Heat transfer enhancement using hybrid nanoparticles in ethylene glycol through a horizontal heated tube

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ABSTRACT

Heating hybrid nanofluids by the mixing of solid nanoparticles suspended in liquid represents a new class of heat transfer enhancement. To enhance heat transfer for many industrial applications, a computational fluid dynamics modelling simulation using the finite volume method and adopting the SIMPLE algorithm was performed. The mixture of aluminium nitride nanoparticles into ethylene glycol which acts as a base fluid is considered as a new concept of hybrid nanofluids that can increase heat transfer. The hybrid nanofluid was prepared experimentally with a volume fraction range of 1% to 4%. The size diameter of nanoparticles, heat flux around a horizontal straight tube, and Reynolds number is approximately 30 nm, 5000 w/m^2 and 5,000 to 17,000, respectively. The computational method had been successfully validated using available experimental data reported in the literature. It was found that 1% to 3% Aluminum nitride hybrid nanofluids can significantly affect efficiency, while more than 3% volume fraction are insignificant as they obtain less than one efficiency. Results show that a combination of aluminium nitride nanoparticles with the EG base fluid tends to augment heat transfer performance significantly.

Keywords: Nanofluid; hybrid; ethylene glycol; turbulent; CFD.

INTRODUCTION

Heat transfer enhancement using hybrid nanofluids is a new trend [1-3]. An experimental investigation was conducted by passing a hybrid nanofluid through a double pipe heat exchanger as shown in [4]. It was found that the hybrid nanofluid performance was enhanced up to 35% in comparison with liquids at high volume concentrations. Experimental studies using other types of nanofluids such as Cu, CuO, Fe_2O_3, Al_2O_3, CNT, SiO_2, TiO_2, SiC, Ag, and zirconia through a tube have been conducted by many researchers [5-13]. Choi [14] prepared a nanofluid by engineering colloids made of a base fluid and nanoparticles. Nanoparticles have thermal conductivities at typically an order of magnitude higher than those of the base fluids and with sizes significantly smaller than 100 nm [15-18]. The benefit of thermal fluid properties plays an important role in improving equipment heat transfer performance. Nanofluids are a new class of working fluids with the capability to enhance suspension stability and conductivity for various industrial applications [19-22]. Recent interesting discussions have focused on nanocomposite materials in order to find new hybrid nanofluids that give the highest heat

transfer rates [23, 24]. Cu-Al₂O₃/water hybrid nanofluids were synthesized using a two-step method by adopting the hydrogen reduction technique by Suresh et al. [25]. The hybrid nanofluids' volume fractions from 0.1% to 2% were prepared by dispersing the synthesized nanocomposite powder in deionized water. Results indicated that both thermal conductivity and viscosity of the prepared hybrid nanofluids increase as the nanoparticles' volume fraction increases. It was found that the increase in viscosity is higher than the increase in the thermal conductivity of hybrid nanofluids. A fully developed laminar convective heat transfer and pressure drop characteristics investigation using a uniformly heated circular tube and Cu-Al₂O₃/water hybrid nanofluid has been carried out by Suresh et al. [25]. The results showed that the Nusselt number was enhanced by 13.56% at a Reynolds number of 1730, compared to the Nusselt number of water. The regression equations between the input and output parameters were in good agreement with the experimental data.

