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HIGH SPIN STATES OF CONFIGURATION $(1d_{5/2})_{5+,0}^2$ AND $(1g_{9/2})_{9+,0}^2$ STRONGLY POPULATED BY THE (α , d) REACTION

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High Spin States of Configuration $(ld_{5/2})_{5+,0}^2$ and $(lg_{9/2})_{9+,0}^2$ Strongly Populated by the (α ,d) Reaction*

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ABSTRACT

The (α ,d) reactions on targets of ¹³C, ¹⁴C, ¹⁵N, and ²⁰Ne were studied using alpha particle beams of 40.1, 46.0, 45.4, and 44.5 MeV, respectively. Angular distributions were obtained. States where the captured protonneutron pair is in the $(1d_{5/2})_{5+,0}^2$ configuration coupled to an unperturbed target core are located and possible spin assignments are suggested. These states are ¹⁵N, 13.03 MeV (11/2-), 11.95 MeV (9/2-); ¹⁶N, 5.75 MeV (5+); ¹⁷O, 7.74 MeV (11/2-), 9.14 MeV (9/2-); ²²Na, 1.528 MeV (5+).

Separated isotopes 52 Cr, 54,56 Fe, 58,60,62 Ni, and 64,66,68 Zn were used as targets to study the (α ,d) reaction with a 50 MeV alpha particle beam. States with a probable configuration of $(lg_{9/2})_{9+,0}^2$ were located. These states are 54 Mn, 9.47 MeV; 56 Co, 8.92 MeV; 58 Co, 6.79 MeV; 60 Cu, 5.99 MeV; 62 Cu, 4.75 MeV; 64 Cu, 4.57 MeV; 66 Ga, 2.99 MeV; 68 Ga, 2.88 MeV.

The residual interaction energies between the proton and neutron in the configurations $(ld_{5/2})_{5+,0}^2$, $(lf_{7/2})_{7+,0}^2$, and $(lg_{9/2})_{9+,0}^2$ were derived from the excitation energies determined in the present work and previous work on $(ld_{5/2})_{5+,0}^2$ and $(lf_{7/2})_{7+,0}^2$ states. For $T_z \neq 0$ nuclides, an "interaction model" method was proposed to extract the residual interaction energy. The mean values of the residual interaction energies are about -3.9, -3.0, -2.2 MeV, respectively, for the three mentioned configurations. There is a slight decrease of residual interaction energy with increasing A. These results are reproduced satisfactorily by conventional shell model calculations.

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Both the interaction model method and Talmi's shell model calculation method were used to calculate the excitation energies of states with $(1d_{5/2})_{5+,0}^2$ configuration. In general, the former method gives better agreement with the experimental results.

I. INTRODUCTION

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Pioneering spectroscopic studies of (α,d) reactions on nuclides with $A \leq 40$ using alpha particle beam energies from 42 MeV to 53 MeV^{1,2,3} have suggested that the most strongly populated states are those in which the captured proton and neutron enter the same shell model state¹ and couple to the maximum angular momentum with zero isobaric spin.² The pair couples to the spin and isobaric spin of the target nuclide to give the total angular momentum and isobaric spin of the preferentially populated state. The situation can be represented by the following vector coupling relation:

$$[\vec{j}_{i},\vec{T}_{i} + (\vec{j},\vec{t} + \vec{j},\vec{t})_{J=2j,T=0}]_{J_{f},T_{f}} = T_{i}$$

where J_i, T_i are the total angular momentum and isobaric spin of the target nuclide, j,t are those of the shell model state into which the proton and neutron are captured, and J_f, T_f are those of the final state. The allowed J_r values have the range:

$$J_{i} - J \leq J_{f} \leq J_{i} + J$$

Hence, levels with a multiplicity of $(2J_i+1)$, if $J>J_i$, or (2J+1), if $J<J_i$, will be strongly populated.

These studies of (α, d) reactions were carried out by Rivet et al.³ on target nuclides 12 C, 14 , 15 N, 16 O, 20 Ne, 24 , 26 Mg, 28 Si, 32 S, 40 Ar, and 40 Ca. The following levels of the residual nuclides were strongly populated and were assigned to the configuration $[J_i, T_i + (1d_{5/2})^2_{5+0}]_{J_f}, T_f = T_i$:

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¹⁴N: 9.00 MeV (5+) ¹⁶O: 14.39 MeV (4+), 14.81 MeV (6+), 16.24 MeV (5+) (Refs. 3,75) ¹⁷O: 7.6 MeV (11/2-), 9.0 MeV (9/2-) ¹⁸F: 1.119 MeV (5+) (Ref. 4) ²²Na: 1.53 MeV (5+) ²⁶Al: Ground state (5+) Those of $[J_i,T_i + (lf_{7/2})_{7+,0}^2]_{J_f}, T_f = T_i$ are: ²⁶Al: 8.27 MeV (7+) ²⁸Al: 9.80 MeV (7+) ³⁰P: 7.03 MeV (7+) ³⁴cl: 5.2 MeV (7+)

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⁴²K: 1.87 MeV (7+) ⁴²Sc: 0.60 MeV (7+)

Since $J>J_i$ in all these cases, we expect a multiplicity of $(2J_i+1)$ levels for each nuclide. For even-even target nuclides, where $J_i=0$, there should be only one highly populated level. For target nuclides ${}^{14}N(J_i=1)$ and ${}^{15}N(J_i=1/2)$ we expect a multiplet of three and two levels, respectively, to occur. These predictions are borne out by the experiments.

The assignments of these high spin levels were based on three criteria:

a) Largest cross section

b) Similarity in the shape of angular distribution (a more or less monotonically decreasing curve with little structure)

c) A smooth decreasing curve when $-Q_f$ was plotted against A residual, where $-Q_f$ is equal to the sum of -[Q value of the (α,d) reaction] and the excitation energy of the assigned state, and $A_{residual}$ is the mass number of the residual nucleus (A_{target} + 2). At the time when these assignments were made, the only spins known from other work were a possible 5+ state at about 1 MeV in 18 F, 26 Al g.s. 5+, and 42 Sc 0.6 MeV 7+ or 6+. Recently, the 8.963 MeV level of 14 N was assigned spin 5+, 5,6 the 1.131 MeV level of 18 F was definitely established as having spin 5+, 7 and the 1.530 MeV level of 22 Na was assigned the spin 5+. 8 All these direct experimental assignments are in agreement with the predictions of the proposed model obtained from the systematics of the (α ,d) reactions. These agreements strongly indicate the reliability of the model.

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In order to test further the validity of the model and to extend the study to the medium mass region $(52 \le A \le 70)$ in a search for the existence of $[J_i,T_i + (\lg_{9/2})_{9+,0}^2]_{j+,T_f=T_i}$ states, the targets $^{13,14}C$, ^{15}N , ^{20}Ne , ^{52}Cr , $^{54,56}Fe$, $^{58,60,62}Ni$, $^{64,66,68}Zn$ were used in the study of the (α,d) reaction with alpha-particle beam energies from 40 MeV to 50 MeV. The multiplicities of the strongly populated levels were found to be in accord with the predictions. Levels with a probable $(\lg_{9/2})_{9+,0}^2$ configuration were located.

II. EXPERIMENTAL

The Berkeley 88-inch sector-focused cyclotron was used to provide alpha particle beams from 40 MeV to 50 MeV. A counter telescope consisting of two lithium-drifted silicon semiconductor detectors was used to measure the energy as well as to identify the particles. The details of this system have been described previously.^{9,3}

A cylindrical chamber of approximately 3" in diameter and 1" in height was used as a gas target. The windows for entry and exit of beam particles and for the escape of secondary particles were 0.0001" thick Havar foil.¹⁰ A typical pressure of about 20 cm Hg was used in the gas cell.

