Thermoelectric Materials

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High Thermoelectric Figure of Merit and Nanostructuring in Bulk p-type $Na_{1-x}Pb_mSb_vTe_{m+2}**$

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Thermoelectric materials are special types of semiconductors that function as "heat pumps" and as heat-to-electricity converters. Thermoelectric power generation allows for small size, high reliability, and quiet operation. Efficient thermoelectric-based heat-to-electricity converters require higher performance materials than are currently available.^[1,2] Direct conversion of heat to electricity could be achieved with solidstate devices based on thermoelectric materials. These devices could play an important role in future energy production, conversion, management, and utilization. When a temperature gradient is created across a thermoelectric module, a voltage is generated, owing to the Seebeck effect. This voltage can be used to drive an external load.[3] Currently, there is a strong scientific and technological drive to identify new materials with enhanced thermoelectric figures of merit $ZT = (\sigma S^2/\kappa) T$ (where σ is the electrical conductivity, S the thermopower or Seebeck coefficient, κ the thermal conductivity, and T the temperature). The numerator σS^2 is called the power factor PF. Several classes of materials are currently under investigation, including complex chalcogenides, [4] doped PbTe and its solid solutions, such as $Pb_{1-x}Sn_xTe_x^{[5,6]}$ superlattice thin films, [7,8] and quantum-dot superlattices. [9-11] Also of interest are skutterudites, [12,13] metal oxides,[14] and intermetallic clathrates.[15-17] The superlattice thin-film structures of Bi₂Te₃/Sb₂Te₃ grown from chemical vapor deposition, $^{[18]}$ and of $PbSe_{0.98}Te_{0.02}/PbTe$ formed by molecular beam epitaxy (MBE) $^{[11,19,20]}$ have figures of merit greater than ZT=2 (at approximately 300 and 550 K, respectively). The MBE-grown thin films PbSe_{0.98}Te_{0.02}/PbTe are n-type materials and contain pyramid-shaped "nanodots" of PbSe of uniform size (approximately 20 nm), which form spontaneously inside a matrix of PbTe. [11,19,20] Because energy-

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conversion applications require materials in large quantities, we seek bulk analogues of these systems with similar figures of merit.

A recent contribution to these efforts was the discovery of the n-type Ag-based tellurides AgSbTe₂/PbTe, which can exhibit high figures of merit (ZT≈1.7 at 700 K) when properly doped. [21,22] To construct a fully functioning optimal thermoelectric device, both n- and p-type materials are needed. To date, there is no p-type counterpart to AgSbTe₂/ PbTe with similar performance. The highest figure of merit reported for p-type bulk materials (ZT≈1.2 at 700 K) is exhibited by the so-called TAGS system (based on Te, Ag, Ge, and Sb: $(GeTe)_{1-x}((Ag_2Te)_{1-y}(Sb_2Te_3)_y)_x).^{[23]}$ These Ge-containing materials, though more efficient than PbTe, have found limited use, owing to their high cost and to a lowtemperature phase transition. Recently, we described the ptype materials $Ag(Pb_{1-\nu}Sn_{\nu})_mSbTe_{2+m}$, which show outstanding thermoelectric properties, reaching a maximum figure of merit of ZT \approx 1.45 at 630 K.^[24]

Herein, we report that the Ag-free system $Na_{1-x}Pb_mSb_vTe_{m+2}$, with appropriate combinations of m, y, and x, achieves record-high ZT values for a p-type bulk thermoelectric material. The effect of the composition on the thermoelectric properties is profound. We show that the high performance of these materials derives mainly from a low thermal conductivity. High-resolution transmission electron microscopy (HRTEM) demonstrates pervasive nanostructuring in $Na_{1-x}Pb_mSb_vTe_{m+2}$, which may be the root cause for the remarkably low thermal conductivity. [25] The $Na_{1-x}Pb_mSb_vTe_{m+2}$ system was selected for study because it should be naturally prone to create Na, Sb-rich clusters in the lattice. The distribution of Na⁺ and Sb³⁺ ions in the Pb²⁺ sublattice cannot be random, as would be demanded by a solid solution, because Coulombic forces alone tend to drive the system to clustering at the nanoscale, thereby lowering the overall energy.^[26] The results described herein are in agreement with long-standing theoretical predictions that nanostructuring in semiconductors would lead to enhanced thermoelectric figures of merit. [25,27] The Na_{1-x}Pb_mSb_vTe_{m+2} materials could find applications in devices for power generation from a wide variety of hot sources, for example, vehicle exhausts, coal-burning installations, or electric power utilities.

