

Research Article

Image Segmentation Method Using Thresholds Automatically Determined from Picture Contents

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Image segmentation has become an indispensable task in many image and video applications. This work develops an image segmentation method based on the modified edge-following scheme where different thresholds are automatically determined according to areas with varied contents in a picture, thus yielding suitable segmentation results in different areas. First, the iterative threshold selection technique is modified to calculate the initial-point threshold of the whole image or a particular block. Second, the quad-tree decomposition that starts from the whole image employs gray-level gradient characteristics of the currently-processed block to decide further decomposition or not. After the quad-tree decomposition, the initial-point threshold in each decomposed block is adopted to determine initial points. Additionally, the contour threshold is determined based on the histogram of gradients in each decomposed block. Particularly, contour thresholds could eliminate inappropriate contours to increase the accuracy of the search and minimize the required searching time. Finally, the edge-following method is modified and then conducted based on initial points and contour thresholds to find contours precisely and rapidly. By using the Berkeley segmentation data set with realistic images, the proposed method is demonstrated to take the least computational time for achieving fairly good segmentation performance in various image types.

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1. Introduction

Image segmentation is an important signal processing tool that is widely employed in many applications including object detection [1], object-based coding [2–4], object tracking [5], image retrieval [6], and clinical organ or tissue identification [7]. To accomplish segmentations in these applications, the methods can be generally classified as region-based and edge-based techniques. The region-based segmentation techniques such as semisupervised statistical region refinement [8], watershed [9], region growing [10], and Markov-random-field parameter estimation [11] focus on grouping pixels to become regions which have uniform properties like grayscale, texture, and so forth. The edge-based segmentation techniques such as Canny edge detector [12], active contour [13], and edge following [14–16] emphasize on detecting significant gray-level changes near object boundaries. Regarding to the above-mentioned

methods, the segmenting mechanisms associated with users can be further categorized as either supervised segmentation or unsupervised segmentation.

The advantage of the region-based segmentation is that the segmented results can have coherent regions, linking edges, no gaps from missing edge pixels, and so on. However, its drawback is that decisions about region memberships are often more difficult than those about edge detections. In the literature, the Semisupervised Statistical Region Refinement (SSRR) method developed by Nock and Nielsen is to segment an image with user-defined biases which indicate regions with distinctive subparts [8]. SSRR is fairly accurate because the supervised segmentation is not easily influenced by noise, but is highly time-consuming. The unsupervised DIScovering Objects in Video (DISCOV) technique developed by Liu and Chen could discover the major object of interest by an appearance model and a motion model [1]. The watershed method that is applicable

to nonspecific image type is also unsupervised [9, 17]. The implementation manners of the watershed method can be classified into rain falling and water immersion [18]. Some recent watershed methods use the prior information-based difference function instead of the more-frequently-used gradient function to improve the segmented results [19] and employ the marker images as probes to explore a gradient space of an unknown image and thus to determine the best-matched object [20]. The advantage of the watershed method is that it can segment multiple objects in a single threshold setting. The disadvantage of the watershed method is that the different types of images need different thresholds. If the thresholds are not set correctly, then the objects are under-segmented or over-segmented. Additionally, slight changes in the threshold can significantly alter the segmentation results. In [21, 22], the systematic approach was demonstrated to analyze nature images by using a Binary Partition Tree (BPT) for the purposes of archiving and segmentation. BPTs are generated based on a region merging process which is uniquely specified by a region model, a merging order, and a merging criterion. By studying the evolution of region statistics, this unsupervised method highlights nodes which represent the boundary between salient details and provide a set of tree levels from which segmentations can be derived.

The edge-based segmentation can simplify the analysis by drastically minimizing the amount of pixels from an image to be processed, while still preserving adequate object structures. The drawback of the edge-based segmentation is that the noise may result in an erroneous edge. In the literature, the Canny edge detector employed the hysteresis threshold that adapts to the amount of noise in an image, to eliminate streaking of edge contours where the detector is optimized by three criteria of detection, localization, and single response [12]. The standard deviation of the Gaussian function associated with the detector is adequately determined by users. The Live Wire On the Fly (LWOF) method proposed by Falcao et al. helps the user to obtain an optimized route between two initial points [23]. The user can follow the object contour and select many adequate initial points to accomplish that an enclosed contour is found. The benefit of LWOF is that it is adaptive to any type of images. Even with very complex backgrounds, LWOF can enlist human assistance in determining the contour. However, LWOF is limited in that if a picture has multiple objects, each object needs to be segmented individually and the supervised operation significantly increases the operating time. The other frequently adopted edge-based segmentation is the snake method first presented by Kass et al. [24]. In this method, after an initial contour is established, partial local energy minima are calculated to derive the correct contour. The flaw of the snake method is that it must choose an initial contour manually. The operating time rises with the number of objects segmented. Moreover, if the object is located within another object, then the initial contours are also difficult to select. On the other hand, Yu proposed a supervised multiscale segmentation method in which every pixel becomes a node, and the likelihood of two nodes belonging together is interpreted by a weight attached to the edge

linking these two pixel nodes [25]. Such approach allows that image segmentation becomes a weighted graph partitioning problem that is solved by average cuts of normalized affinity. The above-mentioned supervised segmentation methods are suitable for conducting detailed processing to objects of segmentation under user's assistance. In the unsupervised snake method also named as the active contour scheme, the geodesic active contours and level sets were proposed to detect and track multiple moving objects in video sequences [26, 27]. However, the active contour scheme is generally applied when segmenting stand-alone objects within an image. For instance, an object located within the complicated background may not be easily segmented. Additionally, contours that are close together cannot be precisely segmented. Relevant study, the Extended-Gradient Vector Flow (E-GVF) snake method proposed by Chuang and Lie has improved upon the conventional snake method [28]. The E-GVF snake method can automatically derive a set of seeds from the local gradient information surrounding each point, and thus can achieve unsupervised segmentation without manually specifying the initial contour. The noncontrast-based edge descriptor and mathematical morphology method were developed by Kim and Park and Gao et al., respectively, for unsupervised segmentation to assist object-based video coding [29, 30].

The conventional edge-following method is another edge-based segmentation approach that can be applied to nonspecific image type [14, 31]. The fundamental step of the edge-following method attempts to find the initial points of an object. With these initial points, the method then follows on contours of an object until it finds all points matching the criteria, or it hits the boundary of a picture. The advantage of the conventional edge-following method is its simplicity, since it only has to compute the gradients of the eight points surrounding a contour point to obtain the next contour point. The search time for the next contour point is significantly reduced because many points within an object are never used. However, the limitation of the conventional edge-following method is that it is easily influenced by noise, causing it to fall into the wrong edge. This wrong edge can form a wrong route to result in an invalid segmented area. Moreover, the fact that initial points are manually selected by users may affect accuracy of segmentation results due to inconsistency in different times for selection. To improve on these drawbacks, the initial-point threshold calculated from the histogram of gradients in an entire image is adopted to locate positions of initial points automatically [15]. Additionally, the contour thresholds are employed to eliminate inappropriate contours to increase the accuracy of the search and to minimize the required searching time. However, this method is limited in that the initial-point threshold and contour threshold remain unchanged throughout the whole image. Hence, optimized segmentations cannot always be attained in areas with complicated and smooth gradients. If the same initial-point threshold is employed throughout an image with areas having different characteristics, for example, a half of the image is smooth, and the other half has major changes in gradients, then the adequately segmented results can clearly

