## Improved measurements of the branching fractions for $B^{0} \rightarrow \pi^{+} \boldsymbol{\pi}^{-}$and $B^{0} \rightarrow K^{+} \boldsymbol{\pi}^{-}$, and a search for $\boldsymbol{B}^{\mathbf{0}} \rightarrow \boldsymbol{K}^{+} \boldsymbol{K}^{-}$

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We present measurements of the branching fractions for the charmless two-body decays $B^{0} \rightarrow \pi^{+} \pi^{-}$ and $B^{0} \rightarrow K^{+} \pi^{-}$, and a search for the decay $B^{0} \rightarrow K^{+} K^{-}$. We include the effects of final-state radiation from the daughter mesons for the first time, and quote branching fractions for the inclusive processes $B^{0} \rightarrow h^{+} h^{\prime-} n \gamma$, where $h$ and $h^{\prime}$ are pions or kaons. The maximum value of the sum of the energies of the $n$ undetected photons, $E_{\gamma}^{\max }$, is mode-dependent. Using a data sample of approximately $227 \times 10^{6}$ $Y(4 S) \rightarrow B \bar{B}$ decays collected with the BABAR detector at the PEP-II asymmetric-energy $e^{+} e^{-}$collider at SLAC, we measure: $\mathcal{B}\left(B^{0} \rightarrow \pi^{+} \pi^{-} n \gamma ; E_{\gamma}^{\max }=150 \mathrm{MeV}\right)=(5.1 \pm 0.4 \pm 0.2) \times 10^{-6}, \quad \mathcal{B}\left(B^{0} \rightarrow\right.$ $\left.K^{+} \pi^{-} n \gamma ; E_{\gamma}^{\max }=105 \mathrm{MeV}\right)=(18.1 \pm 0.6 \pm 0.6) \times 10^{-6}, \mathcal{B}\left(B^{0} \rightarrow K^{+} K^{-} n \gamma ; E_{\gamma}^{\max }=59 \mathrm{MeV}\right)<0.5 \times$ $10^{-6}(90 \%$ confidence level), where the first uncertainty is statistical and the second is systematic. Theoretical calculations can be used to extrapolate from the above measurements the nonradiative branching fractions, $\mathcal{B}^{0}$. Using one such calculation, we find: $\mathcal{B}^{0}\left(B^{0} \rightarrow \pi^{+} \pi^{-}\right)=(5.5 \pm 0.4 \pm 0.3) \times 10^{-6}, \mathcal{B}^{0}\left(B^{0} \rightarrow\right.$ $\left.K^{+} \pi^{-}\right)=(19.1 \pm 0.6 \pm 0.6) \times 10^{-6}, \quad \mathcal{B}^{0}\left(B^{0} \rightarrow K^{+} K^{-}\right)<0.5 \times 10^{-6}(90 \%$ confidence level $)$. Meaningful comparison between theory and experiment, as well as combination of measurements from different experiments, can be performed only in terms of these nonradiative quantities.

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Charmless hadronic two-body $B$ decays to pions and kaons provide a wealth of information on $C P$ violation in the $B$ system, including all angles of the unitarity triangle. The time-dependent $C P$ asymmetries in the $\pi \pi$ system can be used to estimate the angle $\alpha$ [1]; the decay rates for the $K \pi$ channels provide information on $\gamma$ [2]. Recently, direct $C P$ violation in decay was established in the $B$ system through observation of a significant rate asymmetry between $B^{0} \rightarrow K^{+} \pi^{-}$and $\bar{B}^{0} \rightarrow K^{-} \pi^{+}$decays [3,4]. As $B$ physics experiments accumulate much larger data sets, charmless two-body $B$ decays will continue to play a fundamental role in testing the standard model description of $C P$ violation. Measurements of branching fractions for all the charmless two-body decays are invaluable in testing the various theoretical approaches to the underlying hadron dynamics [5]. We present measurements of branching fractions for the decays $B^{0} \rightarrow \pi^{+} \pi^{-}$and $K^{+} \pi^{-}$[6], and a search for the decay $B^{0} \rightarrow K^{+} K^{-}$using a data sample about 2.5 times larger than that used for the most precise, previously published measurements [7-9] of these quantities.

