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Hemodynamics of Cerebral Aneurysms

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Abstract

The initiation and progression of cerebral aneurysms are degenerative processes of the arterial wall driven by a complex interaction of biological and hemodynamic factors. Endothelial cells on the artery wall respond physiologically to blood-flow patterns. In normal conditions, these responses are associated with nonpathological tissue remodeling and adaptation. The combination of abnormal blood patterns and genetics predisposition could lead to the pathological formation of aneurysms. Here, we review recent progress on the basic mechanisms of aneurysm formation and evolution, with a focus on the role of hemodynamic patterns.

Keywords

intracranial aneurysms; computational fluid dynamics; wall shear stress; growth; rupture

1. Introduction

Cerebral aneurysms are pathological dilatations of the arterial walls frequently located near arterial bifurcations in the circle of Willis (Stehbens 1972, Weir 2002, Wiebers et al. 2004). Their most serious consequences are their rupture and intracranial hemorrhage, with an associated high mortality and morbidity rate (Kaminogo et al. 2003, Linn et al. 1996, Winn et al. 2002). Intracranial aneurysms are particularly difficult to treat and often do not produce symptoms before they rupture. Improvement of neuroradiological techniques has resulted in more frequent detection of unruptured aneurysms. Because prognosis of subarachnoid hemorrhage is still poor, preventive surgery is increasingly considered as a therapeutic option. However, every treatment carries a risk, which sometimes matches or exceeds the yearly risk of aneurysm rupture. Therefore, the best patient care would be to treat only those aneurysms that are likely to rupture (Kassell et al. 1990). Planning elective surgery requires a better understanding of the process of aneurysm formation, progression, and rupture so that one can make a sound judgment of the risks and benefits of possible therapies. Unfortunately, these processes are not well understood. Previous studies (Boecher-Schwarz et al. 2000, Buonocore 1998, Gobin et al. 1994, Groden et al. 2001, Kayembe et al. 1984, Kerber & Heilman 1983, Kerber et al. 1999, Kyriacou & Humphrey 1996, Metcalfe 2003, Ortega 1998, Stehbens 1972) have identified the major factors involved in these processes: (a) hemodynamics, (b) wall biomechanics, (c) mechanobiology, and (d) the intracranial environment. In the following sections, we review these factors and, in particular, concentrate on the role of hemodynamics.

2. Mechanisms of Aneurysm Growth and Rupture

Central to any hypothesis of the pathogenesis of aneurysm growth and rupture is the interaction between the hemodynamic forces and the vessel wall biology and the resulting impact on the wall's mechanics. Ultimately, any rupture is the consequence of the inability of the wall to contain the force of the flowing blood. Yet hemodynamic studies have not found evidence of excessive elevations of peak pressure within cerebral aneurysms to explain the wall failure on a purely mechanical basis. Consequently, there must be an alteration of the aneurysmal wall that results in its mechanical weakening over time.

2.1. Histological Observations

Histological studies have found a decreased number (or the degeneration of) endothelial cells, the degeneration of the internal elastic lamina, and thinning of the medial layer (Stehbens 1963, Stehbens 1989). Because the internal elastic lamina and vascular extracellular matrix are considered the main contributors to the structural integrity of the vessel, investigators have examined a variety of enzymes related to their remodeling and potential degeneration. Circulating levels of serum gelatinase or elastase are increased in patients with cerebral aneurysms (Chyatte & Lewis 1997). Increased matrix metalloproteinase has been found in aneurysm walls (Bruno et al. 1998). These enzymes are largely responsible for intracellular matrix degradation as part of the process of wall remodeling; therefore, increased activity could cause weakening of the wall. Thinning of the medial layer in the aneurysm wall seen histologically has been largely explained by a decreased number of smooth muscle cells (Kondo et al. 1998; Stehbens 1963, 1989). Both experimental and clinical studies have attributed the decrease of smooth muscle cells to their apoptosis (Hara et al. 1998, Kondo et al. 1998). Consequently, it is widely believed that smooth muscle–cell apoptosis and elastin/collagen fiber–reconstitution mechanisms are central to the process of wall weakening.

2.2. Genetic Factors

The interplay of genetics and biomechanical stimuli generated by blood flow seems to be a critical element in the pathogenesis of cerebral aneurysms. Animal studies have pointed to endothelial degeneration and cell loss as the initiating event of aneurysm wall remodeling (Kojima et al. 1986). Furthermore, a study on Japanese patients found a genetic locus for cerebral aneurysms localized within or close to the elastin gene locus on chromosome 7 (Onda et al. 2001). Endothelial gene expression is related to wall shear stress (WSS). Prolonged laminar WSS regulates expression to only a small percentage (1%–5%) of endothelial genes, and this transcriptional profile produces an endothelial phenotype that is quiescent, protected from apoptosis, inflammation, and oxidative stress (Wasserman 2004). Therefore, triggering for genetic traits, potentially affecting arterial wall mechanical-load tolerance, may be attributed to a hemodynamic condition.

