

Inertial Vibration Control Using a Shunted Electromagnetic Transducer

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Abstract—Inertial drives and passive tuned-mass dampers utilize a suspended mass to reduce the vibration experienced by a host structure. Active vibration control systems typically include a voice coil type electromagnetic actuator to develop the required reaction forces. In this paper, the technique of sensorless active shunt control is applied to inertial vibration absorption. An electrical impedance is designed and connected to an electromagnetic coil with a view to minimizing structural vibration. Standard optimal control tools can be applied to design the required shunt impedance. This technique requires no additional feedback sensors. Vibration in an experimental structure is heavily attenuated by the application of an active shunt impedance.

Index Terms—Control, electromagnetic, inertial, proof mass, sensorless, shunt damping, vibration.

I. INTRODUCTION

TUNED mass dampers, or inertial drives, are commonly used for mechanical vibration control [1], [2]. Passive tuned mass absorbers utilize an inertial mass and tuned support to introduce additional dynamics and mitigate vibration over a certain frequency range. Inertial drives, comprising an electromagnetic transducer and suspended inertial mass, are used in active feedback control systems to regulate measured acceleration.

Electromagnetic transducers can be used as sensors, actuators, or both [3]–[8]. A simple technique for mitigation of mechanical vibration is known as *passive electromagnetic shunt damping* [9]. Analogous to the well-known technique of piezoelectric shunt damping [10], an electrical impedance, designed to reduced vibration, is connected to the terminals of an electromagnetic transducer. A great variety of piezoelectric shunt circuit designs, reviewed in [11], have been proposed for reducing structural vibration. A subset of these techniques has been adapted for use with electromagnetic transducers [9]. Unfortunately, such techniques find limited application, as the control objective offered by piezoelectric shunt damping circuits is not valid in the context of electromagnetic vibration control. Piezoelectric shunt damping circuits result in the reduction of strain under the transducer [11]; analogously, their adapted electromagnetic equivalents mitigate the relative velocity experienced

by the coil and magnetic field [9]. Practical vibration control applications utilizing electromagnetic transducers can be categorized almost universally as: inertial mass systems, isolation systems, or suspension systems. In each application, minimizing the relative velocity experienced by the transducer is contradictory to the respective performance objective. For this reason, previous results in the field of smart structures and piezoelectric shunt damping cannot be applied directly.

A technique for the synthesis of active electromagnetic shunt impedances was presented in [12]. Using active synthesis, performance objectives other than minimization of the relative velocity are possible. Active electromagnetic shunt control is potentially applicable to vibration damping, isolation systems, and suspension systems.

This paper considers vibration reduction using an electromagnetically actuated inertial drive. Both the passive and active drive dynamics are considered when constructing a model of the mated mechanical and inertial drive systems. In doing so, the performance of a passive absorber can be augmented with an active feedback system. A method is presented for the modeling, design, and implementation of a shunt controlled electromagnetic inertial drive for vibration suppression. By viewing the coil current and voltage as system inputs and outputs, the task of impedance synthesis can be cast as a standard feedback design problem. Arbitrary objectives such as LQR , LQG , or \mathcal{H}_2 goals are easily specified. In this work, displacement is minimized subject to a penalty on the inertial mass travel and applied terminal voltage. Using this technique, the need for external sensors is eliminated, significantly reducing the cost, complexity, and sensitivity to transducer failure that in many applications may preclude the use of an active control system.

Experiments are performed on a simple single-mode host structure with integrated electromagnetic transducer and suspended absorber mass. The combination of passive and active control results in significant vibration suppression.

This paper is organized as follows. In Section II, we begin with the modeling of mechanical and electromagnetic systems. A method is then presented in Section III for the design of active impedance and admittance controllers to minimize a specified performance objective. The presented techniques are then applied to an experimental electromagnetic system in Section IV. Finally, the paper is concluded in Section V.

II. MODELING

In this section, the dynamics of an electromagnetic and mechanical system are studied independently, then combined to reveal the dynamics of a shunted electromagnetic inertial actuator.

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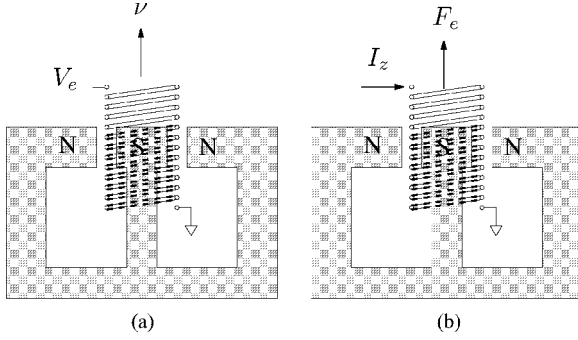


Fig. 1. A voice-coil-type electromagnetic transducer in (a) a velocity sensing role and (b) force acting role.