As radiative corrections have already proved to be important in precise determinations of interesting quantities in the context of kaon physics [10], we account for them in this analysis as well. We can relate the observable decay rates $\Gamma_{h h^{\prime}}\left(E_{\gamma}^{\max }\right)$ for $B^{0} \rightarrow h^{+} h^{\prime-} n \gamma$ (and thus the branching fractions) to the theoretical nonradiative widths $\Gamma_{h h^{\prime}}^{0}$, using the energy-dependent correction factors $G_{h h^{\prime}}\left(E_{\gamma}^{\max } ; \mu\right)$ [11]

$$
\begin{align*}
\Gamma_{h h^{\prime}}\left(E_{\gamma}^{\max }\right) & =\left.\Gamma\left(B^{0} \rightarrow h^{+} h^{-} n \gamma\right)\right|_{h E_{\gamma}<E_{\gamma}^{\max }} \\
& =\Gamma_{h h^{\prime}}^{0}(\mu) G_{h h^{\prime}}\left(E_{\gamma}^{\max } ; \mu\right), \tag{1}
\end{align*}
$$

where $E_{\gamma}^{\text {max }}$ is the maximum value allowed for the sum of the undetected photon energies and $\mu$ is the renormalization scale at which $\Gamma_{h h^{\prime}}^{0}$ and $G_{h h^{\prime}}\left(E_{\gamma}^{\max }\right)$ are calculated (the
product being independent of $\mu)$. Extracting $\Gamma_{h h^{\prime}}^{0}$ allows a more meaningful comparison with theoretical calculations and also between different experimental results. Additionally, for $E_{\gamma}^{\max }$ at the kinematic limit, $G$ approaches unity (to order $\alpha_{\mathrm{QED}} / \pi$ ), so that the $\Gamma_{h h^{\prime}}^{0}$, and the corresponding branching fractions, can be interpreted theoretically in a cleaner way.

The data sample used for this analysis contains (226.6 $\pm$ $2.5) \times 10^{6} Y(4 S) \rightarrow B \bar{B}$ decays collected by the $B A B A R$ detector [12] at the SLAC PEP-II $e^{+} e^{-}$asymmetric-energy storage ring. The primary detector components used in the analysis are a charged-particle tracking system consisting of a five-layer silicon vertex detector and a 40-layer drift chamber surrounded by a $1.5-\mathrm{T}$ solenoidal magnet, an electromagnetic calorimeter comprising $6580 \mathrm{CsI}(\mathrm{Tl})$ crystals, and a dedicated particle-identification system consisting of a detector of internally reflected Cherenkov light providing at least $3 \sigma K-\pi$ separation over the range of laboratory momentum relevant for this study (1.5-4.5 GeV/c).

The data sample used in this analysis is similar to that used in the $B A B A R$ measurements of direct $C P$ violation in $B^{0} \rightarrow K^{+} \pi^{-}$[3] and time-dependent $C P$-violating asymmetry amplitudes $S_{\pi \pi}$ and $C_{\pi \pi}$ in $B^{0} \rightarrow \pi^{+} \pi^{-}$[13] (the reader is referred to those references for further details of the analysis technique). Event selection criteria are identical to those used in the $C P$ analyses [3,13], except that we remove the requirement on the difference in the decay times $(\Delta t)$ between the two $B$ mesons in order to minimize systematic uncertainties on the branching fraction measurements.

