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### Hexagonal LuMnO3 revisited

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Acta Crystallographica Section E Structure Reports Online

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#### **Key indicators**

Single-crystal X-ray study T = 293 KMean  $\sigma(\text{Mn-O}) = 0.007 \text{ Å}$  R factor = 0.027 wR factor = 0.065 Data-to-parameter ratio = 26.0

For details of how these key indicators were automatically derived from the article, see http://journals.iucr.org/e. The crystal structure of hexagonal LuMnO<sub>3</sub> at room temperature is isomorphous with YMnO<sub>3</sub> and deviates in important details from the early work of Yakel *et al.* [Acta Cryst. (1963), **16**, 957–962]. Mn is near the centre of its oxygen coordination environment. On the threefold axes, the apical O–Lu bonds have alternating long and short bond lengths, leading to ferroelectric behaviour. The sample studied was composed of almost equal volumes of inversion twins.

Hexagonal LuMnO<sub>3</sub> revisited

### Comment

As part of a programme to investigate the origin of the ferroelectric behaviour in the hexagonal  $LnMnO_3$  family, we have determined accurate structural parameters for single crystals of this series (Van Aken *et al.*, 2001*a,b,c*). Here we report the structure of LuMnO<sub>3</sub>. Single-crystal growth of LuMnO<sub>3</sub> has frequently been reported (Yakel *et al.*, 1963; Bertaut *et al.*, 1963) and the structure was reported by Yakel *et al.* Our refinement shows small but significant differences from the work of Yakel *et al.* (1963), as discussed below. The hexagonal LnMnO<sub>3</sub> family has been described in great detail previously (Van Aken *et al.*, 2001*d*).

The M-O bond lengths are given in Table 1. The nonequivalent Mn-O atomic distances, both within the basal plane and to the apices, have smaller differences than in previous reports on LuMnO<sub>3</sub> (Yakel *et al.*, 1963). In-plane differences are 0.023 (7) Å (this work) and 0.09 Å (Yakel *et al.*, 1963), apical 0.031 (7) Å (this work) and 0.08 Å (Yakel *et al.*, 1963). As a result Mn is approximately in the centre of its oxygen environment. Likewise, the equatorial Lu-O1 and Lu-O2 bond lengths show less variation than the result of Yakel *et al.* (1963). Our data yield equatorial bond lengths of 2.227-2.294 Å, whereas Yakel *et al.* report 2.18-2.35 Å. The differences in apical bond distances of Lu1 and Lu2 are larger [1.192 (14) and 0.879 (10) Å] respectively, than those reported by Yakel *et al.* (0.84 and 0.96 Å).

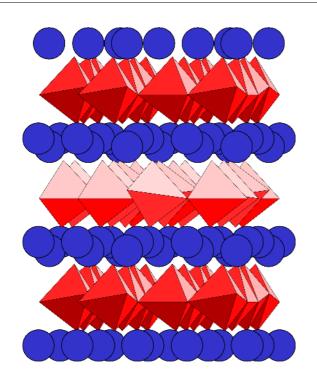
Yakel *et al.* (1963) only measured reflections of one asymmetric *hkl* set, *i.e.* no Bijvoet pairs. Based on the observation of ferroelectricity (Bertaut *et al.*, 1963) and systematic absences, the non-centrosymmetric space group  $P6_3cm$  was chosen. Our experiment included over 90% of the Friedel pairs and subsequent analysis confirmed this space group. Yakel *et al.* also discuss the possibility of the existence of domains with reversed polar direction. Our refinement indicated that our sample contained roughly equal volumes of twin domains.