The convective heat transfer of hybrid nanofluid flow through a tubular heat exchanger was experimentally studied on by Madhesh et al. [26]. The hybrid nanofluid was prepared by dispersing copper-titanium nanocomposite in water at 0.1% to 1.0% volume fractions. Results showed that the convective heat transfer coefficient increased by 48.4% for up to 0.7% of the volume fraction of the hybrid nanofluid. The effect of the functionalisation method on the stability and thermal conductivity of CNT- Alumina hybrid nanofluid was investigated on by Abbasi et al. [27]. The thermal conductivities of different hybrid nanofluids were measured using a modified transient hot wire method. Results showed that functional groups have a significant influence on the thermal conductivity of hybrid nanofluids. Thermal conductivity improved up to 20.68% at a 0.1% volume concentration of hybrid nanofluid. Mosayebidorcheh et al. [28] studied the turbulent nanofluid heat transfer in the presence of a magnetic field. Results illustrated that the Nusselt number increases linearly with the Reynolds number, nanoparticle volume fraction and turbulent Eckert number, while it is inversely proportional with the Hartmann number and turbulent parameter. Labib et al. [29] selected a two-phase mixture model to study hybrid nanofluid convective heat transfer. They employed two different base fluids individually to investigate their effect on convective heat transfer mixing of Alumina nanoparticles. Results indicated that the use of EG as base fluid gives better heat transfer augmentation than that of water. A comparison of the computational model for CNTs/water nanofluid was conducted in order for it to be validated using available data in the literature. Sundar et al. [30] studied turbulent heat transfer of hybrid nanofluids flowing through a circular tube. The Fe₃O₄/MWCNT nanocomposites were prepared by in-situ method which included the dispersion of carboxylated carbon nanotubes in distilled water and the mixing of ferrous chloride and ferric chloride. Results showed that heat transfer was enhanced by 31.10% with a penalty of 1.18-times increase of pumping power for a particle loading of 0.3% at a Reynolds number of 22,000 as compared to base fluid data. The correlation equations proposed for the input and output parameters were in good agreement with the experimental data. Baby and Ramaprabhu [31] synthesized Fe₃O₄/MWNTs and Fe₃O₄-SiO₂/MWNTs using a simple chemical reduction technique and dispersed it in water using ultrasonication. It was observed that Fe₃O₄/MWNTs with surfactant and Fe₃O₄-SiO₂/MWNTs without surfactant at 0.03% volume concentrations of a magnetic field improve thermal conductivity by 20% and 24.5%, respectively.

The present article studies the heat transfer and pressure drop characteristics of hybrid nanofluids under turbulent flow conditions in a circular tube. This article proves the heat transfer enhancement and pressure drop of hybrid nanofluids using CFD analysis

by commercial software. The two nanocomposites used in this work are aluminium and nitride from 1% to 4% volume fractions dispersed in EG as a base fluid.

METHODS AND MATERIALS

Nanofluid Preparation
The nanofluids were prepared in a thermal laboratory of the Faculty of Mechanical Engineering, University Malaysia Pahang. Nanopowders were purchased from US Research Nanomaterials, Inc. (NovaScientific Resources (M) Sdn. Bhd). Measured quantities of nanoparticles were dispersed in EG to obtain mass concentration nanofluids. A mechanical stirrer was used to achieve a homogenously dispersed solution. This method was done according to [32] and then subjected to ultrasonic for at least 3 hrs to break up any residual agglomerations. The mass of the nanoparticles (m_p) and EG (m_f) were measured accurately (0.001 g). The sedimentation of nanoparticles at the bottom of the samples showed the changes in physical properties of the bulk nanofluids with time [33]. In the case undertaken, the measurement of nanofluids' thermal properties require many individual measurements for at least one month in order to check for sample stability. Samples were checked after the conclusion of each test was finished but no visible sedimentation was found. The transient hot-wires method shown in Figure 1(a) was used to measure the thermal conductivity of nanofluids experimentally. The wire was placed along the axis of a container and surrounded by the nanofluid in order to measure the nanofluid's thermal conductivity. Platinum has a high electrical resistivity; i.e., 1.06 × 10−7Ω m (at 20 °C), an order of magnitude higher than that of other metals.
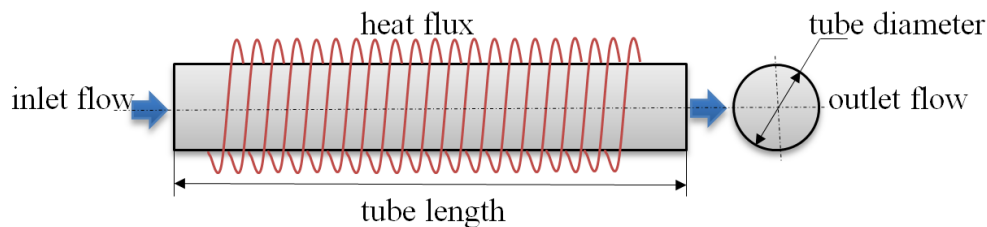
(a) Schematic diagram of physical model
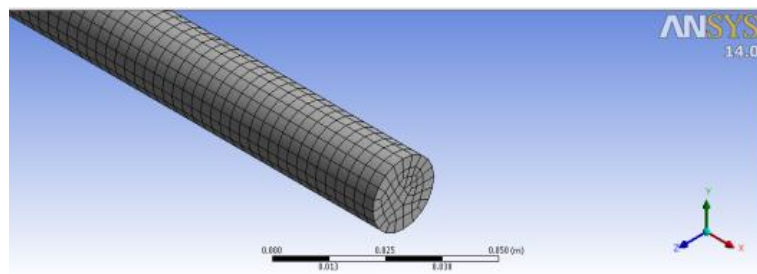
(b) Meshing surfaces

