

Improvement of Electromagnetic Compatibility of Motor Drives Using Chaotic PWM

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In this paper, a new chaotic pulse width modulation (PWM) scheme is proposed and implemented to reduce the conducted electromagnetic interference (EMI) in motor drives. The key is the use of logistic mapping to chaoticize a frequency-modulated signal which then modulates the carrier frequency. Compared with the sinusoidal PWM and random PWM, the proposed scheme not only suppresses the peaky EMI, but also avoids the occurrence of low-order noises and mechanical resonance. Both simulation and experimental results are given to support the validity.

Index Terms—Chaos, EMC, EMI, motor drives, PWM.

I. INTRODUCTION

IN the field of variable-speed motor drives, there is a trend for pushing up switching frequencies of pulse width modulation (PWM) inverters to reduce both volume and weight. This trend inevitably contributes to an increasing level of electromagnetic interference (EMI). It leads to degrade the electromagnetic compatibility (EMC) for electronic devices [1]. Consequently, EMC legislation is increasingly stringent in many countries.

In recent years, random PWM (RPWM) schemes, including both nonoptimized and optimized ones, have been developed to improve the EMC of motor drives [2]. The RPWM can effectively spread the discrete spectral power over a continuous spectrum by varying the widths of individual switching intervals randomly. The optimized version can further even out the spectral power distribution. However, these schemes have ignored the consideration of low-order harmonic frequencies and the system natural frequency. So, they inevitably introduce low-order noises, and increase the possibility to create mechanical resonance [3].

Because of the deterministic but random-like behavior, chaos is becoming attractive for application to motor drives [4]. Recently, it has been identified that the use of chaotic PWM to replace sinusoidal PWM (SPWM) can reduce EMI in motor drives [5]. This chaotic PWM scheme employs the Bernoulli shift map to chaoticize an amplitude-modulated signal which then modulates the carrier frequency, so-called the chaotically amplitude-modulated PWM (CAMPWM). Although the CAMPWM takes the advantage of easier implementation than the RPWM which needs a truly random source, their performance comparison is absent. Also, the CAMPWM is inflexible to tune the spectral power distribution, and is limited to those chaotic maps satisfying some specific characteristics, namely the mixing rate and probability density function.

In this paper, a chaotically frequency-modulated PWM (CFMPWM) scheme is proposed and implemented, which not only suppresses the peaky EMI, but also avoids the occurrence of low-order noises and mechanical resonance. Both simulation and experimental results will be given to compare the power spectra resulting from SPWM, CFMPWM, and RPWM. More-

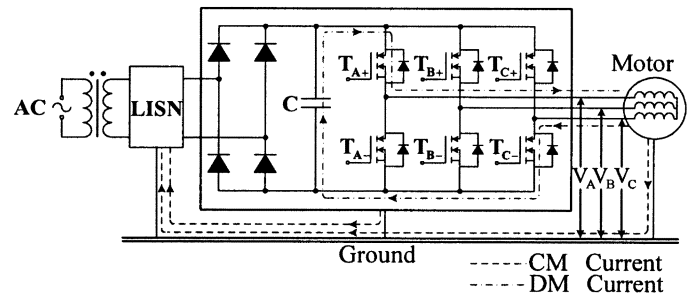


Fig. 1. Conducted EMI in motor drives.

over, a comparison between CFMPWM and CAMPWM will be given and discussed.

II. PROPOSED CFMPWM

In general, the total conducted EMI is caused by two mechanisms: the common-mode (CM) noise V_{CM} which is related to capacitive coupling of switching voltage into the line impedance stabilizing network (LISN), and the differential-mode (DM) noise V_{DM} which is related to switching current. Fig. 1 shows typical current flows of the conducted EMI in motor drives.

The key of the CFMPWM is to modulate the switching frequency by chaotic sequences. The corresponding carrier signal is given by

$$V_C = \frac{2}{\pi} \arcsin(X) \quad (1)$$

$$X = \sin \left\{ \int_{-\infty}^t \left[2\pi f_{sw} + 2\pi \Delta f \sin \left(\int_{-\infty}^t 2\pi \xi_i f_m dt \right) \right] dt \right\} \quad (2)$$

where f_{sw} is the nominal switching frequency, Δf is the deviation frequency, f_m is the modulation frequency, and $\xi_i \in (0, 1)$ is the chaotic sequences generated by the logistic map $\xi_{i+1} = A\xi_i(1 - \xi_i)$ with $A \in [0.1, 3.9]$. Hence, the spectrum of V_C can be expressed as

$$S_n(f) = \sum_{m=-\infty}^{+\infty} A_{n,m}(\beta) \delta(f - nf_{sw} - m\xi_i f_m) \quad (3)$$

where $\beta = \Delta f/f_m$ is the frequency modulation index, n is the harmonic order, m is the Fourier order, $\delta(\cdot)$ is the im-

