Hotspot conditions achieved in inertial confinement fusion experiments on the National Ignition Facility

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🔟 P. K. Patel, P. T. Springer, 🔟 C. R. Weber, et al.

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P. K. Patel,^{1,a),b)} P. T. Springer,¹ C. R. Weber,¹ L. C. Jarrott,¹ O. A. Hurricane,¹ B. Bachmann,¹ K. L. Baker,¹ L. F. Berzak Hopkins,¹ D. A. Callahan,¹ D. T. Casey,¹ C. J. Cerjan,¹ D. S. Clark,¹ E. L. Dewald,¹ L. Divol,¹ T. Döppner,¹ J. E. Field,¹ D. Fittinghoff,¹ J. Gaffney,¹ V. Ceppert-Kleinrath,² G. P. Grim,¹ E. P. Hartouni,¹ R. Hatarik,¹ D. E. Hinkel,¹ M. Hohenberger,¹ K. Humbird,¹ N. Izumi,¹ O. S. Jones,¹ S. F. Khan,¹ A. L. Kritcher,¹ M. Kruse,¹ O. L. Landen,¹ S. Le Pape,^{1,3} T. Ma,¹ S. A. MacLaren,¹ A. G. MacPhee,¹ L. P. Masse,¹ N. B. Meezan,¹ J. L. Milovich,¹ R. Nora,¹ A. Pak,¹ J. L. Peterson,¹ J. Ralph,¹ H. F. Robey,¹ J. D. Salmonson,¹ V. A. Smalyuk,¹ B. K. Spears,¹ C. A. Thomas,⁴ D. P. L. Volegov,² A. Zylstra,¹ D and M. J. Edwards¹

AFFILIATIONS

¹Lawrence Livermore National Laboratory, Livermore, California 94551, USA

²Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

³Laboratoire pour L'Utilisation des Lasers Intenses, Ecole Polytechnique, 91128 Palaiseau Cedex, France

⁴Laboratory for Laser Energetics, University of Rochester, Rochester, New York 14620, USA

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^{a)}Invited speaker.

^{b)}Author to whom correspondence should be addressed: patel9@llnl.gov

ABSTRACT

We describe the overall performance of the major indirect-drive inertial confinement fusion campaigns executed at the National Ignition Facility. With respect to the proximity to ignition, we can describe the performance of current experiments both in terms of no-burn ignition metrics (metrics based on the hydrodynamic performance of targets in the absence of alpha-particle heating) and in terms of the thermodynamic properties of the hotspot and dense fuel at stagnation—in particular, the hotspot pressure, temperature, and areal density. We describe a simple 1D isobaric model to derive these quantities from experimental observables and examine where current experiments lie with respect to the conditions required for ignition.

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I. INTRODUCTION

The indirect-drive approach to inertial confinement fusion (ICF) aims to achieve ignition through the spherical compression of a deuterium–tritium (DT) filled capsule driven by x rays generated from the laser irradiation of a high-Z hohlraum.^{1,2} Since the beginning of the experimental program following the completion of the National Ignition Facility (NIF) in 2009, considerable progress has been made both in our understanding of the implosion behavior and in the overall performance attained. The highest yield to date has increased by more than $20 \times$ from the end of the first campaign in 2012, reaching 2.0×10^{16} neutrons or a fusion energy of 55 kJ. While the total yield

produced by an implosion provides an essentially unambiguous yardstick for whether or not the implosion has ignited, given the implicit threshold behavior of ignition, the total yield is not the best quantitative measure of the proximity, or gap, to ignition. For this assessment, other metrics based on power balance in the hotspot or the yield amplification from equivalent no - burn implosions, i.e., hydrodynamically equivalent implosions with alpha-heating artificially turned off, can be more meaningful.

The purpose of this paper is to summarize the overall performance of DT-layered experiments at the NIF in terms of the hotspot conditions produced at stagnation and the implications for the proximity to ignition. We begin with a brief introduction to the major implosion campaigns. In Sec. II, we describe the method used to infer no-burn ignition metrics and yield amplification. In Sec. III, we describe a static hotspot model used to infer hotspot properties including pressure, temperature, and areal density. Finally, in Sec. IV, we employ a dynamic model to relate these inferred hotspot properties to those required for ignition.

We first summarize the performance of the four major campaigns performed at the NIF since 2009. Two of these used a plastic (CH) ablator and the other two a high-density-carbon (HDC) ablator. Figure 1 shows the overall performance of the experiments in these campaigns in terms of the measured neutron yield and downscattered ratio (DSR). The DSR is the ratio of observed neutrons with energies between 10 and 12 MeV over 13-15 MeV and is an approximate measure of the total DT fuel areal density $\left[\rho R_{tot} \left(g/cm^2\right)\right]$ $\approx 21 \times DSR$].³ In this parameter space, contours can be drawn of constant yield amplification for a given DT fuel mass (the method for calculating these contours is described in Sec. II). For each level of yield amplification shown, the lower line corresponds to a DT fuel mass of 138 μ g, the typical value used in the HDC designs, and the upper line corresponds to a DT fuel mass of 180 μ g, typically used in the CH designs. The original CH 4-shock low-foot (CH LF) design, with a design adiabat of $\alpha \sim 1.6$, achieved relatively high values of DSR in the range of DSR \sim 4%–6%, equivalent to fuel areal densities of $\rho R_{tot} \sim 0.8 - 1.2 \,\mathrm{g/cm^2}$, but the maximum yield was limited to 9×10^{14} neutrons, in large part because of high levels of radiation



FIG. 1. Performance of DT implosion experiments in terms of total neutron yield and neutron down-scattered ratio. Dotted lines represent the contours of yield amplification due to alpha-particle self-heating. For each level of yield amplification, the lower line corresponds to the DT fuel mass generally used in HDC ablator experiments and the upper line corresponds to the DT fuel mass used in CH ablator experiments.

drive asymmetry, hydro-instability see ded by the capsule support tent, and high-Z mix in the hot spot. 4,5

The CH high-foot (CH HF) implosion used a modified 3-shock drive with a stronger first shock designed to reduce ablation-front Rayleigh–Taylor instability to produce a hydrodynamically more stable implosion at the cost of higher adiabat ($\alpha \sim 2.3$) and lower theoretical fuel compression. Performance did indeed dramatically improve with neutron yields, increasing a factor of $10 \times$ over the CH LF design to 1×10^{16} neutrons.^{6,7} As expected, the higher adiabat resulted in a lower DSR of $\sim 3.2\% - 4.2\%$ or $\rho R_{tot} \sim 0.64 - 0.84$ g/cm². As can be seen in Fig. 1, the best performing high-foot implosions achieved for the first time a doubling of fusion yield due to alpha-particle self-heating. Ultimately, the performance at the highest implosion velocities was again limited by 3D drive asymmetries and the tent perturbation.

