. Self-adaptive harmony search algorithm for optimization. Expert Syst Appl 2010;37:2826–37.
- [39] Mahdavi M, Fesanghary M, Damangir E. An improved harmony search algorithm for solving optimization problems. Appl Math Comput 2007;188:1567–79.
- [40] Omran MGH, Mahdavi M. Global-best harmony search. Appl Math Comput 2008;198:643– 56.
- [41] Zou D, Gao L, Wu J, Li S, Li Y. A novel global harmony search algorithm for reliability problems. Comput Ind Eng 2010;58:307–16.
- [42] Abdel-Raouf O, El-henawy I, Abdel-Baset M. Chaotic harmony search algorithm with different chaotic maps for solving assignment problems. Int J Comput Eng Manag 2014;17:10–5.
- [43] Yadav A, Yadav N, Kim JH. A study of harmony search algorithms: Exploration and convergence ability. Harmon. Search Algorithm, Springer; 2016, p. 53–62.
- [44] Geem ZW, Sim K-B. Parameter-setting-free harmony search algorithm. Appl Math Comput 2010;217:3881–9.
- [45] Kayhan AH, Korkmaz KA, Irfanoglu A. Selecting and scaling real ground motion records using harmony search algorithm. Soil Dyn Earthq Eng 2011;31:941–53.
- [46] Zou D, Gao L, Li S, Wu J. Solving 0–1 knapsack problem by a novel global harmony search algorithm. Appl Soft Comput 2011;11:1556–64.
- [47] Gao XZ, Govindasamy V, Xu H, Wang X, Zenger K. Harmony search method: theory and applications. Comput Intell Neurosci 2015;2015.
- [48] Moh'd Alia O, Mandava R. The variants of the harmony search algorithm: an overview. Artif Intell Rev 2011;36:49–68.

- [49] Zou D, Gao L, Wu J, Li S. Novel global harmony search algorithm for unconstrained problems. Neurocomputing 2010;73:3308–18.
- [50] Siddique N, Adeli H. Hybrid harmony search algorithms. Int J Artif Intell Tools 2015;24:1530001.
- [51] Niu Q, Zhang H, Wang X, Li K, Irwin GW. A hybrid harmony search with arithmetic crossover operation for economic dispatch. Int J Electr Power Energy Syst 2014;62:237–57.
- [52] Kaveh A, Talatahari S. Particle swarm optimizer, ant colony strategy and harmony search scheme hybridized for optimization of truss structures. Comput Struct 2009;87:267–83.
- [53] Srikanth R, Bikshalu K. Multilevel thresholding image segmentation based on energy curve with harmony Search Algorithm. Ain Shams Eng J 2021;12:1–20.
- [54] Fachrurrozi M, Dela NR, Mahyudin Y, Putra HK. Tongue image segmentation using hybrid multilevel otsu thresholding and harmony search algorithm. J. Phys. Conf. Ser., vol. 1196, IOP Publishing; 2019, p. 12072.
- [55] Yang Z, Shufan Y, Li G, Weifeng D. Segmentation of MRI brain images with an improved harmony searching algorithm. Biomed Res Int 2016;2016.
- [56] Tuo S, Liu H, Chen H. Multipopulation harmony search algorithm for the detection of highorder SNP interactions. Bioinformatics 2020;36:4389–98.
- [57] Koti P, Dhavachelvan P, Kalaipriyan T, Arjunan S, Uthayakumar J, Sujatha P. An efficient healthcare framework for kidney disease using hybrid harmony search algorithm. Electron Gov an Int J 2020;16:56–68.
- [58] Tuo S, Zhang J, Yuan X, He Z, Liu Y, Liu Z. Niche harmony search algorithm for detecting complex disease associated high-order SNP combinations. Sci Rep 2017;7:1–18.
- [59] Hickmann KS, Fairchild G, Priedhorsky R, Generous N, Hyman JM, Deshpande A, et al. Forecasting the 2013–2014 influenza season using Wikipedia. PLoS Comput Biol 2015;11:e1004239.