2.3. Hemodynamic Factors

The capacity of the endothelial cell to sense WSS is an important determinant of lumen diameter and overall vessel structural remodeling (Drexler & Hornig 1999, Luscher & Tanner 1993). This morphological variation of the vascular endothelium layer results in different production levels of vasoactive substances such as nitric oxide (NO) (Guzman et al. 1997, Kamiya et al. 1988, Luscher & Tanner 1993). Studies indicate that low wall stress and high oscillatory patterns of WSS cause intimal wall thickening (Dardik et al. 2005, Friedman et al. 1981, Ku et al. 1985). A uniform shear stress field tends to stretch and align the endothelial cells in the direction of the flow, whereas low–shear stress levels in an oscillatory hemodynamic environment cause irregular shape and the loss of a particular orientation. Furthermore, low WSS was found to switch the endothelial cell phenotype from atheroprotective to atherogenic

with a high endothelial cell turnover rate (Ford et al. 2005a). This could be protective for aneurysms because the wall tends to thicken.

In summary, the caliber and also the histological structure of arterial walls are regulated by blood flow, particularly by WSS. In the presence of endothelial cells and smooth muscle cells, a chronic increase of WSS due to increased arterial blood flow elicits an adaptive response of the arterial wall histology, leading to vessel enlargement and a reduction in WSS to physiological baseline values. However, if WSS is increased focally, it can potentially cause a focal enlargement of and damage to the arterial wall, termed destructive remodeling, which is induced by the excessive production of molecules such as NO.

2.4. Aneurysm Initiation

The formation of cerebral aneurysms is believed to be related to an interaction between high-flow hemodynamic forces and the arterial wall owing to several clinical and experimental observations. Cerebral aneurysms are commonly associated with anatomic variations and pathological conditions (such as hypoplasia or occlusion of a segment of the circle of Willis) (Kayembe et al. 1984; Matsuda et al. 1983; Salar & Mingrino 1977, 1981; Yasargil 1984), or high-flow arteriovenous malformations that cause locally increased flow in the cerebral circulation (Peerless & Drake 1982), and, at points of flow bifurcation, a site of flow separation and elevated WSS. Observations from animal models have shown that elevations of WSS to levels found in these conditions can cause fragmentation of the internal elastic lamina of blood vessels (Steiger 1990), as well as alterations in endothelial phenotype or endothelial damage (Stehbens 1989). Additionally, increased flow and systemic hypertension are required to create experimental cerebral aneurysms in rats and primates (Hashimoto et al. 1980, Kim et al. 1989, Kondo 1997, Nagata et al. 1980).

2.5. Aneurysm Progression

Despite the agreement on the mechanism of aneurysm initiation, there is significant controversy regarding the mechanisms responsible for the growth and ultimate rupture of a cerebral aneurysm, with two main schools of thought: high-flow effects and low-flow effects. In each theory, the hemodynamic environment within the aneurysm interacts with the cellular elements of the aneurysmal wall to cause a weakening of the wall. From histological observations, investigators concluded that the mechanical properties of the aneurysmal wall are mainly related to collagen. Measurements of the strength of the aneurysm walls from cadaveric and surgical specimens demonstrated that the yield stress of tissue in the fundi of aneurysms was mildly in excess of the calculated systolic stresses in contrast to the normal arterial wall, which were higher by a factor of 10 to 20 (Steiger et al. 1989). Furthermore, this analysis showed that the stress tolerated by aneurysm walls for a prolonged period was in the range of the stress imposed in vivo by the mean blood pressure. Therefore, aneurysm growth could be understood as a passive yield to blood pressure and reactive healing and thickening of the wall with increasing aneurysm diameter. The distinguishing feature between the two schools of thought is in the mechanisms responsible for wall weakening.

The high-flow theory focuses on the effects of WSS elevation. Elevation of maximal WSS can cause endothelial injury and thus initiates wall remodeling and potential degeneration (Nakatani et al. 1991). A vascular endothelium malfunction and/or an abnormal shear stress field can cause an overexpression of endothelium-dependent NO production, which leads to a lower, nonphysiological local arterial tone via processes connected to the scarcity and apoptosis of wall-embedded smooth muscle cells and wall remodeling (Fukuda et al. 2000, Guzman et al. 1997, Hara et al. 1998, Sho et al. 2001). This results in a disturbance of the equilibrium between the blood-pressure forces and the internal wall stress forces, in favor of the former, and subsequently dilates the arterial wall locally. The resulting abnormal blood shear stress

field is the driving factor for further growth of the aneurysmal geometry. This geometrical growth stretches the collagen and elastin fibers of the medial and adventitial layers and gives rise to internal stresses that contribute to the arterial stiffness. Eventually, the biomechanical system equilibrates at a state at which the internal wall stresses and the transmural pressure are equal while the local hemodynamics cannot alter the arterial properties any more. At this point, the elastin and the collagen fibers are constantly under a nonphysiologically large mechanical load and eventually undergo remodeling.

The low-flow theory points to low flows within aneurysms as the cause of localized blood-flow stagnation against the wall in the dome. Blood stagnation causes a dysfunction of flow-induced NO, which is usually released by mechanical stimulation from increased shear stress. This dysfunction results in the aggregation of red blood cells, as well as the accumulation and adhesion of both platelets and leukocytes along the intimal surface (Griffith 1994, Liepsch 1986, Moncada et al. 1991, Moritake et al. 1973). This process may cause intimal damage, leading to the infiltration of white blood cells and fibrin inside the aneurysm wall, all of which have been seen in pathological examinations of aneurysm walls (Crawford 1959, Crompton 1966). The inflammation leads to the localized degeneration of the aneurysm wall, resulting in a lower pressure threshold at which physiological tensile forces could be supported. The aneurysm wall progressively thins and finally may cause the tissue to tear.