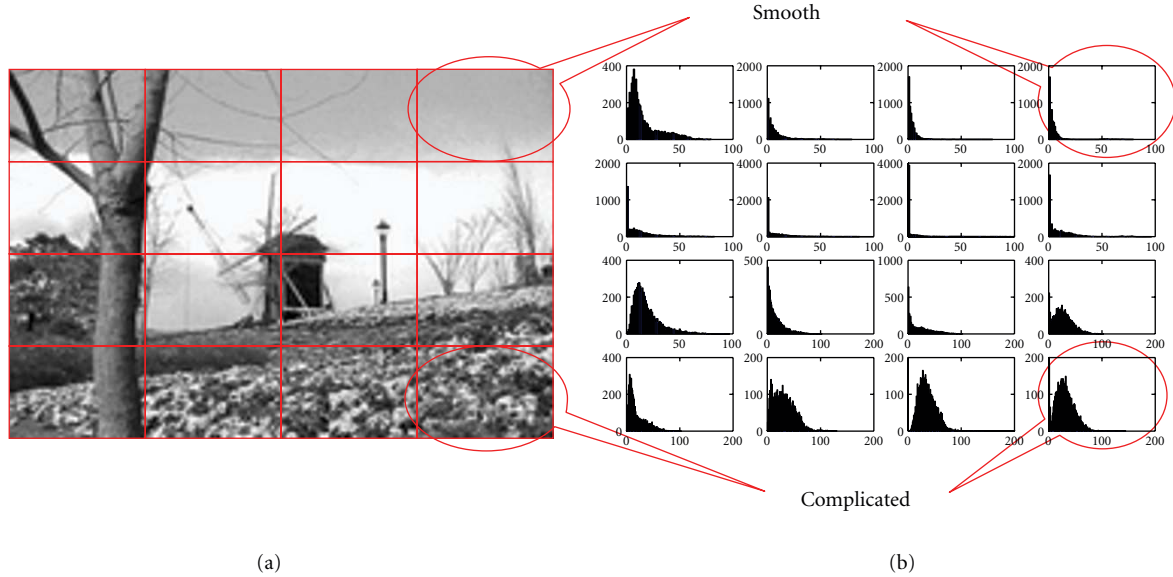


FIGURE 1: Content characteristics of the “garden” image. (a) Image partitioned into 16 blocks. (b) Histogram formed by average values of gradients for all points in each block.

only be obtained from one side of the image, while the objects from the other side are not accurately segmented.

This work proposes a robust segmentation method that is suitable for nonspecific image type. Based on the hierarchical segmentation under a quad-tree decomposition [32, 33], an image is adequately decomposed into many blocks and subblocks according to the image contents. The initial-point threshold in each block is determined by the modified iterative threshold selection technique and the initial-point threshold of its parent block. Additionally, the contour threshold is calculated based on the histogram of gradients in each block. Using these two thresholds, the modified edge-following scheme is developed to automatically and rapidly attain fairly good segmentation results. Segmentations on various types of images are performed during simulations to obtain the accuracy of segmentations using methods such as the proposed, watershed, active contour, and others. To do fair comparison, the data set and benchmarks from the Computer Vision Group, University of California at Berkeley were used [34]. Simulation results demonstrate that the proposed method is superior to the conventional methods to some extent. Owing to avoiding human interferences and reducing operating time, the proposed method is more robust and suitable to various image and video applications than the conventional segmentation methods.

2. Proposed Robust Image Segmentation Method

This work develops a robust image segmentation method based on the modified edge-following technique, where different thresholds are automatically generated according to the characteristics of local areas. Taking the “garden” image in Figure 1(a) as an example, Figure 1(b) divides this image

into 16 blocks and calculates the average value of gradients between the currently processed point and its neighboring points in eight compass directions to plot a histogram of the average values from all points in each block. Looking at these histograms, the complicated part circled in the diagram represents the area of extreme changes in gradients. With a larger variation of gradients, the threshold for this area must also be larger than that adopted in the smooth area to prevent over-segmentation. To adapt to variations of gradients in each area, the quad-tree decomposition is adopted to divide an image into four blocks at an equal size and would continue to divide further depending on complexities of the blocks. If the criteria for further decomposition are satisfied, then the block or subblock is divided into four subblocks or smaller subblocks; otherwise, it would stop here. The proposed decomposition would continue until all blocks and subblocks are completely obtained, as shown in Figure 2. During the quad-tree decomposition process, different threshold values can be determined for each decomposed block, according to variations in the gradients of each decomposed block, to attain accurate segmentation results. The major differences between the proposed robust image segmentation method and our previous work [15] are quad-tree decomposition, adaptive thresholds in each decomposed blocks, and direction judgment in the edge following. To clearly illustrate the proposed method, four stages are introduced. First, the iterative threshold selection technique is modified to calculate the initial-point threshold of the whole image or a particular block from the quad-tree decomposition. Second, the quad-tree decomposition is applied to establish decomposed blocks, where gray-level gradient characteristics in each block are computed for deciding further decomposition or not. After the quad-tree decomposition, the contour threshold of each decomposed block is calculated in the third stage. Initial-point thresholds

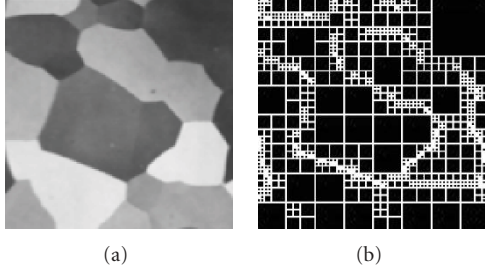


FIGURE 2: Blocks and subblocks resulted from the quad-tree decomposition process. (a) Original image. (b) Decomposed blocks.

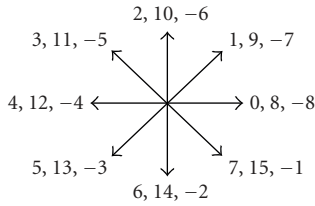


FIGURE 3: Values of d representing eight compass directions.

are used to determine the initial points while contour thresholds can eliminate inappropriate contours to increase the accuracy of search and minimize the required searching time. Finally, the modified edge-following method is used to discover complete contours of objects. Details of each stage are described below.

2.1. Stage of Applying the Modified Iterative Threshold Selection Technique. In this stage, the gradient between the currently processed point (x, y) and its neighboring point in one of eight compass directions is first determined by using the following equation:

$$G^d(x, y) = |I(x, y) - I(x^d, y^d)|, \quad (1)$$

where (x^d, y^d) neighbors to (x, y) in direction d , and $I(x, y)$ and $I(x^d, y^d)$ denote the gray-level values at locations (x, y) and (x^d, y^d) , respectively. Here, d is a value denoting one of the eight compass directions as shown in Figure 3. For $d > 7$, the remainder of d divided by 8 is taken. When $d < 0$, d is added by a multiple of 8 to become a positive value smaller than 8. Hence, “1”, “9”, and “-7” denote the same directions. This will be useful in Section 2.4.

$\bar{G}(x, y)$ is defined to take a mean of $G^d(x, y)$ in eight directions for the point (x, y) in the following equation:

$$\bar{G}(x, y) = \frac{1}{8} \sum_{d=0}^7 G^d(x, y). \quad (2)$$

The iterative threshold selection technique that was proposed by Ridler and Calvard to segment the foreground and background is modified to calculate the initial-point threshold of the whole image or a particular block from the quad-tree decomposition, for identifying initial points [35]. The modified iterative threshold selection technique is illustrated as follows.

- (1) Let $k = 0$, $T_k = (\text{MAX}[\bar{G}(x, y) \mid (x, y) \in \text{all points in a decomposed block}])/2$, where MAX is a function to select the maximum value.
- (2) T_k is adopted to classify all points in a decomposed block into initial and noninitial points. A point with $\bar{G}(x, y) \geq T_k$ is an initial point, while a point with $\bar{G}(x, y) < T_k$ is a noninitial point. The groups of initial and noninitial points are denoted by I and NI , respectively. In these two groups, the averaged $\bar{G}(x, y)$ is computed by

$$u_k = \frac{\sum_{(x,y) \in I} \bar{G}(x, y)}{\#I}, \quad (3)$$

$$v_k = \frac{\sum_{(x,y) \in NI} \bar{G}(x, y)}{\#NI},$$

where $\#I$ and $\#NI$ denote the numbers of initial and noninitial points, respectively,

(3)

$$T_{k+1} = \text{round}(w_I \times u_k + w_{NI} \times v_k), \quad (4)$$

where $\text{round}(\lambda)$ rounds off the value of λ to the nearest integer number. w_I and w_{NI} , ranging from 0 to 1, denote the weighting values of initial and noninitial groups, respectively. Additionally, $w_I + w_{NI} = 1$.

- (4) If $T_{k+1} \neq T_k$, then $k = k + 1$ and go to Step 2, else $Tg = T_k$.