Na_{1-x}Pb_mSb_yTe_{m+2} ($y \le 1$) samples (see Supporting Information for synthesis details^[28]) exhibit p-type conduction from 300 to 700 K. Ingots with the composition Na_{0.95}Pb₁₉SbTe₂₁ (m = 19, x = 0.05, y = 1) exhibit an electrical conductivity of $\sigma = 1422$ S cm⁻¹ with a positive thermopower of $S = 105 \,\mu\text{V K}^{-1}$ at room temperature. This leads to the relatively high power factor of PF = 15.6 μ W cm⁻¹ K⁻². The temperature dependence of the electrical conductivity and the thermopower of Na_{0.95}Pb₁₉SbTe₂₁ are shown in Figure 1 A. The conductivity decreases with increasing temperature, which is consistent with degenerate semiconductors, and reaches $\sigma = 150$ S cm⁻¹ at 700 K. However, the thermopower increases rapidly to $S = 357.6 \,\mu\text{V K}^{-1}$ at 700 K, yielding a much higher power factor of PF = 19 μ W cm⁻¹ K⁻².

For samples of composition $Na_{0.95}Pb_{20}SbTe_{22}$ (m = 20, x = 0.05, y = 1), an electrical conductivity of $\sigma = 1541$ S cm⁻¹ and a

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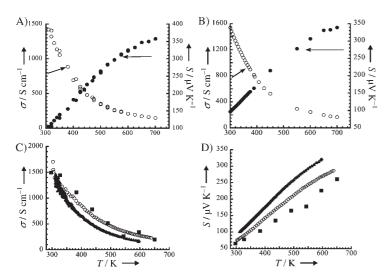


Figure 1. Temperature dependence of the electrical conductivity σ (\odot) and the Seebeck coefficient S (\bullet) for A) Na_{0.95}Pb₁₉SbTe₂₁ and B) Na_{0.95}Pb₂₀SbTe₂₂. Temperature dependence of C) the electrical conductivity σ and D) the Seebeck coefficient S for Na_{0.8}Pb₂₀Sb_yTe₂₂ with γ = 0.4 (\blacksquare), 0.6 (\odot), and 0.8 (\blacktriangle). The conductivity and thermopower measurements were performed simultaneously on samples of typical size 7×5×4 mm³. See Supporting Information for measurement details. [²⁸]

thermopower of $S=96~\mu V~K^{-1}$ were measured, which result in a power factor of $PF=14.2~\mu W~cm^{-1}~K^{-2}$ at 300 K. As observed for $Na_{0.95}Pb_{19}SbTe_{21}$, the electrical conductivity decreases rapidly with rising temperature (Figure 1B). At 700 K, the conductivity is $\sigma=165~S~cm^{-1}$ and the thermopower is $S=339~\mu V~K^{-1}$, yielding a power factor of $PF=19~\mu W~cm^{-1}~K^{-2}$. Therefore, the electrical performance (power factor) of $Na_{1-x}Pb_mSb_yTe_{m+2}$ samples remains almost unchanged upon small variation of m for a constant Na/Sb ratio.

To study the influence of the Na/Sb ratio on the properties of the materials, samples with compositions Na_{0.8}Pb₂₀Sb_yTe₂₂, (m = 20, x = 0.2, y = 0.4, 0.6, 0.8) were examined. As shown in Figure 1 C, the electrical conductivity increases slightly with decreasing Sb content. The drop in conductivity with rising temperature is more pronounced as the Na/Sb ratio decreases. The room-temperature Seebeck coefficient of the Na_{0.8}Pb₂₀Sb_vTe₂₂ samples tends to increase with decreasing Na/Sb ratio (Figure 1D). As the temperature increases, a more substantial divergence is observed in the thermopower plots, which suggests higher performance at high temperatures with decreasing Na/Sb ratio. From Figure 2A, we can see that the power factor of the Na_{0.8}Pb₂₀Sb_vTe₂₂ materials at room temperature increases with decreasing Na/Sb ratio. The highest power factor of PF = $22 \mu W \text{ cm}^{-1} \text{ K}^{-2}$ is found for the sample with Na/Sb=1 (y=0.8) at 450 K. At 600 K, the sample with y = 0.6 showed a power factor of PF= $19.5 \,\mu\text{W}\,\text{cm}^{-1}\,\text{K}^{-2}$, which is the highest among the $Na_{1-x}Pb_mSb_yTe_{m+2}$ samples for this temperature.