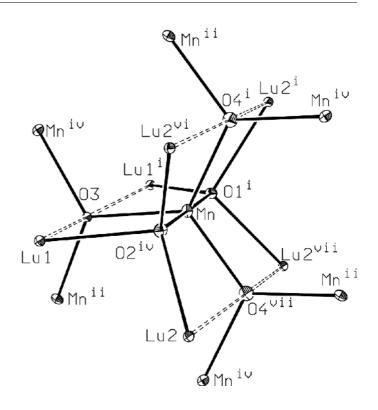
### **Experimental**

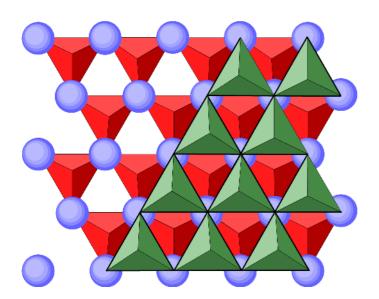
 $\bigcirc$  2001 International Union of Crystallography Printed in Great Britain – all rights reserved Single crystals of LuMnO<sub>3</sub> were obtained using a flux method by weighing appropriate amounts of  $Lu_2O_3$  and  $MnO_2$  with  $Bi_2O_3$  in a

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## inorganic papers







### Figure 1

Schematic view of the crystallographic structure of LuMnO<sub>3</sub>. The top panel shows a view along the basal plane. Lu is represented by shaded spheres, and the  $MnO_5$  clusters are represented by trigonal bipyramids. This panel highlights the two-dimensional nature of the structure. The lower panel depicts a view along the *c*-axis of two layers to show the stacking of the bipyramids.

1:12 ratio (Yakel *et al.*, 1963). The powders were thoroughly mixed and heated for 48 h at 1523 K in a Pt crucible. The crystals were separated from the flux by increasing the temperature to 1723 K and evaporating the  $Bi_2O_3$  flux (Bertaut *et al.*, 1963).

### Figure 2

Perspective *ORTEPII* (Johnson, 1976) drawing of all inequivalent atoms. All atoms are represented by atomic displacement ellipsoids drawn to encompass 50% of the electron density.

### Crystal data

LuMnO<sub>3</sub>  $M_r = 277.90$ Hexagonal,  $P6_3cm$  a = 6.038 (1) Å c = 11.361 (1) Å V = 358.70 (9) Å<sup>3</sup> Z = 6 $D_x = 7.719$  Mg m<sup>-3</sup>

### Data collection

Enraf–Nonius CAD-4F diffractometer  $\omega/2\theta$  scans Absorption correction: analytical (de Meulenaer & Tompa, 1965)  $T_{min} = 0.084, T_{max} = 0.759$ 4711 measured reflections 833 independent reflections 610 reflections with  $F > 4\sigma(F)$ 

### Refinement

Refinement on  $F^2$  R(F) = 0.027  $wR(F^2) = 0.065$  S = 1.05833 reflections 32 parameters  $w = 1/[\sigma^2(F_o^2) + (0.0293P)^2]$ where  $P = (F_o^2 + 2F_c^2)/3$  Mo  $K\alpha$  radiation Cell parameters from 22 reflections  $\theta = 28.0-28.8^{\circ}$  $\mu = 46.03 \text{ mm}^{-1}$ T = 293 KPlatelet, black  $0.120 \times 0.100 \times 0.004 \text{ mm}$ 

 $\begin{aligned} R_{\rm int} &= 0.094 \\ \theta_{\rm max} &= 40.0^{\circ} \\ h &= -10 \rightarrow 9 \\ k &= 0 \rightarrow 10 \\ l &= -20 \rightarrow 20 \\ 3 \text{ standard reflections} \\ \text{frequency: 180 min} \\ \text{intensity decay: none} \end{aligned}$ 

 $\begin{array}{l} (\Delta/\sigma)_{\rm max} < 0.001 \\ \Delta\rho_{\rm max} = 2.0 \ (4) \ {\rm e} \ {\rm \AA}^{-3} \\ \Delta\rho_{\rm min} = -5.6 \ (4) \ {\rm e} \ {\rm \AA}^{-3} \\ {\rm Extinction \ correction: \ SHELXL97} \\ ({\rm Sheldrick, \ 1997}) \\ {\rm Extinction \ coefficient: \ 0.0024 \ (2)} \end{array}$ 

 Table 1

 Selected geometric parameters (Å,  $^{\circ}$ ).