Notably, T_k is limited to the range between 0 and 255, and rounded off into a specific integer in the iterative procedure so that the above-mentioned iteration always converges. Usually, w_I and w_{NI} are set to 0.5 to allow Tg locating in the middle of two groups. To avoid missing some initial points in low-contrast areas of an image with complicated contents, w_{NI} can be increased to lower Tg . However, with an increasing decomposition level in the quad-tree decomposition process, w_{NI} can be lowered for a small decomposed block that has a consistent contrast. Taking the “alumgrns” image in Figure 4 as an example, the initial-point threshold Tg of the entire image calculated by the modified iterative threshold selection is 16 under $w_I = w_{NI} = 0.5$. The rough contour formed by initial points can be found as depicted in Figure 4(b), but the contour is not intact. Hence, the quad-tree decomposition in the following stage would take this Tg as the basis to compute the initial-point threshold value of each decomposed block depending on the complexity of each area.

2.2. Stage of the Quad-Tree Decomposition Process. In this stage, the whole image is partitioned into many blocks by using quad-tree decomposition. The quad-tree decomposition process starts with the initial-point threshold, mean and standard deviations derived from the entire image on the top level. At each block, the process determines the initial-point threshold and whether this block should be further decomposed. For the whole image or each block, Figure 5

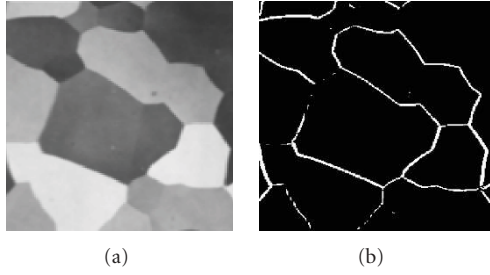


FIGURE 4: “alumgrns” image. (a) Original image. (b) White points with $\bar{G}(x, y) > Tg$.

shows the flow chart of the quad-tree decomposition to determine whether the currently processed block is further decomposed and to calculate the initial-point threshold of this block. Assume that the block B_t with a mean M_t and a standard deviation S_t of gray-level gradients is currently processed. The parent block of B_t is represented by B_{t-1} in which initial-point threshold, mean and standard deviations are denoted by Tg_{t-1} , M_{t-1} and S_{t-1} , respectively. While $\bar{G}(x, y)$ of each point in the block B_t is smaller than Tg_{t-1} , the block B_t does not contain any initial point and thus its initial-point threshold Tg_t is set to Tg_{t-1} in order to avoid the initial-point generation. Under such a situation, there is no further decomposition in the block B_t . On the other hand, when $\bar{G}(x, y)$ of any point of the block B_t is larger than Tg_{t-1} , the block B_t is further decomposed into four subblocks. Additionally, Tg_t is temporarily given by the value computed by the modified iterative threshold selection technique in the block B_t . If $M_t < M_{t-1}$ and $S_t < S_{t-1}$, then the block B_t would contain a smoother area than the block B_{t-1} . Let $Tg_t = Tg_{t-1}$ to prevent the reduction of the initial-point threshold from yielding the undesired initial points. If $M_t \geq M_{t-1}$ and $S_t \geq S_{t-1}$, the complexity of the block B_t is increased. In this situation, the block B_t may contain contour points, but may also include many undesired noises or complicated image contents. Hence, raising the initial-point threshold by $Tg_t = \text{MAX}(Tg_t, Tg_{t-1})$ to allow that $Tg_t \geq Tg_{t-1}$ can eliminate the noises and reduce the oversegmentation result in the block B_t . Otherwise, the initial point threshold Tg_t of the block B_t that may contain objects is remained as the value from the modified iterative threshold selection technique conducted in the block B_t .

During the quad-tree decomposition process, w_l can be set by a value smaller than 0.5 at the first decomposition level to lower Tg for capably attaining initial points from low-contrast areas. Additionally, w_l is increased with a decomposition level. For the smallest decomposed block in the last decomposition level, w_l can be a value larger than or equal to 0.5 for increasing Tg to avoid the undesired initial points. Notably, the initial-point thresholds of blocks with drastic gray-level changes would rise, whereas the initial-point thresholds of blocks with smooth gray-level changes would fall. This approach of determining initial-point threshold can obtain adequate initial points based on the complexity of image contents.

After the quad-tree decomposition is finished, the positions and moving directions of initial points in each block are recorded accordingly.

- (1) (x, y) is a point from a decomposed block B_t .
- (2) If $\bar{G}(x, y) \geq Tg_t$ then (x, y) is labeled as the initial point and d^* is recorded where $G^{d^*}(x, y) = \text{MAX}[G^d(x, y), \text{ for } 0 \leq d \leq 7]$.
- (3) Repeat step 2 for all points in the block B_t .

2.3. Stage of Determining the Contour Threshold Tc . At the end of the quad-tree decomposition process, the gradients of each decomposed block are computed to determine the contour threshold Tc . According to (1), the largest value of $G^d(x, y)$ in the eight directions is $G^{d^*}(x, y)$, where d^* is a specific value of d for yielding the maximum $G^d(x, y)$. The histogram of $G^{d^*}(x, y)$ from all points of the decomposed block is calculated. Here, $H(k)$ is assumed to be the number of the absolute gray-level difference being k . If a decomposed block comprises many one-pixel lines that are all black and white in an interlaced manner, then this decomposed block contains the maximum number of contour points, which is half the number of points in the decomposed block. Restated, the first half of the histogram results from noncontour points at least. Accordingly, the contour threshold Tc can be the index value, indicating that $\sum_{k=0}^{Tc} H(k)$ denotes half the number of points in a decomposed block, as indicated in Figure 6. This threshold does not miss any contour points. When the search is conducted for contour points, Tc is used to determine whether to stop the search procedure in the modified edge-following scheme. If the differences between the predicted contour point and its left and right neighboring points are less than Tc , then the search has taken the wrong path, and should stop immediately. This approach not only prevents searching in the wrong path, but also saves on the search time. Additionally, Tc of each decomposed block is independently determined to adapt to the characteristics of each area.

2.4. Stage of Applying the Modified Edge-Following Method. The initial-point threshold Tg , contour threshold Tc , and initial points are obtained in the previous stages. In this stage, the searching procedure is started from each initial point until the closed-loop contour is found. The position and direction of the k th searched contour point are represented by $\mathbf{w}_k = (x_k, y_k)$ and d_k , respectively. The modified edge-following method is given as follows.

- (1) Select an initial point and its d^* . This initial point is represented by \mathbf{w}_0 and set $d_0 = d^* + 2$ where the edge-following direction d_0 is perpendicular to the maximum-gradient direction d^* . Here, d_0 is a value denoting one of the eight compass directions as shown in Figure 3.
- (2) Let $k = 0$, where k is the contour-point index. The searching procedure begins from the initial point \mathbf{w}_0 and the direction d_0 .
- (3) First, to reduce computational time, the search is restricted to only three directions by setting $i = 3$, where i

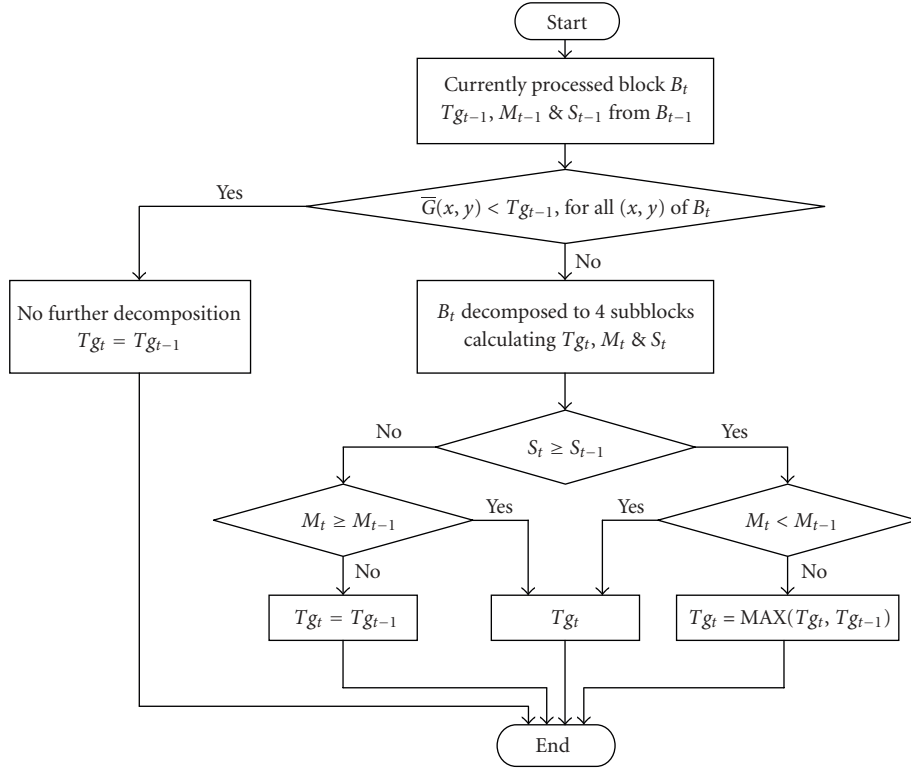
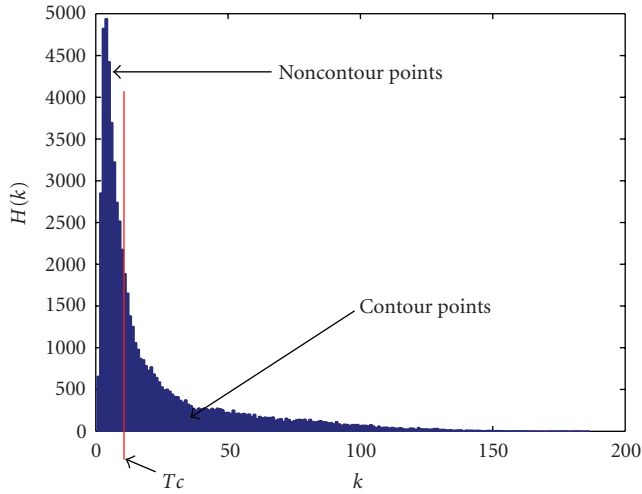


