Higher-Order Leaky-Mode Bessel-Beam Launcher

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Abstract—We present a Bessel-beam launcher based on a leaky radial waveguide consisting of a capacitive sheet over a ground plane that supports higher-order leaky modes. A propagating Bessel beam is generated above the radiating waveguide. The Bessel beam is Transverse Magnetic (TM) polarized with a vertical component of electric field that is a zeroth-order Bessel function of the first kind. A higher-order leaky-wave mode is used to reduce losses at millimeter waves and, at the same time, avoid the thin dielectric layers used in previously proposed lower-order leaky-wave Bessel launchers. Closed-form design equations are provided for the proposed structure. In addition, the operating bandwidth of the launcher is defined using dispersion analysis. Near-field measurements of a prototype operating in the frequency range 38-39.5 GHz validate the concept. The measured launcher generates a Bessel beam with a stable spot size of about 4.3 mm (0.57 λ) over a non-diffractive range of about 16.4 mm (2.2λ) , within about a 4% fractional bandwidth.

Index Terms—Bessel beams, near-field focusing, artificial surface, leaky waves, high-order modes, millimeter waves.

I. INTRODUCTION

HE non-diffractive behavior and focusing/collimating capabilities of Bessel beams make them attractive for a wide range of applications at millimeter waves. In particular, the non-diffractive property may open new possibilities in medical and security imaging, optical manipulation, confinedbeam spectroscopy, etc. [1]-[7]. In brief, ideal Bessel beams are monochromatic localized solutions [8], [9] to the scalar wave equation that do not undergo diffractive spreading when propagating in free space [10]. An infinite radiating aperture is required for the generation of ideal Bessel beams. In practice, it is possible to generate Bessel beams using finite-size radiating aperture at the expense of a limited non-diffractive range. A rigorous vector analysis of the generation of Bessel beams by finite apertures can be found in [5], and [11]-[13], which avoids the paraxial approximation of earlier works [10], [14], [15].

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A vector analysis of a Bessel-beam launcher working at around 10 GHz is reported in [16] and [17]. It consists of a leaky-wave radial waveguide loaded by an impedance sheet, shown in Fig. 1. In these papers, the lowest-order azimuthallyinvariant TM (with respect to z axis) leaky mode is excited centrally by a coaxial probe. A metallic rim at the edge of the structure is used to reflect an outward going cylindrical wave launched by the feed in order to generate a radiated vertical electric field E_z with a J_0 profile, and a radial field E_ρ with a J_1 profile (zeroth- and first-order Bessel function of the first kind, respectively). Simple design rules are provided, based on the required Bessel profile.

The single mode operation of the launcher in [16] and [17] restricts the separation between the impedance sheet and ground plane of the radial waveguide to thicknesses much smaller than the operating wavelength. Scaling the structure to the millimeter-wave range would require extremely thin waveguides (e.g., a thickness of the dielectric substrate equal to $37.6 \ \mu m$ at $f = 40 \ \text{GHz}$) leading to restrictively high ohmic losses [18] and practical mechanical problems.

For this reason, here we propose a Bessel-beam launcher at millimeter waves using higher-order TM leaky modes. The structure is again based on a radial waveguide loaded by a capacitive sheet. However, in contrast to the previous designs [16], [17], larger separation distances (on the order of half the wavelength) are considered between the ground plane and the impedance sheet. The launcher can then support higher-order leaky modes and possibly surface waves. A completely novel design approach is thus proposed based on dispersion analysis. Suitable closed-form equations are derived to establish the annular spectrum needed for the generation of propagating



Fig. 1. Illustration of the leaky-mode Bessel-beam launcher under consideration. The red arrows show the outward and inward cylindrical waves launched within the structure by a central coaxial probe. The interference of these cylindrical waves creates a Bessel beam.

Bessel beams.

The use of higher-order modes requires a frequency range where the presence of lower-order modes and possible surface waves does not affect the pattern of the generated Bessel beam. A bandwidth of operation of the proposed structure is then derived and verified.

The proposed concept and design relations are experimentally validated with a prototype operating at 38.3 GHz, which is fabricated using a standard Printed Circuit Board (PCB) fabrication process. Measurements of the vertical electric field demonstrate that, within the considered band (38-39.5 GHz), the generated Bessel beam presents a stable spot size. These results may pave the way for the generation of other kinds of localized waves and in particular X-waves that are a combination of propagating Bessel beams in a defined frequency range [8], [9].

