

# High Strain Rate Mechanics of Polymers: A Review

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**Abstract** The mechanical properties of polymers are becoming increasingly important as they are used in structural applications, both on their own and as matrix materials for composites. It has long been known that these mechanical properties are dependent on strain rate, temperature, and pressure. In this paper, the methods for dynamic loading of polymers will be briefly reviewed. The high strain rate mechanical properties of several classes of polymers, i.e. glassy and rubbery amorphous polymers and semi-crystalline polymers will be reviewed. Additionally, time–temperature superposition for rate dependent large strain properties and pressure dependence in polymers will be discussed. Constitutive modeling and shock properties of polymers will not be discussed in this review.

**Keywords** Polymer · High strain rate · Split Hopkinson pressure bar · Taylor test

## Introduction

An understanding of the mechanical properties of polymers over a range of strain rates, temperatures, and pressures is required in fields such as military applications, automotive, aerospace, and medical devices. As well as being governed by the composition and microstructure of the materials, these properties are highly dependent on a number of

external factors such as pressure, temperature, and frequency (strain rate).

Some of the first papers on dynamic loading studied the material response of polymers including Kolsky's 1949 paper [1] and Davies and Hunter [2]. Over the past 40 years, the mechanical response (principally the relationship between stress and strain) of a number of polymers has been characterized at strain rates between  $10^{-4}$  and  $10^5$  s<sup>-1</sup>, see for example [3–5]. Most polymers exhibit time dependent mechanical behavior, as evidenced by rate dependent elastic moduli, yield strength, and post-yield behavior. Over a range of temperatures and strain rates, the mechanical response of a polymer may change from rubbery to ductile plastic to brittle [6–12]. Additionally, many rubbery polymers can exhibit large, recoverable deformation, and, for hyperelastic materials, experimental measurements at large strain may be required to characterize the strain hardening [13].

Time–temperature superposition has been used to address the response of polymers over a range of strain rates by comparing the temperature and strain rate dependencies of yield stress. This is an extension of the well-known time–temperature superposition that is often applied to modulus data [14]. Although, the time–temperature superposition of yield stress was initially studied in the 1970s [15–18], it was not applied again in this context until research by Siviour et al. ([19], in which a linear mapping between strain rate and temperature was used to show that rate dependence in many glassy amorphous polymers was affected by lower order  $\beta$  transitions, which causes increased strength and stiffness. Alternatively, the increased strength in rubbery amorphous polymers is accounted for by the change in molecular mobility during the glass transition, or  $\alpha$ -transition. The key feature is that a transition, which is typically observed below room temperature, is observed at room temperature for high strain

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rates, as the transition temperature increases with increasing strain rate [5, 15, 16, 19, 20]

The effect of confining pressure has not been well studied in polymers, and there are limited reports in the literature [21, 22]. Quasi-static experiments have shown that increased hydrostatic confining pressure results in linearly-dependent, increased yield strength and decreased strain to failure in tension [22]. This pressure dependence manifests itself in differences between the tensile and compressive yield stresses, which can aid in the determination of pressure dependence without a requirement for the complex loading apparatus required for applying hydrostatic pressure [18, 20, 23].

Constitutive models of polymers typically depend on the structure of the polymer (amorphous or semi-crystalline) as well as whether the polymer is glassy over the temperature range of interest. The parameters for these constitutive models typically require a considerable amount of experimental data to determine the model parameters. Although these models require significant effort to parameterize and, once parameterized, are specific to the particular material that was characterized, they are very useful for utilizing polymers in engineering simulations, such as ABAQUS.

The first model to describe the rate dependent yield in glassy polymers was proposed by [24]. This theory allows for multiple rate activated processes, which are related to specific degrees of freedom of the polymer chains, to control the yield [20]. The molecular motions of the polymer chains become restricted at particular temperatures/strain rates, the effects are seen in increased yield strength.

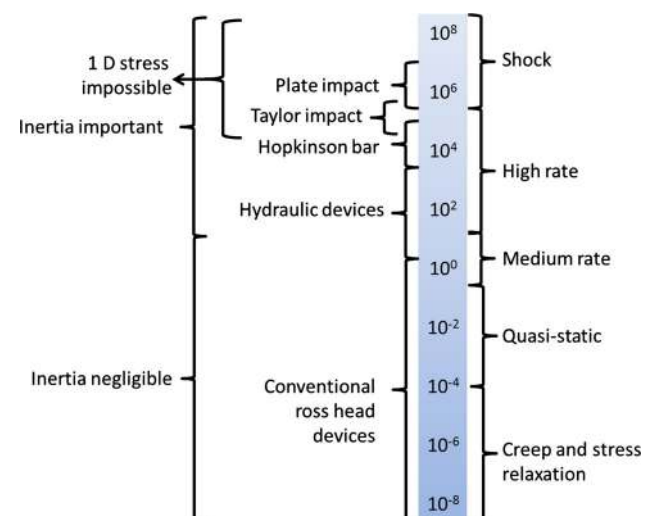
The first 1D model to describe polymer behavior based on the Ree and Eyring [24] theory was proposed by Haward and Thackray [25]. This model employed a Hookean spring and Eyring dashpot to capture the intramolecular resistance to chain segment rotation, and the Langevin spring represents the entropic resistance to chain alignment. The nonlinear dashpot(s) are responsible for the rate-dependent yield in the material [26]. Multiple dashpots may be used to model multiple molecular processes that affect yield, e.g.  $\alpha$ - and  $\beta$ -transitions. The Langevin spring accounts for the strain hardening post-yield due to the alignment of the macromolecular network built of entangled polymer molecules [26]. A large family of 3D pressure, temperature, and strain rate dependent models [27–29] has developed based on the Ree-Eyring [24] theory. The most recent of these model developments by Mulliken and Boyce [20] provides a three-dimensional temperature, pressure, and rate dependent finite-strain model capable of capturing both the  $\alpha$ - and  $\beta$ -transitions. These empirical models describe the behavior of glassy polymers well. However, since they are empirical, they require a large data set to adequately calibrate all of the model parameters,

which can make them unwieldy for describing many materials. Another model which directly links the constitutive behavior of polymers to the frequency and temperature dependence, thereby implicitly including the effects of lower order transitions on the rate dependence is the Porter-Gould model [30–34]. This model also has the advantage of being able to predict a number of key polymer properties from knowledge of the polymer chain composition without the need for extensive calibration data.

This review includes a brief discussion of experimental techniques to characterize the mechanical response of polymers. For additional detail, on relevant experimental techniques, the reader is referred to the paper by Chen [35] in this issue. The primary focus of this paper is the properties of different classes of polymers, as well as properties of polymers across classes, i.e. time–temperature superposition and pressure dependence. Constitutive modeling and shock properties of polymers is beyond the scope of this review.