Lu1-O1	2.234 (9)	Lu2-O4 <sup>ii</sup>	3.279 (10)
$Lu1 - O1^{i}$	2.294 (10)	$Lu2 - O2^{iii}$	2.277 (12)
Lu1-O3 <sup>i</sup>	2.244 (14)	Mn-O1	1.882 (7)
Lu1-O3	3.436 (14)	Mn-O2	1.859 (7)
Lu2-O1	2.227 (12)	Mn-O3	2.050 (6)
Lu2-O4	2.401 (10)	Mn-O4	2.019 (7)
O1-Mn-O2	179.6 (6)	O4-Mn-O4 <sup>iv</sup>	119.4 (3)
O1-Mn-O3	93.6 (5)	Mn-O3-Mn <sup>v</sup>	117.7 (3)
O1-Mn-O4	86.2 (5)	Mn-O4-Mn <sup>vi</sup>	118.8 (3)
O3-Mn-O4	120.2 (3)		
	1 . (**) 1	. 1. (***)	1 1 (1)

Symmetry codes: (i)  $x - y, x, \frac{1}{2} + z$ ; (ii)  $-1 - x + y, y, \frac{1}{2} + z$ ; (iii)  $x - y - 1, x, \frac{1}{2} + z$ ; (iv) y, x, z; (v) -y, x - y, z; (vi) -1 - y, x - y, z.

The space group is determined to be  $P6_3cm$ , taking into consideration the unit cell parameters, statistical analyses of intensity distributions and systematic extinctions  $(h-hl: l \neq 2n; 00l: 1 \neq 2n)$ . Attempts to fit the intensities with a crystal structure in space group  $P6_3/mcm$  were unsuccessful. Anisotropic displacement parameters and *SHELXL*97 indicated that the Lu ions should be shifted away from the mirror plane perpendicular to the *c* axis.

The integrated intensities were measured in 'flat mode' as the absorption is very large. In 'flat mode' every reflection is measured in the orientation that minimizes the path length through the crystal and thus the absorption. The minimum transmission factor is therefore larger than expected from the crystal size.

The structure was solved by using initial co-ordinates which were taken from a previous reported hexagonal manganite,  $YMnO_3$  (Van Aken *et al.*, 2001*a*). The positional and anisotropic displacement parameters were refined.

The final difference Fourier map showed a peak of 2.0 (4) e Å<sup>-3</sup> near the Lu position and a hole of 5.7 (4) e Å<sup>-3</sup> also near the Lu position. No other significant peaks having chemical meaning above the general background (0.9 e Å<sup>-3</sup>) were observed in the final difference Fourier map.

The Flack parameter (Flack, 1983) of an initial refinement indicated that the crystal was twinned. Therefore an inversion twin was added to the structure model, similar to the one reported for YMnO<sub>3</sub> (Van Aken *et al.*, 2001*a*). An initial attempt gave a twin fraction near 50%. We expect a 50%–50% distribution because this yields no net electrical polarization. We fixed the twin fraction at 50%, which had no significant influence on any other parameter.

Data collection: *CAD*-4-*UNIX Software* (Enraf–Nonius, 1994); cell refinement: *SET*4 (de Boer & Duisenberg, 1984); data reduction: *HELENA* (Spek, 1997); program(s) used to refine structure: *SHELXL*97 (Sheldrick, 1997); molecular graphics: *ORTEP*-3 (Farrugia, 2000); software used to prepare material for publication: *PLATON* (Spek, 2001).

This work is supported by the Netherlands Foundation for the Fundamental Research on Matter (FOM).

