# INDEPENDENT COMPONENT ANALYSIS APPLIED TO DIGITAL IMAGE WATERMARKING

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### ABSTRACT

The authors propose a new solution to the watermarking of images. This approach uses Independent Component Analysis (ICA) to project the image into a basis with its components as statistically independent as possible. The watermark is then introduced in this representation of the space. Thus, the change of basis is the key of the steganography problem. The algorithm applied to the fragile watermarking problem locates any change in the image since it also applies to the watermark. The problem of robust watermarking is also addressed from this new point of view. Some results are included to illustrate the method.

# 1. INTRODUCTION

Watermarking usually consists in the use of perceptually invisible authentification techniques. In this sense, "controlled" distortion is introduced in a multimedia element. And the owner wants to "protect" this content. The goals are on the one hand the verification of the owner and the detection of forgeries of an original image. This is usually referred as Fragile Watermark (FW) and is mainly an authentification problem. A fragile watermark is readily destroyed if the watermarked data is only slightly altered. On the other hand the Robust Watermarking (RW) focuses on the identification of illegal copies of the image and the prevention of unauthorized distribution. A typical scenario is that of an owner placing digital images on a network server. A robust watermark is resilient in the face of attacks that attempt to remove it, either intentionally or unintentionally.

In digital image watermarking the watermark is inserted in the image so that the watermarked image is public. In this sense, steganography [1] is used to prevent any user from removing the watermark. The method to insert the watermark along with a private key characterise the watermarking process. In RW, the illegal use of the watermarked image is usually associated to the image "attack". The goal of these attacks is to remove the watermark from the image. This must be as difficult as possible even if the adversary knows the method as long as he does not have key. Many watermarking methods working either in spatial or transformed domain exists [2] [3] [4] [5]. Our approach may be classified in the second group as the watermarking is inserted in the image after it has been projected into a new space.

We propose to use the change of basis provided by ICA [6] or Blind Separation of Sources [7] methods. Consider a  $k^2 \times 1$  vector  $\boldsymbol{x}_t$  projected into a space of  $k^2$  components  $\boldsymbol{y}_t$ as statistically independent as possible. The ICA problem consists of finding this change of basis represented by an  $k^2 \times k^2$  matrix B.

$$\boldsymbol{y}_t = B\boldsymbol{x}_t \quad t = 1, 2, \dots \tag{1}$$

Let's matrix I be an intesity image of size  $n \times m$ . The matrix is divided into blocks of  $k \times k C_{p,q}$ . The enter  $C_{p,q}(i,j)$ with indexes

is the sample t = m(p-1)/k + q of the component k(i-1) + j of vector  $x_t$ . The analysis (and synthesis) expression yields

$$x(k(i-1) + j)_{(m(p-1)/k+q)} = C_{p,q}(i,j)$$
  
=  $I(k(p-1) + i, k(q-1) + j)$  (3)

By applying ICA to  $x_t$  we obtain the ICA components  $y_t$  of the image. Operating on these components leads to compression or codification algorithms [8]. Compression algorithms exploit this decomposition as they retain only the *r* ICA components with larger energy and it restores the image starting from these *r* components. The codification approach is based upon the idea that images with similar features may be restored from a common set of components. That is, it is possible to use ICA to define a set of basis functions to build a group of images. If the image is

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a RGB image, the process is applied to each color. We next use the concepts above to propose a new solution to the watermarking problem.

### 2. WATERMARKING

In this section we apply ICA to the watermarking of an image. We first address the problem of inserting the watermark and then the watermak extraction.

## 2.1. Insertion

In the last section we described how to decompose an image I into components  $x_t^I$  in (3). By applying an ICA algorithm [9] [10] to the image to watermark, we get matrix  $B^I$  and components ICA  $y_t^I$ . Besides, suppose the watermark is another image W of the same size than  $I, n \times m$ . We may obtain its ICA decomposition by dividing it in blocks of the same size as before, k. This pair of decompositions may be written as

$$\begin{aligned} \boldsymbol{y}_t^I &= B^I \boldsymbol{x}_t^I \\ \boldsymbol{y}_t^W &= B^W \boldsymbol{x}_t^W \quad t = 1, \dots, mn/k^2 \end{aligned}$$

where the components have been arranged in descending order of energy.

