Hybrid Modulation Scheme Combining PPM with Differential Chaos Shift Keying Modulation

Meiyuan Miao, Lin Wang, Senior Member, IEEE, Marcos Katz, Member, IEEE and Weikai Xu, Member, IEEE

Abstract—In conventional M-ary differential chaos shift keying modulation (DCSK) systems, the distance between constellation points gets closer as M increases, resulting in poor performance. A hybrid modulation scheme based on pulse position modulation (PPM) and DCSK is proposed in the paper to improve bit-error-rate (BER) performance. In this scheme, one part of the bits is modulated by PPM while the other part is modulated by DCSK. Thus, information bearing signals are simultaneously modulated by the information bit and the selected pulse position of PPM which is determined by extra information bits. Analytical bit-error-rate (BER) performance of the proposed scheme is derived and verified by simulations. Results show that the considered scheme outperforms conventional M-DCSK, code index modulation DCSK (CIM-DCSK) and commutation code index DCSK (CCI-DCSK) in additive white Gaussian noise (AWGN) and multipath Rayleigh fading channels.

Index Terms—Differential chaos shift keying modulation(DCSK), pulse position modulation(PPM), hybrid modulation, bit error rate (BER).

I. INTRODUCTION

Chaotic communication has gained increasing attention as it can be used widely in spread spectrum communication systems due to its low-power, low complexity, and excellent anti-fading capabilities [1], [2]. Differential chaos shift keying (DCSK), a modulation scheme proposed for chaotic communications [3], is characterized by its simple transceiver configuration and excellent performance over multipath fading channels [4], only requiring a simple non-coherent demodulator without channel estimators and equalization [5]. Some variants of DCSK, such as permutation index DCSK(PI-DCSK) [6] and code index modulation DCSK (CIM,CCI-DCSK) [1] [7] which used index modulation [8][9] have also been proposed. A multi-resolution M-ary DCSK with M-ary phase-shiftkeying (MPSK) constellation is proposed based on quadrature chaotic shift keying (QCSK) [10] which offers better BER performance by changing the structure of constellation.

Due to its simplicity and high performance, pulse position modulation (PPM) is also widely used in spread spectrum communications. The idea of a hybrid combining modulation using PPM was first proposed in optical communications [11]. A hybrid pulse PPM-BPSK add space for transmitted reference pulse cluster (TRPC) is proposed to improve performance in [12]. Similarly, DCSK also can be combined with PPM

M. Miao, L. Wang and W. Xu are with the Department of Communication Engineering, Xiamen University, Xiamen, 361005, P. R. China. L. Wang is the corresponding author (e-mail: meiyuanmiao@foxmail.com; wanglin@xmu.edu.cn; xweikai@xmu.edu.cn).

M. Katz is with the Centre for Wireless Communications, University of Oulu, Oulu 90014, Finland (e-mail:marcos.katz@ee.oulu.fi).

for better performance in spread spectrum communication systems.

1

To improve the BER performance of conventional M-ary DCSK, a hybrid PPM-DCSK modulation scheme is proposed in this letter. The main contribution of the brief are summarized as follows. Firstly, based on a hybrid two-dimensional modulation scheme, a mixed modulation scheme with PPM and DCSK is proposed which the PPM parts bearing m_c bits signal. Secondly, the bit error rate (BER) expression for the considered system is obtained analytically and validated then by simulations. Results show that the proposed system has better BER performance than conventional M-DCSK, multidimensional CIM-DCSK and CCI-DCSK schemes.

The paper is organized as follows. Section II presents the system model of PPM-DCSK system. The calculation of the BER expressions of the proposed system is derived in section III. Simulation results and discussions are presented in section IV. Section V concludes the paper.

II. SYSTEM MODEL

The transmitter of proposed system is shown in Fig. 1, where the total transmitted bits are m_c+1 and symbol duration is $(2^{m_c}+1)R$. In the proposed system, m_c bits are mapped into a PPM position. The transmitted signal s_l can be expressed as

$$\mathbf{s}_{\mathbf{l}} = \begin{bmatrix} \mathbf{c}_{x} \\ reference \end{bmatrix}, \underbrace{b_{l} \mathbf{s}_{PPM} \bigotimes \mathbf{c}_{x}}_{information-bearing}$$
(1)

where \mathbf{c}_x is a *R*-length chaotic signal, $b_l \in \{-1, 1\}$ is information bit, \bigotimes is Kronecker operator. In the proposed system, the information bit is transmitted on one position in the PPM frame. The position is determined by mapping bits. $\mathbf{s}_{PPM} = [0, 0, ...1_{a_l}, ..., 0]_{1 \times P}$ $(P = 2^{m_c})$ in the PPM signal, where 1_{a_l} represents that the a_l^{th} position of \mathbf{s}_{PPM} is 1. a_l is a position index modulation symbol which is converted by mapping bits.