To test whether further improvements could be realized by maintaining comparable levels of ablative stabilization, but increasing the areal density of the DT fuel, the so-called "adiabat-shaped" (AS) versions of the CH LF and CH HF drives were developed. These designs utilized a decaying first shock in order to combine low ablation-front hydro-instability with low adiabat and consequently high theoretical fuel compression.⁸ For the adiabat-shaped version of the CH LF (CH LF AS), the improvement in hydro-stability was verified in hydrodynamic growth radiography (HGR) experiments9 and a subsequent DT implosion¹⁰ produced a neutron yield of 1.4×10^{15} —an increase over similar companion CH LF shots, though still lower than companion CH HF shots. Two DT implosion experiments using the adiabatshaped high-foot pulse (CH HF AS) resulted in an increased DSR but similar neutron yields to comparable CH HF shots, suggesting that the benefit of the higher DSR was offset by other factors such as worsening 3D shapes at higher convergence.

At that time, a persistent problem in all the campaigns that used high-gas-fill hohlraums (He gas densities of 0.96-1.6 mg/cc) was the low efficiency with which laser energy was being converted to x-ray drive energy. Typically, 15% of the laser light entering the hohlraum underwent backscattering due to laser-plasma instabilities (LPIs), and a further 15%-25% deficit in effectively coupled drive energy was unexplained, resulting in an overall hohlraum efficiency of just 60%–70%.¹¹ This, in turn, exacerbated the difficulty in achieving the uniformity of drive needed for a symmetric implosion.¹² A new design was developed to mitigate these problems primarily by reducing the hohlraum gas-fill density to 0.03-0.3 mg/cc and using a high-density carbon (HDC) ablator instead of CH. With higher density, the HDC ablator permitted the use of a thinner shell, and hence, a shorter drive duration is needed to permit the reduction in gas-fill density.¹³ The 3-shock HDC design, operating at a design adiabat of $\alpha \sim 2.5$, achieved a $2 \times$ improvement in neutron yield over the CH HF, to 1.89×10^{16} corresponding to the fusion energy output of 53 kJ.^{14,15} A second HDC ablator design, termed the "Big Foot" (HDC BF), was developed to operate at a higher design adiabat of $\alpha \sim 4$, as well as to incorporate other changes to the laser and target geometry intended to make the hohlraum symmetry control better and more predictable.¹⁶ The HDC BF campaign achieved a similar level of overall performance as the HDC, reaching a peak neutron yield of 1.96×10^{16} or a fusion energy of 55 kJ.¹⁷ Despite the different design adiabats, both types of implosion achieved a similar DSR of $\sim 3.2\%$ ($\rho R_{tot} \sim 0.64 \text{ g/cm}^2$). The reason for this is not well understood although current modeling suggests that different levels of implosion stability may have led to

similar DSRs in the two designs despite the different design adiabats. Current designs are focusing on further improving upon the high performing HDC designs by increasing the capsule size to couple more energy to the implosion.^{18,19}

In terms of understanding, our proximity to ignition is useful to look not just at the absolute yield, but at the degree of alpha-heating that boosts or amplifies the yield, ultimately leading to the runaway process of ignition. This is the subject of Sec. II.

II. YIELD AMPLIFICATION AND IGNITION PARAMETERS

Analytical and computational studies have shown that the amplification in yield from alpha-heating can be expressed by a single metric that is a function of the neutron yield, the fuel areal density, and the fuel mass at stagnation. Spears *et al.*^{20–22} developed the experimentally observable ignition threshold factor (ITFX) based on a large ensemble of 2D radiation-hydrodynamics simulations of the original CH lowfoot (CH LF) design.²³ ITFX is defined by

$$ITFX_{n\alpha,\alpha} = \left(\frac{170}{M_{DT}}\right) \left(\frac{Y_{n\alpha,\alpha}^{13-15}}{4E15}\right) \left(\frac{DSR_{n\alpha,\alpha}}{0.067}\right)^{2.1},$$
(1)

where M_{DT} is the total DT fuel mass in μ g (170 μ g for this design) and Y^{13-15} is the measured neutron yield between 13 MeV and 15 MeV. In Eq. (1), ITFX is defined both for implosions where alpha-particle deposition is included, $ITFX_{\alpha}$, and for implosions where alpha-particle deposition is artificially turned off in the simulation, $ITFX_{n\alpha}$. The metric is normalized such that $ITFX_{n\alpha} = 1$ for this design when the yield $Y^{DT} = 1$ MJ. Y^{DT} is the total neutron yield from D–T fusion reactions, over all energies. As is evident from Eq. (1), the neutron yield corresponding to an $ITFX_{n\alpha} = 1$ is not unique for all target designs, but will vary with the fuel mass and DSR. While the absolute yield is not unique across target designs, the yield amplification due to alpha-particle self-heating, $Y_{\alpha}^{DT}/Y_{n\alpha}^{DT}$, is found to correlate strongly with *ITFX* independent of target design. Figure 2 shows the

relationship between the yield amplification with both $ITFX_{\alpha}$ and $ITFX_{n\alpha}$ for a set of 1D and 2D postshot simulations spanning a variety of target designs and capsule scales, including CH LF, CH HF, HDC, and HDC BF experiments. The simulations include a variety of sources of asymmetry including low-mode radiation drive asymmetries and, in some cases, high-mode capsule surface roughness and tent and fill-tube models.^{12,24} The solid lines in Fig. 2 are best fits to the simulation database and are given by