The ¹³C target was a CH_{4} gas which contained 93.7% ¹³ CH_{4} .¹¹ The ¹⁵N target gas had an isotopic purity of 99.71%¹² and the ²⁰Ne target gas had an isotopic purity of 98.1%.¹³ The solid ¹⁴C target,¹⁶ which contained large amounts of ¹²C and ¹⁶O impurities, was mounted on a 2 mg/cm² gold backing.

The solid targets of medium mass nuclides¹⁵ were prepared by vacuum evaporation of the metal onto a glass or metal plate coated with a thin layer of NaCl or Teepol¹⁴ as parting agent to permit separation of the foil from the plate. The self-supporting foils were then mounted on aluminum rectangular plates with 3/4 inch holes in the center. The isotopic purity of the various targets was: 52 Cr (99.9%), 54 Fe (90-98%), 56 Fe (98-99.9%), 58 Ni (98-99.9%), 60 Ni (95-99.8%), 62 Ni (95-99%), 64 Zn (99%), 66 Zn (90-99%), and 68 Zn (95-99%).

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III. RESULTS A. $\frac{13_{C(\alpha,d)}}{15_{N}}$

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This reaction was studied with a 13 C methane gas target at an alpha particle beam energy of 40.1 MeV. A typical spectrum taken at $\theta(1ab) = 12.0^{\circ}$ is shown in Fig. 1. The methane gas was found to decompose at a constant rate under irradiation of the incident beam. This effect was corrected by using the results of a monitor counter mounted at a fixed angle of 19° (1ab). Angular distributions for $\theta(cm) = 12.4^{\circ}-88.2^{\circ}$ are shown in Fig. 2. The energy resolution (FWHM) was about 130 keV. The excitation energies determined here, together with the total cross sections and previously known level information, are listed in Table I.

As shown in Fig. 1, only a few levels were populated strongly. The 13.028 MeV and 11.950 MeV levels were assigned as the doublet state with configuration:

$$\left[({}^{13}_{C \text{ g.s.}})_{1/2-,1/2} ({}^{1d}_{5/2})_{5+,0}^2 \right]_{11/2-,1/2}_{9/2-,1/2}$$

These assignments will be discussed in detail in Sect. IV.

$$\frac{14}{C(\alpha,d)} \frac{16}{N}$$

Solid ¹⁴C on a gold backing was used as the target. This reaction was studied with an alpha particle beam energy of 46.0 MeV. A typical spectrum taken at $\theta(lab) = 15.6^{\circ}$ is shown in Fig. 3. Angular distributions for $\theta(cm) = 14.5^{\circ}-93.9^{\circ}$ are shown in Fig. 4. The energy resolution (FWHM) was about 160 keV. The only highly populated level (at excitation 5.745 MeV) was assigned to have the dominant configuration:

$$\left[({}^{14}C \text{ g.s.})_{0+,1} ({}^{1d}_{5/2})_{5+,0}^2 \right]_{5+,1}$$

The measured excitation energies and total cross sections together with recent energy level information of ${}^{16}N$ are listed in Table II.

c. $15_{N(\alpha,d)}17_{0}$

Gaseous ¹⁵N was used as the target. The reaction was studied with an alpha particle beam energy of 45.4 MeV. A spectrum taken at $\theta(lab) = 13.2^{\circ}$ is shown in Fig. 5. Angular distributions for $\theta(cm) = 13.5^{\circ}-82.2^{\circ}$ are shown in Fig. 6. The energy resolution (FWHM) was about 150 keV. The measured excitation energies and total cross sections, together with energy level information of ¹⁷O are listed in Table III.

Two strong levels at 7.742 and 9.137 MeV were assigned to have the dominant configuration:

$$\left[\binom{15_{N \text{ g.s.}}}{1/2-,1/2} \binom{1d_{5/2}}{5+,0} \frac{2}{11/2-,1/2} \frac{2}{9/2-,1/2} \frac{2}{9/2-,1/2} \frac{2}{11/2-,1/2} \frac{2}{11/2-,1/$$

This result is in agreement with the previous (α, d) study at 47 MeV.² Better resolution was obtained in this work.

D. $\frac{20}{\text{Ne}(\alpha,d)^{22}\text{Na}}$

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This reaction was studied with an alpha particle beam energy of 44.5 MeV and a gaseous ²⁰Ne target. Figure 7 is a spectrum taken at $\theta(lab) = 11.2^{\circ}$. Angular distributions for $\theta(cm) = 10.5^{\circ}-57.4^{\circ}$ are shown in Fig. 8. The energy resolution was about 110 keV (FWHM). The measured excitation energies and total cross sections together with energy level information of ²²Na are listed in Table IV.

In general, the levels populated were the same as a previous study of this reaction.³ However, better resolution was obtained and the excitation energy studied was extended to about 16 MeV. Three levels (1.528, 7.460, and 7.874 MeV) were strongly populated. The level at 1.528 MeV was assigned to have the dominant configuration:

 $\left[\binom{20_{\text{Ne g.s.}}}{0+0}\binom{1d_{5/2}}{5+0}\right]_{5+0}$

E. $\frac{52_{Cr(\alpha,d)}^{54}Mn, 54,56_{Fe(\alpha,d)}^{56,58}Co, 58.60.62_{Ni(\alpha,d)}^{60,62,64}Cu}{and 64,66,68_{Zn(\alpha,d)}^{66,68,70}Ga}$

These reactions were studied with an alpha particle beam energy of 50.0 MeV at four lab angles--14°, 20°, 34° (or 35°) and 40° (or 41°). Separated isotope targets with purity ranging from 90% to 99.9% were used. The target thicknesses varied from 153 to 630 μ g/cm². In order to stop the deuterons, a counter telescope with a Δ E counter 0.06" thick and an E counter 0.12" thick was used. The dead layer of this thick Δ E detector was the main cause of the loss of energy resolution to a typical value of 170 keV (FWHM). Spectra of deuterons from these reactions are shown in Figs. 9-17. The high selectivity

in populating states by the (α,d) reaction again prevailed in this mass region. States where the captured proton-neutron pair are probably both in the $\lg_{9/2}$ state and coupled to 9+ were assigned for these nuclides. The differential cross sections for formation of these states at forward angles were about 1 mb/sr. Previously known level information for the product nuclei can be found in Refs. 26-37.

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IV. DISCUSSION

A. Criteria to Identify the $(1d_{5/2})^{2}_{5+,0}$ and $(1g_{9/2})^{2}_{9+,0}$ Levels

The $(1d_{5/2})_{5+,0}^2$ levels in light nuclides assigned by the present study and previous work^{2,3} are summarized in Table V. If from other work there are more accurately determined excitation energies for these levels, these values are listed. Angular distributions corresponding to the $(1d_{5/2})_{5+,0}^2$ levels obtained by this work are shown in Fig. 18. These angular distributions are similar to those of known 5+ levels of previous (α ,d) work. Only one of the latter, that of the 8.963 MeV 5+ level of 14 N, is also shown in Fig. 18.

As stated in the introduction, the criteria for identification of these states are that the cross section be large, the angular distributions be similar to each other and that the value of $-Q_f$ decrease monotonically with increasing A of the residual nucleus. (Q_f is the Q-value for formation of the level.)

