Improving FPGA Design Robustness with Partial TMR

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Abstract— This paper describes an efficient approach of applying mitigation to an FPGA design to protect against Single Event Upsets (SEUs). This approach applies mitigation selectively to FPGA circuit structures depending on the importance of structure within the design. Higher priority is given to structures causing "persistent" errors within the design. For certain applications, applying partial mitigation to the persistent components can provide higher returns in reliability for the investment in mitigation cost than full mitigation. A software tool is also introduced which automatically classifies circuit structures based on this concept and applies Triple Modular Redundancy (TMR) selectively based on the classification of the circuit structure.

Index Terms—SEU, FPGA, TMR, persistence, error propagation, simulator, radiation, selective mitigation

I. INTRODUCTION

FPGAs are an increasingly attractive solution for space systems. They perform well in high-throughput signal processing applications often used in space. Furthermore, their programmability allows in-field application adjustments.

Unfortunately, FPGAs are susceptible to radiation-induced Single-Event Upsets (SEU). Since FPGAs store their configuration in an SRAM-like configuration memory, an SEU can actually alter the desired configuration. As such, FPGAs destined for a radiation environment must employ a form of SEU mitigation to insure reliable operation [1]–[3].

SEU sensitivity in the configuration memory can be mitigated through techniques such as Triple Modular Redundancy (TMR) [1], [2]. These mitigation strategies offer tremendous improvements in reliability, but are often expensive in terms of FPGA resource utilization, power consumption, etc. [1], [4]. We seek new ways to offer acceptable levels of reliability at much lower costs.

One way to reduce the cost of mitigation is to apply mitigation selectively on a sub-set of an FPGA design. By selectively applying design mitigation, the designer can trade off the improvements in reliability with the cost of design mitigation. In this paper we will show that applying TMR to a subset of the user design allows the designer to make this trade-off. Applying TMR selectively to a user design is called "Partial TMR". This paper introduces a tool for *automatically*

M. Wirthlin is with the Department of Electrical and Computer Engineering, Brigham Young University, Provo, UT. applying TMR selectively and reports on the improvements in reliability obtained from this tool.

II. FPGA SINGLE EVENT EFFECTS

Much like SRAM and DRAM memory, programmable FPGAs contain a large number of memory cells susceptible to radiation-induced upset. Within FPGAs, the vast majority of memory cells are devoted to the configuration memory. Configuration memory upsets are particularly troublesome as they may *change* the operation of the circuit within the device. Upsets within the configuration memory may alter the function of the configurable logic, routing network, I/O, or other FPGA resources.

One technique used to reduce the effects of upsets within the configuration memory is called *configuration scrubbing* [5]. Configuration scrubbing involves the continual reading and evaluation of the FPGA configuration memory contents. If a fault is found in the configuration memory, the FPGA configuration is repaired by reloading the correct configuration information back into the FPGA. Configuration scrubbing prevents the build-up of configuration faults and significantly reduces the time in which an invalid circuit configuration is allowed to operate.

A. FPGA Design Sensitivity

Although a modern FPGA contains a large amount of configuration cells, not all of the configuration memory cells affect behavior of the design. A configuration memory cell that impacts the behavior of a particular design is called a *sensitive* configuration bit. The set of sensitive configuration bits is unique for each design and depends on the logic, I/O, routing, and other FPGA resources used by the given design.

In a previous effort, we developed a fault injection tool that identifies the *sensitive* configuration bits of the device for any given FPGA design [6], [7]. The tool operates by artificially injecting faults within the configuration bitstream and monitoring the behavior of the device. By comparing the behavior of the device under test against a golden device, we can determine when the device behavior changes. By testing every configuration bit of the device, a detailed sensitivity profile of a given design can be created.

This fault injection tool has been used to characterize the sensitivity of many FPGA designs. A sample of these results is shown in Table I. For each design tested, the table provides the utilization (in logic slices and percentage) and the number of sensitive configuration bits. In addition, it provides an

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Fig. 1. The diagram on the left is a screen capture of the layout of the DSP Kernel design. The center and right diagrams are graphical representations of the portion of the DSP Kernel design layout which correspond to the sensitive and persistent bits respectively.



Fig. 2. The diagram on the left is a screen capture of the layout of the Synthetic design. The center and right diagrams are graphical representations of the portion of the Synthetic design layout which correspond to the sensitive and persistent bits respectively.

overall "sensitivity" measure that indicates the percentage of configuration bits that are sensitive in the design. It is important to note that the configuration sensitivity is design dependent and must be characterized on a design by design basis.

