

HyDRA-H: Simultaneous Hybrid Retrieval of Exoplanetary Emission Spectra

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Abstract

High-resolution Doppler spectroscopy has been used to detect several chemical species in exoplanetary atmospheres. Such detections have traditionally relied on cross correlation of observed spectra against spectral model templates, an approach that is successful for detecting chemical species but not optimized for constraining abundances. Recent work has explored ways to perform atmospheric retrievals on high-resolution spectra (HRS) and combine them with retrievals routinely performed for low-resolution spectra (LRS) by developing a mapping from the cross-correlation function to a likelihood metric. We build upon previous studies and report HyDRA-H, a hybrid retrieval code for simultaneous analysis of low- and high- resolution thermal emission spectra of exoplanets in a fully Bayesian approach. We demonstrate HyDRA-H on the hot Jupiter HD 209458b as a case study. We validate our HRS retrieval capability by confirming previous results and report a simultaneous hybrid retrieval using both HRS and LRS data. The LRS data span the HST WFC3 (1.1–1.7 μ m) and Spitzer photometry (IRAC 3.6-8 μ m) bands, while the HRS data were obtained with CRIRES on VLT at 2.3 μ m. The constraints on the composition and temperature profiles for the hybrid retrieval are more stringent than retrievals with either LRS or HRS data sets individually. We retrieve abundances of $log(H_2O) = -4.11^{+0.91}_{-0.30}$ and $log(CO) = -2.16^{+0.99}_{-0.47}$, and $C/O = 0.99^{+0.01}_{-0.02}$, consistent with previous works. We constrain the photospheric temperature to be 1498^{+216}_{-57} K, consistent with the equilibrium temperature. Our results demonstrate the significant advantages of hybrid retrievals by combining strengths of both HRS and LRS observations, which probe complementary aspects of exoplanetary atmospheres.

Unified Astronomy Thesaurus concepts: Exoplanet atmospheres (487); Exoplanet atmospheric composition (2021); High resolution spectroscopy (2096); Spectroscopy (1558); Exoplanets (498); Hot Jupiters (753)

1. Introduction

The characterization of exoplanet atmospheres has experienced rapid growth in recent years as an increasing number of spectra are becoming available with ever-improving data quality. Constraints on the chemical abundances, C/O ratios and thermal profiles of several exoplanets have been obtained using a wide variety of observations from both space-based and ground-based telescopes, and in both the optical and infrared wavelength ranges. Low-resolution spectra (LRS) from both space and the ground have allowed for unprecedented chemical characterization thanks to the photometric precision achieved. In particular, spectra from the *Hubble Space Telescope* (*HST*) have led to constraints on the chemical and thermal properties of several exoplanets (e.g., Kreidberg et al. 2014; Madhusudhan et al. 2014b; Sing et al. 2016; Evans et al. 2017; Sheppard et al. 2017).

A variety of techniques have been used to extract atmospheric properties from LRS. In particular, atmospheric retrievals provide a data-driven approach to inferring properties such as chemical compositions and thermal profiles (Madhusudhan 2018). This method involves coupling an atmospheric model to a parameter-estimation algorithm in order to fit observed spectra and derive statistical constraints on the model parameters. A variety of both models and Bayesian estimators have been used in the literature (e.g., Madhusudhan & Seager 2009, 2010; Line et al. 2013, 2016; Barstow et al. 2017; Lavie et al. 2017; Evans et al. 2018; Benneke et al. 2019). The model parameters span a wide range of chemical compositions and temperature profiles for a given observing geometry, e.g., transmission or emission spectra. Other model considerations include treatment of clouds/hazes (Line & Parmentier 2016;

Barstow et al. 2017; MacDonald & Madhusudhan 2017), radiative disequilibrium (Gandhi & Madhusudhan 2018), stellar heterogeneities (Pinhas et al. 2018), and multi-dimensional effects (Feng et al. 2016; Blecic et al. 2017).

Emission spectra of transiting planets observed at secondary eclipse provide a unique window into the dayside of their atmospheres. In particular, such spectra probe a wide range of pressures and temperatures, allowing the thermal profile of the atmosphere to be constrained. Since the thermal emission of exoplanets peaks in the infrared, observations to date have largely been restricted to this spectral range. In particular, nearinfrared spectra and photometry from HST and Spitzer have resulted in constraints on multiple chemical abundances as well as the inference of thermal inversions in several exoplanets (e.g., Haynes et al. 2015; Evans et al. 2017; Sheppard et al. 2017; Kreidberg et al. 2018). However, most compositional constraints have been obtained for H₂O given the spectral range of these observations. Retrievals of emission spectroscopy have not only been performed on transiting planets, but also on directly imaged planets and field brown dwarfs, providing insight into the properties of a wide range of sub-stellar objects (e.g., Burningham et al. 2017; Lavie et al. 2017; Line et al. 2017).

On another front, high-resolution Doppler spectroscopy (HRS) has enabled the detection of several chemical species in exoplanet atmospheres (e.g., Snellen et al. 2010; Brogi et al. 2012; Birkby et al. 2017; Nugroho et al. 2017). These ground-based observations resolve individual transition lines from the planetary spectrum, which are distinguished from the stellar spectrum thanks to the Doppler motion of the planet as it orbits the host star (see, e.g., review by Birkby 2018). Thanks to

stable high-resolution spectrographs on telescopes such as the Very Large Telescope (VLT), Keck and Subaru, HRS has begun to play a significant role in the characterization of exoplanet atmospheres (e.g., Brogi et al. 2012; Nugroho et al. 2017). Molecules such as H₂O and CO have been detected in multiple hot Jupiters using this method (Snellen et al. 2010; Brogi et al. 2012; Birkby et al. 2013, 2017; Rodler et al. 2013). One of the key strengths of high-resolution Doppler spectroscopy is its ability to detect trace species in exoplanet atmospheres. For example, TiO has been detected in WASP-33b (Nugroho et al. 2017), HCN has been seen in multiple planets (Hawker et al. 2018; Cabot et al. 2019), and various atomic and ionic species have also been observed using highresolution observations (Hoeijmakers et al. 2018). In the next decade, this new era of atmospheric observations is expected to flourish thanks to upcoming facilities such as the Extremely Large Telescope (ELT) and the Giant Magellan Telescope (GMT), which will allow an increasing range of chemical species to be probed for ever-smaller planets, potentially allowing for the characterization of rocky exoplanets (Rodler & López-Morales 2014; Snellen et al. 2015).

More recently, retrievals have begun to be adapted for highresolution spectra as well. HRS observations have traditionally been analyzed by cross correlation with model spectra, and detections of chemical species were made by exploring spectra over a grid of atmospheric parameters (e.g., Brogi et al. 2012; Birkby et al. 2017; Nugroho et al. 2017). However, a gridsearch approach does not offer a robust statistical exploration of the parameter space, thereby precluding statistical estimates of the model parameters given the data. This is in contrast to the retrievals performed on LRS, as discussed above. Brogi et al. (2017) first performed a joint analysis of high-resolution and low-resolution observations for HD 209458b. Brogi & Line (2019) went on to suggest a cross correlation to loglikelihood mapping and performed the first, fully Bayesian retrieval on HRS observations. This method not only allows the presence of chemical species to be inferred, but also provides some constraints on their abundances and the thermal profile of the atmosphere using HRS observations.

Combined retrievals with low- and high-resolution spectra offer new promise for atmospheric characterization. Since LRS and HRS are sensitive to different atmospheric properties, analyzing both types of observations in parallel allows more robust constraints to be made on the properties of exoplanet atmospheres. For example, LRS observations are more sensitive to absolute abundances than HRS, but are affected by degeneracies between the overlapping opacities of different species in the observed spectral bands. However, HRS is sensitive to the unique fingerprints of each species and could potentially be used to break these degeneracies. Moreover, HRS observations probe regions higher up in the atmosphere (i.e., lower pressures) compared to LRS. Brogi & Line (2019) developed a fully Bayesian framework for combining LRS and HRS observations in atmospheric retrievals of thermal emission spectra of exoplanets. In this work, we demonstrate this framework on combined LRS and HRS observations of HD 209458b.

