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Soft dielectric materials typically exhibit poor heat transfer properties due to the dynamics of phonon transport, which constrain thermal conductivity (k) to decrease monotonically with decreasing elastic modulus (E). This thermal–mechanical trade-off is limiting for wearable computing, soft robotics, and other emerging applications that require materials with both high thermal conductivity and low mechanical stiffness. Here, we overcome this constraint with an electrically insulating composite that exhibits an unprecedented combination of metal-like thermal conductivity, an elastic compliance similar to soft biological tissue (Young's modulus < 100 kPa), and the capability to undergo extreme deformations (>600% strain). By incorporating liquid metal (LM) microdroplets into a soft elastomer, we achieve a $\sim 25\times$ increase in thermal conductivity ($4.7 \pm 0.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) over the base polymer ($0.20 \pm 0.01 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) under stress-free conditions and a $\sim 50\times$ increase ($9.8 \pm 0.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) when strained. This exceptional combination of thermal and mechanical properties is enabled by a unique thermal–mechanical coupling that exploits the deformability of the LM inclusions to create thermally conductive pathways in situ. Moreover, these materials offer possibilities for passive heat exchange in stretchable electronics and bioinspired robotics, which we demonstrate through the rapid heat dissipation of an elastomer-mounted extreme high-power LED lamp and a swimming soft robot.

liquid metal | thermal conductivity | soft materials | soft robotics | stretchable electronics

Materials with high thermal conductivity are typically rigid and elastically incompatible with soft and mechanically deformable systems (1–6). In the general case of nonmetallic and electrically insulating solids, this limitation arises from kinetic theory and the Newton–Laplace equation, which imply that thermal conductivity (k) will increase with a material's elastic modulus (E) according to the approximation $k \approx (E/\rho)^{1/2}(C_V\ell/3)$, where C_V is the volumetric heat capacity, ℓ is the average mean free path of phonons, and ρ is the density (7, 8). For polymers like polyethylene, thermal conductivity can be enhanced through macromolecular chain alignment (from $k \approx 0.3 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ to $100 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$), but this also leads to a dramatic increase in elastic modulus from $\sim 1 \text{ GPa}$ to 200 GPa (9). Likewise, glassy polymer blends have been engineered to increase thermal conductivity through interchain hydrogen bonding (1), and relatively higher thermal conductivity has been observed in amorphous polythiophene ($k \approx 4.4 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) (2), but the high elastic modulus ($E \approx 3 \text{ GPa}$) and low strain at failure (<5% strain) of films make them unsuitable for soft functional materials (3).

To overcome this fundamental tradeoff with thermal transport in soft materials, attempts have been made to engineer composites with various fillers (10), including metals (11, 12), ceramics (13), carbon fibers (14), and nanomaterials such as carbon nanotubes and graphene (4, 15, 16). Anisotropic thermal conductivity can arise in composite systems by using 1D fillers such as carbon fibers where thermal transport preferentially occurs along the major dimension of the filler (14). Thermal anisotropy can also be induced in polymeric materials during drawing processes that increase chain alignment

(17). Although these composites exhibit increased thermal conductivity, they typically use rigid fillers that result in mechanically stiff materials that cannot support stretchable functionality (4–6) and, in the case of carbon-based fillers, become electrically conductive even at low-volume loadings, which can interfere with functionality (18). To date, the combination of low elastic modulus on the order of biological tissue, large mechanical deformability, and high thermal conductivity remains elusive.

Here, we show that a soft-matter composite consisting of elongated liquid metal (LM) microdroplets dispersed in a highly deformable silicone elastomer (Fig. 1A–D) exhibits an unprecedented combination of high thermal conductivity ($4.7 \pm 0.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ under stress-free conditions; $9.8 \pm 0.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ at 400% strain) with a low modulus ($89 \pm 2 \text{ kPa}$ after 200% prestrain) and high strain limit (>600%). This approach overcomes the Newton–Laplace scaling because the inclusions have a thermal conductivity that is dominated by electrons, rather than phonons, and can deform with the surrounding matrix to support strain and thermal–mechanical coupling (*Electronic Contribution to Thermal Conductivity of EGaln* and Fig. 1C and D). Previously, we showed that LM-embedded elastomers can be engineered to exhibit dramatic enhancements in electrical permittivity (19) and conductivity (20) without sacrificing the elastic properties of the matrix elastomer. A subsequent effort by another group attempted to show enhanced thermal conductivity with a polydisperse suspensions of irregularly shaped LM inclusions (12). Although an enhanced thermal conductivity of $2.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$