 $Y_{\alpha}^{\mathrm{DT}}/Y_{n\alpha}^{\mathrm{DT}} = \exp\left(0.9ITFX_{\alpha}^{0.47}\right)$

(2)

$$ITFX_{n\alpha} = ITFX_{\alpha} \times \exp\left(-0.9ITFX_{\alpha}^{0.47} + 0.007ITFX_{\alpha}^{1.65}\right).$$
(3)

The fits are generally valid up to yield amplifications of approximately $20-30\times$, where the increased fusion yield predominately originates from self-heating and ignition of the hotspot. As the thermonuclear burn begins to propagate into the dense fuel surrounding the hotspot, one can expect a much higher variability in the total yield and yield amplification.²⁵

An alternative ignition parameter based on the Lawson criterion is given by Betti *et al.*^{26–28}

$$\chi_{n\alpha} = (\rho R_{n\alpha})^{0.61} \left(\frac{0.12 Y_{n\alpha}^{16}}{M_{stag}} \right)^{0.34},\tag{4}$$

where ρR is the neutron-weighted fuel areal density, Y^{16} is the total neutron yield in units of 10^{16} neutrons, and M_{stag} is the stagnated DT mass in mg. The two metrics have a very similar form and are approximately related by $\chi_{n\alpha} \approx ITFX_{n\alpha}^{0.34}$. This provides a convenient method to infer the approximate value of $\chi_{n\alpha}$ from the experimentally measured value of $ITFX_{\alpha}$ and Eq. (3).

Using the experimentally measured $ITFX_{\alpha}$ and the fits in Eqs. (2) and (3), we infer $ITFX_{n\alpha}$ and yield amplification for all the HDC and



FIG. 2. Yield amplification due to alpha-heating as a function of $ITFX_{\alpha}$ (left) and $ITFX_{n\alpha}$ (right), for a suite of 1D and 2D postshot simulations of CH LF, CH HF, HDC, and HDC BF target experiments at the NIF. Solid lines represent the best fits to the simulation points.

BF experiments and plot in Fig. 3. The highest value reached to date is *ITFX*_{nx} = 0.43, equivalent to $\chi_{nx} \approx 0.75$, which corresponds to a yield amplification of $Y_{\alpha}^{\text{DT}}/Y_{n\alpha}^{\text{DT}} = 2.55 \pm 0.17$. We see that at the present value of $\chi_{n\alpha}$, the yield amplification begins to steepen rapidly, so that a small increase in $\chi_{n\alpha}$ would be expected to result in rapidly increasing levels of yield amplification and absolute yield. In Fig. 4, we plot the measured experimental yields vs the ignition parameter. The solid and dotted lines are the expected yields for implosions with and without alpha-heating, respectively, for the case of $M_{DT} = 138 \,\mu \text{g}$ and $DSR_{n\alpha} = 3.2$, which are representative of the majority of shots in these campaigns. In both Figs. 3 and 4, one can see the signature of the onset of hotspot ignition by the distinct changes in curvature or rates of increase in yield amplification and absolute yield, at $\chi_{n\alpha} \approx 0.90$, a value that is \sim 20% beyond the highest achieved to date. Conceptually, there are two paths for increasing $\chi_{n\alpha}$ —either to increase the stagnation pressure by improving the implosion quality at a fixed scale or to increase the scale while maintaining constant pressure, effectively increasing the confinement time. A particular form of scaling is hydroequivalent scaling, in which all spatial and temporal dimensions are increased by some factor S. In this case, it has been shown by Nora et al.²⁹ that the ignition parameter scales as $\chi_{n\alpha} \sim S^{1.1}$. Thus, in the absence of further improvements to the stagnation pressure, the scale would need to increase by $S \sim 20\%$ to reach a $\chi_{n\alpha}$ value of 0.90 and by $S \sim 30\%$ to reach a $\chi_{n\alpha}$ value of 1.0.

III. STAGNATION CONDITIONS

While the ignition parameters discussed in Sec. II provide a quantitative measure of the proximity to ignition in terms of no-burn neutron yield and total fuel ρR , one can gain much more physical



FIG. 3. Yield amplification vs $ITFX_{n\alpha}^{0.34}$ for HDC and HDC BF designs, where $ITFX_{n\alpha}^{0.34} \approx \chi_{n\alpha}$. The solid line is from Eqs. (2) and (3). The highest value of $\chi_{n\alpha}$ reached to date is $\chi_{n\alpha} \approx 0.75$, corresponding to a yield amplification of 2.55 \pm 0.17.



FIG. 4. Yield vs $ITEX_{nx}^{0.34}$ for HDC and HDC BF designs. The solid line is Eq. (1) for $DSR_{nx} = 3.2$. The dotted line is the equivalent yield in the case of no alpha-deposition.

insight by studying the thermodynamic conditions in the hotspot at stagnation. We use a 1D static model to infer the hotspot conditions from experimental measurements. While this is a highly simplified model, we can test it with synthetic data from multi-D simulations to quantify how well it approximates realistic implosions for the parameters of interest. The hotspot is approximated to be isobaric and have a temperature profile determined by thermal conduction within the hotspot.^{30,31} We further assume the electrons and ions to be in thermal equilibrium with each other. The solution of the heat flow equation in this case has the approximate form,

$$T(r) = T_o \left(1 - \left(\frac{r}{R_o}\right)^2 \right)^{\frac{1}{1+\beta}},\tag{5}$$

where T_o is the central temperature, R_o is the radius of the hotspot boundary, and β is the temperature exponent of the thermal conductivity, $K \propto T^{\beta}$.