We report HyDRA-H, a new hybrid retrieval code building upon our existing HyDRA retrieval framework for LRS (Gandhi & Madhusudhan 2018), and adopting the high-resolution retrieval framework of Brogi & Line (2019). We use this method to perform a fully Bayesian, simultaneous

hybrid retrieval on observations of HD 209458b. The low-resolution spectrum we use is from the *Hubble Space Telescope*'s Wide Field Camera 3 (*HST*/WFC3) in the 1.1–1.7 μ m range and Spitzer's Infrared Array Camera (IRAC) at 3.6, 4.5, 5.8 μ m and 8.0 μ m. For the high-resolution spectrum we use archival observations at 2.3 μ m obtained using the CRIRES instrument on the VLT (Snellen et al. 2011). With the results from this hybrid retrieval, we explore the chemical detections, abundances, and *P-T* profile of the dayside atmosphere of HD 209458b.

In what follows, we discuss the retrieval method and its architecture in Section 2. In Section 3, we outline the high-resolution data used for this work as well as its detrending and analysis. We validate the method against published results in Section 4. Using these methods, we perform a hybrid retrieval on the combined HRS and LRS observations of HD 209458b, presenting our results in Section 5. Our conclusions are discussed in Section 6.

2. Methods

In this work, we develop a hybrid retrieval code, HyDRA-H, capable of simultaneously retrieving low-resolution and highresolution emission spectra of transiting exoplanets. In the past, retrievals have typically been designed for LRS only, while high-resolution spectra were analyzed separately using crosscorrelation methods. Recently, Brogi et al. (2017) presented the first joint analysis of low- and high-resolution spectra on the dayside emission spectra of HD 209458b. This method involved performing a retrieval on low-resolution data and using the resulting posterior probability distributions as priors in the analysis of the high-resolution data. Following this, Brogi & Line (2019) made a further step by developing a joint retrieval framework for low- and high-resolution spectra to be analyzed in parallel. To do this, they developed a metric to calculate the likelihood of model spectra based on the cross correlation of the model with the high-resolution data. They demonstrate the capabilities of this method on simulated data, showing that the low- and high-resolution spectra contribute complimentary constraints on the atmospheric model parameters. Furthermore, this method has the advantage of allowing both types of spectra to freely explore the full parameter space.

Here, we adapt the HyDRA retrieval framework (Gandhi & Madhusudhan 2018) to analyze high-resolution data as well as LRS, using the methods from Brogi & Line (2019) to treat the high-resolution models and data. We then apply this hybrid retrieval method, HyDRA-H, to demonstrate the first simultaneous retrieval on low- and high-resolution spectra of HD 209458b. The architecture of HyDRA-H is shown in Figure 1. In this section, we first describe the retrieval framework and the calculation of model spectra in Section 2.1. We then outline how a combined LRS-HRS likelihood is calculated for each model spectrum in Section 2.3.

2.1. Retrieval Architecture

The central element of the retrieval framework is the calculation of model spectra and their comparison to low-/high-resolution data. In this work, we calculate model spectra using an adaptation of the HyDRA retrieval framework (Gandhi & Madhusudhan 2018). Each atmospheric model in the retrieval is defined by parameters describing its chemical abundances and *P-T* profile. The model computes radiative

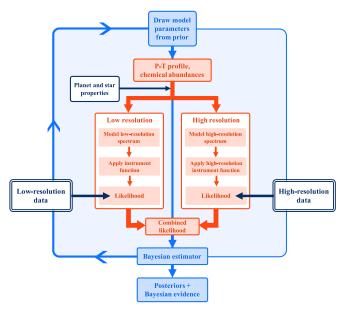


Figure 1. The hybrid modeling and retrieval framework. Model parameters are drawn from the priors listed in Table 1 and used to generate two types of model spectra: low-resolution for comparison with low-resolution data, and high-resolution for comparison to high-resolution Doppler spectroscopy.

transfer in a plane-parallel atmosphere, assuming hydrostatic equilibrium and an ideal gas equation of state. The methodology used to compute radiative transfer is described in Gandhi & Madhusudhan (2018). The chemical species we include in this work are H₂O, CO, CO₂, and HCN, which are known to have strong opacity in hot-Jupiter atmospheres, and their mixing fractions are assumed to be constant with depth. The molecular cross sections for these species are calculated as in Gandhi & Madhusudhan (2017) using line lists from the HITEMP database for H₂O, CO, and CO₂ (Rothman et al. 2010) and the ExoMol database for HCN (Harris et al. 2006; Barber et al. 2014; Tennyson et al. 2016). Figure 2 shows the cross sections for the low- and high-resolution spectral ranges. CO_2 has a very weak cross section in the 2.29–2.35 μ m spectral range compared to the other species, and thus, we do not include this species in our HRS calculations. The CO2 can however show strong degeneracies with CO in the Spitzer $4.5 \,\mu \text{m}$ band due to their similar strong cross sections. In addition to the molecular absorption, all of our spectral models also include collisionally induced absorption (CIA) from H₂-H₂ and H₂-He interactions (Richard et al. 2012). We parameterize the P-T profile analytically using the method of Madhusudhan & Seager (2009), which requires six parameters (Table 1). Once a model spectrum is generated, the relevant instrument function is applied before it is compared to the data and a likelihood is calculated. The Bayesian inference and parameter estimation is performed using PyMultiNest (Feroz & Hobson 2008; Feroz et al. 2009, 2013; Buchner et al. 2014), a Nested Sampling Bayesian parameter-estimation algorithm (Skilling 2006).

The HyDRA-H retrieval framework is shown in Figure 1. This differs from the HyDRA retrieval framework as a high-resolution spectrum is computed as well as a low-resolution spectrum. In particular, this method takes advantage of the fact that low- and high-resolution spectra are sensitive to different atmospheric properties to optimize the spectral calculations.

Once a set of atmospheric parameters is drawn by the Bayesian estimator, the low- and high-resolution model spectra are computed separately, and each compared to the low- and highresolution data, respectively. Since low-resolution emission spectra are sensitive to the absolute planet-star flux ratio, the low-resolution model is computed using the more accurate double-ray quadrature scheme for radiative transfer, as described by Gandhi & Madhusudhan (2018). Due to the self-calibration of high-resolution data (described in Section 3), sensitivity to absolute flux levels is reduced. We therefore use single-ray radiative transfer to compute the high-resolution models, for computational efficiency. In contrast, the highresolution observations resolve individual molecular lines and are very sensitive to the presence of individual molecules as well as their relative abundances. The high-resolution model spectra are therefore calculated at a wavenumber spacing of $0.01 \, \mathrm{cm}^{-1} \ (R \sim 5 \times 10^5 \, \mathrm{at} \, 2 \, \mu \mathrm{m})$. The low-resolution models are calculated at a slightly lower spectral resolution (Gandhi & Madhusudhan 2017) using cross sections with a wavenumber spacing of $0.1 \, \text{cm}^{-1}$.

In addition to the chemical and thermal model parameters, three extra parameters are needed to compare the high-resolution models to high-resolution data. The parameters $dK_{\rm p}$ and $dV_{\rm sys}$ are perturbations to the known planetary radial velocity semi-amplitude and the systemic velocity, respectively. Including these parameters prevents the retrieval from being biased by uncertainties in the measurements of $K_{\rm p}$ and $V_{\rm sys}$. Their retrieved values are expected to be consistent with zero, which indicates that the planetary signal is detected at the expected location in $K_{\rm p}-V_{\rm sys}$ space. We also include a scaling parameter, $\log(a)$, which is discussed further in Section 3.2. The full list of model parameters used and their priors are shown in Table 1.

