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## Authors

Aubert, B
Barate, R
Boutigny, D
et al.

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# Improved Measurement of the Cabibbo-Kobayashi-Maskawa Angle $\alpha$ Using $B^{\boldsymbol{0}}(\bar{B}) \rightarrow \boldsymbol{\rho}^{+} \boldsymbol{\rho}^{-}$Decays 

B. Aubert, ${ }^{1}$ R. Barate, ${ }^{1}$ D. Boutigny, ${ }^{1}$ F. Couderc, ${ }^{1}$ Y. Karyotakis, ${ }^{1}$ J. P. Lees, ${ }^{1}$ V. Poireau, ${ }^{1}$ V. Tisserand, ${ }^{1}$ A. Zghiche, ${ }^{1}$ E. Grauges, ${ }^{2}$ A. Palano, ${ }^{3}$ M. Pappagallo, ${ }^{3}$ A. Pompili, ${ }^{3}$ J. C. Chen, ${ }^{4}$ N. D. Qi, ${ }^{4}$ G. Rong, ${ }^{4}$ P. Wang, ${ }^{4}$ Y. S. Zhu, ${ }^{4}$ G. Eigen, ${ }^{5}$ I. Ofte, ${ }^{5}$ B. Stugu, ${ }^{5}$ G. S. Abrams, ${ }^{6}$ A. W. Borgland, ${ }^{6}$ A. B. Breon, ${ }^{6}$ D. N. Brown, ${ }^{6}$ J. Button-Shafer, ${ }^{6}$ R. N. Cahn, ${ }^{6}$ E. Charles, ${ }^{6}$ C. T. Day, ${ }^{6}$ M. S. Gill, ${ }^{6}$ A. V. Gritsan, ${ }^{6}$ Y. Groysman, ${ }^{6}$ R. G. Jacobsen, ${ }^{6}$ R. W. Kadel, ${ }^{6}$ J. Kadyk, ${ }^{6}$ L. T. Kerth, ${ }^{6}$ Yu. G. Kolomensky, ${ }^{6}$ G. Kukartsev, ${ }^{6}$ G. Lynch, ${ }^{6}$ L. M. Mir, ${ }^{6}$ P. J. Oddone, ${ }^{6}$ T. J. Orimoto, ${ }^{6}$ M. Pripstein, ${ }^{6}$ N. A. Roe, ${ }^{6}$
M. T. Ronan, ${ }^{6}$ W. A. Wenzel, ${ }^{6}$ M. Barrett, ${ }^{7}$ K. E. Ford, ${ }^{7}$ T. J. Harrison, ${ }^{7}$ A. J. Hart, ${ }^{7}$ C. M. Hawkes, ${ }^{7}$ S. E. Morgan, ${ }^{7}$ A. T. Watson, ${ }^{7}$ M. Fritsch, ${ }^{8}$ K. Goetzen, ${ }^{8}$ T. Held, ${ }^{8}$ H. Koch, ${ }^{8}$ B. Lewandowski, ${ }^{8}$ M. Pelizaeus, ${ }^{8}$ K. Peters, ${ }^{8}$ T. Schroeder, ${ }^{8}$ M. Steinke, ${ }^{8}$ J. T. Boyd, ${ }^{9}$ J. P. Burke, ${ }^{9}$ N. Chevalier, ${ }^{9}$ W. N. Cottingham, ${ }^{9}$ M. P. Kelly, ${ }^{9}$ T. Cuhadar-Donszelmann, ${ }^{10}$ C. Hearty, ${ }^{10}$ N.S. Knecht, ${ }^{10}$ T. S. Mattison, ${ }^{10}$ J. A. McKenna, ${ }^{10}$ D. Thiessen, ${ }^{10}$ A. Khan, ${ }^{11}$ P. Kyberd, ${ }^{11}$ L. Teodorescu, ${ }^{11}$ A. E. Blinov, ${ }^{12}$ V. E. Blinov, ${ }^{12}$ A. D. Bukin, ${ }^{12}$ V. P. Druzhinin, ${ }^{12}$ V. B. Golubev, ${ }^{12}$ V. N. Ivanchenko, ${ }^{12}$ E. A. Kravchenko, ${ }^{12}$ A. P. Onuchin, ${ }^{12}$ S. I. Serednyakov, ${ }^{12}$ Yu. I. Skovpen, ${ }^{12}$ E. P. Solodov, ${ }^{12}$ A. N. Yushkov, ${ }^{12}$ D. Best, ${ }^{13}$ M. Bondioli, ${ }^{13}$ M. Bruinsma, ${ }^{13}$ M. Chao, ${ }^{13}$ I. Eschrich, ${ }^{13}$ D. Kirkby, ${ }^{13}$ A. J. Lankford, ${ }^{13}$ M. Mandelkern, ${ }^{13}$ R. K. Mommsen, ${ }^{13}$ W. Roethel, ${ }^{13}$ D. P. Stoker, ${ }^{13}$ C. Buchanan, ${ }^{14}$ B. L. Hartfiel, ${ }^{14}$ A. J. R. Weinstein, ${ }^{14}$ S. D. Foulkes, ${ }^{15}$ J. W. Gary, ${ }^{15}$ O. Long, ${ }^{15}$ B. C. Shen, ${ }^{15}$ K. Wang, ${ }^{15}$ L. Zhang, ${ }^{15}$ D. del Re, ${ }^{16}$ H. K. Hadavand, ${ }^{16}$ E. J. Hill, ${ }^{16}$ D. B. MacFarlane, ${ }^{16}$ H. P. Paar, ${ }^{16}$ S. Rahatlou, ${ }^{16}$ V. Sharma, ${ }^{16}$ J. W. Berryhill, ${ }^{17}$ C. Campagnari, ${ }^{17}$ A. Cunha, ${ }^{17}$ B. Dahmes, ${ }^{17}$ T. M. Hong, ${ }^{17}$ A. Lu, ${ }^{17}$ M. A. Mazur,,$^{17}$ J. D. Richman, ${ }^{17}$ W. Verkerke, ${ }^{17}$ T. W. Beck, ${ }^{18}$ A. M. Eisner, ${ }^{18}$ C. J. Flacco, ${ }^{18}$ C. A. Heusch, ${ }^{18}$ J. Kroseberg, ${ }^{18}$ W. S. Lockman, ${ }^{18}$ G. Nesom, ${ }^{18}$ T. Schalk, ${ }^{18}$ B. A. Schumm,,$^{18}$ A. Seiden, ${ }^{18}$ P. Spradlin, ${ }^{18}$ D. C. Williams, ${ }^{18}$ M. G. Wilson, ${ }^{18}$ J. Albert, ${ }^{19}$ E. Chen, ${ }^{19}$ G. P. Dubois-Felsmann, ${ }^{19}$ A. Dvoretskii, ${ }^{19}$ D. G. Hitlin, ${ }^{19}$ I. Narsky, ${ }^{19}$ T. Piatenko, ${ }^{19}$ F. C. Porter, ${ }^{19}$ A. Ryd, ${ }^{19}$ A. Samuel, ${ }^{19}$ S. Yang, ${ }^{19}$ R. Andreassen, ${ }^{20}$ S. Jayatilleke, ${ }^{20}$ G. Mancinelli, ${ }^{20}$ B. T. Meadows, ${ }^{20}$ M. D. Sokoloff, ${ }^{20}$ F. Blanc, ${ }^{21}$ P. Bloom, ${ }^{21}$ S. Chen, ${ }^{21}$ W. T. Ford, ${ }^{21}$ U. Nauenberg, ${ }^{21}$ A. Olivas, ${ }^{21}$ P. Rankin, ${ }^{21}$ W. O. Ruddick, ${ }^{21}$ J. G. Smith, ${ }^{21}$ K. A. Ulmer, ${ }^{21}$ J. Zhang, ${ }^{21}$ A. Chen, ${ }^{22}$ E. A. Eckhart, ${ }^{22}$ J. L. Harton, ${ }^{22}$ A. Soffer, ${ }^{22}$ W. H. Toki, ${ }^{22}$ R. J. Wilson, ${ }^{22}$ Q. Zeng, ${ }^{22}$ B. Spaan, ${ }^{23}$ D. Altenburg, ${ }^{24}$ T. Brandt, ${ }^{24}$ J. Brose, ${ }^{24}$ M. Dickopp, ${ }^{24}$ E. Feltresi, ${ }^{24}$ A. Hauke, ${ }^{24}$ V. Klose, ${ }^{24}$ H. M. Lacker, ${ }^{24}$ E. Maly, ${ }^{24}$ R. Nogowski, ${ }^{24}$ S. Otto, ${ }^{24}$ A. Petzold, ${ }^{24}$ G. Schott, ${ }^{24}$ J. Schubert, ${ }^{24}$ K. R. Schubert, ${ }^{24}$ R. Schwierz, ${ }^{24}$ J. E. Sundermann, ${ }^{24}$ D. Bernard, ${ }^{25}$ G. R. Bonneaud, ${ }^{25}$ P. Grenier, ${ }^{25}$ S. Schrenk, ${ }^{25}$ Ch. Thiebaux, ${ }^{25}$ G. Vasileiadis, ${ }^{25}$ M. Verderi, ${ }^{25}$ D. J. Bard, ${ }^{26}$ P. J. Clark, ${ }^{26}$ W. Gradl, ${ }^{26}$ F. Muheim, ${ }^{26}$ S. Playfer, ${ }^{26}$ Y. Xie, ${ }^{26}$ M. Andreotti, ${ }^{27}$ V. Azzolini, ${ }^{27}$ D. Bettoni, ${ }^{27}$ C. Bozzi, ${ }^{27}$ R. Calabrese, ${ }^{27}$ G. Cibinetto, ${ }^{27}$ E. Luppi, ${ }^{27}$ M. Negrini, ${ }^{27}$ L. Piemontese, ${ }^{27}$ A. Sarti, ${ }^{27}$ F. Anulli, ${ }^{28}$ R. Baldini-Ferroli, ${ }^{28}$ A. Calcaterra, ${ }^{28}$ R. de Sangro, ${ }^{28}$ G. Finocchiaro,,${ }^{28}$ P. Patteri, ${ }^{28}$ I. M. Peruzzi, ${ }^{28}$ M. Piccolo, ${ }^{28}$ A. Zallo, ${ }^{28}$ A. Buzzo, ${ }^{29}$ R. Capra, ${ }^{29}$ R. Contri, ${ }^{29}$ M. Lo Vetere,,${ }^{29}$ M. Macri, ${ }^{29}$ M. R. Monge, ${ }^{29}$ S. Passaggio, ${ }^{29}$ C. Patrignani, ${ }^{29}$ E. Robutti, ${ }^{29}$ A. Santroni, ${ }^{29}$ S. Tosi, ${ }^{29}$ S. Bailey, ${ }^{30}$ G. Brandenburg, ${ }^{30}$ K. S. Chaisanguanthum, ${ }^{30}$ M. Morii, ${ }^{30}$ E. Won, ${ }^{30}$ R. S. Dubitzky, ${ }^{31}$ U. Langenegger, ${ }^{31}$ J. Marks, ${ }^{31}$ S. Schenk, ${ }^{31}$ U. Uwer, ${ }^{31}$ W. Bhimji, ${ }^{32}$ D. A. Bowerman, ${ }^{32}$ P. D. Dauncey, ${ }^{32}$ U. Egede, ${ }^{32}$ J. R. Gaillard, ${ }^{32}$ G. W. Morton,,${ }^{32}$ J. A. Nash, ${ }^{32}$ M. B. Nikolich, ${ }^{32}$ G. P. Taylor, ${ }^{32}$ M. J. Charles, ${ }^{33}$ G. J. Grenier, ${ }^{33}$ U. Mallik, ${ }^{33}$ A. K. Mohapatra, ${ }^{33}$ J. Cochran, ${ }^{34}$ H. B. Crawley, ${ }^{34}$ V. Eyges, ${ }^{34}$ W. T. Meyer, ${ }^{34}$ S. Prell, ${ }^{34}$ E. I. Rosenberg, ${ }^{34}$ A. E. Rubin, ${ }^{34}$ J. Yi, ${ }^{34}$ N. Arnaud, ${ }^{35}$ M. Davier, ${ }^{35}$ X. Giroux, ${ }^{35}$ G. Grosdidier, ${ }^{35}$ A. Höcker, ${ }^{35}$ F. Le Diberder, ${ }^{35}$ V. Lepeltier, ${ }^{35}$ A. M. Lutz, ${ }^{35}$ T. C. Petersen, ${ }^{35}$ M. Pierini, ${ }^{35}$ S. Plaszczynski, ${ }^{35}$ S. Rodier, ${ }^{35}$ P. Roudeau, ${ }^{35}$ M. H. Schune, ${ }^{35}$ A. Stocchi, ${ }^{35}$ G. Wormser, ${ }^{35}$ C. H. Cheng, ${ }^{36}$ D. J. Lange, ${ }^{36}$ M. C. Simani, ${ }^{36}$ D. M. Wright, ${ }^{36}$ A. J. Bevan, ${ }^{37}$ C. A. Chavez, ${ }^{37}$ J. P. Coleman, ${ }^{37}$ I. J. Forster, ${ }^{37}$ J. R. Fry, ${ }^{37}$ E. Gabathuler, ${ }^{37}$ R. Gamet, ${ }^{37}$ K. A. George, ${ }^{37}$ D. E. Hutchcroft, ${ }^{37}$ R. J. Parry, ${ }^{37}$ D. J. Payne, ${ }^{37}$ C. Touramanis, ${ }^{37}$ C. M. Cormack, ${ }^{38}$ F. Di Lodovico, ${ }^{38}$ C. L. Brown, ${ }^{39}$ G. Cowan, ${ }^{39}$ R. L. Flack, ${ }^{39}$ H. U. Flaecher, ${ }^{39}$ M. G. Green, ${ }^{39}$ P. S. Jackson, ${ }^{39}$ T. R. McMahon, ${ }^{39}$ S. Ricciardi, ${ }^{39}$ F. Salvatore, ${ }^{39}$ D. Brown, ${ }^{40}$ C. L. Davis, ${ }^{40}$ J. Allison, ${ }^{41}$ N. R. Barlow, ${ }^{41}$ R. J. Barlow, ${ }^{41}$ M. C. Hodgkinson, ${ }^{41}$ G. D. Lafferty, ${ }^{41}$ M. T. Naisbit, ${ }^{41}$ J. C. Williams, ${ }^{41}$ C. Chen, ${ }^{42}$ A. Farbin, ${ }^{42}$ W. D. Hulsbergen, ${ }^{42}$ A. Jawahery, ${ }^{42}$ D. Kovalskyi, ${ }^{42}$ C. K. Lae, ${ }^{42}$ V. Lillard, ${ }^{42}$ D. A. Roberts, ${ }^{42}$ G. Blaylock, ${ }^{43}$ C. Dallapiccola, ${ }^{43}$ S. S. Hertzbach, ${ }^{43}$ R. Kofler, ${ }^{43}$ V. B. Koptchev, ${ }^{43}$ T. B. Moore, ${ }^{43}$ S. Saremi, ${ }^{43}$ H. Staengle, ${ }^{43}$ S. Willocq, ${ }^{43}$ R. Cowan, ${ }^{44}$ K. Koeneke, ${ }^{44}$ G. Sciolla, ${ }^{44}$ S. J. Sekula, ${ }^{44}$ F. Taylor, ${ }^{44}$ R. K. Yamamoto, ${ }^{44}$ H. Kim, ${ }^{45}$ P. M. Patel, ${ }^{45}$ S. H. Robertson, ${ }^{45}$ A. Lazzaro, ${ }^{46}$ V. Lombardo, ${ }^{46}$ F. Palombo, ${ }^{46}$ J. M. Bauer, ${ }^{47}$ L. Cremaldi, ${ }^{47}$ V. Eschenburg, ${ }^{47}$ R. Godang, ${ }^{47}$ R. Kroeger, ${ }^{47}$ J. Reidy, ${ }^{47}$ D. A. Sanders, ${ }^{47}$ D. J. Summers, ${ }^{47}$ H. W. Zhao, ${ }^{47}$ S. Brunet, ${ }^{48}$ D. Côté, ${ }^{48}$ P. Taras, ${ }^{48}$ B. Viaud, ${ }^{48}$ H. Nicholson, ${ }^{49}$ N. Cavallo, ${ }^{50, *}$ G. De Nardo, ${ }^{50}$ F. Fabozzi, ${ }^{50, *}$ C. Gatto, ${ }^{50}$ L. Lista, ${ }^{50}$ D. Monorchio, ${ }^{50}$ P. Paolucci, ${ }^{50}$ D. Piccolo, ${ }^{50}$ C. Sciacca, ${ }^{50}$ M. Baak, ${ }^{51}$ H. Bulten, ${ }^{51}$ G. Raven, ${ }^{51}$ H. L. Snoek, ${ }^{51}$ L. Wilden, ${ }^{51}$ C. P. Jessop, ${ }^{52}$ J. M. LoSecco, ${ }^{52}$
T. Allmendinger, ${ }^{53}$ G. Benelli, ${ }^{53}$ K. K. Gan, ${ }^{53}$ K. Honscheid, ${ }^{53}$ D. Hufnagel,,${ }^{53}$ P. D. Jackson,,${ }^{53}$ H. Kagan, ${ }^{53}$ R. Kass, ${ }^{53}$ T. Pulliam, ${ }^{53}$ A. M. Rahimi, ${ }^{53}$ R. Ter-Antonyan, ${ }^{53}$ Q. K. Wong, ${ }^{53}$ J. Brau, ${ }^{54}$ R. Frey, ${ }^{54}$ O. Igonkina, ${ }^{54}$ M. Lu, ${ }^{54}$ C. T. Potter,,${ }^{54}$ N. B. Sinev, ${ }^{54}$ D. Strom, ${ }^{54}$ E. Torrence, ${ }^{54}$ F. Colecchia, ${ }^{55}$ A. Dorigo, ${ }^{55}$ F. Galeazzi, ${ }^{55}$ M. Margoni, ${ }^{55}$ M. Morandin, ${ }^{55}$ M. Posocco, ${ }^{55}$ M. Rotondo, ${ }^{55}$ F. Simonetto, ${ }^{55}$ R. Stroili, ${ }^{55}$ C. Voci, ${ }^{55}$ M. Benayoun, ${ }^{56}$ H. Briand, ${ }^{56}$ J. Chauveau, ${ }^{56}$ P. David, ${ }^{56}$ L. Del Buono, ${ }^{56}$ Ch. de la Vaissière, ${ }^{56}$ O. Hamon, ${ }^{56}$ M. J. J. John, ${ }^{56}$ Ph. Leruste, ${ }^{56}$ J. Malclès, ${ }^{56}$ J. Ocariz, ${ }^{56}$ L. Roos, ${ }^{56}$ G. Therin, ${ }^{56}$ P. K. Behera, ${ }^{57}$ L. Gladney, ${ }^{57}$ Q. H. Guo, ${ }^{57}$ J. Panetta, ${ }^{57}$ M. Biasini,,${ }^{58}$ R. Covarelli, ${ }^{58}$ M. Pioppi, ${ }^{58}$ C. Angelini, ${ }^{59}$ G. Batignani, ${ }^{59}$ S. Bettarini, ${ }^{59}$ F. Bucci, ${ }^{59}$ G. Calderini, ${ }^{59}$ M. Carpinelli, ${ }^{59}$ F. Forti, ${ }^{59}$ M. A. Giorgi, ${ }^{59}$ A. Lusiani, ${ }^{59}$ G. Marchiori, ${ }^{59}$ M. Morganti, ${ }^{59}$ N. Neri, ${ }^{59}$ E. Paoloni, ${ }^{59}$ M. Rama, ${ }^{59}$ G. Rizzo, ${ }^{59}$ G. Simi, ${ }^{59}$ J. Walsh, ${ }^{59}$ M. Haire, ${ }^{60}$ D. Judd, ${ }^{60}$ K. Paick, ${ }^{60}$ D. E. Wagoner, ${ }^{60}$ J. Biesiada, ${ }^{61}$ N. Danielson, ${ }^{61}$ P. Elmer, ${ }^{61}$ Y. P. Lau, ${ }^{61}$ C. Lu, ${ }^{61}$ J. Olsen, ${ }^{61}$ A. J. S. Smith, ${ }^{61}$ A. V. Telnov, ${ }^{61}$ F. Bellini, ${ }^{62}$ G. Cavoto, ${ }^{62}$ A. D' Orazio, ${ }^{62}$ E. Di Marco, ${ }^{62}$ R. Faccini, ${ }^{62}$ F. Ferrarotto, ${ }^{62}$ F. Ferroni, ${ }^{62}$ M. Gaspero, ${ }^{62}$ L. Li Gioi, ${ }^{62}$ M. A. Mazzoni, ${ }^{62}$ S. Morganti, ${ }^{62}$ G. Piredda, ${ }^{62}$ F. Polci, ${ }^{62}$ F. Safai Tehrani, ${ }^{62}$ C. Voena, ${ }^{62}$ S. Christ, ${ }^{63}$ H. Schröder, ${ }^{63}$ G. Wagner, ${ }^{63}$ R. Waldi, ${ }^{63}$ T. Adye, ${ }^{64}$ N. De Groot, ${ }^{64}$ B. Franek, ${ }^{64}$ G. P. Gopal, ${ }^{64}$ E. O. Olaiya, ${ }^{64}$ F.F. Wilson ${ }^{64}$ R. Aleksan, ${ }^{65}$ S. Emery, ${ }^{65}$ A. Gaidot, ${ }^{65}$ S. F. Ganzhur, ${ }^{65}$ P.-F. Giraud, ${ }^{65}$ G. Graziani, ${ }^{65}$ G. Hamel de Monchenault, ${ }^{65}$ W. Kozanecki, ${ }^{65}$ M. Legendre, ${ }^{65}$ G. W. London, ${ }^{65}$ B. Mayer,,${ }^{65}$ G. Vasseur, ${ }^{65}$ Ch. Yèche, ${ }^{65}$ M. Zito, ${ }^{65}$ M. V. Purohit, ${ }^{66}$ A. W. Weidemann, ${ }^{66}$ J. R. Wilson, ${ }^{66}$ F. X. Yumiceva, ${ }^{66}$ T. Abe, ${ }^{67}$ M. T. Allen, ${ }^{67}$ D. Aston, ${ }^{67}$ R. Bartoldus, ${ }^{67}$ N. Berger, ${ }^{67}$ A. M. Boyarski, ${ }^{67}$ O. L. Buchmueller, ${ }^{67}$ R. Claus,,${ }^{67}$ M. R. Convery,${ }^{67}$ M. Cristinziani, ${ }^{67}$ J. C. Dingfelder, ${ }^{67}$ D. Dong, ${ }^{67}$ J. Dorfan, ${ }^{67}$ D. Dujmic, ${ }^{67}$ W. Dunwoodie, ${ }^{67}$ S. Fan, ${ }^{67}$ R. C. Field, ${ }^{67}$ T. Glanzman, ${ }^{67}$ S. J. Gowdy, ${ }^{67}$ T. Hadig, ${ }^{67}$ V. Halyo, ${ }^{67}$ C. Hast, ${ }^{67}$ T. Hryn'ova, ${ }^{67}$ W. R. Innes, ${ }^{67}$ S. Kazuhito, ${ }^{67}$ M. H. Kelsey, ${ }^{67}$ P. Kim, ${ }^{67}$ M. L. Kocian, ${ }^{67}$ D. W. G.S. Leith, ${ }^{67}$ J. Libby, ${ }^{67}$ S. Luitz, ${ }^{67}$ V. Luth,,${ }^{67}$ H. L. Lynch,,${ }^{67}$ H. Marsiske, ${ }^{67}$ R. Messner, ${ }^{67}$ D. R. Muller, ${ }^{67}$ C.P. O'Grady, ${ }^{67}$ V.E. Ozcan,,${ }^{67}$ A. Perazzo, ${ }^{67}$ M. Perl, ${ }^{67}$ B. N. Ratcliff,,${ }^{67}$ A. Roodman, ${ }^{67}$ A. A. Salnikov, ${ }^{67}$ R. H. Schindler, ${ }^{67}$ J. Schwiening, ${ }^{67}$ A. Snyder, ${ }^{67}$ A. Soha, ${ }^{67}$ J. Stelzer, ${ }^{67}$ J. Strube, ${ }^{54,67}$ D. Su, ${ }^{67}$ M. K. Sullivan, ${ }^{67}$ J. M. Thompson, ${ }^{67}$ J. Va'vra, ${ }^{67}$ S. R. Wagner,,${ }^{67}$ M. Weaver, ${ }^{67}$ W. J. Wisniewski, ${ }^{67}$ M. Wittgen, ${ }^{67}$ D. H. Wright, ${ }^{67}$ A. K. Yarritu, ${ }^{67}$ C. C. Young, ${ }^{67}$ P. R. Burchat, ${ }^{68}$ A. J. Edwards, ${ }^{68}$ S. A. Majewski, ${ }^{68}$ B. A. Petersen, ${ }^{68}$ C. Roat, ${ }^{68}$ M. Ahmed, ${ }^{69}$ S. Ahmed,,${ }^{69}$ M. S. Alam, ${ }^{69}$ J. A. Ernst, ${ }^{69}$ M. A. Saeed, ${ }^{69}$ M. Saleem, ${ }^{69}$ F. R. Wappler, ${ }^{69}$ W. Bugg, ${ }^{70}$ M. Krishnamurthy, ${ }^{70}$ S. M. Spanier, ${ }^{70}$ R. Eckmann, ${ }^{71}$ J. L. Ritchie, ${ }^{71}$ A. Satpathy, ${ }^{71}$ R. F. Schwitters, ${ }^{71}$ J. M. Izen, ${ }^{72}$ I. Kitayama, ${ }^{72}$ X.C. Lou, ${ }^{72}$ S. Ye, ${ }^{72}$ F. Bianchi, ${ }^{73}$ M. Bona, ${ }^{73}$ F. Gallo, ${ }^{73}$ D. Gamba, ${ }^{73}$ M. Bomben, ${ }^{74}$ L. Bosisio, ${ }^{74}$ C. Cartaro, ${ }^{74}$ F. Cossutti, ${ }^{74}$ G. Della Ricca, ${ }^{74}$ S. Dittongo, ${ }^{74}$ S. Grancagnolo, ${ }^{74}$ L. Lanceri,,${ }^{74}$ P. Poropat,,${ }^{74, *}$ L. Vitale, ${ }^{74}$ G. Vuagnin, ${ }^{74}$ F. Martinez-Vidal, ${ }^{75}$ R. S. Panvini, ${ }^{76, *}$ Sw. Banerjee, ${ }^{77}$ B. Bhuyan, ${ }^{77}$ C. M. Brown, ${ }^{77}$ D. Fortin, ${ }^{77}$
K. Hamano, ${ }^{77}$ R. Kowalewski, ${ }^{77}$ J. M. Roney, ${ }^{77}$ R. J. Sobie, ${ }^{77}$ J. J. Back, ${ }^{78}$ P. F. Harrison, ${ }^{78}$ T. E. Latham, ${ }^{78}$ G. B. Mohanty, ${ }^{78}$ H. R. Band, ${ }^{79}$ X. Chen, ${ }^{79}$ B. Cheng, ${ }^{79}$ S. Dasu, ${ }^{79}$ M. Datta, ${ }^{79}$ A. M. Eichenbaum, ${ }^{79}$ K. T. Flood, ${ }^{79}$ M. Graham, ${ }^{79}$ J. J. Hollar, ${ }^{79}$ J. R. Johnson, ${ }^{79}$ P.E. Kutter, ${ }^{79}$ H. Li, ${ }^{79}$ R. Liu, ${ }^{79}$ B. Mellado, ${ }^{79}$ A. Mihalyi, ${ }^{79}$ Y. Pan, ${ }^{79}$ R. Prepost, ${ }^{79}$ P. Tan, ${ }^{79}$ J. H. von Wimmersperg-Toeller, ${ }^{79}$ J. Wu, ${ }^{79}$ S.L. Wu, ${ }^{79}$ Z. Yu, ${ }^{79}$ M. G. Greene, ${ }^{80}$ and H. Neal ${ }^{80}$
(BABAR Collaboration)