The paper is organized as follows. In Section II, the leaky radial waveguide is presented. In Section III, a modal analysis is outlined and used to derive design equations for the launcher operating with higher-order modes. The maximum achievable bandwidth of the device is also provided. Section IV describes the design of a higher-order Bessel-beam launcher operating at 38.3 GHz. In Section V the prototype is reported, and measurement results are shown that validate the design. Finally, conclusions are drawn in Section VI.

II. LEAKY RADIAL WAVEGUIDE

This section briefly summarizes the design principles for the generation of a Bessel beam using a launcher that supports lower-order leaky-wave modes [16]. In particular, we consider a TM propagating Bessel beam whose vertical component (zcomponent in Fig. 1) of the electric field E_z assumes a zerothorder Bessel function of the first-kind $J_0(k_\rho\rho)$, where k_ρ is the transverse propagation constant of the generated beam. As presented in [16], the radiated E_z field can be expressed as a superposition of an outward traveling cylindrical wave $(A_2H_0^{(2)}(k_\rho\rho))$, a zeroth-order Hankel function of the second kind) and of an inward wave $(A_1 H_0^{(1)}(k_\rho \rho))$, a zeroth-order Hankel function of the first kind), whose amplitude coefficients $(A_1 \text{ and } A_2)$ are stipulated by the boundary conditions and excitation. A Bessel function J_0 can then be generated when the amplitude coefficients are the same $(A_1 = A_2)$. In this case, the required Bessel function $J_0(k_{\rho}\rho)$ is generated by placing a circular metallic rim at the radial location (ρ) of one of the zeros of $J_0(k_\rho\rho)$. The required equations to establish the condition $A_1 = A_2$ can be found in [16], and are reported here for completeness:

$$\beta_{\rho}\rho_{\rm ap} \simeq m\pi - \pi/4 \qquad m = 1, 2, \dots$$
 (1)

$$\alpha_{\rho}\rho_{\rm ap} \ll 1 \tag{2}$$

where $\rho_{\rm ap}$ is the rim radius, and β_{ρ} and α_{ρ} are the real and imaginary part of the radial wavenumber, respectively: $k_{\rho} = \beta_{\rho} - j\alpha_{\rho}$. These conditions require that the outward and inward modes are out of phase at $\rho_{\rm ap}$ and slowly attenuated. The rim radius ρ_{ap} is also related to the non-diffractive range z_{ndr} of the generated Bessel beam through [10]

$$z_{\rm ndr} = \rho_{\rm ap} \sqrt{\left(\frac{k_0}{\beta_{\rho}}\right)^2 - 1},\tag{3}$$

where k_0 is the free-space wavenumber. As a result, the nondiffractive range can be tuned by varying the value of the transverse propagation constant β_{ρ} . Alternatively, if β_{ρ} and the frequency are fixed, it is possible to obtain larger nondiffractive distances with larger apertures, provided that (1) and (2) are still satisfied. Note that a larger non-diffractive range may be also achieved at the expenses of a wider spotsize. The null-to-null beamwidth (NNBW) is given by

$$\text{NNBW} = \frac{2\chi_{0,1}}{\beta_{\rho}},\tag{4}$$

where $\chi_{0,1} = 2.4048$ is the first null of the J_0 function. Hence, a trade-off exists between the beam size and the maximum non-diffractive range, for a fixed launcher radius.

III. DESIGN OF THE STRUCTURE

In order to investigate the modal properties of the waves supported by the structure in Fig. 1, we solve the dispersion equation of the radial waveguide for TM modes [16], [19]. In the general case of a dielectric-filled leaky radial waveguide the dispersion equation can be expressed by standard transverse resonance technique [20] as

$$Y_{air} + Y_s - jY_0\varepsilon_r \cot(k_{z1}h) = 0, \tag{5}$$

where $Y_0 = \omega \varepsilon_0 / k_{z1}$, $Y_{air} = \omega \varepsilon_0 / k_z$ are the characteristic admittances in the slab and free-space (air), respectively and Y_s is the sheet admittance [16]; $k_{z1} = \sqrt{k_0^2 \varepsilon_r - k_\rho^2}$ and $k_z = \sqrt{k_0^2 - k_\rho^2}$ are the vertical wavenumbers in the slab and in the air, respectively, which are generally complex quantities $(k_z = \beta_z - j\alpha_z, k_{z1} = \beta_{z1} - j\alpha_{z1})$. In the following, we will use wavenumbers normalized with respect to k_0 (identified with a hat) for the sake of simplicity.