The large cross sections arise from the following causes:

a) These states have higher spins than other states and hence the cross section is enhanced by a large statistical factor (2J+1).

b) The structure factor G for these states is large.³⁸ This means roughly that the initial state plus the deuteron picked up from the α particle have large overlap with the final state.

c) At 40-50 MeV alpha particle beam energy the momentum transferred to the target ($12 \le A \le 24$) by the captured proton-neutron pair at the nuclear surface is about 4m which favors capture of the two particles into the $1d_{5/2}$ shell model state (which can give an $L = \ell_n + \ell_p = 2 + 2 = 4$ transfer).³

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For $T_z = 0$ nuclei the calculation is simple. For example, in ${}^{14}N$, the 8.963 MeV 5+ level was assigned to have the configuration

$$\binom{12}{12} \operatorname{core}(13) \binom{12}{5/2} \binom{2}{5+,0} = 0$$

The total separation energy of the proton and neutron in this configuration from the $^{12}\mathrm{C}$ core, denoted by $\mathrm{S}_{\mathrm{m}},$ is

$$T = S_{pn} - E^* = S_p + S_n - E(1d_{5/2})^2_{5+,0}$$
(1)

where S_{pn} is the separation energy of the last proton and neutron in the ground state of ¹⁴N from the ¹²C core, E^{*} is the excitation energy of the $(1d_{5/2})_{5+,0}^2$ state (equal to 8.963 MeV in this case), S_p is the separation energy of a proton in the $1d_{5/2}$ single-particle state of ¹³N(3.56 MeV 5/2+ state), S_n is the separation energy of a neutron in the $1d_{5/2}$ single-particle state of $^{13}C(3.85 \text{ MeV } 5/2+ \text{ state})$, and $E(1d_{5/2})_{5+,0}^2$ is the résidual interaction energy between the proton and the neutron in the configuration $(1d_{5/2})_{5+,0}^2$. The results of these calculations for the nuclides ¹⁴N, ¹⁸F, ²²Na, and ²⁶Al are listed in Table VII. The neighboring single particle state of Ref. 74 is used in calculating the separation energies. The residual interaction energies stay fairly constant over this mass region from A = 14 to 26 with a value of about -3.9 MeV, (i.e., attractive). Except for the nucleus ²⁶Al, the residual interaction decreases slightly with increasing A.

For $T_z \neq 0$ nuclei the situation is more complicated. As an example, the ll/2-, T = 1/2 state of ¹⁵N, which is assumed to have the following configuration:

$$\left[(^{13}_{\text{C core}})_{1/2-,1/2} (^{1d}_{5/2})_{5+,0}^{2} \right]_{11/2-,1/2}$$

will be discussed below.

The S_n value in Eq. (1) is equal to the neutron separation energy from the ¹³C ground state in the ¹⁴C state with configuration $(d_{5/2}, p_{1/2})_{3-,1}$. The S_p value in Eq. (1) is equal to the mean value of the proton separation energy from the ¹³C ground state weighted by assuming that the probability in the ¹⁴N($d_{5/2}, p_{1/2}$)_{3-,0} state is a_J , and the probability in the ¹⁴N($d_{5/2}, p_{1/2}$)_{3-,1} is b_J . The probabilities a_J , and b_J , are obtained by requiring that the total interaction energy of the two $d_{5/2}$ nucleons in a configuration $(1d_{5/2})_{5+,0}^2$ to the $p_{1/2}$ neutron of ¹³C be equal to the sum of the interaction of the $d_{5/2}$ proton to the $p_{1/2}$ neutron and of the $d_{5/2}$ neutron to the $p_{1/2}$ neutron. That is,

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$$\left< \left(1d_{5/2} \right)_{5+,0}^{2} p_{1/2} J = 11/2 T = 1/2 \left| \sum_{i=1}^{2} v_{i3} \right| \left(1d_{5/2} \right)_{5+,0}^{2} p_{1/2} J = 11/2, T = 1/2 \right)$$

$$= \left[a_{3} v_{3,0} + b_{3} v_{3,1} \right] + v_{3,1} .$$

On the right side of the above equation the notation $V_{J',T'}$ is used. The quantities in the bracket represent the neutron-proton interaction and the last term represents the neutron-neutron interaction. The quantity on the left side of the above equation can be expressed in terms of two body matrix elements $V_{J',T'}$ by applying Eq. (37-19) of Ref. 50. However, it must be noted that in the $(d_{5/2}, p_{1/2})_{3-,0}$ or $(d_{5/2}, p_{1/2})_{3-,1}$ state of ¹⁴N the proton is in the $d_{5/2}$ state half of the time while the proton in the $\left[(d_{5/2})_{5+,0}^2 p_{1/2}\right]_{J,T}$ state of ¹⁵N can only be in the $d_{5/2}$ state. Therefore, an additional Coulomb

energy correction must be introduced. The Coulomb energy difference between a $d_{5/2}$ proton coupled to the ¹²C core and a $p_{1/2}$ proton coupled to the ¹²C core is just the difference of the excitation energy between the $d_{5/2}$ single particle excited states of ¹³C and ¹³N, which are 3.85 MeV and 3.56 MeV, respectively. This difference is equal to 0.29 MeV. The Coulomb energy correction is equal to half of this value, i.e., 0.15 MeV.

The above method is used to calculate the residual interaction for the $^{15}N(13.023 \text{ MeV})$, $^{17}O(7.743 \text{ MeV})$, $^{16}O(16.24 \text{ MeV})$, and $^{16}N(5.747 \text{ MeV})$ levels assuming that these states have spins 11/2, 11/2, 6, and 5 respectively. The Coulomb energy corrections are 0.15, 0.22, 0, and 0.13 MeV respectively. The values obtained, as well as the level information of neighboring nuclides used, are listed in Table VII. The name "interaction model" is used to signify the present separation of interaction energy of $(1d_{5/2})^2_{5+,0}$ -to-core into proton-to-core and neutron-to-core interactions.

From (a,d) experiments, a level in each of the four $T_z = 0$ nuclei ¹⁴N, ¹⁸F, ²²Na, and ²⁶Al was assigned spin 5+ and the configuration (core)(1d_{5/2})²_{5+,0}. From independent work, each of these levels is known to have spin 5+. One may therefore safely assume that the main configuration is indeed (core)(1d_{5/2})²_{5+,0}. Further, the experimental residual interaction energies stay constant at about -3.9 MeV over the mass region A = 14 to 26, as will be shown in Part D. This value of the $(1d_{5/2})^2_{5+,0}$ interaction energy is very reasonable, proving that the method used for the extraction of the interaction energies for the T = 0 nuclei is correct. Since the calculation of the interaction energy for the $T_z \neq 0$ nuclei gives a result in excellent agreement with that obtained for the $T_z = 0$ nuclei, one may have considerable confidence in the method of calculation as well as in the assignments of spins and parities for the levels of $T_z \neq 0$ nuclei shown in Table VII. Alternatively, an experimental verification of the spin of these states would prove the correctness of the above interaction model approach used for the $T_z \neq 0$ nuclides.

One can expect that the above calculational method, for both $T_z = 0$ or $T_z \neq 0$ nuclides, is quite good on the following two accounts:

a) Because of the high spin value of the state considered, configuration mixing is small.

b) By using experimental energies of neighboring nuclei, some core excitation has already been taken into account. That is to say, the states of neighboring nuclei used in the calculation need not have a very pure configuration. As long as the presence of the additional $d_{5/2}$ nucleon of the two particle state does not alter this configuration appreciably, the interaction energy thus calculated may still be accurate even though the true configuration of the target is not purely $[({}^{12}C \text{ core})(p_{1/2})^n]$.

Following the same method as discussed above, the residual interaction energy between proton and neutron in the $(lf_{7/2})_{7+,0}^2$ configuration has been calculated. The results are listed in Table VIII. The excitation energies of the two-particle excited states used here are from Ref. 3. For ²⁸Al, the values of a_J , and b_J , are 2/3 and 1/3, respectively. The Coulomb energy correction is 0.11 MeV. The residual interaction energy stays fairly constant but decreases slightly faster with increasing A as compared to the $(ld_{5/2})_{5+,0}^2$ residual interaction energies.