We identify $B^{0} \rightarrow h^{+} h^{\prime-}\left(h, h^{\prime}=\pi\right.$ or $\left.K\right)$ candidates with selection requirements on track and Cherenkov angle $\left(\theta_{c}\right)$ quality, $B$ decay kinematic variables, and event topology. The final sample contains 69264 events and is defined by requirements on two kinematic variables: (1) the dif-
ference $\Delta E=E_{B}^{*}-\sqrt{s} / 2$ between the reconstructed energy of the $B$ candidate in the $e^{+} e^{-}$center-of-mass (CM) frame and $\sqrt{s} / 2$; and (2) the beam-energy substituted mass $m_{\mathrm{ES}}=\sqrt{\left(s / 2+\mathbf{p}_{i} \cdot \overline{\mathbf{p}}_{\mathbf{B}}\right)^{2} / E_{i}^{2}-\mathbf{p}_{\mathbf{B}}^{2}}$. Here, $\sqrt{s}$ is the total CM energy, and the $B$ momentum $\mathbf{p}_{\mathbf{B}}$ and the fourmomentum $\left(E_{i}, \mathbf{p}_{\mathbf{i}}\right)$ of the $e^{+} e^{-}$initial state are defined in the laboratory frame. To simplify the analysis, we use the pion mass for all tracks in the track reconstruction and the calculation of the kinematic variables. We select those $B$ candidates with $|\Delta E|<150 \mathrm{MeV}$, and $5.20<m_{\mathrm{ES}}<$ $5.29 \mathrm{GeV} / c^{2}$.

The efficiencies of the selection criteria are determined in samples of GEANT-4 based [14] Monte Carlo (MC) simulated signal decays, where we include the effects of electromagnetic radiation from the final-state charged particles using the PHOTOS simulation package [15].

We compare the performance of our simulation with a scalar QED calculation [11] resummed to all orders of $\alpha_{\text {QED }}$. Among events selected by the $|\Delta E|<150 \mathrm{MeV}$ requirement, the MC simulation and Ref. [11] predict different fractions of events with photons with energy below 2.6 MeV , the soft photon energy cut-off used in our simulation (see Table I). We therefore reweight the $\Delta E$ distributions for each mode to account for this different fraction of radiating events and use these reweighted distributions in the final maximum-likelihood fit. The difference in event yields obtained with the original distributions and with the reweighted ones is used to evaluate the associated systematic error, and it is found to be negligible.

As explained in Ref. [11], while taking into account radiative corrections, one needs to be careful to quote the results in such a way that the radiation effects can be disentangled. In principle, it would be necessary to select $B$ candidates with a specified maximum amount of $\mathcal{O}(100 \mathrm{MeV})$ photon energy in the final state, a quantity that is difficult to reconstruct with the $B A B A R$ detector. Instead, we define our data sample by selecting on $\Delta E$, an observable that can be related to the maximum allowed total energy of the photons, $E_{\gamma}^{\max }$. The chosen $\Delta E$ window allows for the presence of radiated photons with total energy up to $150 \mathrm{MeV}+\langle\Delta E\rangle$, where the average value of $\Delta E,\langle\Delta E\rangle$, differs for each mode, due to the pion mass hypothesis being assigned to all tracks. As the $\pi^{+} \pi^{-}$ events are centered at $\Delta E \sim 0 \mathrm{MeV}$, while the $K^{+} \pi^{-}$

TABLE I. Percentage of events with $|\Delta E|<150 \mathrm{MeV}$ and photon energy below the cut-off ( 2.6 MeV ) in the Monte Carlo simulation, as given by the simulation and by the QED calculation described in the text.

| Mode | MC | QED calculation |
| :--- | :---: | :---: |
| $\pi^{+} \pi^{-}$ | $89.8 \pm 0.1$ | $88.8 \pm 0.5$ |
| $K^{+} \pi^{-}$ | $92.4 \pm 0.1$ | $91.7 \pm 0.5$ |
| $K^{+} K^{-}$ | $94.7 \pm 0.1$ | $94.7 \pm 0.5$ |

and $K^{+} K^{-}$distributions are shifted by -45 MeV and -91 MeV , respectively, the corresponding energy requirements on the radiated photons are $E_{\gamma}^{\max }=150,105$ and 59 MeV for $\pi^{+} \pi^{-}, K^{+} \pi^{-}$, and $K^{+} K^{-}$, respectively. The smearing of $\Delta E$ due to finite momentum resolution leads to a small difference between the number of events that satisfy the $\Delta E$ requirement and the number of events that satisfy an equivalent $E_{\gamma}^{\max }$ requirement. We use the MC simulation to evaluate the associated systematic error on the branching fractions from this difference.