FIGURE 5: Flow chart of quad-tree decomposition.

FIGURE 6: Histogram of $G^{d^*}(x, y)$.

denotes the number of directions needed. The direction d_{k+1} of the next point thus has three possible values: d_{k-1} , d_k and d_{k+1} . For instance, if $d_k = 1$, then the next contour point \mathbf{w}_{k+1} could appear at the predicted contour point \mathbf{p}_{k+1}^0 , \mathbf{p}_{k+1}^1 or \mathbf{p}_{k+1}^2 , as shown in Figure 7(a). With the left-sided point $\mathbf{l}_{k+1}^{d_k+j}$ and right-sided point $\mathbf{r}_{k+1}^{d_k+j}$ of the predicted contour point $\mathbf{p}_{k+1}^{d_k+j}$, the line formed by \mathbf{w}_k and $\mathbf{p}_{k+1}^{d_k+j}$ points is perpendicular to the line between $\mathbf{l}_{k+1}^{d_k+j}$ and $\mathbf{r}_{k+1}^{d_k+j}$, where j indicates the

direction deviation, as revealed in Figure 7(b) under $d_k = 1$ and $j = 0$. Additionally, $\mathbf{l}_{k+1}^{d_k+j}$ and $\mathbf{r}_{k+1}^{d_k+j}$ can be represented as

$$\begin{aligned} \mathbf{l}_{k+1}^{d_k+j} &= \left(x_k + \text{round} \left(2 \cos \left((d_k + j + 1) \times \frac{\pi}{4} \right) \right), \right. \\ &\quad \left. y_k - \text{round} \left(2 \sin \left((d_k + j + 1) \times \frac{\pi}{4} \right) \right) \right), \\ \mathbf{r}_{k+1}^{d_k+j} &= \left(x_k + \text{round} \left(2 \cos \left((d_k + j - 1) \times \frac{\pi}{4} \right) \right), \right. \\ &\quad \left. y_k - \text{round} \left(2 \sin \left((d_k + j - 1) \times \frac{\pi}{4} \right) \right) \right), \end{aligned} \quad (5)$$

respectively, where j ranges from $-(i-1)/2$ to $(i-1)/2$, $\text{round}(\lambda)$ rounds off the value of λ to the nearest integer number.

(4) The gray-level average values \bar{L}_k and \bar{R}_k of the previous contour points are calculated as

$$\begin{aligned} \bar{L}_k &= \frac{1}{k+1} \sum_{p=0}^k I(\mathbf{l}_{k-p}^{d_k-p}), \\ \bar{R}_k &= \frac{1}{k+1} \sum_{p=0}^k I(\mathbf{r}_{k-p}^{d_k-p}). \end{aligned} \quad (6)$$

(5) $E_{k+1,l}(j)$ and $E_{k+1,r}(j)$ that interpret the relationships among the predicted point, its left-sided and right-sided

points, and \bar{L}_k and \bar{R}_k , are used to obtain the next probable contour point:

$$E_{k+1,l}(j) = |I(\mathbf{p}_{k+1}^{d_k+j}) - I(\mathbf{l}_{k+1}^{d_k+j})| - |I(\mathbf{l}_{k+1}^{d_k+j}) - \bar{L}_k|, \quad (7)$$

$$E_{k+1,r}(j) = |I(\mathbf{p}_{k+1}^{d_k+j}) - I(\mathbf{r}_{k+1}^{d_k+j})| - |I(\mathbf{r}_{k+1}^{d_k+j}) - \bar{R}_k|. \quad (8)$$

Equations (7) and (8) are used to determine the $(k+1)$ th contour point. The first term represents the gradient between the predicted point and its left-sided or right-sided point. The second term may prevent (7) or (8) from finding the wrong contours due to the noise interference. If the difference in the second term is too large, then the wrong contour point may be found.

(6) Select the largest value by using $F_{k+1}(j) = \text{MAX}[E_{k+1,l}(j) \text{ or } E_{k+1,r}(j)]$, for $-(i-1)/2 \leq j \leq (i-1)/2$. If $F_{k+1}(j) \geq Tc$, then the correct direction has been found, and go to step 8. Here, Tc comes from the decomposed block which the predicted contour point $\mathbf{p}_{k+1}^{d_k+j}$ belongs to.

(7) If $i = 3$, then the previously searched direction may have deviated from the correct path and set $i = 7$ to obtain the seven neighboring points for direction searching, going to step 5. Otherwise, stop the search procedure, and go to step 10.

(8) From $F_{k+1}(j)$, the correct direction d_{k+1} and position of the $(k+1)$ th contour point are calculated as follows:

$$\begin{aligned} d_{k+1} &= d_k + j, \\ \mathbf{w}_{k+1} &= \left(x_k + \text{round} \left(\cos \left(d_{k+1} \times \frac{\pi}{4} \right) \right), \right. \\ &\quad \left. y_k - \text{round} \left(\sin \left(d_{k+1} \times \frac{\pi}{4} \right) \right) \right). \end{aligned} \quad (9)$$

(9) The searching procedure is finished when the $(k+1)$ th contour point is in the same position as any of the previous searched contour points or has gone beyond the four boundaries of the image. If neither condition is true, then set $k = k + 1$, and return to step 3 to discover the next contour point.

(10) If $d_0 = d^* + 2$, set $d_0 = (d^* + 6)$ and go to step 2 to search for the contour points in the opposite direction to $d^* + 2$.

(11) Go to step 1 for another initial point that is not searched. When all initial points are conducted, the procedure of the modified edge-following method is ended.

During the searching process, taking in the left and right neighboring points of the next predicted contour point in computation would significantly reduce the tendency of the edge-following method to deviate from the correct edge due to noise interferences. Only three directions are first searched in the searching process. If the $F_{k+1}(j)$ values of these three directions are all below Tc , then the search proceeds to the seven directions. The searching time is thus significantly decreased, since most searches only need the computation of the gradients in three directions. Figure 8 depicts the flow chart of the proposed modified edge-following scheme that searches from an initial point.

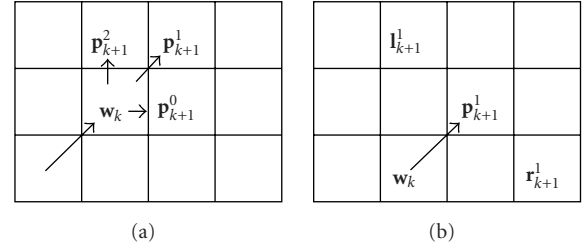


FIGURE 7: Relationship of \mathbf{w}_k with its neighboring points. (a) Predicted points of \mathbf{p}_{k+1}^0 , \mathbf{p}_{k+1}^1 and \mathbf{p}_{k+1}^2 under $d_k = 1$. (b) \mathbf{p}_{k+1}^1 , \mathbf{l}_{k+1}^1 and \mathbf{r}_{k+1}^1 under $d_k = 1$ and $j = 0$.