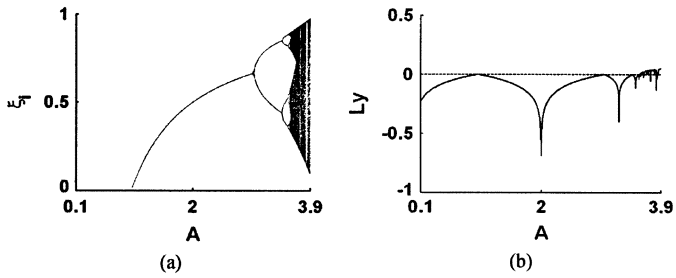


Fig. 2. Logistic map: (a) Bifurcation diagram; (b) Lyapunov exponent.

pulse function, and $A_{n,m}(\beta)$ is the magnitude coefficient. According to the Carson's rule, if $\beta \gg 1$, 98% of the power around $n f_{sw}$ is distributed to the discrete terms at $f = n f_{sw} + m \xi_i f_m$ within a limited frequency range ($n f_{sw} - n \Delta f, n f_{sw} + n \Delta f$). Fig. 2(a) shows the bifurcation diagram of ξ_i against A . It illustrates that A can be used to tune the spectral power distribution among no frequency modulation (FM), periodic FM, multi-periodic FM and chaotic FM. When $A \in [3.57, 3.9]$, chaos occurs and the corresponding Lyapunov exponent is positive as shown in Fig. 2(b).

Based on a practical 3-phase 400-W 220-V 4-pole induction motor drive, the mechanical resonant frequency of the rotor can be estimated by using the Holzer method. Given $f_{ref} = 30$ Hz and $f_{sw} = 7.5$ kHz, it deduces $\Delta f = 2.2$ kHz and $f_m = 50$ Hz so as to avoid overlapping with the mechanical resonant frequency of 10.2 kHz. Hence, three indicators are defined to assess the EMC of this motor drive. Since the conducted EMI with a frequency exceeding 9 kHz is stringently limited by the VDE standards, the maximum power spectral density (PSD) of V_{CM} and V_{DM} within 9–150 kHz is used as the first indicator. In order to evaluate the content of low-order noises while the power spectrum is mainly from $(f_{sw} - \Delta f)$ to $(f_{sw} + \Delta f)$, the power of V_{CM} and V_{DM} within 4.99–5.01 kHz is used as the second indicator. In order to evaluate the possibility of mechanical resonance at 10.2 kHz, the power of V_{CM} and V_{DM} within 10.19–10.21 kHz is used as the third indicator. Therefore, the CFMPWM is created by tuning A equal to 3.9 so that the first indicator is minimum while the others are low.

III. SIMULATION RESULTS

Computer simulation of the whole system is carried out by using the Matlab Simulink. The corresponding power spectra are plotted by a Matlab function, namely the periodogram method. The power spectra of V_{CM} and V_{DM} using SPWM, CFMPWM, and RPWM are computed from zero to 150 kHz under the same f_{sw} and Δf . Figs. 3–5 show the corresponding power spectra within 0–22.5 kHz so as to depict their spectral power distributions.

First, by comparing the maximum PSD of their V_{CM} spectra within 9–150 kHz, namely 21.3 dBm/Hz for SPWM, 10.8 dBm/Hz for CFMPWM and 7.3 dBm/Hz for RPWM, it shows that the CFMPWM and RPWM have remarkable improvements over the SPWM. Similarly, by comparing those V_{DM} spectra, namely 31.4 dBm/Hz for SPWM, 10.2 dBm/Hz for CFMPWM, and 6.2 dBm/Hz for RPWM, it further shows that the CFMPWM and RPWM have remarkable improvements over the SPWM. Thus, it indicates that both the CFMPWM

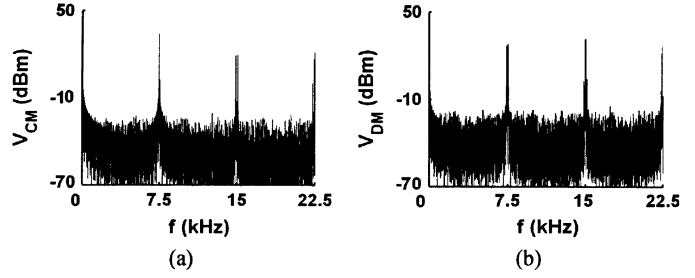


Fig. 3. Simulated power spectra of SPWM: (a) V_{CM} ; (b) V_{DM} .