A. Electromagnetic System

When an electrical conductor, in the form of a coil, moves in a magnetic field as shown in Fig. 1(a), a voltage V_e proportional to the velocity ν is induced and appears across the terminals of the coil

$$V_e \propto \nu. \quad (1)$$

Specifically,

$$\frac{V_e}{\nu} = Bl \quad (2)$$

where B is the magnetic flux (in T), l is the length of the conductor (in m), and ν is the velocity of the conductor relative to the magnetic field (in ms^{-1}). A permanent magnet is usually the source of the magnetic field. In another configuration, the coil is kept stationary and the magnet is free to move.

Assuming the coil is exposed to a field of constant flux density and the relative displacement is small, (2) can be rewritten [1] as

$$\frac{V_e}{\nu} = \frac{F_e}{I_z} = Bl = C_e \quad (3)$$

where F_e denotes the force (in newtons) acting on the coil carrying a current I_z (in amperes), and C_e is the ideal electromechanical coupling coefficient. When the coil is employed as a force actuator, (3) relates the induced force to an applied current. Electrodynamics shakers and acoustic speakers operate on this principle. As shown in Fig. 2, the coil can be modeled as the series connection of an inductor L , a resistor R , and a dependent voltage source V_e [4]. When coupled to a mechanical system, the induced electromotive force (EMF) and, hence, mechanical velocity, can be determined from the open circuit coil terminal voltage. The electrical and mechanical transducer dynamics are summarized in Fig. 3. In response to a relative velocity ν and terminal voltage V_z , the transducer E develops a force F_e and current I_z . When short circuited; i.e., when $V_z = 0$, the transducer develops a force opposite in direction to the relative coil velocity ν . This damping force is utilized in electrodynamic braking systems and eddy-current dampers.

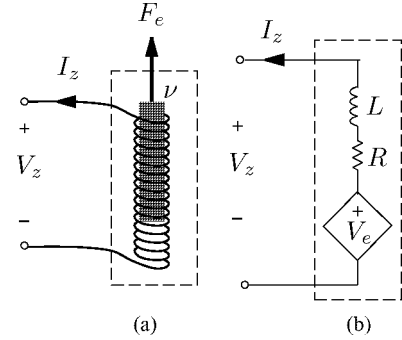


Fig. 2. (a) An electromagnetic transducer generating a force F_e in response to the terminal current I_z . (b) The electrical equivalent model includes the coil inductance L , the coil resistance R , and a voltage source V_e proportional to the velocity between the coil and magnetic field.

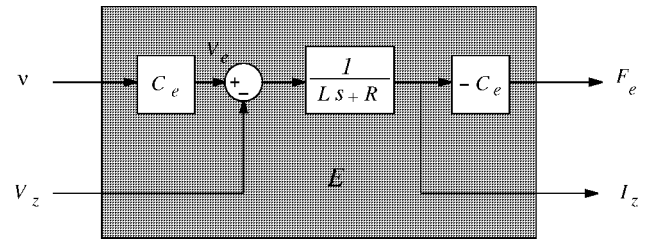


Fig. 3. The electrical and mechanical dynamics of an electromagnetic transducer.

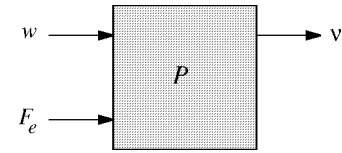


Fig. 4. A general mechanical system suitable for coupling to an electromagnetic transducer. In addition to a disturbance input w , the model also includes a force input F_e and relative velocity output ν .

The following state-space representation of the coil admittance $Y_c(s) = \frac{1}{Ls+R}$ will be required as

$$A_y = \left[\frac{-R}{L} \right] \quad B_y = [1] \quad C_y = \left[\frac{1}{L} \right]. \quad (4)$$

B. Mechanical System

The general model of a mechanical system is shown in Fig. 4. In addition to various application-specific inputs and outputs, in order to couple the system to an electromagnetic actuator, the model requires a force input F_e and a relative velocity output ν . In a typical scenario, the model would also describe the influence of a specific disturbance input w . A single degree-of-freedom tuned-mass, or inertial vibration control system, is shown in Fig. 5. The reaction force F_e generated by an electromagnetic actuator is employed to minimize the vibration d_2 resulting from a disturbance force F_d . The quantities denoted M , k , b , and d represent the mass (in kg), the spring constant (in $\text{N} \cdot \text{m}^{-1}$), the damping coefficient (in $\text{N} \cdot \text{s} \cdot \text{m}^{-1}$), and the displacement (in meters), respectively. The symbols \dot{v} and ν are used to represent acceleration and velocity, respectively.