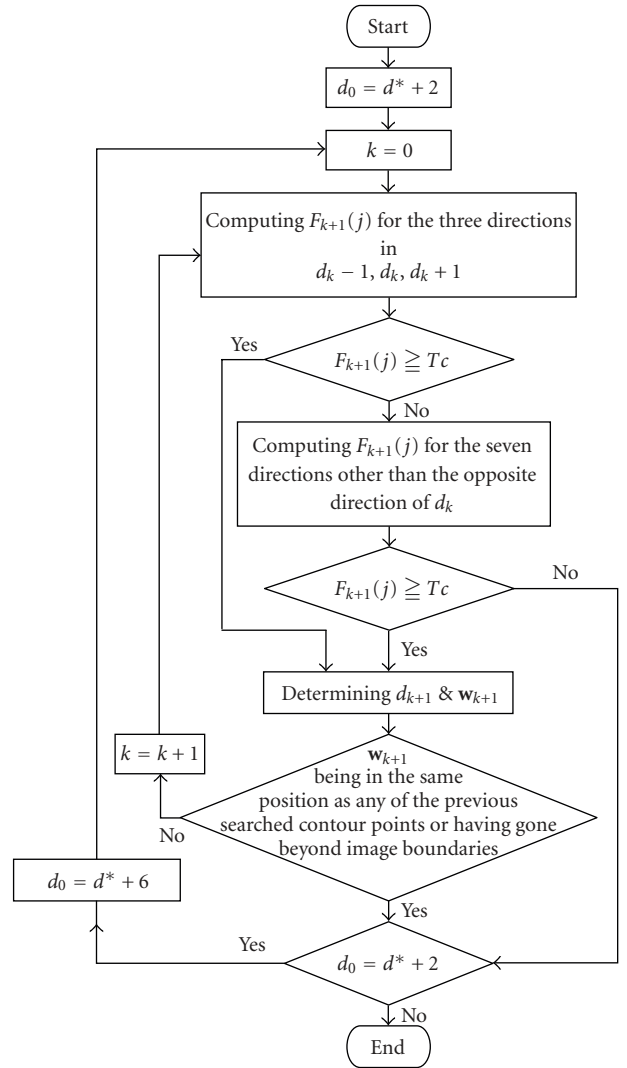


FIGURE 8: Flow chart of the modified edge-following scheme.

3. Computational Analyses

In the following experiment, the LWOE, E-GVF snake, watershed and proposed methods are adopted and compared in processing time and segmentation accuracy. Among these methods, LWOE is a supervised segmentation method, with

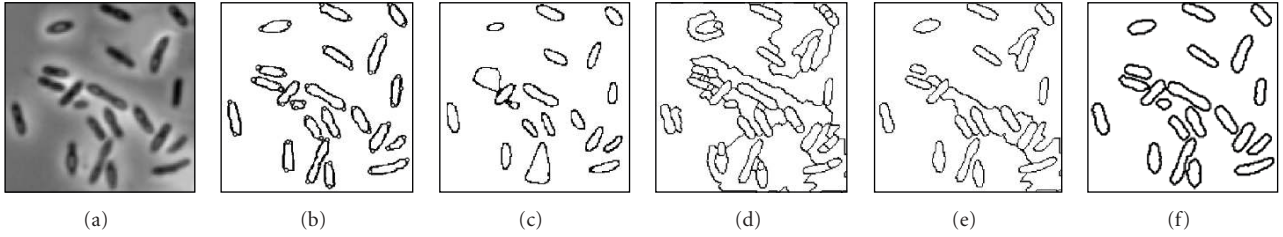


FIGURE 9: Segmented results of the “bacteria” image. (a) Original image. (b) Result obtained by the LWOF method. (c) Result obtained by the E-GVF snake method. (d) Result obtained by the watershed method with a threshold of 20. (e) Result obtained by the watershed method with a threshold of 40. (f) Result obtained by the proposed method.

small circles indicating the positions selected by the user for segmentation. The user can adequately select some points close to an object to obtain a segmentation result that is closest to that observed with naked eyes. However, LWOF requires a very long computational time, and is dependent on the user. Consequently, the processing time of LWOF must include the manual operational time. The segmentation function adopted by the watershed method is gradient [9]. Additionally, the merging operation is based on the region mean where the threshold indicates the criterion of region merging. Here, two quantities, precision and recall, are employed to evaluate the segmented results from each segmentation method [34, 36]. Precision, P , is the probability that a detected pixel is a true one. Recall, R , is the probability that a true pixel is detected:

$$\text{Precision}(P) = \frac{\text{True boundary pixels extracted}}{\text{Total number of boundary pixels extracted}},$$

$$\text{Recall}(R) = \frac{\text{True boundary pixels extracted}}{\text{Total number of true boundary pixels}}.$$
(10)

Additionally, the F-measure, F , with considering P and R is adopted and defined as

$$F = \frac{PR}{\alpha R + (1 - \alpha)P},$$
(11)

where α is set to 0.5 in our simulations.

Figure 9(a) shows a 256×256 -pixel “bacteria” image, which includes about 20 bacteria objects that do not overlap with each other. The shot was taken out of focus, causing the image edges to be blurry, thus affecting some of the segmented results. Figure 9(b) displays the result from LWOF. LWOF takes a long time because it must perform about 20 object selection operations. Figure 9(c) depicts the result from the E-GVF snake method. Some groups of connected neighboring bacteria objects are mistaken for single objects. Figures 9(d) and 9(e) show the results from utilizing the watershed method with thresholds of 20 and 40, respectively. Many erroneous borders are found when the threshold is 20, with some single objects being segmented into multiple smaller parts. While fewer erroneous contours are found when the threshold is 40, some objects are still missing. The number of missing objects increases with the

threshold. Contrasts in this picture are significantly reduced owing to the unfocused image, making the threshold hard to adjust. An excessively large threshold causes missing objects, but a very small threshold would cause the background to blur with the bacteria, which make it even more difficult to segment. To do fair comparison, the watershed method is iteratively conducted under different thresholds to yield the best segmented results in the following analyses. Figure 9(f) displays the results from the proposed method, which is not affected by the out-of-focus image due to adequate initial points attained, and thus can segment every bacteria object.

Figure 10(a) shows the 540×420 -pixel “chessboard” image, which is a 3D manmade image including a chessboard and cylinders. The light effect is added in the picture, reflecting shadows of the cylinders on the chessboard. Figure 10(b) shows the ground truth from Figure 10(a). The result from LWOF is depicted in Figure 10(c). A fairly good result is obtained using the manual operation, but a large number of initial points required means that the computational time is very long. Figure 10(d) displays the result from the E-GVF snake method, which is clearly not appropriate for an image, with objects all very close to each other. The simulation result indicates that contour of the outermost layer is segmented, but that the squares inside the chessboard cannot be detached from each other, leaving the result with only one object. Figure 10(e) shows results from using the watershed method at a threshold being 27 with the maximum F-measure. Figure 10(f) depicts the result from the proposed method. The proposed method not only can segment the two letters and the cylinders, it also segments the chessboard itself better than does the watershed method with the best threshold value. The segmentation of the side surface in the chessboard is also far more accurate than that generated from the watershed method. Table 1 lists the segmentation results from the LWOF, E-GVF snake, watershed at a threshold with the maximum F-measure, and proposed methods. Objects from the picture include two areas of cylinders, 24 areas of the chessboard’s top side, letters “A” and “B”, and 10 areas of the chessboard’s front and right sides, for a total of 36 close-looped independent areas. While the supervised LWOF method has the highest F-measure, it also requires a long time. Amongst the unsupervised methods, the proposed method can segment the most objects, and also has a significantly higher F-measure than the E-GVF snake and watershed methods.