2.6. Peri-Aneurysmal Environment Factors

The evolution of an aneurysm (its final shape or rupture) results from the interplay among the intravascular forces, the mechanical properties of the aneurysm wall, and their interaction with the structures around the aneurysm, which is known as the peri-aneurysmal environment (PAE). As an aneurysm grows, it comes in contact with structures in the peri-aneurysmal space such as bone, brain tissue, nerves, and dura. Symptoms related to this interaction are well known clinically, manifesting as bone erosion, obstructive hydrocephalus, and cranial nerve palsy (Hongo et al. 2001, Platania et al. 2002), and indicate the pressure exerted by the aneurysm in contact with the surrounding structures. However, the PAE's effect on aneurysm evolution is poorly understood. Using finite-element analyses of stress fields in a mathematical model, Seshaiyer & Humphrey (2001) have shown that certain distributions of contact constraints in some aneurysm geometries may decrease stresses and provide a protective effect. Using high-resolution computed-tomography imaging, Ruiz et al. (2006) showed that contact constraints from the PAE influence both aneurysm shape and the risk of rupture. They associated balanced contact with unruptured aneurysms and unbalanced or absent contact with ruptured aneurysms. Logically, the expansion of the aneurysm should eventually lead to contact with surrounding structures that locally reinforce the wall and resist further expansion. However, as with hemodynamic factors such as WSS, contact is not uniformly distributed around the aneurysm wall, leading to a potentially complex interaction between wall-damaging mechanisms and peri-aneurysmal support. The result of this could be either protective or detrimental for the evolution of the aneurysm.

3. Cerebral Hemodynamics

3.1. Modeling Hemodynamics

The blood-flow dynamics of cerebral aneurysms have been studied in numerous experimental models and clinical studies to investigate the role of hemodynamics in the initiation, growth, and rupture of aneurysms (Burlison et al. 1995, Gobin et al. 1994, Gonzalez et al. 1992, Liou & Liou 1999, Nakatani et al. 1991, Satoh et al. 2003, Tateshima et al. 2001, Tenjin et al. 1998, Ujiie et al. 1999). Although this work has characterized the complexity of intra-aneurysmal hemodynamics, the studies have largely focused on idealized aneurysm geometries or surgically created aneurysms in animals. Each of these previous approaches has had

significant limitations in connecting the hemodynamic factors studied to clinical events. In vitro studies using idealized geometries have allowed detailed measurement of hemodynamic variables (Liou & Liou 1999) but cannot be used directly to understand the hemodynamic forces in an individual clinical case.

Computationally based models circumvent this problem owing to their ability to study all possible geometries (Cebal et al. 2004, Hassan et al. 2004, Jou et al. 2003, Steinman et al. 2003). Although current imaging modalities are limited for the in vivo quantification of blood-flow patterns, the geometrical shape of aneurysms can be accurately reconstructed from anatomical images. This has allowed the application of computational fluid dynamics (CFD) techniques in subject-specific geometries extracted from medical images (Butty et al. 2002, Cebal et al. 2004, Hassan et al. 2004, Jou et al. 2003, Steinman et al. 2003). A number of experimental studies have also been carried out with realistic anatomical models constructed from images using rapid prototyping techniques (Tateshima et al. 2001, 2003a,b). Using simulated or virtual angiograms, researchers recently showed that image-based patient-specific computational models are capable of reproducing the flow structures in cerebral aneurysms observed in vivo during angiographic examinations (Cebal et al. 2007, Ford et al. 2005b).

Most CFD modeling approaches approximate blood flow as a continuous incompressible fluid. The corresponding mathematical model is described by the three-dimensional unsteady incompressible Navier-Stokes equations (Mazumdar 1992) (see Figure 1). Newtonian models may provide a reasonable approximation for blood flow in large arteries (Perktold et al. 1991, Perktold & Rappitsch 1995, Steinman 2004, Stuhne & Steinman 2004, Taylor & Draney 2004, Zhao et al. 2000). However, for aneurysmal flows, this approximation may be not entirely justified because of the presence of slow-flow regions in which non-Newtonian properties become important (Basombrio et al. 2000). A number of non-Newtonian models have been developed to approximate the observed rheological behavior of blood (Mazumdar 1992) and have been incorporated into patient-based models (Cebal et al. 2005a). Although many hemodynamic studies consider vessel compliance to be a second-order effect and neglect it (Perktold & Rappitsch 1994, 1995; Steinman 2004; Taylor & Draney 2004), its influence on in vivo intra-aneurysmal flow patterns has not been characterized (Shojima et al. 2004). Fluid-structure interaction algorithms have been developed to incorporate wall compliance into the vascular CFD models (Cebal et al. 2002, Taylor & Draney 2004, Zeng & Ethier 2003, Zeng et al. 2003, Zhao et al. 2000). However, this is a challenging problem because it requires knowledge about the distribution of wall thickness, wall elasticity, and intra-arterial pressure waveform (Cebal 2002, Cebal et al. 2002). In a recent study, the pulsation of the wall was measured using dynamic angiography images and nonrigid registration algorithms and was imposed as a boundary condition in CFD models (Dempere-Marco et al. 2006, Oubel et al. 2007). Although the WSS and velocity magnitudes were affected by the wall motion, the main characteristics of the flow patterns (such as location and size of the inflow jet and the complexity and stability of the intra-aneurysmal flow pattern) were not significantly altered.