In addition to signal $\pi^{+} \pi^{-}, K^{+} \pi^{-}$, and (possibly) $K^{+} K^{-}$events, the selected data sample includes background from the process $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s, c)$. According to the MC simulation, backgrounds from other $B$ decays are small relative to the signal yields $(<1 \%)$, and are treated as a systematic uncertainty. We use an unbinned, extended maximum-likelihood (ML) fit to extract simultaneously signal and background yields in the three topologies $(\pi \pi, K \pi$, and $K K)$. The fit uses the discriminating variables $m_{\mathrm{ES}}, \Delta E$, the Cherenkov angles of the two tracks, and a Fisher discriminant $\mathcal{F}$, based on the momentum flow relative to the $h^{+} h^{\prime-}$ thrust axis of all tracks and clusters in the event, excluding the $h^{+} h^{\prime-}$ pair, as described in Ref. [7]. The likelihood for event $j$ is obtained by summing the product of the event yield $N_{i}$ and probability $\mathcal{P}_{i}$ over the signal and background hypotheses $i$. The total likelihood for a sample of $N$ events is

$$
\begin{equation*}
\mathcal{L}=\frac{1}{N!} \exp \left(-\sum_{i} N_{i}\right) \prod\left[\sum_{i} N_{i} \mathcal{P}_{i}\left(\vec{x}_{j} ; \vec{\alpha}_{i}\right)\right] \tag{2}
\end{equation*}
$$

The probabilities $\mathcal{P}_{i}$ are evaluated as the product of the probability density functions (PDFs) with parameters $\vec{\alpha}_{i}$, for each of the independent variables $\vec{x}_{j}=$ $\left\{m_{\mathrm{ES}}, \Delta E, \mathcal{F}, \theta_{c}^{+}, \theta_{c}^{-}\right\}$, where $\theta_{c}^{+}$and $\theta_{c}^{-}$are the Cherenkov angles for the positively- and negativelycharged tracks, respectively. We check that the variables are almost independent. The largest correlation between the $\vec{x}_{j}$ is $13 \%$ for the pair $\left(m_{\mathrm{ES}}, \Delta E\right)$, and we have confirmed that it has a negligible effect on the fitted yields. For both signal and background, the $K^{ \pm} \pi^{\mp}$ yields are parameterized as $N_{K^{ \pm} \pi^{\mp}}=N_{K \pi}\left(1 \mp \mathcal{A}_{K \pi}\right) / 2$, and we fit directly for the total yield $N_{K \pi}$ and the asymmetry $\mathcal{A}_{K \pi}$. The result for $\mathcal{A}_{K \pi}$ is used only as a consistency check and does not supersede our previously published result [3].

The eight parameters describing the background shapes for $m_{\mathrm{ES}}, \Delta E$, and $\mathcal{F}$ are allowed to vary freely in the ML fit. We use a threshold function [16] for $m_{\mathrm{ES}}$ (one parameter), a second-order polynomial for $\Delta E$ (two parameters), and a sum of two Gaussian distributions for $\mathcal{F}$ (five parameters). For the signal shape in $m_{\mathrm{ES}}$, we use a single Gaussian distribution to describe all three channels and allow the mean and width to vary in the fit. For $\Delta E$, we use the sum of two Gaussian distributions (core + tail), where the core parameters are common to all channels and are allowed to vary freely, and the tail parameters are deter-
mined separately for each channel from the reweighted MC simulation (explained above), and fixed in the fit. For the signal shape in $\mathcal{F}$, we use an asymmetric Gaussian function with different widths below and above the mean. All three parameters are determined from MC simulation and fixed in the maximum-likelihood fit. The $\theta_{c} \mathrm{PDFs}$ are obtained from a sample of approximately $430000 D^{*+} \rightarrow$ $D^{0} \pi^{+}\left(D^{0} \rightarrow K^{-} \pi^{+}\right)$decays reconstructed in data, where $K^{-} / \pi^{+}$tracks are identified through the charge correlation with the $\pi^{+}$from the $D^{*+}$ decay. We construct the PDFs separately for $K^{+}, K^{-}, \pi^{+}$, and $\pi^{-}$tracks as a function of momentum and polar angle using the measured and expected values of $\theta_{c}$, and its uncertainty. We use the same PDFs for tracks in signal and background events.