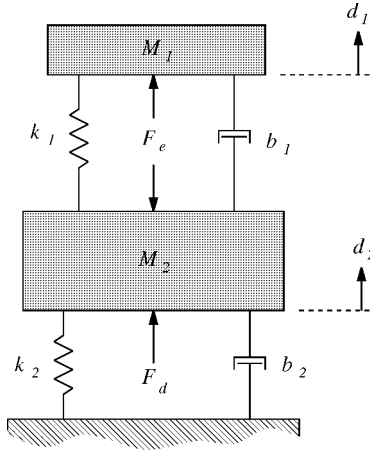


Fig. 5. A suspended mass M_2 disturbed by a force F_d . The absorber mass M_1 is maneuvered by the reaction force F_e to reduce the displacement d_2 .

The equations of motion governing the system can be written as

$$M_1 \dot{\nu}_1 = -b_1(\nu_1 - \nu_2) - k_1(d_1 - d_2) + F_e \quad (5)$$

$$M_2 \dot{\nu}_2 = b_1(\nu_1 - \nu_2) + k_1(d_1 - d_2) - b_2 \nu_2 - k_2 d_2 - F_e + F_d. \quad (6)$$

By choosing the state variables ν_1, d_1, ν_2 , and d_2 , the system can be cast in the following state-space form:

$$\dot{x}_p(t) = \mathbf{A}_p x_p(t) + \mathbf{B}_p \begin{bmatrix} F_d(t) \\ F_e(t) \end{bmatrix} \quad (7)$$

$$\begin{bmatrix} d_2(t) \\ \nu_1 - \nu_2 \end{bmatrix} = \mathbf{C}_p x_p(t)$$

where the subscript p denotes the mechanical plant, and the output $\nu_1 - \nu_2$ represents the relative velocity between the two masses. The system matrices are

$$x_p(t) = \begin{bmatrix} \nu_1 \\ d_1 \\ \nu_2 \\ d_2 \end{bmatrix} \quad (8)$$

$$\mathbf{B}_p = [\mathbf{B}_{p1} \ \mathbf{B}_{p2}] = \begin{bmatrix} 0 & \frac{1}{M_1} \\ 0 & 0 \\ \frac{-1}{M_2} & \frac{1}{M_2} \\ 0 & 0 \end{bmatrix}$$

$$\mathbf{A}_p = \begin{bmatrix} \frac{-b_1}{M_1} & \frac{-k_1}{M_1} & \frac{b_1}{M_1} & \frac{k_1}{M_1} \\ 1 & 0 & 0 & 0 \\ \frac{b_1}{M_2} & \frac{k_1}{M_2} & \frac{-b_1 - b_2}{M_2} & \frac{-k_1 - k_2}{M_2} \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad (9)$$

$$\mathbf{C}_p = \begin{bmatrix} \mathbf{C}_{p1} \\ \mathbf{C}_{p2} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & -1 & 0 \end{bmatrix}. \quad (10)$$

A block diagram of the mechanical system (7) is shown in Fig. 6. As the system includes a control force input F_e and a relative velocity output ν , the model is easily coupled to that of an electromagnetic transducer.

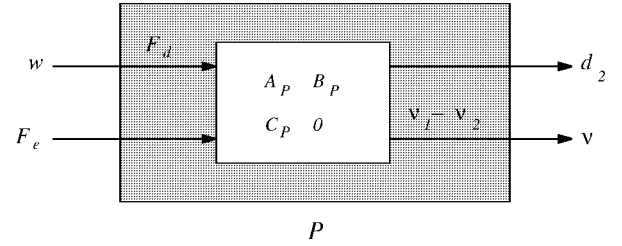


Fig. 6. The mechanical system (7) shown with force disturbance and control inputs F_d and F_e , a performance output d_2 , and the relative velocity output ν .