In order to solve the dispersion equation for k_{ρ} , the values of Y_s and h are needed. Conversely, these parameters can be found through (5) once the transverse k_{ρ} or the vertical k_z propagation constants of the required Bessel beam are fixed, together with the operating frequency f_0 , and the dielectric constant ε_r . Note that when the so-calculated values (Y_s and h) are used to solve (5), they give rise to the previously fixed k_{ρ} at the operating frequency f_0 .

In Subsection III.A, we develop simple closed forms in order to determine Y_s and h as functions of ε_r , k_ρ , and f_0 using (5). In Subsection III.B, we replace these values in the dispersion equation to discuss the overall modal properties of the structure, thus gaining physical insight about the possible excitation of Bessel beams. In Subsection III.C, we provide simple closed-form expressions for the determination of the maximal available bandwidth of the structure.

A. Closed-form expressions for X_s and h

By assuming that the argument of the cotangent function is close to a multiple n = 0, 1, 2, ... of π [21], a first-order approximation of the cotangent function in (5) can be made,

$$Y_{air} + Y_s - \frac{jY_0\varepsilon_r}{k_{z1}h - n\pi} = 0.$$
 (6)

For typical values of the dielectric constant and the radial wavenumber, this approximation is justified when $|k_{z1}h|$ is close to $n\pi$. Furthermore, assuming that the impedance sheet is purely reactive $Y_s = jB_s = -jX_s^{-1}$ (as required to support a TM leaky mode [22]), the approximate dispersion equation (6) becomes

$$\frac{1}{\hat{k}_{z}} - j\frac{\eta_{0}}{X_{s}} - \frac{j\varepsilon_{r}}{\hat{k}_{z1}} \left(\frac{1}{k_{0}\hat{k}_{z1}h - n\pi}\right) = 0,$$
(7)

where $\eta_0 = k_0/\omega\varepsilon_0$ is the free-space characteristic impedance and *n* is related to the modal vertical integer index. Following the same procedure outlined in [16], we can rearrange the terms in (7) and solve for X_s ,

$$X_{s} = -\frac{\hat{k}_{z1}}{\hat{k}_{z}\epsilon_{r}}(jX_{s} + \eta_{0}\hat{k}_{z})(k_{0}\hat{k}_{z1}h - n\pi).$$
 (8)

After some algebraic manipulations, a quadratic equation in h is obtained,

$$a_2h^2 + a_1h + a_0 = 0 \tag{9}$$

where

$$a_{2} = k_{0}^{2} [2\hat{\alpha}_{z1}\hat{\beta}_{z1}w_{1} - (\hat{\beta}_{z1}^{2} - \hat{\alpha}_{z1}^{2})z_{1}]$$

$$a_{1} = k_{0} \{2\epsilon_{r}\hat{\alpha}_{z1}\hat{\beta}_{z1}(\hat{\beta}_{z}^{2} + \hat{\alpha}_{z}^{2})$$

$$- n\pi [2\hat{\alpha}_{z1}\hat{\beta}_{z1}w_{2} + \hat{\alpha}_{z1}w_{1} - z_{2}(\hat{\beta}_{z1}^{2} - \hat{\alpha}_{z1}^{2}) - z_{1}\hat{\beta}_{z1}]\}$$

$$a_{0} = -n\pi [\epsilon_{r}\hat{\alpha}_{z1}(\hat{\beta}_{z}^{2} + \hat{\alpha}_{z}^{2}) + n\pi (\hat{\beta}_{z1}z_{2} - \hat{\alpha}_{z1}w_{2})], \quad (10)$$

with:

$$w_{1} = (-\hat{\alpha}_{z}\hat{\alpha}_{z1}^{2} + \hat{\alpha}_{z}\hat{\beta}_{z1}^{2} - 2\hat{\alpha}_{z1}\hat{\beta}_{z1}\hat{\beta}_{z})$$

$$w_{2} = (\hat{\beta}_{z1}\hat{\alpha}_{z} - \hat{\beta}_{z}\hat{\alpha}_{z1})$$

$$z_{1} = (\hat{\beta}_{z}\hat{\beta}_{z1}^{2} - \hat{\beta}_{z}\hat{\alpha}_{z1}^{2} + 2\hat{\alpha}_{z1}\hat{\alpha}_{z}\hat{\beta}_{z1})$$

$$z_{2} = (\hat{\beta}_{z1}\hat{\beta}_{z} + \hat{\alpha}_{z1}\hat{\alpha}_{z}).$$
(11)