2.2. Observations

Here, we discuss the LRS and HRS observations for the retrievals conducted in this work. We obtain dayside emission spectra for HD 209458b at low and high spectral resolution covering a wide spectral range. We retrieve the LRS-only, HRS-only, and the combined data in separate retrievals in this work, which is discussed in detail in Sections 4 and 5. The LRS data consists of *HST* WFC3 and *Spitzer* observations, and the HRS data is obtained from archival CRIRES observations (Snellen et al. 2011). The low-resolution *HST* observations have been obtained from Line et al. (2016) and span the 1.1–1.7 μ m range. The *Spitzer* photometric observations cover the IRAC 1–4 bands in the \sim 3–10 μ m range (Diamond-Lowe et al. 2014).

The high-resolution K-band observations of HD 209458b have been obtained by the CRIRES spectrograph (Kaeufl et al. 2004) at the VLT. These were obtained as part of the CRIRES survey of hot-Jupiter atmospheres (Snellen et al. 2011) first presented in Schwarz et al. (2015) and more recently reanalyzed in Brogi et al. (2017), Hawker et al. (2018), and Brogi & Line (2019). These observations cover the 2.29–2.35 μ m range, where H₂O and CO show strong absorption (see Figure 2). The HRS data analysis on these high-resolution observations is discussed in Section 3.

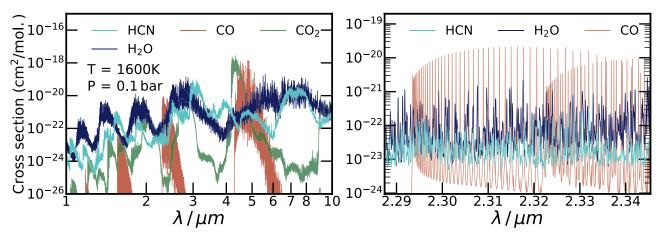


Figure 2. Molecular cross sections for the four species retrieved in the hybrid retrieval. In the left panel, we show the cross sections between 1 and 10 μ m for the HST WFC3 and Spitzer observations and the 2.29–2.35 μ m CRIRES range is shown on the right.

Table 1
Priors and Prior Ranges for the Model Parameters: Molecular Mixing Fractions $(X_{\text{H}_2\text{O}}, X_{\text{CO}}, X_{\text{CO}_2}, X_{\text{HCN}}), P$ -T Profile Parameters $(T_{100\text{mb}}, \alpha_1, \alpha_2, P_1, P_2, P_3),$ and Doppler Spectroscopy Parameters $(dK_p, dV_{\text{sys}}, \log(a))$

Parameter	Prior	Prior Range
$\overline{X_{\text{H}_2\text{O}}, X_{\text{CO}}, X_{\text{CO}_2}, X_{\text{HCN}}}$	log-uniform	10 ⁻¹⁵ -1
$T_{100\mathrm{mb}}/\mathrm{K}$	linear	300-2800
$\alpha_1/\mathrm{K}^{-1/2}$	linear	0-1
$\alpha_2/K^{-1/2}$	linear	0-1
P_1 /bar	log-uniform	$10^{-6} - 10^2$
P_2 /bar	log-uniform	$10^{-6} - 10^2$
P_3 /bar	log-uniform	$10^{-2} - 10^2$
$dK_{\rm p}/{\rm km~s^{-1}}$	linear	-50 to 50
$dV_{\rm sys}/{\rm km~s^{-1}}$	linear	-50 to 50
$\log(a)$	linear	-2 to 2

2.3. Likelihood Calculation

Once the low- and high-resolution models have been computed, their log-likelihoods are calculated relative to the low- and high-resolution data, respectively. The overall likelihood for the atmospheric model is then found by taking the product of the low- and high-resolution likelihoods. The log-likelihood for the model comparison with LRS data is based on the chi-square metric, as has been used in many previous works (e.g., Gandhi & Madhusudhan 2018; Brogi & Line 2019):

$$\ln(\mathcal{L}_{\text{low}}) = -\sum_{i} \frac{(y_{\text{obs},i} - y_{\text{model},i})^{2}}{2\sigma_{i}^{2}},$$

where the sum is over all data points, $y_{\text{obs},i}$ are the observed fluxes with uncertainties σ_i , and $y_{\text{model},i}$ are the corresponding model fluxes.

Since the high-resolution Doppler spectroscopy observations are analyzed using cross correlation, a different metric is used to assess the goodness of fit. As discussed by Brogi & Line (2019), such a metric should preserve the sign of the correlation coefficient such that emission lines are not fitted by absorption lines (and vice versa), and the metric should be sensitive to the scaling of the model. In this work, we use the metric developed by Brogi & Line (2019; discussed in Section 3.2) to calculate

the high-resolution log-likelihood, $ln(\mathcal{L}_{high})$. The total log-likelihood for a given atmospheric model is then

$$ln(\mathcal{L}_{tot}) = ln(\mathcal{L}_{low}) + ln(\mathcal{L}_{high}).$$

3. High-resolution Observations

Here, we describe the data analysis of the HRS observations. The data were taken over two nights (2011 July 18 and 25) across the 2.29-2.35 μ m K-band (Snellen et al. 2011) with a spectral resolution $R \sim 10^5$. There are 59 and 54 spectra from the first and second night, respectively. Both sets of spectra are phase resolved across a range of $\phi \sim 0.5$ –0.6 capturing bright dayside emission of HD 209458b just after secondary eclipse. This data set was first used to provide evidence for CO in the dayside atmosphere (Schwarz et al. 2015) and subsequent studies combining low-resolution observations detected CO (Brogi et al. 2017; Brogi & Line 2019). A more recent analysis of the high-resolution data set has also resulted in the detection of CO and H₂O (Hawker et al. 2018), though we note that detecting H₂O is somewhat sensitive to the detrending procedure for removing telluric lines. We use the same data reduction procedure as that described in Hawker et al. (2018) and Cabot et al. (2019).

3.1. Detrending

Once reduced, the spectra from each detector form an M by N matrix where M is the number of frames from a given observation and N is the number of wavelength channels, typically 1024. The flux in a given pixel, F, is a function of wavelength and time given by the sum of the stellar (F_s) and planetary flux (F_p) multiplied by the telluric absorption (T_E).

$$F(\lambda, t) = T_{E}(\lambda, t)F_{s}(\lambda, t)\left(1 + \frac{F_{p}(\lambda, t)}{F_{s}(\lambda, t)}\right). \tag{1}$$

The telluric absorption is expected to be constant with time and stellar flux quasi-constant with time as the stellar motion is on the order of ms^{-1} with negligible Doppler shift compared to the planet motion ($\sim km \, s^{-1}$), which shifts the planet signal across many wavelength channels during a night of observations. Using the same procedure outlined in Brogi & Line (2019), we

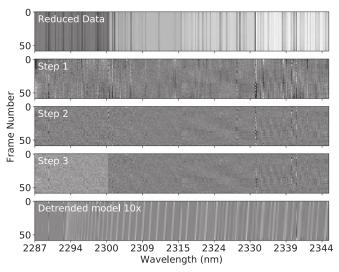


Figure 3. Illustration of the detrending steps (detailed in Section 3.2) as performed on the K-band CRIRES observations from 2011 July 18 with the data from all four detectors shown. The bottom panel shows a $10 \times$ strength model constructed prior to cross correlation (see Section 3.2) treated with same detrending method. The noisy channel (\sim 2332 nm) seen in steps 1 and 2 is from a detector edge and is dealt with by masking in step 3.

remove the stellar and telluric features through the steps illustrated in Figure 3 and described as follows:

- We find the mean spectrum over time and fit it to each individual spectrum with a second-order polynomial and divide out the fit.
- We remove significant time-dependent residuals by fitting a second-order polynomial to each wavelength channel and divide out the fit. Such residuals are associated with telluric H₂O lines.
- 3. We mask any noisy wavelength channels and update N; these masked noisy channels have a standard deviation >3 times the standard deviation of the matrix. The data corresponding to each spectrum are also mean subtracted, removing the continuum prior to cross correlation.