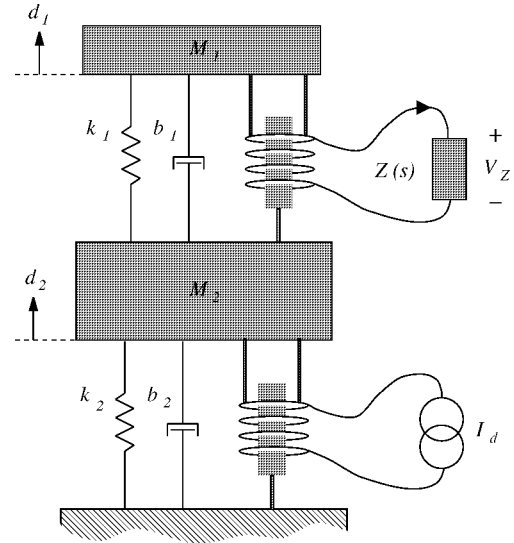


Fig. 7. A two-mass system with electromagnetic transducers to realize the disturbance force F_d and control force F_e .

C. Shunted Composite Electromechanical System

As shown in Fig. 7, we now consider a mechanical system P coupled to an impedance shunted electromagnetic transducer. The force disturbance F_d is realized with the use of an auxiliary transducer and current source

$$F_d = I_d C_e. \quad (11)$$

Within the modeling framework introduced in Sections II-A and II-B, i.e., by treating the mechanical plant and shunted electromagnetic coil as shown in Figs. 6 and 3, the composite plant is easily constructed as that shown in Fig. 8. In Fig. 8, the impedance $Z(s)$, appears analogous to a feedback controller for the electromechanical system. By concatenating the mechanical and electromagnetic systems, P and E , as shown in Fig. 9, the composite system is cast as a typical regulation problem for the abstracted system G . The state equation of the electrical (4) and mechanical systems (7) can be collected to describe the system G

$$\dot{x}_g(t) = \mathbf{A}_g x_g(t) + \mathbf{B}_g \begin{bmatrix} I_d(t) \\ V_z(t) \end{bmatrix}$$

$$\begin{bmatrix} d_2(t) \\ I_z(t) \end{bmatrix} = \mathbf{C}_g x_g(t) \quad (12)$$

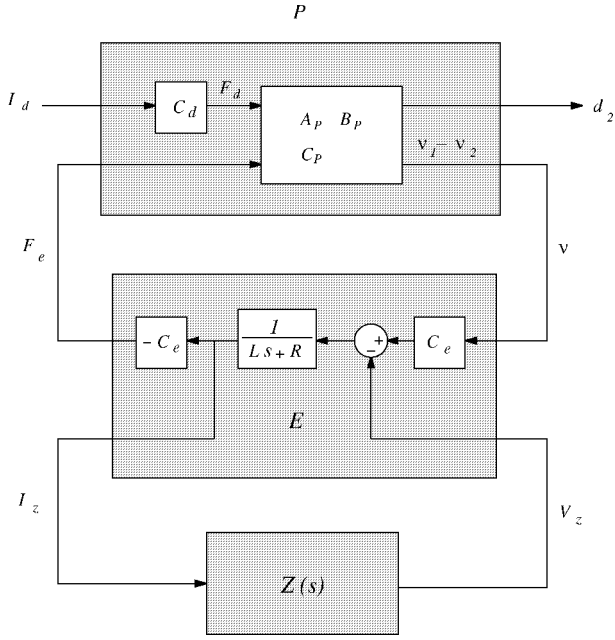


Fig. 8. Mechanical system P coupled to an impedance shunted electromagnetic transducer E .

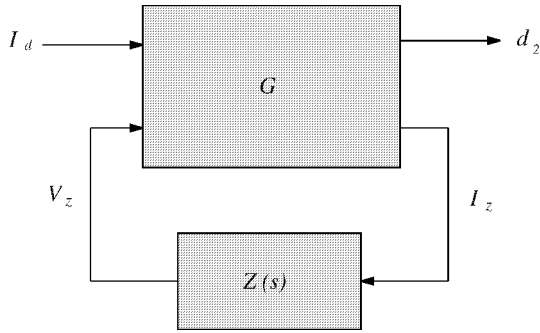


Fig. 9. Composite system G comprising the mechanical and electromagnetic subsystems.

where

$$\mathbb{A}_g(t) = \begin{bmatrix} x_p(t) \\ x_y(t) \end{bmatrix} \quad (13)$$

$$\mathbf{A}_g = \begin{bmatrix} \mathbf{A}_p & -C_e \mathbf{B}_{p2} \mathbf{C}_y \\ B_y \mathbf{C}_{p2} C_e & A_y \end{bmatrix}$$

and

$$\mathbf{B}_g = \begin{bmatrix} \mathbf{B}_{p1} C_d & 0 \\ 0 & -B_y \end{bmatrix}, \quad \mathbf{C}_g = \begin{bmatrix} \mathbf{C}_{p1} & 0 \\ 0 & C_y \end{bmatrix}. \quad (14)$$

III. CONTROL DESIGN

As shown in Fig. 8, an impedance connected to a mechanically coupled electromagnetic transducer can be viewed as parameterizing a velocity feedback controller for the mechanical system P . Section III-A introduces a technique for the synthesis of active impedance controllers designed to minimize structural vibration.