Figure 1. Geometry and grid computational model.

In addition, platinum has a temperature coefficient of resistance of 0.0003925 °C^{-1} (for pure platinum) which is much higher than that of other metals available to be chosen as wire material. The wire was also used as a line heat source, thus the wire's diameter was kept within 100 μm. The length of the wire was kept to just a few centimetres

compared to the wire's diameter which represents an infinitely long line heat source so as to assure a directional (radial) heat transfer. Calibration was conducted using a standard fluid (glycerine) which was already brought with the device. The error between reading data and the standard was 0.0023. After verification was performed using pure EG and compared with the standard, the error between them was 0.0014 [2]. Viscosity is an important indication in evaluating the thermal properties of nanofluids. A commercial Brookfield DV-I prime viscometer was used to measure viscosity at different temperatures and rotor RPMs as shown in Figure 1(b). Base fluid ethylene glycol (EG) was used to measure viscosity for calibration purposes. After that, the experimented nanofluid was used to measure viscosity.

Thermal properties

The masses of nanoparticles (m_p) and EG (m_f) were measured accurately (0.001 g) to estimate the weight percentage (φ) by using Eq. (1) [34, 35]:

$$\varphi = \left(\frac{m_p}{\left(m_p + m_f \right)} \right) \times 100 \tag{1}$$

Equation (2) was used to estimate the volume fraction of the nanofluid ϕ depending on the nanoparticles' density (ρ_p) and base fluid density (ρ_f) at 25 °C.

$$\phi = \frac{\dfrac{m_p}{\rho_p}}{\dfrac{m_p}{\rho_p} + \dfrac{m_f}{\rho_f}} \tag{2}$$

The pH values of the nanofluid were measured using an OAKTON device for the nanofluid volume fractions of 1% to 4%. The pH values before and after experimental tests refer to the nanofluids stability and changes in thermophysical properties. If the pH values of a suspension decrease, the force among particles will increase and the movement of the nanoparticle suspension enhances the heat transfer process. In order to augment heat transfer for many applications, the pH of the nanofluids should be kept at low values [36]. The hybrid mixture of aluminium nanopowders and nitrides suspended in EG nanofluids were considered as a single-phase flow incompressible Newtonian fluid. The isotropic and thermal properties of aluminium and nitride nanopowders are shown in Table 1.

Table 1. Thermal properties.

