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Identification of a Class of Nonlinear State-Space Models using RPE Techniques

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Summary

The recursive prediction error methods in state-space form have been efficiently used as parameter identifiers for linear systems, and especially Ljung's innovations filter using a Newton search direction has proved to be quite ideal. In this paper, the RPE method in state-space form is developed to the nonlinear case and extended to include the exact form of a nonlinearity, thus enabling structure preservation for certain classes of nonlinear systems. Both the discrete and the continuous-discrete versions of the algorithm in an innovations model are investigated, and a nonlinear simulation example shows a quite convincing performance of the filter as combined parameter and state estimator.

1. Introduction

In this paper we present two parameter identifiers for nonlinear discrete and continuous-discrete state-space models. These algorithms are investigated by using the linear recursive prediction error (RPE) method, Ljung and Söderström [1983], in combination with nonlinear secondorder filtering theory Jazwinski [1970], Mayback [1982], Zhou [1985].

2. Model and algorithm in discrete version

We assume a nonlinear discrete state-space model of the following form,

 $\int \mathbf{x}(t+1) = \mathbf{f}(\boldsymbol{\theta}, \mathbf{u}; t, \mathbf{x}(t)) + \mathbf{v}(t)$ (1-a)

$$\int \mathbf{y}(t) = \mathbf{h}\left(\mathbf{\theta}(t, \mathbf{x}(t)) + \mathbf{e}(t)\right)$$
(1-b)

where f() and h() are nonlinear functions of the state, v(t) is white process noise, and e(t) is uncorrelated measurement noise with statistics

$$\begin{split} \mathbf{E} \mathbf{v}(t) &= \mathbf{E} \mathbf{e}(t) = 0\\ \mathbf{E} \mathbf{v}(t) \mathbf{v}^{T}(t) &= \mathbf{R}_{1}(\theta) \, \delta_{tt}\\ \mathbf{E} \mathbf{e}(t) \, \mathbf{e}^{T}(t) &= \mathbf{R}_{2}(\theta) \, \delta_{tt} \end{split} \tag{1-c} \\ \mathbf{E} \mathbf{v}(t) \, \mathbf{e}^{T}(t) &= \mathbf{R}_{12}(\theta) \, \delta_{tt} \end{split}$$

The initial value of the state x(o) has the properties

$$\begin{cases} \mathbf{E} \mathbf{x}(0) = \mathbf{x}_{o}(\theta) \\ \mathbf{E} [\mathbf{x}(0) - \mathbf{x}_{o}(\theta)] [\mathbf{x}(0) - \mathbf{x}_{o}(\theta)]^{\mathrm{T}} = \Pi_{o}(\theta) \end{cases}$$
(1-d)

From the nonlinear filtering theory [Jazwinski, 1970][Mayback, 1982] it is known that an attractive and appliable nonlinear filter is the first-order filter with bias correction term (FOFBC), which is based on using first-order covariance and gain computations, but with the second-order terms in state expectation and prediction error equations. In this study we use the FOFBC method for identification of the nonlinear model (1-a, b). When a fixed value θ is given, the predictor corresponding to (1-a, b) will be

$$\int \hat{\mathbf{x}}(t+1,\theta) = f(\theta,u;t,\hat{\mathbf{x}}(t,\theta)) + B_{\mathbf{x}}(t) + K(t)[y(t) - h(\theta;t,\hat{\mathbf{x}}(t,\theta)) - B_{\mathbf{y}}(t)] \quad (2-a)$$

$$\hat{\mathbf{y}}(\mathbf{t}|\boldsymbol{\theta}) = \mathbf{h}\left(\boldsymbol{\theta}; \mathbf{t}, \hat{\mathbf{x}}(\mathbf{t}, \boldsymbol{\theta})\right) \tag{2-b}$$

where the second order term $B_{\boldsymbol{x}}(t)$ is the $\boldsymbol{n}_{\boldsymbol{x}}\text{-vector}$ with K^{th} component

$$B_{xk}(t) = \frac{1}{2} tr \left\{ \frac{\partial^2 f_k(\theta, u; t, \hat{x}(t, \theta))}{\partial x^2} P(t) \right\}$$
(2-c)

and By(t) is the ny-vector with Kth component

$$B_{yk}(t) = \frac{1}{2} tr \left\{ \frac{\partial^2 h_k(\theta; t, \hat{x}(t, \theta))}{\partial x^2} P(t) \right\}$$
(2-d)