[^0]${ }^{20}$ University of Cincinnati, Cincinnati, Ohio 45221, USA<br>${ }^{21}$ University of Colorado, Boulder, Colorado 80309, USA<br>${ }^{22}$ Colorado State University, Fort Collins, Colorado 80523, USA<br>${ }^{23}$ Universität Dortmund, Institut fur Physik, D-44221 Dortmund, Germany<br>${ }^{24}$ Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany<br>${ }^{25}$ Ecole Polytechnique, LLR, F-91128 Palaiseau, France<br>${ }^{26}$ University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom<br>${ }^{27}$ Università di Ferrara, Dipartimento di Fisica and INFN, I-44100 Ferrara, Italy<br>${ }^{28}$ Laboratori Nazionali di Frascati dell'INFN, I-00044 Frascati, Italy<br>${ }^{29}$ Università di Genova, Dipartimento di Fisica and INFN, I-16146 Genova, Italy<br>${ }^{30}$ Harvard University, Cambridge, Massachusetts 02138, USA<br>${ }^{31}$ Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany<br>${ }^{32}$ Imperial College London, London SW7 2AZ, United Kingdom<br>${ }^{33}$ University of Iowa, Iowa City, Iowa 52242, USA<br>${ }^{34}$ Iowa State University, Ames, Iowa 50011-3160, USA<br>${ }^{35}$ Laboratoire de l'Accélérateur Linéaire, F-91898 Orsay, France<br>${ }^{36}$ Lawrence Livermore National Laboratory, Livermore, California 94550, USA<br>${ }^{37}$ University of Liverpool, Liverpool L69 72E, United Kingdom<br>${ }^{38}$ Queen Mary, University of London, London E1 4NS, United Kingdom<br>${ }^{39}$ University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom<br>${ }^{40}$ University of Louisville, Louisville, Kentucky 40292, USA<br>${ }^{41}$ University of Manchester, Manchester M13 9PL, United Kingdom<br>${ }^{42}$ University of Maryland, College Park, Maryland 20742, USA<br>${ }^{43}$ University of Massachusetts, Amherst, Massachusetts 01003, USA<br>${ }^{44}$ Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA<br>${ }^{45}$ McGill University, Montréal, Québec, Canada H3A 2T8<br>${ }^{46}$ Università di Milano, Dipartimento di Fisica and INFN, I-20133 Milano, Italy<br>${ }^{47}$ University of Mississippi, University, Mississippi 38677, USA<br>${ }^{48}$ Université de Montréal, Laboratoire René J. A. Lévesque, Montréal, Québec, Canada H3C $3 J 7$<br>${ }^{49}$ Mount Holyoke College, South Hadley, Massachusetts 01075, USA<br>${ }^{50}$ Università di Napoli Federico II, Dipartimento di Scienze Fisiche and INFN, I-80126, Napoli, Italy<br>${ }^{51}$ NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands<br>${ }^{52}$ University of Notre Dame, Notre Dame, Indiana 46556, USA<br>${ }^{53}$ The Ohio State University, Columbus, Ohio 43210, USA<br>${ }^{54}$ University of Oregon, Eugene, Oregon 97403, USA<br>${ }^{55}$ Università di Padova, Dipartimento di Fisica and INFN, I-35131 Padova, Italy<br>${ }^{56}$ Universités Paris VI et VII, Laboratoire de Physique Nucléaire et de Hautes Energies, F-75252 Paris, France<br>${ }^{57}$ University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA<br>${ }^{58}$ Università di Perugia, Dipartimento di Fisica and INFN, I-06100 Perugia, Italy<br>${ }^{59}$ Università di Pisa, Dipartimento di Fisica, Scuola Normale Superiore and INFN, I-56127 Pisa, Italy<br>${ }^{60}$ Prairie View A\&M University, Prairie View, Texas 77446, USA<br>${ }^{61}$ Princeton University, Princeton, New Jersey 08544, USA<br>${ }^{62}$ Università di Roma La Sapienza, Dipartimento di Fisica and INFN, I-00185 Roma, Italy<br>${ }^{63}$ Universität Rostock, D-18051 Rostock, Germany<br>${ }^{64}$ Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom<br>${ }^{65}$ DSM/Dapnia, CEA/Saclay, F-91191 Gif-sur-Yvette, France<br>${ }^{66}$ University of South Carolina, Columbia, South Carolina 29208, USA<br>${ }^{67}$ Stanford Linear Accelerator Center, Stanford, California 94309, USA<br>${ }^{68}$ Stanford University, Stanford, California 94305-4060, USA<br>${ }^{69}$ State University of New York, Albany, New York 12222, USA<br>${ }^{70}$ University of Tennessee, Knoxville, Tennessee 37996, USA<br>${ }^{71}$ University of Texas at Austin, Austin, Texas 78712, USA<br>${ }^{72}$ University of Texas at Dallas, Richardson, Texas 75083, USA<br>${ }^{73}$ Università di Torino, Dipartimento di Fisica Sperimentale and INFN, I-10125 Torino, Italy<br>${ }^{74}$ Università di Trieste, Dipartimento di Fisica and INFN, I-34127 Trieste, Italy<br>${ }^{75}$ IFIC, Universitat de Valencia-CSIC, E-46071 Valencia, Spain<br>${ }^{76}$ Vanderbilt University, Nashville, Tennessee 37235, USA<br>${ }^{77}$ University of Victoria, Victoria, British Columbia, Canada V8W 3P6<br>${ }^{78}$ Department of Physics, University of Warwick, Coventry CV4 7AL, United Kingdom<br>${ }^{79}$ University of Wisconsin, Madison, Wisconsin 53706, USA<br>${ }^{80}$ Yale University, New Haven, Connecticut 06511, USA