Table II summarizes the fitted signal and background yields, and $K \pi$ charge asymmetries. We find a value of $\mathcal{A}_{K \pi}$ consistent with our previously published result [3], and a background asymmetry consistent with zero. The signal yields are slightly higher than the values reported in Ref. [3] due to the removal of the $\Delta t$ selection requirement and the addition of the radiative tail in the signal $\Delta E$ PDF. In order to quantify the effect of FSR on the fitted yields, we perform a second fit using a single Gaussian for the $\Delta E$ PDF, allowing the mean and width to vary. The results are shown in the second column of Table II, where we find that ignoring FSR lowers the $\pi \pi$ yield by $3.4 \%$ and the $K \pi$ yield by $1.3 \%$.

As a crosscheck, in Fig. 1 we compare the PDF shapes (solid curves) to the data using the event-weighting technique described in Ref. [17]. For each plot, we perform a fit excluding the variable being plotted and use the fitted yields and covariance matrix to determine the relative probability that an event is signal or background. The distribution is normalized to the yield for the given component and can be compared directly to the assumed PDF shape. We find excellent agreement between the data and the PDFs. Figure 2 shows the likelihood ratio $\mathcal{L}_{S} / \sum \mathcal{L}_{i}$ for all 69264 events in the fitted sample, where $\mathcal{L}_{S}$ is the

TABLE II. Summary of results from the ML fit for the yields. The subscript $b$ refers to background. For the nominal fit, we use a double Gaussian for the signal $\Delta E$ PDF, as described in the text. We also show, for comparison purposes, the results using a single Gaussian, which corresponds to an analysis that ignores FSR effects.

| Parameter | Nominal Fit | Ignoring FSR |
| :--- | :---: | :---: |
| $N_{\pi \pi}$ | $485 \pm 35$ | $469 \pm 34$ |
| $N_{K \pi}$ | $1656 \pm 52$ | $1634 \pm 52$ |
| $\mathcal{A}_{K \pi}$ | $-0.136 \pm 0.030$ | $-0.135 \pm 0.030$ |
| $N_{K K}$ | $3 \pm 13$ | $5 \pm 13$ |
| $N_{b \pi \pi}$ | $32983 \pm 194$ | $32998 \pm 194$ |
| $N_{b K \pi}$ | $20778 \pm 169$ | $20801 \pm 169$ |
| $\mathcal{A}_{b K \pi}$ | $0.002 \pm 0.008$ | $0.002 \pm 0.008$ |
| $N_{b K K}$ | $13358 \pm 126$ | $13356 \pm 126$ |

likelihood for a given signal hypothesis, and the summation in the denominator is over all signal and background components in the fit. We find good agreement between data (points with error bars) and the distributions obtained by directly generating events from the PDFs (histograms).

Systematic uncertainties on the branching fractions arise from uncertainties on the selection efficiency, signal yield, and number of $B \bar{B}$ events in the sample. Uncertainty on the efficiency is dominated by track reconstruction efficiency $(1.6 \%)$ and by the uncertainty on FSR ( $1.3 \%$ for $\pi \pi, 1.4 \%$ for $K \pi$ and $2.9 \%$ for $K K$ ), which is evaluated assuming $100 \%$ uncertainty on the smearing effect on $\Delta E$.