One finds that use of the recursive prediction error method by Ljung and Söderström, [1983], directly on the nonlinear predictor model (2-a, b) is hardly feasible, due to computational complexity. If a linear measurement equation is chosen instead, however, complexity of the algorithm is reduced significantly. Then the predictor has the following form

$$\int \hat{\mathbf{x}}(t+1,\theta) = \mathbf{f}(\theta,\mathbf{u};t,\hat{\mathbf{x}}(t,\theta)) + \mathbf{B}_{\mathbf{x}}(t) + \mathbf{K}(t)[\mathbf{y}(t) - \mathbf{H}(\theta)\hat{\mathbf{x}}(t,\theta)]$$
(3-a)

$$\bigcup_{\mathbf{\hat{y}}(t|\mathbf{\theta})=\mathbf{H}(\mathbf{\theta})\mathbf{\hat{x}}(t,\mathbf{\theta})}$$
(3-b)

The assumption of a linear measurement is valid in a wide class of practical applications. Then the recursive prediction error method using a Newton search direction for parameter updating can be applied to the model (3-a, b). The algorithm will consist of the following set of recursive equations:

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$$\begin{aligned} \varepsilon(t) &= y(t) - \widehat{y}(t) & (4-a) \\ R(t) &= R(t-1) + \alpha(t) [\psi(t) S^{-1}(t) \psi^{T}(t) - R(t-1)] & (4-b) \end{aligned}$$

$$\hat{\theta}(t) = \hat{\theta}(t-1) + \alpha(t) R^{-1}(t) \psi(t) S^{-1}(t) \varepsilon(t)$$
 (4-c)

 $K(t) = [F_{t} P(t) H_{t}^{T} + R_{12}(t)] S^{-1}(t)$ (4-d)

 $P(t+1) = F_{t} P(t) F_{t}^{T} + R_{t}(t) - K(t) S(t) K^{T}(t)$ (4-e)

$$\mathbf{S}(t) = \mathbf{H}_{t} \mathbf{P}(t) \mathbf{H}_{t}^{\mathrm{T}} + \mathbf{R}_{0}(t)$$
(4-f)

$$\hat{\mathbf{x}}(t+1) = f(\theta, \mathbf{u}; t, \hat{\mathbf{x}}(t, \theta)) + \mathbf{B}_{\mathbf{x}}(t) + \mathbf{K}(t) \varepsilon(t)$$
(4-g)

$$\hat{y}(t+1) = H_t \hat{x}(t+1)$$
 (4-h)

$$W(t+1) = \overline{W}_{x}(t,\theta) + \overline{M}_{\theta}(t) + \overline{K}_{t}\varepsilon(t) - K(t) D_{t}$$
(4-i)

(4-i)

(4-j)

$$\Psi^{T}(t+1) = H_{t}W(t+1) + D_{t}$$

where

$$\mathbf{F}_{i} = \frac{\partial \mathbf{f}(\boldsymbol{\theta}, \mathbf{u}; \mathbf{t}, \hat{\mathbf{x}}(\mathbf{t}, \boldsymbol{\theta}))}{\left(\mathbf{5} - \mathbf{a}\right)}$$
(5-a)

$$\begin{array}{c|c} t & \partial x & |_{\theta = \widehat{\theta}(t)} \\ H_{t} = H(\widehat{\theta}(t)) \end{array}$$
 (5-b)

$$\overline{W}_{\mathbf{x}}(t,\theta) = \frac{\partial}{\partial \theta} \left\{ f(\theta, u; t, \hat{\mathbf{x}}(t,\theta)) + B_{\mathbf{x}}(t, \hat{\mathbf{x}}(t,\theta)) - K(t) H(\theta) \hat{\mathbf{x}}(t,\theta) \right\} \Big|_{\theta = \hat{\theta}(t)}$$
(5-c)