#### Abstract

We present results from an analysis of $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$using $232 \times 10^{6} \Upsilon(4 S) \rightarrow B \bar{B}$ decays collected with the $B A B A R$ detector at the PEP-II asymmetric-energy $B$ factory at SLAC. We measure the longitudinal polarization fraction $f_{L}=0.978 \pm 0.014$ (stat) ${ }_{-0.029}^{+0.021}$ (syst) and the $C P$-violating parameters $S_{L}=-0.33 \pm 0.24(\text { stat })_{-0.14}^{+0.08}$ (syst) and $C_{L}=-0.03 \pm 0.18$ (stat) $\pm 0.09$ (syst). Using an isospin analysis of $B \rightarrow \rho \rho$ decays, we determine the unitarity triangle parameter $\alpha$. The solution compatible with the standard model is $\alpha=(100 \pm 13)^{\circ}$.


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In the standard model, $C P$-violating effects in the $B$-meson system arise from a single phase in the Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix [1]. Interference between direct decay and decay after $B^{0} \bar{B}^{0}$ mixing in $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$results in a timedependent decay-rate asymmetry that is sensitive to the angle $\alpha \equiv \arg \left[-V_{t d} V_{t b}^{*} / V_{u d} V_{u b}^{*}\right]$ in the unitarity triangle of the CKM matrix. This decay proceeds mainly through a $b \rightarrow u \bar{u} d$ tree diagram. The presence of penguin loop contributions introduces additional phases that shift the experimentally measurable parameter $\alpha_{\text {eff }}$ away from the value of $\alpha$. However, measurements of the $B^{+} \rightarrow \rho^{+} \rho^{0}$ branching fraction and the upper limit for $B^{0} \rightarrow \rho^{0} \rho^{0}[2,3]$ show that the penguin contribution in $B \rightarrow \rho \rho$ is small with respect to the leading tree diagram, and $\delta \alpha_{\rho \rho}=$ $\alpha_{\text {eff }}-\alpha$ is constrained at $\pm 11^{\circ}$ at $1 \sigma$ [3]. This Letter presents an update of the time-dependent analysis of $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$and measurement of the CKM angle $\alpha$ reported in [4].