In essence, the detrending process uses the data to find an approximation of the multiplicative term $T_{\rm E}(\lambda, t)F_{\rm s}(\lambda, t)$ in Equation (1) and divide it out to leave the planet to star flux ratio (plus one). In reality, the multiplicative term is not perfectly removed, hence, the need to detect the planet via cross correlation of the detrended data with models. We use this detrending method, however, for the following reasons. First, we can validate our hybrid retrieval framework through comparison of our high-resolution results with Brogi & Line (2019). Second, it is computationally straightforward and has relatively few parameters (e.g., order of each polynomial fit, and n-sigma masking). Thus, during the retrieval, it can be applied to each of the tested models to fairly account for the effects of the detrending process on the planet signal to avoid biases. The potential limitation of the method is whether it approximates the $T_{\rm E}(\lambda, t)$ $F_{\rm s}(\lambda, t)$ term as well as other more computationally expensive algorithms such as SYSREM or PCA, potentially preventing it from being as effective. This is especially pertinent for analysis of more heavily contaminated spectral ranges such as the 3 μ m L-band. Further discussions and comparisons on detrending methods can be found in Hawker et al. (2018) and Cabot et al. (2019).

3.2. The HRS Log-likelihood Calculator

As noted above, the detrending process will alter the planet signal. Thus, prior to cross correlation, we treat each model in as similar way as possible to real data. A high-resolution model spectrum (generated by the architecture detailed in Section 2) is fed to the HRS likelihood calculator along with the retrieval parameters $dV_{\rm sys}$ and $dK_{\rm p}$. The model spectrum is convolved to the CRIRES spectral resolution $R\approx 84,000$, then Doppler shifted using linear interpolation by velocities calculated according to Equation (2) to produce a model equivalent of the $F_{\rm p}/F_{\rm s}$ term in Equation (1) as an M by N matrix

$$V_{\rm p}(t) = (K_{\rm p} + dK_{\rm p})\sin(2\pi\phi(t)) + V_{\rm sys} + dV_{\rm sys} + V_{\rm b}(t).$$
 (2)

The model $(1+F_{\rm p}/F_{\rm s})$ is then multiplied by the $T_{\rm E}$ $F_{\rm s}$ matrix obtained from and divided out of the data during detrending. The detrending steps 1–3 are then applied to the model $T_{\rm E}$ $F_{\rm s}(1+F_{\rm p}/F_{\rm s})$, similar to detrending the observations. The detrended model is then cross correlated with the detrended data. The likelihood is calculated via the likelihood mapping derived in Brogi & Line (2019), which uses Zucker (2003) as a base and is summarized as follows. Each detrended observed spectrum $s(\lambda)$ is modeled by a detrended model spectrum $m(\lambda)$ Doppler shifted in wavelength by $\Delta\lambda$ and scaled by a factor a, added with some Gaussian noise with a standard deviation $\sigma(\lambda)$ according to Equation (3)

$$s(\lambda) = am(\lambda - \Delta\lambda) + \sigma(\lambda)\mathcal{N}(0, 1). \tag{3}$$

The log-likelihood for such a model is given by Equation (4), where N is the number of wavelength channels

$$\log(\mathcal{L}_{high}) = -N \log(\sigma(\lambda)) - \frac{1}{2\sigma^2} \sum_{\lambda} [s(\lambda) - am(\lambda - \Delta\lambda)]^2.$$
 (4)

The maximum likelihood estimator $\hat{\sigma}$ is found by setting the partial derivative $\partial_{\sigma} \log(L) = 0$. Setting $\sigma = \hat{\sigma}$ in Equation (4) and discarding the additive constant N/2, gives Equation (5)

$$\log(\mathcal{L}_{high}) = -\frac{N}{2} \log \left[\frac{1}{N} \sum_{\lambda} [s(\lambda)^2 - 2s(\lambda) am(\lambda - \Delta \lambda) + a^2 m(\lambda - \Delta \lambda)^2] \right]. \tag{5}$$

A final detail is in setting the scale factor a. Mathematically, the maximum likelihood estimator can be used and found from $\partial_a \log(L) = 0$. A more physically motivated approach would be to set a = 1 to avoid unphysical scalings of the planet to star flux ratio and line strengths. In an HRS retrieval, imposing a = 1 ensures the line depths of the tested models are set by the physical/chemical properties of the atmospheric model. In the hybrid retrieval, including a as a retrieval parameter is useful as a method of ensuring the P-T profile is correctly constrained by the low-resolution data. This is because the HRS has a tendency to favor stronger line strengths corresponding to higher temperatures but given the lack of continuum the highresolution data should not be used to constrain the absolute temperature thus using a makes an allowance for this effect. By performing the summation and setting a = 1, the meaning of the terms inside the log of Equation (5) becomes clear (see

Equation (6))

$$\log(\mathcal{L}_{high}) = -\frac{N}{2}\log(\langle s^2 \rangle_{\lambda} - 2\langle sm \rangle_{\lambda} + \langle m^2 \rangle_{\lambda}).$$
 (6)

The first and third terms are the variances of a given detrended observed spectrum and detrended model spectrum, respectively. The second term is twice the normalized dot product of the detrended observed spectrum with the detrended model spectrum and calculated when the two are cross correlated. While the first term is a constant, the second and third terms are model dependent and also vary with $\Delta\lambda$ (a proxy for $dV_{\rm sys}$ and dK_p). Using this method, every spectrum from a given night and detector yields a log-likelihood which are summed for all spectra to obtain a single log-likelihood from the highresolution analysis. This log-likelihood can then be used to either perform a standalone HRS retrieval or used in a joint LRS+HRS retrieval by simply summing the log-likelihoods produced from the two analyses. As detailed in Section 2, Bayesian analysis can then be performed to retrieve the parameters of interest. For additional details about the likelihood mapping, we refer the reader to Brogi & Line (2019) and Zucker (2003).

4. Validation

We now validate our hybrid retrieval framework HyDRA-H by comparing to previous work (Brogi & Line 2019), which uses HRS-only observations. We retrieve the atmospheric properties of HD 209458b using high-resolution spectra of the system observed over two nights at phases of $\phi \sim 0.5$ –0.6, i.e., shortly after secondary eclipse. As discussed in Section 3, we use archival observations obtained as part of the CRIRES survey of hot Jupiters (Snellen et al. 2011). These spectra span the 2.29–2.35 μ m wavelength range and have been obtained at a resolution of $R \sim 10^5$. Following Brogi & Line (2019), we retrieve the H_2O and CO volume mixing ratios, dK_p , dV_{sys} and the temperature profile. We parameterize the P-T profile over six free parameters, $T_{100\text{mb}}$, α_1 , α_2 , P_1 , P_2 , and P_3 using the prescription of Madhusudhan & Seager (2009). We run our retrievals using Nested Sampling with 1000 live points and \sim 22,000 wavelength points at 0.01 cm⁻¹ spacing between 2.25 and 2.37 μ m. This corresponds to a model spectral resolution of $R \sim 4 \times 10^5$. We conduct the retrievals using the highresolution observations only as was done in Brogi & Line (2019).