is the derivative of $x(t,\theta)$ in the right-hand side of (3-a) with respect to $\theta.$ Further

$$\widetilde{\mathbf{M}}_{\theta}(t) = \frac{\partial}{\partial \theta} \left\{ f(\theta, u; t, \hat{\mathbf{x}}) + \mathbf{B}_{\mathbf{x}}(\theta; t) \right\} \Big|_{\theta = \hat{\theta}(t)}$$
(5-d)

is the derivative of the parameter matrices in the bracket with respect to $\boldsymbol{\theta},$ and

$$\overline{K}_{t} = \frac{\partial}{\partial \theta} K(t) \Big|_{\theta = \widehat{\theta}(t)}$$
(5-e)

$$D_{t} = \frac{\partial}{\partial \theta} (H(\theta) \hat{x}) \Big|_{\theta = \hat{\theta}(t)}$$
(5-f)

$$B_{t}(t)$$
 is defined in $(2 - c)$ (5-g)

This version of the filter $(4-a \sim j)$ includes a calculation of the Kalman gains in (4-d,e,f) and K_t is calculated from (4-d,e,f). As per the suggestion given by Ljung (1979), the parameter identifier can assume an innovations model of the form:

$$f(\hat{\mathbf{x}}(t+1,\theta) = f(\theta, u; t, \hat{\mathbf{x}}(t,\theta)) + B_{u}(t) + K(\theta) \varepsilon(t)$$
(6-a)

$$\mathbf{y}(t) = \mathbf{H}(\theta)\mathbf{\hat{x}}(t,\theta) + \varepsilon(t) \tag{6-b}$$

where $\varepsilon(t)$ is the innovation due to measurement t, and $K(\theta)$ is a set of (as yet undetermined) steady state Kalman gains, which is parameterized and will be identified directly along with the system parameters. This gives less complex compatations, and the algorithm corresponding to (6-a,b) will then be as follows:

$$\varepsilon(t) = y(t) - \hat{y}(t) \tag{7-a}$$

$$\Lambda(t) = \Lambda(t-1) + \alpha(t)[e(t)e^{t}(t) - \Lambda(t-1)]$$
(7-b)

$$R(t) = R(t-1) + \alpha(t) \left[\psi(t) \hat{\Lambda}^{-1}(t) \psi^{1}(t) - R(t-1) \right]$$
(7-c)

 $\hat{\theta}(t) = \hat{\theta}(t-1) + \alpha(t) R^{-1}(t) \psi(t) \hat{\wedge}^{-1}(t) \varepsilon(t)$ (7-d)

$$\hat{\mathbf{x}}(t+1) = \mathbf{f}(\boldsymbol{\theta}, \mathbf{u}; t, \hat{\mathbf{x}}(t, \boldsymbol{\theta})) + \mathbf{B}_{\mathbf{x}}(t) + \mathbf{K}_{t} \mathbf{z}(t)$$
(7-e)

$$\hat{y}(t+1) = H_t \hat{x}(t+1)$$
 (7-f)

$$W(t+1) = \overline{W}_{x}(t,\theta) + \overline{M}_{\theta}(t) - K_{t}D_{t}$$
(7-g)

$$\Psi^{T}(t+1) = H_{A}W(t+1) + D_{A}$$
 (7-h)

where

$$K_{t} = K(\hat{\theta}(t))$$
$$H_{t} = H(\hat{\theta}(t))$$

 $\overline{W}_x(t,\theta)$, $\overline{M}_{\theta}(t)$, D_t are defined in (5-c,d,f) respectively, and $B_x(t)$ is defined in (2-c). It is noted that in version (7-a~h) one has to use equations (4-e) and (4-f) in order to obtain the covariance matrix P(t) in $B_x(t)$. If the measurement vector y(t) has the same dimension as the state x, and the matrix H is an identity matrix then the covariance matrix is

$$P(t) = E \{ (x(t) - \hat{x}(t)) (x(t) - \hat{x}(t))^{T} \}$$

 $= E \{ \epsilon(t) \epsilon^{T}(t) \}$

Since $y(t) = H_1(\hat{x}(t) = \hat{x}(t))$. Consequently, the matrix P(t) can be replaced by $\hat{A}(t)$ in this case, and P(t) need no longer be calculated.