Finally, by solving (8) and (9) we get:

$$h = \frac{-a_1 \pm \sqrt{a_1^2 - 4a_2 a_0}}{2a_2} \tag{12}$$

$$X_s = -\frac{\eta_0 \hat{\alpha}_{z1} (2k_0 h \hat{\beta}_{z1} - n\pi) (\hat{\beta}_z^2 + \hat{\alpha}_z^2)}{k_0 h z_1 - n\pi z_2}$$
(13)

It is easy to verify that for n = 0 and $\varepsilon_r = 1$ these results coincide with those presented in [16] for the lowest-order leaky-mode launcher. However, in contrast to earlier works [3], [16], higher-order leaky-wave Bessel-beam launchers can generate non-diffractive radiation for two different impedance values (see Eqs. (12) and (13)) and corresponding substrate heights. This gives designers an additional degree of freedom during the design process.



Fig. 2. (a) Normalized phase constant and (b) normalized attenuation constant vs. frequency f from DC to 100 GHz for the first TM modes of a partiallyopen layered structure as in Fig. 1. The solid and dashed lines denote the dispersion curves for the proper and improper modes, respectively. The black and grey curves represent the dispersion curves for the real and complex modes, respectively. Hence surface-wave (SW) modes are shown by black solid lines, whereas the leaky-wave (LW) modes are shown by grey dashed lines. In these plots, it is assumed that $X_s = -25 \ \Omega$, $\varepsilon_r = 2.17$, h = 3.175 mm.

B. Modal analysis

The modes supported by the partially-open layered structure are computed by numerically solving eq. (5). The values of X_s and h are derived using (12), (13) for a tangential wavenumber $k_{\rho} = (0.8 - j0.007)k_0$ at $f \simeq 40$ GHz and $\varepsilon_r = 2.17$. This set of parameters does not limit the general discussion presented in this subsection, since the dispersion diagrams of the structure are qualitatively very similar for a large range of parameters. The numerical parameters chosen here were used for the realized prototype described in Sections IV and V.

Figs. 2(a) and 2(b) provide the normalized phase constant β_{ρ}/k_0 and attenuation constant α_{ρ}/k_0 as functions of the frequency f. Three leaky-wave (LW) modes are observed. By setting $k_{\rho} = 0$ in (5), an approximate expression can be obtained for the cutoff frequencies

$$f_n^{\text{LW}} \simeq \frac{c}{2\pi h\sqrt{\varepsilon_r}} \cot^{-1}\left(\frac{-\eta_0}{X_s \epsilon_r}\right) + \frac{nc}{2h\sqrt{\varepsilon_r}}$$
(14)

where c is the light velocity in vacuum. The phase constant of each leaky-wave mode above cutoff varies in the range approximately from 0 to k_0 . As is typical [19], [22]–[25], slightly after $\beta_{\rho} > k_0$, the two conjugate leaky poles merge, and afterwards give rise to a couple of purely real improper (nonphysical) poles. Specifically, one real improper pole (with a β_{ρ} greater than k_0) has a decreasing β_{ρ} with respect to the frequency, until it reaches the value $\beta_{\rho} = k_0$. At this point, the real improper mode becomes a real proper pole, i.e. a physical surface wave guided at the interface, whose β_{ρ} tends to the asymptotic value of $k_0\sqrt{\varepsilon_r}$ [19], [22]–[25]. The cutoff frequency of this surface-wave (SW) mode can be determined by replacing β_{ρ} with k_0 in the dispersive equation. Note that a zeroth-order surface wave propagates from DC frequency, since

$$f_n^{\rm SW} \simeq \frac{nc}{2h\sqrt{\varepsilon_{\rm r} - 1}}$$
 (15)

Since small values of α_{ρ} are always required to launch a Bessel profile with the proposed leaky radial waveguide [16], each leaky-wave mode can be used only at frequencies $f > f_n^{LW}$. As is known [26], slow improper waves do not actually contribute to the aperture field, but conversely the excitation of proper surface waves can deteriorate the profile of the generated Bessel beam. It is then important to define the frequency band where a mono-modal leaky-wave propagation can be obtained.