Figure 4 shows the posterior distributions for the retrieved parameters. The P-T profile is shown in Figure 9 and agrees well with the constrained P-T profile from the high-resolution retrieval by Brogi & Line (2019). The planet's photospheric temperature is also within 1σ of the equilibrium temperature and shows no signs of a thermal inversion.

The deviations $dK_{\rm p}$ and $dV_{\rm sys}$ are within $\sim 1\sigma$ of the expected value of 0, indicating that the planet's signal has been detected at the expected location in the $K_{\rm p}-V_{\rm sys}$ plane without any spurious peaks (e.g., from stellar lines) interfering with the result significantly. We do observe a very weak peak at positive $dK_{\rm p}$ and $dV_{\rm sys}$ values, which we attribute to noise in the $K_{\rm p}-V_{\rm sys}$ plane. Figure 4 shows that the two parameters are correlated with each other in a similar way to that seen in previous

high-resolution studies that perform cross correlation on the spectral models (Schwarz et al. 2015; Hawker et al. 2018).

We also find good agreement in the retrieved chemical abundances of H₂O and CO to both previous high- and lowresolution retrievals (Line et al. 2016; Brogi & Line 2019). We constrain the H₂O to be $log(H_2O) = -4.0^{+1.2}_{-2.7}$, consistent to within $\sim 1\sigma$ of Brogi & Line (2019) as shown in the HRS-only posterior in Figure 7. This abundance estimate is also consistent with expectations from chemical equilibrium at solar abundance (Madhusudhan 2012; Moses et al. 2013) but also allows for significantly sub-solar H₂O. The retrieval does indicate a long tail in the distribution at low abundance for the H₂O. Hence, our detection significance for H₂O in this HRSonly retrieval is lower than the other retrievals we conduct (see Table 2). We are not able to strongly constrain the H₂O given that its features are weak in this spectral range. On the other hand, CO has a strong cross section in this part of the spectrum (see Figure 2) and is therefore better constrained at $log(CO) = -1.9^{+1.2}_{-0.9}$. The CO thus has a higher detection significance than the H₂O in the high-resolution only retrieval at 4.6σ confidence because of its stronger cross section. This result is also consistent with Brogi & Line (2019). In Section 5, we will compare and contrast these to the low-resolution and hybrid constraints.

Previous work has shown that the choice of line list for H_2O can influence detections and the abundance estimates (Brogi & Line 2019). Thus, we have used line lists for H_2O and CO from the HITEMP database (Rothman et al. 2010) as used by Brogi & Line (2019). Our temperature profile on the other hand has been parameterized differently to Brogi & Line (2019); but ultimately, the P-T profiles are in agreement to within 1σ , particularly for the photosphere at $P \sim 0.1$ bar. We are able to constrain the temperature profile similarly despite the differences in parameterization as both allow a full exploration of the possible parameter space, encompassing thermal inversions and non-inverted profiles.

While we generally observe good agreement with previous work by Brogi & Line (2019), we do note some differences in the posteriors for the HRS-only retrieval. While consistent to within 1σ , our abundance peak for H₂O is at a slightly higher abundance and our CO abundance only shows a strong lower limit. Previous high-resolution analysis using a different method also indicated sub-solar H₂O (Brogi et al. 2017) whereas we see an H₂O peak at a sub-solar value but which allows for solar values as well. This difference may be attributed to some differences in our models and/or data analysis. Our P-T profile is parameterized from the work in Madhusudhan & Seager (2009), whereas Brogi & Line (2019) use the Guillot (2010) prescription. We see a slightly shallower temperature gradient in the atmosphere which allows the abundance of H₂O and CO to extend to higher values to explain the line depths seen in the observations. However, this difference is less of a concern as the LRS observations are much more sensitive to the temperature profile than HRS and thus give better constraints for the hybrid and LRS-only retrieval as shown in the posteriors in Figures 5 and 8 and discussed in Section 5. We also see some differences in the retrieved values of dK_p and $dV_{\rm sys}$. These likely arise from our analysis of the CRIRES data. Our wavelength calibration is performed independently and our orbital solution is potentially different to that used in Brogi & Line (2019), which would affect dK_p and dV_{sys} . This could also slightly alter the retrieved

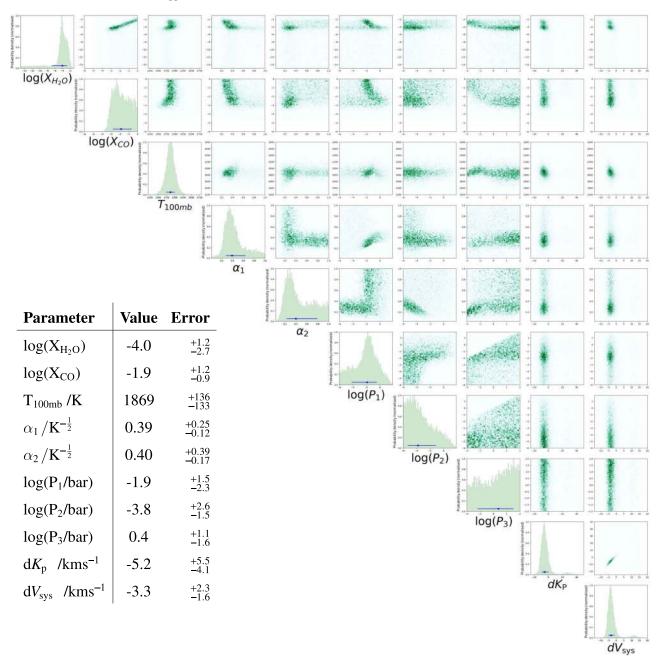


Figure 4. Posterior distribution of HD 209458b from the retrieval of the high-resolution 2.29–2.35 μ m CRIRES observations (Snellen et al. 2011). We retrieved two volatile chemical species, H₂O and CO, and parameterized the atmospheric temperature profile with six parameters, as discussed in Gandhi & Madhusudhan (2018). We also include two additional parameters, dK_p and dV_{svs} .

 Table 2

 Detection Significances for H₂O and CO for Each of the Retrievals Conducted

Species	Retrieval	Detection Significance
H ₂ O	Low-resolution	7.0σ
	High-resolution	2.0σ
	Hybrid	7.3σ
CO	Low-resolution	2.6σ
	High-resolution	4.6σ
	Hybrid	5.3σ

abundances. Overall, the differences in the retrieved parameters are small and show good agreement with Brogi & Line (2019) and expected values from known orbital parameters.

With this, we are now ready to perform the hybrid retrieval of HD 209458b using both the low-resolution and the high-resolution observations simultaneously. We include three additional parameters for our hybrid retrieval, namely, the HCN and CO_2 volume mixing ratios, and the high-resolution model scale factor $\log(a)$ as included for the simulated retrievals in Brogi & Line (2019). We include H_2O , CO, and HCN as there has been evidence for their presence in hot-Jupiter atmospheres from previous analyses of high-resolution infrared spectra (e.g., Birkby et al. 2013; Schwarz et al. 2015; Brogi et al. 2017; Hawker et al. 2018; Cabot et al. 2019). The CO_2 has also been shown to have a degeneracy with CO in the $4.5~\mu m$ *Spitzer* band (Madhusudhan & Seager 2010; Line et al. 2016; Gandhi & Madhusudhan 2018), and thus we include it to