Other systematic uncertainties on selection efficiency are those due to requirements on the quality of the $\theta_{c}$ measurement $(1.0 \%$ for $\pi \pi, 0.8 \%$ for $K \pi$ and $0.5 \%$ for $K K$ ) and on event topology ( $1.1 \%$ ). Uncertainty on the fitted signal yields is dominated by the shape of the signal PDF for $\mathcal{F}(2.9 \%$ for $\pi \pi, 1.5 \%$ for $K \pi)$ and potential bias ( $2.2 \%$ for $\pi \pi, 0.9 \%$ for $K \pi$ ) in the fitting technique, as determined from large samples of MC-simulated signal events and a large ensemble of pseudoexperiments generated from the PDF shapes. Uncertainties due to imperfect knowledge of the PDF shapes for $m_{\mathrm{ES}}, \Delta E$, and $\theta_{c}$ are all less than $1 \%$. Tables III and IV summarize the uncertainties on the signal yields and branching fractions, respectively.

Table V summarizes the results for the charge-averaged branching fractions. For comparison, we use the efficiencies and signal yields determined under the assumption of no FSR and find $\mathcal{B}\left(B^{0} \rightarrow \pi^{+} \pi^{-}\right)=5.0 \times 10^{-6}$ and $\mathcal{B}\left(B^{0} \rightarrow K^{+} \pi^{-}\right)=18.0 \times 10^{-6}$, which are consistent with our previously published results [7]. We determine the upper limit for the signal yield for $K^{+} K^{-}$using a Bayesian procedure that assumes a flat prior on the number of events. The upper limit is given by the value of $N_{0}$ for which $\int_{0}^{N_{0}} \mathcal{L}_{\text {max }} d N / \int_{0}^{\infty} \mathcal{L}_{\text {max }} d N=0.90$, corresponding to a one-sided $90 \%$ confidence interval. Here, $\mathcal{L}_{\text {max }}$ is the likelihood as a function of the $K^{+} K^{-}$yield $N$, maximized with respect to the remaining fit parameters. We find $N_{0}=$ 25.4 , and the upper limit on the branching fraction is calculated by increasing the signal yield upper limit and reducing the efficiency by their respective total errors (Table IV). For the purpose of combining with measurements by other experiments, we also evaluate the central value for the branching fraction and find $\mathcal{B}\left(B^{0} \rightarrow\right.$ $\left.K^{+} K^{-} n \gamma\right)=(4 \pm 15 \pm 8) \times 10^{-8}$.

Although we cannot directly measure the nonradiative, or "bare" branching fractions, due to the intrinsic and unavoidable features of QED, they can be extrapolated from our measurements by employing theoretical calculations, such as those found in Ref. [11]. The results for these bare branching fractions for the three channels are shown in Table VI, and the central value for the bare $K^{+} K^{-}$ branching fraction is $\mathcal{B}^{0}\left(B^{0} \rightarrow K^{+} K^{-}\right)=(4 \pm 15 \pm 8) \times$ $10^{-8}$. We stress the importance of being able to disentangle radiation effects from the experimental measurements, as a

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FIG. 1 (color online). Data distributions (points with error bars) of $m_{\mathrm{ES}}, \Delta E$, and $\mathcal{F}$ for signal $\pi^{+} \pi^{-}(\mathrm{a}, \mathrm{b}, \mathrm{c})$, signal $K^{+} \pi^{-}(\mathrm{d}, \mathrm{e}, \mathrm{f})$ and background for the three channels ( $\mathrm{g}, \mathrm{h}, \mathrm{i}$ ), using the weighting technique described in the text. Solid curves represent the corresponding PDFs used in the fit. The distribution of $\Delta E$ for signal $K^{+} \pi^{-}$events is shifted due to the assignment of the pion mass for all tracks.


FIG. 2 (color online). (Color online) Distribution of the likelihood ratio $\mathcal{L}_{S} / \sum \mathcal{L}_{i}$, where $\mathcal{L}_{S}$ is the likelihood for each event to be a signal $\pi^{+} \pi^{-}$(left), $K^{+} \pi^{-}$(middle), or $K^{+} K^{-}$(right) event. The points with error bars show the distribution obtained on the fitted data sample, while the histograms show the distributions obtained by generating signal (dark shaded, red) and background (light shaded, yellow) events directly from the PDFs.