3. Model and algorithm in continuous-discrete version

In most applications involving the identification of parameters of a physical continuous time system, it is generally preferable to use a continuous-discrete algorithm. The reasons are primarily structure preservation of known parts of the system and the possibility to include bounds on parameter estimates of physical parameters whose constraints are known. The latter is a practical way to overcome part of the difficulties with possible local minima when identifying parameters of nonlinear systems. As in the presentation in section 2, the discrete measurement equation will be chosen in its linear version, and an innovations model is employed. We hence assume the nonlinear continuousdiscrete state-space model of the form:

$$\begin{cases} \frac{d}{dt} x(t|t_i) = f(\theta, u; t, x(t|t_i)) + v(t|t_i) \end{cases}$$
(8-a)

$$\int_{0}^{1} y(t_{i+1}) = H(\theta) x(t_{i+1}) + e(t_{i+1})$$
(8-b)

where f() is the nonlinear function of state. $v(t|t_i)$ is white process noise, $e(t_i)$ is uncorrelated measurement noise with statistics,

$$E v(t) = E e(t_i) = 0$$
$$E v(t) v^{T}(\tau) = R_1(\theta) \delta(t - \tau)$$
$$E e(t_i) e^{T}(t_j) = R_2(\theta) \delta_{ij}$$

The second order predictor using an innovations model will be

$$\frac{d}{dt} \hat{\mathbf{x}}(t|t_i, \theta) = \mathbf{f}(\theta, u; t, \hat{\mathbf{x}}(t|t_i, \theta)) + \mathbf{B}_{\mathbf{x}}(t|t_i)$$
(9-a)

$$\varepsilon(t_{i+1}) = y(t_{i+1}) - H(\theta) \hat{x}(t_{i+1}, \theta)$$
(9-b)

$$\hat{\mathbf{x}}(\mathbf{t}_{i+1}^{+}, \boldsymbol{\theta}) = \hat{\mathbf{x}}(\mathbf{t}_{i+1}^{-}, \boldsymbol{\theta}) + \mathbf{K}(\mathbf{t}_{i+1}^{-}, \boldsymbol{\theta}) \, \boldsymbol{\varepsilon}(\mathbf{t}_{i+1}^{-}) \tag{9-c}$$

where $\epsilon(t_{i+1})$ is the innovation due to measurement t_{i+1} , and $K(t_{i+1},\theta)$ comprise parameterized steady state Kalman gains. The algorithm corresponding to (9-a,b,c) will be as follows:

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$$\frac{d}{dt} \hat{\mathbf{x}}(t|t_i) = \mathbf{f}(0, u; t, \hat{\mathbf{x}}(t|t_i, \theta)) + \mathbf{B}_{\mathbf{x}}(t|t_i)$$

$$d \qquad - \qquad (10-b)$$

$$\frac{d}{dt} P(t|t_i) = F_i P(t|t_i) + P(t|t_i) F_i^T + R_1(t_i)$$

$$d - * - (10-c)$$

$$\frac{d}{dt} W(t|t_i) = W_X(t|t_i) + M_{\theta}(t_i)$$

After integration of (10-a,b,c), $\boldsymbol{\hat{x}}(t_{i+1}\text{-}),~P(t_{i+1}\text{-}),~W(t_{i+1}\text{-})$ are available, and

$$W(t_{i+1}^{+}) = [I - K(t_{i}, \theta) H_{i}] W(t_{i+1}^{-}) + N(t_{i+1}, \theta) - K(t_{i}, \theta) D(\theta, \hat{x}(t_{i+1}^{-}))$$
(10-d)