- [60] Gandhi TK, Chakraborty P, Roy GG, Panigrahi BK. Discrete harmony search based expert model for epileptic seizure detection in electroencephalography. Expert Syst Appl 2012;39:4055–62.
- [61] Koti P, Dhavachelvan P, Kalaipriyan T, Arjunan S, Uthayakumar J, Sujatha P. Heart Disease Prediction Using Hybrid Harmony Search Algorithm with Levi Distribution. Int J Mech Eng Technol Vol n.d.;9:980–94.
- [62] Sarkar SS, Sheikh KH, Mahanty A, Mali K, Ghosh A, Sarkar R. A harmony search-based wrapper-filter feature selection approach for microstructural image classification. Integr Mater Manuf Innov 2021;10:1–19.
- [63] Dash R. An adaptive harmony search approach for gene selection and classification of high dimensional medical data. J King Saud Univ Inf Sci 2021;33:195–207.
- [64] Bae JH, Kim M, Lim JS, Geem ZW. Feature Selection for Colon Cancer Detection Using K-Means Clustering and Modified Harmony Search Algorithm. Mathematics 2021;9:570.
- [65] Mousavi SM, Abdullah S, Niaki STA, Banihashemi S. An intelligent hybrid classification algorithm integrating fuzzy rule-based extraction and harmony search optimization: Medical diagnosis applications. Knowledge-Based Syst 2021;220:106943.

- [66] Kar S, Das Sharma K, Maitra M. Adaptive weighted aggregation in Group Improvised Harmony Search for lung nodule classification. J Exp Theor Artif Intell 2020;32:219–42.
- [67] Sudha MN, Selvarajan S. Hybrid approach towards feature selection for breast tumour classification from screening mammograms. Int J Biomed Eng Technol 2019;29:309–26.
- [68] Alexandre E, Cuadra L, Gil-Pita R. Sound classification in hearing aids by the harmony search algorithm. Music. Harmon. Search Algorithm, Springer; 2009, p. 173–88.
- [69] Alexandre E, Álvarez L, Amor J, Gil-Pita R, Huerta E. Music-inspired harmony search algorithm applied to feature selection for sound classification in hearing AIDS. Audio Eng. Soc. Conv. 124, Audio Engineering Society; 2008.
- [70] Al-Shaikh A, Mahafzah BA, Alshraideh M. Hybrid harmony search algorithm for social network contact tracing of COVID-19. Soft Comput 2021:1–23.
- [71] Rajinikanth V, Dey N, Raj ANJ, Hassanien AE, Santosh KC, Raja N. Harmony-search and otsu based system for coronavirus disease (COVID-19) detection using lung CT scan images. ArXiv Prepr ArXiv200403431 2020.
- [72] Panchal A. Harmony search in therapeutic medical physics. Music. Harmon. search algorithm, Springer; 2009, p. 189–203.
- [73] Alinaghian M, Hejazi SR, Bajoul N. A novel hierarchical model to locate health care facilities with fuzzy demand solved by harmony search algorithm. Int J Supply Oper Manag 2014;1:245–59.
- [74] Landa-Torres I, Manjarres D, Salcedo-Sanz S, Del Ser J, Gil-Lopez S. A multi-objective grouping harmony search algorithm for the optimal distribution of 24-hour medical emergency units. Expert Syst Appl 2013;40:2343–9.
- [75] Doush IA, Al-Betar MA, Awadallah MA, Hammouri AI, Ra'ed M, ElMustafa S, et al. Harmony search algorithm for patient admission scheduling problem. J Intell Syst 2020;29:540–53.
- [76] Yagmur EC, Sarucan A. Nurse scheduling with opposition-based parallel harmony search algorithm. J Intell Syst 2019;28:633–47.