C. Determination of the maximal available bandwidth

As was noted in Section II, in order to create a Bessel beam, a circular metallic rim is placed at a radial distance $\rho_{\rm ap}$ corresponding to a null of the required zeroth-order Bessel function, i.e.

$$\frac{\beta_{\rho}}{k_0} = \frac{\chi_{0,q}}{\rho_{\rm ap}k_0} \quad q = 1, 2, \dots$$
(16)

where $\chi_{0,q}$ is the *q*-th zero of J_0 . The above relation is represented by hyperbolic curves (dashed line in Fig. 3). The intersections with the first higher-order (n = 1) leaky-wave (LW_1) and zeroth-order (n = 0) surface-wave (SW_0) phase constants (see also Fig. 2(a)) identify a grid of resonant modes of the radially waveguide with a metallic rim, as shown in Fig. 3.

The intersection of these curves with the required leakywave mode (here n = 1) defines the operating frequency f_0 of the Bessel-beam launcher, and the operating phase constant $\hat{\beta}_0 = \hat{\beta}(f_0)$. In addition, we can define the maximum available bandwidth B_{av} for mono-modal operation as the smallest frequency range containing f_0 and delimited at its ends by adjacent intersections with the adjacent resonant modes. It should be stressed that this maximum theoretical bandwidth should not be confused with the practical bandwidth of the launcher, which will likely be narrower and limited by the input impedance match and the frequency dependence of the artificial surface.

In Fig. 3, it is clear that the lower bound of $B_{\rm av}$ is given by $f_{\rm low} = \max\{f_{\rm inf}^{\rm SW0}, f_{\rm inf}^{\rm LW1}\}$, whereas the upper bound is given by $f_{\rm high} = \min\{f_{\rm sup}^{\rm SW0}, f_{\rm sup}^{\rm LW1}\}$. These four frequencies can be expressed through simple closed-form relationships. In fact by exploiting the asymptotical periodicity of the zeros of the Bessel functions [27], i.e.

$$\chi_{0,q+1} - \chi_{0,q} \simeq \pi \tag{17}$$



Fig. 3. Dispersion curves for the design of the higher-order launcher prototype. The operating points are given by the intersections of the fast leaky-wave modes and the hyperbolic curves given by the Bessel zeros. Once the operating point is chosen, the operating bandwidth is fixed by the closest intersections of either the fast leaky-wave or the surface-wave modes. The parameters used in Fig. 2 are also assumed here.

from (16) the vertical distance Δ between two consecutive hyperbolas at a given frequency f is given by

$$\Delta(f) = \frac{\chi_{0,q+1}}{\rho_{\rm ap}k_0} - \frac{\chi_{0,q}}{\rho_{\rm ap}k_0} \simeq \frac{c_0}{2\rho_{\rm ap}f}.$$
 (18)

By assuming a nearly linear leaky-wave phase constant between $f_{\rm inf}^{\rm LW1}$ and $f_{\rm sup}^{\rm LW1},$ we get

$$f_{\text{inf,sup}}^{\text{LW1}} = f_0 \pm \frac{\Delta(f_0)}{\xi + \psi},\tag{19}$$

where

$$\xi = \frac{d\beta_{\rho}^{\text{LW1}}(f)}{df}\Big|_{f_0}, \quad \psi = \frac{\chi_{0,q}c_0}{2\pi\rho_{\text{ap}}f_0^2}.$$
 (20)

Moreover, if the fundamental surface-wave phase constant is close to the asymptotic value $\hat{\beta}_{\rho}^{SW0} \simeq \sqrt{\varepsilon_r}$, we have

$$f_{\rm inf}^{\rm SW0} = \frac{\chi_{0,r}c_0}{2\pi\rho_{\rm ap}}, \ f_{\rm sup}^{\rm SW0} = \frac{\chi_{0,r+1}c_0}{2\pi\rho_{\rm ap}}$$
 (21)

where

1

$$r = \left\lfloor \frac{\rho_{\rm ap} k_0 \delta \beta^{\rm SW0}(f_0)}{\pi} \right\rfloor,\tag{22}$$

 $\delta\beta^{\text{SW0}}(f_0) = \sqrt{\varepsilon_r} - \hat{\beta}_0$ being the phase difference between the leaky wave and the fundamental surface wave at the operating frequency f_0 , and $\lfloor \cdot \rfloor$ is the floor function.