Design	Utilization	Sensitive	Persistent		
	(Slices)	Bits	Bits		
DSP Kernel	5,746 (46.8%)	575,448 (9.9%)	13,841 (0.24%)		
Synthetic	2,538~(20.6%)	189,835 (3.3%)	77,159 (1.3%)		
Multiplier	10,305 (83.9%)	550, 228 (9.5%)	0 (0%)		
Counter	2,151 (17.5%)	201,691 (3.5%)	108,750 (1.9%)		

TABLE I

CONFIGURATION SENSITIVITY AND PERSISTENCE FOR SEVERAL DESIGNS.

Figures 1 and 2 visually demonstrate the concept of configuration sensitivity for two different FPGA designs. The first design (Figure 1) is a digital signal processing (DSP) kernel developed at Los Alamos National Laboratory. The second design (Figure 2) is a synthetic design made from feedback shift registers (LFSRs) that feed an array of multipliers and adders.

The left most figure for both design representations is a depiction of the logic resources used by the design. This was obtained by taking a screen capture of the fpga_editor resource editor provided by the manufacturer. The middle figure

is a plot of the sensitive configuration bits within the device. Points marked in this plot indicate a sensitive configuration bit. Note the correspondence between the resource utilization and sensitivity map. As expected, sensitive configuration bits are located in areas where the FPGA device is utilized.

III. CLASSIFICATION OF SENSITIVE CONFIGURATION BITS

To successfully pursue partial mitigation techniques, we need a method of more finely categorizing or ranking the sensitive configuration bits. Since mitigation techniques will be applied to only a subset of the circuit, only a subset of the corresponding sensitive configuration bits will be addressed. To maximize the benefit of partial mitigation techniques, the importance of the all circuit structures will be ranked and mitigation will be applied to the most important circuit structures in the design. This section will describe a method for characterizing the sensitive configuration bits into two categories. We will use this classification to direct our partial mitigation strategy.

A. Persistent Configuration Upsets

In [8] and [9] we introduced a new way to categorize the sensitive configuration bits by separating them into two categories called "persistent" and "non-persistent". A nonpersistent configuration bit is a sensitive configuration bit that will cause a design fault when upset through radiation. This will introduce functional errors. When the non-persistent configuration bit is repaired through configuration scrubbing, however, the design returns to normal operation. Eventually all previously induced functional errors will disappear. No additional intervention is required to return the circuit to normal functionality.

A persistent configuration bit is also a sensitive configuration bit that will cause a design fault when upset. However, even after repairing persistent configuration bits through configuration scrubbing, the FPGA circuit *does not* return to normal operation. Persistent configuration upsets introduce functional errors which persist after the bit is repaired through scrubbing. Persistent upsets put the design into an incorrect state that cannot self-restore. In this case, a global reset is needed to return the circuit to proper state, or normal operation. This global reset takes the circuit offline for the time needed to reset the circuit and start up in normal operating mode.

The differing behavior of the two types of sensitive configuration bits can be seen in the plots of Figure 3. Each figure plots the arithmetic difference of the output signal between the Design Under Test (DUT) and a golden circuit design as captured by our fault injection simulation environment. When the two circuits are operating correctly, the arithmetic difference is zero. When one of the circuits has functional errors, the arithmetic difference is non-zero.

The left figure demonstrates the behavior of non-persistent configuration upsets. After an upset, the difference between the two circuits is non-zero. The output of the corrupted design is incorrect. Once repaired through scrubbing, the difference returns to zero. The corrupted circuit returns to normal behavior.

The right figure demonstrates the behavior of persistent configuration upsets. Almost immediately after the configuration upset, the arithmetic difference is non-zero. The outputs of the DUT and golden circuits do not match. In this case, even after the upset bit is repaired through scrubbing, the corrupted circuit continues to generate incorrect output. In other words, the circuit fails to return to normal operation. Only a system reset will restore the circuit to a proper state.



Fig. 3. The left and right plots show the delta between the outputs of a DUT and golden circuit before, during and after a sensitive and persistent upset respectively.

The fault injection tool of [7] was augmented to measure configuration persistence. The tool begins by determining the sensitive configuration bits within the design. Once the sensitive configuration bits are identified, the tool performs additional tests to identify the subset of sensitive configuration bits that are also persistent configuration bits. Table I lists the configuration persistence for several designs tested within the fault injection framework. In some designs, the persistent component is a major portion of the design (i.e. synthetic) while the persistence in other designs is relatively small (i.e. multiplier). The persistence of two designs can be seen visually in the right-most plot of Figure 1 and Figure 2. In general, the persistent configuration bits represent a small fraction of the overall configuration bits within the device.

