

# Identification of Continuous-Time Systems

Methodology and Computer Implementation

*edited by*

N. K. SINHA

*McMaster University,  
Hamilton, Ontario, Canada*

and

G. P. RAO

*Indian Institute of Technology,  
Kharagpur, India*



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