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48	Abstract	<p>This work aims to elucidate how molecular parameters dictate the occurrence of inhomogeneous cohesive failure during step strain and large amplitude oscillatory shear (LAOS) respectively in entangled polymer mixtures. Based on three well-entangled polybutadiene (PB) mixtures, we perform simultaneous rheometric and particle-tracking velocimetric (PTV) measurements to illustrate how the slip length controls the degree of shear banding. Specifically, the PB mixtures were prepared using the same parent polymer (<math>M_w \cdot 10^6</math> g/mol) at 10 wt.% concentration in respective polybutadiene solvents (PBS) of three different molecular weights 1.5, 10, and 46 K. After step strain, the entangled PB mixture with PBS-1.5 K displayed interfacial failure whereas the PB mixture with PBS-10 K showed bulk failure, demonstrating the effectiveness of our strategy to suppress wall slip by controlling PBS' molecular weight. Remarkably, the PBS-46K actually allows the elastic yielding to occur homogeneously so that no appreciable macroscopic motions were observed upon shear cessation. PBS is found to play a similar role in LAOS of these three PB mixtures. Finally, we demonstrate that in case of the slip-prone mixture based on PBS-1.5 K the interfacial failure could be drastically reduced by use of shearing plates with considerable surface roughness.</p>	
49	Keywords separated by ' - '	<p>Nonlinear rheology - Entangled polymer solutions - Shear inhomogeneity - Elastic yielding - Wall slip</p>	
50	Foot note information		

# How polymeric solvents control shear inhomogeneity in large deformations of entangled polymer mixtures

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1 **Abstract** This work aims to elucidate how molecular  
2 parameters dictate the occurrence of inhomogeneous  
3 cohesive failure during step strain and large ampli-  
4 tude oscillatory shear (LAOS) respectively in entan-  
5 gled polymer mixtures. Based on three well-entangled  
6 polybutadiene (PB) mixtures, we perform simulta-  
7 neous rheometric and particle-tracking velocimetric  
8 (PTV) measurements to illustrate how the slip length  
9 controls the degree of shear banding. Specifically, the  
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13 different molecular weights 1.5, 10, and 46 K. After  
14 step strain, the entangled PB mixture with PBS-1.5 K  
15 displayed interfacial failure whereas the PB mixture  
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17 effectiveness of our strategy to suppress wall slip by  
18 controlling PBS' molecular weight. Remarkably, the  
19 PBS-46K actually allows the elastic yielding to occur  
20 homogeneously so that no appreciable macroscopic  
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22 found to play a similar role in LAOS of these three PB  
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24 slip-prone mixture based on PBS-1.5 K the interfacial  
25 failure could be drastically reduced by use of shearing  
26 plates with considerable surface roughness.

**Keywords** Nonlinear rheology · Entangled polymer  
solutions · Shear inhomogeneity · Elastic yielding ·  
Wall slip

**Introduction** 30

Response of entangled polymer mixtures to nonlinear  
deformations has been extensively studied in conventio-  
nal rheometric setups such as cone-plate fixture, planar  
and circular Couette cells (Macosko 1994; Graessley  
2008). These fixtures are capable of generating uniform  
shear rate across the gap and thereby can provide in-  
formation about the constitutive behavior of entangled  
polymer mixtures. Until recently, shear deformation  
and flow of such materials had been assumed to occur  
homogeneously across the sample thickness in these  
apparatuses. Emerging particle-tracking velocimetric  
(PTV) observations in these fixtures recently indicated  
that this assumption is often violated: Upon a rapid  
startup shear, an entangled polymeric liquid first un-  
dergo elastic deformation before such a transient solid  
yields to allow permanent (irrecoverable) deformation,  
i.e., flow. Apparently, after the shear stress overshoot  
(i.e., the yield point), the quasi-elastic "solid", unable  
to sustain indefinite amount of deformation, can col-  
lapse in an inhomogeneous manner (Tapadia and Wang  
2006; Boukany and Wang 2007; Hu et al. 2007;  
Ravindranath and Wang 2008a, b; Ravindranath and  
Wang 2007a). Sufficiently entangled polymers also  
show shear banding in large amplitude oscillatory shear  
(LAOS; Tapadia et al. 2006; Ravindranath and Wang  
2008a, b). Finally and most strikingly, inhomogeneous  
breakup was discovered for both entangled mixtures  
(Wang et al. 2006; Ravindranath and Wang 2007b) and

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59 melts (Boukany et al. 2009b) after large step strain in  
60 both simple shear and uniaxial extension (Wang et al.  
61 2007a, b). On the other hand, the “solid” character  
62 diminishes when the level of chain entanglement is re-  
63 duced. Consequently, less-entangled liquids can avoid  
64 shear banding in steady state as previously demon-  
65 strated (Ravindranath and Wang 2008a, b; Boukany  
66 and Wang 2009a).

67 The present work further explores the nature of  
68 inhomogeneous breakup in entangled polybutadiene  
69 (PB) mixtures and elucidates how uneven yielding can  
70 be prevented by increasing the polymeric solvent’s  
71 molecular weight. Specifically, we focus on two com-  
72 mon modes of deformation, step strain and LAOS.  
73 We show that failure at sample/wall interfaces can be  
74 minimized by reducing the intrinsic slip length  $b$  of  
75 the mixture. Even elastic breakdown and shear band-  
76 ing can be completely annihilated by using a PB sol-  
77 vent of sufficiently high molecular weight (i.e.,  $M_w =$   
78 46 kg/mol) to prepare a 10 wt.% PB mixture. In con-  
79 trast, 10 wt.% PB mixtures made with PBS of either  
80  $M_w = 1.5$  kg/mol or  $M_w = 10$  kg/mol show considerable  
81 uneven structural breakdown.