The $C P$ analysis of $B$ decays to $\rho^{+} \rho^{-}$is complicated by the presence of a mode with longitudinal polarization and two with transverse polarizations. The longitudinal mode is $C P$ even, while the transverse modes contain $C P$-even and $C P$-odd states. Empirically, the decay is observed to be dominated by the longitudinal polarization [4], with a fraction $f_{L}$ defined by the fraction of the helicity zero state in the decay. The angular distribution is

$$
\begin{align*}
\frac{d^{2} \Gamma}{\Gamma d \cos \theta_{1} d \cos \theta_{2}}= & \frac{9}{4}\left[f_{L} \cos ^{2} \theta_{1} \cos ^{2} \theta_{2}\right. \\
& \left.+\frac{1}{4}\left(1-f_{L}\right) \sin ^{2} \theta_{1} \sin ^{2} \theta_{2}\right], \tag{1}
\end{align*}
$$

where $\theta_{i=1,2}$ is the angle between the $\pi^{0}$ momentum and the direction opposite the $B^{0}$ in the $\rho$ rest frame, and we have integrated over the angle between the $\rho$ decay planes.

The analysis reported here is improved over our earlier publication [4] by a change in selection requirements resulting in an increased signal efficiency, introduction of a signal time dependence that accounts for possible misreconstruction, and use of a more detailed background model. This measurement uses $232 \times 10^{6} \mathrm{Y}(4 S) \rightarrow B \bar{B}$ decays collected with the BABAR [5] detector at the PEPII asymmetric-energy $B$ factory at SLAC.

We reconstruct $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$candidates $\left(B_{\mathrm{rec}}\right)$ from combinations of two charged tracks and two $\pi^{0}$ candidates.

We require that both tracks have particle identification information inconsistent with the electron, kaon, and proton hypotheses. The $\pi^{0}$ candidates are formed from pairs of photons, each of which has a measured energy greater than 50 MeV . The reconstructed $\pi^{0}$ mass must satisfy $0.10<m_{\gamma \gamma}<0.16 \mathrm{GeV} / c^{2}$. The mass of the $\rho$ candidates must satisfy $0.5<m_{\pi^{ \pm} \pi^{0}}<1.0 \mathrm{GeV} / c^{2}$. When multiple $B$ candidates can be formed, we select the one that minimizes the sum of $\left(m_{\gamma \gamma}-m_{\pi^{0}}\right)^{2}$ where $m_{\pi^{0}}$ is the true $\pi^{0}$ mass. If more than one candidate has the same $\pi^{0}$ mesons, we select one at random.

Combinatorial backgrounds dominate near $\left|\cos \theta_{i}\right|=1$, and backgrounds from $B$ decays tend to concentrate at negative values of $\cos \theta_{i}$. We reduce these backgrounds with the requirement $-0.90<\cos \theta_{i}<0.98$.

Continuum $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s, c)$ events are the dominant background. This background is reduced by requiring that $\left|\cos B_{T R}\right|<0.8$, where $B_{T R}$ is the angle between the $B$ thrust axis and that of the rest of the event, ROE. The thrust axis of the $B$ is the direction that maximizes the longitudinal momenta of the particles in the $B$ candidate. To distinguish signal from continuum we use a neural network $(\mathcal{N})$ to combine ten discriminating variables: the event shape variables that are used in the Fisher discriminant in Ref. [6], the cosine of the angle between the direction of the $B$ and the collision axis $(z)$ in the $e^{+} e^{-}$ center-of-mass (c.m.) frame, the cosine of the angle between the $B$ thrust axis and the $z$ axis, $\left|\cos B_{T R}\right|$, the decay angle of each $\pi^{0}$ (defined in analogy to the $\rho$ decay angle, $\theta_{i}$ ), and the sum of transverse momenta in the ROE relative to the $z$ axis.

Signal events are identified kinematically using two variables, the difference $\Delta E$ between the c.m. energy of the $B$ candidate and $\sqrt{s} / 2$, and the beam-energysubstituted mass $m_{\mathrm{ES}}=\sqrt{\left(s / 2+\mathbf{p}_{i} \cdot \mathbf{p}_{B}\right)^{2} / E_{i}^{2}-\mathbf{p}_{B}^{2}}$, where $\sqrt{s}$ is the total c.m. energy. The $B$ momentum $\mathbf{p}_{B}$ and four-momentum of the initial state $\left(E_{i}, \mathbf{p}_{i}\right)$ are defined in the laboratory frame. We accept candidates that satisfy $5.23<m_{\mathrm{ES}}<5.29 \mathrm{GeV} / c^{2} \quad$ and $\quad-0.12<\Delta E<$ 0.15 GeV . The asymmetric $\Delta E$ selection reduces background from higher-multiplicity $B$ decays.

To study the time-dependent asymmetry, one needs to measure the proper-time difference, $\Delta t$, between the two $B$ decays in the event, and to determine the flavor of the other $B$ meson ( $B_{\text {tag }}$ ). We calculate $\Delta t$ from the measured sepa-
ration $\Delta z$ between the $B_{\text {rec }}$ and $B_{\text {tag }}$ decay vertices [7]. We determine the $B_{\text {rec }}$ vertex from the two charged-pion tracks in its decay. The $B_{\text {tag }}$ decay vertex is obtained by fitting the other tracks in the event, with constraints from the $B_{\text {rec }}$ momentum and the beam-spot location. The rms resolution on $\Delta t$ is 1.1 ps . We use only events that satisfy $|\Delta t|<$ 20 ps and for which the error on $\Delta t$ less than 2.5 ps . The flavor of the $B_{\text {tag }}$ meson is determined with a multivariate technique [6] that has a total effective tagging efficiency of $(29.9 \pm 0.5) \%$.

Signal candidates may pass the selection requirement even if one or more of the pions assigned to the $\rho^{+} \rho^{-}$state belongs to the other $B$ in the event. These self-cross-feed (SCF) candidates constitute $50 \%(26 \%)$ of the accepted signal for $f_{L}=1\left(f_{L}=0\right)$. The majority of SCF events have both charged pions from the $\rho^{+} \rho^{-}$final state, and unbiased $C P$ information (correct-track SCF). There is a SCF component ( $14 \%$ of the signal) where at least one track in $B_{\text {rec }}$ is from the rest of the event. These wrongtrack events have biased $C P$ information, and are treated separately for the $C P$ result. The probability density function (PDF) describing wrong-track events is used only in determining the signal yield and polarization. A systematic error is assigned to the $C P$ results from this type of signal event.