3.2. Hemodynamics in the Circle of Willis

The study of blood flows in normal cerebral arteries and the circle of Willis is essential for a better understanding of the local hemodynamics environment in which aneurysms form and develop. Several studies of the hemodynamics in the circle of Willis have been carried out using computational models (Alastruey et al. 2007, Alnaes et al. 2007, Cassot et al. 2000, Cebal et al. 2003, Ferrandez et al. 2000). A recent study used CFD to investigate the impact of variations in vessel radii and bifurcation angles on pressure and WSS in the complete circle of Willis (Alnaes et al. 2007). The authors found that deviations from normal anatomy result in a redistribution of wall pressures and increased WSS at branch points. One weakness in this interesting study is the use of idealized geometries, which could be overcome by using patient-

based models of the complete circle of Willis (Cebal et al. 2003). Recently, four-dimensional phase-contrast magnetic resonance techniques have been used to image in vivo blood-flow patterns in cerebral arteries of normal subjects (Bammer et al. 2007, Wetzel et al. 2007). Both the in vivo imaging and computational modeling studies have characterized the complexities of the blood-flow patterns and WSS distributions in the major cerebral arteries. In particular, they have demonstrated the nonuniform distribution of WSS along the vessels, with increased and decreased zones at arterial bifurcations and regions of high vessel curvature, which coincide with the most common locations for aneurysm development (Brisman et al. 2006). Helical or swirling flows (also called secondary flows) induced by the curving geometry of the cerebral arteries are fundamentally important because they govern the local distribution of WSS forces acting on the vessel walls. Figure 2 illustrates the hemodynamic characteristics of the major cerebral vessels, showing CFD models constructed from phase-contrast magnetic resonance images of a normal subject and the corresponding blood-flow pattern and WSS distribution at peak systole.

3.3. Hemodynamics in Cerebral Aneurysms

Numerous computational and experimental studies of cerebral aneurysms have been carried out using realistic geometries obtained from medical images (Cebal et al. 2005b, Hassan et al. 2004, Jou et al. 2003, Kerber et al. 1999, Shojima et al. 2004, Steinman et al. 2003, Tateshima et al. 2003a, Valencia & Solis 2006). These investigations reveal a wide variety of complex intra-aneurysmal flow patterns that are strongly dependent on the patient-specific vascular geometry and thus are not easily predictable by a simple inspection or by extrapolation from idealized models.

The intra-aneurysmal flow patterns range from those that are simple and stable to those that are complex and unstable (or turbulent). Simple flow patterns consist of a single recirculation region or a vortical structure within the aneurysm. This main vortex can remain stable or move during the cardiac cycle. More complex flow patterns contain more than one recirculation region that can remain stable, move, or become intermittent during the cardiac cycle. Figure 3 presents examples of intra-aneurysmal flow patterns with different degrees of complexity.

The intra-aneurysmal flow structures depend not only on the size and shape of the aneurysm but also on the way the blood flows from the parent vessel into the aneurysm, which in turn is influenced by the geometry of the parent artery. In some aneurysms, the blood flows from the parent vessel directly into the aneurysm, resulting in a concentrated inflow jet that impacts the aneurysm wall, producing a region of locally elevated WSS. Other aneurysms have a more diffuse inflow jet that produces a slower intra-aneurysmal flow pattern and a more uniform WSS distribution, with magnitudes typically lower than those of the parent vessels. Examples of aneurysms with concentrated and diffuse inflow jets and the corresponding WSS distributions are shown in Figure 4. The regions of elevated WSS can be small or large relative to the aneurysm size, depending on whether the inflow jet is concentrated or diffuse.

The blood flow in the curved arteries of the brain is characterized by strong secondary flows that create swirling helical patterns. These patterns determine the location of the inflow portion of the aneurysm neck, as well as the location and size of the impact zone on the aneurysm wall. In contrast with idealized models that place the inflow at the distal part of the aneurysm neck, patient-specific models show that the inflow can also be located on the sides or at the proximal part of the neck. Examples of aneurysms with different inflow locations are shown in Figure 5.

The impingement of the inflow jet against the aneurysm wall produces a local elevation of the WSS. Depending on the geometric configuration of the aneurysm with respect to the parent

artery, the zone of flow impingement can be located at the neck, the body, or the dome of the aneurysm (Figure 6).