82 **Experimental**

83 Sample preparation

84 Our experiments are based on three entangled 1,4-  
85 polybutadiene (PB) mixtures made with the same parent  
86 polymer ( $M_w \sim 10^6$  g/mol) at 10 wt.% concentration  
87 in three different polybutadiene solvents. The molec-  
88 ular weights of the three PB solvents (PBS) were 1.5,  
89 10, and 46 K respectively. The mixtures are labeled  
90 as 1 M(10%)-1.5 K, 1 M(10%)-10 K and 1 M(10%)-  
91 46 K respectively. The number of entanglements per  
92 chain  $Z = M_w/M_e\phi^{-1.2}$  in each of the three mixtures  
93 is around 40, where  $M_w$  is the molecular weight of  
94 the parent polymer,  $M_e$  is the entanglement molecu-  
95 lar weight of the pure PB equal to 1.6 kg/mol, and  $\phi$  is the  
96 volume fraction of parent polymer. The molecular char-  
97 acteristics of the parent polymer and the PB solvents  
98 are listed in Table 1. The parent PB was first dissolved  
99 in excess of toluene to which PBS was added and

intimately mixed. Silver-coated silica particles with an 100  
average diameter of 10  $\mu\text{m}$  (Dantec Dynamics S-HGS) 101  
were first ultrasonicated in toluene and then added to 102  
the mixture with the final loading of the particles being 103  
500–600 ppm. Most of the toluene was evaporated at 104  
room temperature under hood over a period of 2 weeks 105  
and the remaining was removed in vacuum condition 106  
until the residue is less than 0.5%. 107

Apparatus and particle-tracking velocimetry 108

All measurements were made at room temperature of 109  
around 25°C, using cone-plate geometry of  $\theta = 5.4^\circ$  110  
and diameter of 25 mm. The overall chain relaxation 111  
time  $\tau$  and mixture viscosity  $\eta_0$  reported in Table 2 112  
were obtained from small amplitude oscillatory shear 113  
frequency sweep measurements done at room temper- 114  
ature on an Advanced Rheometrics Expansion Sys- 115  
tem (ARES). Step strain and LAOS experiments on 116  
1 M(10%)-46 K mixture were done on ARES. All 117  
other measurements were made on a Bohlin-CVOR 118  
rheometer. Both smooth and rough surfaces were used 119  
to determine how surface condition may alter the shear 120  
responses. Rough surfaces are made by gluing sand- 121  
paper onto the cone and plate, where a small hole is 122  
left on the sandpaper surface of the stationary bottom 123  
plate for a laser sheet (cross-section of 0.2 mm  $\times$  2 mm) 124  
to pass vertically across the gap. The gap distance is 125  
determined by zeroing the gap with the sandpaper cov- 126  
ered plates. The sandpaper is from Virginia abrasives, 127  
USA with catalog number 4687A13 and roughness of 128  
240 grit. 129

The PTV consists of a CCD camera (with a maxi- 130  
mum speed of 30 fps) placed horizontally to observe 131  
particle movements from the meniscus that is wrapped 132  
around with a transparent film. The location of the PTV 133  
measurements is at a distance of 3 to 4 mm from the 134  
meniscus of the cone-plate with 25 mm diameter. This 135  
scheme A of placing the CCD horizontally is more con- 136  
venient than the scheme B involving placing the CCD 137  
at an angle and peeking through a transparent window 138  
on the stationary plate (Tapadia et al. 2006). We have 139  
shown previously that the film around the meniscus 140  
does not affect the PTV observations as long as it is 141  
made sufficiently away from the film (Tapadia et al. 142

**Table 1** Molecular characteristics of parent PB and various PB solvents at room temperature

Sample	$M_n$ (g/mol)	$M_w$ (g/mol)	$M_w/M_n$	Source	$\eta_s$ (Pa s)	
1 M	$1.014 \times 10^6$	$1.052 \times 10^6$	1.03	University of Akron	–	t1.1
PBS-1.5 K	1500	–	–	Sigma-Aldrich <i>Cat. No. 20,0484</i>	0.7	t1.2
PBS-10 K	8900	10500	1.18	Bridgestone	14	t1.3
PBS-46 K	45000	46000	1.02	Goodyear	2600	t1.4
						t1.5
						t1.6

**Table 2** Properties of PB mixtures at room temperature

Mixture	$\phi^{1.2} M_w/M_e$	$\tau$ (s)	$\eta_0$ (Pa.s)	$\eta_0/\eta_s$	$l_{ent}$ (nm)	$b$ (mm)	
1 M(10%)-1.5 K	40	17	50,000	71,428	17	1.2	t2.1
1 M(10%)-10 K	40	50	$1.7 \times 10^5$	12,142	17	0.2	t2.2
1 M(10%)-46 K	40	75	$3.9 \times 10^5$	150	17	0.002	t2.3
							t2.4
							t2.5