Property	EG	Aluminum nitride (AlN)
Density (kg/m^3)	1101	3260
Specific heat (J/kg.K)	2382	735
Thermal conductivity (W/m.K)	0.256	180
Viscosity (kg/m.s)	0.0095	-

Simulation Process

The forced convection of a hybrid nanofluid consisting of EG and AlN nanopowders through a straight horizontal tube with 27 nm size diameter and 5000 W/m^2 uniform heat flux around the tube wall was employed under turbulent conditions. The schematic diagram of the physical model shown in Figure 2 represents a two-dimensional nanofluid flow through a circular horizontal tube with a length of 2000 mm. In this study, rectangular cells were used as the meshing surfaces of the tube wall as shown in Figure 2.
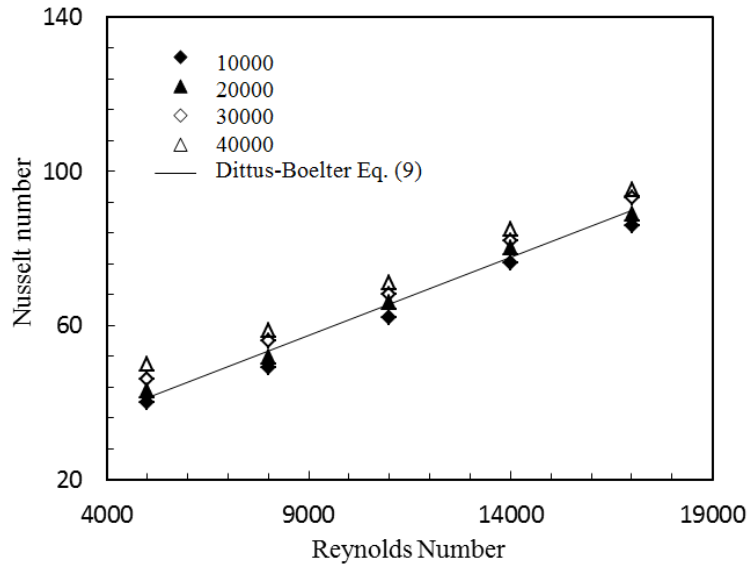

Figure 2. Grid independent test.

The diameter and thickness of the tube is 19 mm and 2 mm, respectively. It is similar in geometry to the numerical work used by [34] who numerically investigated the turbulent convective heat transfer and pressure drop characteristics of TiO$_2$/water nanofluid inside a circular tube. The model assumed that the flow is steady, turbulent, and symmetrical with respect to the horizontal plane passing through the circular tube. For all these assumptions, the dimensional conservation equations are the continuity, momentum, and energy equations [35]:

$$\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 0 \tag{3}$$

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = -\frac{1}{\rho}\frac{\partial P}{\partial x} + \upsilon\frac{\partial^2 u}{\partial x^2} \tag{4}$$

$$u\frac{\partial T}{\partial x} + v\frac{\partial T}{\partial y} = \alpha\frac{\partial^2 T}{\partial x^2} \tag{5}$$

A high Reynolds number was included as an input parameter, the pressure treatment adopted used the SIMPLE scheme, and a turbulent viscous k-ε model was also used. The solutions were considered to be converged at residuals lower than 10^{-6}. The simulation results were compared to equations for the friction factor (8) and Nusselt number (9) correlated by Blasius and Dittus-Boelter respectively [6, 35]:

$$f = \frac{0.316}{Re^{0.25}} \qquad (6)$$
$$Nu = 0.023 \times Re^{0.8} \times Pr^{0.4} \qquad (7)$$

The percentages of heat transfer enhancement and efficiency depending on the nanofluid and base fluid used were evaluated as [35]:

$$E\% = \frac{Nu_{nf} - Nu_f}{Nu_{nf}} \times 100 \qquad (8)$$

$$\eta = \left(\frac{Nu_{nf}}{Nu_f}\right) \bigg/ \left(\frac{f_{nf}}{f_f}\right)^{1/3} \qquad (9)$$

Boundary Conditions
The volume fractions of the AlN-EG hybrid nanofluid used as the input fluid were 1, 2, 3, and 4% with an inlet temperature of 30 ℃. EG was used as the working fluid for comparison purposes and a CFD analysis was performed with a uniform velocity profile at the inlet and a pressure outlet condition at the outlet regions. The tube was assumed to have perfectly smooth walls and the Reynolds number was varied from 5000 to 17000 at each iteration step as input data.