Similarly, the interaction model method can be applied to calculate the residual interaction energies between proton and neutron in the $(\lg_{9/2})_{9+,0}^2$ configuration. These calculations need the value of the excitation energies of the analog states. The single particle $\lg_{9/2}$ states in 59 Cu and 61 Cu analog to 59 Ni and 61 Ni are known. The Coulomb displacement energies, E_c , of the 53 Mn, 55 Co, 63 Cu, and Ga (natural mixture of isotopes) analogs to the ground states of 53 Cr, 55 Fe, 63 Ni, and Zn are equal to 8.390 MeV, 8.660 MeV, 9.300 MeV, and 9.76 MeV, respectively. 57 The $\lg_{9/2}$ analog states are assumed to have the same excitation energies above the analogs of the ground states of 53 Cr, 55 Fe, 63 Ni, 65 Zn, and 67 Zn as the excitation energies of the $\lg_{9/2}$ single particle states of the latter nuclei. Coulomb energy corrections are not included because there is not enough experimental information to calculate these values. This is justified from the previous calculations for $(\lg_{5/2})_{5+,0}^2$ which have shown that these corrections are only about 150-220 keV.

The constants a_J , and b_J , for each nucleus are determined with the following assumption about the configuration of the ground state of the target core:

⁵²Cr:
$$(lf_{7/2})_{0+,2}^{12}$$

⁵⁴Fe: $(lf_{7/2})_{0+,1}^{14}$
⁵⁸Ni: $(2p_{3/2})_{0+,1}^{2}$ or $(lf_{5/2})_{0+,1}^{2}$
⁶⁰Ni: $(2p_{3/2})_{0+,2}^{4}$ or $(lf_{5/2})_{0+,2}^{4}$
⁶²Ni: $(lf_{5/2})_{0+,3}^{6}$
⁶⁴Zn: $(lf_{5/2})_{0+,2}^{8}$
⁶⁶Zn: $(2p_{1/2})_{0+,0}^{4}$ $(lf_{5/2})_{0+,3}^{6}$

In all the cases thus calculated, the constants a_J , and b_J , have the value:

$$a_{J}$$
, = $2T_{i}/(2T_{i}+1)$ b_{J} , = $1/(2T_{i}+1)$

where T_i is the isobaric spin quantum number of the target. The results of these calculations are listed in Table IX. For the nuclei 58 Co and 170 Ga, the target nuclei (56 Fe and 68 Zn) have to occupy two shell model states (i.e., $(f_{7/2})^{-2}(p_{3/2})^{-2}$ or $(p_{3/2})^{6}(f_{5/2})^{6}$, respectively) beyond a closed $lf_{7/2}$ shell. Then, one needs to calculate the interaction energy between the $g_{9/2}$ nucleons and the j_1 and j_2 nucleons in the configuration

$$\begin{bmatrix} (\mathbf{j}_1)^{n_1} & (\mathbf{j}_2)^{n_2} \\ \mathbf{j}_1^{T_1} & (\mathbf{j}_2)^{T_2} \end{bmatrix}^{n_2} (\mathbf{lg}_{9/2})^{2}_{9+,0} \mathbf{J}_{9+,0}$$

Equation (37-19) of Ref. 50 is no longer adequate to treat this case. Hence, no calculation has been made for these two nuclides. Although configurations which may be different from the true ones are assumed for the g.s. of 62 Ni, 64 Zn, and 66 Zn, the calculated values may still be correct due to the second reason discussed above.

C. Calculation of Excitation Energies of States

with the Configuration $(1d_{5/2})_{5+0}^{2}$

One could use the following method to calculate the excitation energies of the $(1d_{5/2})_{5+,0}^2$ states for the nuclei ${}^{15}N$, ${}^{16}N$, ${}^{16}O$, and ${}^{17}O$. It is assumed that the residual interaction energy of $(1d_{5/2})_{5+,0}^2$ stays constant over this mass region and has a value of 3.90 MeV. Then one uses Talmi's method with the change that the $(d_{5/2}P_{1/2})$ interaction energies (i.e., $V_{3,0}$, $V_{2,0}$, $V_{3,1}$, and $V_{2,1}$) are expressed in terms of excitation energies of certain states of neighboring nuclei that can also be expressed in terms of $(d_{5/2}p_{1/2})$ interaction energies.

In the calculations for ${}^{16}N$, the 0.75 MeV 5/2+,3/2 level of ${}^{15}C$ and the 5.276 MeV 5/2+,1/2; 12.502 MeV 5/2+,3/2 levels of ${}^{15}N$ are assumed to be the J,T states of the configuration $[(p_{1/2})_{0,1}^2 d_{5/2}]_{J,T}$, where J = 5/2 and T = 1/2 or 3/2. For ${}^{16}O$, the 7.563 MeV 7/2+,1/2 and 7.154 MeV 5/2+,1/2 levels of ${}^{15}N$ and the 7.28 MeV 7/2(+),1/2 and 6.86 MeV 5/2+,1/2 levels of ${}^{15}O$ are assumed to be the J,T states of the configuration $[(p_{1/2})_{1,0}^2 d_{5/2}]_{J,T}$ with J = 7/2 or 5/2 and T = 1/2. For ${}^{17}O$, the 6.13 MeV 3-,0; 8.88 MeV 2-,0; 13.26 MeV 3-,1; and 12.97 MeV 2-,1 levels of ${}^{16}O$ and the ground state 2-,1; 0.300 MeV 3-,1 levels of ${}^{16}N$ are assumed to be the J,T states of the configuration $(p_{1/2}^{-1} d_{5/2})_{J,T}$ with J = 3 or 2 and T = 0 or 1. The results are presented in Fig. 20.

Comparable but less accurate results are obtained for the levels using Talmi and Unna's empirical matrix elements.⁴⁸ The results are shown in Fig. 21. Because the first method uses the excitation energies of neighboring nuclides which may contain some core excitation, this method will give better agreement to the experimental value if the target has a core excitation component (i.e., cannot be represented as a simple $(p_{1/2})^n$ configuration). For example, recent analysis of core polarization effects in ${}^{15}N_{-}{}^{15}O$ by Brown and Shukla suggest that there may be 10% of 2p-3h components in the ground state wave function of ${}^{15}N$ or ${}^{15}O.{}^{66}$ If, on the other hand, there is a considerable fragmentation of single-particle strength in the A+l nuclei, then associating the configuration with only one state may also be inappropriate. The ordering of the triplet in ¹⁶0 is interesting. Previous experimental work³ suggested that the ordering of the states might be 4+, 6+, 5+ based on the (2J + 1) rule. However, the (2J+1) rule is not followed for the doublet levels of both ¹⁵N and ¹⁷O strongly populated with the (α ,d) reaction. This is perhaps not unexpected since, particularly for the lowest spin member of a multiplet, configuration mixing is generally possible. In ¹⁶O there are quite a few known 4+ states and at least one 6+ state⁶⁷ (at 16.2 MeV) which could possibly mix with the 2p-2h states observed in the (α ,d) reaction. Recently the ¹⁴N(α ,d)¹⁶O experiment was repeated⁷⁵ at E_{α} = 40 MeV. With much better resolution than the previous experiment³ a state at 15.8 MeV, unobserved in the earlier work, was found to be contributing to the cross section of the 16.24 MeV state. Thus, the agreement with the (2J + 1) rule was only apparent. The excitation energies used here are those from Ref. 75.

The known 6+ in this region was identified by Carter, et al.⁶⁷ as a member of a 4p-4h rotational band built on the 6 MeV 0+ state. It has also been observed in the four-particle transfer ${}^{12}C({}^{6}Li,d){}^{16}O$ reaction.⁶⁸ However, Carter⁶⁷ quotes a width of 380 keV for the 4p-4h 6+ state at 16.2 MeV, with a lower limit of 200 keV.⁷⁷ Our data⁷⁵ indicates that the strong state observed in the (α ,d) reaction at 16.24 MeV has a width almost surely less than 200 keV, which seems inconsistent with associating it with the 16.2 MeV 4p-4h 6+ state.