Significance

Efficient thermal transport is critical for applications ranging from electronics and energy to advanced manufacturing and transportation; it is essential in emerging domains like wearable computing and soft robotics, which require thermally conductive materials that are also soft and stretchable. However, heat transport within soft materials is limited by the dynamics of phonon transport, which results in a trade-off between thermal conductivity and compliance. We overcome this by engineering an elastomer composite embedded with elongated inclusions of liquid metal (LM) that function as thermally conductive pathways. These composites exhibit an extraordinary combination of low stiffness (<100 kPa), high strain limit (>600%), and metal-like thermal conductivity (up to $9.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) that far exceeds any other soft materials.

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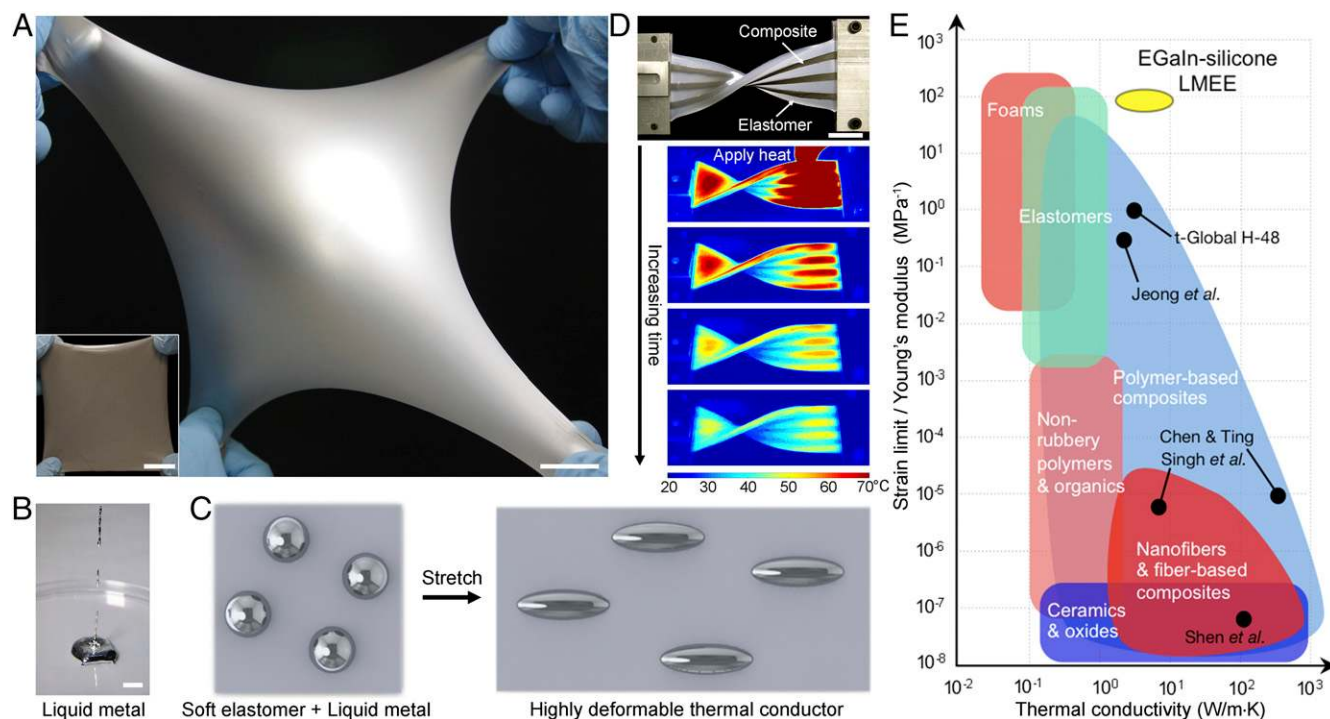