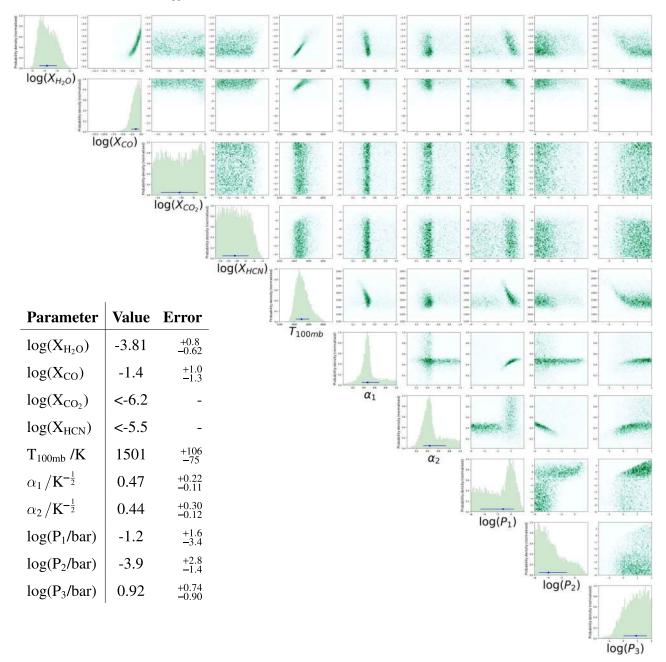


Figure 5. Posterior distribution of HD 209458b from the retrieval of the low-resolution *HST* WFC3 and *Spitzer* observations (Diamond-Lowe et al. 2014; Line et al. 2016). We retrieved four volatile chemical species, H₂O, CO, CO₂, and HCN, and parameterized the atmospheric temperature profile with six parameters, as discussed in Gandhi & Madhusudhan (2018).

compare any degeneracies which may arise. We include the scale factor log(a) as a way for the hybrid retrieval to weight the likelihoods independently from each set of observations following Brogi & Line (2019).

5. Results

In this section, we discuss the results from our simultaneous hybrid retrieval of the LRS and HRS of HD 209458b in thermal emission. The HRS data in the 2.29–2.35 μ m range are described in Section 4. The LRS data in the *HST* WFC3 band (1.1–1.7 μ m) are obtained from Line et al. (2016), and the *Spitzer* observations in the ~3–10 μ m range are obtained from Diamond-Lowe et al. (2014). The HyDRA-H retrieval framework developed to perform the simultaneous hybrid retrieval is

discussed in Section 2. We will compare and contrast the results from the hybrid retrieval with the HRS-only retrieval discussed in Section 4 as well an LRS-only retrieval.

Figure 6 shows the planet/star flux ratio for the best-fit high-resolution model as well as the spectral fit to the low-resolution observations from the hybrid retrieval. We see a good fit to the *HST* WFC3 and *Spitzer* observations, with a clear absorption feature in the WFC3 observations at $\sim 1.4 \, \mu \text{m}$ due to the presence of H₂O in the atmosphere. The *Spitzer* observations for the 4.5 μm band also show a feature due to CO. The high-resolution spectral model at $R \sim 400,000$ in the 2.29–2.35 μm range also shows clear absorption features due to the presence of both H₂O and CO, as both species have strong cross sections in this band (see Figure 2). The constraints on these species are

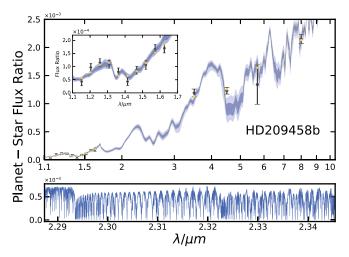


Figure 6. Thermal emission spectrum of of HD 209458b. The black data points in the top panel show the low-resolution *HST* and *Spitzer* observations of the planet-star flux ratio (Line et al. 2016) with their associated error bar. The inset shows the 1.1–1.7 μ m *HST* Wide Field Camera 3 region. The dark and light shaded regions show the 1σ and 2σ uncertainties, respectively, from the retrieval models and the gold markers indicate the binned data points from the median model. The bottom panel shows the best-fit spectrum from the hybrid retrieval in the observed 2.29–2.35 μ m spectral range of the high-resolution observations.

given in the histograms in Figure 7, and the full posterior distributions for all of the parameters are shown in Figure 8.

Our results for the abundances are in good agreement with previous low- and high-resolution retrievals on HD 209458b (Line et al. 2016; Brogi et al. 2017; Brogi & Line 2019). The posterior distribution for the low-resolution retrieval that we performed with HyDRA (Gandhi & Madhusudhan 2018) is shown in Figure 5. The H₂O and CO abundances have been well constrained (Figure 7) and are consistent with previous work (Line et al. 2016; Brogi & Line 2019). In addition, the deviations from the known planetary and systemic velocities, $dK_{\rm p}$ and $dV_{\rm sys}$, and the scale factor $\log(a)$ are also consistent with 0 within 2σ , as expected. This further validates that the high-resolution observations are able to constrain the planetary signal at the known location and strength without spurious detections. We will now further discuss each of these parameters below and compare and contrast the results with those obtained from the separate retrievals with the individual HRS versus LRS data sets.

5.1. H₂O Abundance

Figure 7 shows the H_2O abundance for the hybrid retrieval as well as the LRS-only and HRS-only retrievals. The hybrid retrieval is able to better constrain the abundances as it utilizes both the lower-resolution HST as well as the high-resolution CRIRES observations. Our detection significance of 7.3σ is also improved with the hybrid retrieval as shown in Table 2. The hybrid H_2O constraint is $\log(H_2O) = -4.11^{+0.91}_{-0.30}$, which lies within each of the HRS- and LRS-only constraints. This abundance is also consistent with that seen from previous retrievals (Line et al. 2016; Brogi et al. 2017; Brogi & Line 2019). While being consistent with solar to within 1σ , the H_2O abundance peaks at a sub-solar value of $\log(H_2O) \sim -4.2$.

The LRS-only retrieval is able to constrain H₂O due to the presence of an absorption feature in the *HST* WFC3 data. This

is caused by the strong broad molecular cross section of H_2O at $\sim 1.4~\mu m$ as shown in Figure 2. Hence, our detection significance of H_2O is 7.0σ (see Table 2). We constrain an H_2O abundance that is consistent with solar, but with a larger uncertainty than the hybrid retrieval. This result is consistent with previous low-resolution retrievals of the same data set (Line et al. 2016) as well as previous retrievals of the planet with transmission spectra which indicate sub-solar abundances (Madhusudhan et al. 2014b; Barstow et al. 2017; Pinhas et al. 2019).

The HRS data on the other hand are able to constrain and refine the $\rm H_2O$ estimate due to the numerous transition lines that $\rm H_2O$ possesses in the 2.29–2.35 μm spectral range. In this spectral range, there are $\sim 1.6 \times 10^6 \rm \, H_2O$ transition lines. The cross correlation is able to account for $\sim \! 10^3$ of these transition lines, which most strongly influence the spectrum (see Figure 6). However, given the weaker cross section of $\rm H_2O$ in this spectral range (see Figure 2), the abundance is not well constrained in this case compared with the other two retrievals. The detection significance of $\rm H_2O$ with the HRS-only retrieval is thus only 2.0σ . The uncertainty in the $\rm H_2O$ abundance is therefore also greatest when considering the HRS data alone. This is an important consideration that has also been discussed in previous work (Brogi & Line 2019).

5.2. CO Abundance

Figure 7 shows the CO abundance constraints for the hybrid retrieval. The CO abundance is most strongly constrained from the *Spitzer* and HRS observations as CO does not have a strong cross section in the *HST* WFC3 range. Our detection significance for CO for the hybrid retrieval is 5.3σ (see Table 2). The hybrid constraints suggest a super-solar CO abundance of $\log(\text{CO}) = -2.16^{+0.99}_{-0.47}$ compared to the solar value of $\log(\text{CO}) \sim -3.4$ (Moses et al. 2013). This, combined with the H₂O abundance, means that the C/O ratio for HD 209458b is obtained to be \sim 1, consistent with that seen from previous high-resolution observations (Brogi et al. 2017; Brogi & Line 2019).