We obtain a sample of 68703 events that enter a maximum-likelihood fit. These events are dominated by backgrounds: roughly $92 \%$ from $q \bar{q}$ and $7 \%$ from $B \bar{B}$ events. The remaining $1 \%$ of events is signal. We distinguish the following candidate types: (i) correctly reconstructed signal; (ii) SCF signal, split into correct and wrong-track parts; (iii) charm $B^{ \pm}$background $(b \rightarrow c)$; (iv) charm $B^{0}$ background $(b \rightarrow c)$; (v) charmless $B$ backgrounds; and (vi) continuum background. The dominant charmless backgrounds are $B$ decays to $\rho \pi,\left(a_{1} \pi\right)^{ \pm}$, $\left(a_{1} \pi\right)^{0}$, and longitudinally polarized $a_{1} \rho$ final states. For these decays we use the inclusive branching fractions (in units of $10^{-6}$ ), $34 \pm 4$ [8], $42 \pm 42,42 \pm 6$ [9], and $100 \pm$ 100 , respectively. The corresponding expected number of events in the sample are $82 \pm 13,87 \pm 87,65 \pm 9$, and $202 \pm 202$. We also account for contributions from higher kaon resonances ( $112 \pm 112$ events) and $\rho^{+} \rho^{0}(82 \pm 19$ events). In addition, we expect $2551 \pm 510(1316 \pm 263)$ charged (neutral) $B$ decays to final states containing charm mesons. The $B$-background decays are included as separate components in the fit.

Each candidate is described with the eight $B_{\text {rec }}$ kinematic variables: $m_{\mathrm{ES}}, \Delta E$, the $m_{\pi^{ \pm}} \pi^{0}$ and $\cos \theta_{i}$ values of the two $\rho$ mesons, $\Delta t$, and $\mathcal{N}$. For each fit component, we construct a PDF that is the product of PDFs for these variables, neglecting correlations. This introduces a fit bias that is corrected with the use of Monte Carlo (MC) simulation. The continuum-background yield and its PDF parameters for $m_{\mathrm{ES}}, \Delta E, \cos \theta_{i}$, and $\mathcal{N}$ are floated in the fit to data. The continuum $m_{\pi^{ \pm} \pi^{0}}$ distribution is described by
a Breit-Wigner and polynomial shape, and is derived from $m_{\mathrm{ES}}$ and $\Delta E$ data sidebands. For all other fit components the PDFs are extracted from high-statistics MC samples. The $\cos \theta_{i}$ distributions for the background are described by a nonparametric (NP) PDF derived from the MC samples, as the detector acceptance and selection modify the known vector-meson decay distribution. The true signal distribution is given by Eq. (1) multiplied by an acceptance function determined from signal MC samples, whereas SCF signal is modeled using NP PDFs.

The signal decay-rate distribution for both polarizations $f_{+}\left(f_{-}\right)$for $B_{\text {tag }}=B^{0}\left(\bar{B}^{0}\right)$ is given by

$$
f_{ \pm}(\Delta t)=\frac{e^{-|\Delta t| / \tau}}{4 \tau}\left[1 \pm S \sin \left(\Delta m_{d} \Delta t\right) \mp C \cos \left(\Delta m_{d} \Delta t\right)\right]
$$

where $\tau$ is the mean $B^{0}$ lifetime, $\Delta m_{d}$ is the $B^{0} \bar{B}^{0}$ mixing frequency, and $S=S_{L}$ or $S_{T}$ and $C=C_{L}$ or $C_{T}$ are the $C P$-asymmetry parameters for the longitudinally and transversely polarized signal. The parameters $S$ and $C$ describe $B$-mixing-induced and direct $C P$ violation, respectively. $S$ and $C$ for the longitudinally polarized wrong-track signal are fixed to zero. The $\Delta t$ PDF takes into account incorrect tags and is convolved with the resolution function described below. Since $f_{L}$ is approximately 1 , the fit has no sensitivity to either $S_{T}$ or $C_{T}$. We set these parameters to zero and vary them in the evaluation of systematic uncertainties.

The signal $\Delta t$ resolution function consists of three Gaussians $(\sim 90 \%$ core, $\sim 9 \%$ tail, $\sim 1 \%$ outliers), and takes into account the per-event error on $\Delta t$ from the vertex fit. The resolution is parametrized using a large sample of fully reconstructed hadronic $B$ decays [7]. For wrong-track SCF we replace the $B$-meson lifetime by an effective lifetime obtained from MC simulation to account for the difference in the resolution. The nominal $\Delta t$ distribution for the $B$ backgrounds is a NP representation of the MC samples; in the study of systematic errors we replace this model with the one used for signal. The resolution for continuum background is described by the sum of three Gaussian distributions whose parameters are determined from data.

We perform an unbinned extended maximum-likelihood fit. The results of the fit are $617 \pm 52$ signal events, after correction of a 68 event fit bias, with $f_{L}=0.978 \pm 0.014$, $S_{L}=-0.33 \pm 0.24$, and $C_{L}=-0.03 \pm 0.18$. The measured signal yield, polarization, and $C P$ parameters are in agreement with our earlier publication [4], with significantly improved precision. Figure 1 shows distributions of $m_{\mathrm{ES}}, \Delta E, \cos \theta_{i}$, and $m_{\pi^{ \pm} \pi^{0}}$ for the highest purity tagged events with a loose requirement on $\mathcal{N}$. The plot of $m_{\text {ES }}$ contains $14 \%$ of the signal and $1.5 \%$ of the background. For the other plots there is an added constraint that $m_{\mathrm{ES}}>$ $5.27 \mathrm{GeV} / c^{2}$; these requirements retain $11.5 \%$ of the signal and $0.4 \%$ of the background. Figure 2 shows the $\Delta t$ distribution for $B^{0}$ and $\bar{B}^{0}$ tagged events. The time-


FIG. 1 (color online). The distributions for the highest purity tagged events for the variables (a) $m_{\mathrm{ES}}$, (b) $\Delta E$, (c) cosine of the $\rho$ helicity angle, and (d) $m_{\pi^{ \pm} \pi^{0}}$. The dotted lines are the sum of backgrounds, and the solid lines are the full PDF.
dependent decay-rate asymmetry $\quad[N(\Delta t)-\bar{N}(\Delta t)] /$ $[N(\Delta t)+\bar{N}(\Delta t)]$ is also shown, where $N(\bar{N})$ is the decay rate for $B^{0}\left(\bar{B}^{0}\right)$ tagged events.