Assuming that the transmitted signal is corrupted by a multipath Rayleigh fading channel, the received signal can be written as

$$\mathbf{r}_{l} = \sum_{l=1}^{L} \alpha_{l} \delta(t - \tau_{l}) \otimes \mathbf{s}_{l} + \mathbf{n}_{l}, \qquad (2)$$

where L is the number of paths, α_l and τ_l are the channel coefficient and the path delay of the *l*th path, respectively, \otimes denotes the convolution operator. Moreover, the channel coefficients are constant over each symbol duration and the maximum multipath delay is much shorter than R, i.e., R >> τ_{lmax} . n_l is the additive white Gaussian noise (AWGN) with



Fig. 1. Block diagram of PPM-DCSK transmitter.

zero mean value and variance of $N_0/2$. The block diagram of the receiver is shown in Fig. 2. The receiver not only needs to detect the modulation bits from DCSK signal, but also the index position of PPM. That means the received reference signal need to be correlated with each *R*-length parts of received s_{PPM} , thus the a_t th part of information-bearing signal in PPM signal can be written as

$$\mathbf{r}_{inf} = \mathbf{r}_{a_l}, \quad 1 \le a_l \le P,\tag{3}$$

The decision variable I_m of the m^{th} branch when $m = a_l$ can be expressed as

$$I_m = \sum_{i=1}^R \left(\sum_{l=1}^L \alpha_l \mathbf{c}_x + \mathbf{n}_r \right) \left(\sum_{l=1}^L \alpha_l b_l \mathbf{c}_x + \mathbf{n}_{r-R}, \right) \quad (4)$$

Similarly, when $m \neq a_l$, the decision variable of the m_{th} branch can be expressed as

$$I'_{m} = \sum_{i=1}^{R} \left(\sum_{l=1}^{L} \alpha_{l} \mathbf{c}_{x} + \mathbf{n}_{r} \right) (\mathbf{n}_{r-R})$$

$$= \sum_{i=1}^{R} \sum_{l=1}^{L} \alpha_{l} \mathbf{c}_{x} \mathbf{n}_{r-R} + \sum_{i=1}^{R} \mathbf{n}_{r} \mathbf{n}_{r-R},$$
 (5)

where the symbol a_l and b_l can be estimated respectively as

$$\hat{a}_l = \arg \max_{m=1,\dots,P} (|I_m|, |I'_m|),$$

$$\hat{b}_l = \operatorname{sign}(I_{\hat{a}_l}),$$
(6)

it can be seen from (6) that the maximum of estimated a_l is decided as the position of information bearing signal in PPM frame, and b_l can be obtained by demodulating outputs of corresponding correlators. Then the bits mapped by position can be obtained from the decimal-to-binary converting part. For m_c mapped bits, the symbol duration of PPM-DCSK, CIM-DCSK and CCI-DCSK is $(2^{m_c}+1)*R$ [2], $(2^{m_c}+1)*R$ and $2^n * R(n \ge m_c)$ [7], respectively. Thus they have similar bandwidth efficiency.

III. PERFORMANCE OF PPM-DCSK ANALYSIS

A. System BER analysis

The total system BER is a function of the BER of the modulated bits P_{em} and the BER of the mapped P_{ecim} , which is the function of the error probability of PPM detection error probability P_{ed} . We set m_c as the number of bits mapped to one position of PPM index modulating symbol. The symbol



Fig. 2. Block diagram of PPM-DCSK receiver.

 a_l is mapped from m_c bits and the probability of detecting one of the remaining P-1 incorrect positions are the same at all positions. Thus, the expectation of the number of errors can be expressed as

$$Q = \sum_{i=1}^{m_c} i \frac{\binom{m_c}{i}}{P-1},$$
(7)

where P-1 incorrect position probability is $\frac{1}{P-1}$ and $\binom{n}{m} = \frac{n!}{m!(n-m)!}$. Thus the BER of mapped bits is calculated as

$$P_{ecim} = \frac{Q}{m_c} P_{ed},\tag{8}$$

the BER for modulated bits can be given by

$$P_{em} = P_e(1 - P_{ed}) + 0.5P_{ed},$$
(9)

where the P_e is bit error probability of the DCSK, and the probability of wrong PPM position detection is 50% when error probability of modulating bits is wrong, therefore the error probability of total system is expressed by

$$P_{sys} = \frac{m_c}{m_c + 1} P_{ecim} + \frac{1}{m_c + 1} P_{em}.$$
 (10)