IV. NUMERICAL VALIDATION

A. Design procedure for the Bessel-beam launcher

A leaky radial waveguide exciting a Bessel beam with $k_{\rho} = (0.8 - j0.007)k_0$ around the operating frequency of $f_0 = 39.7$ GHz has been designed to validate the results of the previous section. The value of $\rho_{\rm ap}$ is fixed by f_0 , whereas h, X_s are derived using (12) and (13) once the radial (q) and vertical (n) order of the resonance are chosen. A choice of q = 5, the fifth



Fig. 4. Radial behavior of the normalized electric field $|E_z|$ at f = 39.7 GHz, for the launcher under analysis (parameters as in Fig. 2), for various distances from the aperture, computed using COMSOL Multiphysics.

zero of the Bessel function, and n = 1, the first higher-order leaky-wave mode, leads to the following set of parameters:

$$\rho_{\rm ap} = 22.3 \text{ mm},$$

 $h = 3.175 \text{ mm},$

 $X_s = -25 \Omega$
(23)

where we have considered a dielectric substrate with a relative permittivity $\varepsilon_r = 2.17$ as in Section III. These values lead to the desired operating point with a relative accuracy on the order of 1%, in agreement with the small-argument firstorder approximation of the cotangent function made in Subsection III-A. The dispersion diagram of the structure in the range of interest is shown in Fig. 3. Note that a mono-modal propagation is obtained between frequencies $f_{\rm low} = 37.3$ GHz and $f_{\rm high} = 40.3$ GHz, respectively.

The operation of the structure as a Bessel-beam launcher has been validated numerically using COMSOL Multiphysics [28]. The artificial surface is modeled as an infinitesimally thin layer. In Fig. 4, the computed normalized vertical electric field $E_z(\rho)$ at different distances (z) from the radiating aperture is shown. Clearly, a Bessel beam is generated at the expected frequency f = 39.7 GHz. The typical Bessel function J_0 profile is observed up to the non-diffractive range, equal to 16.4 mm $\simeq 2.2\lambda_0$ ($\lambda_0 = 7.5$ mm, at $f_0 = 40$ GHz), where the sidelobes are no longer clearly distinct, and the main beam starts to widen. This behavior is evident in Fig. 5(a), which shows the same electric field component in a 2-D plot along the ρz -plane. The full-wave simulation confirms the operation of the radial waveguide as a Bessel-beam launcher.

B. Bandwidth verification

In this subsection, 2-D plots of E_z along the ρz -plane are shown at both the lower $f_{\rm low}$ and higher $f_{\rm high}$ limits of the maximum available bandwidth, in order to validate the closedform expressions (19) and (21) for the bandwidth. At the lower limit $f_{\rm low} = 37.3$ GHz, the radiated E_z field has a larger beamwidth (see Fig. 5(b)). This is due to the smaller transverse propagation constant of the leaky-wave mode which intersects the hyperbolic curve corresponding to q = 4. At the upper end, $f_{\rm high} = 40.3$ GHz, the E_z radiated field is spoiled by the excitation of a surface wave, and hence no useful focused beam is generated (see Fig. 5(c)). However, within the maximum available bandwidth 37.3 - 40.3 GHz, a Bessel beam with a quasi-constant spot size can be observed, as confirmed in the following section by experimental tests.

V. PROTOTYPE AND MEASUREMENTS

A. Realization

The Bessel launcher designed in the previous section has been fabricated using a PCB process at IETR, Rennes, France. The radial waveguide consists of a substrate with permittivity $\varepsilon_{\rm r} = 2.17$ (Neltec NY9217) and height h = 3.175 mm. The sheet reactive impedance $(X_s \simeq -25 \ \Omega)$ is realized by etching a two-dimensional array of interleaved squared metallic patches [17] (see Fig. 6) with a periodicity $p = 750 \ \mu {\rm m}$ $(\lambda_0/10 \ {\rm at} \ f_0 = 40 \ {\rm GHz})$ and a border distance $d = 50 \ \mu {\rm m}$ on a double-side patterned substrate of permittivity $\varepsilon_{\rm r} = 6.15$ (Rogers Duroid 6006) and height $h_{\rm FSS} = 0.127 \ {\rm mm}$. Fullwave simulations with Ansys HFSS [29] have been used to design the impedance sheet [30]. The impedance sheet has been glued to the radial waveguide using an adhesive layer Taconic fastRise FR-27-0030-25 of permittivity $\varepsilon_{\rm r} = 2.78$