## Experimental Techniques for Polymers

Over the past 100 years, a wide range of experimental apparatus has been developed for characterizing the response of materials to deformation at different strain rates, as seen in Fig. 1. Many of these techniques have been specially adapted for polymer characterization. The change between experimental techniques to capture different rates can cause doubts as to whether the observed responses are really an intrinsic material behavior or an artifact of the experimental testing technique, and it is challenging,



**Fig. 1** Approximate division of strain rate regimes (in s<sup>-1</sup>) and the experiments used to investigate these regimes. Further information on the various techniques can be found in Field et al. [36]

experimentally, to overlap the range of rates at which the techniques work. A brief overview of experimental techniques relevant to polymer characterization is presented in this section. For a more detailed review of high rate experimental techniques for low impedance materials, the reader is referred to the paper by Chen [35] in this issue, and for a general overview of experimental methods, the reader is referred to Field et al. [36].

### Quasi-static Experiments

For quasi-static experiments, conventional servo-hydraulic and screw-driven machines are typically used. Such testing machines have been available commercially since the late nineteenth Century [37, 38] and have gone through several evolutions, moving from purely mechanical machines to sophisticated electromechanical and servo-hydraulic systems with advanced electronic control.

Dynamic Mechanical Analysis (DMA) machines apply oscillating displacements with systematic variations of temperature and/or frequency (up to approximately 100 Hz). By measuring force and displacement as functions of time, with particular reference to the phase of these quantities, it is possible to calculate the complex modulus and loss tangent of a polymeric material. Commonly used configurations include single and dual cantilever, tension, and compression. DMA results provide valuable insight into the temperature and frequency dependence of features such as the  $\alpha$ - and  $\beta$ -transitions in the material. For comparison to other mechanical properties, the frequencies from DMA experiments can be converted to strain rates using the following approximation, which is commonly found in the literature [20]:

$$\dot{\varepsilon} \approx \frac{\Delta\varepsilon}{\Delta t} = \frac{\varepsilon_0}{1/4f} = 4f\varepsilon_0 \quad (1)$$

where  $\varepsilon_0$  is the strain amplitude reported by the DMA, and  $f$  is the oscillation frequency. It should be noted, however, that these strain rates are approximations, giving the mean rate seen in a tension or compression specimen. For bending or cantilever arrangements the strain rates in the specimen vary considerably through the specimen volume. However, as will be described later, many researchers have had success relating DMA measurements to those obtained in other testing apparatus.

### Intermediate Strain Rates

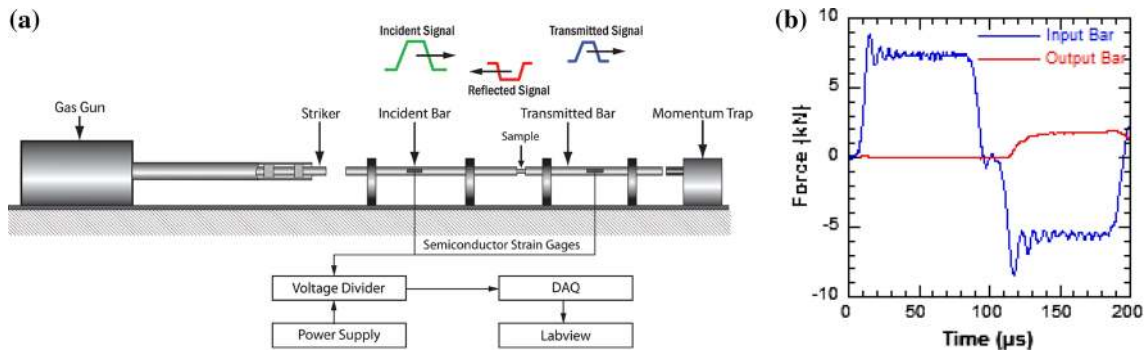
Intermediate strain rate experiments (between circa 1 and 500 s<sup>-1</sup>) pose a significant challenge for all material characterization programs. The frequency at which experimental data are required is similar to the natural frequency

of both the loading apparatus (e.g. piston) and the instrumentation (e.g. load cell). In addition, it is necessary to overcome the effects of the inertia of the apparatus, so that high speed deformations can be applied after a very short period of acceleration. Hydraulic machines are often used; however, systems based on dropping weights [39–48], fly wheel systems [49, 50], expanding ring [51], cam plastometer [52], very long Hopkinson bars [53], or the ‘wedge bar’ [54] have also been applied successfully. Accurate experiments in this strain rate regime are key because molecular mobility transitions often become activated between 1 and 1000 s<sup>-1</sup>.

### Dynamic Loading: Split Hopkinson Pressure Bar

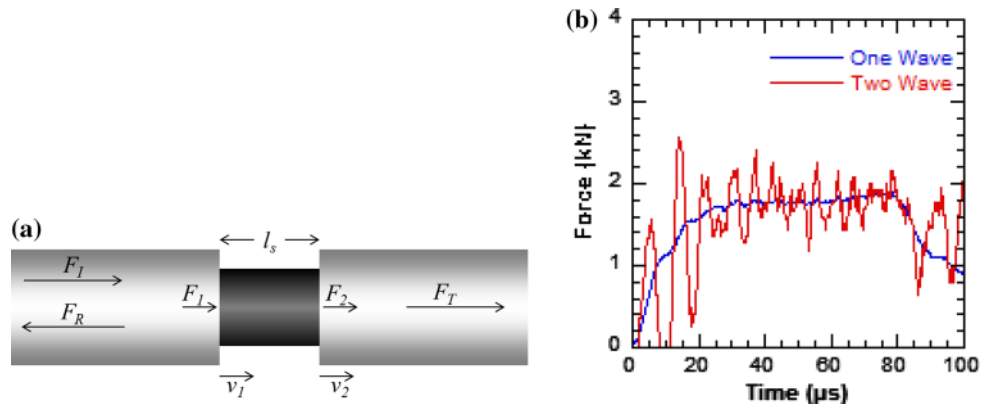
Although a number of techniques have been developed to measure material properties at high strain rates, the split-Hopkinson pressure bar [55–58], or Kolsky bar, has now become ubiquitous for materials characterization between 500 and 10<sup>4</sup> s<sup>-1</sup>, or even higher if miniaturized systems are used [59, 60]. A schematic of the split Hopkinson pressure bar system at the Air Force Research Laboratory, Eglin AFB, FL is shown in Fig. 2a. The data acquisition systems tend to be specific to the SHPB laboratory. However, the bar system itself has common elements across all laboratories.

During an SHPB test, the specimen is sandwiched between two slender rods, known as the input and output bars, or incident and transmitted bars, which are instrumented with strain gauges, or, more recently photon Doppler velocimetry (PDV) [61]. A loading system, typically a gas gun, is used to propel a shorter third rod, or striker, into the incident bar. This generates a stress wave, shown as the incident signal in Fig. 2a, which propagates down the bar to the specimen. At the bar-specimen interface, the change in impedance (density times sound speed) between the bar and the specimen causes some of the wave to be reflected back down the input bar and some to be transmitted to the output bar, forming the reflected and transmitted signals in Fig. 2a, respectively. Typically, all three waves are measured using strain gauges mounted on the incident and transmitted bars; although quartz gauges [62–64] and interferometric techniques [59, 65] have been used. Representative voltage–time curves are shown in Fig. 2b, where the compressive pulse is shown as positive. It is common practice to mount two strain gauges at each location which are diametrically opposed to each other, which will result in cancelling out bending waves and, subsequently, measurement of a purely compressive pulse. Using the three waves, and a simple 1D wave analysis, the velocities and forces at the two bar specimen interfaces, Fig. 3a, can be calculated from the following equations:



**Fig. 2** **a** Schematic of Split Hopkinson Pressure Bar at the Air Force Research Laboratory, Eglin AFB, FL and **b** representative voltage–time curves for an SHPB experiment

**Fig. 3** **a** Forces and displacements at the bar–specimen interfaces in a split Hopkinson pressure bar and **b** comparison of forces calculated from one-wave and two-wave analyses



$$F_1 = F_I + F_R \tag{2}$$

$$F_2 = F_T \tag{3}$$

$$v_1 = \frac{F_I - F_R}{\rho c A_b} \tag{4}$$

$$v_2 = \frac{F_T}{\rho c A_b} \tag{5}$$

where  $F_I$ ,  $F_R$ , and  $F_T$  are the forces associated with the incident, reflected, and transmitted waves,  $\rho$  is the density of the bar,  $A_b$  is the area of the bars, and  $c$  is the wavespeed of the bars defined as:

$$c = \sqrt{\frac{E}{\rho}} \tag{6}$$

where  $E$  is the Young’s modulus of the bar. Typically, the same material is used for both of the bars, but it is simple to modify Eqs. (5) and (6) if different bar materials are used.

It is usual to assume that the specimen is in stress equilibrium during deformation, which occurs after a number of wave oscillations in the specimen, as shown in Fig. 3(b). If this is the case, then the force supported by the specimen is equal to both  $F_1$  and  $F_2$  and the stress–strain relationship in the specimen can be calculated using the forces and bar velocities. It is necessary

to ensure that polymeric, or other low wave speed specimens, are in equilibrium [66]. This is typically done by comparing the two forces. For polymeric materials, considerable strains can develop before equilibrium is achieved as the stress wave oscillates in the specimen [67, 68], and specimens should be designed to allow this to happen before material properties are measured from stress–strain curves.

The one wave stress can be calculated from the forces by:

$$\sigma(t) = \frac{F_T(t)}{A_s(t)} \tag{7}$$

where  $A_s$  is the area of the specimen. The engineering stress can be calculated using the constant initial area, and the true stress can be calculated using the area as a function of time. The two wave stress can be calculated from the forces by:

$$\sigma(t) = \frac{F_I(t) + F_R(t)}{A_s(t)} \tag{8}$$

The specimen equilibrium can be verified by comparing the one wave and two wave stresses. When the specimen is in equilibrium, the two wave stress will oscillate around the one wave stress.

The strain rate in the sample can be determined using all three forces:

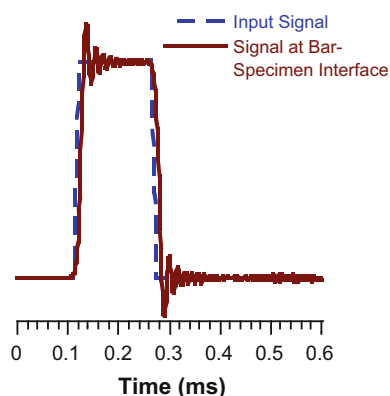
$$\dot{\varepsilon}(t) = \frac{F_I(t) - F_R(t) - F_T(R)}{\rho c A_b} \quad (9)$$

which can be numerically integrated to determine the strain as function of time.

The propagation of the stress wave in the bar can be dispersive when the wavelength is on the same order of magnitude as the bar diameter [69, 70]. Dispersion of the wave will result in an increased rise time and oscillations about the peak stress, as seen in Fig. 1. There are methods for correcting for the dispersion, one of which has been presented by Gorham [71]. In these methods, the incident and transmitted signals are translated to frequency space using a Fast Fourier Transform (FFT). The signals are then corrected by changing the phase of each component by a given amount that is a function of frequency. The corrected signals are then converted back to real space using an inverse FFT (Fig. 4).

The low impedance of polymeric samples, which can result in a very small transmitted signal, presents additional considerations during testing. There are several approaches to mitigating the effect of the low impedance: increased sensitivity or additional gauges, changing the cross-sectional area of the bars or specimens, pulse-shaping and changing the pressure bar material [72]. Johnson et al. [72] carried out an experimental comparison with polyurea of these different techniques and found that they all had their own advantages and disadvantages, which must be considered when designing a particular characterization experiment. An extensive review of testing techniques for soft materials, e.g. elastomers, biological tissues, and foams, can be found in Chen and Song [73].

In traditional SHPB systems, foil strain gauges, which have a gauge factor  $\sim 2$ , are mounted on the surface of the



**Fig. 4** Dispersion of a stress pulse produced by traveling 1.5 m in a 25.4 mm diameter steel bar. Signal at bar-specimen interface has been shifted in time to overlay the input signal for comparison

incident and transmitted bars. For polymeric materials, these foil gauges can result in transmitted signals that cannot be distinguished from the noise. Increased sensitivity semiconductor strain gauges, which have a gauge factor  $\sim 140$  can be used to enable accurate measurement of small transmitted signals [74]. Additionally, piezoelectric gauges, such as x-cut quartz or lead zirconium titanate (PZT), can be placed in the experiment to provide enhanced sensitivity or to directly measure input and output forces [62–64, 75]. Early experiments with quartz gauges placed them directly in contact with the specimen [63]. However, polymeric materials, with large diameter increases during testing, will damage the quartz gauges. Chen et al. [62] embedded an x-cut quartz gauge in a hollow aluminum transmitter bar, since the quartz gauge is more sensitive than the surface mounted strain gauges. They found that the stress measurements using this modified system were three times more sensitive than a traditional steel bar. Kendall et al. [64] utilized PZT crystals mounted on either side of the specimen near the ends of the incident and transmitted bars and were able to measure loads of less than 10 N on a soft, rubbery polymer.

A second approach to addressing the low impedance of polymers is to change the cross-sectional area of the specimen or the bars. Increasing the cross-sectional area of the specimens to obtain a larger signal poses difficulties since it would require larger bars, which may be prohibited by the available laboratory facilities. Chen et al. [76] pioneered the use of hollow, aluminum transmitted bars. Using aluminum reduces the impedance of the bar material itself, and the hollow bar provides a reduced cross-sectional area. Both of these modifications resulted in increased transmitted signal, and the ability to reduce the data.

A third approach, is to change the bar material to either a low impedance metal, e.g. titanium, magnesium alloy or aluminum, or a polymer, e.g. polymethylmethacrylate (PMMA), PC, or nylon [77–88]. Low impedance metallic bars do not require any changes to the experimental apparatus or data reduction. Use of viscoelastic, polymeric bars requires more complex data reduction correcting for dispersion and attenuation occurring in the bar. The polymers used for the bars must be well characterized at high rates in order to determine the specimen properties from the signals measured on the bars [79].

Specimens for SHPB experiments are typically right circular cylinders. When designing specimens for high rate experiments, two key factors must be taken into account:

- (1) The specimens must be short enough to allow stress equilibrium to occur in a reasonable time scale [89]. A reasonable rule of thumb is that three wave reverberations are required along the specimen



length. For glassy polymers, this limits the specimen length to about 5 mm, and less for rubbery polymers.