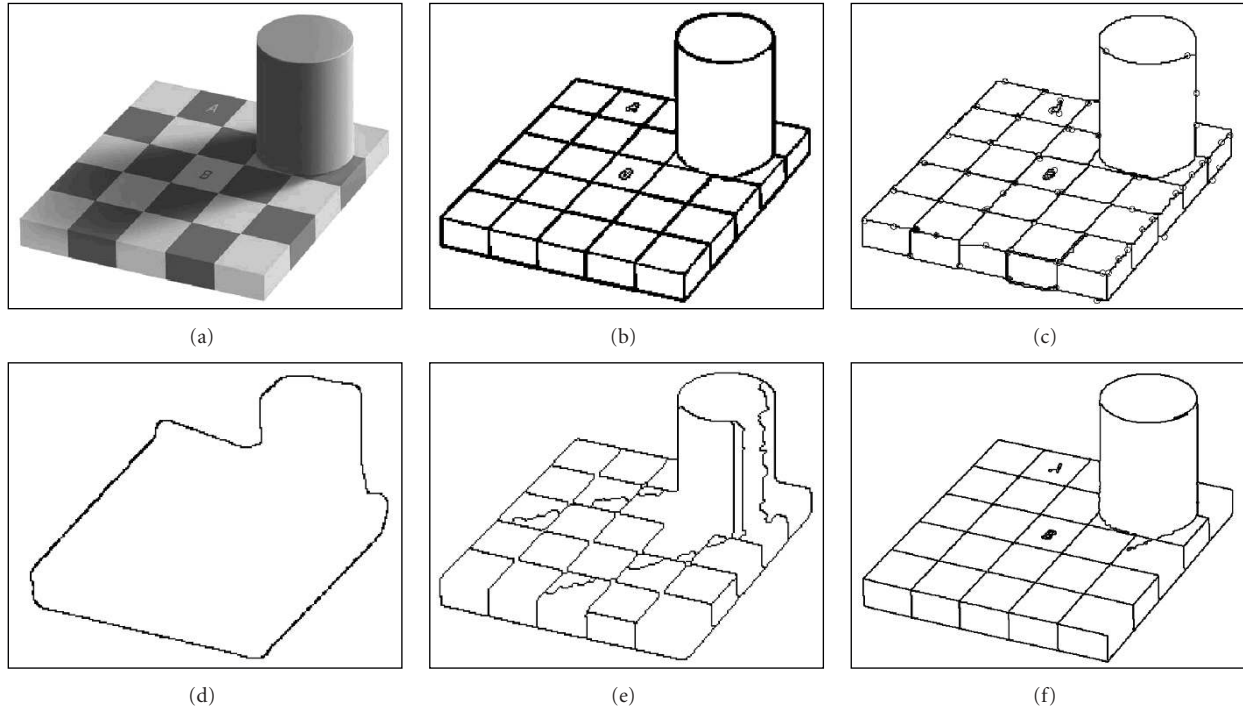


FIGURE 10: Segmented results of the “chessboard” image. (a) Original image. (b) Ground truth. (c) Result obtained by the LWOFF method. (d) Result obtained by the E-GVF snake method. (e) Result obtained by the watershed method with a threshold value of 27. (f) Result obtained by the proposed method.

TABLE 1: Segmentation results of the LWOFF, E-GVF, watershed and proposed methods.

Methods	Numbers of segmented objects	Performance	
		F-measures	Segmentation manners
LWOFF	36	0.97	supervised
E-GVF	1	0.44	unsupervised
Watershed	29	0.86	unsupervised
Proposed	32	0.95	unsupervised

Figure 11 shows the 360×360 -pixel “square” image corrupted by the Gaussian noise, at the Signal-to-Noise Ratio (SNR) of 18.87 dB. Figures 11(a) and 11(b) depict the noisy image and ground truth, respectively. The result from adopting the LWOFF segmentation is displayed in Figure 11(c). Not many points are selected manually since the angles of turns are not very large. However, the contour is not smooth due to the noise. Figure 11(d) shows the result obtained by using the E-GVF snake method. Some dark areas could be lost in the sharp corners. The result from using the watershed method at a threshold being 45 with the maximum F-measure is depicted in Figure 11(e). The proposed method can eliminate the problem and obtain the correct area as shown in Figure 11(f). Table 2 compares F-measures and computational time of the four segmentation methods at SNRs of 18.87 dB, 12.77 dB and 9.14 dB in which the watershed method adopts thresholds of 42, 44, and 45, respectively. By using the proposed method, the segmented

area has the highest F-measures in each of the three SNR scenarios. The proposed method using the modified edge-following technique is significantly faster than LWOFF when the manual operational time is considered. Additionally, the proposed method provides comparable or even better results than the LWOFF. The results obtained by the watershed method at thresholds with the maximum F-measures take slightly lower processing time than the proposed method when the threshold selection time is not counted in the watershed method. The above experiments were conducted by using C programs running on a Pentium IV 2.4 GHz CPU under Windows XP operating system.

The above experimental results demonstrate that the proposed method performs better than the other methods. As for the blurry objects resulting from the out-of-focus shot in Figure 9, the proposed method can accurately segment all objects without incurring over-segmentation and under-segmentation as does the watershed method

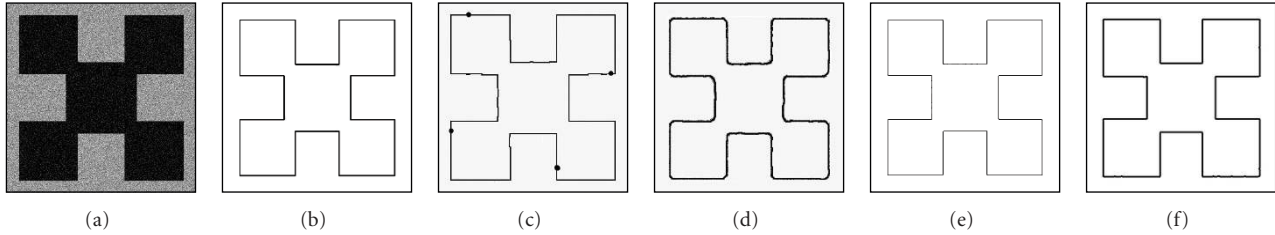


FIGURE 11: Segmented results of the “square” image added by noises with the Gaussian distribution at SNR of 18.87 dB. (a) Noisy image. (b) Ground truth. (c) Result obtained by the LWOFF method. (d) Result obtained by the E-GVF snake method. (e) Result obtained by the watershed method with a threshold of 45. (f) Result obtained by the proposed method.

TABLE 2: F-measures and computational time of the LWOFF, snake, watershed and proposed methods.

Methods	Performance					
	SNR = 18.87 dB		SNR = 12.77 dB		SNR = 9.14 dB	
	F-measures	Processing time (sec)	F-measures	Processing time (sec)	F-measures	Processing time (sec)
LWOFF	0.95	7.20*	0.86	10.60*	0.80	15.30*
E-GVF Snake	0.93	1.21	0.81	1.32	0.75	1.51
Watershed	0.94	0.26**	0.86	0.29**	0.81	0.31**
Proposed	0.96	0.31	0.88	0.32	0.82	0.34

Note: the symbol of “*” indicates the processing time including manual operational time. Additionally, the symbol of “**” denotes that the processing time is calculated under a specific threshold where the iterative process under different thresholds is not included.

in Figures 9(d) and 9(e), respectively. Figure 10 reveals that both the proposed and watershed methods demonstrate the capability of fully segmenting objects inside another object and overlapping objects but the E-GVF snake method cannot be applied in these pictures. The proposed method can segment more objects out of the image in Figure 10, which contains many individual objects, than the watershed method. In the simulation results shown in Figure 11, by considering the gray-level changes of the left and right neighboring points during the contour-searching process, the proposed method not only reduces the noise interference, it also outperforms both the E-GVF snake and watershed methods against noise interference.

To do fair comparison, the data set and benchmarks from the Computer Vision Group, University of California at Berkeley were applied in the proposed and watershed methods, where the watershed method is also iteratively performed to search for the optimized threshold. Since the E-GVF snake method is not suitable for the image with objects inside another object, it is not addressed in this data set. The segmentation results of the conventional methods such as Brightness Gradient (BG), Texture Gradient (TG), and Brightness/Texture Gradients (B/TG) are referred from [34] for comparison. The precision-recall (P - R) curve shows the inherent trade-off between P and R . Figure 12 depicts the segmented results and the precision-recall curves from Human, BG, TG, B/TG, watershed and proposed methods. In Figures 12(c), 12(d), 12(e), and 12(f), the BG, TG, B/TG and watershed methods are iteratively conducted under different thresholds to yield the best segmented results with F of 0.87, 0.88, 0.88, and 0.83, respectively. In the proposed method, the threshold is automatically determined

to be a specific value that only yields a converged point in Figure 12(g), where the F-measure of 0.93 can be achieved. Hence, the proposed method does not need the ground truth to iteratively determine the best-matched thresholds and thereby greatly reduces the computational time demanded by the BG, TG, B/TG, and watershed methods.