B. Derivation of P_{ed}

Assuming that both the modulating symbol $b_l = +1$ and $a_l = \hat{m}$ (it selects position index for PPM) are transmitted. Thus the mean and the variance of I_m and I'_m are calculated by, respectively

$$\mu_{1} = \mathrm{E}\{\mathrm{I}_{\mathrm{m}}\} = \frac{\sum_{l=1}^{L} \alpha_{l}^{2} E_{s}}{2}, \quad \mu_{2} = \mathrm{E}\{\mathrm{I}_{\mathrm{m}}'\} = 0,$$

$$\sigma_{1}^{2} = \sum_{l=1}^{L} \mathrm{Var}\{\mathrm{I}_{\mathrm{m}}\} = \frac{\sum_{l=1}^{L} \alpha_{l}^{2} E_{s} N_{0}}{2} + \frac{N_{0}^{2} R}{4},$$

$$\sigma_{2}^{2} = \mathrm{Var}\{\mathrm{I}_{\mathrm{m}}'\} = \frac{\sum_{l=1}^{L} \alpha_{l}^{2} E_{s} N_{0}}{4} + \frac{N_{0}^{2} R}{4}$$

$$= E_{s} N_{0} \underbrace{\left(\frac{\sum_{l=1}^{L} \alpha_{l}^{2}}{4} + \frac{R}{4r_{s}}\right)}_{\lambda}$$
(11)

where $E_s = 2RE\{x^2\}$ is symbol energy of PPM-DCSK, $r_s = \sum_{l=1}^{L} \alpha_l^2 E_s / N_0$ is signal-to-noise ratio, $E\{\bullet\}$ is the expectation operator, and $Var\{\bullet\}$ is the variance operator, then the random variables $|I_m|$ and $|I'_m|$ follow identical folded normal distribution, thus the probability density function of

3

 $|I_m|$ and cumulative distribution function of $|I'_m|$ are calculated respectively as

$$f_{|I_m|}(y) = \frac{1}{\sqrt{2\pi\sigma_{|I_m|}^2}} \left\{ e^{-\frac{(y-\mu_{|I_m|})^2}{2\sigma_{|I_m|}^2}} + e^{-\frac{(y+\mu_{|I_m|})^2}{2\sigma_{|I_m|}^2}} \right\}, \quad (12)$$
$$F_{|I'_m|}(y) = \operatorname{erf}\left(\frac{y}{\sqrt{2\sigma_2^2}}\right). \quad (13)$$

The $\mu_{|I_m|}$ and $\sigma_{|I_m|}^2$ are the mean and variance of the $|I_m|$ which can be expressed as

$$\mu_{|I_m|} = \sqrt{\frac{2\sigma_1^2}{\pi}} e^{-\frac{\mu_1^2}{2\sigma_1^2}} - \mu_1 \operatorname{erf}\left(\frac{-\mu_1}{\sqrt{2\sigma_1^2}}\right) = \sqrt{E_s N_0} \gamma, \quad (14)$$

where

$$\gamma = \sqrt{\frac{1}{2\pi} + \frac{R}{4\pi r_s}} e^{-\left(\frac{1}{\frac{4}{r_s} + \frac{2R}{r_s^2}}\right)} - \frac{\sqrt{r_s}}{2} \operatorname{erf}\left(-\sqrt{\frac{1}{\frac{4}{r_s} + \frac{2R}{r_s^2}}}\right),$$
(15)

here and

$$\sigma_{|I_m|}^2 = \mu_1^2 + \sigma_1^2 - \mu_{|I_m|}^2$$

= $E_s N_0 \underbrace{\left(\frac{r_s}{4} + \frac{1}{2} + \frac{R}{4r_s} - \gamma^2\right)}_{\alpha}$ (16)

Assume that $X_1 = \max\{|I_m|\}, m = 1, 2, ., P - 1$. And the position of PPM detection error probability is calculated by,

$$P_{ed} = 1 - P_r \{ Y \ge X \}$$

$$= \int_{0}^{\infty} [1 - P_r \{ y \ge X \}] f_{|I_m|}(y) dy$$

$$= \frac{1}{\sqrt{2\pi\sigma_{|I_m|}^2}} \int_{0}^{\infty} \left[1 - \left[\operatorname{erf} \left(\frac{y}{\sqrt{2\sigma_2^2}} \right) \right]^{P-1} \right] \quad (17)$$

$$\times \left\{ e^{-\frac{(y - \mu_{|I_m|})^2}{2\sigma_{|I_m|}^2}} + e^{-\frac{(y + \mu_{|I_m|})^2}{2\sigma_{|I_m|}^2}} \right\} dy.$$