Zuker, et al.⁶⁹ have done a shell model calculation of the levels of ¹⁶0 using a closed ¹²C core and considering particles in the $lp_{1/2}$, $ld_{5/2}$, and $2s_{1/2}$ shells. They found a 4p-4h 6+ state (presumably that of Carter, et al.⁶⁷) at 17.4 MeV and a triplet of levels of configuration

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$\left[\left({}^{12}c \right)_{0+,0} \left({}^{p}_{1/2} \right)_{1+,0}^{2} \left({}^{d}_{5/2} \right)_{5+,0}^{2} \right]_{4,5,6+,0} \right]$

which were relatively pure. Their wave functions 76 indicate that the states (14.9 MeV), 5+ (15.5 MeV), and 4+ (16.19 MeV). The 4+ wave function has about 20% 4p-4h mixed with the dominant 2p-2h configuration, while the 5+ and 6+ states are more pure, having only about 5% 4p-4h admixture. 76 Our own calculations suggest that the 6+ 2p-2h state is the one at 16.24 MeV (see Fig. 20), but unless the lower limit quoted by Carter 77 is incorrect, this seems unlikely.

D. Shell Model Calculations

Conventional shell model calculations are also used to calculate the residual interaction energies between proton and neutron in the configurations $(1d_{5/2})_{5+,0}^2$, $(1f_{7/2})_{7+,0}^2$, and $(1g_{9/2})_{9+,0}^2$. In these calculations only a triplet-even potential is needed. This is taken from Ref. 43 and is equal to:

$$V_{\rm TE} = -52 \ e^{-0.2922} \ r^2 \ (MeV)$$

Tables X, XI, and XII list the results of these calculations for the above mentioned three configurations, respectively. Two sets of Harmonic Oscillator parameter, v, (i.e., v_1 and v_2) are used. Within each set, the v value for the nucleus 18 F, 42 Sc, and 66 Ga is fixed first. The other v's for states with the same configuration are obtained by assuming an inverse dependence on $A^{1/3}$. The v_1 values for the nuclei 18 F, 42 Sc, and 66 Ga are calculated according to the following equation⁷⁰:

$$v_1 = (2n + \ell - 1/2)/R^2$$

where n, ℓ are the principle quantum number and orbital angular momentum of the shell model state concerned, respectively, and R is its rms radius. For ¹⁸F and ⁴²Sc, R is assumed to be the same as

the equivalent uniform radius of A = 17 and A = 41 nuclei obtained from the Coulomb energy difference of mirror nuclei.⁷¹ The v_1 value of ⁶⁶Ga is fixed by first calculating a v_1 value for ⁷³Ge (the first $\lg_{9/2}$ neutron) using the above equation with R calculated from Eq. (1) of Ref. 57 and then taking an inverse proportionality to $A^{1/3}$. The v_2 values of ${}^{18}F$ and ${}^{66}Ga$ are obtained by adjusting their values such that they will give the same residual interaction energies as the experimentally calculated values. The v values which are calculated from the often-used formula $\hbar\omega = 41 A^{-1/3}$ give too strong interaction energies and are not used here.

Comparison of the theoretical results thus obtained for the residual interaction energy with the experimentally extracted values allows the conclusion that the agreement is in general satisfactory. A reasonable slight adjustment of v's (the second set) for $(1d_{5/2})_{5+,0}^2$ and $(1g_{9/2})_{9+,0}^2$ configuration gives excellent agreement while no adjustment is needed for the v's of the $(1f_{7/2})_{7+,0}^2$ configuration. Kuo and Brown have calculated the residual interaction energy between proton and neutron in the configuration $(1d_{5/2})_{5+,0}^2$ for the nucleus 18 F (Ref. 72) and both $(1f_{7/2})_{7+,0}^2$ and $(1g_{9/2})_{9+,0}^2$ for 42 Sc (Ref. 73) from a free nucleon-nucleon scattering potential (i.e., the Hamada-Johnston potential). The results, -3.69 MeV, -2.199 MeV, and -1.840 MeV for the three configurations, are in agreement with the experimentally calculated values as well as with the values obtained from conventional shell model calculations. Their wave function for the 7+, T = 0 state of 42 Sc is 73

1.0 $(lf_{7/2})_{7+,0}^2$ -0.07 $(lg_{9/2})_{7+,0}^2$

which supports the postulate that this 7+ state has dominant configuration

$$\left[\left(\frac{40}{2} \text{ ca core}\right)\left(1 \int_{7/2}^{2} \int_{7+,0}^{2}\right]_{7+,0}\right]$$

These results indicate that the assignments of states with pure configuration

3

 $(ld_{5/2})_{5+,0}^2$, $(lf_{7/2})_{7+,0}^2$, and $(lg_{9/2})_{9+,0}^2$ made in the last section and previous work³ are reasonable.

v.

CONCLUSIONS

From the evidence presented in the previous section it can be concluded that:

a) The systematic trend of (α, d) reactions at alpha particle energy 40-50 MeV to populate strongly the states with a $(j)^2_{2j+,0}$ configuration still persists in the medium mass region nuclides studied.

b) States with configuration [(target core)(lg_{9/2})²_{9+,0}] are located.
c) States with configuration [(target core)(ld_{5/2})²_{5+,0})] of ¹⁵N, ¹⁶N, ¹⁷₀, and ²²Na are located.

d) The residual interaction energies between proton and neutron in the configurations $(1d_{5/2})_{5+,0}^2$, $(1f_{7/2})_{7+,0}^2$, and $(1g_{9/2})_{9+,0}^2$ are about -3.9, -3.0, -2.2 MeV, respectively. There is a slight decrease of these residual interaction energies with increasing A for all three configurations. The magnitudes of these residual interaction energies and their variation with A are reproduced satisfactorily by conventional shell model calculations.

e) The "interaction model" method used to extract from the experimental results the residual interaction energies for $T_z \neq 0$ nuclides is believed to be good, because it generates residual interaction energies which are in agreement both with those obtained for $T_z = 0$ nuclides, and with the results obtained by the shell model calculations. This method, which uses the excitation energy information of nuclei with mass number A to calculate the residual interaction energies or excitation energies of levels in the nucleus with mass number A+1 is believed to be more accurate than the method which tries to get a set of matrix elements from fitting the excitation energies of nuclides with a wider range of A.

f) The 16.24 MeV level of ¹⁶0 has a dominant 2p-2h configuration, $\left[\binom{14}{N} \text{ g.s.}_{1+,0} \binom{14}{5/2}_{5+,0}^2\right]_{4,5,6+,0}$ and may have a spin-parity 6+. Experimental determination of the spin of this state is needed in order to confirm this assignment.

The identification of the configuration of those states which are populated with medium cross sections in the (α,d) reaction by establishing systematic trends, spin and parity determination, and shell model calculation will be very interesting.