We have studied possible sources of systematic uncertainties on $f_{L}, S_{L}$, and $C_{L}$. The dominant uncertainties for $f_{L}$ come from floating the $B$ background yields $\left({ }_{-0.02}^{+0.00}\right)$, nonresonant events ( 0.015 ), and fit bias ( 0.01 ). The dominant systematic uncertainty on the $C P$ results comes from the uncertainty in the $B$-background branching ratios. This results in a shift on $S_{L}\left(C_{L}\right)$, as large as ${ }_{-0.12}^{+0.00}\left({ }_{-0.003}^{+0.008}\right)$. Additional uncertainties on the $C P$ results come from possible $C P$ violation in the $B$ background, calculated as


FIG. 2. The $\Delta t$ distribution for a sample of events enriched in signal for (a) $B^{0}$ and (b) $\bar{B}^{0}$ tagged events. The dotted lines are the sum of backgrounds, and the solid lines are the sum of signal and backgrounds. The time-dependent $C P$ asymmetry (see text) is shown in (c), where the curve is the measured asymmetry.
in Ref. [4]. We allow for a $C P$ asymmetry up to $20 \%$ in $B$ decays to final states with charm, resulting in an uncertainty of $0.027(0.045)$ on $S_{L}\left(C_{L}\right)$. Allowing for possible $C P$ violation in the transverse polarization results in an uncertainty of $0.02\left({ }_{-0.016}^{+0.002}\right)$ on $S_{L}\left(C_{L}\right)$. We estimate the systematic error on our $C P$ results from neglecting the interference between $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$and other $4 \pi$ final states: $B \rightarrow a_{1} \pi, \rho \pi \pi^{0}$, and $B \rightarrow \pi \pi \pi^{0} \pi^{0}$. Strong phases and $C P$ content of the interfering states are varied between zero and maximum using uniform prior distributions, and the rms deviation of the parameters from the nominal fit is taken as the systematic error; this is found to be 0.02 on $S_{L}$ and $C_{L}$. Other contributions that are large include knowledge of the vertex detector alignment 0.034 ( 0.005 ) on $S_{L}\left(C_{L}\right)$, and possible $C P$ violation in the doubly Cabibbo-suppressed decays on the tag side of the event [10]. We allow $C P$ violation in the wrong-track SCF to vary between -1 and +1 , which results in changes of 0.007 (0.012) in $S_{L}\left(C_{L}\right)$. The nominal fit does not account for nonresonant background. If we add a nonresonant component of $B \rightarrow \rho \pi \pi^{0}$ events to the likelihood, we fit $83 \pm 59$ nonresonant events and observe only a $(6 \pm 4) \%$ drop in signal yield. This effect is included in our total systematic uncertainty. Possible contributions from $\sigma(400) \pi^{0} \pi^{0}$ decays are neglected due to the small reconstruction efficiency ( $0.4 \%$ ). Our results are

$$
\begin{aligned}
& f_{L}=0.978 \pm 0.014(\text { stat }) \\
& \begin{array}{l}
+0.021 \\
-0.029
\end{array}(\text { syst }) \\
&+0.08 \\
& S_{L}=-0.33 \pm 0.24(\text { stat }) \\
&-0.14 \\
& C_{L}=-0.03 \pm 0.18(\text { systat }) \\
& \pm 0.09(\text { syst })
\end{aligned}
$$

where the correlation between $S_{L}$ and $C_{L}$ is -0.042 .
We constrain the CKM angle $\alpha$ from an isospin analysis [11] of $B \rightarrow \rho \rho$. The inputs to the isospin analysis are the amplitudes of the $C P$-even longitudinal polarization of the $\rho \rho$ final state, as well as the measured values of $S_{L}$ and $C_{L}$ for $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$. We use the measurements of $f_{L}, S_{L}$, and $C_{L}$ presented here, the branching fraction of $B^{0} \rightarrow$ $\rho^{+} \rho^{-}$from [4], which uses information from [12], the


FIG. 3 (color online). C.L. on $\alpha$ obtained from the isospin analysis with the statistical method described in [15]. The dashed lines correspond to the $68 \%$ (top) and $90 \%$ (bottom) C.L. intervals.
combined branching fraction and $f_{L}$ for $B \rightarrow \rho^{+} \rho^{0}$ from Ref. [2], and the central value corresponding to the upper limit of $\mathcal{B}\left(B \rightarrow \rho^{0} \rho^{0}\right)$ from Ref. [3]. We ignore electroweak penguins and possible $I=1$ amplitudes [13].

To interpret our results in terms of a constraint on $\alpha$ from the isospin relations, we construct a $\chi^{2}$ that includes the measured quantities expressed as the lengths of the sides of the isospin triangles, and we determine the minimum $\chi_{0}^{2}$. As the isospin triangles do not close with the current central values of the branching ratios, we have adopted toy MC techniques to compute the confidence level (C.L.) on $\alpha$; our method is similar to the approach proposed in Ref. [14]. For each value of $\alpha$, scanned between $0^{\circ}$ and $180^{\circ}$, we determine the difference $\Delta \chi_{\text {DATA }}^{2}(\alpha)$ between the minimum of $\chi^{2}(\alpha)$ and $\chi_{0}^{2}$. We then generate MC experiments around the central values obtained from the fit to data with the given value of $\alpha$, and we apply the same procedure. The fraction of these experiments in which $\Delta \chi_{\mathrm{MC}}^{2}(\alpha)$ is smaller than $\Delta \chi_{\mathrm{DATA}}^{2}(\alpha)$ is interpreted as the C.L. on $\alpha$. Figure 3 shows $1-\mathrm{C} . L$. for $\alpha$ obtained from this method. Selecting the solution closest to the CKM combined fit average $[15,16]$, we find $\alpha=100^{\circ} \pm 13^{\circ}$, where the error is dominated by $\delta \alpha_{\rho \rho}$ which is $\pm 11^{\circ}$ at $1 \sigma$. The $90 \%$ C.L. allowed interval for $\alpha$ is between $79^{\circ}$ and $123^{\circ}$.

In summary, we have improved the measurement of the $C P$-violating parameters $S_{L}$ and $C_{L}$ in $B^{0}\left(\bar{B}^{0}\right) \rightarrow \rho^{+} \rho^{-}$ using a data sample 2.6 times larger than that in Ref. [4]. We do not observe mixing-induced or direct $C P$ violation. We derive a model-independent measurement of the CKM angle $\alpha$, which is the most precise to date.

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*Also with Università della Basilicata, Potenza, Italy. ${ }^{\dagger}$ Deceased.
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[^0]:    ${ }^{1}$ Laboratoire de Physique des Particules, F-74941 Annecy-le-Vieux, France
    ${ }^{2}$ IFAE, Universitat Autonoma de Barcelona, E-08193 Bellaterra, Barcelona, Spain
    ${ }^{3}$ Università di Bari, Dipartimento di Fisica and INFN, I-70126 Bari, Italy
    ${ }^{4}$ Institute of High Energy Physics, Beijing 100039, China
    ${ }^{5}$ University of Bergen, Institute of Physics, N-5007 Bergen, Norway
    ${ }^{6}$ Lawrence Berkeley National Laboratory and University of California, Berkeley, California 94720, USA
    ${ }^{7}$ University of Birmingham, Birmingham, B15 2TT, United Kingdom
    ${ }^{8}$ Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany
    ${ }^{9}$ University of Bristol, Bristol BS8 1TL, United Kingdom
    ${ }^{10}$ University of British Columbia, Vancouver, British Columbia, Canada V6T 1Z1
    ${ }^{11}$ Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom
    ${ }_{13}^{12}$ Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia
    ${ }^{13}$ University of California at Irvine, Irvine, California 92697, USA
    ${ }^{14}$ University of California at Los Angeles, Los Angeles, California 90024, USA
    ${ }^{15}$ University of California at Riverside, Riverside, California 92521, USA
    ${ }^{16}$ University of California at San Diego, La Jolla, California 92093, USA
    ${ }^{17}$ University of California at Santa Barbara, Santa Barbara, California 93106, USA
    ${ }^{18}$ University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, California 95064, USA
    ${ }^{19}$ California Institute of Technology, Pasadena, California 91125, USA