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# supporting information

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### S1. Comment

As part of a program to investigate the origin of the ferroelectric behaviour in the hexagonal LnMnO<sub>3</sub> family, we have determined accurate structural parameters for single crystals of this series (Van Aken *et al.*, 2001*a*,b,c). Here we report the structure of LuMnO<sub>3</sub>. Single crystal growth of LuMnO<sub>3</sub> has frequently been reported (Yakel *et al.*, 1963; Bertaut *et al.*, 1963) and the structure was reported by Yakel *et al.* Our refinement shows small but significant differences from the work of Yakel *et al.* as discussed below. The hexagonal LnMnO<sub>3</sub> family has been described in great detail previously (Van Aken *et al.*, 2001 d).

The metal-oxygen bond lengths are given in Table 1. The non-equivalent Mn—O atomic distances, both within the basal plane and to the apices, have smaller differences than in previous reports on LuMnO<sub>3</sub> (Yakel *et al.*, 1963). In-plane differences are 0.023 (7) Å (this work) and 0.09 Å (Yakel *et al.*), apical 0.031 (7) Å (this work) and 0.08 Å (Yakel *et al.*). As a result the Mn is approximately in the centre of its oxygen environment. Likewise, the equatorial Lu—O1 and Lu—O2 bond lengths show less variation than Yakel *et al.*'s result. Our data yield equatorial bond lengths of 2.227–2.294 Å, whereas Yakel *et al.* report 2.18–2.35 Å. The differences in apical bond distances of Lu1 and Lu2 are larger [1.192 (14) and 0.879 (10) Å] respectively, than those reported by Yakel *et al.* (0.84 and 0.96 Å).

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### **S2. Experimental**

Single crystals LuMnO<sub>3</sub> were obtained using a flux method by weighing appropriate amounts of Lu<sub>2</sub>O<sub>3</sub> and MnO<sub>2</sub> with  $Bi_2O_3$  in a 1:12 ratio (Yakel *et al.*, 1963). The powders were thoroughly mixed and heated for 48 h at 1523 K in a Pt crucible. The crystals were separated from the flux by increasing the temperature to 1723 K and evaporating the  $Bi_2O_3$  flux, (Bertaut *et al.*, 1963).

### **S3. Refinement**

The space group is determined to be P6<sub>3</sub>cm, taking into consideration the unit cell parameters, statistical analyses of intensity distributions and systematic extinctions (h-hl:  $1 \neq 2n$ ; 00 l:  $1 \neq 2n$ ). Attempts to fit the intensities with a crystal structure in space group P6<sub>3</sub>/*mcm*, were unsuccessful. Anisotropic displacement parameters and *SHELXL97* indicated that the Lu ions should be shifted away from the mirror plane perpendicular to the *c* axis.

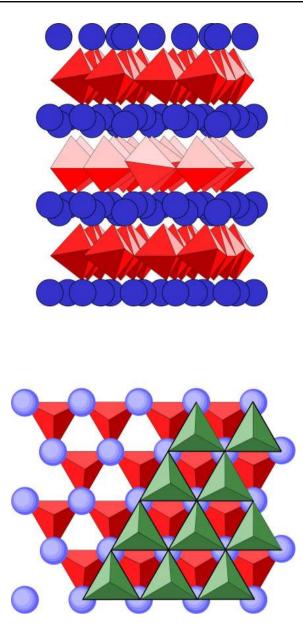
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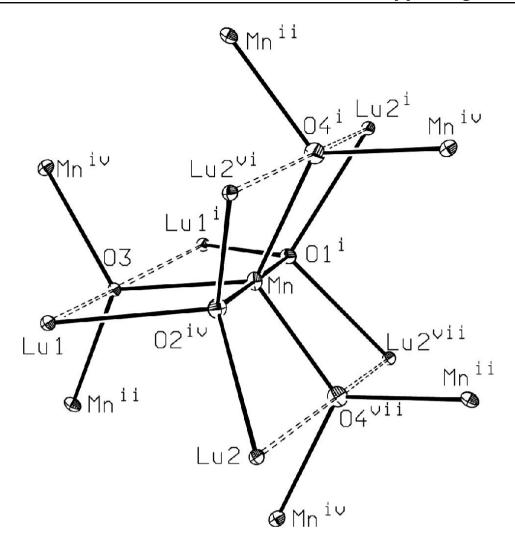
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### Figure 1

Schematic view of the crystallographic structure of LuMnO<sub>3</sub>. The top panel shows a view along the basal plane. Lu is represented by shaded spheres, and the MnO<sub>5</sub> clusters are represented by trigonal bipyramids. This panel highlights the two-dimensional nature of the structure. The lower panel depicts a view along the *c* axis of two layers to show the stacking of the bipyramids.