ICA based compression methods remove the r less energy ICA components of an image. We propose to replace these r components from  $y_t^I$  with the first  $k^2 - r$  ICA components of the watermark  $y_t^W$ . Note that any other interchange of components may be valid. The components of the watermarked image V yields

$$y_t^V(h) = y_t^I(h) \quad h = 1, \dots, k^2 - r$$
 (5)

$$y_t^V(k^2 - h + 1) = \alpha(h)y_t^W(h) \quad h = 1, \dots, r$$
 (6)

where  $\alpha$  is a weight vector to control the perception of the watermark. The watermarking process outlined above may be summarized in the following algorithm

Algorithm 1: insertion.

- 1 *Image components*. Compute the components  $x_t^I$  and  $x_t^W$  of the image I and the watermark W by dividing it in blocks of  $k \times k$  as in (3).
- 2 *ICA components*. Compute the ICA components  $y_t^I$  and  $y_t^W$  of the image and the watermark as in (4). Arrange the component in descending order of energy.
- 3 *ICA Watermarked Image components*. Compute the ICA components  $y_t^V$  by replacing the latest ICA components of image *I* by the ones of the watermark as described in (5) and (6).
- 4 *Restoring Watermarked Image*. Restore the watermarked image V from components  $x_t^V = B_I^{-1} y_t^V$ by using (3).

5 *Store the Key.* Store matrices  $B_I$  and  $B_W$  as the keys of the method.

Once we have the image with the watermark we need to define the procedure to extract it.

#### 2.2. Extraction

The aim of this section is the extraction of the watermark W from the watermarked image V. We go back on the steps of algorithm 1. We first compute the components  $x_t^V$  as in (3). Next the projected ones  $y_t^V$  by using  $B^I$  stored in step 5. Then we recover the ICA components of the watermark in (6)

$$y_t^W(h) = y_t^V(k^2 - h + 1) \quad h = 1, \dots, r$$
 (7)

and set the rest of them to zero. The image is restored by using matrix  $B^{W}$  in step 5. The watermark extraction yields *Algorithm 2*: Extraction.

- 1 Watermarked Image components. Compute the components  $x_t^V$  of the image V by dividing it in  $k \times k$  blocks as in (3).
- 2 Watermarked Image ICA components. Compute the components  $y_t^V$  of the image as  $y_t^V = B^I x_t^V$ .
- 3 Watermark ICA components. Compute the components  $\boldsymbol{y}_t^W$  of the watermark as in (7).
- 4 *Restoring the Watermark.* Compute the components  $x_t^W = B_W y_t^W$  and use (3) to obtain the image.

# 3. DISCUSSION

An important issue in watermarking extraction is the knowledge of the original image in the extraction process. Our aim is to propose an extraction method not based in this knowledge. Notice that if we had this information, the ICA components of the watermark could be added to the ones of the image instead replacing them as in (6) [11]. This way the method would be more robust to attacks. In order to make our extraction algorithm independent of the image, the key  $B_I$  should be known at step 5. In [8] a common set of basis were proposed for natural images. In fact B in (1) is just a change of basis and it may be applied to any image. We applied this idea to our approach: Matrix  $B^I$  in step 2 of the insertion algorithm may be the ICA change of basis computed for any other image.

We use an image as the watermark. However, the watermark could be any signal such as a message. Notice that once the components of the watermark has been extracted, matrix  $B^W$  is used to restore the watermark. In this sense this second matrix is the key of a cryptographic problem.

As it will be described in the next section, the proposed method applied to FW allows to detect any change in the image by simply subtracting the original watermark from the extracted one. Any adversary must know the exact change of basis, the key, to manipulate the image. On the other hand, the method is flexible as the number r of components to replace is not fixed. Thus, in the case of RW this number may be increased. One of the main attacks to take into account is that of compression. In the case of JPEG compression, the watermark usually disappears from low frequency regions. A perceptual mask could be used to palliate this problem. Another point we do not face in this paper is that of the automatic detection or synchronization of the watermark. We just focus on the watemark extraction to show the proposed method to be an alternative method. Synchronization methods in the literature [12] could be adapted for our approach.