143 2006). For the present step strain and LAOS, it is actu-  
 144 ally feasible to adopt the scheme B: Given the limited  
 145 strain in such tests, the meniscus would remain stable.  
 146 For smooth surfaces, a laser sheet was passed at an an-  
 147 gle of ca. 45° through a glass window of 5 mm radius on  
 148 the stationary plate, as depicted previously by Ravin-  
 149 dranath and Wang (2007a, b). Movements of the illumi-  
 150 nated particles across the entire sample thickness were  
 151 captured with a black–white CCD camera placed at ca.  
 152 45°, but perpendicular to the direction of the laser. To  
 153 eliminate optical reflection from the rotating steel cone,  
 154 its surface was blackened using tool black mixture from  
 155 Precision Brand ([www.precisionbrand.com](http://www.precisionbrand.com), UPC No.  
 156 45125). The CCD camera is mounted with a DIN ob-  
 157 jective lens (3.2×) through an adaptive tube (Edmund  
 158 Optics: U54-868). During image analysis, the distance  
 159 traveled by a particle is determined by playing 1 to 3  
 160 frames using MGI Videowave 4 software.

161 **Interfacial failure in polymer mixtures**

162 Table 2 reports the crucial characterization of the sam-  
 163 ple’s intrinsic ability to undergo interfacial slip in terms  
 164 of the slip length  $b$ . The magnitude of  $b$  is controlled  
 165 by the ratio of the bulk viscosity  $\eta$  and viscosity  $\eta_i$   
 166 at the failure plane where chain entanglement is lost:  
 167  $b = (\eta/\eta_i)l_{ent}$ , where  $l_{ent}$  is the entanglement spacing  
 168 comparable to the thickness of a disentanglement layer.  
 169 Thus, the value of  $b$  can be reduced by increasing  $\eta_i$   
 170 whose lower bound is the solvent viscosity for entan-  
 171 gled mixtures. Consequently, we have prepared three  
 172 mixtures of equal level of chain entanglement with  
 173 vastly different ability to undergo slip as shown in terms  
 174 of  $b$  in Table 2. Further detailed discussion about slip  
 175 extrapolation length for polymer mixtures can be found  
 176 in Ravindranath and Wang (2007b).

177 **Results and discussion**

178 Step strain experiments

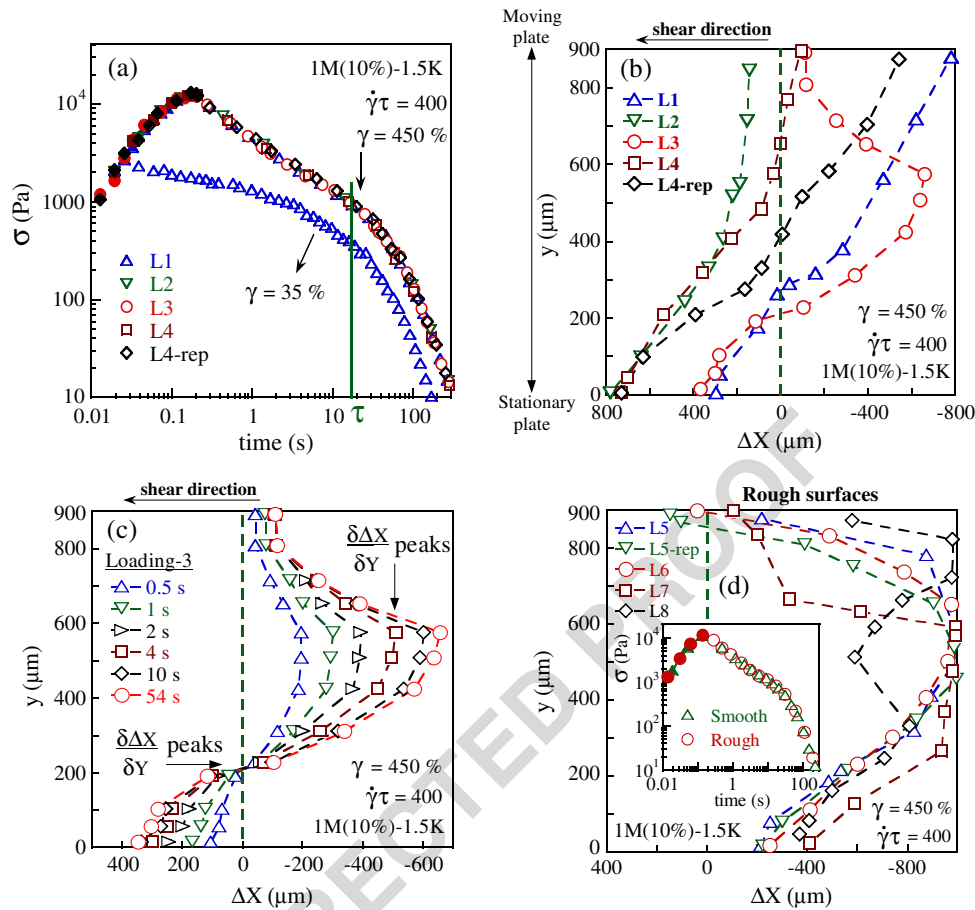
179 Rheological and PTV observations of step strain de-  
 180 formation of the three mixtures have been reported in

this section. Figure 1a shows the shear stress vs. time 181  
 data of five repeats on the 1 M(10%)-1.5 K mixture. 182  
 The applied shear strain is  $\gamma = 450\%$ , produced at a 183  
 Weissenberg number of  $W_i = 400$ . For comparison with 184  
 linear response behavior, step strain data at  $\gamma = 35\%$  185  
 have also been plotted in Fig. 1a. The filled symbols 186  
 represent the shear stress build up during the step 187  
 strain, and the open symbols are the shear stress relax- 188  
 ation data after shear cessation. The five repeats come 189  
 from 4 different loadings, labeled as L1, L2, L3, and 190  
 L4, respectively. For the fourth loading, the same step 191  
 strain was repeated and labeled as L4-rep. In case of 192  
 L1, L3, and L4-rep, the mixture was allowed to relax 193  
 for nearly 12 h before the step strain experiments were 194  
 performed and in case of L2 and L4, the mixture was 195  
 relaxed for 3 h after loading. 196