### Figure 2

Perspective *ORTEPII* (Johnson, 1976) drawing of all inequivalent atoms. All atoms are represented by atomic displacement ellipsoids drawn to encompass 50% of the electron density.

### Lutetium Manganese Oxide

Crystal data	
LuMnO <sub>3</sub> $M_r = 277.90$ Hexagonal, $P6_3cm$ Hall symbol: P 6c -2 a = 6.038 (1) Å c = 11.361 (1) Å V = 358.70 (9) Å <sup>3</sup> Z = 6 F(000) = 720	Unit cell parameters (Duisenberg, 1992. J. Appl. Cryst. 25, 92-96) and orientation matrix were determined from a least-squares treatment of SET4 (de Boer & Duisenberg, 1984) setting. Reduced cell calculations did not indicate any higher metric lattice symmetry and examination of the final atomic coordinates of the structure did yield extra symmetry elements (Spek, 1988. J. Appl. Cryst. 21, 578-579; Le Page 1987. J. Appl. Cryst. 20, 264-269; Le Page, Y. 1988. J. Appl. Cryst. 21, 983-984), but they are not compatible with the structure. $D_x = 7.719 \text{ Mg m}^{-3}$
	Mo <i>Ka</i> radiation, $\lambda = 0.71073$ Å Cell parameters from 22 reflections

 $\theta = 28.0-28.8^{\circ}$   $\mu = 46.03 \text{ mm}^{-1}$ T = 293 K

### Data collection

Enraf Nonius CAD-4F diffractometer
Radiation source: fine focus sealed Philips Mo tube
Perpendicular mounted graphite
monochromator $\omega/2\theta$ scans
Absorption correction: analytical (Meulenaer & Tompa, 1965)
$T_{\rm min} = 0.084, T_{\rm max} = 0.759$

### Refinement

Refinement on  $F^2$ Least-squares matrix: full  $R[F^2 > 2\sigma(F^2)] = 0.027$  $wR(F^2) = 0.065$ S = 1.05833 reflections 32 parameters 1 restraint 0 constraints

### Special details

Platelet, black  $0.12 \times 0.10 \times 0.004 \text{ mm}$ 

4711 measured reflections 833 independent reflections 610 reflections with  $F > 4\sigma(F)$  $R_{int} = 0.094$  $\theta_{max} = 40.0^\circ, \theta_{min} = 3.6^\circ$  $h = -10 \rightarrow 9$  $k = 0 \rightarrow 10$  $l = -20 \rightarrow 20$ 3 standard reflections every 180 min intensity decay: no decay, variation 2.8%

$$\begin{split} &w = 1/[\sigma^2(F_o^2) + (0.0293P)^2] \\ &\text{where } P = (F_o^2 + 2F_c^2)/3 \\ (\Delta/\sigma)_{\text{max}} < 0.001 \\ \Delta\rho_{\text{max}} = 2.0 \ (4) \ \text{e} \ \text{\AA}^{-3} \\ \Delta\rho_{\text{min}} = -5.6 \ (4) \ \text{e} \ \text{\AA}^{-3} \\ &\text{Extinction correction: } SHELXL97 \ (\text{Sheldrick}, \\ 1997), \ \text{Fc}^* = \text{kFc}[1+0.001\text{xFc}^2\lambda^3/\sin(2\theta)]^{-1/4} \\ &\text{Extinction coefficient: } 0.0024 \ (2) \end{split}$$