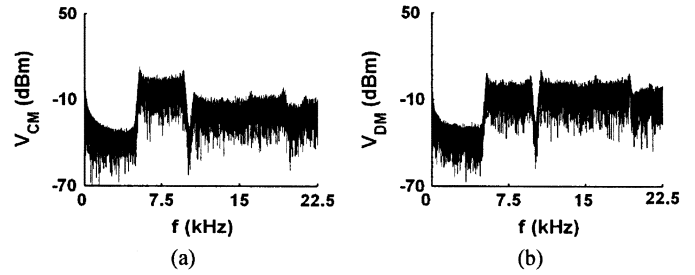


Fig. 4. Simulated power spectra of CFMPWM: (a) V_{CM} ; (b) V_{DM} .

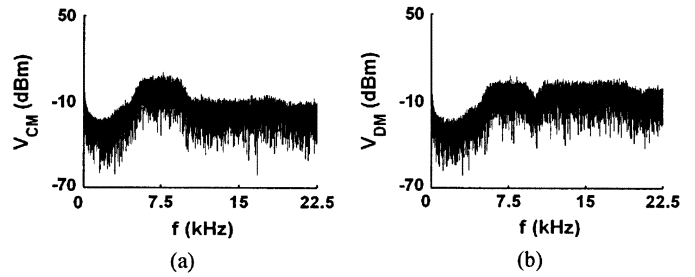


Fig. 5. Simulated power spectra of RPWM: (a) V_{CM} ; (b) V_{DM} .

and RPWM have much better performance than the SPWM in suppressing the peaky EMI.

Second, by comparing the power of their V_{CM} spectra within 4.99–5.01 kHz, namely -25.8 dBm for SPWM, -11.4 dBm for CFMPWM, and 2.5 dBm for RPWM, it shows that the CFMPWM has a significant improvement over the RPWM. Similarly, by comparing those V_{DM} spectra, namely -22.6 dBm for SPWM, -13.9 dBm for CFMPWM and -1.4 dBm for RPWM, it further shows that the CFMPWM has a significant improvement over the RPWM. Thus, this comparison indicates that the CFMPWM has much better performance than RPWM in avoiding low-order noises.

Third, by comparing the power of their V_{CM} spectra within 10.19–10.21 kHz, namely -25.8 dBm for SPWM, -21.2 dBm for CFMPWM, and -0.4 dBm for RPWM, it illustrates that the CFMPWM provides a much greater attenuation than the RPWM. Similarly, by comparing those V_{DM} spectra, namely -25.7 dBm for SPWM, -15.6 dBm for CFMPWM, and -0.2 dBm for RPWM, it further illustrates that the CFMPWM provides a much greater attenuation than the RPWM. Thus, it indicates that the CFMPWM has much better performance than RPWM in avoiding mechanical resonance.

It should be noted that even though the SPWM offers the lowest spectral power within 4.99–5.01 kHz and 10.19–10.21 kHz, its severely peaky EMI will create annoying

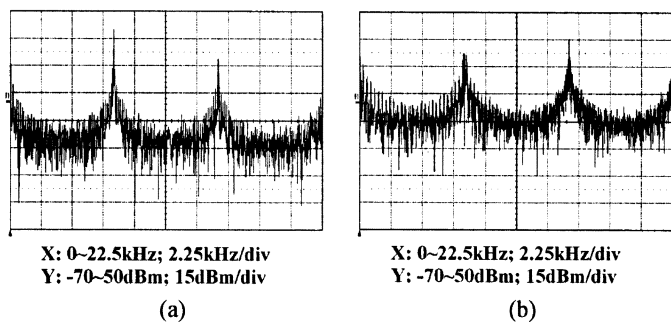


Fig. 6. Measured power spectra of SPWM: (a) V_{CM} ; (b) V_{DM} .