Figure 5 compares normalized temperature profiles for different values of β with a profile taken at the time of peak neutron production (bangtime) from a 1D simulation of an HDC implosion using the radiation-hydrodynamics code HYDRA. The best agreement is obtained for a value of $\beta = 0.67$. This is lower than the value of $\beta = 2.5$ from classical Spitzer conductivity or $\beta = 2.0$ from a fit to the Sesame database for a DT plasma. Partly, this is expected given the approximate form of Eq. (5)—a more complete solution is given in the study by Betti *et al.*³² Additionally, other physical processes included in the full simulation will play a role in establishing the actual temperature profile. In order to best match the simulation, we use the value of $\beta = 0.67$ in the model.



FIG. 5. Hotspot temperature profiles from Eq. (5) for different values of the parameter β . The black line is the temperature profile at bangtime from a 1D simulation. The best agreement is obtained for a value of $\beta = 0.67$.

For a hotspot pressure *P*, the density profile is given by the ideal gas law,

$$\rho(r) = 1.3P/T(r),\tag{6}$$

where ρ is in g/cm², *P* is in Gbar, and *T* is in keV. The neutron yield per unit radius is

$$\frac{dY_n(r)}{dr} = 4\pi f_D f_T \frac{N_A^2}{A_{DT}^2} \rho(r)^2 \sigma_{DT}(T(r)) \tau_{BW} r^2,$$
(7)

where f_D and f_T are the deuterium and tritium fractions, respectively, A_{DT} is the average DT atomic mass, N_A is Avogadro's number, σ_{DT} is the DT fusion reactivity rate, and the integral over time is approximated by multiplying with the burnwidth τ_{BW} . The neutron-weighted ion temperature is then

$$\langle T_i \rangle_n = \frac{1}{Y_n} \int T(r) \frac{dY_n(r)}{dr} dr.$$
 (8)

The temperature is usually obtained from the variance of the Doppler-broadened DT neutron spectral peak at 14 MeV.³³ At the NIF, this is measured using several neutron-time-of-flight (NTOF) detectors arrayed around the target chamber.³⁴ However, the DT neutron peak can be broadened not only by thermal ion motion but also by the presence of residual velocity flow, or residual kinetic energy (RKE), in the hotspot resulting from incomplete conversion of kinetic to thermal energies during burn.^{35,36} In this case, the variance of the DT neutron peak corresponds to an apparent temperature, T_{app} , which is the sum of the neutron-weighted thermal ion temperature, $\langle \sigma_v^2 \rangle_n$, along the detector line-of-sight,

$$T_{app} = \langle T_i \rangle_n + (m_D + m_T) \langle \sigma_v^2 \rangle_n.$$
(9)

Experiments performed in the high-foot campaign gave the measured NTOF T_{app} temperatures systematically higher than that expected from both theory and detailed postshot simulations, often by as much as $\Delta T \sim 1$ keV.^{12,37} Experiments in low-gas fill hohlraums (HDC and HDC BF campaigns) at lower convergence and with improved radiation drive symmetry produced measured T_{app} temperatures more consistent with expectation. This suggested that the high-foot implosions may have had higher levels of RKE and, hence, T_{app} temperatures significantly higher than the thermal temperatures.^{35,38}

An alternate method for measuring thermal temperature-one not affected by residual hotspot flows-was developed by Jarrott et al.^{39,40} The method was to use measurements of the high-energy x-ray continuum spectrum from the hotspot to infer the thermal electron temperature. Electron and ion temperature measurements can differ, however, due to two possible effects. The first is from any difference in their equilibrium thermal temperatures. At early time, the shock traversing the initial central gas preferentially heats the ions. As the hotspot is compressed, the ions and electrons rapidly equilibrate and simulations predict that for the majority of burn, they are within a few percent of each other. At high levels of alpha-heating, they can depart again in the opposite direction as alpha-particles preferentially heat the electrons. The second effect arises from the fact that there is a temperature distribution within the hotspot and the single value of temperature that we infer is that distribution weighted by the particles being measured, i.e., neutrons for ion temperature and x rays for electron temperature. Whereas the neutron emission scales with temperature, the x-ray emission scales with both temperature and photon energy, $h\nu$, as exp $(-h\nu/T_e)$, and hence, the temperature inferred from the x-ray continuum slope depends on the photon energies being measured. If $\epsilon_{h\nu}$ is the x-ray emission from the hotspot, then the x-ray emission-weighted electron temperature is given by

$$\langle T_e \rangle_{h\nu} = -\epsilon_{h\nu} \left(\frac{d\epsilon_{h\nu}}{dh\nu} \right)^{-1}.$$
 (10)

Using the 1D isobaric hotspot model, we can relate the two quantities in Eqs. (8) and (10) and express one as a function of the other, $\langle T_i \rangle_n = f(\langle T_e \rangle_{h\nu})$. We find that this function is close to unity when evaluated at $h\nu = 20$ keV for temperatures in the range of $\langle T_i \rangle_n \sim 3$ -6 keV.^{40} Figure 6 plots the measured T_{app} vs $\langle T_e \rangle_{h\nu}$ from a number of recent DT experiments. The solid line represents T_{app} vs $\langle T_e \rangle_{h\nu}$ for the case of zero residual kinetic energy, where the apparent temperature would be equal to the thermal temperature, i.e., $T_{app} = \langle T_i \rangle_n$. Hence, the vertical offset between T_{app} and the line represents additional broadening due to residual velocity flows in the hotspot. The experiments are separated by the hohlraum gas-fill density: low gas-fill $(\rho_{gas}=0.3\,{\rm mg/cc})$ and high gas-fill ($\rho_{gas}=1.6\,{\rm mg/cc}).$ The ten lowgas fill experiments show generally good agreement between the two measurements with a mean vertical offset of $\Delta T \approx 120 \,\mathrm{eV}$. The two high-gas fill experiments (both using the CH HF design) have offsets of $\Delta T \approx 540$ eV and 730 eV. These measurements are consistent with the hypothesis that the neutron-weighted thermal ion temperatures of the CH HF experiments were significantly lower than the observed NTOF apparent ion temperatures. Assuming these results to be generally applicable to all previous low and high gas-fill experiments, we can apply systematic corrections to the NTOF T_{app} measurements to estimate the actual hotspot thermal ion temperatures $\langle T_i \rangle_n$.