The stress relaxation characteristics show excellent 197  
 overlapping among the five data sets. Such phenom- 198  
 enology made sure that no discrepancy can be rheo- 199  
 logically apparent. In situ PTV observations show in 200  
 Fig. 1b that the step-strained samples did not relax 201  
 quiescently. In the case of L1, L2, L4, and L4-rep, the 202  
 samples appear to suffer interfacial failure that allowed 203  
 the residual stress to decline faster than quiescent chain 204  
 relaxation would cause. In other words, the traced 205  
 particles near the two interfaces made maximum move- 206  
 ments, as much as 600 to 800  $\mu\text{m}$ , after shear cessation. 207

It is statistically significant with enough repeats that 208  
 the sample disintegration may be different in each 209  
 sample loading. For example, a detailed PTV analysis 210  
 reveals in Fig. 1c that internal failure occurs for L3. 211  
 Maximum relative movements of the traced particles 212  
 are observed to take place at two locations as indicated. 213  
 In some of the repeats, Y-motion of a few particles 214  
 was also observed on the order of 20–30  $\mu\text{m}$ . More 215  
 importantly, the PTV observations in Fig. 1c show that 216  
 most of the movements occur within the first 10 s 217  
 after shear cessation, which is consistent with the initial 218  
 faster stress decline shown in Fig. 1a. On the other 219  
 hand, no discernible motions can be seen for the small 220  
 step strain of  $\gamma = 35\%$ . 221

The 1 M(10%)-1.5 K mixture tends to undergo inter- 222  
 facial failure because it has a sizable slip length  $b$ . With 223  
 $b$  comparable to the sample thickness, interfacial slip 224  
 can cause quick macroscopic recoil, resulting in acceler- 225  
 ated stress relaxation (Ravindranath and Wang 2007a, 226



**Fig. 1** **a** Shear stress vs. time plot of 5 step strain experimental repeats of 1 M(10%)-1.5 K mixture. L1, L2, L3, and L4 correspond to four different loadings and L4-rep corresponds to the repeat experiment of the fourth loading. Closed symbols indicate build up of shear stress during deformation, while open symbols are stress relaxation data. The step strain is produced at a Weissenberg number  $Wi = 400$ . Both the surfaces were smooth unlike in Fig. 1e and Fig. 4d, where the surfaces were rough. **b** Total displacement of tracer particles across the gap after cessation of step deformation for 5 repeats as observed through

PTV. **c** Displacement of tracer particles across the gap at different times after cessation of step deformation for loading-3 (L3) as observed through PTV. The two surfaces are smooth. **d** Total displacement of tracer particles across the gap after cessation of step deformation for five repeats of four different loadings. Both the surfaces were roughened by gluing sandpaper. PTV was done by placing the camera horizontally and viewing through the edge. Inset shows the rheological response of the mixture with smooth and rough surfaces

227 **b**). Majority of the previous cases in the literature,  
 228 employed either small molecular organic liquids or low  
 229 molecular weight oligomers to make well-entangled PS  
 230 or PB mixtures (Einaga et al. 1971; Fukuda et al. 1975;  
 231 Osaki and Kurata 1980; Vrentas and Graessley 1982;  
 232 Larson et al. 1988; Archer et al. 1995, 2002; Sanchez-  
 233 Reyes and Archer 2002; Islam et al. 2001, 2003; Venerus  
 234 and Nair 2006; Wen and Hua 2009). In all of these  
 235 cases, owing to large values of interfacial slip length  $b$ ,  
 236 significant interfacial failure may take place after shear  
 237 cessation similar to the one shown in Fig. 1b.

238 Sanchez-Reyes and Archer (2003) have shown that  
 239 surface roughness could minimize wall slip. Thus, it  
 240 seems a reasonable idea to examine the effect of surface

roughness on the phenomenon of non-quietest relax- 241  
 ation after step strain for the present sample. 242

Figure 1d shows the PTV measurements of the same 243  
 step strain as depicted in Fig. 1a-c except that the 244  
 surfaces of the cone and plate are made of sandpapers. 245  
 It can be clearly seen from Fig. 1d that for the five 246  
 repeats from four separate loadings, largest displace- 247  
 ment and maximum relative movements both occur in 248  
 the sample interior. Thus, the sandpaper has largely 249  
 removed the chance for the step-strained sample to 250  
 undergo (entanglement) network disintegration at the 251  
 interface between the sample and the shear surface, 252  
 leaving the sample no choice but to suffer structural 253  
 breakdown in the sample interior. It is important to 254