Fig. 5. Contour plot of the electric field $|E_z|$ along the ρz -plane for the mm-wave launcher under analysis at (a) f = 39.7 GHz, (b) f = 37.3 GHz, and (c) f = 40.3 GHz.

TABLE I GEOMETRICAL DIMENSIONS FOR THE MATCHING NETWORK OF THE MM-WAVE BESSEL-BEAM LAUNCHER





Fig. 6. Schematic of the coaxial probe transition used for matching the mm-wave launcher.

and thickness $h_{glue} = 86 \ \mu m$. A commercial connector (SRI Connector Gage 85131100080) has been used to feed the structure from the back side of the launcher. For matching purposes, the geometry of the impedance surface has been modified close to the inner probe of the coaxial connector, as shown in detail in Fig. 6. In fact the radius of the metallic disk $r_{\rm disk1}$ and its distance from the adjacent patches are critical parameters for impedance matching. The final design parameters are reported in Table I. It should be noted that the inner probe of the coax is only connected to the upper layer of the impedance sheet. The stacked structure is placed within a circular waveguide of radius $\rho_{\rm ap}$. The final prototype is shown



Fig. 7. Prototype of the mm-wave leaky-mode Bessel-beam launcher. The feeding probe can be recognized at the center of the structure.



Fig. 8. (a) Measured reflection coefficient ($|S_{11}|$ in dB) of the prototype in the frequency range $37 \div 40$ GHz. The blue region highlights the frequency range for which the return loss is under -10 dB. (b) Effects of fabrication tolerances for the launcher under analysis. Dispersion curves within the frequency range $36 \div 42$ GHz. The dashed and solid lines denote the dispersion curves for the realized impedance sheet with a patched period of $p = 750 \ \mu m$ and $p = 700 \ \mu m$, respectively. The distance d is equal to $50 \ \mu m$, in both cases. A shift of the operating point from f = 39.7 GHz down to f'' = 38.3 GHz is observed.

in Fig. 7. The prototype has been measured in the frequency range 38 – 39.5 GHz with a frequency step of 100 MHz, and compared with full-wave results of the complete structure performed in HFSS. The vertical component of the electric field E_z has been measured above the prototype, using a small electric probe scanning an area of 45 mm × 45 mm with a step of 0.75 mm at six different z-planes starting from 3.75 mm ($\lambda_0/2$) up to 18 mm ($5\lambda_0/2$), in order to verify the Bessel beam generation. This probe is made of a semirigid coaxial cable (UT-85) with the inner conductor extending 0.75 mm ($\lambda_0/10$ at $f_0 = 40$ GHz) beyond the outer conductor and dielectric. In addition, the E_z component has been also measured along the xz-plane ($\phi = 0^{\circ}$) in order to highlight the overall non-diffractive behavior of the generated Bessel beam within the expected non-diffractive range.

Through measurements, a minimum in reflection coefficient of the prototype was found at a frequency of $f_m = 38.3$ GHz



Fig. 9. Measured patterns of the normalized E_z component of the electric field at f = 38.3 GHz at three different distances $z = 0.5 \lambda_0, 0.75 \lambda_0, 1 \lambda_0$ from the impedance surface, where λ_0 equal to 7.5 mm. (a)-(c) Contour plots of the measured field. (d)-(f) A comparison between measurements and simulations along different azimuthal ϕ planes.

as shown in Fig. 8(a). Around this frequency, the measured $|S_{11}|$ shows a $-10 \,\mathrm{dB}$ fractional bandwidth of approximately 3.7%. It is noted that f_m is shifted of 2.5% relative to the expected operating frequency f_0 . This frequency shift may be attributed to fabrication tolerances. Indeed, by assuming a systematic error of 50 μm (a value that fits the PCB industry standard tolerances) for the realization of the periodic impedance sheet in the dispersion analysis of the prototype, as shown in Fig. 8(b), an operating point f'' equal to 38.3 GHz is found (see solid line in Fig. 8(b)), in agreement with the 2.5% shift observed in measurements. Therefore, in the following subsections we provide measurements results within the measured frequency range 38 - 39.5 GHz, with an operating frequency equal to $f_m = 38.3 \,\text{GHz}$. It is worth mentioning that fabrication tolerances also affect the available bandwidth (refer to Subsection III-C) by shifting downward the lower limit of the bandwidth to f = 36.4 GHz. On the other hand, the upper limit remains unaffected.