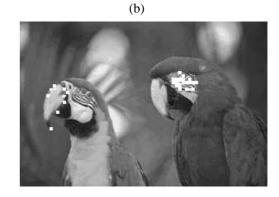
## 4. EXPERIMENTAL RESULTS

We first propose to apply FW to the image I in Fig.1.a. The image was divided in blocks of size  $4 \times 4$ . Then ICA was performed to compute matrix  $B_I$ . The first ICA component of the image in Fig. 2.b., the logo of the University Carlos III de Madrid, was introduced as the last ICA component of the watermarked image. We then applied some changes: we copied the beak of one arara on the other one and copied the eye area of this one to the other. These changes can be observed in Fig.1.b. Next we extracted the watermark and compared to the original one to obtain image in Fig1.c were the watermark was detected except in the altered areas.

We next include an example of RW of the intensity image of lena in Fig.2.a with, as in the previous case, the logo in Fig.2.b. We computed the "ICA components" of the image as  $y_t^I = B_I x_t^I$  where matrix  $B_I$  was the one obtained for image in Fig.1.a. The first ICA component of the watermark was introduced as the ICA components number 14, 15 and 16 multiplied by  $\alpha = .5$ . We performed the following attacks: In Fig.2.c the image was smoothed with a  $3 \times 3$  mask with a ratio of 0.3 between any border entry of the mask and the central one, in Fig.2.e we cropped the 30% of the image and added white noise with variance  $\sigma/255 = 0.1$ , and in Fig.2.g the image was converted to jpeg format with a compression factor of 80%. The results in extracting the watermark are shown on the right hand column: Fig.2.d for the case of smoothing, Fig.2.f when cropping and adding white noise, and Fig.2.h. if the image is compressed. In the two first cases the watermark may be visually detected. In the last case only in the areas with higher frequency (face, hat and feathers) it can be observed remains of the watermark. This is a characteristic of the compression algorithm JPEG that compresses the low frequency areas. Introducing a perceptual mask and a good detecting algorithm is needed



(a)



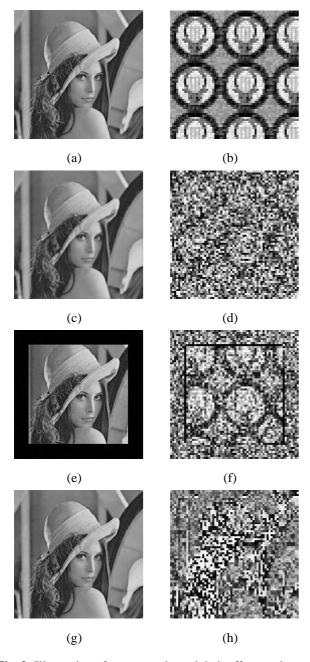
(c)

**Fig. 1**. Illustration of Fragile Watermarking : (a) watermarked image, (b) altered watermarked image, (c) finding the altered regions.

to face this attack.

## 5. CONCLUSIONS

In this paper we present a new approach to image watermarking based in independent component analysis. The starting point is the ICA based image processing in [8]. We apply these concepts to write a new watermarking algorithm. The key of this steganographic method is the change of basis performed with ICA. This change of basis for the



**Fig. 2**. Illustration of some attacks and their effect on the extracted watermark: (a) and (b) the watermarked image and the watermark, (c) and (d) smoothing, (e) and (f) cropping 30% and white noise of variance  $\sigma = 0.1$ , and (g) and (h) jpeg compression of ratio 80%

watermark is also a cryptographic key. The problems of robust and fragile watermarking are addressed. The experiments included show how this new method successes in extracting the watermark even when the image has been attacked. It also allows solving the authentification problem in the FW case detecting any change in the image.

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