3.4. Hemodynamics and Cerebral Aneurysm Evolution

Computational models have provided some insight into mechanisms for aneurysm rupture, although explanations for these mechanisms differ. Proponents of the low-shear stress theories rely on several clinical observations and CFD data they consider to be incompatible with the high-shear stress mechanisms. First, prior CFD modeling has shown that focal elevations in WSS are largely confined to the downstream lip of an aneurysm, yet the dome is clinically the most common site of rupture (Suzuki & Ohara 1978), and WSS in the dome is low. Thus, they reason, shear stress can be related to aneurysm growth only if one assumes that the active matrix of aneurysm growth is located at the orifice. However, angiographically documented cases of aneurysm growth generally show progression of the dome but only rarely changes in the neck region (Ono et al. 1985). Second, the strongest known predictor of an aneurysm's rate of rupture is size, with larger sizes corresponding to elevated rates of rupture. Flow velocities in aneurysms depend on the volume, with velocity being inversely proportional to the square of the maximum diameter of the fundus (Liepsch et al. 1987; Perktold et al. 1989; Steiger & Reulen 1986; Steiger et al. 1987, 1988). Moreover, a direct relationship exists between the area of the orifice and the intra-aneurysmal flow velocities (Black & German 1960). These observations have led to a clinical measure called the aspect ratio (which is the depth of aneurysm divided by the neck width). Some studies have found an aspect ratio greater than 1.6 to be correlated with a risk of rupture (Ujiie et al. 2001). Finally, CFD analysis and experimental in vitro measurements of WSS have shown that the WSS magnitude of the aneurysm region is significantly lower than that of the vessel region, and WSS inversely correlates with the aspect ratio (Shojima et al. 2004). Naturally, these authors' conclusion is that high shear stress cannot be the cause of aneurysm rupture.

Despite these admittedly compelling arguments, the low-shear stress theory may not be the best explanation for aneurysm rupture. First, low WSS at the bifurcations of carotid arteries is causally connected with proliferative degenerative alterations (i.e., atheromas). Although atheromas are found in a minority of cerebral aneurysms, their presence is not a common finding in histological examinations of ruptured aneurysms. Why would we anticipate the biological response to be different intra-aneurysmally? Second, much of the previous CFD work was performed using idealized lateral wall aneurysm models that are not representative of the wide range of geometries found in patients. More recent patient-specific CFD modeling (Cebal et al. 2005b,c; Shojima et al. 2004) has shown that the point of flow impingement by the inflow jet is located in the neck region in only a minority of cases. Areas of elevated shear stress are commonly found in the body or dome of an aneurysm (Tateshima et al. 2003a), although the spatial average WSS is lower than the parent artery for most aneurysms. Finally, the size of the wall impingement zone is statistically associated with a prior clinical event of rupture (Cebal et al. 2005b,c). This may imply that the aspect ratio may predict aneurysmal rupture, not as a predictor of low-flow recirculation (i.e., low WSS) but because narrow necks in large aneurysms geometrically induce concentrated inflow jets and small concentrated impaction zones.

4. Concluding Remarks

The role of blood-flow physiological parameters regulating aneurysm morphology and natural history is poorly understood. It is necessary to model intra-aneurysmal hemodynamics using realistic aneurysm geometries because aneurysm geometry is one of the most important factors determining aneurysm flow patterns and WSS distributions that influence aneurysm progression. Most models tend to oversimplify the complex flow patterns observed in aneurysms in vivo. The difficulty of developing reliable in vitro and animal models has

hampered an accurate evaluation of those physiologic parameters. Furthermore, better understanding of the mechanisms of aneurysmal growth requires the study of the interaction among hemodynamics, wall mechanobiology, wall biomechanics, and contacts with the PAE structures. This will help improve patient evaluation and treatment.

Summary Points

1. The rupture of intracranial aneurysms cannot be explained on a purely mechanical basis.
2. The weakening of aneurysmal walls has been demonstrated in histological studies that found degeneration of endothelial cells, degeneration of the internal elastic lamina, and thinning of the medial layer.
3. Aneurysm formation is believed to be caused by the interaction of abnormally high-flow hemodynamic forces (caused by anatomical variations and pathological conditions) and the arterial wall mechanobiology.
4. High-flow theories claim that abnormally high WSS causes an excessive production of NO, which results in lower local arterial tone owing to the scarcity and apoptosis of smooth muscle cells and wall remodeling.
5. Low-flow theories claim that low WSS causes a dysfunction of flow-induced NO, which results in the aggregation of red blood cells and the accumulation and adhesion of platelets and leukocytes, which in turn cause intimal damage and inflammation, leading to localized degeneration of the aneurysm wall.
6. Contacts with extravascular structures play an important role in the evolution of aneurysms and can have a protective or damaging effect on the aneurysm wall.
7. Investigators can make patient-specific image-based hemodynamics models to accurately represent in vivo conditions. These models reveal a wide variety of complex intra-aneurysmal flow patterns that are strongly dependent on the patient-specific vascular geometry and thus are not easily predictable by simple inspection or by extrapolation from idealized models.

Future Directions

1. Researchers need to develop realistic models of aneurysm growth that combine hemodynamics, biomechanics, mechanobiology, and the PAE.
2. Researchers also need to correlate model-predicted variables with clinical observations to further understand the mechanisms responsible for aneurysm evolution and rupture.