- (2) Specimen inertia must be considered [71, 90]. When a specimen is loaded, some force is required to overcome the intrinsic material strength, while some is required to accelerate the material to the high deformation speeds, in both the axial and radial directions. Gorham [91] calculated that the pressure measured on the output bar is given by

$$P_2 = \sigma_y - \rho \left( \frac{r^2}{8} - \frac{h^2}{6} \right) \ddot{\epsilon} + \rho \left( \frac{r^2}{16} - \frac{h^2}{6} \right) \dot{\epsilon}^2 - \frac{\rho h \dot{v}}{2} \quad (10)$$

where  $\sigma_y$  is the intrinsic material strength,  $r$  and  $h$  are the specimen radius and height, respectively, and  $\dot{v}$  is the velocity of the output bar. This equation, which has been derived for an incompressible specimen, can be used as a guide to specimen design, ensuring that the inertial contribution is significantly smaller than the actual material strength.

Once the experimental configuration has been determined, control of the incident pulse can aid in ensuring that specimen deformation is occurring at a constant rate [73]. The incident pulse can be controlled through the use of pulse shapers, which are thin layers of metals or plastic placed on the impact surface of the incident bar. The pulse shaper should be chosen to ensure that the reflected signal has a plateau, which will ensure constant strain-rate deformation in the specimen [73]. Additionally, pulse shapers will reduce the oscillations due to wave dispersion in the bar.

Lubrication is an important consideration in all compression experiments, but especially in high rate testing of polymers, where low sound speeds mean that short specimens are required, and the low strengths often encourage the use of specimens with large diameters. Hence, the aspect ratio of the specimen ( $h/r$ ) is small, which can lead to significant frictional effects. If there is excessive friction, a barreling effect is observed, causing stress inhomogeneity and an increase in the measured specimen strength: such tests are not valid for the measurement of bulk properties of a material. Studies of different lubricants [47, 92, 93] have shown that paraffin wax, petroleum jelly, and molybdenum disulfide grease provide adequate lubrication for high strain rate experiments.

The change from broadly isothermal to broadly adiabatic conditions as the strain rate increases is an important feature of high rate deformation, and the associate temperature rise as mechanical work is converted to heat during plastic deformation must be considered alongside the dependence on initial temperature when considering material response. Although the strain rate at which an experiment may be considered adiabatic depends on both material properties and specimen size, for typical tests on

polymers it may be of the order  $0.01\text{--}1 \text{ s}^{-1}$  [94]. Important studies involving the temperature rise in specimens during high rate deformation have been conducted by a number of authors [95–101]. A notable achievement was by Chou et al. [95], who showed that the temperature rise in specimens increases significantly after yield. Furthermore, Arruda et al. [96] presented visible increases in strain softening with increases in strain rate, coupled with corresponding temperature measurements using infrared techniques. Additionally, Garg et al. [97] used infrared techniques to measure the temperature rise of PC undergoing high rate deformation. Good agreement was observed between the experimentally measured temperature rise and the “theoretical” rise obtained by assuming that 100 % of the mechanical work is converted to heat and adiabatic conditions prevail. Hillmansen et al. [98, 99] studied plastic work being converted to heat by studying high density polyethylene (HDPE) and found, similarly, that the plastic work at large strains was approximately 100 % converted to heat.

### Dynamic Loading: Taylor Tests and Dynamic Tensile Extrusion

The above testing methods are primarily used to characterize materials and develop parameters for constitutive models. Taylor testing and Dynamic Tensile Extrusion are primarily used to validate models as they involve complex loading of the material. Taylor testing was developed in 1946 [102–105], primarily to measure the dynamic yield strength of metals. However, even these early tests were used to investigate the underlying deformation mechanism through microstructure [105]. In the original test, a slender rod of material is impacted at high speed into a rigid, semi-infinite anvil. The specimen is recovered, and the dynamic yield strength is assessed using the initial and final lengths and the length of the plastic deformation zone [103]. However, this purely post-mortem analysis is not sufficient for polymers, due to the viscoelastic recovery of the materials. With the advent of high speed cameras, the ability to measure the polymer deformation in situ became possible. Additionally, experimental studies and theoretical analysis by Hutchings [106, 107] brought together a new analysis appropriate for these materials. The complex loading in compression of the Taylor test, where stress, strain rate, and final strain vary within the specimen makes it an ideal test for validating constitutive models, where the complex loading is thought to provide a more robust test of the model [36]. In polymers, the test has been used to understand the behavior of the materials under complex loading for modeling efforts [108–113] and to elucidate phase transitions in the polymeric materials [12, 114].

More recently, Dynamic-Tensile-Extrusion (Dyn-Ten-Ext) has been developed to provide model validation in dynamic tension [115, 116]. In this test, a sphere of material is fired through a conical extrusion die. Initially, the sphere is not affected by the die; however, the trailing side decelerates creating a ligament between the two portions of the sphere, which is pulled in high rate tension to high strains and, ultimately, failure. High speed photography is used to capture the deformation and compare with results from computer models. Several polymers have been studied showing that both the deformation and failure behavior can be directly observed and the internal history can be understood through integration with finite element simulations [117–122].

## Dynamic Response of Polymers

The dynamic response of polymers dates to the first paper using a split bar configuration for high rate testing [1], and interest in the dynamic response of these materials has continued to the present. Walley and Field [5] published an extensive set of data characterizing the compressive stress–strain response over a range of strain rates for a broad range of polymers. They observed a range of material responses depending on the polymer structure. In this section, the dependence of mechanical response on the polymer structure will be discussed for different classes of polymers, namely glassy amorphous polymers and semi-crystalline polymers.

### Glassy Amorphous Polymers

There are several glassy polymers that have been extensively studied at high strain rate in the literature, including polymethylmethacrylate (PMMA) [16, 95, 100, 123–132], polycarbonate (PC) [15, 18–20, 100, 110, 124, 126, 127, 133–136], polyvinylchloride (PVC) [137, 138] and varying classes of epoxy [23, 74, 139–141]. The large number of studies on a “single” material indicates that it is critical to understand the pedigree of the polymer being tested, including processing history and storage.