FIG. 6. Experimental measurements of the apparent ion temperature, T_{app} , measured by NTOF, and the electron temperature, $\langle T_e \rangle_{h\nu}$, measured via x-ray continuum emission. The solid line corresponds to the case of zero residual kinetic energy. Hence, the vertical offset of the data from the line represents the increase in T_{app} above the neutron-weighted thermal ion temperature due to hotspot RKE.

Given experimental measurements of the neutron yield, temperature, volume, and burnwidth, we can use Eqs. (5)-(8) to infer the pressure P, central temperature T_o , and hotspot boundary R_o .³¹ Replacing the density profile, $\rho(r)$, in Eqs. (7) by (6) makes the radial dependence of the yield a function of just temperature. In this case, T_o is given directly by the burn-weighted neutron temperature using Eq. (8). Then, computing a normalized synthetic neutron image and matching it with the experimental image (at the 17% intensity contour) gives R_{o} . Finally, integrating Eq. (7) and substituting the measure neutron yield and burnwidth give P. Equation (6) then gives $\rho(r)$, with which other quantities such as the areal density can be derived. In reality, as can be seen in Fig. 5, there is no well-defined boundary between the hotspot and dense fuel. Some boundary needs to be defined, however, to infer any extrinsic property such as mass $m_{\rm hs}$, energy $E_{\rm hs}$, or areal density $\rho R_{\rm hs}$. Since our main interest is that volume that predominantly contributes to fusion yield, we define an effective hotspot radius, $R_{\rm hs}$, by the central region that produces 98% of the total neutron yield.

To validate the model, we use an ensemble of 2D HYDRA capsule simulations. The simulations take a nominal HDC BF design and vary a number of inputs including the capsule scale, the peak and duration of the radiation drive, L = 1 and L = 2 Legendre mode drive asymmetries, and a simple model that adds entropy to the DT fuel to mimic the effects of high-mode fuel-ablator mix.^{41,42} The neutron yield, neutron-weighted ion temperature, and nuclear burnwidth are taken directly from the simulations. For the volume, synthetic neutron images are generated along equatorial and polar views and the 17% intensity contours are fit with Legendre polynomial (equatorial view) or spherical harmonic (polar view) distributions, as is done with the experimental data. We compute an approximate hotspot volume bound by the 17% intensity contour using the first two even modes, $V_{17\%} = 4\pi/3 \times (P0 + P2) \times M0^2$. The equivalent 1D radius is then $R_{17\%} = (3V_{17\%}/4\pi)^{1/3}$. We fit the hotspot model to the synthetic data and calculate a

We fit the hotspot model to the synthetic data and calculate a hotspot pressure, P_{model} , which can be compared with the neutronweighted hotspot pressure at bangtime, P_{sim} , extracted directly from the simulation. Figure 7 plots histograms of the ratio $P_{\text{model}}/P_{\text{sim}}$, showing generally good agreement across the simulation suite. For relatively symmetric implosions (hotspot P2/P0 < 10%), we obtain the mean and standard deviations in $P_{\text{model}}/P_{\text{sim}} = 1.03 \pm 0.05$. Including increasingly asymmetric implosions skews the distribution to higher values of $P_{\text{model}}/P_{\text{sim}}$. However, even allowing for highly distorted implosions up to hotspot P2/P0 < 50%, we find that the model still does a reasonably good job of inferring the true pressure with $P_{\text{model}}/P_{\text{sim}} = 1.05 \pm 0.10$.

To apply the model to the experiments, we run it over several thousand sets of measurement values obtained by Monte Carlo sampling the probability distribution of each input parameter, defined by its mean value and 1σ measurement error. We, thus, obtain a probability distribution for each inferred quantity, from which we can extract the mean value and standard deviation. As an example, in Table I, we list the input measurements and inferred stagnation quantities for one of the highest performing HDC implosions to date (N170827). We note that for the experimental burnwidth, we use the x-ray burnwidth (measured using an x-ray streak camera⁴³) rather than the neutron burnwidth (measured using the gamma reaction history diagnostics⁴⁴). The reason for this choice is the smaller uncertainty in the x-ray measurement and the fact that the measured x-ray



FIG. 7. Histograms of the ratio of inferred pressure from the 1D hotspot model to the neutron-weighted pressure at bangtime from the simulation for an ensemble of 2D simulated capsule implosions. The histogram on the left is restricted to relatively symmetric implosions with hotspot P2/P0 < 10% and has a mean and standard deviation of $P_{\rm model}/P_{\rm sim} = 1.03 \pm 0.05$. The histogram on the right includes highly asymmetric implosions up to P2/P0 < 50% and has a distribution of $P_{\rm model}/P_{\rm sim} = 1.05 \pm 0.10$.

TABLE I. Experimental measurements and inferred stagnation quantities for one of
the highest performing HDC implosion to date (N170827). The inferred parameters
$R_{\rm hs}, \rho R_{\rm hs}, m_{\rm hs},$ and $E_{\rm hs}$ are defined by the central volume producing 98% of the
total neutron vield.