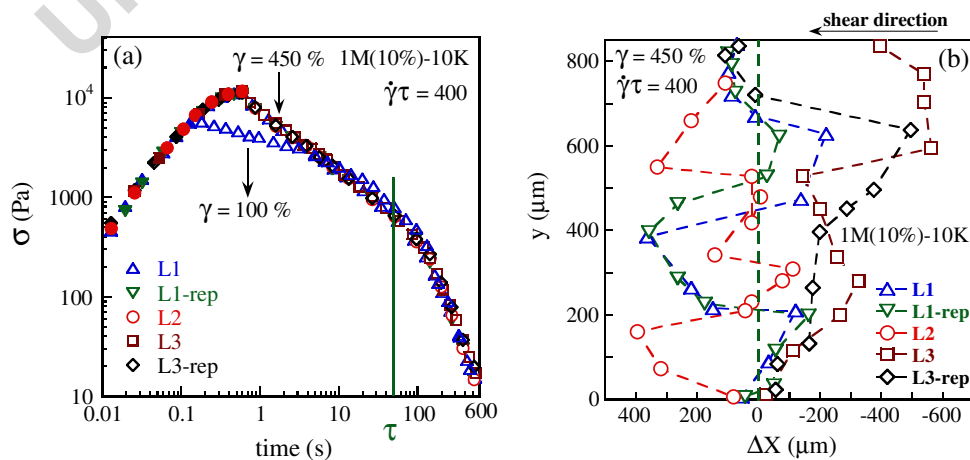
255 observe that despite the apparent difference in the  
 256 failure locations the stress relaxation signals are the  
 257 same for both smooth and rough surfaces as shown in  
 258 the inset.

259 The elastic yielding behavior observed in Fig. 1a–  
 260 d is expected to depend on the “slip characteristics”.  
 261 Table 2 shows that 1 M(10%)-10 K has much reduced  
 262 ability to undergo wall slip. So let us contrast its behav-  
 263 ior under the same step strain with the previous sam-  
 264 ple. Figure 2a and b show respectively the rheological  
 265 behavior and corresponding in situ PTV observations  
 266 in five repeats. Again, the rheological responses of all  
 267 five repeats are identical, involving accelerated stress  
 268 decline relative to that from a step strain of  $\gamma = 100\%$ .  
 269 Although the rheological character is indistinguishable  
 270 from that of the 1 M(10%)-1.5 K, the PTV observations  
 271 in Fig. 2b indicate that interfacial failure is largely  
 272 removed by employing the PBS of higher molecular  
 273 weight.

274 Further increasing the molecular weight of the  
 275 polybutadiene solvent (PBS) to 46 kg/mol, which is  
 276 a well-entangled melt itself, we give the 1 M(10%)-  
 277 46 K mixture with little ability to make any sizable  
 278 interfacial or internal slip. Consider a large step strain  
 279 (i.e.,  $\gamma = 450\%$ ): Upon shear cessation, the residual  
 280 elastic retraction force overcomes the entanglement  
 281 (cohesion) force to cause disentanglement (Wang et al.  
 282 2007a, b) over a length scale given by the entanglement  
 283 spacing  $l_{ent} \sim \phi^{-1.2} M_e$ . Let us estimate the amount of  
 284 displacement due to this disentanglement and deter-  
 285 mine whether it would result in significant macroscopic  
 286 (elastic) recoil. Assume that the mutual chain sliding

in the entanglement-free layer of thickness  $l_{ent}$  corre- 287  
 sponds to a “slip velocity”  $V_s$  at shear stress  $\sigma$ . This dis- 288  
 entanglement layer of viscosity  $\eta_i$  would be sheared at a 289  
 rate of  $V_s/l_{ent}$  so that  $\eta_i(V_s/l_{ent}) = \sigma$ . Let us assume that 290  
 this displacement would last for a period of  $\Delta t$ , leading 291  
 to  $\Delta x \sim V_s \Delta t = (l_{ent} \sigma / \eta_i) \Delta t$ . Here, the level of shear 292  
 stress  $\sigma$  can be evaluated approximately according to 293  
 $\sigma \sim G\gamma = (\eta/\tau)\gamma$  for a sudden step strain of  $\gamma$ . Thus, 294  
 we have  $\Delta x \sim b\gamma(\Delta t/\tau)$ , where  $b = (\eta/\eta_i)l_{ent}$ , and  $\tau$  295  
 is the terminal relaxation time. It is clear that  $\Delta t$  can- 296  
 not exceed  $\tau$ , beyond which the diffusion-dominated 297  
 relaxation would occur. Thus, the displacement would 298  
 only last for  $\Delta t < \tau$ . We consequently conclude for 299  
 $b/H \ll 1$  that the recoil measured in terms of a strain 300  
 $\Delta\gamma_s \sim \Delta x/H$  is negligibly small, relative to the imposed 301  
 strain because  $\Delta\gamma_s/\gamma < (b/H) \ll 1$ . The third mixture 302  
 of 1 M(10%)-46 K is designed to have  $b \sim 2 \mu\text{m} \ll$  303  
 $H \sim 1 \text{ mm}$ . Therefore, any disentanglement starting 304  
 on a length scale of  $l_{ent}$  would not produce significant 305  
 motions and would not appreciably accelerate stress 306  
 relaxation. As consequence, the rest of the sample 307  
 would retain the same amount of residue shear stress. 308  
 In other words, no part of the sample would be singled 309  
 out to undergo cohesive breakdown, and disentanglement 310  
 could only evolve democratically and uniformly 311  
 throughout the sample. 312