- [77] Hadwan M, Ayob M, Rassam MA, Hezam EA. Deluge harmony search algorithm for nurse rostering problems. 2019 First Int. Conf. Intell. Comput. Eng., IEEE; 2019, p. 1–5.
- [78] Hadwan M, Ayob M, Al-Hagery M, Al-Tamimi BN. Climbing harmony search algorithm for nurse rostering problems. Int. Conf. Reliab. Inf. Commun. Technol., Springer; 2018, p. 74– 83.
- [79] Hadwan M, Ayob M, Sabar NR, Qu R. A harmony search algorithm for nurse rostering problems. Inf Sci (Ny) 2013;233:126–40.
- [80] Ayob M, Hadwan M, Ahmad Nazr MZ, Ahmad Z. Enhanced harmony search algorithm for nurse rostering problems. J Appl Sci 2013;13:846–53.
- [81] Awadallah MA, Khader AT, Al-Betar MA, Bolaji AL. Global best harmony search with a new pitch adjustment designed for nurse rostering. J King Saud Univ Inf Sci 2013;25:145– 62.
- [82] Awadallah MA, Khader AT, Al-Betar MA, Bolaji AL. Nurse scheduling using harmony search. 2011 Sixth Int. Conf. Bio-Inspired Comput. Theor. Appl., IEEE; 2011, p. 58–63.

- [83] Awadallah MA, Khader AT, Al-Betar MA, Bolaji AL. Nurse rostering using modified harmony search algorithm. Int. Conf. Swarm, Evol. Memetic Comput., Springer; 2011, p. 27–37.
- [84] Awadallah MA, Al-Betar MA, Khader AT, Bolaji AL, Alkoffash M. Hybridization of harmony search with hill climbing for highly constrained nurse rostering problem. Neural Comput Appl 2017;28:463–82.
- [85] Alomoush AA, Younis MI, Aloufi KS, Alsewari AA, Zamli KZ. Pressure Vessel Design Simulation Using Hybrid Harmony Search Algorithm. Proc. 2019 3rd Int. Conf. Big Data Res., 2019, p. 37–41.
- [86] Firmansyah E, Rosmawati R, Fuadi RS, Fauzy D, Ramdhani MA. Design of expert system to determine the proper diet using harmony search method. J. Phys. Conf. Ser., vol. 1402, IOP Publishing; 2019, p. 77006.
- [87] Gupta B, Tiwari M, Lamba SS. Visibility improvement and mass segmentation of mammogram images using quantile separated histogram equalisation with local contrast enhancement. CAAI Trans Intell Technol 2019;4:73–9.
- [88] Haridoss R, Punniyakodi S. Compression and enhancement of medical images using opposition based harmony search algorithm. J Inf Process Syst 2019;15:288–304.
- [89] Taghipour S, Zarrineh P, Ganjtabesh M, Nowzari-Dalini A. Improving protein complex prediction by reconstructing a high-confidence protein-protein interaction network of Escherichia coli from different physical interaction data sources. BMC Bioinformatics 2017;18:1–9.
- [90] Dongardive J, Patil A, Bir A, Jamkhedkar S, Abraham S. Finding motifs using harmony search. Proc. Int. Symp. Biocomput., 2010, p. 1–4.
- [91] Panchal A, Tom B. Harmony search optimization for HDR prostate brachytherapy. Int J Radiat Oncol Biol Phys 2009;75:S720–1.
- [92] Saka MP, Hasançebi O, Geem ZW. Metaheuristics in structural optimization and discussions on harmony search algorithm. Swarm Evol Comput 2016;28:88–97.
- [93] Weyland D. A rigorous analysis of the harmony search algorithm: How the research community can be misled by a "novel" methodology. Int J Appl Metaheuristic Comput 2010;1:50–60.
- [94] Hassan BA, Rashid TA. Operational framework for recent advances in backtracking search optimisation algorithm: A systematic review and performance evaluation. Appl Math Comput 2019:124919.