The temperature dependence of the thermal conductivity of $Na_{0.95}Pb_{20}SbTe_{22}$, along with the lattice and carrier contributions to the thermal conductivity, are plotted in Figure 2B. At room temperature, the total thermal conductivity of the sample is $\kappa = 1.8~Wm^{-1}K^{-1}$, which is approximately

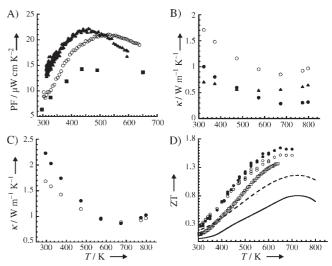


Figure 2. A) Temperature dependence of the power factor PF = σ S² for Na_{0.8}Pb₂₀Sb_yTe₂₂ with y = 0.4 (■), 0.6 (○), and 0.8 (▲). B) Temperature dependence of the thermal conductivity κ of Na_{0.95}Pb₂₀SbTe₂₂ (○), showing the lattice κ_{latt} (▲) and carrier κ_{el} (●) contributions. See text for details. C) Temperature dependence of the thermal conductivity κ of Na_{0.95}Pb₁₉SbTe₂₁ (○) and Na_{0.8}Pb₂₀Sb_{0.6}Te₂₂ (●). D) Temperature dependence of the thermoelectric figure of merit ZT for Na_{0.95}Pb₂₀SbTe₂₂ (●), Na_{0.95}Pb₁₉SbTe₂₁ (○), and Na_{0.8}Pb₂₀Sb_{0.6}Te₂₂ (□), compared to those of the state-of-the-art p-type materials PbTe (solid line) and TAGS (dashed line). See Supporting Information for measurement details. [²⁸]

22% lower than the typical value of $\kappa = 2.3 \text{ W m}^{-1} \text{ K}^{-1}$ reported for p-type PbTe.[29] The thermal conductivity decreases with increasing temperature, reaching a minimum of $\kappa = 0.85 \text{ W} \text{ m}^{-1} \text{ K}^{-1}$ at 675 K, and then increasing slightly from 675 to 800 K. The lattice thermal conductivity κ_{latt} was determined by subtracting the electronic contribution $\kappa_{\rm el}$ as calculated using the Wiedemann-Franz law ($\kappa_{\rm el} = L \sigma T$, where $L \approx 2.45 \times 10^{-8} \,\mathrm{W}\,\Omega\,\mathrm{K}^{-2}$ is the Lorenz number) from the total thermal conductivity (that is, $\kappa_{\text{latt}} = \kappa - \kappa_{\text{el}}$). The value of $\kappa_{\text{latt}} = 0.74 \text{ W m}^{-1} \text{ K}^{-1}$ at 300 K is only one third of that of PbTe $(\kappa_{\text{latt}} = 2.2 \text{ W m}^{-1} \text{ K}^{-1})$. Below 500 K, the thermal conductivity is mostly due to the electronic contribution, whereas above 500 K, the lattice contribution dominates. The $Na_{0.95}Pb_{19}SbTe_{21}$ and $Na_{0.80}Pb_{20}Sb_{0.6}Te_{22}$ samples also show low thermal conductivities with a temperature dependence similar to that of Na_{0.95}Pb₂₀SbTe₂₂ (Figure 2 C). For both samples, the thermal conductivity drops very rapidly with rising temperature and reaches a minimum value of $\kappa =$ 0.85 W m⁻¹ K⁻¹ near 700 K. The lattice contribution reaches a minimum of $\kappa_{latt} = 0.55 \text{ W m}^{-1} \text{K}^{-1}$, which approaches the values reported for the superlattice thin films of PbSe_{0.98}Te_{0.02}/ PbTe $(\kappa_{\text{latt}} \approx 0.35 \text{ W m}^{-1} \text{K}^{-1}).^{[11,20]}$