The proposed method is applied to all test images, and its segmentation results are evaluated according to the ground truths. Particularly, six images from 100 test images are added by the Gaussian noise to become noisy images at the SNR of 18.87 dB. Figure 13 displays the segmented results of original and noisy images using the proposed and watershed methods, where F-measures and computational time are listed in Table 3. From Figure 13, the segmented results from the proposed method exhibit more apparent and complete objects than those from the watershed method at specific thresholds with the maximum F-measures. In Figures 13(a), 13(b), 13(c), 13(d), 13(e), and 13(f), the watershed method is conducted under thresholds of 23, 30, 7, 45, 16, and 32 to yield the best segmented results, respectively. Additionally, P - R curves from proposed and watershed methods are depicted. Moreover, the proposed method with thresholds adapting to image contents has higher or equal F-measure values than the watershed methods as illustrated in Table 3. Regarding to computational time, the proposed method at most cases takes slightly longer time than the watershed method owing to additional threshold determination process required by the proposed method when the iterative process of determining the best threshold of the watershed method is not included.

The histograms of F-measures from 100 test images by using BG, TG, B/TG, and proposed method are shown in

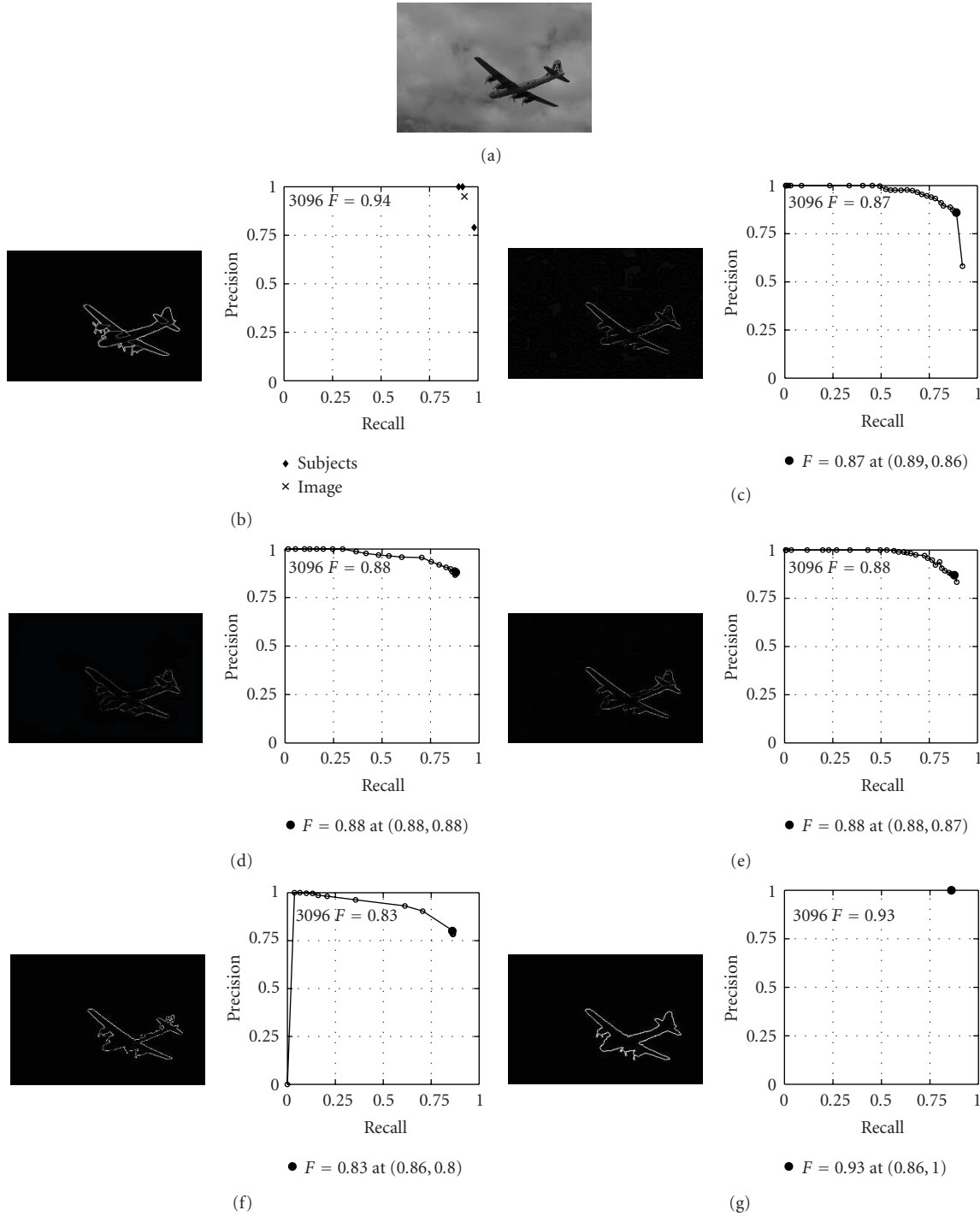


FIGURE 12: Segmented results and precision-recall curves of the 3096th image in the Berkeley segmentation data set. (a) Original image. (b) Human. (c) Brightness gradient. (d) Texture gradient. (e) Brightness/texture gradients. (f) Watershed. (g) Proposed method.

Figure 14. Although the proposed method yields little poor performance in few images under very low contrast, it still has above 0.6 of F-measure for 70 test images. The number of F-measures between 0.6 and 0.9 in the proposed method is 68 larger than 64 in BG and 59 in TG, and smaller than 73 in B/TG while the number of F-measures between 0.9 and 1.0 in the proposed method is 2 better than none in

BG, TG, and B/TG. Restated, when the images have apparent contours, the proposed method can yield segmented results close to the ground truth done by humans. The proposed method can effectively determine the main foreground and is not trapped to the complex background. Hence, the values of F in these cases under the proposed method can be superior to those using the conventional methods. From