TABLE III. Summary of relative systematic uncertainties on signal yields. For the $K^{+} K^{-}$yield we show the absolute uncertainty. The total uncertainties are calculated as the sum in quadrature of the individual contributions.

| Source | $\pi^{+} \pi^{-}(\%)$ | $K^{+} \pi^{-}(\%)$ | $K^{+} K^{-}$(events) |
| :--- | :---: | :---: | :---: |
| $m_{\mathrm{ES}}$ | 0.2 | 0.4 | 1.3 |
| $\Delta E$ | 0.1 | 0.0 | 0.3 |
| signal $\mathcal{F}$ | 2.9 | 1.5 | 2.8 |
| bkgd $\mathcal{F}$ | 0.5 | 0.2 | 5.9 |
| $\theta_{c}$ quality | 0.2 | 0.1 | 0.4 |
| Fit bias | 2.2 | 0.9 | 1.3 |
| $B$ bkgd | 0.8 | 0.2 | $<0.1$ |
| Total | 3.8 | 1.8 | 6.8 |

TABLE IV. Summary of relative systematic uncertainties on yields, efficiencies, and number of $B \bar{B}$ pairs. For the $K^{+} K^{-}$yield we show the absolute uncertainty. The total uncertainties are calculated as the sum in quadrature of the individual contributions.

| Source | $\pi^{+} \pi^{-}$ | $K^{+} \pi^{-}$ | $K^{+} K^{-}$ |
| :--- | :---: | :---: | :---: |
| yields | $3.8 \%$ | $1.8 \%$ | 6.8 events |
| efficiency | $2.5 \%$ | $2.5 \%$ | $3.5 \%$ |
| $N_{B \bar{B}}$ | $1.1 \%$ | $1.1 \%$ | $1.1 \%$ |
| Total | $4.7 \%$ | $3.3 \%$ | see text |

meaningful comparison between theory and experiment can be performed only in terms of the bare quantities. Likewise, bare quantities should be used when combining measurements from different experiments.

In summary, we have presented updated measurements of charge-averaged branching fractions for the decays $B^{0} \rightarrow \pi^{+} \pi^{-}$and $B^{0} \rightarrow K^{+} \pi^{-}$, with FSR effects taken into account. We find that the branching fractions are a few percent higher when the effect of FSR is included in the calculation of the efficiency and signal yield determination. This difference should be taken into account when comparing with previous measurements of these quantities [7-9,18] that do not include these effects. In order to perform the most meaningful comparison, we also evaluated the bare branching fractions for the three channels, as explained in Ref. [11]. Our results are consistent with

TABLE V. Summary of branching fraction results. We give signal yields $N_{S}$, total detection efficiencies ( $\epsilon$ ) and branching fractions $\mathcal{B}_{E_{\gamma}}$, where the subscript $E_{\gamma}$ serves as a reminder of the dependence on the cut on soft photon energy as explained in the text. The errors are statistical and systematic, respectively, and the upper limit on $B^{0} \rightarrow K^{+} K^{-} n \gamma$ corresponds to the $90 \%$ confidence level.

| Mode | $N_{S}$ | $\epsilon(\%)$ | $\mathcal{B}_{E_{\gamma}}\left(10^{-6}\right)$ |
| :--- | ---: | ---: | ---: |
| $\pi^{+} \pi^{-}$ | $485 \pm 35 \pm 18$ | $41.8 \pm 0.2 \pm 1.0$ | $5.1 \pm 0.4 \pm 0.2$ |
| $K^{+} \pi^{-}$ | $1656 \pm 52 \pm 30$ | $40.5 \pm 0.2 \pm 1.0$ | $18.1 \pm 0.6 \pm 0.6$ |
| $K^{+} K^{-}$ | $3.2 \pm 12.9 \pm 7$ | $39.0 \pm 0.3 \pm 1.4$ | $<0.5$ (90\% C.L.) |

TABLE VI. Summary of experimental branching fractions, $\mathcal{B}_{E_{\gamma}}$, with a defined cut on soft photon energy, together with the electromagnetic correction factor $G\left(E_{\gamma}^{\max }\right)$ and the evaluated bare branching fractions (nonradiative), $\mathcal{B}^{0}$. The errors on branching fractions are statistical and systematic respectively; the error on $G\left(E_{\gamma}^{\max }\right)$ is taken as the difference between its value at $\mu=M_{\pi}$ and $\mu=M_{\rho}$.