Fig. 1. Soft, thermally conductive composite. (A) Highly deformable LMEE. (scale bars, 25 mm.) (B) EGaIn alloy is liquid at room temperature and shows fluid characteristics as demonstrated by falling droplets. (Scale bar, 10 mm.) (C) Schematic illustration of the LMEE composite where LM microdroplets are dispersed in an elastomer matrix and, upon deformation, the LM inclusions and elastomer elongate in the direction of stretching. (D) Alternating strips of LMEE and unfilled elastomer are heated with a heat gun, and the IR photo time sequence shows the LMEE dissipating heat more rapidly than the elastomer (images correspond to $t = 0, 5, 10$, and 15 s after the heat source is removed). (Scale bar, 25 mm.) (E) The $\phi = 50\%$ LMEE composites described here occupy a unique region of the material properties space when comparing thermal conductivity with the ratio of strain limit to Young's modulus. (Data points are from refs. 2, 9, 12, and 14.)

was measured at high LM volume fraction (66% by vol.; 92.5% by weight), these samples exhibited an increased stiffness (Young's modulus increased from 0.65 MPa to 3.3 MPa) and reduced stretchability (strain limit decreased from 150 to 50%), which limits the ability to elongate LM droplets in situ. Comparing previous results with the exceptional performance reported here (Fig. 1E) highlights the critical importance of LM microstructure (and not just material composition) in enabling elastomers to exhibit metal-like thermal conductivity without altering their natural elasticity.

Experimental Results

The LM embedded elastomer (LMEE) is composed of a Pt-catalyzed silicone elastomer embedded with a randomly distributed, polydisperse suspension of nontoxic (21), liquid-phase eutectic gallium–indium (EGaIn) microdroplets (19, 20, 22). As shown in Fig. 1D and Movie S1, stretched and twisted strips of LMEE exhibit rapid thermal dissipation compared with adjacent strips of unfilled elastomer subject to the same initial heating. Compared with previous attempts with LM-filled elastomers (12), we have discovered that strain creates thermally conductive pathways through the in situ elongation of the deformable liquid inclusions, which significantly enhances thermal conductivity in the stretching direction. For permanent (stress-free) and strain-controlled elongation of the LM inclusions, this enhanced k is nearly 25 \times to 50 \times greater than the unfilled elastomer ($0.20 \pm 0.01 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) and approaches the limit for the parallel rule of mixtures of an EGaIn–silicone composition (23) without the aid of percolating networks. Referring to Fig. 1E, the exceptional combination of high thermal conductivity, low elastic modulus, and high strain limit allows the LMEE composites to occupy an uncharted region of the material properties space.

The thermal composite is fabricated by shear mixing EGaIn alloy (75% Ga, 25% In, by weight; Gallium Source) with an uncured silicone elastomer (Ecoflex 00-30; Smooth-On) (see Methods for material fabrication). During mixing, the LM droplets form a

self-passivating Ga_2O_3 coating that helps prevent coalescence and eliminates the need to add surfactants or other dispersing agents (24). The droplets have a statistically uniform spatial distribution and are polydisperse, with a median diameter of $\sim 15 \mu\text{m}$ (19). Thermal conductivity is measured using the transient hotwire (THW) method in which an embedded wire simultaneously acts as a resistive heat source and thermometer that measures the change in temperature (ΔT) as a function of time (t), which is related to thermal conductivity through the cylindrical heat diffusion equation (Methods and Fig. S1). Experimental measurements are presented in Fig. 2A and show that, as LM volume fraction (ϕ) increases, thermal conductivity increases (Fig. S2). These values are in good agreement with theoretical predictions obtained from the Bruggeman effective medium theory (EMT) formulation (25) for a uniform dispersion of spherical EGaIn inclusions [$k = 26.4 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ (23)] in a silicone matrix ($k = 0.20 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$).

We further configure the THW method to enable directional measurements of thermal conductivity upon deformation by laminating LMEE strips around wires that are parallel (axial) and perpendicular (transverse) to stretch, as shown in Fig. 2B. Ellipsoidal heat spreading yields effective anisotropic thermal conductivities in the axial and transverse directions that can be transformed to measure the orthotropic (k_x , k_y , k_z) bulk values (see EMT for derivation) (26, 27). This configuration enables examination of the thermal–mechanical coupling between thermal conductivity and deformation. We find that, upon stretching the unfilled ($\phi = 0\%$) homogenous elastomer, the thermal conductivity in the direction of stretch ($k_y \approx 0.20 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$) remains largely unchanged (Fig. 2C). However, when stretching the $\phi = 50\%$ LMEE, the thermal conductivity in the longitudinal direction (k_y) dramatically increases and reaches a value of $9.8 \pm 0.8 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ at 400% strain (Figs. S3 and S4). This represents an increase of $\sim 50\times$ relative to the unfilled material and a value that approaches