Grid Independence Test
The grid independence test was performed using the ANSYS software and it was found that 20000 cells (2000×10) was the best size of mesh, thus was adopted as the optimum meshing size. Four different meshing sizes were considered; 10000 cells (1000×10), 20000 cells (2000×10), 30000 cells (1000×30) and 40000 cells (2000×20) for EG to check grid sizing. A comparison of the Nusselt number for all four meshing sizes using the Dittus-Boelter Eq. (9) showed good agreement with a maximum deviation of not more than 5% (see Figure 2). It can be seen that all of the meshing sizes chosen could have been used but the 20000 cells meshing size was considered the optimum meshing size due to its best accuracy.

CFD Analysis
CFD simulations were performed using the ANSYS software with solver strategy. The governing single-phase conservation equations were solved using the control volume approach. The simulation results were compared to the predicted results of [28-30] and [34]. The simulation study consisted of building a geometry construction of a circular tube and meshing to create a physical model, choosing boundary conditions, and finally setup and solving. All scalar values and velocity components of the problem were calculated at the centre of the control volume interface where grid schemes were used intensively. Residuals appeared throughout the iterative process. Finally, the results were obtained when the solution converged, defined by a set of convergence criteria. The Nusselt number and pressure drop inside the circular tube were determined throughout the computational domain in the post-process stage.

RESULTS AND DISCUSSION

Validation
The CFD analysis was successfully validated with experimental data reported by Hejazian et al. [36] and Sundar & Sharma [37] for Al_2O_3/water under turbulent flow conditions as shown in Figure 3. Likewise, the CFD results were compared to the numerical data of

Bianco et al. [38] and Bianco et al. [39] under turbulent flow conditions for Al_2O_3/water nanofluid through a circular tube. It can be seen that the maximum deviations between the experimental and numerical results of the friction factor and Nusselt number did not exceed 8%.
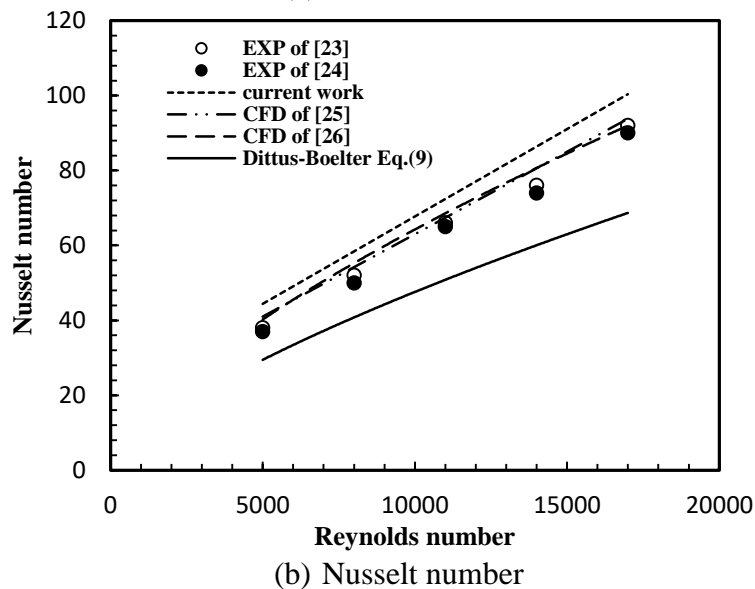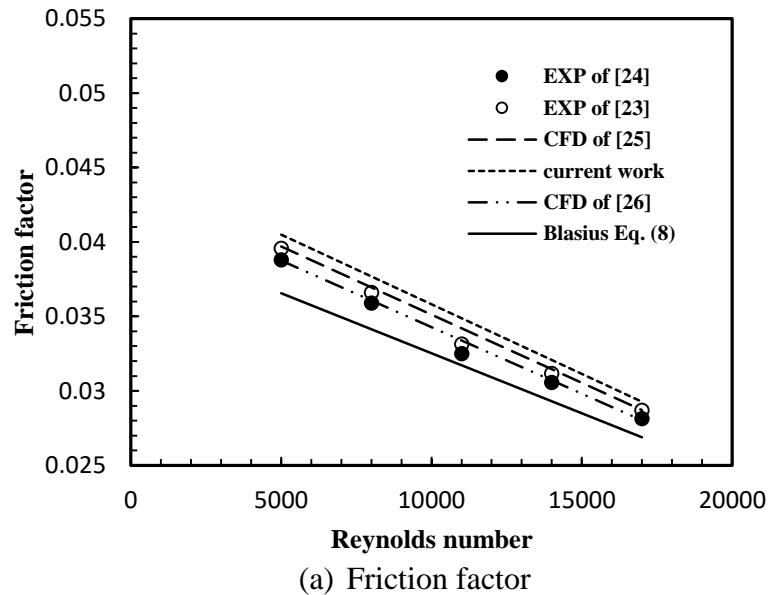