- [95] Hassan BA, Rashid TA. Datasets on statistical analysis and performance evaluation of backtracking search optimisation algorithm compared with its counterpart algorithms. Data Br 2020;28:105046.
- [96] Tian Z. Backtracking search optimization algorithm-based least square support vector machine and its applications. Eng Appl Artif Intell 2020;94:103801.
- [97] Hassan BA, Rashid TA. A multidisciplinary ensemble algorithm for clustering heterogeneous datasets. Neural Comput Appl 2021. https://doi.org/10.1007/s00521-020-05649-1.

- [98] Hassan BA, Rashid TA, Hamarashid HK. A Novel Cluster Detection of COVID-19 Patients and Medical Disease Conditions Using Improved Evolutionary Clustering Algorithm Star. Comput Biol Med 2021:104866.
- [99] Hassan BA, Rashid TA, Mirjalili S. Formal context reduction in deriving concept hierarchies from corpora using adaptive evolutionary clustering algorithm star. Complex Intell Syst 2021:1–16.
- [100] Hassan BA, Rashid TA, Mirjalili S. Performance evaluation results of evolutionary clustering algorithm star for clustering heterogeneous datasets. Data Br 2021:107044.
- [101] Hassan BA. CSCF: a chaotic sine cosine firefly algorithm for practical application problems. Neural Comput Appl 2020:1–20.
- [102] Maaroof BB, Rashid TA, Abdulla JM, Hassan BA, Alsadoon A, Mohamadi M, et al. Current Studies and Applications of Shuffled Frog Leaping Algorithm: A Review. Arch Comput Methods Eng 2022:1–16.
- [103] Hassan BA, Rashid TA. Artificial Intelligence Algorithms for Natural Language Processing and the Semantic Web Ontology Learning. ArXiv Prepr ArXiv210813772 2021.
- [104] Tian Z. Short-term wind speed prediction based on LMD and improved FA optimized combined kernel function LSSVM. Eng Appl Artif Intell 2020;91:103573.
- [105] Tian Z. Modes decomposition forecasting approach for ultra-short-term wind speed. Appl Soft Comput 2021;105:107303.
- [106] Tian Z, Li H, Li F. A combination forecasting model of wind speed based on decomposition. Energy Reports 2021;7:1217–33.
- [107] Tian Z, Chen H. Multi-step short-term wind speed prediction based on integrated multimodel fusion. Appl Energy 2021;298:117248.
- [108] Tian Z, Chen H. A novel decomposition-ensemble prediction model for ultra-short-term wind speed. Energy Convers Manag 2021;248:114775.
- [109] Tian Z, Li S, Wang Y. A prediction approach using ensemble empirical mode decomposition-permutation entropy and regularized extreme learning machine for short-term wind speed. Wind Energy 2020;23:177–206.
- [110] Tian Z. Preliminary research of chaotic characteristics and prediction of short-term wind speed time series. Int J Bifurc Chaos 2020;30:2050176.
- [111] Tian Z. Approach for short-term traffic flow prediction based on empirical mode decomposition and combination model fusion. IEEE Trans Intell Transp Syst 2020;22:5566– 76.
- [112] Saeed MHR, Hassan BA, Qader SM. An Optimized Framework to Adopt Computer Laboratory Administrations for Operating System and Application Installations. Kurdistan J Appl Res 2017;2:92–7.
- [113] Hassan BA, Ahmed AM, Saeed SA, Saeed AA. Evaluating e-Government Services in Kurdistan Institution for Strategic Studies and Scientific Research Using the EGOVSAT Model. Kurdistan J Appl Res 2016;1:1–7.
- [114] Hassan BA, Qader SM. A New Framework to Adopt Multidimensional Databases for Organizational Information Sys-tem Strategies n.d.

- [115] Hassan BA. Analysis for the overwhelming success of the web compared to microcosm and hyper-G systems. ArXiv Prepr ArXiv210508057 2021.
- [116] Hassan B, Dasmahapatra S. Towards Semantic Web: Challenges and Needs n.d.