B. Persistent Circuit Structures

The circuit structures that correspond to persistent configuration bits can be identified statically by analyzing the structure of the circuit netlist. Specifically, circuit primitives that are part of feedback structures within the design contribute to the persistent error behavior. If a circuit fault occurs within a feedback structure, the incorrect values produced by the faulty circuit are propagated into the feedback state. Once the state of the feedback circuit has been corrupted, the circuit will not behave correctly until the circuit state has been reinitialized with a global reset. Although configuration scrubbing will repair the faulty circuit, it will not restore the proper circuit state.

The schematics in Figure 4 illustrate the major subsections of a simple circuit that may cause persistent configuration faults. Figure 4(a) highlights a feedback structure of a sample design. An upset within this feedback structure will indefinitely propagate incorrect values within the state flip flops. Upsets within the logic feeding *into* feedback structures will also cause persistent configuration faults (see Figure 4 (b)). Logic calculations made in these feedback input structures contribute to the state values within the feedback structure circuit. Upsets within logic structures driven by a feedback structure or that operate independently of feedback do not cause persistent faults (see Figure 4 (c)). To maximize the benefits of partial mitigation, redundancy should be added for circuits highlighted in Figure 4 (a) and (b) before addressing the circuits of Figure 4 (c).

IV. PARTIAL MITIGATION

SEU mitigation is essential to ensure absolute reliable operation of FPGA devices in a radiation environment. Triple Modular Redundancy is one of the common methods of SEU mitigation. It has been shown to greatly reduce the dynamic cross section of an FPGA design and, when combined with bitstream scrubbing, virtually eliminate the configuration bitstream from SEU susceptibility [1], [2]. TMR can greatly decrease the downtime of the circuit in radiation environments.

Full mitigation of an FPGA design using techniques such as TMR, however, is costly in terms of FPGA resource utilization, power consumption, and circuit performance. Many user designs, in fact, cannot be mitigated with full TMR due to the more than $3\times$ increase in design resource utilization.

An attractive alternative to full mitigation is to mitigate only the most critical sections of a design. This reduces mitigation costs while efficiently reducing circuit downtime



(c)

Fig. 4. A simple representation of a circuit with different sections highlighted (a) The feedback section (b) The input to the feedback section (c) The feed-forward logic section

[3]. By selectively applying mitigation to a design, one can find the most effective balance of mitigation cost and reliability.

A. Partial Mitigation With Respect to Persistence

We can leverage the concept of persistence, discussed in Section III, to efficiently apply partial mitigation to an FPGA design. Since a persistent upset causes a permanent interruption in service, we would like to first apply mitigation to persistent circuit components. A non-persistent upset simply causes a temporary service interruption, thus non-persistent circuit structures are a lower mitigation priority.

A partial mitigation strategy based on the concept of persistence should rank the different structures of a circuit by their contribution to the persistence of a design. The more critical sections of a design should be mitigated first, with those of lower priority following as constraints allow. Referring back to Figure 4, the feedback structures of the design should be mitigated first. Any logic feeding into the feedback structures should follow, since these contribute to the state of the design and thus the persistence. The feedforward logic—the non-persistent circuit components—does not contribute to the persistence of a design and should be mitigated last.

It must be made clear that only certain FPGA applications are candidates for partial mitigation, as the non-persistent portion of the sensitive configuration bits remains after mitigation. The output of the system may be incorrect after an SEU in the remaining set of unmitigated bits. However, applications that can tolerate this data-loss stand to realize tremendous gains in Mean Time Between Failure (MTBF).

Even an application that can tolerate temporary data-loss will still fail after all persistent upsets. As discussed in Section III, these upsets cause the circuit to enter an incorrect state, which will not self-correct, even after configuration scrubbing. However, these tolerant circuits may take advantage of incremental partial mitigation, starting with the persistent circuit structures. Valuable circuit resources are utilized to first eliminate failure. In Section V we will show that, in some cases, non-linear improvements in MTBF can be achieved at a linear cost.

B. BYU-LANL Partial TMR Tool

In cooperation with Los Alamos National Laboratory (LANL), a software tool was developed at Brigham Young University (BYU) to automatically apply partial mitigation on any EDIF-format design. The BYU-LANL Triple Modular Redundancy (BLTmr) tool uses TMR and the concepts presented in this paper to increase the uptime of the design with minimal user intervention.



Fig. 5. Basic flow of the BYU-LANL Partial TMR (BLTmr) tool.

Figure 5 shows the basic flow of the BYU-LANL Partial TMR (BLTmr) tool. The tool first parses the input EDIF file(s) into a netlist data structure. The data structure is analyzed to identify feedback structures by searching for strongly connected graph components. Once all feedback structures are identified, the feedback input, and feedback output structures are identified and classified. These circuit classes are separated for later analysis by the BLTmr tool.