(a) Friction factor

(b) Nusselt number

Figure 3. Validation of the friction factor and Nusselt number.

Pressure Drop

In order to apply hybrid nanofluids in industrial applications, pressure drop should be investigated with Nusselt number inherently. The CFD data of pressure drop against Reynolds number are illustrated in Figure 4. It can be noted that the pressure drop increased by 13% with an increase in Reynolds number due to the increase of velocity inside the tube. Likewise, the pressure drop increased by 14% with an increase of the hybrid nanofluid volume fraction due to the increase in viscosity of the hybrid nanofluid. Meanwhile, the hybrid nanofluid incurred a little penalty in the pressure drop. The numerical data on pressure drop in this study are in good agreement with [36] and [40].
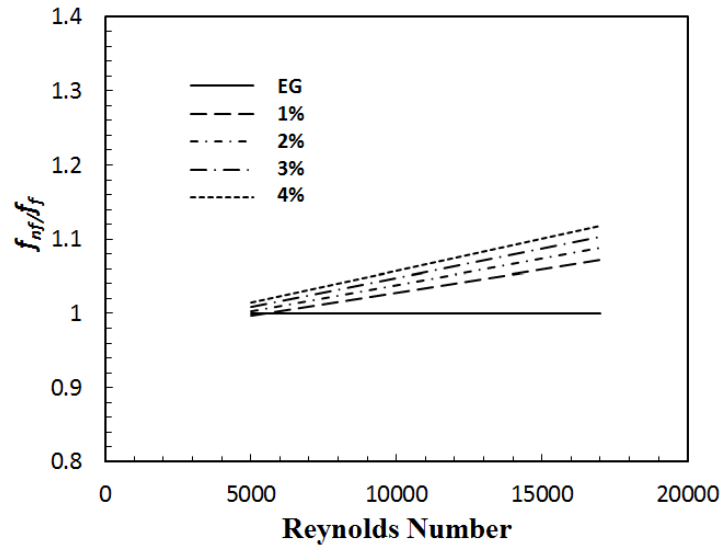
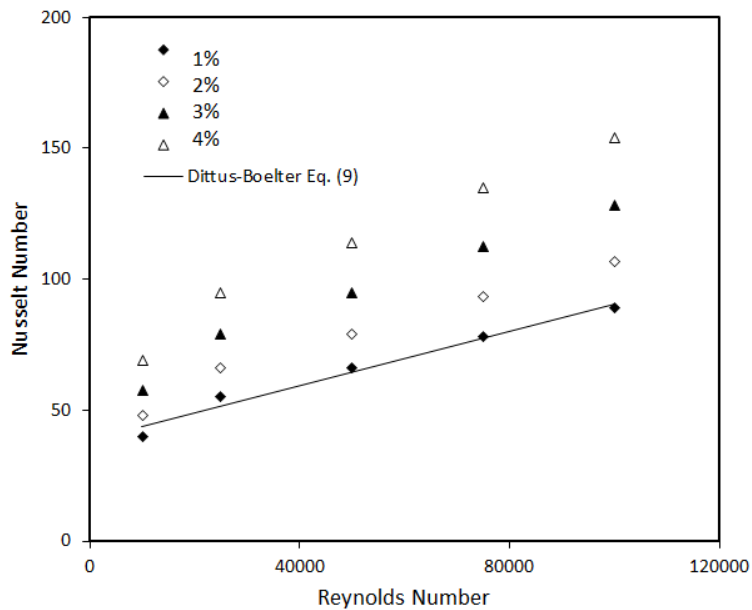Figure 4. The friction factor ratio at different Reynolds numbers.