| Mode | $\mathcal{B}_{E_{\gamma}}\left(10^{-6}\right)$ | $G\left(E_{\gamma}^{\max }\right)$ | $\mathcal{B}^{0}\left(10^{-6}\right)$ |
| :--- | :---: | :---: | ---: |
| $\pi^{+} \pi^{-}$ | $5.1 \pm 0.4 \pm 0.2$ | $0.937 \pm 0.005$ | $5.5 \pm 0.4 \pm 0.3$ |
| $K^{+} \pi^{-}$ | $18.1 \pm 0.6 \pm 0.6$ | $0.947 \pm 0.005$ | $19.1 \pm 0.6 \pm 0.6$ |
| $K^{+} K^{-}$ | $<0.5$ (90\% C.L.) | $0.952 \pm 0.005$ | $<0.5$ (90\% C.L.) |

current theoretical estimates from different models [5]. We find no evidence for the decay $B^{0} \rightarrow K^{+} K^{-}$and set an upper limit of $5.0 \times 10^{-7}$ at the $90 \%$ confidence level.

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[1] M. Gronau, Phys. Rev. Lett. 63, 1451 (1989); M. Gronau and D. London, Phys. Rev. Lett. 65, 3381 (1990).
[2] M. Gronau, J. L. Rosner, and D. London, Phys. Rev. Lett. 73, 21 (1994); R. Fleischer and T. Mannel, Phys. Rev. D 57, 2752 (1998); M. Neubert and J. L. Rosner, Phys. Lett. B 441, 403 (1998); A. J. Buras and R. Fleischer, Eur. Phys.
J. C 11, 93 (1999); for a recent review see M. Gronau and J. L. Rosner, Report No. SLAC-R-709.
[3] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 93, 131801 (2004).
[4] Y. Chao et al. (Belle Collaboration), Phys. Rev. Lett. 93, 191802 (2004).
[5] M. Ciuchini et al., Phys. Lett. B 515, 33 (2001); C. W. Bauer, S. Fleming, D. Pirjol, and I. W. Stewart, Phys. Rev. D 63, 114020 (2001); M. Beneke and M. Neubert, Nucl. Phys. B675, 333 (2003); J. Charles et al., Eur. Phys. J. C 31, 503 (2003); Y.-Y. Keum, Pramana 63, 1151 (2004); C.W. Chiang, M. Gronau, J. L. Rosner, and D. A. Suprun, Phys. Rev. D 70, 034020 (2004); A. J. Buras, R. Fleischer, S. Recksiegel, and F. Schwab, Nucl. Phys. B697, 133 (2004).
[6] The use of charge conjugate modes is implied throughout this paper unless otherwise stated.
[7] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 89, 281802 (2002).
[8] Y. Chao et al. (Belle Collaboration), Phys. Rev. D 69, 111102 (2004).
[9] K. Abe et al. (Belle Collaboration), Phys. Rev. Lett. 95, 231802 (2005).
[10] F. Ambrosino et al. (KLOE Collaboration), Phys. Lett. B

632, 43 (2006).
[11] E. Baracchini and G. Isidori, Phys. Lett. B 633, 309 (2006).
[12] B. Aubert et al. (BABAR Collaboration), Nucl. Instrum. Methods A 479, 1 (2002).
[13] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 95, 151803 (2005).
[14] S. Agostinelli et al., Nucl. Instrum. Methods A 506, 250 (2003).
[15] E. Barberio and Z. Was, Comput. Phys. Commun. 79, 291 (1994); We use version 2.03 .
[16] H. Albrecht et al. (ARGUS Collaboration), Z. Phys. C 48, 543 (1990).
[17] M. Pivk and F. R. Le Diberder, Nucl. Instrum. Methods A 555, 356 (2005).
[18] A. Bornheim et al. (CLEO Collaboration), Phys. Rev. D 68, 052002 (2003).


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