Parameter	Value	Uncertainty
Y_n^{DT} (neutrons)	$1.89 imes 10^{16}$	$\pm 5 imes 10^{14}$
NTOF T_{app} (keV)	4.70	± 0.12
Nuc $P0(\mu m)$	28.4	± 3.5
Nuc P2/P0 (%)	-27%	$\pm 5\%$
Nuc $M0(\mu m)$	33.0	± 1.2
X-ray BW (ps)	142	±13
Inferred $R_{17\%}(\mu m)$	28.2	-1.9, +1.8
Inferred $R_o(\mu m)$	34.7	-2.4, +2.2
Inferred $R_{\rm hs}$ (μ m)	31.8	-2.2, +2.0
Inferred $T_{\rm hs}$ (keV)	4.30	-0.26, +0.26
Inferred $\rho_{\rm hs}$ (g/cm ³)	110	-11, +13
Inferred $P_{\rm hs}$ (Gbar)	337	-33, +42
Inferred $\rho R_{\rm hs}$ (g/cm ²)	0.311	-0.017, +0.019
Inferred $m_{\rm hs}$ (µg)	16.8	-1.8, +1.8
Inferred $E_{\rm hs}$ (kJ)	6.8	-0.8, +0.7

and neutron burnwidths are statistically within ~10 ps of each other on average.⁴⁵ Probability distributions for two of the inferred quantities, hotspot pressure and areal density, are shown in Fig. 8. The inferred stagnation pressure for this shot is $P_{\rm hs} = 337 (-33,$ +42) Gbar, and the hotspot areal density $\rho R_{\rm hs} = 0.311 (-0.017,$ +0.019) g/cm². The uncertainty in $\rho R_{\rm hs}$ is relatively low because the uncertainties in $\rho_{\rm hs}$ and $R_{\rm hs}$ are correlated and partially cancel.

An important model uncertainty lies in the correct form of temperature profile T(r) to use, characterized by the parameter β in Eq. (5). We chose a value of $\beta = 0.67$ to match a HYDRA simulated



FIG. 8. Hotspot pressure and hotspot areal density probability distributions inferred for shot N170827. The mean and standard deviations are $P_{\rm hs} = 337 \, (-33, \, +42)$ Gbar and $\rho R_{\rm hs} = 0.311 \, (-0.017, \, +0.019) \, {\rm g/cm^2}$, respectively.

TABLE II. Dependence of inferred stagnation quantities on the value of β in the tem-
perature profile given by Eq. (5). The inferred values of hotspot $P_{\rm hs}$, $\rho_{\rm hs}$, and $\rho R_{\rm hs}$
are quite insensitive to the temperature profile assumed.

Parameter	eta=0	eta=0.67	$\beta = 2$
Inferred R_o (μ m)	39.1	34.7	31.7
Inferred $R_{\rm hs}$ (μ m)	33.3	31.8	30.3
Inferred $\rho_{\rm hs}$ (g/cm ³)	111	110	109
Inferred $P_{\rm hs}$ (Gbar)	330	337	344
Inferred $\rho R_{\rm hs}$ (g/cm ²)	0.332	0.311	0.296
Inferred $m_{\rm hs}$ (µg)	20.8	16.8	13.5
Inferred E_{hs} (kJ)	7.6	6.8	6.0

profile. As seen in Fig. 5, an ideal conduction-limited profile corresponding to $\beta = 2-2.5$ would have a much steeper gradient at the hotspot boundary. On the other hand, there are suggestions from detailed 3D neutron reconstructions of some shots that the profile may be more centrally peaked and less steep at the boundary.⁴⁶? To assess the sensitivity of the inferred quantities to the precise form of the temperature profile used, we rerun the model for $\beta = 0$ and $\beta = 2$ and list the results in Table II. The inferred hotspot pressure and density are essentially insensitive over this range of T(r) profiles, varying by not more than $\pm 2\%$. The sensitivity to hotspot areal density $\rho R_{\rm hs}$ is relatively modest at $\pm 6\%$. The effect on hotspot energy and mass is more significant at $\pm 12\%$ and $\pm 22\%$, respectively. Shown in Fig. 9 are the



FIG. 9. Sensitivity of inferred 1D hotspot profiles to the value of β used in Eq. (5). All profiles are constrained by the same experimental measurement inputs listed in Table I. Temperature profiles are in blue (absolute units), neutron emission per unit radius dY/dr in green (normalized to peak), and synthetic neutron image profiles dY/dx in magenta (normalized to peak).

corresponding profiles for the temperature T(r), neutron emission dY_n/dr , and synthetic neutron image dY_n/dx . By construction, these hotspot profiles are all constrained by the same experimentally observed yield, neutron-weighted ion temperature, 17% neutron image contour, and burnwidth. One can see that while the peak temperatures and hotspot boundaries vary, the bulk of the neutron emission comes from very similar plasma conditions. The experimental observables do not well constrain either the location of or conditions near the hotspot boundary, resulting in larger uncertainties in those quantities strongly weighted at the large radii, such as hotspot mass and energy.

IV. HOTSPOT POWER BALANCE

We can use the inferred hotspot temperatures and areal densities to assess the net power balance in the hotspot and the proximity to ignition. We use the results of a 3D dynamic model developed by Springer *et al.*⁴⁷ In this model, a 3D shell is broken up into facets where each facet is 1D and shares a common hotspot. The model calculates the evolution of the hotspot pressure and temperature by evaluating the *PdV* work done by the faceted shell elements on the hotspot, beginning in the deceleration phase of the implosion. A key approximation is that the hotspot is isobaric and has a conduction-dominated temperature profile. In this case, the thermodynamic properties of the hotspot and the rates entering the power balance can be specified as a function of time by just three parameters: the pressure *P*, the central temperature *T*, and the hotspot radius *R*.

The net rate of change in the energy of the hotspot in an ICF implosion, Q_{net} is given by the balance of power flow into and out of the hotspot,

$$Q_{net} = f_{\alpha} Q_{\alpha} - Q_{rad} - Q_{cond} - P \frac{dV}{dt}, \qquad (11)$$

where Q_{α} is the alpha-particle energy production rate and f_{α} is the fraction of that energy deposited within the hotspot, Q_{rad} is the radiative loss rate, Q_{cond} is the conduction loss rate, and P(dV/dt) is the rate of mechanical work on the hotspot, which is an energy source during the compression phase but reverses sign and is an energy sink during the explosion phase.