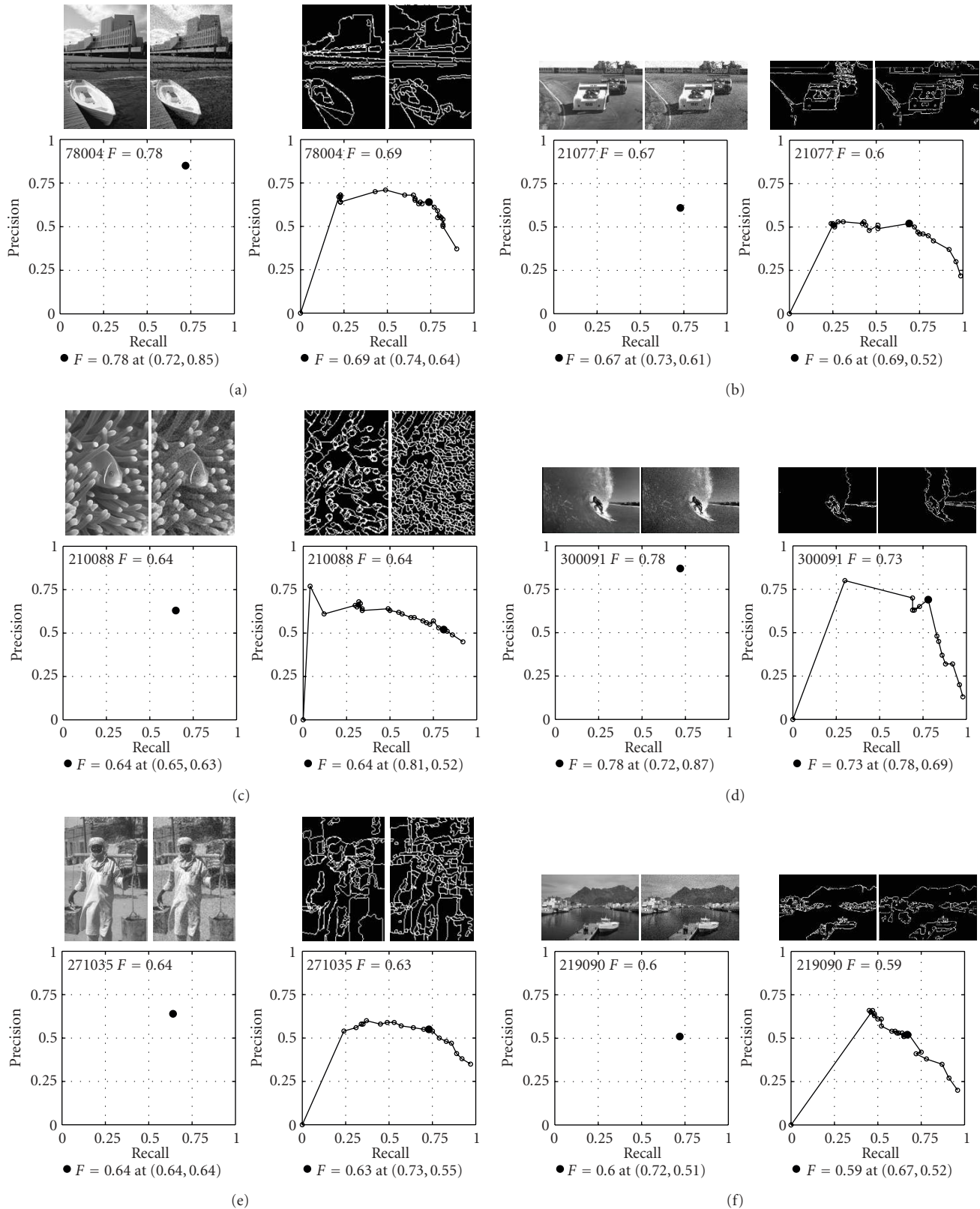


FIGURE 13: Original image, noisy image, segmented noisy image from the proposed method, segmented noisy image from the watershed method at a threshold with the maximum F-measure, P - R curve by using the proposed method, P - R curve by using the watershed method, displaying from left to right in two rows. (a) 78004th image. (b) 21077th image. (c) 210088th image. (d) 300091st image. (e) 271035th image. (f) 219090th image.

TABLE 3: F-measures and computational time of the noisy images conducted by the proposed and watershed methods.

Image indices	Performance			
	Proposed method		Watershed	
	F-measures	Processing time (sec)	F-measures	Processing time (sec)
78004	0.78	0.34	0.69	0.35*
21077	0.67	0.37	0.60	0.36*
210088	0.64	0.48	0.64	0.38*
300091	0.78	0.32	0.73	0.30*
271035	0.64	0.36	0.63	0.38*
219090	0.60	0.37	0.59	0.35*

Note: the symbol of “*” denotes that the processing time is calculated under a specific threshold where the iterative process under different thresholds is not included.

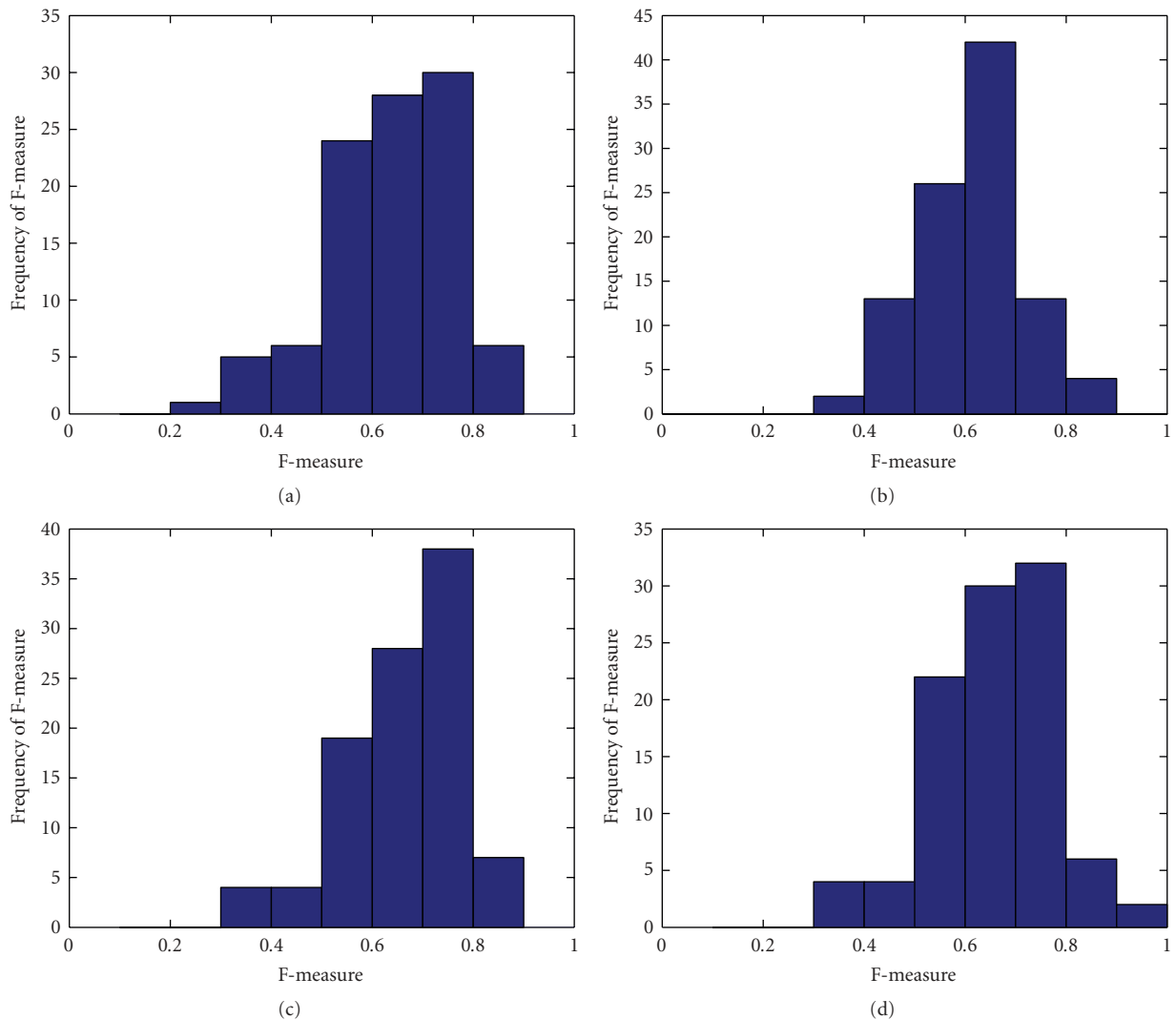


FIGURE 14: Histograms of F-measures from 100 test images. (a) BG. (b) TG. (c) B/TG. (d) Proposed method.

computational time point of view, the proposed method that uses automatically determined thresholds to perform image segmentation apparently takes the least time than the conventional methods that are iteratively conducted under different thresholds to converge their minima.

In practical applications, the ground truths are not available. The conventional methods, BG, TG, and B/TG, that need the ground truths to determine the best-matched thresholds or parameters may not obtain good segmentation results under no ground truth. However, the proposed robust

segmentation method does not need the ground truths and iterative operations to determine the segmentation results, and therefore is very suitable to various real-time image and video segmentation applications under no ground truth.

4. Conclusion

This work proposes an automatically determined threshold mechanism to perform a robust segmentation. Different initial-point thresholds are determined and given to areas with drastic and smooth changes in gray-level values. The contour thresholds are generated by analyzing the decomposed blocks, thus preventing the search from falling into the wrong path, and saving computational time. The contour search process also considers the gradients of the left and right neighboring points of every predicted contour point, in order to lower the possibility of the method being affected by the neighboring noise interferences. Additionally, most of the searching process requires only the computation of the gradients of three directions, thus minimizing the searching time. The proposed method can perform segmentation on objects inside another object and objects that are close to each other, which the E-GVF snake method cannot perform. The proposed method also solves problems encountered by the watershed method, in which the results may change significantly as the threshold values differ. The proposed method can significantly reduce noise interference, which easily affects the conventional edge-following method. In handling blurry objects from an out-of-focus shot, the proposed method can also segment the required objects. Finally, the benchmark from Computer Vision Group, University of California at Berkeley was conducted to demonstrate that the proposed method could take the least computational time to obtain robust and good segmentation performance than the conventional ones. Therefore, the proposed method can be widely and effectively employed in various segmentation applications.

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