 $\psi^{T}(t_{i+1}) = H_{i} W(t_{i+1}^{+}) + D(\theta, \hat{x}(t_{i+1}^{-}))$ (10-e)

$$\hat{\mathbf{y}}(\mathbf{t}_{i+1}^{-}) = \mathbf{H}_{i} \hat{\mathbf{x}}(\mathbf{t}_{i+1}^{-})$$
 (10-1)

$$\epsilon(t_{i+1}) = y(t_{i+1}) - \hat{y}(t_{i+1})$$
(10-g)

$$\hat{\wedge}(t_{i+1}) = \hat{\wedge}(t_i) + \alpha(t_{i+1}) \left[\epsilon(t_{i+1}) \epsilon^{\mathrm{T}}(t_{i+1}) - \hat{\wedge}(t_i) \right]$$
(10-h)

$$R(t_{i+1}) = R(t_i) + \alpha(t_{i+1}) [\Psi(t_{i+1}) \hat{\Lambda}^{-1}(t_{i+1}) \Psi^{T}(t_{i+1}) - R(t_i)]$$
(10-i)

$$\hat{\theta}_{t_{i+1}}) = \hat{\theta}(t_{i}) + \alpha(t_{i+1}) R^{-1}(t_{i+1}) \psi(t_{i+1}) \hat{\wedge}^{-1}(t_{i+1}) \epsilon(t_{i+1})$$
(10-j)

$$\hat{\mathbf{x}}(t_{i+1}^{+}) = \hat{\mathbf{x}}(t_{i+1}^{-}) + K(t_{i+1}^{-}, \theta) \, \varepsilon(t_{i+1}^{-})$$
(10-k)

$$P(t_{i+1}^{+}) = P(t_{i+1}^{-}) - K(t_{i+1}^{-}, \theta) H_i P(t_{i+1}^{-})$$
(10)

where $B_x(t|t_i)$ is the n_x-vector with kth component

$$\begin{split} B_{xk}(t|t_i) &= \frac{1}{2} \ tr \left\{ \frac{\partial^2 f_k(\theta, u; t, \hat{x}(t|t_i, \theta))}{\partial x^2} \ P(t) \right\} \\ \text{and} \end{split}$$

$$\overline{W}_{x}^{*}(t|t_{i},\theta) = \frac{\partial}{\partial \theta} \left\{ f(\theta;t, \hat{x}(t|t_{i},\theta)) + B_{x}(t|t_{i}) \right\} \Big|_{\theta = \hat{\theta}(t)}$$

is the derivative of $x(t|t_i,\theta)$ in the right-hand side of (9-a) with respect to θ .

$$\overline{\mathbf{M}}_{\theta}(\mathbf{t}_{i}) = \frac{\partial}{\partial \theta} \left\{ f(\theta, u; \mathbf{t}, \widehat{\mathbf{x}}) + \mathbf{B}_{\mathbf{x}}(\theta; t|\mathbf{t}_{i}) \right\} \Big|_{\theta = \widehat{\theta}(\mathbf{t}_{i})}$$

is the derivative of the parameter matrices in the right-hand side of (9-a) with respect to $\theta.$ Further the following notation is used

$$\begin{split} \mathbf{D}(\theta, \hat{\mathbf{x}}(\mathbf{t}_{i+1}^{-})) &= \frac{\partial}{\partial \theta} \left\{ \mathbf{H}(\theta) \hat{\mathbf{x}} \right\} \Big|_{\theta = \hat{\theta}(\mathbf{t}_{i})} \\ \mathbf{N}(\mathbf{t}_{i+1}, \theta) &= \left[\left| \frac{\partial}{\partial \theta} \mathbf{K}(\mathbf{t}_{i+1}, \theta) \right] \right|_{\theta = \hat{\theta}(\mathbf{t}_{i})} \epsilon(\mathbf{t}_{i+1}) \\ \mathbf{H}_{i} &= \mathbf{H}(\hat{\theta}(\mathbf{t}_{i})) \\ \mathbf{D}_{i} &= \frac{\partial}{\partial t} \mathbf{f}(\theta, \mathbf{u}; \mathbf{t}, \hat{\mathbf{x}}(\mathbf{t} | \mathbf{t}_{i}, \theta)) \Big|_{\theta} \end{split}$$

 $\theta = \hat{\theta}(t_i)$

The same treatment will be used when H_i is an identity matrix and has the same dimension as the state vector x. In this case the $P(t_i)$ matrix will not be calculated any longer and is replaced by $\hat{\Lambda}(t_i)$.