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Glossary

WSS	wall shear stress
NO	nitric oxide
PAE	peri-aneurysmal environment
CFD	computational fluid dynamics

Continuity equation:	$\nabla \cdot \mathbf{v} = 0$	ρ : density
Momentum equation:	$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = -\nabla p + \nabla \cdot \boldsymbol{\tau}$	p : pressure
Stress tensor:	$\tau_{ij} = \mu \varepsilon_{ij}$	\mathbf{v} : velocity
Strain-rate tensor:	$\varepsilon_{ij} = \frac{1}{2} \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)$	μ : viscosity
Strain rate:	$\dot{\gamma} = 2\sqrt{\varepsilon_{ij}\varepsilon_{ij}}$	
Yield stress:	τ_0	
Newtonian fluid:	$\boldsymbol{\tau} = \mu_0 \dot{\gamma} \quad \rightarrow \mu = \mu_0$	
Casson fluid:	$\sqrt{\tau} = \sqrt{\mu_0 \dot{\gamma}} + \sqrt{\tau_0} \quad \rightarrow \mu = (\sqrt{\mu_0} + \sqrt{\tau_0/\dot{\gamma}})^2$	

Figure 1.
Mathematical model of blood flows.

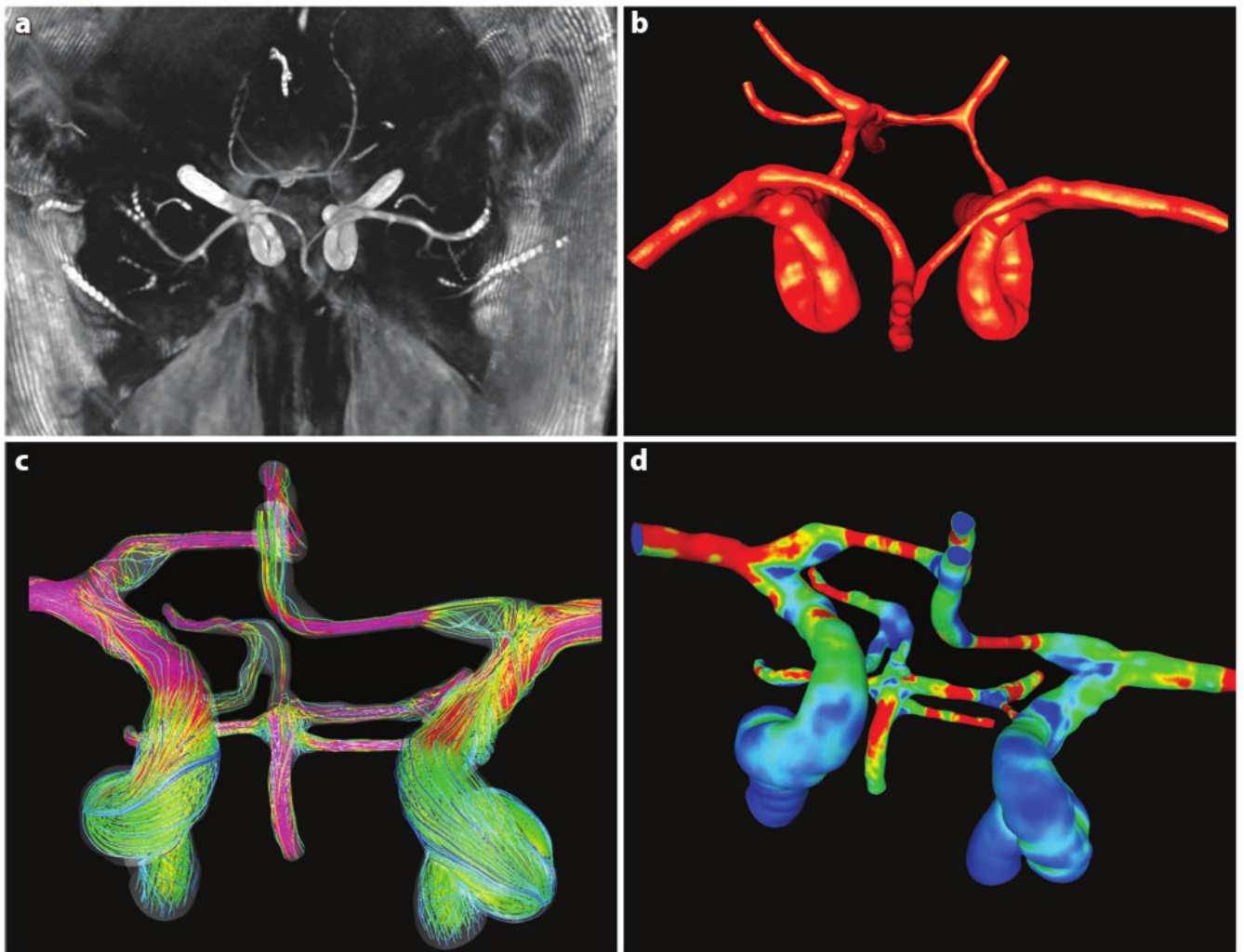


Figure 2. Computational model of the hemodynamics in the circle of Willis of a normal subject. (a) Original medical image and (b) corresponding vascular model. (c) The complex swirling flows and (d) nonuniform wall shear stress (WSS) distribution (with *red* representing the highest WSS) along the major cerebral vessels.