Because of the PBS’ high molecular weight of 313  
 46 kg/mol and corresponding solvent viscosity, Fig. 3a 314  
 shows an initial stress drop due to the viscous stress 315  
 associated with the PBS of, which is a smaller frac- 316  
 tion of the total residual stress for  $\gamma = 350\%$  than for 317  
 $\gamma = 35\%$ . The stress relaxation following  $\gamma = 350\%$  is 318

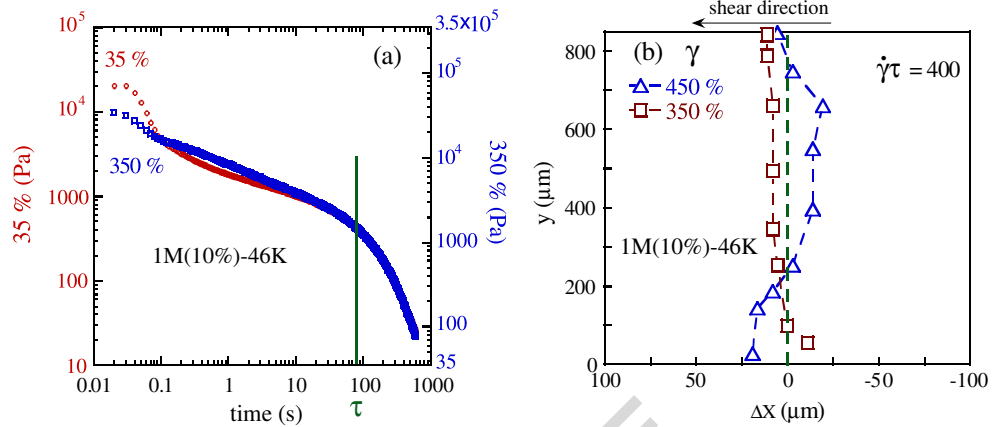


**Fig. 2** **a** Shear stress vs. time plot of five-step strain experimental repeats of 1 M(10%)-10 K mixture. L1, L2, and L3 correspond to three different loadings. L1-rep and L3-rep corresponds to the repeat experiment of the first and third loading. Closed symbols indicate build up of shear stress during deformation, while open

symbols are stress relaxation data. Both the surfaces are smooth. **b** Total displacement of tracer particles across the gap after cessation of step deformation for five repeats of three loadings as observed through PTV



**Fig. 3** **a** Relaxing shear stress vs. time for strains of 35% and 350%. **b** Total displacement of tracer particles across the gap after cessation of step deformation as observed through PTV. Both the surfaces are smooth



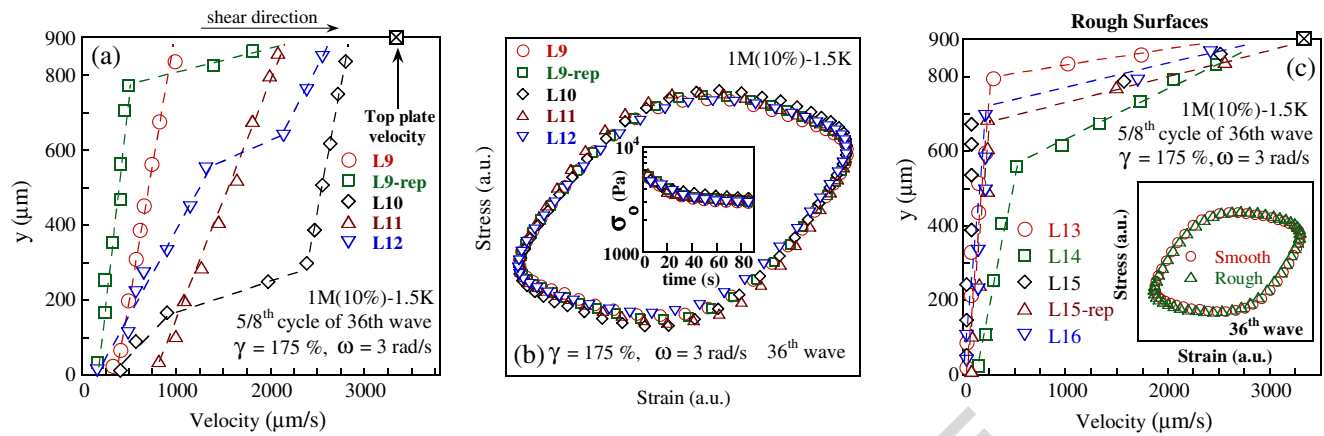
319 compared with the linear relaxation behavior for  $\gamma =$   
 320 35% by matching the stress level around the dominant  
 321 relaxation dynamics at  $\tau$ , using double  $Y$  axes. The  
 322 mismatch on the time scales ranging from 0.1 to 10 s  
 323 is real and arises from the fact that the small step strain  
 324 of 35% allows less stress relaxation during shear and  
 325 consequently contains a fuller spectrum of relaxation  
 326 dynamics, particularly some faster relaxing components  
 327 in the shear stress. Figure 3b indicates that macroscopic  
 328 motion is greatly reduced after step strain at both  $\gamma =$   
 329 350% and 450%. In absence of significant macroscopic  
 330 motions after shear cessation, the stress decrease with  
 331 time is not much different from what is observed in the  
 332 linear response regime. Actually, as noted above, the  
 333 stress decline is less rapid over the period from 0.1 to  
 334 10 s.