Figure 5. Nusselt number at different Reynolds numbers.

Nusselt Number

Figure 5 shows the ratio of the hybrid nanofluid's Nusselt number to that of the base fluid at different Reynolds numbers. It can be seen that there was a significant increase of Nusselt number with the increase in Reynolds number. In this CFD analysis, the maximum heat transfer enhancement achieved was about 1.5 for 3% of hybrid nanopowder volume fraction in EG at a Reynolds number of 17000. The Nusselt number values for the hybrid nanofluid were up to 50% higher than the values gained for EG flows in the circular tube. The results are similar to the Nusselt number enhancement of Al_2O_3/water nanofluid at different volume fractions achieved by Hejazian et al. [36] and Heyhat et al. [40]. It can be said that heat transfer enhancement using hybrid nanofluid volume fractions agree with the literature results of [36] and [40]. A numerical study by

[34] reported an increase in Nusselt number at 13.6% for TiO_2/water using the same geometry. The benefit of using AlN hybrid nanofluids in a horizontal circular tube is significantly clear compared to using the TiO_2/water nanofluid.

Heat transfer enhancement

Figure 6 shows the heat transfer enhancement with the nanofluid volume fractions. It was observed that the heat transfer enhancement obtained ranged from 28% to 50% at hybrid nanoparticles' volume fractions of 1% to 3%, respectively, whereas, 33% of heat transfer enhancement was observed at the 4% hybrid nanofluid volume fraction. The CFD analysis of the heat transfer enhancement appeared to have slightly closer results to the experimental data of [36]and [40] for the Al_2O_3/water nanoparticle volume fractions under turbulent flow conditions inside a circular tube.
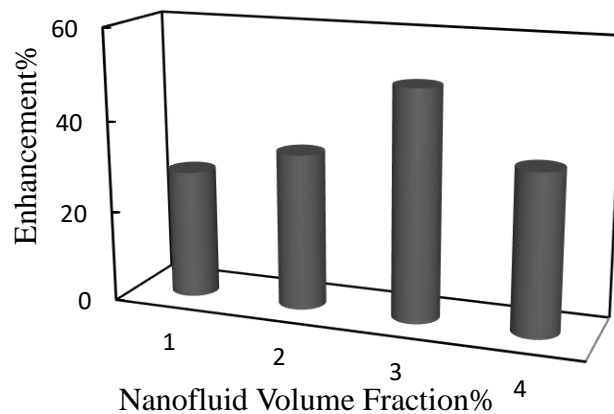