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FOOTNOTES AND REFERENCES

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Levels observed (MeV)	Previously Energy (MeV)	reported levels ^{a,b,c} Jπ	Intensity ^d (mb)	Dominant ^e configuration
0	Ò	1/2-	0.61	(p _{1/2}) ⁻¹
5.266±0.020	5.270	5/2+	2.25	$(p_{1/2})_{0}^{2} d_{5/2}$
	.5 . 299	1/2+		$(p_{1/2})_{0}^{2} 2s_{1/2}$
6.336±0.030	6.323	3/2-		$(p_{3/2})_2^{-1}$ f
7.170±0.020	7.154	5/2+	0.70	$(p_{1/2})_{1}^{2} d_{5/2}$
	7.300	3/2+		$(p_{1/2})_{1}^{2} 2s_{1/2}$
7.581±0.020	7.563	7/2+	0.94	$(p_{1/2})_{1}^{2} a_{5/2}$
	8.312	1/2+(3/2+)		$(p_{1/2})_1^2 2s_{1/2}$
8.587±0.020	8.570	3/2+	0.50	(p _{1/2}) ² d _{5/2}
	9.052	1/2+,3/2+		
9.169±0.030	9.155	3/2-(5/2)	1.19	
	9.233	≤5/2		
	9.762	5/2-		
9.808±0.020	9.832	7/2(-)	2.15	
	9.929	1/2+,3/2+		
	10.074	3/2+		
10.451±0.020	10.458	3/2,5/2,7/2		
	10.548	5/2		
10.698±0.020	10.710	3/2+		
	10.815	3/2		
	11.243	>1/2-		(a ant ; mu - 2)

Table I. $15_{\rm N}$ levels observed in $13_{\rm C}(\alpha,d)^{15}_{\rm N}$ reaction at 40.1 MeV.

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14.7

Levels observed	Previously rep	ported levels ^{a,b,c}	Intensity ^d (mb)	Dominant ^e configuration
(MeV)	Energy (MeV)	Jπ		
	11.299	1/2-		
	11.438	1/2+	n de la constante de la consta La constante de la constante de	
	11.616	1/2+(T=3/2)		
	11.773	3/2+		
	11.885	3/2-		
11.950±0.020	11.950	(9/2-) ^g	3.20	$(a_{5/2})_{5}^{2} p_{1/2}$
		>1/2		
	11.972	1/2-		
	12.103	5/2		
	12.152	3/2		
12.318±0.030	12.333	5/2		
	12.502	5/2+(T=3/2)		
	12.928	3/2-		•
	12.93	7/2-		
13.028±0.020		(11/2-) ^g	4.82	$(a_{5/2})_{5}^{2} p_{1/2}$
	13.15			
	13.18			
a _{Reference} 17.	b _{Reference}	18. ^C Reference	19.	
d Range of integ	gration: 10.0 t	co 75.0 deg (lab).		
e Reference 20.	f Reference	21.		
^g Assigned by th	nis work.			

Table I. Continued.

c

Levels observed (MeV)	Previously Energy (MeV)	reported levels ^a Jπ	Intensity ^b (mb)	Dominant ^a configuration
0	0 0	2-	1.35	$(p_{1/2})^{-1} d_{5/2}$
	0.120	0-		$(p_{1/2})^{-1} 2s_{1/2}$
0.307±0.02	0.300	3-	2.52	$(p_{1/2})^{-1} d_{5/2}$
	0.399			$(p_{1/2})^{-1} 2s_{1/2}$
	3.359	1+		
	3.519	(0-)		
3.961±0.02	3.957	(1,2,3)+	3.43	
	4.318			
	4.391			
	4.725	1-		$(p_{1/2})^{-1} d_{3/2}$
	4.774	(1,2,3)+		
	5.053			
	5.130			
	5.150			
	5.226			
	5.305	2-		$(p_{1/2})^{-1} d_{3/2}$
	5.520			
5.745±0.02	5.730	(5+) ^c	10.07	$(a_{5/2})_{5+}^{2} (p_{1/2})_{0}^{2}$
	6.009	(3-)		$(p_{3/2})^{-1} d_{5/2}$
	6.167			
	6.371			

Table II. ¹⁶N levels observed in ${}^{14}C(\alpha,d){}^{16}N$ reaction at 46.0 MeV.

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1.

Levels observed (MeV)	Previously Energy (MeV)	reported levels ^a Jπ	Intensity ^b (mb)	Dominant ^a configuration
	6.422	(2-)		$(p_{3/2})^{-1} d_{5/2}$
	6.512			
	6.613			
	6.854			
	7.006			
	7.133			
	7.250			
7.599±0.03	7.573		4.30	
	7.640			

Table II. Continued.

^cThis work.
Levels	Previously rep	orted levels ^{a,b}	Intensity ^C	Dominant
(MeV)	Energy (MeV)	Jπ	(mb)	contiguiación
0	0	5/2+	1.15	^d 5/2 s.p.
0.870±0.050	0.871	1/2+	0.11	2s _{1/2} s.p.
	3.058	(1/2-)		
3.850±0.050	3.846	5/2 -	0.18	
4.566±0.050	4.555	3/2-	0.09	
	5.083	3/2+		d _{3/2} s.p.
5.208±0.030	5.217		1.35	
	5.378	3/2-		
5.690±0.030	5.697	7/2-	1.37	
	5.729			
	5.866	≥3/2		12 · 2 · 2 · 2 · 2 · 2 · 2 · 2 · 2 · 2 ·
	5.940	1/2-		
	6.24			
	6.38	1/2+		
	6.87			
	7.161	5/2		
	7.28	3/2+		
7.367±0.030	7.373	5/2	0.67	
	7.560	≥7/2		
	7.676	3/2		
	7.691	7/2		

Table III. 17_0 levels observed in $15_N(\alpha,d)^{17}_0$ reaction at 45.4 MeV.

(continued)

	-	37	'-	-	•
÷.,		8			
	•				

Previously reported levels^{a,b} Intensity^c (mb) Levels Dominant observed configuration Jπ (MeV) Energy (MeV) 3/2 7.694 $(d_{5/2})_{5}^{2} p_{1/2}^{-1} d, e$ (11/2-)^{d,e} 6.58 7.742±0.020 1/2 7.91 8.08 3/2 8.147±0.030 8.20 3/2 0.30 8.27 8.340 1/2 8.390 5/2 8.459±0.030 8.460 0.68 7/2 8.493 3/2 (8.59) 8.70 3/2 8.890±0.030 8.89 3/2 0.53 8.96 7/2 9.06 (9/2-)^{d,e} $(d_{5/2})_{5}^{2} p_{1/2}^{-1} d, e$ 2.70 9.137±0.030 9.15 9.20 5/2 9.50 7/2 9.73 7/2 0.69 9.814±0.030 9.78 9.89 9/2

Table III. Continued.

(continued)

Ξú

Table III. Continued.

^a_{Reference 19.} ^b_{Reference 23.} ^c_{Range of integration: 11.2 to 70.8 deg (lab). ^d_{Reference 2.}}

^eAssigned by this work.

Table IV.	Na levels	observed in	$Ne(\alpha, \alpha)$	Na reaction	at 44.7 Mev.
Levels observed (MeV)	Previously Energy (MeV)	reported leve Jπ	els ^{a,b} T	Intensity ^d (mb)	Dominant configuration
0	0	3+	0	0.17	
	0.58305	1+	0		
	0.656	0+	1		
	0.8909	4+	0		
1.528±0.020	1.5281	5+	0	2.49	(d _{5/2}) ^{2 e,f}
1.946±0.030	1.9359	1+		0.35	
	1.9518	(2+)	1		
	1.9835	2+,3+			
	2.2104	1-			
2.558±0.040	2.5715	1(+),2		0.07	
2.976±0.020	2.9686	(3)		0.70	
	3.0594	(2)			
	3.526	≥2	· · · · ·	-	
	3.712	≥2			
	3.949	l			
	4.077		(1)		
	4.325				
	4.363	1,2			
4.488±0.030				0.34	
4.733±0.020	High leve	el density		0.50	
5.339±0.030	Spin and	parity unknow	'n	0.28	
					(continued)

Table IV. ²²Na levels observed in 20Ne(α ,d)²²Na reaction at 44.5 MeV

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Levels observed	Previously report	ed levels ^{a,b}	Intensity ^d (mb)	Dominant configuration
(MeV)	Energy Jn (MeV)	Г Т		
6.274±0.020			0.22	
6.617±0.030			0.63	
7.042±0.030		2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	0.42	
7.460±0.030	7.48 ^c		2.05	$(d_{5/2}, f_{7/2})_{6}^{e}$
7.874±0.030	7.89 [°]		0.97	
8.091±0.040			0.42	
8.659±0.040			0.72	
9.356±0.040			0.59	
9.990±0.040	High level dens	sity	0.45	
10.990±0.040	Spin and parity	unknown	0.69	
^a Reference 24.				
^b Reference 8.				
c _{Reference} 25.				
d Range of integ	ration: 9.0 to 50).0 deg (lab).		
e _{Reference} 3.				
f Assigned by th	is work.			