The BLTmr tool uses this information to select circuit structures for triplication. Based on the user constraints, the BLTmr tool will select as much of the feedback, feedback input, and output logic as possible. Once the triplicated circuit elements are selected, the tool determines where in the design to insert the voters necessary to support TMR. The newly constructed circuit, which has the same functionality of the original, is then written out in EDIF format. The new circuit structure can then mapped to the corresponding FPGA technology.

Our tool follows the basic decision-making process described in Section IV-A, prioritizing the application of TMR based on a circuit component's contribution to design persistence. The feedback structures of a design are of the most concern and thus are triplicated first. If resources allow, TMR is applied to the input to the feedback to further reduce persistence. Finally, mitigation is applied to the non-persistent circuit structures to reduce the remaining design sensitivity.

		Slices	Utilization	Sensitive	Sensitivity	Persistent	Persistence
Design	BLTmr Level			Bits		Bits	
	Unmitigated	5,746	46.8%	575,448	9.9%	13,841	0.24%
DSP	Feedback	7,276	59.2%	572,605	9.9%	5,074	0.087%
Kernel	Feedback &						
design	Input to FB	8,036	65.4%	569,700	9.8%	152	0.0026%
	Max TMR [†]	11,114	90.4%	556,062	9.6%	154	0.0027%
	Unmitigated	2,538	20.7%	189,835	3.3%	77,159	1.3%
Synthetic	Feedback	9,867	80.3%	125,017	2.2%	804	0.014%
design	Feedback &						
	Input to FB	9,867	80.3%	125,017	2.2%	804	0.014%
	Full TMR [‡]	11,961	97.3%	20,256	0.3%	671	0.012%

TABLE II

MEASUREMENTS OF THE SENSITIVITY AND PERSISTENCE OF THE DSP KERNEL AND SYNTHETIC DESIGNS. THE XILINX XCV1000 CONTAINS 12, 288 SLICES AND 5, 810, 048 CONFIGURATION BITS.

[†] Full TMR could not be applied due to FPGA resource constraints.

 ‡ "Full" TMR here does not include triplication of the clock and output signals.

V. EXPERIMENTAL RESULTS

As a verification of our partial TMR tool, we used the tool in various configurations on two FPGA designs. The first is a digital signal processing (DSP) kernel developed at Los Alamos National Laboratory. The second is a synthetic design made up of linear feedback shift registers (LFSRs) that feed into an array of multipliers and adders.

A. Design Measurements

The BLTmr tool was used to investigate the improvements in reliability for various levels of partial TMR. Four different mitigation approaches were used and tested for each of the two designs: first, an unmitigated design was created for a baseline, second, TMR was applied to feedback structures only, third, TMR applied to feedback plus the input to the feedback, and fourth, TMR was applied to as much of the circuit as allowed by the device density limitations. The sensitive and persistent configuration bits were measured and plotted for each of these test cases.

The fault injection results for the DSP Kernel and Synthetic designs are summarized in Table II. For the DSP kernel, the number of persistent bits was reduced by two orders of magnitude for a relatively small hardware cost. The sensitivity was reduced by over 3%. The synthetic design also demonstrated two orders of magnitude reduction in persistent configuration bits. In addition, the sensitive configuration bits were reduced by 90%.

Figure 7 and Figure 8 show layouts, sensitivity plots, and persistence plots of the mitigated DSP Kernel and Synthetic designs, respectively. The figures of the DSP Kernel correspond to the "Feedback & Input to FB" mitigation level in Table II, while the figures of the Synthetic design correspond to the "Full TMR" mitigation level. Notice that the persistence of each design has been virtually eliminated.

B. Mean Time Between Failure

An important motivation for measuring the sensitivity and/or persistence of a design is to determine how often a given system will fail. Like sensitivity and persistence, Mean Time Between Failure (MTBF) is application dependent. However, MTBF also depends on the destined system environment. A detailed explanation of how we predicted MTBF can be found in [10].

Table III shows our predictions of MTBF for the DSP Kernel design. The first set of values (columns 4-6) shows the MTBF prediction for an application that does not tolerate any service interruptions. Applications in this category will "fail" after all dynamic upsets. The second set of values (columns 7-9) corresponds to applications that can function with temporary data-loss. Applications in this category "fail" only after persistent upsets. The final set of values in Table III corresponds to the DSP Kernel with mitigation applied to just persistent structures. Here too, the application will only "fail" after persistent upsets. However, they have been virtually eliminated.