The net power into the hotspot is related to the hotspot temperature, *T*, by

$$Q_{net} = c_P m \frac{dT}{dt} = \frac{E_{hs}}{T} \frac{dT}{dt},$$
(12)

where c_P is the DT heat capacity at constant pressure, *m* is the hotspot mass, and E_{hs} is the hotspot energy. The hotspot temperature is then given by

$$\frac{dT}{dt} = \frac{T}{E_{hs}} \left(f_{\alpha} Q_{\alpha} - Q_{rad} - Q_{cond} - P \frac{dV}{dt} \right).$$
(13)

The hotspot volume decreases in time, reaches a minimum value on bounce, and then increases. At the time of minimum volume, dV/dt = 0, and we obtain the familiar Lawson condition for selfheating of a *static* hotspot,

$$\frac{dT_{\text{static}}}{dt} = \frac{T}{E_{hs}} (f_{\alpha} Q_{\alpha} - Q_{rad} - Q_{cond}) > 0.$$
(14)

Using analytical expressions for f_{α} , Q_{α} , Q_{rad} , and Q_{cond} , as a function of (P, R, T),⁴⁷ we can compute the Lawson self-heating boundary in the parameter space (T_{hs}, PR) or equivalently $(T_{hs}, \rho R_{hs})$.

In Fig. 10, we plot the experimentally inferred values of $(T_{\rm hs}, \rho R_{\rm hs})$ for the major campaigns, as well as the static self-heating boundary. The original CH LF experiments were clearly very far from the self-heating boundary. The CH HF campaign achieved considerably better performance with hotspot temperatures reaching $T_{\rm hs} \sim 4.4 \,\rm keV$ and hotspot areal densities $\rho R_{\rm hs} \sim 0.2 \,\rm g/cm^2$. Finally, in the HDC and HDC BF campaigns, implosions reached similar temperatures to CH HF, but up to 50% higher areal densities, reaching $\rho R_{\rm hs} \sim 0.3 \,\rm g/cm^2$. This is likely due to improved symmetry and shell confinement, which allows more time for the hotspot to accumulate mass through ablation of the inner surface of the DT shell, thereby increasing both the hotspot mass and the areal density.

The self-heating boundary shown in Fig. 10 applies to a clean DT hotspot. However, experiments have often shown signatures of high-Z ablator mix entering the hotspot, typically from perturbations seeded



FIG. 10. Hotspot temperature, T_{hs} , and areal density, ρR_{hs} , of DT implosion experiments in the CH LF (left), CH HF (middle), and HDC and HDC BF campaigns (right). The dashed line is the Lawson self-heating boundary (dT/dt = 0), for a static plasma (dV/dt = 0). These are similar to the plots shown in the study by Hurricane *et al.*⁴⁵ but use updated values for the inferred stagnation quantities using the static hotspot model described above.

by engineering features such as the fill-tube, support tent, or particulates on the capsule surface.^{5,49,50} High-Z mix increases the radiation loss from the hotspot and can be accounted for in the radiative loss term as $Q_{rad} = Q_{DT} + Q_{mix}$. The effect is to increase the temperature required to meet the self-heating condition. As an example, the change in the self-heating boundary for the case of a 20% increase in radiative loss due to mix ($Q_{mix}/Q_{DT} = 20\%$) is shown in Fig. 11. Excess radiative loss from ablator mix seeded by the fill-tube alone has been estimated from x-ray imaging data to vary between 2 and 14% across a subset of shots analyzed.⁴⁶ Mix observed from other seeds, such as surface particulates, which vary shot to shot, can significantly add to the total radiative loss.

The self-heating condition, dT/dt > 0, is a necessary but insufficient condition for ignition. On expansion of the hotspot, PdV work is a loss term, and for the hotspot to ignite, it is necessary that at the time of minimum volume, the net alpha-heating heating rate is both positive and also increases faster than the rate of PdV expansion. This is equivalent to requiring both the first and second derivatives of temperature to be greater than zero at a minimum volume. As described in Ref. 47, the second derivative condition, $d^2T/dt^2 > 0$, can be estimated by expanding Eq. (13) about the minimum volume to obtain

$$\frac{d^2 T_{\text{static}}}{dt^2} > \frac{2}{3} \frac{T}{V} \frac{d^2 V}{dt^2}$$
$$> \frac{2}{3} \frac{T}{V} \int r^2 \ddot{r} + 2r \dot{r}^2 \, d\Omega.$$
(15)



FIG. 11. Effect of mix and expansion work on moving the self-heating and ignition boundaries. The dashed line is the Lawson self-heating boundary (dT/dt = 0) for a clean static DT hotspot. The lower dotted-dashed line is the boundary for a case where mix in the hotspot increases the radiative loss by 20%, i.e., $Q_{mix}/Q_{DT} = 20\%$. The upper dotted-dashed line is the ignition requirement, $d^2T/dt^2 = 0$, for a $\rho R_{\text{shell}} = 1 \text{ g/cm}^2$ (this line is for a clean DT or $Q_{mix} = 0$ case).

The right-hand side contains two terms. The first term includes the radial acceleration of the hotspot boundary, \ddot{r} , and can be regarded as a confinement parameter. The acceleration is approximately the differential pressure across the stagnated shell over the areal density of the shell, $\ddot{r} \approx \Delta P / \rho R_{\text{shell}}$. The second term includes the radial velocity, \dot{r} , and represents the residual shell velocity, which would be nonzero in the presence of 3D shape asymmetry. In the limit of a 1D implosion with an infinitely thick shell, the right-hand side of Eq. (15) is zero and the second derivative ignition condition is automatically met by the static self-heating condition, dT/dt > 0. However, as the shell areal density decreases, the second derivative boundary moves up in temperature and the ignition parameter space becomes increasingly more restricted. Figure 11 shows the $d^2T/dt^2 > 0$ region for the example case of $\rho R_{\text{shell}} = 1 \text{ g/cm}^2$. We see that for hotspot areal densities of $\rho R_{hs} \sim 0.3 \,\mathrm{g/cm^2}$, the temperature required for ignition increases from 4.8 keV in the static case to 5.7 keV in the dynamic case.