Our design objective is to minimize the displacement d_2 while restraining both the magnitude of control voltage V_z and the absorber mass travel $d_1 - d_2$. As the reaction force F_e results in an acceleration of the absorber, at low frequencies, the magnitude of available force is strictly limited by the maximum travel $d_1 - d_2$. In a linear quadratic sense, our objective is to minimize

$$J = \int_0^\infty \{d_2^2(t) + k_v V_z^2(t) + k_d (d_1(t) - d_2(t))^2\} dt. \quad (15)$$

where k_v and k_d represent weightings on the applied shunt voltage V_z and the absorber mass travel $d_1 - d_2$, respectively. By substituting the state solutions into $d_1(t)$ and $d_2(t)$, we obtain

$$J = \int_0^\infty \left\{ x_p'(t) b f C_{p1}' \mathbf{C}_{p1} x_p(t) + V_z(t)' k_v V_z(t) + x_p'(t) \mathbf{C}_{p3}' k_d \mathbf{C}_{p3} x_p(t) \right\} dt. \quad (16)$$

where $d_1(t) - d_2(t) = \mathbf{C}_{p3} x_p(t)$, and $\mathbf{C}_{p3} = [0 \ -1 \ 0 \ 1]$. Restated in the standard LQR context,

$$J = \int_0^\infty \{x_g'(t) \mathbf{Q} x_g(t) + u(t)' \mathbf{R} u(t)\} dt \quad (17)$$

where

$$\mathbf{Q} = [b f C_{p1} \ 0]' [\mathbf{C}_{p1} \ 0] + k_d [\mathbf{C}_{p3} \ 0]' [\mathbf{C}_{p3} \ 0] \quad (18)$$

and

$$\mathbf{R} = k_v. \quad (19)$$

Through the solution of an algebraic Riccati equation [13], a state feedback matrix K can be found that minimizes the objective function J .

A. Observer Design

As the state variables of the system $x_g(t)$ are not available directly, a linear observer is required.

For impedance design, the *ad hoc* pole placement approach to linear observer design becomes difficult. Although an LQR state-feedback regulator is guaranteed (if \mathbf{R} is chosen diagonal) to result in a phase margin of at least 60° at each plant input channel [14], [15], it is well known that considerable degradation of the stability margins is to be expected after inclusion of the observer dynamics. A more automated choice in observer design is the Kalman filter [16]. Here, as shown in Fig. 10, the controller $C(s)$ consists of an optimal state-feedback regulator K and Kalman observer O . By the Certainty Equivalence Principle or Separation Theorem [13], the two entities can be designed independently. After first finding a K to minimize (17), we then design a Kalman filter to minimize

$$J_k = \lim_{t \rightarrow \infty} E \{ [x(t) - \tilde{x}(t)] [x(t) - \tilde{x}(t)]' \}. \quad (20)$$

By the Certainty Equivalence Principle, the optimal K and O also result in minimization of the stochastic performance objective

$$J = E \left\{ \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T \{x'(t) \mathbf{Q} x(t) + u(t)' \mathbf{R} u(t)\} dt \right\}. \quad (21)$$

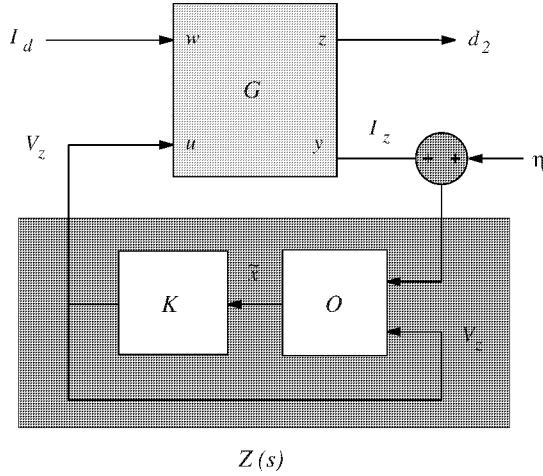


Fig. 10. Composite plant G controlled by $Z(s)$, an impedance consisting of the optimal state-feedback regulator K and Kalman filter O .