Our low-resolution retrieval constrains the CO due to the 4.5 μ m *Spitzer* band where it has a strong cross section (see Figure 2). This data is only able to constrain a lower limit of $\log(\text{CO}) \gtrsim -5$. In addition, the detection significance is weaker at 2.6σ , as shown in Table 2. Whereas the H₂O had numerous *HST* WFC3 points to constrain its abundance, the CO is only constrained by the handful of *Spitzer* data points. Hence, the CO is detected at lower significance for the low-resolution retrieval and has a wider abundance uncertainty than the H₂O.

The HRS observations on the other hand are able to constrain the CO by resolving the CO spectral lines in the 2.29–2.35 μm range. CO possesses strong opacity with $\sim \! 2800$ transition lines in this range, of which $\sim \! 10^2$ are strong enough to be cross correlated (see Figure 6). Despite being less numerous than the H₂O lines, the stronger cross section of CO in this spectral range mean that the high-resolution retrieval is able to detect and constrain CO despite the fewer transitions. Our results show that combining the high- and low-resolution observations provides a substantial improvement in constraining the CO abundance compared to either data set alone.

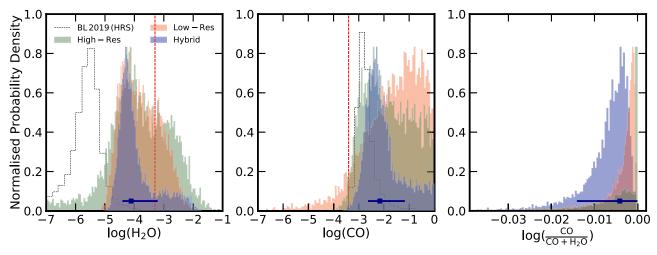


Figure 7. Probability distributions for the retrieved volume mixing ratios of H_2O and CO for the three retrievals run for HD 209458b. The left and center panels show the H_2O and CO abundances, respectively, and the right panel shows the retrieved $CO/(H_2O+CO)$ ratio. The dashed black lines show the posterior distributions for H_2O and CO from the retrieval of the high-resolution data in Brogi & Line (2019). The error bar in each panel indicates the median and 1σ uncertainty from the hybrid retrieval discussed in Section 5. The red dashed lines are the chemical equilibrium solar values at the planet equilibrium temperature and 0.1 bar pressure (Madhusudhan 2012).

5.3. Other Species

We retrieve CO_2 and HCN, but we observe no constraint on either species using the current data sets as shown in the summary table in Figure 8. The HCN does show an upper limit of $log(HCN) \lesssim -5.4$ at 2σ confidence, but without any definitive detection, it is difficult to further quantify this. HCN has previously been reported with HRS in the $3.18-3.27~\mu m$ CRIRES range (Hawker et al. 2018) where it has a strong cross section, but with only $2.29-2.35~\mu m$ observations in this work, we are unable to see any significant constraints due to its weaker opacity compared with CO and H_2O (see Figure 2).

5.4. C/O Ratio

The right panel of Figure 7 shows the $CO/(CO+H_2O)$ ratio. In the absence of any other species, this may be used as a proxy for the C/O ratio, which we constrain to be log(C/O) = $-0.0041^{+0.0041}_{-0.010}$. The corresponding C/O ratio is $0.991^{+0.009}_{-0.022}$, which is consistent with previous estimates using HRS spectra (Brogi et al. 2017; Brogi & Line 2019). This ratio is greater than the solar value of ~ 0.54 (Asplund et al. 2009) and is caused by the retrieved CO abundance being significantly higher than the H_2O , as shown in Figure 7. A $C/O \sim 1$ is also consistent with the recent inference of HCN using HRS data of HD 209458b in the 3.18–3.27 μ m band (Hawker et al. 2018), as well as with the low H2O abundance reported in transmission (e.g., Madhusudhan et al. 2014b). In chemical equilibrium, HCN is only present at significant abundance at C/O ratios near unity (Madhusudhan 2012). We should note however that the C/O ratio of the atmosphere may be influenced by other factors such as rain-out of oxygen bearing species and the presence of other C and O bearing gaseous chemical species.

5.5. Temperature Profile

The P-T profile and the uncertainty are shown for all three retrievals in Figure 9. The majority of the temperature profile constraint occurs from the absorption features in the LRS data

with some constraints from the absorption lines in the HRS data. These clearly indicate that the planet does not possess a thermal inversion (or stratosphere) within the photosphere, consistent with previous studies (Line et al. 2016; Brogi & Line 2019). This is also expected given that species such as TiO or VO would have condensed out given that the planet's dayside temperature is below ~ 1800 K (Spiegel et al. 2009). The retrieved 100 mb temperature is 1498^{+216}_{-57} K, consistent with the equilibrium temperature of ~ 1450 K assuming full redistribution.

From Figure 9, we see that the tightest constraint on the temperature occurs in the photosphere at $P \sim 1$ bar. At pressures greater than this, the optical depth $\tau \gg 1$ and thus does not significantly contribute to the overall spectrum. The onset of the isotherm at pressures $P \sim 1$ –10 bar is consistent with that seen from self-consistent equilibrium models of hot-Jupiter atmospheres (Burrows et al. 2008; Fortney et al. 2008; Gandhi & Madhusudhan 2017). The high-resolution spectra probe the line centers that originate higher up in the atmosphere at lower pressures. However, given that the high-resolution observations are less sensitive to the temperature and more so to the gradient, the temperature constraint does not improve significantly over the low-resolution retrieval. Going to even lower pressures, the temperature is now less well constrained, as the optical depth is too small to contribute significantly to the emergent spectrum even in the line cores. Therefore, the uncertainty for the top of the atmosphere is much greater.

5.6. High-resolution Parameters

In addition to the chemical abundances and temperature profile, we also retrieve the deviation from the known value of the planetary and systemic velocity and the scale factor. Both $dK_{\rm p}$ and $dV_{\rm sys}$ are consistent with 0 to within 1.5σ as shown in the table in Figure 8. The scale factor is also retrieved to be $\log(a)=0.32^{+0.12}_{-0.16}$. These three additional parameters confirm that the high-resolution retrieval is able to retrieve the planetary signal without biasing the results or detecting spurious peaks in the $K_{\rm p}-V_{\rm sys}$ plane.

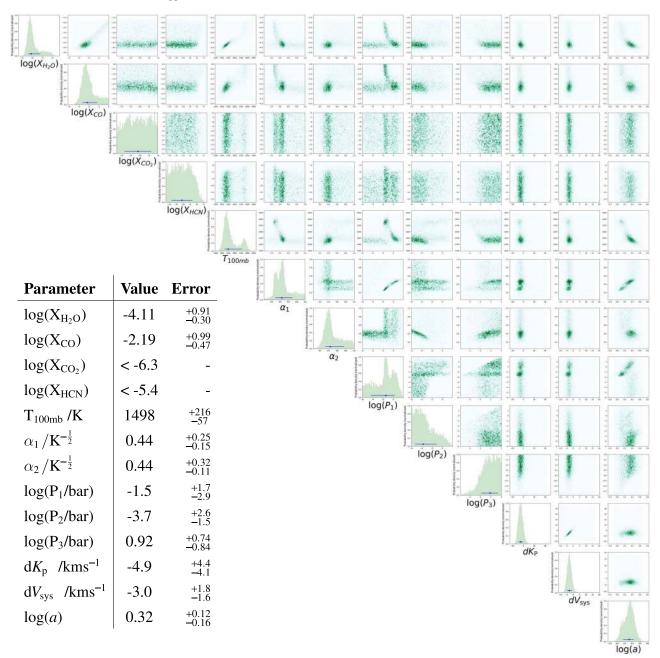


Figure 8. Posterior distribution of the hybrid retrieval of HD 209458b's dayside. The low-resolution data set was obtained from Line et al. (2016) and Diamond-Lowe et al. (2014) and considers *HST* WFC3 and four *Spitzer* photometric channels between 3.6 and 10 μ m and the high-resolution data was obtained from the CRIRES spectral survey (Snellen et al. 2011). We retrieved four volatile chemical species, H₂O, CO, CO₂, and HCN, and parameterized the atmospheric temperature profile with six parameters, as discussed in Gandhi & Madhusudhan (2018). We also include three additional parameters for the high-resolution observations, dK_p , dV_{sys} , and $\log(a)$ as discussed in Section 3.2.