Table IV. Continued.

11. A.		-		
Final nucleus	Energy of excitation (MeV)	-Q _f (MeV)	វា	Т
14 _N	8.963 ±0.002 ^a	22.54	5+ ^a	0
15 _N	11.95 ±0.02	19.64	(9/2-)	1/2
	13.03 ±0.02	20.72	(11/2-)	1/2
16 _N	5.75 ±0.02	19.13	(5+)	l
160	14.39 ±0.03 ^b	17.50	(4,5+) ⁱ	0
	14.81 ±0.03 ^b	17.92	(5,4+) ⁱ	0
	16.24 ±0.03 ^b	19.35	(6+) ^{i,e}	0
170	7.74 ±0.02	17.54	(11/2-)	1/2
	9.14 ±0.03	18.94	(9/2-)	· 1/2
18 _F	1.1310±0.0015 ^c	17.45	5+ ^f	0
22 _{Na}	1.5281±0.0003 ^d	14.10	5+ ^g	0
26 _{Al}	g.s.	12.43	5+ ^h	0
a. Reference	5. ^b Reference 75.	^c Reference 39.	d _{Reference 24} .	
e Reference	40. ^f Reference 7.	^g Reference 8.	^h Reference 41.	•
ⁱ Assigned	by this work.			

Table V. The $(1d_{5/2})_{5+,0}^2$ levels observed in the (α,d) reaction and their $-Q_f$ values.

Final	Energy Level	-Q _f
nuc⊥eu	(MeV)	(MeV)
54 _{Mn}	9.47±0.05	20.04
56 _{Co}	8.92±0.03	19.85
58 _{Co}	6.79±0.03	18.27
60 _{Cu}	5.99±0.03	18.58
62 _{Cu}	4.75±0.03	17.12
⁶⁴ Cu	4.57±0.03	16.60
66 _{Ga}	2.99±0.03	16.00
68 _{Ga}	2.88±0.03	15.40
70 _{Ga}	2.88±0.03	14.69

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Table VI. High spin [probably $(\lg_{9/2})_{9+}^2$] levels observed in the (α ,d) reaction.

Two-particle	Single part:	icle state	
excited states	Assumed ld _{5/2} neutron states	Assumed ld _{5/2} proton states	E(ld _{5/2}) ^{2 c} 5+,0
¹⁴ N: 8.963 5+ ^d	¹³ c: 3.85 5/2+ ^{e,q}	¹³ N: 3,56 5/2+ ^{e,q}	-4.05
¹⁸ F: 1.131 5+ ^f	¹⁷ 0: 0.000 5/2+ ^{e,q}	¹⁷ F: 0.000 5/2+ ^{e,q}	-3.88
²² Na: 1.528 5+ ^g	²¹ Ne: 0.353 5/2+ ^r	²¹ Na: 0.338 5/2+ ^h	-3.47
²⁶ Al: 0.000 5+ ^h	²⁵ Mg: 0.000 5/2+ ^h	²⁵ Al: 0.000 5/2+ ^h	-4.04
¹⁵ N: 13.03 (11/2-) ¹⁷ 0: 7.74 (11/2-)	ⁱ ¹⁴ c: 6.723 3-, T=1 ^{j,q,q} ⁱ ¹⁶ N: 0.300 3-, T=1 ^{ℓ,q}	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-3.57 ^b -3.69 ^b
¹⁶ 0: 16.24 (6+) ⁱ	¹⁵ N: 7.57 7/2+ ⁿ	¹⁵ 0: 7.28 $(7/2+)^n$ $l_n=2$	-3.44 ^b
¹⁶ N: 5.75 (5+) ⁱ	¹⁵ C: 0.75 5/2+,T=3/2 ^{0,0}	1 ¹⁵ N: 5.276 5/2+, T=1/2 ⁿ 12.502 5/2+, T=3/2 ^p	-3.82 ^b
^a All the energies are in	units of MeV.		
^b Calculated by using the	interaction model discuss	ed in the text.	
c Experimental proton-neu	tron residual interaction (energy.	
^d References 5,6. ^e Refer	ence 43. ^f Reference 7. ^g	Reference 8. ^h Reference 41.	ⁱ Reference 44.
^j Reference 45. ^k Referen	ice 43. ^l Reference 22. ^m R	eference 46. ⁿ Reference 18.	^O Reference 19.

Table VII.^a Experimental residual interaction energies for $(ld_{5/2})_{5+,0}^2$ configuration.

^pReference 47. ^qReference 48. ^rReference 49.

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Table VIII.^a Experimental residual interaction energies for the $(lf_{7/2})^2_{7+,0}$ configuration.

Two-particle excited	Single partic.	le states ^C	E(lf _{7/2}) ^{2 b}
states	Assumed 1f7/2 neutron states	Assumed lf _{7/2} proton states	
²⁶ Al: 8.27	²⁵ Mg: 3.97 (5/2,7/2)- $(d,p) \ell = 3$	²⁵ Al: 3.72 7/2- ^c ,	d -3.44
³⁰ P: 7.03	²⁹ Si: 3.623 7/2- (d,p) l_=3	²⁹ P: 3.44 7/2- ^e , (³ He,d), (d,n) l	d _2.89
³⁴ c1: 5.2	³³ s: 2.937 7/2- (d,p) $l_{r}=3$	³³ Cl: (2.5) ^f	p -(3.11)
⁴² Sc: 0.60	⁴¹ Ca: 0.000 7/2- (d,p) l _n =3	⁴¹ Sc: 0.000 7/2- (t,d),(d,n) l _p =	-2.62
²⁸ A1: 9.80	²⁷ Mg: 3.575 (7/2,5/2) T=3/2	- ²⁷ Al: 6.48 7/2(5/ T=1/2 10.50 7/2- ^h T=3/2	2) ^{g,d} -2.96

^aAll the energies are in the units of MeV.

^bExperimental proton-neutron residual interaction energy.

^CAll the single particle state information is from Ref. 41 if not otherwise indicated.

${}^{d}_{\text{Reference}}$	51.	e Reference	52.	^f Reference	53.	g _{Reference}	54.
h Reference	55.		*				-

Two-particle		Single particle states			
states	Assu neut	Assumed lg _{0/2} Assumed neutron states proton s		d lg _{0/2} 1 statesn	
⁵⁴ Mn: 9.47	⁵³ Cr:	3.70 9/2+ ^c	⁵³ Mn:	(6.4) ^g 10.72) ^h	-(2.49)
⁵⁶ co: 8.92	⁵⁵ Fe:	3.80 9/2+ ^d	⁵⁵ co:	6.01 9/2+ ^{g,i} ,. (8.56) ^h	j -(2.54)
⁶⁰ Cu: 5.99	59 _{Ni:}	3.07 9/2+ ^e	⁵⁹ Cu:	2.99 9/2+ ^{g,k} 6.86 (9/2-) ^h	-2.42
62 _{Cu} : 4.75	⁶¹ Ni:	2.13 9/2+ ^e	61 _{Cu:}	2.71 9/2+ ^{g,k} 8.56 (9/2+) ^h	-2.34
64 _{Cu:} 4.57	63 _{Ni} : (centr	1.7 ^d roid)	63 _{Cu} :	2.51 9/2+ ^l 10.46) ^h	-(1.93)
⁶⁶ Ga: 2.99	65 _{Zn} :	1.04 9/2+ ^f	65 _{Ga} :	2.03 9/2+ ^g , ^m (7.10) ^h	-(2.22)
⁶⁸ Ga: 2.88	67 _{Zn} :	0.64 ^f	67 _{Ga} :	2.10 ^g (8.98) ^h	-(2.07)

Table IX.^a Experimental residual interaction energies for $(\lg_{9/2})_{9+,0}^2$ configuration.