In this scenario, we are referring to the original state-space system (12) with zero-mean uncorrelated Gaussian process models for the disturbance I_d and additive measurement noise η . With the inclusion of measurement noise, the system representation (12) becomes

$$\begin{aligned} \dot{x}_g &= \mathbf{A}_g x_g + \mathbf{B}_g \begin{bmatrix} I_d \\ V_z \end{bmatrix} \\ \begin{bmatrix} d_2 \\ I_z \end{bmatrix} &= \mathbf{C}_g x_g + \begin{bmatrix} 0 \\ \eta \end{bmatrix} \end{aligned} \quad (22)$$

where I_d and η satisfy

$$\begin{aligned} E\{I_d I_d'\} &= \mathbf{Q}_n \\ E\{\eta \eta'\} &= \mathbf{R}_n. \end{aligned} \quad (23)$$

Based on \mathbf{Q}_n and \mathbf{R}_n , a Kalman observer that minimizes (20) can be found through the solution of an algebraic Riccati equation [13]. The ratio of \mathbf{Q}_n to \mathbf{R}_n essentially represents the confidence in the measured variable I_z and plant model G . In this work, \mathbf{Q}_n , \mathbf{R}_n , and \mathbf{k}_u are not quantified and are simply treated as design parameters influencing the closed-loop pole locations, damping performance, and closed-loop stability.

IV. EXPERIMENTAL RESULTS

To verify the modeling and design techniques presented in the preceding sections, each method has been applied to an experimental electromechanical system.

A. Experimental Apparatus

A photograph of the experimental apparatus showing the rigid body, flexible end supports, mounting plate, and coils is provided in Fig. 11. As shown in Fig. 12, the apparatus comprises two electromagnetic transducers mounted vertically. While the lower magnet and flexure is fixed, the two connected transducer cases are free to vibrate and represent the mass M_2 . The upper magnet forms the absorber mass M_1 . Each transducer is essen-

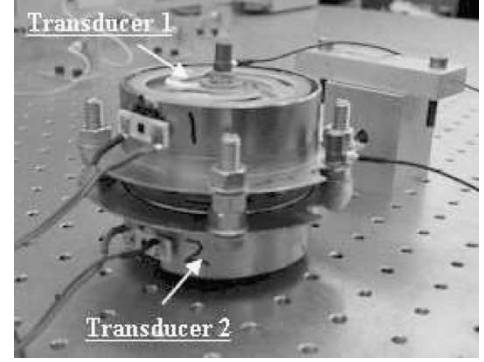


Fig. 11. Experimental apparatus.

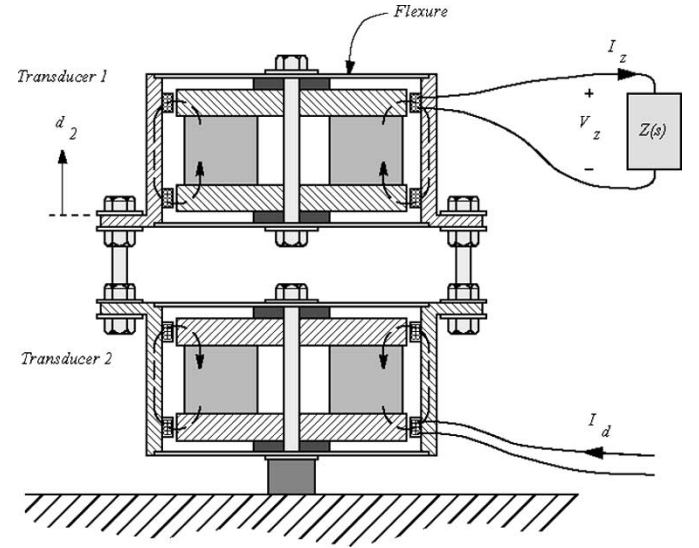


Fig. 12. Cross section of the experiment apparatus shown in Fig. 11.

TABLE I
ELECTROMECHANICAL SYSTEM PARAMETERS

Parameter	Value
Spring constant k_1	28.03 kNm^{-1}
Damping coefficient b_1	1.500 Nsm^{-1}
Absorber mass M_1	0.340 kg
Spring constant k_2	31.14 kNm^{-1}
Damping coefficient b_2	3.582 Nsm^{-1}
Absorber mass M_2	0.593 kg
Coil inductance	41 mH
Coil resistance	2.315 Ω
Electromagnetic Coupling C_e	3.408
Electromagnetic Coupling C_d	-6.714

tially a translational solenoid with two identical coils connected in series; the dashed line identifies the flux path generated by the permanent magnets. The physical parameters of the electromagnetic and mechanical systems are summarized in Table I.

The main mass velocity d_2 is measured using a PSV-300 Polytec Scanning Laser Vibrometer.