In Fig. 12, we plot a simulated trajectory through $T_{\rm hs} - \rho R_{\rm hs}$ space from a nominal 2D capsule simulation that reproduces the neutron yield (~52 kJ) of one of the highest performing HDC implosions. In the simulation, the hotspot temperature rises quickly to ~4.8 keV and then remains relatively flat, while the effects of convergence and mass ablation of DT ice increase the hotspot $\rho R_{\rm hs}$. The black circle shows the neutron-weighted $T_{\rm hs}$ and $\rho R_{\rm hs}$ integrated over time. The white circle is the value of $T_{\rm hs}$ and $\rho R_{\rm hs}$ at the time of minimum volume in the simulation. The black circle is more representative of the inferred values from the experimental data. We do not directly measure the minimum volume conditions given by the white circle, which



FIG. 12. Simulated trajectory through $T_{hs} - \rho R_{hs}$ space from a nominal 2D simulation of an HDC implosion. The black circle is the time-integrated neutron-weighted temperature and hotspot areal density. The white circle is the neutron-weighted temperature and hotspot areal density at the minimum volume time of the implosion.

are the ones relevant for comparing the self-heating and ignition curves. Although at these implosion conditions, the time-integrated and minimum volume time $T_{\rm hs} - \rho R_{\rm hs}$ values are fairly similar because the minimum volume time is very close—within 20 ps of the peak neutron production time—we see that at a minimum volume, the hotspot has just crossed the dT/dt > 0 boundary but failed to cross the $d^2T/dt^2 > 0$ boundary, resulting in a nonigniting implosion.

To illustrate how the behavior of the hotspot changes as we approach ignition, we performed additional capsule simulations, shown in Fig. 13, at progressively larger hydrodynamic scales, ranging from $1.1 \times$ to $1.35 \times$ of the baseline case. At the $1.1 \times$ scale, the temperature is increasing at a minimum volume but still $d^2T/dt^2 < 0$ and the implosion fails to ignite. At the $1.25 \times$ scale, the minimum volume point is right on the $d^2T/dt^2 = 0$ boundary and the hotspot is just at the point of igniting, with the yield boosted to 380 kJ. Finally, at the $1.35 \times$ scale, the minimum volume point has crossed well into the $d^2T/dt^2 > 0$ region and the implosion ignites with a yield of 2.5 MJ. The behavior of the simulations is, therefore, consistent with the model-based ignition criterion. However, we should note that the $d^2T/dt^2 = 0$ boundary shown in these plots is representative of a specific implosion configuration, and in actuality, it will differ for each individual simulation or experiment depending on the particular values of mix, shell areal density, and 3D asymmetry.

We can further verify the relationship between the temperature derivative and the ignition boundary by directly examining the time derivative of the hotspot temperature in the simulations. In Fig. 14, we



FIG. 13. Simulated trajectories from a set of 2D capsule simulations varying in scale from a nominal $1 \times$ to $1.1 \times$, $1.25 \times$, and $1.35 \times$. The total neutron yield is shown for each simulation. Black circles are the time-integrated neutron-weighted temperature and hotspot areal density. White circles are the neutron-weighted temperature and hotspot areal density at the minimum volume time of the implosion.



FIG. 14. Simulated hotspot temperature as a function of time for the four implosions shown in Fig. 13. The horizontal axis is the time relative to the time of minimum volume for each implosion. The curves are labeled by their total neutron yields.

plot the hotspot temperature as a function of time for the same four simulations, with the horizontal axis being the time relative to the time of minimum volume for each simulation. We see that for the first two implosions (producing 52 kJ and 100 kJ), the second derivatives of temperature are less than zero at the time of minimum volume (i.e., the slopes of the lines, or first derivatives, are decreasing). In the third implosion, the second derivative is close to zero. In the fourth implosion—which robustly ignites—it is greater than zero. Another interesting observation from this plot is that the difference in time between the minimum volume and peak neutron production (which is close to peak pressure and approximately peak temperature) increases as we approach ignition. Thus, it is the power balance in the hotspot at a time *prior* to peak neutron production and pressure that determines whether or not the hotspot will ignite.

V. CONCLUSIONS

We have described the overall performance of ICF implosions at the NIF and their proximity to ignition both in terms of the no-burn ignition parameter, $\chi_{n\alpha}$, which depends on the yield and the total fuel areal density, and in terms of the inferred hotspot stagnation conditions. The best performing implosions to date have achieved values of $\chi_{n\alpha} \approx 0.75$, corresponding to yield amplifications from alpha-heating of $2.55 \times \pm 0.17$. As can be seen in Figs. 3 and 4, relatively small improvements in the no-burn $\chi_{n\alpha}$ metric from current experiments would be expected to produce a significant increase in both yield amplification and total fusion yield. In terms of hotspot stagnation conditions, a number of HDC ablator implosions are estimated to have reached neutron-weighted thermal ion temperatures of $T_{\rm hs}$ $\sim 4.4 \,\rm keV$ and hotspot areal densities of $\rho R_{\rm hs} \sim 0.3 \,\rm g/cm^2$. These conditions are very close to the self-heating boundary, dT/dt > 0, at a minimum volume. The ignition boundary, $d^2T/dt^2 > 0$, is somewhat further away, with its precise location being strongly dependent on the shell areal density and 3D shell asymmetry that determine the confinement parameter and on the degree of hotspot mix, which increases the radiation loss term. The gap between current experiments and the ignition boundary can be closed both by further improving the hotspot conditions in terms of pressure, temperature, and areal density to move well into the self-heating regime and from the other direction by bringing the $d^2T/dt^2 = 0$ ignition boundary closer by increasing the shell areal density, reducing 3D shell asymmetry, and reducing hotspot mix.

We note that since the ignition criteria are described here in terms of the hotspot conditions at a minimum volume, it would be valuable to measure the time-dependent hotspot temperature and areal density. Currently, we have time-resolved measurements of the neutron production rate and the hotspot size (through time-resolved x-ray imaging). A cross-timed time-resolved temperature measurement would enable a determination of the $T_{\rm hs} - \rho R_{\rm hs}$ conditions at the minimum volume time. Two new diagnostics are under development that could provide this information: first, a time-resolved magnetic recoil spectrometer (MRS-t) measuring time-resolved T_i^{51} and, second, a time-resolved x-ray continuum measurement to infer the time-resolved $T_e^{.52}$

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