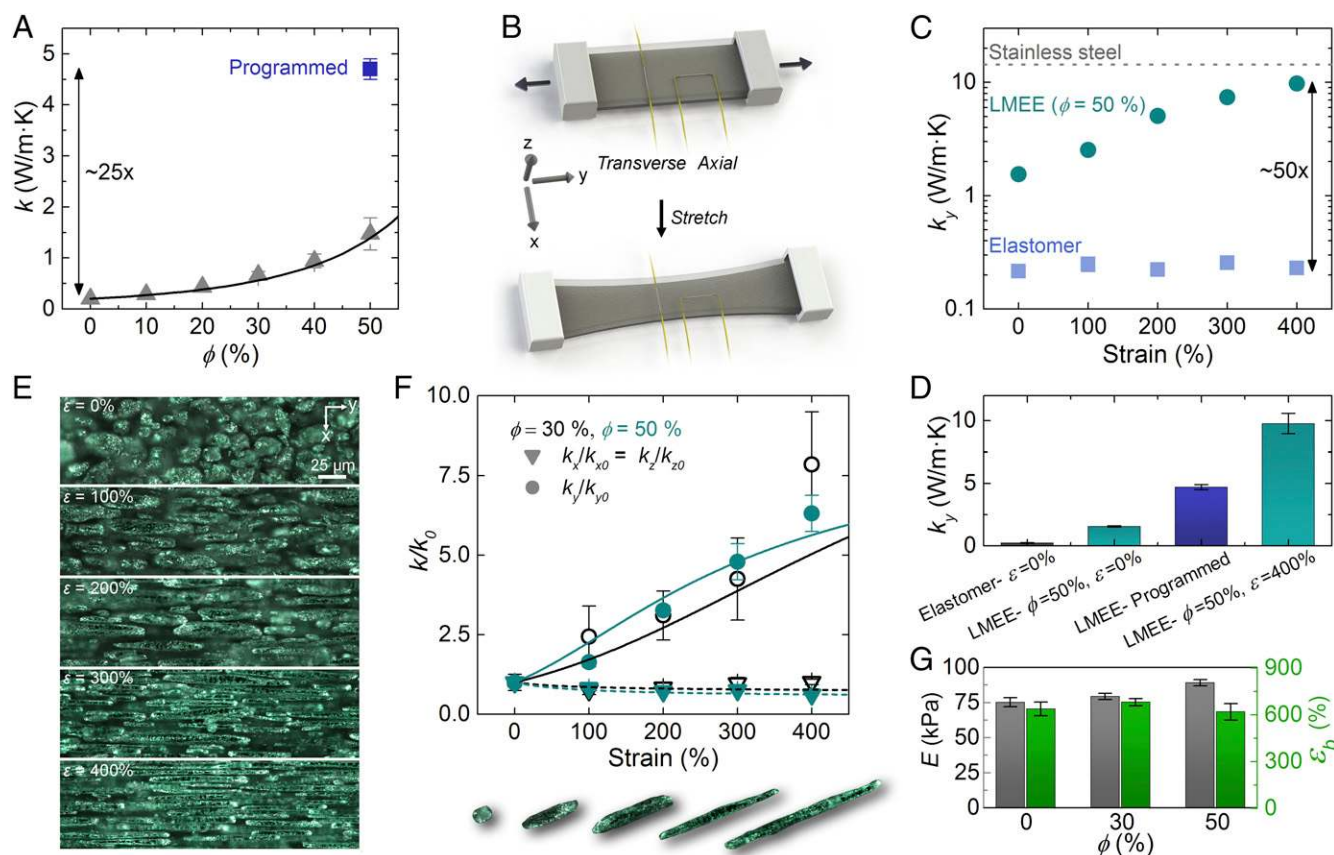


Fig. 2. Thermal–mechanical behavior of the LMEE composite. (A) Thermal conductivity versus LM volume fraction (ϕ) in the stress-free state. The programmed sample refers to a composite that has been stretched to 600% strain and then relaxed to an unloaded state. Here the symbols are the experimental measurements, and the solid curve represents the theoretical prediction from the Bruggeman EMT formulation ($n = 100$ volume fraction dependence, $n = 5$ programmed samples). (B) Schematic of the THW method to measure anisotropic thermal conductivity under deformation. (C) Plot of thermal conductivity in the stretch direction versus strain for the elastomer and the LMEE composites. Upon stretching, the LMEE approaches the thermal conductivity of stainless steel and is $50\times$ greater than the unfilled elastomer ($n = 5$). (D) Thermal conductivity comparison for different LM volume fractions (ϕ) and stress states ($n = 5$). (E) Optical micrographs of the 30% LMEE microstructure during stretching, with the images corresponding to 0 to 400% strain in 100% increments (from top to bottom). (F) Normalized thermal conductivity as a function of strain (blue open symbols are $\phi = 30\%$, and cyan closed symbols are $\phi = 50\%$; $n = 5$). The solid line represents the predicted behavior for the y direction, and the dashed line is the prediction for the x and z direction from our model. The images are representative images of the LM inclusions during the deformation process. (G) Mechanical properties of the LMEE composites with elastic modulus on the left axis and strain at break on the right axis ($n = 3$). All error bars represent ± 1 SD.

the thermal conductivity of some metals like bismuth and stainless steel. These measurements, which were taken at room temperature, are in good agreement with tests performed on samples that were either cooled to 0°C or heated to 60°C (Fig. S5). In addition, the material is robust to cyclical loading, with only a slight increase in thermal conductivity measured after 1,000 cycles of 200% strain (Fig. S6). Furthermore, we can “program” the material to achieve permanently elongated LM inclusions in a stress-free state by stretching a virgin sample of LMEE to 600% strain and then unloading to zero stress. An unrecoverable plastic strain of 210% is induced, enabling elongated inclusions in an unloaded (stress-free) state (Methods and Fig. S7). As shown in Fig. 2A, thermal conductivity of the programmed LMEE sample in the longitudinal direction (k_y) is $4.7 \pm 0.2 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$, which is $\sim 25\times$ greater than that of the base elastomer (Fig. 2D). It is important to note that, when unstrained, both the $\phi = 0$ and 50% samples exhibit values of k that are typically observed in other polymeric composites (12, 28).