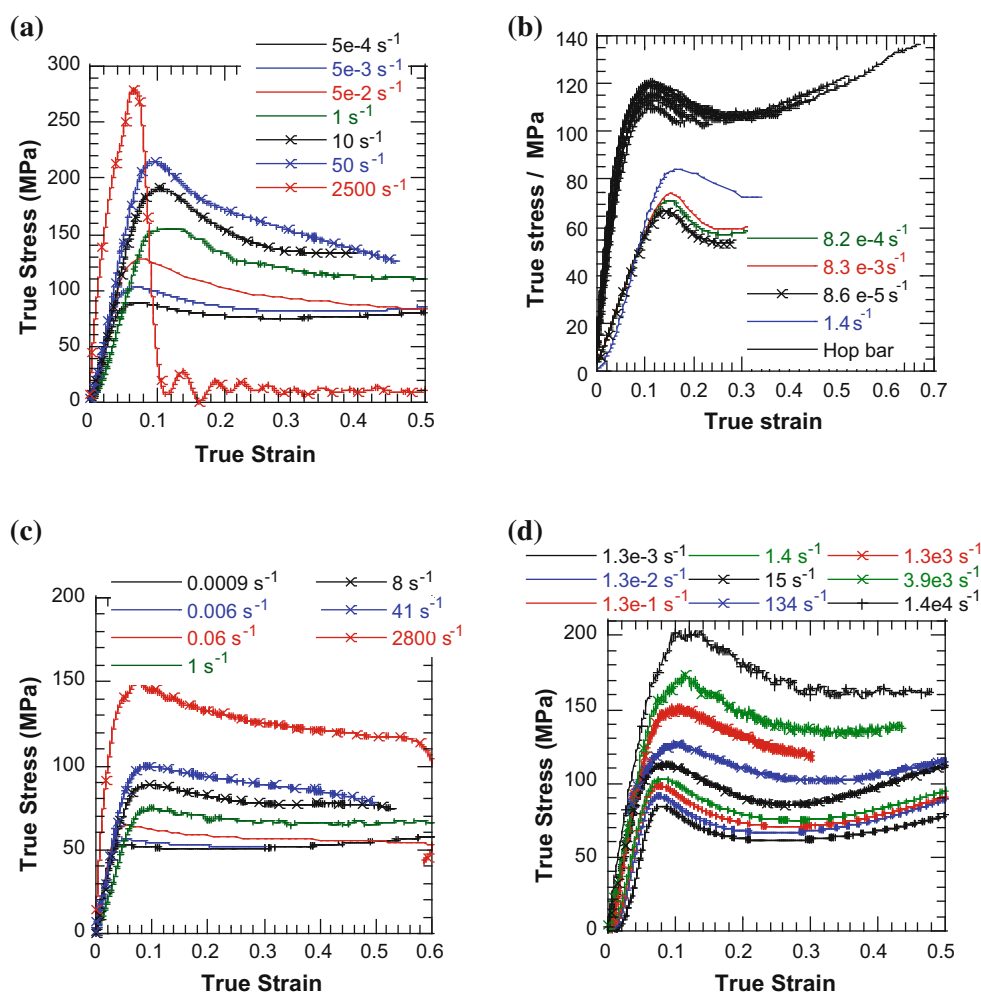
Representative compressive stress–strain curves for these materials across a range of strain rates are shown in Fig. 5, which show many similarities across the class of materials. Typically, the stress–strain curve has an initial viscoelastic behavior which becomes increasingly non-linear as strain increases until it reaches a peak stress. The peak stress is followed by strain softening and then strain hardening. Hasan and Boyce [131] describe the stress–strain response in terms of the evolution of shear transformation sites, where the initial material has a number of sites with a probability of transformation within the time-frame of the experiment. As stress is applied to the material

(viscoelastic rise), transformation sites with high local free volume and, subsequently, low activation energy begin to yield and flow, and the corresponding transformation strain energy is stored in the non-transformed “matrix,” which creates a back stress that initially inhibits further transformation. With increasing stress, transformation sites with higher activation energy can be accessed resulting in increasingly non-linear stress–strain response. The surrounding material stores the transformation strain energy, which exerts a back stress on the transformed material. As the applied stress increases, transformation sites with higher activation energy are accessed and the surrounding material can no longer absorb the transformation strain energy, which results in the creation of new defects, i.e. sites with high local free volume. These new sites result in strain softening in the material, where there are sites available to transform with lower activation energy. At this point, the material is in a steady-state condition where the mobile regions are prolific through the material allowing for indefinite plastic flow [131]. At higher strains, resistance to polymer chain alignment causes strain hardening in the material [96]. However, with increasing strain rate, this strain hardening effect is balanced by adiabatic heating in the material, which ultimately dominates over the hardening from resistance to polymer chain alignment [94, 96, 124, 130, 137, 142]. Finally, in the case of PMMA (Fig. 5a), at high strain rates the material fails catastrophically due to the inability to access particular molecular side chain motions at these fast rates.

The strain rate dependence of these polymers becomes more obvious when the peak stress is plotted versus log strain rate as shown in Fig. 6 for the same range of semi-crystalline polymers presented in Fig. 5. The most interesting observation in these materials is the increased strain rate sensitivity at higher strain rates, which has been observed in a wide variety of polymer materials, in addition to those presented. However, caution should be taken when interpreting these results for three reasons. A similar increase in strain rate sensitivity has been observed in metals, e.g. copper [143–145]. Secondly, the strain rates where the increased sensitivity occurs are also those where inertial effects become relevant, i.e. if the specimen is too large, the stress induced by specimen inertia can become significant compared to the polymer strength [146]. Finally, the transition in behavior occurs over the same regime where test equipment changes from screw-driven or hydraulic load frames to split Hopkinson pressure bars.

Careful studies like those conducted on PMMA [128], shown as the blue data points and fitted line in Fig. 6a, and epoxy [74] where experiments are conducted at every decade of strain rate using novel hydraulic loading devices capable of testing the intermediate rate regime reduced the uncertainty associated with the third reason described

**Fig. 5** Representative compressive stress–strain curves for **a** PMMA [128], **b** PC [19], **c** PVC [138], and **d** epoxy [74] across a range of strain rates



above. Typically, the increase in strain rate sensitivity in glassy polymers is attributed to activation of particular molecular mobility, often due to side chain motion or ring flips called the  $\beta$ -transition.

There is considerable scatter between the data from different studies, as seen in Fig. 6a, again emphasizing that the polymer pedigree is important in determining the mechanical response. For PMMA, which is used as a reference and window material in shock experiments, understanding the cause of these differences is critical. Consideration of polymer processing, particularly annealing as-received or aged materials, should be done prior to experimentation.