B. Power Amplifier and Instrumentation

In order to implement an arbitrary shunt impedance, a power amplifier was developed capable of driving differential terminal

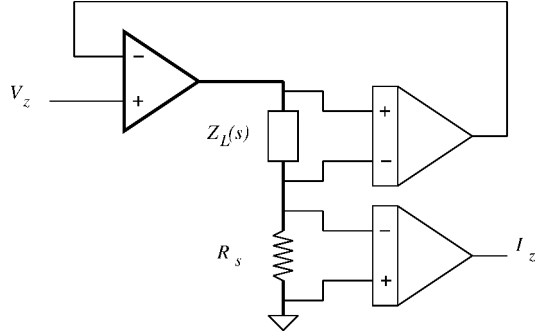


Fig. 13. Simplified schematic of a voltage source with current instrumentation. The load impedance $Z_L(s)$ represents the electromagnetic coil.

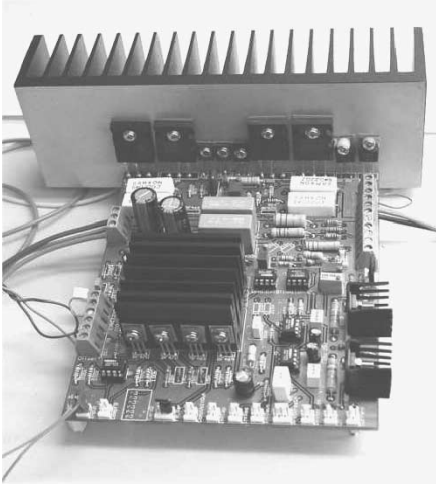


Fig. 14. Practical implementation of a voltage amplifier with current instrumentation.

voltages with load current instrumentation. The simplified schematic of a circuit realizing this function is shown in Fig. 13. A practical implementation of the amplifier is shown in Fig. 14. The device is capable of ± 200 V operation at a maximum dc current of 32 A. Further analysis and a more detailed discussion of the implementation can be found in [17]. A dSpace 1005 based system is used to implement the required impedance and admittance transfer functions.

C. Impedance Synthesis

Fig. 15 shows the instrumentation and driver gains associated with the underlying electromechanical system. The voltages V_1 – V_4 represent the signals applied to, or measured from, the power amplifiers and instrumentation, respectively. The gain and units associated with each signal can be found in Table II. The actual electrical shunt impedance presented to the coil is related to the controller through the gains a_3 and a_4 ; specifically,

$$Z(s) = \frac{V_z(s)}{I_z(s)} = a_3 C(s) a_4. \quad (24)$$

To assess the accuracy of the analytic model (discussed in Section II-C), the simulated frequency response is compared to that measured directly from the experimental system. A multi-

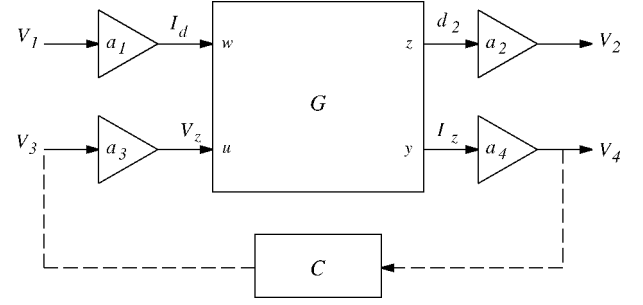


Fig. 15. External gains associated with the amplifier and instrumentation.

TABLE II
EXTERNAL GAINS ASSOCIATED WITH THE EXPERIMENTAL SYSTEM

Gain	Value
a_1	1.006 A/V
a_2	1 V/m
a_3	-1.012 V/V
a_4	-10.01 V/A

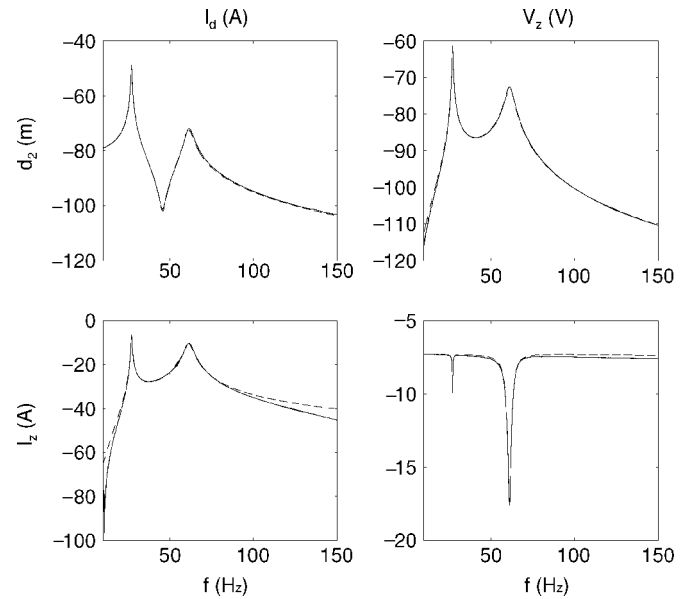


Fig. 16. Simulated (—) and experimental (---) magnitude frequency response.