Let $\mu = \frac{y}{\sqrt{E_s N_0}}$, then the position detection error probability is derived as

$$P_{ed} = \frac{1}{\sqrt{2\pi\rho}} \int_{0}^{\infty} \left[1 - \left[\operatorname{erf} \left(\frac{\mu}{\sqrt{2\lambda}} \right) \right]^{P-1} \right]$$

$$\times \left\{ e^{-\frac{(y-\gamma)^2}{2\rho}} + e^{-\frac{(y+\gamma)^2}{2\rho}} \right\} d\mu,$$
(18)

 ${\cal P}_e$ is bit error probability of the DCSK which can be calculated as

$$P_{e} = \frac{1}{2} \operatorname{erfc}\left(\left[\frac{4}{r_{s}} + \frac{2R}{r_{s}^{2}}\right]^{-\frac{1}{2}}\right).$$
(19)

total system Finally, substituting these above into (10), we obtain the instantaneous BER of PPM-DCSK over Rayleigh

fading channel, and the multipath Rayleigh fading channel can be given as

$$P_{mul} = \int_{0}^{\infty} P_e \cdot f(r_s) \mathrm{d}r_s, \qquad (20)$$

where $f(r_s)$ is the PDF of r_s which can be found in [5].

IV. SIMULATION RESULTS AND DISCUSSION

In this section, simulations are carried out to evaluate the performance of the proposed system over AWGN and multipath Rayleigh fading channels. These results are then contrasted with the theoretical results derived in previous analysis on both AWGN and multipath Rayleigh fading channel. In all figures, SF represents the spreading factor and m_c is the number bits mapped into one position of the PPM modulation. In multipath Rayleigh fading channel, three paths L = 3, are considered, having equal average power gain $E[\alpha_1^2] = E[\alpha_2^2] = E[\alpha_3^2] = 1/3$, with path delays $\tau_1 = 0, \tau_2 = 1, \tau_3 = 2$. To quickly illustrate, m_c in PPM-DCSK means modulated bits number of PPM parts and the whole number of modulated bits is $m_c + 1$ while the whole number of M-DCSK is only m_c .

The analytical and simulated results for PPM-DCSK are shown in Fig. 3, where the analytical results match the simulations at high SNR. As can be also seen, BER always decreases as m_c increases and as SF decreases in AWGN while less influence in multipath fading. The reason for this behavior is that more bits in the same symbol energy are transmitted with increasing m_c , which means each transmitted bit needs less energy. Fig. 4 shows performance comparisons of PPM-DCSK, CIM-DCSK, CCI-DCSK and M-DCSK over AWGN channel. Note that the PPM-DCSK exhibits lower BER than the others, moreover the BER of M-DCSK increases as m_c increases, while PPM-DCSK decreases as m_c increases. The gain of PPM-DCSK over M-DCSK is at least about 4dB as m_c increase, and over CIM-DCSK and CCI-DCSK is about 0.3dB, 2.5dB at 10^{-4} . The performance of PPM-DCSK is significantly improved over M-DCSK. As shown in Fig. 5, BER performance of PPM-DCSK on multipath fading channel outperforms those of the other schemes when SF = 64. All schemes have similar increasing BER behavior, PPM-DCSK has less increasing tendency then others when m_c increasing. Note the good performance at high m_c of the proposed PPM-DCSK. Fig. 6 shows BER performance with the modulated bits number of these schemes over AWGN and multipath Rayleigh fading channels. The performance of M-DCSK increases monotonously as m_c increases. As m_c increases, performance of PPM-DCSK, CIM-DCSK and CCI-DCSK increases in fading but decreases in AWGN.

V. CONCLUSIONS

In this letter, a novel hybrid modulation scheme combining PPM and DCSK is considered. The scheme avoids the problem of distinguishing inaccurately the constellation points in M-DCSK systems especially in large values of M. In the proposed system, information bearing signal is carried by PPM, which carries both DCSK modulated bit and extra red m_c

^{2162-2337 (}c) 2018 IEEE. Personal use is permitted, but republication/redistribution requires IEEE permission. See http://www.ieee.org/publications_standards/publications/rights/index.html for more information.