Such an unprecedented enhancement in k arises from the discovery of a unique thermal–mechanical coupling in which the deformable LM inclusions elongate into needle-like microstructures along the prestrained or mechanically loaded direction to create enhanced thermally conductive pathways (Fig. 2E). This is further demonstrated in Fig. 2F, in which compositions with $\phi = 30\%$ and 50% EGaIn (by volume) are subject to strains ranging from 0 to 400% in increments of 100% (Methods and

Figs. S3 and S4). As shown, the thermal conductivity in the y (stretching) direction increases by greater than a factor of 5 beyond 300% strain. To theoretically capture this behavior, we create an EMT model based on the Bruggeman formulation to explain the relative increase in directional thermal conductivity as a function of axial strain (ϵ) (see EMT for details). As seen in Fig. 2F, we find good agreement between the experimentally measured values (markers) and our theoretical predictions (curves), which capture the large increase in thermal conductivity in the stretching direction (k_y) and the slight decrease in the orthogonal directions (k_z , k_x). The agreement with theory is achieved without data fitting and supports the claim that the observed anisotropic thermal–mechanical response is controlled by the directional change in aspect ratio of the LM inclusions (Fig. 1C). Lastly, for all volume fractions, the composite materials have an elastic modulus less than 90 kPa (Fig. S8) and can support uniaxial strains above 600%, properties that are similar to those of the homogeneous elastomer (Fig. 2G). The modest increase in elastic modulus ($<20\%$) for the LMEE composites can be attributed to surface tension at the liquid–solid interface. For liquid inclusions in a compliant matrix, Style et al. (29) have previously shown that surface tension can induce mechanical resistance to droplet deformation and result in an overall stiffening of the composite. Together, these results show that the EGaIn droplets greatly enhance thermal conductivity of soft materials

elastic medium. Here, we report a soft elastomer composite that overcomes this constraint and exhibits the highest-ever combined values of thermal conductivity and stretchability (Fig. 1E). This high performance is accomplished by exploiting the unique thermal–mechanical interactions of LM microdroplets that are suspended within a silicone elastomer. The composite achieves an exceptional combination of low elastic modulus (<100 kPa; i.e., softer than human skin), high strain limit (>600%), and high thermal conductivity (k), which ranges from $4.7 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ (stress-free state) to nearly $10 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ (when stretched). This represents a $25\times$ to $50\times$ increase in thermal conductivity compared with soft rubbers, i.e., similar in magnitude to some metals (e.g., bismuth, manganese, stainless steel) while having a 10^5 to 10^6 lower elastic modulus.