**Geometry**. Bond distances, angles *etc.* have been calculated using the rounded fractional coordinates. All e.s.d.'s are estimated from the variances of the (full) variance-covariance matrix. The cell e.s.d.'s are taken into account in the estimation of distances, angles and torsion angles

**Refinement**. Refinement of  $F^2$  against ALL reflections. The weighted *R*-factor *wR* and goodness of fit *S* are based on  $F^2$ , conventional *R*-factors *R* are based on *F*, with *F* set to zero for negative  $F^2$ . The threshold expression of  $F^2 > 2\sigma(F^2)$  is used only for calculating *R*-factors(gt) *etc.* and is not relevant to the choice of reflections for refinement. *R*-factors based on  $F^2$  are statistically about twice as large as those based on *F*, and *R*-factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters  $(Å^2)$ 

	x	У		Ζ	$U_{ m iso}$ */ $U_{ m eq}$		
Lu1	0.00000	0.00	000	0.27394 (6)	0.00438 (12)		
Lu2	-0.66667	-0.3	3333	0.23038 (2)	0.00460 (1)		
Mn	-0.3355 (10)	-0.3	355 (10)	-0.00077 (13)	0.0048 (	0.0048 (5)	
01	-0.3070 (18)	-0.3	070 (18)	0.1642 (6)	0.0053 (	0.0053 (16)	
O2	-0.3614 (17)	-0.3	614 (17)	-0.1638 (6)	0.0068 (	16)	
O3	0.00000	0.00	000	-0.0285 (12)	0.0034 (	19)	
O4	-0.66667	-0.3	3333	0.0190 (9)	0.0077 (19)		
Atomic	displacement param U <sup>11</sup>	eters $(\hat{A}^2)$ $U^{22}$	$U^{33}$	U <sup>12</sup>	$U^{13}$	$U^{23}$	
Lul	0.0044 (2)	0.0044 (2)	0.0043 (2)	0.0022 (1)	0.0000	0.0000	
Lu2	0.0041 (1)	0.0041 (1)	0.0056 (2)	0.0021 (1)	0.0000	0.0000	

# supporting information

Mn	0.0053 (14)	0.0053 (6)	0.0023 (3)	0.0016 (7)	-0.0005	-0.0005 (3)
01	0.007 (3)	0.007 (3)	0.004 (2)	0.005 (3)	0.0015 (17)	0.0015 (17)
O2	0.006 (3)	0.006 (3)	0.007 (2)	0.002 (3)	-0.0018 (17)	-0.0018 (17)
O3	0.004 (2)	0.004 (2)	0.002 (5)	0.0019 (12)	0.0000	0.0000
O4	0.009 (3)	0.009 (3)	0.005 (4)	0.0045 (14)	0.0000	0.0000

Geometric parameters (Å, °)