B. Bessel beam profile

Contour plots of the measured E_z component of the electric field above the aperture are shown in Figs. 9(a)-(c) at various distances ($z = 0.5 \lambda_0, 0.75 \lambda_0, 1.0 \lambda_0$, where λ_0 is equal to 7.5 mm) from the radiating aperture at the operating frequency 38.3 GHz. An azimuthally symmetric Bessel beam is clearly shown. In particular, it is possible to distinguish the five dark rings corresponding to the five nulls of the Bessel function.

Figs. 9(d)-(f) provide detailed measurements of the normalized E_z component along various azimuthal planes at fixed distances from the radiating aperture. Full-wave results (HFSS) are also provided for comparison. Measurements and simulations are in very close agreement, thereby validating the proposed analysis and design procedures.

Finally, Fig. 10 provides the measured E_z field component along the xz-plane. As expected, the spot size represented here by the Half-Power Beamwidth (HPBW) and the Bessel profile are preserved along the axis of propagation up to the non-diffractive range z = 16.4 mm (marked with a white line). Above this distance, diffraction prevails, and the beam starts to widen.



Fig. 10. Contour plots of the measured E_z component of the normalized electric field at f = 38.3 GHz along the xz-plane. The figure confirms the limited-diffraction behavior of the launcher.



Fig. 11. Variation of the HPBW with frequency for the mm-wave launcher prototype. Full-wave simulation results are shown with dashed lines from 37 to 41 GHz. Measurements are shown with circles, from 38 GHz to 39.5 GHz. The vertical lines mark the extrema of the maximum available bandwidth, as predicted by (19) and (21).

C. Beamwidth variation versus frequency

In this section, the variation of the measured HPBW with the frequency at a fixed distance $(z = \lambda_0)$ from the radiating aperture is reported, and compared to full-wave simulation results (HFSS). As predicted by (4), due to the dispersive behavior of β_{ρ} , both the simulated (see dashed line in Fig. 11) and the measured HPBW (see circles in Fig. 11) decrease monotonically slowly with frequency, within the maximum available bandwidth (37.3-40.3 GHz) given by (19) and (21). Moreover, the measured HPBW remains quasi-stable over the restricted frequency range 38 – 39.5 GHz with a variation coefficient (CV):

$$CV = \frac{\sigma_{HPBW}}{\overline{HPBW}} \simeq 1.1\%$$
 (24)

being $\sigma_{\rm HPBW} \simeq 50 \ \mu {\rm m}$ the standard deviation of the measured HPBW, and $\overline{\rm HPBW} \simeq 4.3 \ {\rm mm}$ is its mean value.

In contrast to [17], the Bessel beam profile is not only verified along the axis of propagation within the non-diffractive range at the operating frequency, but also over a considerable bandwidth.

VI. CONCLUSION

We have presented the design and implementation of a leaky radial launcher operating in the millimeter-wave range that supports higher-order leaky modes in order to generate propagating Bessel beams. Higher-order leaky modes allow for suitable designs with PCB fabrication. In particular, the substrate thickness is no longer impractically thin, with consequent reduced losses if compared to lower-order leaky-wave launcher design. The proposed modal analysis has shown that an operating bandwidth exists over which the simultaneous presence of surface waves and dominant (lower-order) leaky modes does not affect the generation of the Bessel beam. Simple closed formulas useful for the design and for the limits of the frequency band have been provided.

Measurement results of a prototype operating around 38.3 GHz have confirmed the proposed analysis and design.

In particular, it has been verified that within the defined bandwidth, the generated Bessel beam maintains a quasiconstant spot size. The possibility of generating zeroth-order Bessel beams with fixed a spot size over a certain bandwidth can also pave the way for the creation of soliton-like solutions, such as X-shaped pulses.

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