The ability to achieve high thermal conductivity with an elastomer without altering its elastic properties is enabled through LM microstructure and the distinctive thermal–mechanical coupling in which the deformation of an elastomer matrix creates needle-like LM inclusions in situ. Previous studies of LM suspensions in elastomer did not explore such critical factors and hence failed to capture the breakthrough performance presented here. These experimentally measured values are also found to be in strong agreement with predictions from a theoretical model that we derived based on Bruggeman EMT. Such agreement is achieved without the aid of data fitting and provides further evidence for the critical role of in situ elongation of LM inclusions. As previously shown by Style et al. (29), altering the size of liquid inclusions in a compliant matrix can result in changes to the elastic modulus of the composite. However, according to our EMT model, inclusion size has little influence on thermal conductivity (which is instead largely dependent on LM volume loading and inclusion aspect ratio). This difference in dependency can be used for matching the elastic properties of composites without altering the thermal properties (see *Influence of LM Droplet Size on Elastic Modulus* and Fig. S11).

The combination of high thermal conductivity and elasticity is especially critical for rapid heat dissipation in applications such as wearable computing and soft robotics, which rely on soft and stretchable functionality. We show that LMEE composites can be used to manage heat within an SMA-powered swimming robot and stretchable, body-mounted circuits for high-power illumination. Together, these examples show the potential for LMEEs to dramatically improve thermal management in applications that require electrically insulating materials with both rapid heat conduction and soft elastic functionality. In particular, we anticipate that this class of materials will be enabling for soft robotics, shape-changing programmable matter, stretchable electronics, and soft-matter technologies designed for physical interaction with humans.

Methods

Composite Fabrication. LMEE composites are composed of a polydisperse suspension of EGaln microdroplets dispersed in a Pt-catalyzed silicone elastomer (Ecoflex 00-30; Smooth-On). The fabrication method is the same as that reported in Bartlett et al. (19). First, the two-part silicone prepolymer is prepared by combining part A and part B at a 1:1 ratio by mass and then thoroughly mixing and degassing in a planetary centrifugal mixer (THINKY AR-100). EGaln alloy is prepared by mixing gallium and indium (Gallium Source, LLC) at a 3:1 ratio by mass and then heating and homogenizing at 190°C overnight on a hot-plate. The LMEE is then prepared by shear mixing the uncured polymer and EGaln with a mortar and pestle. Components are mixed for 7 min to 10 min until a homogeneous viscous composite is obtained. For volume fractions of LM lower than 30%, the initial mixing is done at higher concentrations and then diluted to maintain similar mixing conditions.

THW Testing. Thermal conductivity is determined using the THW method and the following analytical solution to the cylindrical heat diffusion equation: $k = q/4\pi\xi$ (34). Here, q is the volumetric heating of the wire per unit length, which is calculated using known current and resistance values (see Fig. S1 for reference measurements), and $\xi = d(\Delta T)/d[\ln(t)]$.

Unstrained measurements. Test samples are prepared by first suspending a platinum wire ($D = 25 \mu\text{m}$, $\ell = 40 \text{ mm}$) in a 3D-printed container with