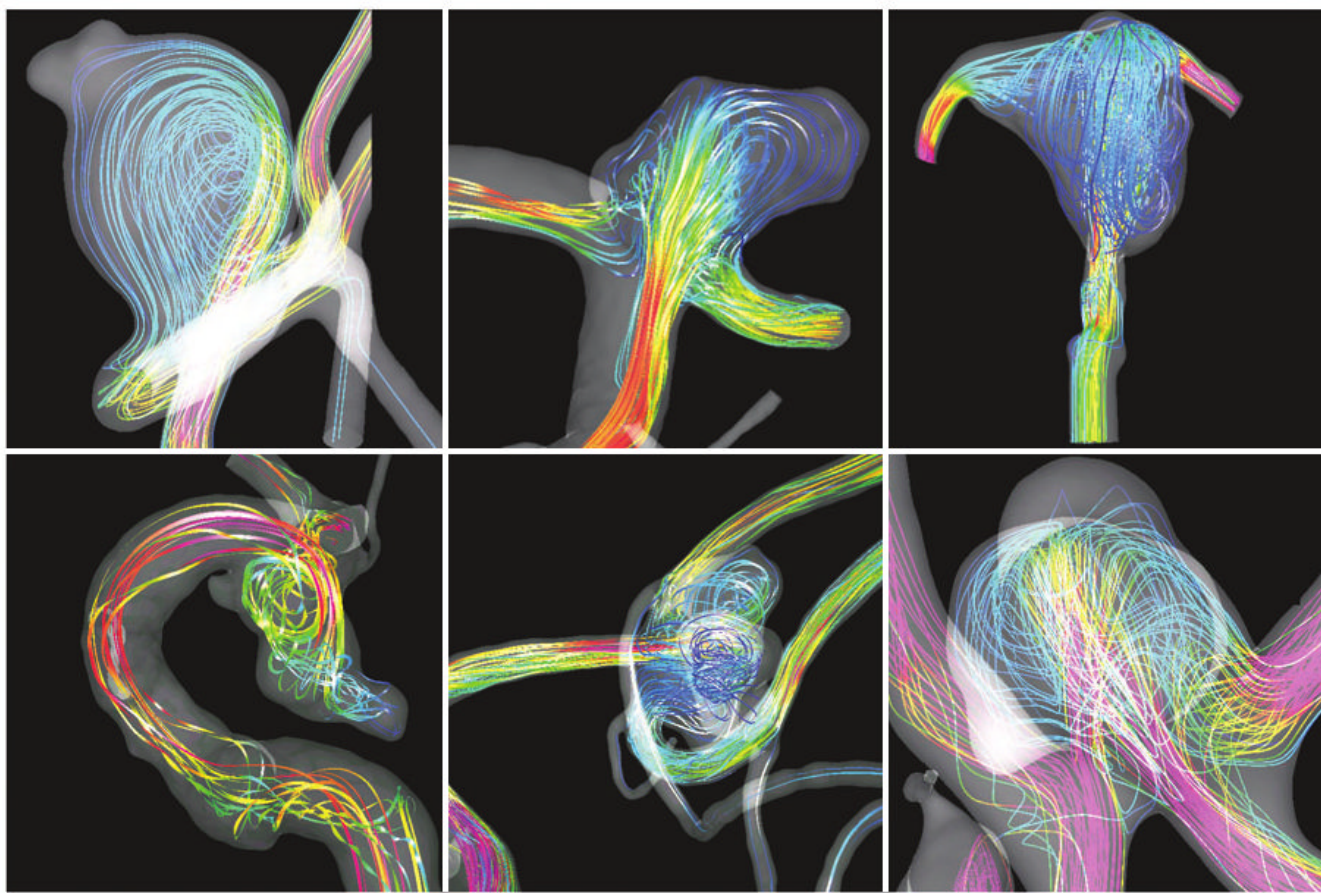


Figure 3. Intra-aneurysmal flow patterns, ranging from simple patterns with a single recirculation region (*top left*) to complex patterns with several vortical structures that can be stable, moving, or intermittent during the cardiac cycle.

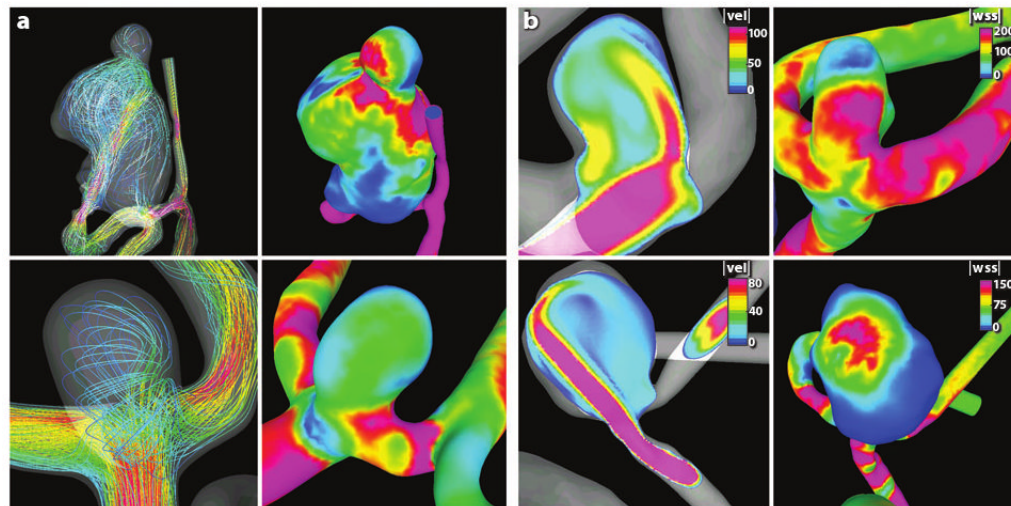


Figure 4.