335 Large amplitude oscillatory shear

336 LAOS has been also used as a tool to probe the  
 337 nonlinear behavior of entangled polymer mixtures and  
 338 melts (Adrian and Giacomin 1992; Reimers and Dealy  
 339 1996; Wilhelm 2002; Debbaut and Burhin 2002; Clemeur  
 340 et al. 2003; Schlatter et al. 2005). Various analyses have  
 341 been applied to extract useful information from LAOS  
 342 measurements, including Fourier analysis (Wilhelm  
 343 et al. 1999, 2000; Dusschoten et al. 2001; Kallus et al.  
 344 2001; Karis et al. 2002; Neidhofer et al. 2003, 2004;  
 345 Sim et al. 2003) geometric aspect of viscoelasticity (Cho  
 346 et al. 2005), network model (Giacomin and Oakley 1992;  
 347 Yosick et al. 1997; Sim et al. 2003; Jeyaseelan and  
 348 Giacomin 2008), Berstein, Kearsley, and Zapas (BKZ)  
 349 model (Giacomin et al. 1993) and molecular stress  
 350 function model (Wapperom et al. 2005). When analyzing  
 351 the origin of the nonlinearities such as the stress  
 352 wave distortions, many of such studies (e.g., Giacomin  
 353 and Oakley 1992; Reimers and Dealy 1996; Jeyaseelan  
 354 and Giacomin 2008; Yu et al. 2009) assume that homo-

geneous deformation prevails during LAOS. To properly  
 explain how the wave distortion occurs using any  
 model, we first need to know from experiment whether  
 LAOS involves homogeneous deformation or not (Li  
 et al. 2009), and secondly we have to use a model that  
 permits shear inhomogeneity. The analyses themselves,  
 such as the FT analysis by Wilhelm et al. (1999) and  
 analytical treatments by Cho et al. (2005), Ewoldt et al.  
 (2009) and Yu et al. (2009), cannot reveal whether  
 shear inhomogeneity occurred or not (Rouyer et al.  
 2008). To determine from the rheometric data whether  
 shear banding occurs in LAOS, one first would have  
 to have a constitutive model that can faithfully depict  
 shear inhomogeneity in LAOS. Even then, in our opinion,  
 there is no one-to-one correspondence to allow  
 one to characterize any strain localization based only  
 on the rheometric information although Klein et al.  
 (2007) tried to do so. For these reasons, we focus on  
 the experimental determination of whether the LAOS  
 is homogeneous or not.

In this section, we report rheological and PTV  
 observations of the three entangled polymer mixtures  
 under LAOS. Velocity profiles at the instant of 5/8th  
 cycle of an oscillatory wave in steady state (when shear  
 stress response is steady) are presented in Fig. 4a for  
 the 1 M(10%)-1.5 K mixture in five repeats. The five  
 repeats come from four different loadings L9, L10, L11,  
 and L12. L9-rep refers to a repeated experiment of the  
 ninth loading-L9. Each of the experiments was done 3 h  
 after the sample loading. The applied strain  $\gamma_0$  is 175%  
 and frequency  $\omega$  is 3 rad/s, corresponding to a Deborah  
 number of  $\omega\tau \sim 51$ . At the instant of 5/8th cycle, the  
 average shear rate across the gap is  $3.7 \text{ s}^{-1}$ . It can be  
 noted from Fig. 4a that interfacial failure is observed in  
 case of L9 and L11, while bulk banding can also be seen  
 along with the interfacial failure in case of L9-rep, L10  
 and L12. Similar to the preceding PTV observations of  
 step strain, the repeats present quite different velocity



**Fig. 4** **a** Velocity profiles at the instant of 5/8th cycle of 36th wave (74.6 s) of five repeat experiments based on four different loadings on smooth surfaces of cone and plate. The applied strain  $\gamma$  is 175% and oscillation frequency  $\omega$  is 3 rad/s. The *crossed square symbol* indicates the velocity of the top moving plate. **b** Lissajous plot of 36th wave of the five repeats has been presented along with the inset showing peak shear stress vs. time data read from the rheometer. The strong distortion observed in the Lissajous plot indicates that the system is alternating between different states of viscoelasticity within each cycle. This alternation does not have to involve shear banding. But when it does, it explicitly reveals why the stress was distorted. Moreover, in presence of shear inhomogeneity, we need to bear in mind the strain used in making the Lissajous plots is only the nominal or the apparent strain. This note is worthwhile whenever one starts to think about such plots in terms of any particular constitutive model.

repeat experiments as directly given by the rheometer. **c** Velocity profiles at the instant of 5/8th cycle of 36th wave (74.6 s) of five repeat experiments of four different loading L13, L14, L15, and L16. By gluing sandpaper, both the surfaces were roughened. PTV was done by placing the camera horizontally and viewing through the edge. The *inset* shows the Lissajous plot of 36th wave with the smooth and rough surfaces