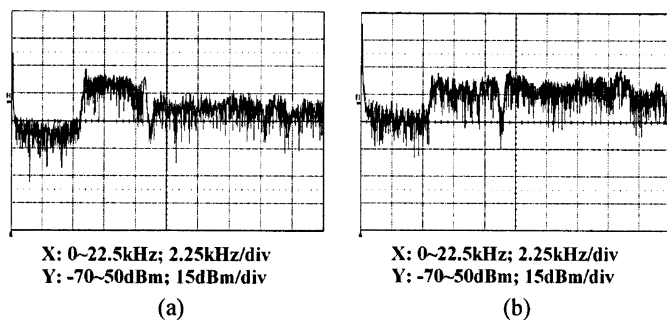


Fig. 7. Measured power spectra of CFMPWM: (a) V_{CM} ; (b) V_{DM} .

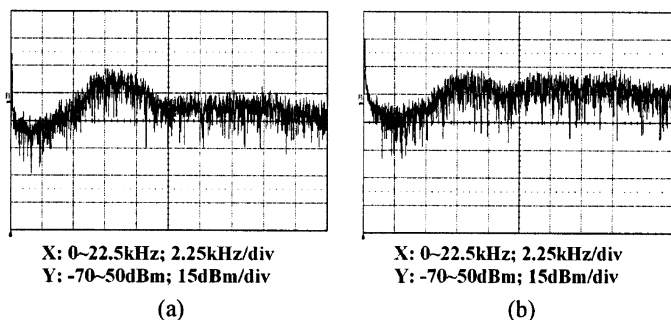


Fig. 8. Measured power spectra of RPWM: (a) V_{CM} ; (b) V_{DM} .

acoustic noise in motor drives. This problem precludes the SPWM competing with CFMPWM and RPWM.

IV. EXPERIMENTAL RESULTS

For experimental verification, an IGBT-based voltage source inverter is constructed to supply the aforementioned induction motor. The CFMPWM scheme is implemented by a single-chip TMS320F240 microcontroller. All power spectra are directly measured by using the LeCroy WR6050 power spectrum analyzer. Figs. 6, 7, and 8 show the measured power spectra of SPWM, CFMPWM, and RPWM, respectively. The resolution bandwidth is set to be 15 Hz. It can be seen that the measured spectra well agree with the simulated counterparts as shown in Figs. 3, 4, and 5. Hence, it experimentally verifies that the proposed CFMPWM not only effectively suppresses the peaky EMI, but also exhibits high immunity to low-order noises and mechanical resonance.

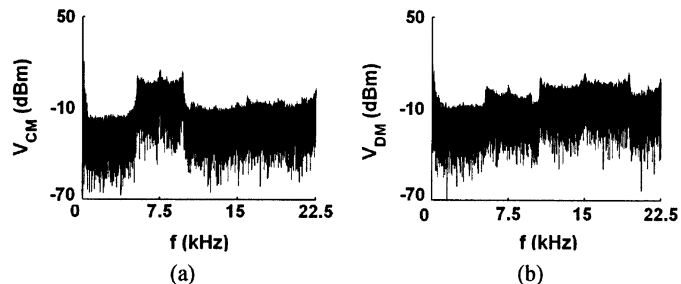


Fig. 9. Simulated power spectra of CAMPWM: (a) V_{CM} ; (b) V_{DM} .

V. FURTHER COMPARISON

In order to compare the CFMPWM with the CAMPWM, the power spectra of V_{CM} and V_{DM} using CAMPWM are computed under the same logistic map, f_{sw} and Δf . Fig. 9 shows their distributions within 0–22.5 kHz. The maximum PSD within 9–150 kHz, the power within 4.99–5.01 kHz, and the power within 10.19–10.21 kHz of V_{CM} using CAMPWM are 14.4 dBm/Hz, -4.6 dBm, and -5.6 dBm, respectively, whereas those using CFMPWM are only 10.8 dBm/Hz, -11.4 dBm, and -21.2 dBm, respectively. Relative data of V_{DM} are similar. Hence, it confirms that the proposed CFMPWM can offer better spectral performances than the CAMPWM.

VI. CONCLUSION

By using the logistic map to chaoticize the frequency-modulated signal for the carrier frequency, a new CFMPWM has been proposed and implemented to improve EMC of motor drives. Both simulation and experimental results have confirmed that the proposed CFMPWM can effectively suppress the peaky EMI which usually occurs in SPWM, and can avoid the possibility of low-order noises and mechanical resonance which generally occur in RPWM. Moreover, the CFMPWM can offer better spectral performances than the CAMPWM.

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