(a) Aneurysms with concentrated inflow jet and regions of locally elevated wall shear stress (WSS) (*top panels*) and with diffuse inflow jet and WSS uniformly lower than the parent artery (*bottom panels*). (b) Aneurysms with large (*top panels*) and small (*bottom panels*) impingement regions compared to the aneurysm size.

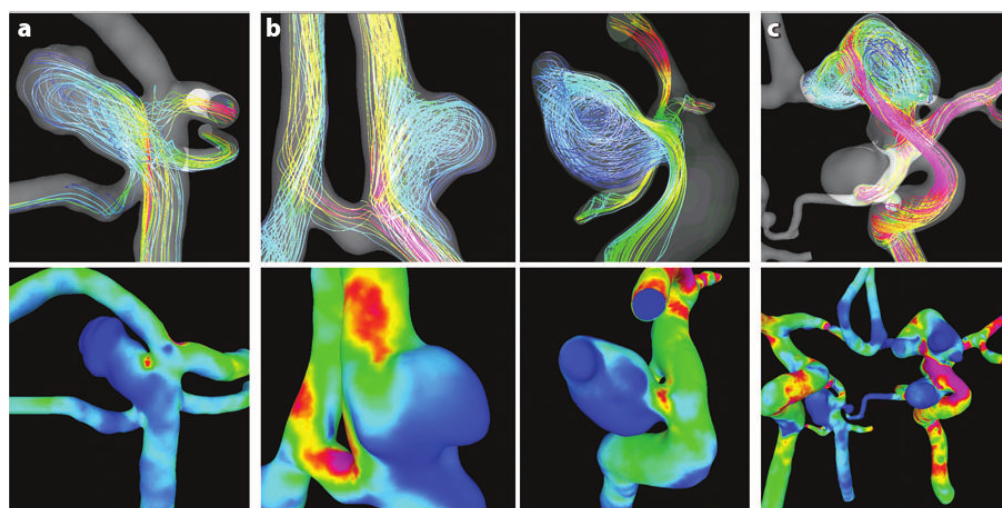


Figure 5. Flow patterns (*top panels*) and wall shear stress distribution (*bottom panels*) of aneurysms with inflow regions located at the distal (*a*), side (*b*), and proximal (*c*) portions of the neck.

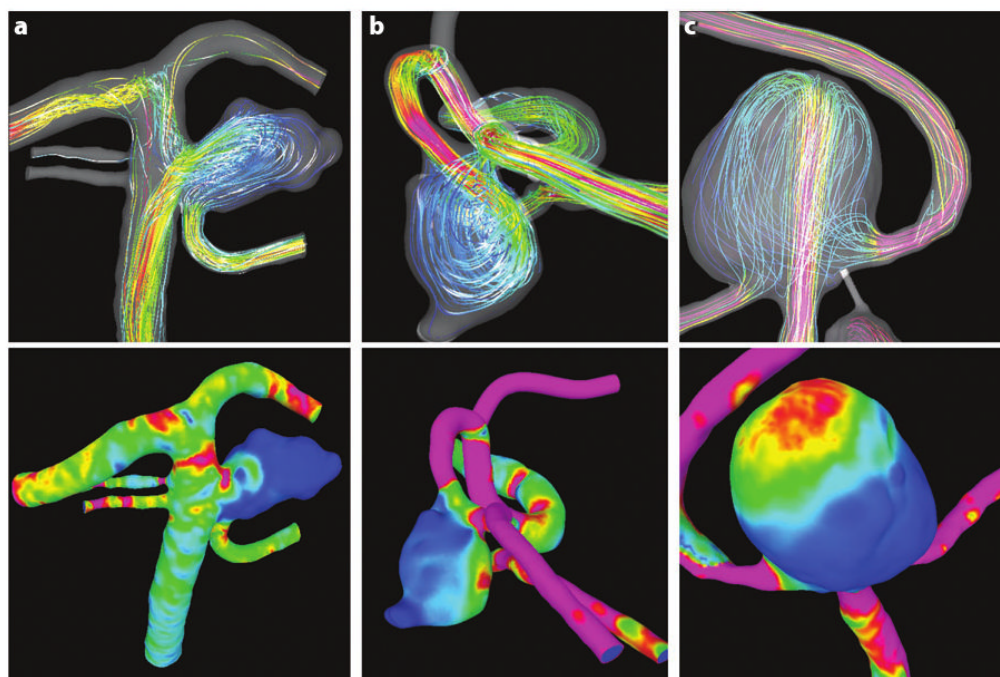


Figure 6. Aneurysms with flow-impingement regions located at the neck (*a*), body (*b*) and dome (*c*) of the aneurysm. Flow patterns are shown in the top panels, and wall shear stress distribution is shown in the bottom panels.