Figure 6 is a plot of MTBF vs. resource utilization for the DSP kernel and Synthetic circuit designs in a GPS orbit. This graph clearly shows a non-linear relationship between resources and MTBF improvement. In both cases, MTBF reaches a "saturation" point. After this point, additional mitigation logic primarily only improves data-loss rates. For both designs saturation occurred after all persistent circuit elements were mitigated (since the feedback in the Synthetic design consists of input-less LFSRs, the feedback and feedback plus input circuits are the same). This indicates that once the persistent circuit elements are triplicated, MTBF will saturate. Additional mitigation logic will only improve data-loss rates, not MTBF.

It is important to analyze the trade-offs made by applying TMR to just the persistence of a design. Since full TMR and other comprehensive mitigation techniques are costly in terms of area and power [1], [4], the positive benefit of partial TMR is a reduction in mitigation circuitry, and consequently power, required. For example, Table I shows that a completely unmitigated implementation of the DSP Kernel design utilized 5,746 slices. Full TMR would require at least a 200% increase. The partial TMR implementation done with the BLTmr tool, on the other hand, needed only 8,036 slices, or a 40% increase.



Fig. 7. The diagram on the left is a screen capture of the layout of a version of the DSP Kernel design which has been mitigated with the BLTmr partial mitigation tool. The center and right diagrams are graphical representations of the portion of the DSP Kernel design layout which correspond to the sensitive and persistent bits respectively.



Fig. 8. The diagram on the left is a screen capture of the layout of a version of the Synthetic design which has been mitigated with the BLTmr partial mitigation tool. The center and right diagrams are graphical representations of the portion of the Synthetic design layout which correspond to the sensitive and persistent bits respectively.

[†] "Full" Mitigation here does not include triplication of the clock and output signals.



Fig. 6. Plot of MTBF vs. resource utilization for the DSP kernel and Synthetic circuit designs in a GPS orbit.

The negative trade-off for only applying partial TMR, is that the non-persistent configuration bits are still vulnerable to SEUs. However, if only persistent upsets are considered failures, as some applications may, the system will only temporarily lose data after non-persistent upsets.

VI. CONCLUSIONS

The selective use of TMR on FPGA circuits was shown to provide improved reliability at a lower cost than full TMR. In fact, the amount of triplication inserted into a design allows a designer to trade off the incremental cost of selective triplication with improvements in reliability. The BLTmr tool was created to perform this selective TMR automatically to a degree directed by the user.

This tool applied selective TMR to several designs and demonstrated the benefits of this approach. Results obtained from the BLTmr tool confirm that for certain applications, MTBF can be more efficiently increased when mitigation is focused on the persistent structures of a design. Specifically, this tool improved the MTBF of both designs by two orders of magnitude for a fraction of the cost of full TMR.

Efforts to improve the BLTmr tool and associated circuit analysis continues. Specifically, additional analysis approaches will be added to improve the classification of FPGA circuit structures. Architecture-specific mitigation techniques may provide greater improvements in reliability at a lower hardware cost. Other efforts include more design testing, radiation testing for tool validation, and improvements in the user interface. We expect this approach to be used on several designs operating on a spacecraft to be launched in 2006.

Orbit	Alt.	Inc.	Unmitigated - Data Loss			Unmitigated - Persistent Failures			Partially Mitigated - Persistent Failures		
Olon	(KIII)	(ueg)	Typical	Stormy	Worst Day	Typical	Stormy	Worst Day	Typical	Stormy	Worst Day
			Solar Min	Solar Max	Solar Max	Solar Min	Solar Max	Solar Max	Solar Min	Solar Max	Solar Max
LEO	560	35.0°	22.9	34.4	32.8	950.5	1428.5	1365.6	86555.7	130077.0	124634.5
Polar	833	98.7°	9.1	11.5	0.2	378.2	479.5	7.0	53350.3	51590.9	179.8
GPS	22,200	55.0°	14.1	13.6	4.7×10^{-2}	585.9	566.6	2.0	53350.3	51590.9	179.8
GEO	36,000	0.00	13.9	11.4	4.7×10^{-2}	579.6	473.3	2.0	52781.9	43101.2	177.8

TABLE III

MEAN TIME BETWEEN FAILURE (MTBF) FOR THE DSP KERNEL DESIGN IN SEVERAL ORBITS FOR THREE DIFFERENT SITUATIONS: UNMITIGATED DESIGN FAILING WITH ANY SENSITIVE UPSET, UNMITIGATED DESIGN FAILING ONLY WITH PERSISTENT UPSET, PARTIALLY MITIGATED DESIGN FAILING ONLY WITH PERSISTENT UPSETS.

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