In Figure 2D, the figures of merit for the $Na_{1-x}Pb_mSb_yTe_{m+2}$ samples calculated from the above data are compared to those of the state-of-the-art p-type TAGS and PbTe-based materials. $Na_{0.95}Pb_{20}SbTe_{22}$ outperforms both systems at their individual temperatures of maximum ZT (near 700 K). At 300 K, the figure of merit of $Na_{0.95}Pb_{20}SbTe_{22}$ (ZT \approx 0.25) is already four times larger than that of doped p-type PbTe and 1.3 times larger than that of TAGS. More

interestingly, the figure of merit of Na_{0.95}Pb₂₀SbTe₂₂ rises dramatically with temperature, reaches ZT=1 near 475 K, and then reaches $ZT \approx 1.7$ at 650 K. The figure of merit is above ZT=1 over a temperature range of approximately 300 K. This is one of the widest temperature ranges of high thermoelectric efficiency reported for a single material. Likewise, the figures of merit of Na_{0.95}Pb₁₉SbTe₂₂ and $Na_{0.8}Pb_{20}Sb_{0.6}Te_{22}$ reach their highest values of $ZT\!\approx\!1.5$ and 1.4 at 650 and 640 K, respectively.

Why do the $Na_{1-x}Pb_mSb_yTe_{m+2}$ materials exhibit such good thermoelectric properties? The key characteristic is their exceptionally low thermal conductivity. The thermal conductivity of a material is typically reduced by large massfluctuation disorder in one atomic position of its crystal structure (random-alloy disorder, point defects, and grain boundaries). However, the large drop observed here may suggest the existence of additional mechanisms. Recently, it has been suggested that nanostructuring in bulk samples could produce strong phonon scattering.^[25] While the conventional disorder condition is very likely present in our samples, the presence of nanostructuring can only be probed through a detailed examination of the structure at the atomic scale. Thus, we performed HRTEM on numerous pieces of various $Na_{1-x}Pb_mSb_vTe_{m+2}$ ingots.

HRTEM images of Na_{0.95}Pb₂₀SbTe₂₂ samples, for example, revealed frequent nanoscale features thought to be favorable for phonon scattering. In Figure 3A, two distinct domains with notably different atomic spacings, which have cocrystallized at the nanoscale, can be seen. The corresponding fast Fourier transforms (FFTs) of the two domains in the HRTEM image reveal a doubling of the periodicity in one direction for domain (a) with respect to the cubic spacing of domain (b), which surrounds domain (a). The nanocrystal domains of type (a) have compositions rich in Na and Sb. Figure 3B shows another area of nanoscale inhomogeneity elsewhere in the sample, in which two areas (c) and (d) have different orientations, [111] and [011], as revealed by the corresponding FFTs. The arrows indicate crystal boundaries between domains of similar orientation. Both domains are coherently grown; this feature is called endotaxy and is important in preserving facile charge transport through the sample, owing to reduced scattering. [2,22] This growth process creates interfaces between Na, Sb-rich, and Pb-rich regions. The Pb-rich regions are indicated by the slightly larger lattice spacing evident in the images (PbTe (NaCl type, $Fm\bar{3}m$) has a larger lattice spacing than NaSbTe₂).

The abundance of nano-interfaces is also apparent in the larger-area view shown in Figure 4, in which the degree of dispersity of the nanocrystals can be better assessed. The nanostructuring of $Na_{0.95}Pb_{20}SbTe_{22}$ is a key feature, whose impact on the properties of the material needs to be further understood. To unequivocally support our view that this nanostructuring is largely responsible for the large drop observed in the lattice thermal conductivity in this system, we need the solid-solution version of these materials. The stabilization of real solid solutions of $Na_{1-x}Pb_mSb_vTe_{m+2}$, however, was not possible in our hands. Instead, we can compare the lattice thermal conductivity of Na_{0.95}Pb₂₀SbTe₂₂ with those of the well-known solid solutions of PbTe_{1-x}Se_x and