dimensions of $40 \text{ mm} \times 7 \text{ mm} \times 7 \text{ mm}$. Next, uncured composite is poured around the wire to ensure conformal contact. The composite is cured with the Pt wire inside in an oven at 50°C for 16 h. The electrical resistance across the wire is measured before and after curing to ensure that there is no mechanical interference in the wire due to thermal expansion or contraction. To administer the tests, each sample is connected to a Keithley 2700 Digital Multimeter and a Keithley 6221 DC/AC Current Source in a four-point measurement configuration. A Heavyside current input of $I = 30 \text{ mA}$ is applied, and 50 voltage values (V) are recorded over 0.9 s. With this voltage data and a known current, the resistance (R) is determined as a function of time following Ohm's Law: $R(t) = V(t)/I$. This is used to calculate the change in temperature $\Delta T(t) = [R(t)/R_0 - 1]/\beta$ and the volumetric heating of the wire per unit length $q = I^2 R_0/\ell$. Here, $R_0 = R(0)$ is the initial resistance of the wire, $\beta = 3.75 \times 10^{-3} \text{ K}^{-1}$ is the coefficient of thermoresistance of platinum, and ℓ is the length of the wire. Next, we plot ΔT versus time (t) and fit the curves using the following three-parameter model: $\Delta T = b_1 \ln(t - b_2) + b_3$, where the constants b_1 , b_2 , and b_3 are the fitting parameters. The fit is performed in MATLAB R2015a (The Mathworks, Inc.) using a nonlinear regression "nlinfit" algorithm. The fitted coefficient b_1 corresponds to $\xi = d(\Delta T)/d[\ln(t)]$, and the thermal conductivity is calculated as $k = q/4\pi\xi$. Our data acquisition has an arbitrary delay relative to initiation of the Heavyside function, and b_2 and b_3 represent the delay time and resultant temperature rise that occur during that period.

The thermal conductivities measured for water and glycerol at room temperature are 0.60 ± 0.07 and 0.33 ± 0.02 , respectively, and are in good agreement with reference data. The thermal conductivity is reported by taking the average k across all runs, and the error represents ± 1 SD. Fig. S1 shows the ΔT versus t plots for these two validation measurements, where the data symbols represent the average and the shaded areas correspond to the SD for 50 measurements.

Average ΔT vs. time for LMEE samples of varied LM volume fraction is shown in Fig. S2. Each measurement is repeated 100 times for each volume fraction of LM composite. The data symbols represent the average, and the shaded areas correspond to the SD for 100 measurements at each volume fraction.

Thermal–mechanical testing. The thermal conductivity as a function of stretch is measured with two Pt wire probes orientated parallel and perpendicular to the primary stretching direction (Fig. 2B). The probes are laminated between two layers of material, which each have dimensions of 60 mm wide, 40 mm long, and $\sim 5 \text{ mm}$ thick. Tests are performed with composites of $\phi = 0\%$, 30%, and 50% that are strained ($\varepsilon = \Delta L/L_0$) to 400% in 100% strain increments. A current of 30 mA is used for $\phi = 0\%$ and 30% (with the exception $\phi = 30\%$ at 400% strain, where 60 mA is applied to improve signal to noise), and 100 mA is used for $\phi = 50\%$. At each strain increment, five measurements are taken on each wire at 2-min intervals. After each strain increment, the two layers of material are delaminated, freeing the wire probes to prevent damage during stretching, then stretched equally in both directions using linear actuators. At the next position, the layers of composite are relaminated around the wires, with a clamping force applied to ensure conformal contact.

Fig. S3 demonstrates the good agreement with the three-parameter fit for the $\phi = 50\%$ LMEE measured on the axial wire at $\varepsilon = 0\%$ and 400%. The symbols are the data points for each run, and the lines represent the corresponding three-parameter fit. Fig. S4 presents ΔT vs. t curves for the axial and transverse wires in the $\phi = 0\%$, 30%, and 50% LMEE. At $\varepsilon = 0\%$, the measured thermal conductivity for both the laminated parallel and transverse sensors are in good agreement with the embedded sensors described in *Unstrained measurements*, proving that the wire is in intimate contact with the LMEE samples.

Strain-dependent thermal conductivity is also evaluated at elevated ($60 \pm 3^\circ\text{C}$) and reduced ($0 \pm 3^\circ\text{C}$) temperatures. A thermocouple embedded in the LMEE is used to monitor temperature, and measurements are conducted when a variance of no more than 0.1°C is observed over a 1-min period. Thermal conductivity measurements are then performed as described above. In between each strain increment, the LMEE is allowed to reach room temperature and then stretched. The LMEE is then reheated or cooled for the next measurement.

Shape-Programmable LMEE. We program the shape of the LM particles by inducing plastic deformation in the films. The samples are made in a dogbone shape and tested on an Instron 5969 mechanical testing machine with 10 N load cell. The sample is stretched with a strain rate of 0.17 min^{-1} , up to a strain of 600%, and unloaded to stress-free state. Plastic strain of 210% is induced in the sample, and LM particles are elongated in the direction of stretch (Fig. S7B). THW data are presented Fig. S7 C and D.