^aAll the energies are in units of MeV.

^bExperimental proton-neutron residual interaction energy. ^cReference 58. ^dReference 59. ^eReference 29. ^fReferences 33,34. ^gReference 60. ^hReference 61. ⁱReference 62. ^jReference 63. ^kReference 56. ^lRef. 64. ^mRef. 65. ⁿOf the two excitation energies listed for each nucleus, the lower one is the analog $g_{9/2}$ state to the neutron $g_{9/2}$ state.

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b

Nucleus	ν ₁ (in F ⁻²)	Shell model o E _l	calculation ^a v_2 (in F ⁻²)	E ₂	Experimental $E(1d_{5/2})^2$
14 _N	0.326	-4.601	0.306	-4.291	-4.05
15 _N	0.318	-4.481	0.299	-4.177	-3.57
16 _N	0.311	-4.365	0.292	-4.068	-3.82
16 ₀	0.311	-4.365	0.292	-4.068	-3.44
170	0 . 304	-4.258	0.285	-3.968	-3.69
18 _F	0.298	-4.165	0.280	-3.880	-3.88
22 _{Na}	0.278	-3.847	0.261	-3.582	-3.47
26 _{Al}	0.262	-3.601	0.246	-3.349	-4.04

Table X. Comparison between theoretical and experimental proton-neutron residual interaction energies of $(1d_{5/2})_{5+}^2$ configuration.

^aThe choices of two sets of ν 's are discussed in the text.

All the enegies are in units of MeV.

^bFrom Table VII.

Nucleus	Shell model	calculation ^a	Experimental ^b
	v_1 (in F^{-2})	E	$E(lf_{7/2})^{2}$,0
26 _{A1}	0.276	-3.150	-3.44
28 _{Al}	0.269	-3.064	-(2.96)
30 _P	0.262	-2.980	-2.89
34 _{Cl}	0.251	-2.836	-(3.11)
⁴² Sc	0.234	-2.614	-2.62

Table XI. Comparison between theoretical and experimental proton-neutron residual interaction energies of $(lf_{7/2})_{7+,0}^2$ configuration.

^aThe choice of v's is discussed in the text. All the energies are in

units of MeV.

^bFrom Table VIII.

Nucleus	s	hell model	calculation ^a	P	Experimental ^b E($\lg_{0/2})^2$
	v (111 F)		v ₂ (111 F)	2	9/2 9+,0
54 _{Mn}	0.226	-2.198	0.244	-2.400	-(2.49)
56 _{Co}	0.224	-2.167	0.241	-2.366	-(2.54)
60 _{Cu}	0.219	-2.111	0.236	-2.303	-2.42
62 _{Cu}	0.216	-2.083	0.233	-2.275	-2.32
64 _{Cu}	0.214	-2.059	. 0.231	-2.247	-(1.93)
66 _{Ga}	0.212	-2.033	0.228	-2.221	-(2.22)
68 _{Ga}	0.209	-2.008	0.226	-2.195	-(2.07)

Table XII. Comparison between theoretical and experimental proton-neutron residual interaction energies of $(\lg_{9/2})_{9+,0}^2$ configuration.

^aThe choice of two sets of ν 's is discussed in the text. All the energies are in units of MeV.

^bFrom Table IX.

FIGURE CAPTIONS

- Fig. 1. Deuteron energy spectrum from the ${}^{13}C(\alpha,d){}^{15}N$ reaction at a scattering angle of 12° (lab).
- Fig. 2. Angular distributions of deuterons from the reaction ${}^{13}C(\alpha,d){}^{15}N$ at $E_{\alpha} = 40.1$ MeV.
- Fig. 3. Deuteron energy spectrum from the reaction ${}^{14}C(\alpha,d){}^{16}N$ at a scattering angle of 15.6° (lab).
- Fig. 4. Angular distributions of deuterons from the reaction ${}^{14}C(\alpha,d){}^{16}N$ at $E_{\alpha} = 46.0$ MeV.
- Fig. 5. Deuteron energy spectrum from the reaction ${}^{15}N(\alpha,d){}^{17}O$ at a scattering angle of 13.2° (lab).
- Fig. 6. Angular distributions of deuterons from the reaction ${}^{15}N(\alpha,d){}^{17}O$ at $E_{\alpha} = 45.4$ MeV.
- Fig. 7. Deuteron energy spectrum from the reaction ${}^{20}\text{Ne}(\alpha,d){}^{22}\text{Na}$ at a scattering angle of 11.2° (1ab).
- Fig. 8. Angular distributions of deuterons from the reaction ${}^{20}Ne(\alpha,d){}^{22}Na$ at $E_{\alpha} = 44.5$ MeV.
- Fig. 9. Deuteron energy spectrum from the reaction ${}^{52}Cr(\alpha,d){}^{54}Mn$ at a scattering angle of 20° (lab).
- Fig. 10. Deuteron energy spectrum from the reaction 54 Fe(α ,d) 56 Co at a scattering angle of 20° (lab).
- Fig. 11. Deuteron energy spectrum from the reaction 56 Fe(α ,d) 58 Co at a scattering angle of 20° (lab).

- Fig. 12. Deuteron energy spectrum from the reaction 58 Ni(α ,d) 60 Cu at a scattering angle of 35° (lab).
- Fig. 13. Deuteron energy spectrum from the reaction ${}^{60}Ni(\alpha,d){}^{62}Cu$ at a scattering angle of 20° (lab).
- Fig. 14. Deuteron energy spectrum from the reaction 62 Ni(α ,d) 64 Cu at a scattering angle of 20° (lab).
- Fig. 15. Deuteron energy spectrum from the reaction 64 Zn(α ,d) 66 Ga at a scattering angle of 20° (lab).
- Fig. 16. Deuteron energy spectrum from the reaction 66 Zn(α ,d) 68 Ga at a scattering angle of 20° (lab).
- Fig. 17. Deuteron energy spectrum from the reaction 68 Zn(α ,d) 70 Ga at a scattering angle of 20° (lab).
- Fig. 18. Angular distributions of deuterons from (α,d) reactions to states of $(ld_{5/2})_{5+,0}^2$ configuration.
- Fig. 19. Relationship between the mass number A of the product nucleus and the Q-value of formation of levels with $(ld_{5/2})_{5+,0}^2$, $(lf_{7/2})_{7+,0}^2$,
 - $(ld_{5/2}, lf_{7/2})_{6-,0}$, and [probably] $(lg_{9/2})_{9+,0}^2$ configurations strongly populated by the (α, d) reaction.
- Fig. 20. Comparison between the experimental excitation energies of the $(1d_{5/2})_{5+,0}^2$ levels and the theoretical values using the level information from neighboring nuclides.
- Fig. 21. Comparison between the experimental excitation energies of the $(1d_{5/2})_{5+,0}^2$ levels and the theoretical values using Talmi's method of shell model calculation.



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Fig. 2



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Fig. 5



Fig. 6



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Fig. 7



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Fig. 12

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 $\sum_{i=1}^{n}$

Fig. 14

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