1 ( , , ,			
Lu1—O1	2.234 (9)	Lu2—O2 <sup>vii</sup>	2.277 (12)
Lu1—O2 <sup>i</sup>	2.294 (10)	Lu2—O1 <sup>viii</sup>	2.227 (15)
Lu1—O3 <sup>i</sup>	2.244 (14)	Lu2—O2 <sup>ix</sup>	2.277 (9)
Lu1—O3	3.436 (14)	Lu2—O1 <sup>x</sup>	2.227 (11)
Lu1—O1 <sup>ii</sup>	2.234 (12)	Lu2—O2 <sup>v</sup>	2.277 (10)
Lu1—O2 <sup>iii</sup>	2.294 (9)	Mn—O1	1.882 (7)
Lu1—O1 <sup>iv</sup>	2.234 (11)	Mn—O2	1.859 (7)
Lu1—O2 <sup>v</sup>	2.294 (12)	Mn—O3	2.050 (6)
Lu2—O1	2.227 (12)	Mn—O4	2.019 (7)
Lu2—O4	2.401 (10)	Mn—O4 <sup>xi</sup>	2.019 (6)
Lu2—O4 <sup>vi</sup>	3.279 (10)		
O1—Lu1—O2 <sup>i</sup>	77.1 (4)	O1 <sup>viii</sup> —Lu2—O2 <sup>v</sup>	76.8 (4)
01—Lu1—O3 <sup>i</sup>	123.9 (2)	O1 <sup>x</sup> —Lu2—O2 <sup>ix</sup>	77.6 (4)
O1—Lu1—O1 <sup>ii</sup>	91.9 (4)	$O2^{ix}$ —Lu2— $O2^{v}$	94.7 (3)
O1—Lu1—O2 <sup>iii</sup>	164.0 (3)	$O1^{x}$ —Lu2— $O2^{v}$	167.8 (3)
O1—Lu1—O1 <sup>iv</sup>	91.9 (4)	O1—Mn—O2	179.6 (6)
O1—Lu1—O2 <sup>v</sup>	77.1 (4)	O1—Mn—O3	93.6 (5)
$O2^{i}$ —Lu1—O3 <sup>i</sup>	72.04 (18)	O1—Mn—O4	86.2 (5)
O1 <sup>ii</sup> —Lu1—O2 <sup>i</sup>	77.1 (5)	O1—Mn—O4 <sup>xi</sup>	86.2 (5)
O2 <sup>i</sup> —Lu1—O2 <sup>iii</sup>	110.9 (4)	O2—Mn—O3	86.0 (5)
$O1^{iv}$ —Lu1— $O2^{i}$	164.0 (3)	O2—Mn—O4	94.0 (5)
$O2^{i}$ —Lu1— $O2^{v}$	110.9 (4)	$O2$ — $Mn$ — $O4^{xi}$	94.0 (5)
O1 <sup>ii</sup> —Lu1—O3 <sup>i</sup>	123.9 (2)	O3—Mn—O4	120.2 (3)
O2 <sup>iii</sup> —Lu1—O3 <sup>i</sup>	72.04 (18)	$O3$ — $Mn$ — $O4^{xi}$	120.2 (3)
$O1^{iv}$ —Lu1— $O3^{i}$	123.9 (2)	O4—Mn—O4 <sup>xi</sup>	119.4 (3)
$O2^v$ —Lu1— $O3^i$	72.04 (19)	Lu1—O1—Lu2	104.2 (4)
O1 <sup>ii</sup> —Lu1—O2 <sup>iii</sup>	77.1 (4)	Lu1—O1—Mn	129.2 (5)
$O1^{ii}$ —Lu1— $O1^{iv}$	91.9 (5)	Lu1—O1—Lu2 <sup>xi</sup>	104.2 (4)
$O1^{ii}$ —Lu1— $O2^{v}$	164.0 (3)	Lu2—O1—Mn	106.8 (5)
O1 <sup>iv</sup> —Lu1—O2 <sup>iii</sup>	77.1 (4)	Lu2—O1—Lu2 <sup>xi</sup>	103.0 (4)
$O2^{iii}$ —Lu1— $O2^{v}$	110.9 (4)	Lu2 <sup>xi</sup> —O1—Mn	106.8 (4)
$O1^{iv}$ —Lu1— $O2^{v}$	77.1 (5)	Lu1 <sup>xii</sup> —O2—Mn	103.1 (4)
O1—Lu2—O4	70.3 (2)	Lu2 <sup>xii</sup> —O2—Mn	123.9 (5)
O1—Lu2—O2 <sup>vii</sup>	167.8 (3)	Lu2 <sup>xiii</sup> —O2—Mn	123.9 (6)
01—Lu2—O1 <sup>viii</sup>	109.2 (4)	Lu1 <sup>xii</sup> —O2—Lu2 <sup>xii</sup>	100.8 (4)
01—Lu2—O2 <sup>ix</sup>	76.8 (3)	Lu1 <sup>xii</sup> —O2—Lu2 <sup>xiii</sup>	100.8 (3)
01—Lu2—O1 <sup>x</sup>	109.2 (5)	Lu2 <sup>xii</sup> —O2—Lu2 <sup>xiii</sup>	99.9 (3)
01—Lu2—O2 <sup>v</sup>	77.6 (4)	Lu1 <sup>xii</sup> —O3—Mn	98.8 (4)
O2 <sup>vii</sup> —Lu2—O4	121.9 (2)	Mn—O3—Mn <sup>ii</sup>	117.7 (3)