Mechanical Testing. Mechanical samples are prepared in a dogbone shape, and tests are performed on an Instron 5969 mechanical testing machine using a 10 N load cell. Three samples are tested with LM volume ratio of 30% and 50%, under a strain rate of 10 mm/min. Samples are cyclically loaded three times at each of the following sequence of strains: 20%, 40%, 60%, 80%, 100%, 150%, and 200%. Fig. S8 A and B presents the stress–strain curves for LMEE for the 30% and 50% samples, respectively. The elastic modulus is calculated as the slope of the loading curve at a nominal strain of 10%. The nominal strain is defined with respect to the absolute stress-free strain of the sample, which increases during cyclical loading. In general, strain is calculated as a percentage defined with respect to the original length of the virgin sample (before initial loading). The 10% elastic modulus for the 30% and 50% samples is presented in Fig. S8 C and D, respectively.

Soft Robotics Implementation. We perform a series of illustrative artificial muscle implementations with SMA wire that enable the propulsion of a bioinspired, silent, soft swimming robot (Fig. 3 A and B and Movie S2). The actuator is composed of two naturally curved loops of SMA wire (0.012 in diameter; Dynalloy) that have an antagonistic arrangement and induce bi-directional bending when serially activated through direct Joule heating. The material encapsulating the SMA actuator is thus required to have both high thermal conductivity to facilitate heat transfer to the outer media and a low Young's modulus to allow significant deflection (Figs. S8 and S9). This advantage can be seen in Fig. 3C when actuators sealed in either LMEE, unfilled silicon, or commercial thermal tapes are actuated at a frequency of 5 Hz in a water bath. The LMEE-sealed actuator reaches a steady-state amplitude of ~10 degrees, whereas the unfilled silicone elastomer becomes saturated with heat and ceases to actuate, and the commercial tape reaches a much smaller amplitude of ~3 degrees because of its high mechanical stiffness. The LMEE-sealed actuator is also able to operate at a range of frequencies (Fig. 3D), with a maximum of 10 Hz. At frequencies above 5 Hz, the electrical pulse duration becomes shorter than the thermal time constant of the fin, and the amplitude of the periodic temperature oscillation within the SMA wire decreases. Details of the SMA actuator fabrication and testing are reported in *Thermal Actuator*.

When incorporated into a silicone-based soft robotic fish, the LMEE-sealed SMA enables forward caudal fin locomotion at ~0.15 body lengths per second (0.7 Hz activation). The body of the soft swimming robot is composed

of polydimethylsiloxane (PDMS; 1:10 base to curing agent ratio; Sylgard-184; Dow Corning) mixed with a blue pigment (0.3% by weight; Smooth-On); it is an assembly of three parts that are bonded to form two chambers as shown in Fig. S10, which are filled with EGaIn and water, respectively, to balance the weight and buoyancy. Each individual part is produced by casting the dyed PDMS in a 3D-printed mold and then bonded together.

The caudal fin of the robot is composed of Ecoflex 00-30 (Smooth-On). As with the PDMS, the Ecoflex silicone is prepared using a THINKY AR-100 planetary centrifugal mixer. The elastomer is poured into molds for the two halves of the fin. After curing, the two layers of the film are bonded together with an additional layer of Ecoflex. The buoyancy is adjusted by filling the embedded chambers of the caudal fin with water.

LED Demonstration. LMEE and elastomer (Ecoflex 00-30; Smooth-On) samples are mounted on a frame and stretched to 400% strain. EGaIn traces are applied with a stencil mask and connected to copper leads. XHP LED lamps (Cree XLamp XHP50, 5 mm × 5 mm) are placed onto the EGaIn traces on the stretched samples. The LEDs are connected in parallel with a power supply, and 6 V and 500 mA are supplied at time $t = 0$ s. IR images are captured with a FLIR A645sc Infrared Camera with a 45° lens at a frame rate of 25 frames per second.

For the wearable electronics demonstration, an XHP LED lamp (Cree XLamp XHP50, 5 mm × 5 mm) is placed on an LMEE layer with 3.5-mm thickness, and is sealed by another layer of LMEE. A thin layer of elastomer is used to seal the EGaIn traces to stop the LM from spreading. EGaIn traces are connected to banana plugs at the terminal end, which are secured in place using silicon adhesive and acrylic clamps. The LED is powered by a 9-V battery.

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