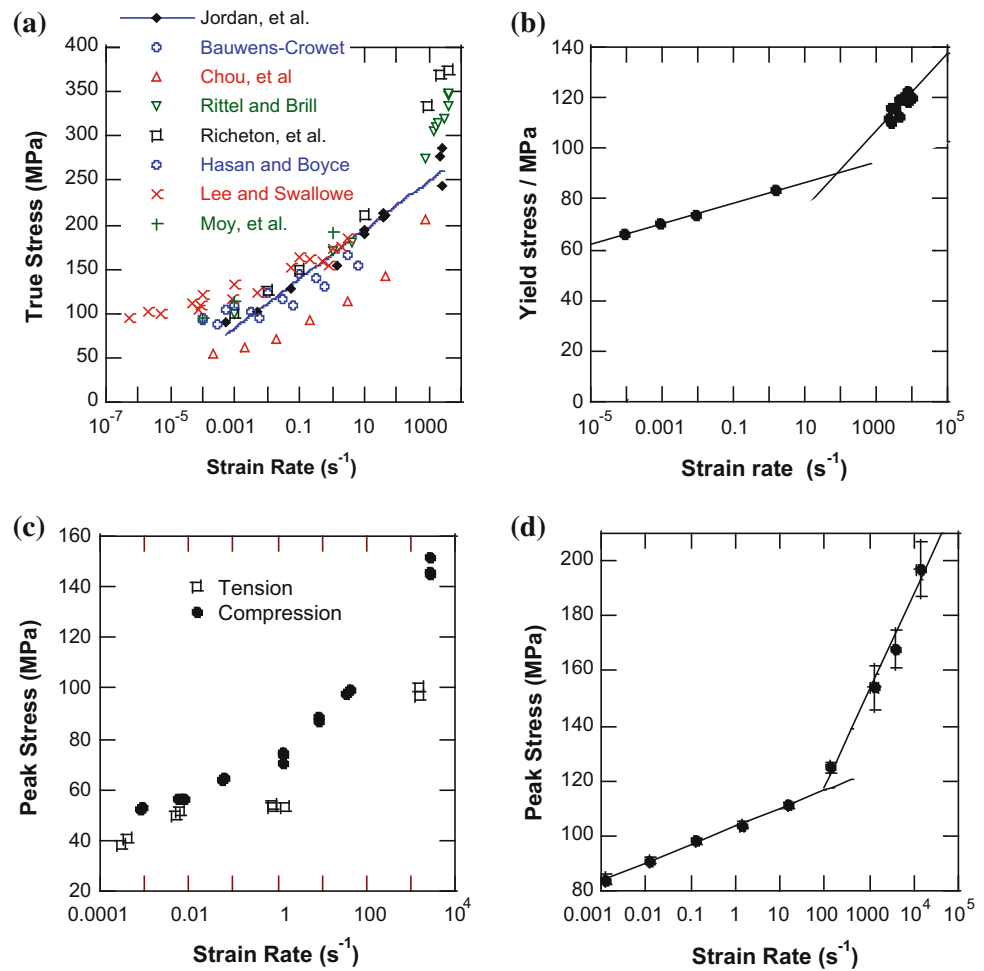
### Rubbery Amorphous Polymers

Characterization of elastomers at high rates of strain presents a number of challenges associated with their relatively low mechanical strength; the most important of these are the low sound speed, which results in the duration of oscillation of stress waves in the specimen being a

significant fraction of the duration of the experiment, the increased effect of lateral inertia [90, 147], and the low intrinsic strength leading to poor signal to noise ratios. Furthermore, many elastomers must be deformed to large strains to fully characterize the mechanical response, especially for hyperelastic materials. However, rubbers were some of the first materials to be characterized in split Hopkinson bar experiments [1, 2], and more recently a number of authors have proposed techniques to address these difficulties through modifications to the Hopkinson bar or other similar systems [57, 66]. These include pulse shaping [62], low impedance Hopkinson bar materials to increase the transmitted force [76, 77, 81, 82, 148] or use of more sensitive force gauges to directly measure the force at the specimen bar interface [62–64]. Longer Hopkinson bars may be used to increase the duration of the experiment [53], as can direct impact systems [149], in addition, if stress gauges are combined with optical measurements of specimen deformation, the experiment duration is no longer limited by wave overlapping in the bars and longer durations can be achieved [150]. The challenges associated



**Fig. 6** Peak stress vs. strain rate for **a** PMMA [16, 95, 125, 128–132], **b** PC [19], **c** PVC [138], and **d** epoxy [74] across a range of strain rates



with these elastomers are similar to those experienced when characterizing many biological materials, giving further motivation to the development of suitable experimental techniques.

Materials which have been well-studied in the literature are silicone elastomers [13, 66, 151], plasticized PVC [152, 153] and polyureas [39, 40, 72, 154–159] and polyurethanes [160–162]. The rate dependence of these materials depends strongly on the glass transition, and in particular whether this transition affects the room temperature response at strain rates of interest. At lower rates, or higher temperatures, the response is typically rubbery, may be described by a suitable material model and is a weak function of both rate and temperature; as the rate increases the apparent stiffness of the rubber may increase owing to the viscoelastic nature of the response, or, if the glass transition takes effect, the material may exhibit ‘leathery’ [155] then glassy behavior.

One of the key limitations of these more established techniques for high rate deformation is that they are not suitable for characterizing material moduli. However, for

specimens with low speeds of sound, the wide availability of high speed cameras gives the opportunity to calculate this property from measurements of stress waves propagating in a specimen, either using the wavespeed to infer material properties, or using accelerations as a virtual load cell, combined with direct calculations of strain to calculate the material response [163–169].

**Semi-crystalline Polymers**

Semi-crystalline polymers like polypropylene (PP) [4, 5, 92, 95, 170, 171], polytetrafluoroethylene (PTFE) [5, 6, 8–10, 172–177], and various classes of polyethylene [108, 136, 178]—low density polyethylene (LDPE), high density polyethylene (HDPE), ultra high molecular weight polyethylene (UHMWPE), and crosslinked polyethylene (PEX)—are widely used in applications that require understanding of the high strain rate response. These materials bring additional complexity over the glassy polymers due to the dependence of properties on the molecular conformation. The percent crystallinity and

molecular conformation are highly dependent on the processing history.

By far, the most studied polymer in this class of materials is PTFE [5, 6, 8–10, 172–177], which can be thought of as a two-phase structure, with a “rigid” crystalline phase in a matrix of the “softer” amorphous phase. The behavior of PTFE strongly depends on the crystallinity, i.e. increasing the percent crystallinity will increase the strength, similar to particulate composites. PTFE has crystalline phase changes at 19 °C from Phase II to Phase IV and at 30 °C from Phase IV to Phase I at ambient pressure [176]. Although Phases II and IV are strongly crystalline, Phase I is sometimes described as mesophase [179]. The crystalline phase has been shown to dramatically effect whether fracture is brittle (Phase II) or ductile (Phases I and IV) [176]. Additionally, the amorphous PTFE has three relaxations,  $\gamma$  and  $\alpha$ , which are similar to glass transitions and  $\beta$ , which encompasses the crystalline phase transitions between Phases II, IV, and I [6, 180].

PTFE has been shown to have both strain rate and temperature dependence as expected in polymers. An example of the strain rate dependence is shown in Fig. 7a [174] showing a nonlinear viscoelastic region to a distributed yield followed by unrecoverable deformation, viscoplastic flow, and stiffening at large strains [181]. Additionally, the true stress at 15 % strain versus strain rate for a variety of PTFE materials is shown in Fig. 7b. It can be seen that all the materials have a bilinear dependence on strain rate, but there are measureable differences between the individual material types. This is due to the different processing conditions, which result in different fractions of crystallinity, as well as the differing types of PTFE.

Another well studied semi-crystalline polymer is polyethylene, which brings the added complication of varying molecular weights and conformations. Brown et al. [108, 178] have investigated polyethylene with a variety of

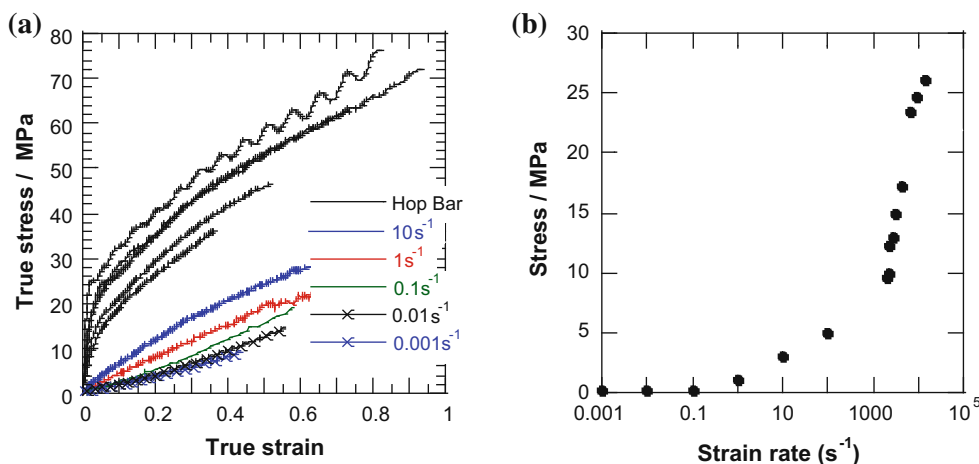
conformations—HDPE, UHMWPE, and PEX. They found similarities between UHMWPE and PEX with both showing significant post-yield strain hardening, and HDPE exhibiting higher yield stress and nearly perfectly plastic flow after yield. Interestingly, the stress at a given strain in all the materials is linear as a function of strain rate indicating that there are no phase transformations affecting the response over the regime tested (Fig. 8).