6. Summary and Discussion

In this work, we develop a new hybrid atmospheric retrieval code and perform the first simultaneous hybrid retrieval of low- and high-resolution data for the exoplanet HD 209458b. Our code, HyDRA-H, builds upon the hybrid retrieval framework of Brogi & Line (2019) and is capable of retrieving atmospheric properties of exoplanets using low- and high-resolution emission spectra simultaneously. The architecture extends our recently developed HyDRA retrieval framework (Gandhi & Madhusudhan 2018) by incorporating methods for retrieval of high-resolution spectra from Brogi & Line (2019). We also perform separate retrievals on the low- and

high-resolution data. These separate retrievals demonstrate the contribution of each approach to the constraints obtained in the simultaneous hybrid retrieval.

We have validated our HyDRA-H retrieval framework by comparing to previous high-resolution retrievals by Brogi & Line (2019). We retrieve the 2.29–2.35 μ m VLT CRIRES observations of HD 209458b (Snellen et al. 2011) and constrain the H₂O and CO volume mixing ratios and parameterized temperature profile. We additionally constrain the deviations from the known value of the planetary and systemic velocities, $dK_{\rm p}$ and $dV_{\rm sys}$. This is to confirm that the planetary signal is located in the expected position in the $K_{\rm p}-V_{\rm sys}$ plane and is not significantly affected by spurious

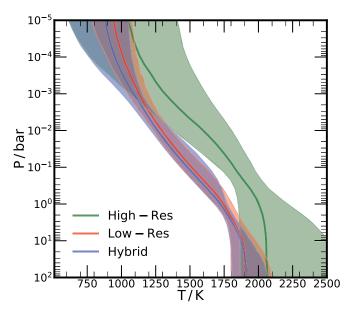


Figure 9. Retrieved atmospheric temperature profile from the three retrievals run for HD 209458b. The thick line and the shaded regions indicate the median P-T profile and 1σ uncertainty, respectively, for each retrieval.

signals such as those from the host star or telluric contamination. We find that the $\rm H_2O$ and CO abundances given in Figure 7 are in agreement with previous high-resolution retrievals (Brogi et al. 2017; Brogi & Line 2019). The temperature profile is also consistent with previous work and the photosphere temperature is consistent with the equilibrium temperature of HD 209458b.

The retrieval on the low-resolution data is able to constrain the molecular abundances and temperature profiles from the spectral features seen in the *HST* WFC3 and *Spitzer* observations. We constrain H_2O from its strong absorption feature in the WFC3 band and find it to be consistent with previous low-resolution retrievals of this data set (Line et al. 2016). Our CO abundance is constrained primarily by the 4.5 μ m *Spitzer* point. Both of these chemical species are consistent with the high-resolution retrieval. The *P-T* profile for the low-resolution retrieval does however show some differences. The retrieval indicates a photosphere temperature that is $\sim 1.5\sigma$ away from the high-resolution observations. However, this is not unexpected given that the high-resolution observations remove the continuum, and thus, an absolute temperature is more difficult to constrain.

Our hybrid retrieval is able to use the strengths of both highand low-resolution observations to constrain the abundances and the temperature profile. Hence, we see a higher detection significance for each species, as shown in Table 2, than for the retrievals on the individual data sets separately. We therefore also see much tighter constraints on the H_2O and CO mixing ratios in Figure 7. The hybrid retrieval is able to use the information from both available observations and combine their likelihoods to obtain more stringent constraints. We retrieve the H_2O abundance to be $log(H_2O) = -4.11^{+0.91}_{-0.30}$ and the CO to be $log(CO) = -2.16^{+0.99}_{-0.47}$. The H_2O is sub-solar but consistent to within 1σ of solar composition whereas the CO is super-solar to $\sim 2\sigma$. We additionally retrieve CO_2 and HCN, but we see no constraints on either species given their weak opacity in the observed wavelength range.

The retrieved temperature profile for the hybrid retrieval is similar to the low-resolution retrieval but $\sim 1.5\sigma$ away from the high-resolution constraint. This is because the HST and Spitzer data are the most sensitive to changes in temperature, particularly variations in the deep atmosphere where the continuum of the emergent spectrum is set. Therefore, the photosphere near $P \sim 0.1$ bar is in very close alignment with the low-resolution observations. The high-resolution observations, on the other hand, are able to probe the line cores and are thus more sensitive to the region at the top of the atmosphere. Hence, the temperature begins to deviate the most away from the low-resolution retrieval in the upper atmosphere. The $dK_{\rm p}$ and dV_{sys} are also tightly constrained near the expected value of 0, indicating that the high-resolution observations are able to detect the planetary signal. We have additionally retrieved the scale factor log(a) as is done in the simulated data set by Brogi & Line (2019). This parameter was included as a way for the hybrid retrieval to weight the likelihoods from the low- and high-resolution data, and we find that this is within 2σ of the expected value of 0.

Our work demonstrates the potential of hybrid retrievals of exoplanetary atmospheres. Using high-resolution data improves the spectral coverage, allowing for the identification of trace species and the constraining of relative abundances. The low-resolution data is key to constraining the *P-T* profile and absolute abundances, as it is able to provide information on the spectral continuum. As such, there is remarkable synergy between the two approaches as reflected in the insights obtained from the results of the joint approach presented here. We have shown the simultaneous hybrid retrieval method has great potential for obtaining improved constraints on chemical abundances such as H₂O and CO. In particular, the hybrid approach has the potential to break degeneracies seen in lowresolution retrievals, such as between CO and CO₂ present in the 4.5 µm Spitzer data (Kreidberg et al. 2014; Gandhi & Madhusudhan 2018). Such improvements will help in determining planetary C/O ratios with potential implications for the understanding of planet formation and/or migration histories (Öberg et al. 2011; Madhusudhan et al. 2014a; Piso et al. 2016). In the current work, we nominally constrain the C/O ratio to $0.991^{+0.009}_{-0.022}$ by determining the CO to $CO+H_2O$ ratio, consistent with that seen in previous work (Brogi et al. 2017; Brogi & Line 2019).

Going forward, the potential for simultaneous hybrid retrievals are numerous. First, the current TESS mission will provide many exoplanet candidates orbiting bright enough stars for characterization with this method. Second, a wealth of highresolution observations is expected with the commissioning of CRIRES+ at the VLT (Follert et al. 2014) as well as other highthroughput instruments such as CARMENES (Quirrenbach et al. 2014). The use of smaller telescopes with high-throughput spectrographs such as GIANO has been shown to prove fruitful in HRS exoplanet spectroscopy (Brogi et al. 2018; Guilluy et al. 2019). Hybrid retrieval methods exploiting synergies between high- and low-resolution data will be vital in fully exploiting the high-resolution spectra obtained with these facilities. The telescopes planned for the next decade will also require such a framework to fully exploit the observations they make. The prospect of JWST with increased sensitivity, spectral coverage, and resolution will greatly improve the low-resolution constraints that are possible. From the ground, the planned ELTs with vast collecting areas and equipped with high-resolution

spectrographs can enhance the insights from *JWST* data through such hybrid retrieval methods. In the longer term, developing these methods to push the limits of exoplanet characterization through such a holistic approach could enable the next generation of facilities to probe smaller potentially habitable worlds.

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