O1 <sup>viii</sup> —Lu2—O4	70.3 (2)	Mn—O3—Mn <sup>iv</sup>	117.7 (3)
$O2^{ix}$ —Lu2—O4	121.87 (19)	Lu1 <sup>xii</sup> —O3—Mn <sup>ii</sup>	98.8 (4)
O1 <sup>x</sup> —Lu2—O4	70.27 (19)	$Lu1^{xii}$ —O3— $Mn^{iv}$	98.8 (4)
O2 <sup>v</sup> —Lu2—O4	121.9 (2)	Mn <sup>ii</sup> —O3—Mn <sup>iv</sup>	117.7 (4)
O1 <sup>viii</sup> —Lu2—O2 <sup>vii</sup>	77.6 (4)	Lu2—O4—Mn	96.4 (3)
$O2^{vii}$ —Lu2— $O2^{ix}$	94.7 (3)	Lu2—O4—Mn <sup>viii</sup>	96.4 (3)
O1 <sup>x</sup> —Lu2—O2 <sup>vii</sup>	76.8 (4)	Lu2—O4—Mn <sup>x</sup>	96.4 (3)
$O2^{vii}$ —Lu2— $O2^{v}$	94.7 (3)	Mn—O4—Mn <sup>viii</sup>	118.8 (3)
$O1^{viii}$ —Lu2— $O2^{ix}$	167.8 (3)	Mn—O4—Mn <sup>x</sup>	118.8 (3)
O1 <sup>viii</sup> —Lu2—O1 <sup>x</sup>	109.2 (5)	Mn <sup>viii</sup> —O4—Mn <sup>x</sup>	118.8 (3)

Symmetry codes: (i) *x*-*y*, *x*, *z*+1/2; (ii) -*y*, *x*-*y*, *z*; (iii) -*x*, -*y*, *z*+1/2; (iv) -*x*+*y*, -*x*, *z*; (v) *y*, -*x*+*y*, *z*+1/2; (vi) -*x*+*y*-1, *y*, *z*+1/2; (vii) *x*-*y*-1, *x*, *z*+1/2; (viii) -*y*-1, *x*-*y*, *z*; (ix) -*x*-*y*, *z*; (ix) -*x*+*y*-1, *y*, *z*+1/2; (vii) *x*-*y*-1, *x*, *z*+1/2; (viii) -*y*-1, *x*-*y*-1, *z*+1/2; (viii) -*x*+*y*-1, *y*, *z*+1/2; (viii) -*x*+*y*-1, *y*, *z*+1/2; (viii) -*y*-1, *x*-*y*-1, *x*, *z*+1/2; (viii) -*y*-1, *x*-*y*-1, *z*+1/2; (viii) -*x*+*y*-1, *y*, *z*-1/2; (viii) -*x*+*y*-1, *y*-1, *z*-1/2; (viii) -*x*+*y*-1, *y*-1/2; (viii) -*x*+*y*-1, *y*-1/2; (viii) -*x*+*y*-1, *y*-1, *z*-1/2; (viii) -*x*+*y*-1, *y*-1, *z*-1/2; (viii) -*x*+*y*-1, *y*-1, *z*-1/2; (viii) -*x*-*y*-1, *z*-1/2; (viii) -*x*-*y*-*y*-1, *z*-1/2; (viii) -*x*-*y*-*y*-1, *z*-1/2; (viii) -*x*-*y*-*y*-1, *z*-1/2; (viii) -*x*-*y*-*y*-*y*-*y*