Interestingly, polypropylene shows a markedly different behavior than PTFE and PE. Okereke et al. [92] showed that PP exhibited a distinct peak in true stress with subsequent strain softening, which they attribute to plastic strain-induced structural evolution of the non-crystalline portion of the polymer, which is approximately 35 %, in concert with adiabatic heating of the material. Additionally, the stress as a function of strain rate in this material exhibited a bilinear dependence on strain rate, which is not observed in PTFE or PE. This may be due to the glass transition moving to room temperature at high strain rates.

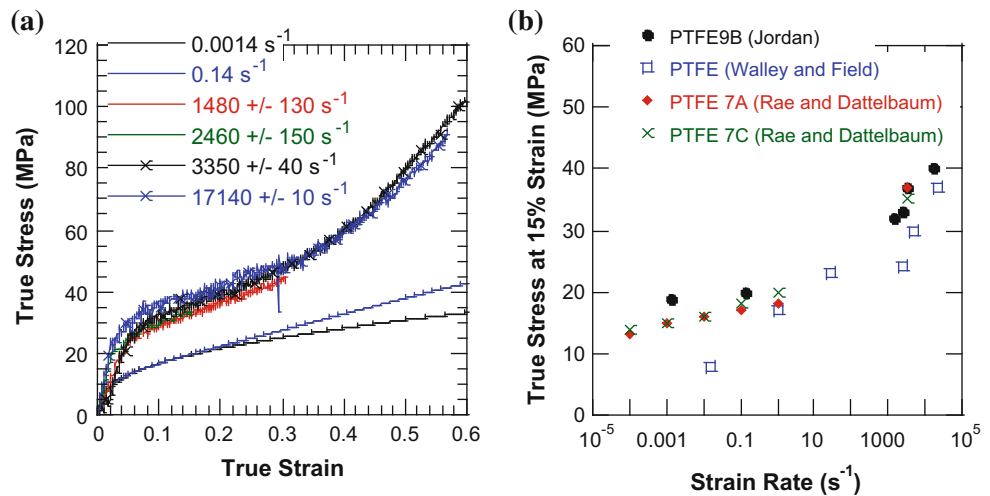
### Time–Temperature Superposition for Large Strain Response of Polymers

The first extensive experimental studies on the temperature and rate dependence of glassy polymers (PMMA [16] and polycarbonate [15, 17, 18, 133]) were conducted by Bauwens and Bauwens-Crowet et al. [15–18, 133]. This series of papers provided the first recognition of two molecular processes, which were responsible for the rate and temperature dependence of the yield strength in glass polymers. With this recognition, they were able to develop a master curve to allow for prediction of response outside of the experimentally tested regime. Similar research on polycarbonate (PC) was performed by Rietsch and Bouette [182], who extended the range of strain rates tested by

**Fig. 7** Plasticized PVC  
**a** stress–strain relationship at different strain rates and  
**b** representative stress close to yield as a function of strain rate.  
 Data from [153]



**Fig. 8 a** Stress versus strain rate for PTFE and **b** true stress at 15 % strain versus strain rate from Jordan et al. [174], Walley and Field [5], and Rae and Dattelbaum [6], at room temperature



using a Split Hopkinson Pressure Bar (SHPB) and observed an increase in the rate dependence of the yield stress above approximately  $100 \text{ s}^{-1}$  at room temperature. Walley and Field [5] studied several polymers, focusing on rate-dependent behavior. The tests were conducted at strain rates ranging from  $10^{-2}$  to  $10^4 \text{ s}^{-1}$ , using four different experimental techniques, including a direct impact Hopkinson bar for strain rates above  $10^3 \text{ s}^{-1}$ . For a significant proportion of polymers it was observed that yield stress increased more rapidly with increasing strain rate at higher rates. Such observations were subsequently made for a number of polymeric materials; however, some authors suggested that the observed response at high rate may have been an artifact of testing [183, 184], rather than an intrinsic property of the polymers under investigation.

It was partly to test such a hypothesis that Siviour et al. [19] reintroduced the use of time–temperature superposition equivalence as a means to interpret rate dependence in PC and polyvinylidene fluoride (PVDF). The materials were characterized over a wide range of strain rates ( $10^{-4}$  to  $10^4 \text{ s}^{-1}$ ) at room temperature and a wide range of temperatures ( $-50$  to  $150 \text{ }^\circ\text{C}$ ) at a constant strain rate ( $10^3 \text{ s}^{-1}$ ). The authors then posed an empirical formula for mapping the yield stress dependence on temperature to the dependence on strain rate, which agreed well with experimental data and comparisons in the literature. The formula employed a linear interdependence of temperature and strain rate, using reference strain rate and temperature as experimental constants, as well as the experimentally determined mapping parameter,  $D$ :

$$T = T_0 + A(\log \dot{\epsilon}_0 - \log \dot{\epsilon}) \tag{11}$$

where  $A$  quantifies the interaction between rate and temperature and maps from a temperature  $T$  to a new temperature  $T_0$  and mapping the strain rate from  $\dot{\epsilon}_0$  to a new strain rate  $\dot{\epsilon}$ . The mapping parameter,  $A$ , may be considered

as the temperature-strain rate equivalence parameter, which relates equivalent stress states in the material and is agnostic to the underlying deformation mechanisms [185] and it is typically found by fitting temperature dependent and rate dependent yield data but, in principle, should be obtainable from Dynamic Mechanical Analysis (DMA) data, and is certainly consistent with these data [153]. Siviour’s formula was able to capture several changes deformation mechanisms which govern changes in yield stress, including the inflection in data which involves the glass transition PVDF, and that which is understood as the beginning of the  $\beta$ -transition in PC. This analysis has subsequently been used on semi-crystalline polymers [174, 178] and particulate composites [41, 186]. Recent data on PVC with different amounts of plasticizer [153] have shown the effects on the analysis of having two transitions influencing the rate dependence, and how this can be dealt with using two shift parameters, similar to the deconstruct, shift, reconstruct method pioneered by Mulliken and Boyce [20], discussed further below.