4. Example

The ability of the nonlinear RPE method to estimate parameters and states of a nonlinear system of practical importance is demonstrated in this example.

The continuous discrete version of the nonlinear filter derived above is compared with the corresponding linear algorithm by Gavel and Azevedo [1982]. The results demonstrate the advantages in terms of bias correction of the nonlinear filter.

(10-d) The nonlinear system considered is an equivalent to the ship speed equation. The parameters identified will, for the real (10-e) ship, mean hull resistance and efficiency in utilizing the prime mover of the vessel for forward thrust. Both values are (10-f) of major technical importance and as they change over time, they have vast impact on the ships's fuel economy and efficiency. The criteria for maintenence of the ship's hull, propeller, and prime mover system can be directly derived (10-h) from these parameters, and it is hence of prime importance that they are estimated without bias.

$$\frac{d}{dt} x(t) = a x^{2}(t) + b u(t) + v(t)$$
(11)

The second order nonlinearity type of system is furthermore technically important when identifying propulsion losses of ships at sea aiming at autopilot and steering gear performance evaluation, Blanke [1981], Blanke and Sørensen [1984], Blanke [1986].

The responses and parameter estimates below were obtained using a square wave pertubation to the input u(t). The amplitude of the pertubation is 10 percent of its steady state value. The practical equivalent to this experiment would be a stepwise increase/decrease in propeller thrust.

The matrices B_x , \overline{W}_x^* , \overline{M}_{θ} , and N in the algorithm (10-a~l) corresponding to the example will be

$$B_{\mathbf{x}}(\mathbf{t}|\mathbf{t}_{i}) = \mathbf{a} p(\mathbf{t}_{i}) = \mathbf{a} \Lambda(\mathbf{t}_{i})$$

$$\overline{W}_{\mathbf{x}}^{*}(\mathbf{t}|\mathbf{t}_{i}) = 2\mathbf{a}\hat{\mathbf{x}}(\mathbf{t}_{i})\mathbf{w}(\mathbf{t}|\mathbf{t}_{i}) \qquad (12)$$

$$\overline{M}_{\theta}(\mathbf{t}_{i}) = [(\hat{\mathbf{x}}^{2}(\mathbf{t}_{i}) + P(\mathbf{t}_{i})), \mathbf{u}(\mathbf{t}_{i}), \mathbf{o}] = [(\hat{\mathbf{x}}^{2}(\mathbf{t}_{i}) + \hat{\Lambda}(\mathbf{t}_{i})), \mathbf{u}(\mathbf{t}_{i}), \mathbf{o}]$$

$$\mathbf{N}(\mathbf{t}_{i}) = [\mathbf{o}, \mathbf{o}, \mathbf{c}(\mathbf{t}_{i})]$$

Figure 1 shows results of identifying the parameters a and b in the nonlinear equation using the nonlinear filter. The curves plotted in figure 2 illustrate the performance of a linear RPE filter applied to the same nonlinear equation. Although the driving signal's pertubation is only 10 percent of its average, the bias of the linear estimator is apparent, and the superior performance of the nonlinear filter is obvious.

5. Conclusions

This paper has presented two algorithms for identifying parameters of a nonlinear discrete state-space system model and a nonlinear continuous-discrete state-space system model. Both versions are treated using a linear discrete measurement equation. These algorithms were investigated with reference to the theory of linear RPE methods and the theory of nonlinear filtering. The innovations model formulation was found to be attractive, and the algorithms were implemented and tested against computer simulations showing excellent convergence, and bias properties that by far exceed those of a linear continuous/discrete filter. The analysis of the convergence properties of the nonlinear estimator and further tests of applications of these algorithms should be persued in a further study.

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