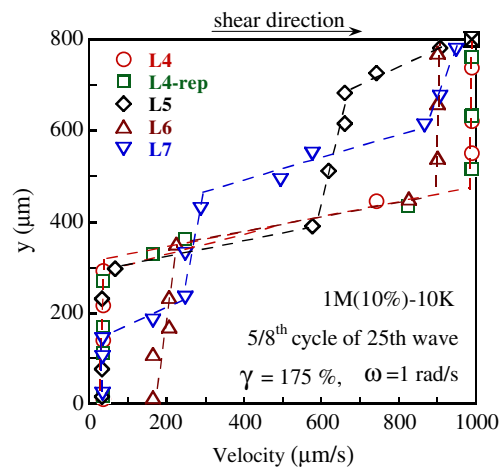
393 profiles. Yet, the rheological measurements essentially  
 394 overlap as shown in Fig. 4b. In Fig. 4b, the Lissajous  
 395 plot of 36th wave of the five repeats has been presented  
 396 along with the inset showing peak shear stress vs. time  
 397 data read from the rheometer. The strong distortion  
 398 observed in the Lissajous plot indicates that the system  
 399 is alternating between different states of viscoelasticity  
 400 within each cycle. This alternation does not have to  
 401 involve shear banding. But when it does, it explicitly  
 402 reveals why the stress was distorted. Moreover, in  
 403 presence of shear inhomogeneity, we need to bear in  
 404 mind the strain used in making the Lissajous plots is  
 405 only the nominal or the apparent strain. This note is  
 406 worthwhile whenever one starts to think about such  
 407 plots in terms of any particular constitutive model.

408 Figure 4c presents the PTV observations made with  
 409 two rough (sandpaper covered) surfaces. Apparently,  
 410 on rough surfaces, significant bulk shear banding can  
 411 take place during LAOS even for this mixture that is  
 412 inherently capable of significant wall slip. Since our  
 413 PTV does not have sufficient resolution to distinguish  
 414 shear banding of immeasurably small thickness at the  
 415 interface from true wall slip, the appreciable shear band  
 416 width produced with the rough surfaces is insightful and  
 417 significant.

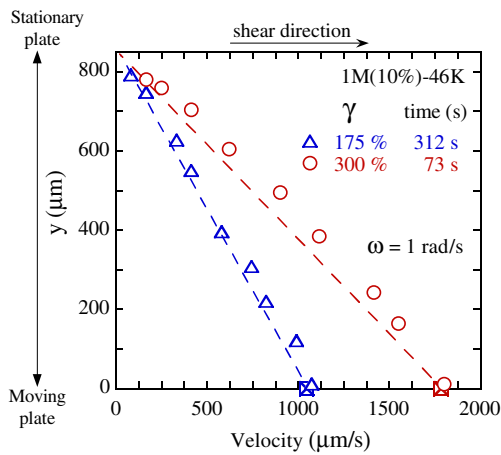
418 The PTV observations of 1 M(10%)-10 K entangled  
 419 mixture under LAOS is shown in Fig. 5. The applied  
 420 strain  $\gamma_0$  is 175% and the oscillation frequency is 1 rad/s.  
 421 For all five repeats based on three separate loadings,  
 422 strong shear banding can be observed in the bulk. In

the case of loading-6 (L6), some failure at the bottom  
 interface can be seen along with bulk banding. Use of  
 10 K PB as the solvent produces a marked difference in  
 the deformation field profiles during LAOS by compar-  
 ison between Figs. 4a and 5. The tendency to fail at the  
 interfaces as in the case of 1.5 K mixture is effectively  
 removed in 1 M(10%)-10 K.

Finally, it is instructive to examine the consequence  
 of further increasing the molecular weight of PBS.



**Fig. 5** Velocity profiles at the instant of 5/8th cycle of 25th wave (154.6 s) of 5 repeat experiments of 4 different loading L4, L5, L6, and L7. The applied strain  $\gamma$  is 175% and frequency  $\omega$  is 1 rad/s. The two surfaces are smooth



**Fig. 6** Velocity profiles at the instant of 5/8th cycle based on smooth surfaces. The applied strain  $\gamma_0$  is 175% and 300% at frequency  $\omega$  of 1 rad/s. The velocity profile is basically linear at all other moments of the cycle

correspond to the same rheological characteristics. (b) Large deformation produces structural inhomogeneity whose spatial characteristics may not be predictable. (c) Surface roughness can effectively eliminate slip-like interfacial failure allowing bulk shear banding to prevail. (d) The high molecular weight polymeric solvent (PBS) saves the entangled PB solution from undergoing severe interfacial failure. (e) The PBS of highest molecular weight (46 kg/mol) actually can suppress inhomogeneous yielding in both step strain and during LAOS. These observations greatly improve our current understanding of nonlinear rheological responses of well-entangled polymeric liquids and are the first step toward depicting how polydispersity in the molecular weight distribution might influence the state of deformation and flow.

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In the preceding subsection we already demonstrated how PBS of  $M_w = 46$  kg/mol suppressed large macroscopic motions after step strain. Figure 6 reveals, at all time, homogeneous LAOS essentially prevails in the 1 M(10%)-46 K mixture for two values of the amplitude. This sample is able to evolve toward its steady state without developing any inhomogeneous structural change. The stress level hardly changed for  $\gamma_0 = 175\%$  over time, and dropped no more than 10% for  $\gamma = 300\%$ .

**Summary**

The important role of the PBS in controlling the nonlinear rheological responses of PB mixtures to step strain and LAOS has been elucidated. Equally important is the demonstration of the effectiveness of rough surfaces in altering the location of structural failure in the 1 M(10%)-1.5 K mixture that has strong inclination to undergo wall slip (i.e., interfacial failure). At the same level of chain entanglement, the three mixtures made with PBS of different molecular weights show significant different responses to external deformation. Different repeats even produced different deformation profiles. Yet, the rheological characteristics, i.e., the stress responses, remain the same in both step strain and LAOS.

In short, there are five important findings of the present work. (a) Different states of material deformation

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