Brown et al. [178] provided a detailed analysis of the linear mapping proposed Siviour [19] starting in the context of polymers with linear rate and temperature dependence but drawing conclusions applicable to all polymers. In particular, they pointed out that, even if the rate dependent and temperature dependent data sets share a common point, with an intersection stress  $\sigma_x$ , it is unlikely that the lines of best fit to these data sets will cross at this point: the lines may be globally suitable but are not pointwise accurate. This error can lead to instabilities in the evaluation of  $A$ , in particular if it is evaluated by pointwise comparison of the temperature and strain rate required to achieve a certain yield stress, around the intersection stress. Hence, in cases where  $A$  must be evaluated in a pointwise manner, for example in cases where the temperature and strain rate dependence of the yield stress do not follow

simple relationships, the points chosen should be as far as practicable from the intersection stress. Furthermore, they also discussed the difficulties in accurately extrapolating glass transition temperatures to high strain rates, where small uncertainties in  $T_g$  can lead to relatively large changes in the strain rate at which its effects can be seen in rate dependent data.

One issue that must be considered when implementing time–temperature superposition in polymers is the effect of adiabatic heating, particularly at high strain rates [185]. At elevated strain rates, the conversion of plastic work to heat in the specimen can occur much faster than the heat can be dissipated away through the platens or other loading device. In this situation, the measured flow stress is the stress at the instantaneous temperature of the specimen rather than the global experimental temperature resulting in thermal softening, which is not truly representative of the material behavior. Adding to the difficulty of understanding adiabatic heating under dynamic loading is the lack of high speed thermal techniques. Only recently have thermal cameras with sufficient acquisition times become available [142, 187–189].

One disadvantage to the Siviour technique as discussed above [19] is that it is limited to mapping a single stress state, i.e. a point-wise mapping, usually of the yield stress. The work of Furmanski, Cady, and Brown [185] considered the full deformation response using a strain-rate jump technique to eliminate the adiabatic effects that can be seen in polymers at strain rates greater than  $0.01 \text{ s}^{-1}$  and 15 % strain. The experiments involved rapidly increasing from low to intermediate ( $1 \text{ s}^{-1}$ ) strain rates, deforming the specimen, and then allowing it to cool. Using this technique, which eliminates adiabatic effects, they observed that the Siviour relationship [19] can be used to map the whole stress strain curve, rather than a single point.

Another approach to using time–temperature superposition to better understand high rate behavior is not to attempt to achieve isothermal conditions by interrupting the experiment, which becomes increasingly difficult as the rate increases, but rather to mimic the adiabatic effects seen in dynamic loading in a low strain rate experiment. For example, to replicate loading at, say,  $1500 \text{ s}^{-1}$  and  $25 \text{ }^\circ\text{C}$ , one may perform an experiment at  $0.001 \text{ s}^{-1}$  and an initial temperature of  $-20 \text{ }^\circ\text{C}$ , or whatever temperature is required to replicate the yield, typically achieved using an environmental chamber. As the loading progresses, the chamber temperature is raised according to the work done on the specimen, i.e.

$$\Delta T(\varepsilon) = \frac{\int^\varepsilon \sigma d\varepsilon}{\rho c}, \quad (12)$$

this replicates the temperature rise observed in an adiabatic high rate experiment, assuming that all of the mechanical

work done on the specimen is converted to heat. Recently, Kendall and Siviour have shown that this approach faithfully allows the high rate behavior of PVC to be replicated in low rate experiments [94]. Furthermore, they have shown that whilst the high rate behavior of PC and PMMA can be replicated, this requires  $\Delta T$  be modified from that predicted by the above equation, implying that there are further processes in these materials which affect the energy partition during deformation [124]. Finally, preliminary data have shown that this technique might prove effective in composite materials in which one component is temperature and rate dependent whilst the other is independent of these conditions [190].

Although not strictly applied to large strain response, when discussing the use of time–temperature superposition to understand the effect of lower order transitions on the high strain rate properties of polymers, mention should also be made of the deconstruct-shift-reconstruct method developed by Mulliken and Boyce [20] in order to predict the modulus of a polymer at high strain rate from low rate data in the case of multiple transitions with different frequency dependencies. Here, modulus-temperature data are split into components corresponding to the various transitions (e.g.  $\alpha$ ,  $\beta$  etc.) and the frequency dependence of the transitions is established. The transitions can then individually be shifted to high strain rate before being reconstructed to produce a new modulus-temperature dependence appropriate for high rate constitutive modeling.

## Pressure Effects in Polymers

Although pressure effects can play a large role on the mechanical properties of polymers, there has been limited research into this topic, particularly recently. The first study where a polymer was loaded under hydrostatic pressure was conducted by Bridgman in 1953 [191]. In 1975, Pae and Bhateja [22] wrote a review of the effects of hydrostatic pressure on the mechanical behavior of polymers, including specific properties of the polymers that had been characterized to date. In their survey of materials, they found that while all polymers exhibit pressure dependent properties, some features are material specific, and some are observed across all polymers, namely that increasing hydrostatic pressure results in increased modulus and yield stress, sometimes by as much as 50–100 %. Increasing pressure in materials where the glass transition is below room temperature was found to shift the transition to room temperature, for example in LDPE [22], similar to time–temperature superposition. Due to the differences in underlying deformation mechanisms, the ductility and post yield behavior in polymers varies by material [22].

**Table 1** Ratio of compressive to tensile yield strength for a range of polymers

Material	$\sigma_c/\sigma_T$	References
High density polyethylene (HDPE)	1.0	[198]
	1.18	[195]
Polycarbonate (PC)	1.20	[192]
	1.11	[18]
Polypropylene (PP)	1.24	[195]
Polyvinylchloride (PVC)	1.33	[192]
	1.3	[198]

The hydrostatic pressure dependence of yield in polymers has been observed by many authors [17, 192, 193]. The physical manifestation of this pressure dependence is a difference in tensile and compressive yield stress for the same material, as demonstrated for PVC in Fig. 6c. As shown in Table 1, these ratios are between 1 and 1.4 for a variety of polymeric materials, where a ratio of 1 indicates that the material is nominally pressure insensitive. Several yield criteria have been used to describe the yield behavior in polymers with the similarity between them being that the yield stress displays a linear dependence on hydrostatic pressure [194–197].

## Summary

The temperature, pressure, and strain rate dependence of polymers has been of interest from the earliest days of high strain rate testing. Although these materials present experimental challenges that are not of concern for metallic specimens, especially for high strain rate characterization, a large number of studies have been performed producing a high quality experimental database for amorphous, semi-crystalline and rubbery polymer materials. A key property of polymers which distinguishes them from metals is the time–temperature superposition effect, namely that increases in the strain rate or frequency of the applied loading have the same effect as decreases in temperature. This is a well-established effect for polymer modulus and associated behavior, and, for example, has been described by the WLF and Arrhenius equations; it can also be described by the deconstruct-shift-reconstruct method. Over the past 40 years, since the first papers investigating rate and temperature dependence of yield stress by Bauwens and Bauwens-Crowet, there has been development in understanding of time–temperature superposition as a tool for understanding large strain behavior under dynamic conditions. A linear mapping between strain rate and temperature is sufficient if only one transition is involved, and can be used to describe both yield and post-yield

behavior. For polymers in which the rate dependence is affected by more than one transition, further mappings may be required. In an extension to this technique, the effects of the change from isothermal to adiabatic conditions as the strain rate increases can also be replicated by suitable temperature profiling. These techniques offer the potential for better understanding of the underlying mechanisms governing high rate behavior in the future.

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