Fig. 3. Simulation and analytical BER of PPM-DCSK system over AWGN and Rayleigh multipath fading channel with spreading factor SF = 64, the PPM modulated bits is m_c and $P = 2^{m_c}$.



Fig. 4. Performance comparisons of PPM-DCSK, CIM-DCSK, CCI-DCSK, M-DCSK over AWGN channel SF=64.

bits by position modulation. The theoretical BER expression were derived and validated by simulations. By comparing the BER performance with conventional M-DCSK, CIM-DCSK and CCI-DCSK, the numerical results show that the proposed hybrid PPM-DCSK system has superior BER performance over AWGN and multipath Rayleigh fading channel.

REFERENCES

- Y. Tan, W. Xu, T. Huang and L. Wang, "A Multilevel Code Shifted Differential Chaos Shift Keying Scheme with Code Index Modulation," *IEEE Trans. Circuits Syst. II*, 2017, DOI: 10.1109/TCSII.2017.2764916.
- [2] W. Xu, Y. Tan, F. C. M. Lau, and G. Kolumban, "Design and Optimization of Differential Chaos Shift Keying Scheme with Code Index Modulation," *IEEE Trans. Commun.*, vol. 66, no. 5, pp. 1970-1980, Mar. 2018.
- [3] G. Kolumban, B. Vizvari, W. Schwarz, and A. Abel, "Differential chaos shift keying: A robust coding for chaos communication," *in Proc. NDES*, Seville, Spain, 1996, pp. 87-92.
- [4] M. Dawa, G. Kaddoum, and Z. Sattar, "A Generalized Lower Bound on the Bit Error Rate of DCSK Systems Over Multi-Path Rayleigh Fading Channels," *IEEE Trans. Circuits Syst. II*, vol. 65, no. 3, pp. 321-325, Mar. 2018.
- [5] G. Cheng, L. Wang, W. Xu, and G. Chen, "Carrier Index Differential Chaos Shift Keying Modulation," *IEEE Trans. Circuits Syst. II*, vol. 64, no. 8, pp. 907-911, Aug. 2017.
- [6] M. Herceg, G. Kaddoum, D. Vranjes, and E. Soujeri, "Permutation Index DCSK Modulation Technique for Secure Multi-User High-Data-Rate Communication Systems," *IEEE. Trans. Veh. Technol.*, vol. 67, no. 4, pp. 2997-3011, Apr. 2018.



4

Fig. 5. BER performance comparisons of PPM-DCSK, CIM-DCSK, CCI-DCSK, M-DCSK over Rayleigh multipath fading channel with SF=64, L=3.



Fig. 6. Effect of the number of modulated bits on BER at PPM-DCSK, CIM-DCSK, CCI-DCSK, M-DCSK over AWGN and Rayleigh multipath fading channel with L = 3, SF = 64.

- [7] M. Herceg, D. Vranjes, G. Kaddoum, and E. Soujeri, "Commutation Code Index DCSK Modulation Technique for High-Data-Rate Communication Systems," *IEEE Trans. Circuits Syst. II*, 2018, DOI: 10.1109/TCSII.2018.2817930.
- [8] G. Kaddoum, M. F. A. Ahmed, and Y. Nijsure, "Code Index Modulation: A High Data Rate and Energy Efficient Communication System," *IEEE Commun. lett.*, vol. 19, no. 2, pp. 7000-7009, Feb. 2015.
- [9] G. Kaddoum, Y. Nijsure, and H. Tran, "Generalized Code Index Modulation Technique for High-Data-Rate Communication Systems," *IEEE. Trans. Veh. Technol.*, vol. 659, no. 9, pp. 175-178, Sept. 2016.
- [10] L. Wang, G. Cai, and G. Chen, "Design and performance analysis of a new multiresolution M-ary differential chaos shift keying communication system," *IEEE Trans. Wireless Commun.*", vol. 14, no. 9, pp. 5197-5208, Sept. 2015.
- [11] L. Bosotti, and G. Pirani, "A PAM-PPM signalling format in optical fiber digital communications," *Opt. Quantum Electron.*, vol. 11, no. 1, pp. 71-86, Jan. 1979..
- [12] Y. Dai, and X. Dong, "Hybrid PPM-BPSK for Transmitted Reference Pulse Cluster Systems in UWB and 60-GHz Channels," *IEEE Trans. Wireless Commun.*, vol. 3, no. 6, pp. 657-660, Dec. 2014.