Figure 6. The heat transfer enhancement at different hybrid nanofluid volume fractions.
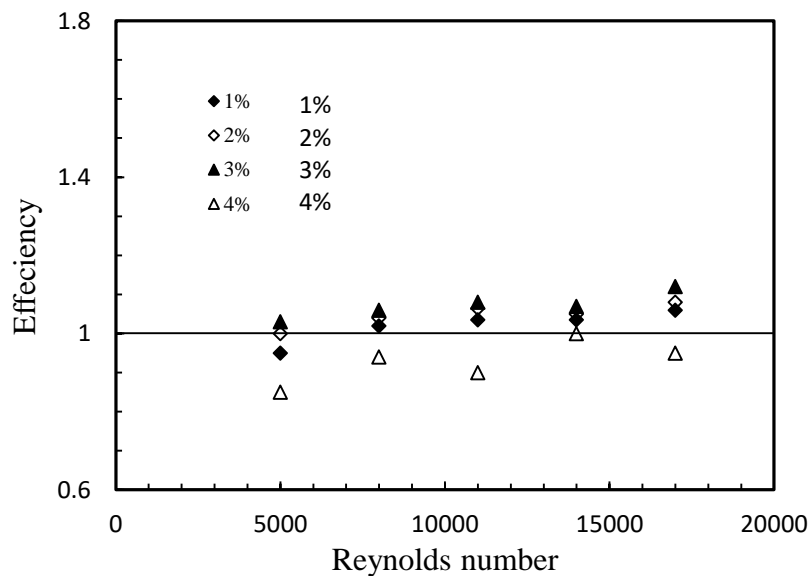

Figure 7. The efficiency of hybrid nanofluids at different Reynolds numbers.

Efficiency

Both the friction factor and Nusselt number do enhance heat transfer. Therefore, the overall efficiency of heat transfer enhancement for various volume fractions of the hybrid

nanofluid against their Reynolds numbers is shown in Figure 7. It can be seen that there is a net energy gain for cases where the heat transfer enhancement is greater than one. Therefore, it can be said that the use of 1% to 3% hybrid nanofluids is significant with respect to both heat transfer and friction factor, while using more than 3% volume fractions gives insignificant results as the readings obtained less than one efficiency. The reason for the insignificance is due to the pressure drop which needs a high pumping power through the circular tube. The study's thermal efficiency results are in agreement with Darzi et al.'s [41] results for heat transfer augmentation using Al_2O_3/water nanoparticles which is higher than the pressure drop penalty.

CONCLUSIONS

In this study, a CFD analysis was conducted to investigate the effect of AlN hybrid nanopowders on heat transfer and pressure drop inside a horizontal circular tube. A grid independence test was performed using the ANSYS/FLUENT software, and the 20000 cells (2000x10) mesh was adopted as the optimum meshing size. The CFD analysis was successfully validated with experimental and numerical results reported in the literature [36-39]. Obviously, the pressure drop grew as the Reynolds number and nanofluid volume fractions increased. It was observed that the maximum values of Nusselt number ratio for the 3% hybrid nanofluid were up to 50% higher than the values gained for EG flows through the circular tube, whereas low values of Nusselt number were observed for the 4% hybrid nanofluid volume fraction. The heat transfer enhancement obtained was from 28% to 50% at the 1% to 3% AlN nanoparticle volume fractions respectively, whereas 33% heat transfer enhancement was observed for the 4% hybrid nanofluid volume fraction. It was found that the use of 1% to 3% AlN hybrid nanofluids was significant with respect to efficiency, while more than 3% volume fraction was insignificant due to obtaining less than one efficiency.

ACKNOWLEDGMENTS

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NOMENCLATURES

C -   specific heat capacity [J/ kg K]
D -   diameter [m]
E -   enhancement
f -   friction factor
h -   convection heat transfer coefficient [W/m^2. K]
k -   thermal conductivity [W/m. K]
Nu - Nusselt Number [hD/k]
P -   Pressure [N/m^2]
Pr - Prandtle Number [$C\mu/k$]
Re - Renolds Number [$\rho Du/\mu$]
u -   Velocity [m/s]
μ -   Viscosity [N.s /m^2]
ρ -   Density [kg/m^3]
φ -   Volume concentration
η -   efficiency

Subscripts
f liquid phases
p solid particle
eff   effective nanofluid