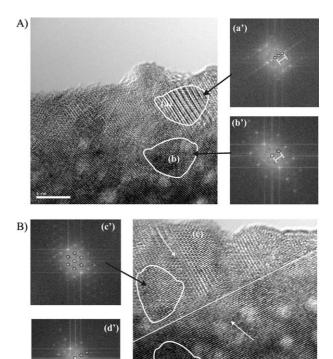


Figure 3. A) HRTEM image (left; scale bar: 5 nm) of a selected part of a Na_{0.95}Pb₂₀SbTe₂₂ sample, showing the coexistence of domains (a) and (b) with different features. The corresponding FFTs (a') and (b') (right) indicate that in one direction the periodicity of domain (a) is doubled compared to that of domain (b) (spacing indicated). B) HRTEM image (right; scale bar: 2 nm) of a selected part of a Na_{0.95}Pb₂₀SbTe₂₂ sample, consisting of two areas (c) and (d). The corresponding FFTs (c') and (d') (left) reveal that area (c) has a [111] orientation and area (d) a [011] orientation. The white arrows in the HRTEM image indicate crystal boundaries between domains of similar orientation. The white line across the HRTEM image, which divides the two areas, is drawn over one atomic row and traverses domains of type (c) and (d), without a shift in atomic row. See Supporting Information for measurement details.[28]

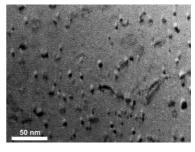


Figure 4. A low magnification TEM image of a Na_{0.95}Pb₂₀SbTe₂₂ sample, showing the evenly dispersed nanoscale features.

 $Pb_{1-x}Sn_xTe$ for x = 0.1. [30,31] This x value represents the same degree of alloying of foreign atoms in the PbTe lattice for all three systems. Given the similar masses of the Sb, Se, and Sn atoms, we can expect that a true solid solution of composition NaPb₂₀SbTe₂₂ (that is, (NaSbTe₂)(PbTe)₂₀) for the same alloy

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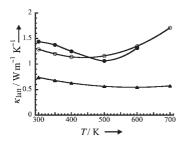


Figure 5. Comparison of the lattice thermal conductivity κ of PbTe_{0.9}Se_{0.1} (∘), Pb_{0.9}Sn_{0.1}Te (●), and Na_{0.95}Pb₂₀SbTe₂₂ (▲). Data for PbTe_{0.9}Se_{0.1} and Pb_{0.9}Sn_{0.1}Te adapted from the literature. [30,31]

fraction would produce a similar phonon scattering to those of PbTe $_{0.9}Se_{0.1}$ and Pb $_{0.9}Sn_{0.1}Te$. This hypothesis is, in fact, supported by the very similar lattice thermal conductivities of $\kappa_{latt} = 1.35$ and $1.44~W~m^{-1}~K^{-1}$ for PbTe $_{0.9}Se_{0.1}$ and Pb $_{0.9}Sn_{0.1}Te$, respectively (Figure 5). Therefore, we expect a true solid solution of composition NaPb $_{20}SbTe_{22}$ to have a comparable lattice thermal conductivity ($\kappa_{latt} \approx 1.4~W~m^{-1}~K^{-1}$), but in contrast, we observe only half this value for Na $_{0.95}Pb_{20}SbTe_{22}$ (Figure 5). Thus, we can provide no other explanation for the reduced thermal conductivity of the Na $_{1-x}Pb_{m}Sb_{y}Te_{m+2}$ materials, but to assign a significant role to the nanostructuring present in the samples.

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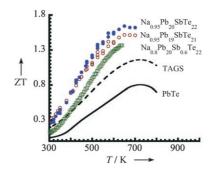
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High Thermoelectric Figure of Merit and Nanostructuring in Bulk p-type $Na_{1-x}Pb_mSb_yTe_{m+2}$



Worthy of merit: The new class of nanostructured p-type thermoelectrics $Na_{1-x}Pb_mSb_vTe_{m+2}$ is reported. The exceptionally high thermoelectric figures of merit ZT of these materials (see graph), which exceed those of the state-of-the-art materials PbTe and $(GeTe)_{1-x}((Ag_2Te)_{1-y}$ $(Sb_2Te_3)_{\gamma})_x$ (TAGS), derive from their very low lattice thermal conductivities.