variable frequency response is measured successively from each input to output pair. During the component SISO frequency response measurements, the residual input is set to zero. The magnitude and phase frequency responses are shown, respectively, in Figs. 16 and 17. In the frequency domain, a good correlation can be observed between the analytic model and measured system.

1) *LQR Impedance Synthesis*: As discussed in Section III, a linear quadratic regulator can be designed to command the shunt terminal voltage V_z with a view to minimizing the vibration d_2 . An observer is required to estimate the system states from the measured shunt current I_z .

Based on the physical model that was validated perviously, and referring to the notation introduced in Section III, an *LQR*

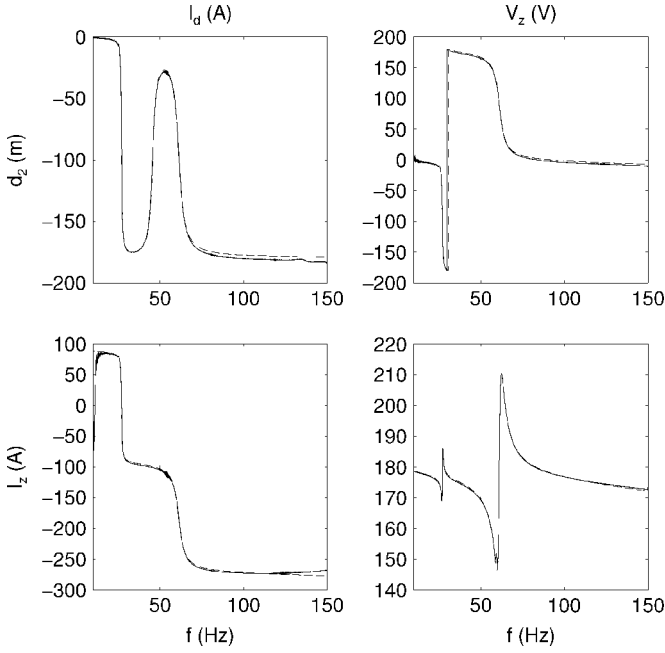


Fig. 17. Simulated (—) and experimental (---) phase frequency response.

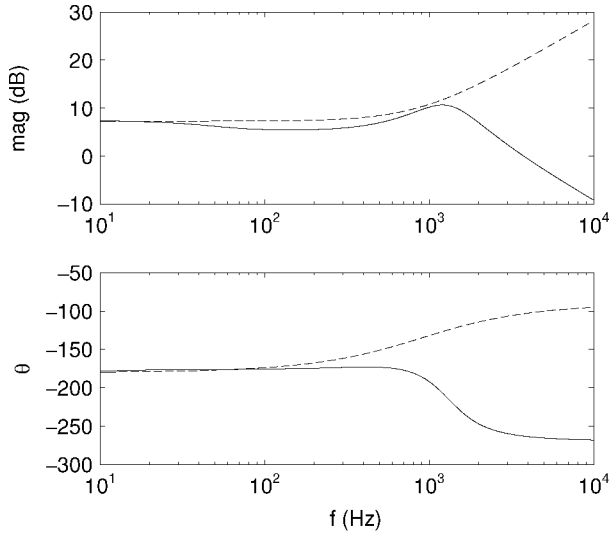


Fig. 18. Magnitude and phase response of the LQG impedance (—) and negative coil impedance (---).

gain matrix was designed to minimize the performance function

$$J = \int_{-\infty}^{\infty} \{d_2^2(t) + k_v V_z^2(t) + k_d (d_1(t) - d_2(t))^2\} dt \quad (25)$$

where the factors $k_d = 1$ and $k_v = 1 \times 10^{-7}$. A Kalman observer was designed to estimate the system state $x_g(t)$ utilizing the measured shunt transducer current I_z and control signal V_z . Referring to Section III-A, the disturbance and output noise process covariance matrices \mathbf{Q}_n and \mathbf{R}_n were chosen to be 100 and 0.1, respectively. Such a weighting, although not quantitative, expresses a moderate confidence in the fidelity of the measured variable I_z .

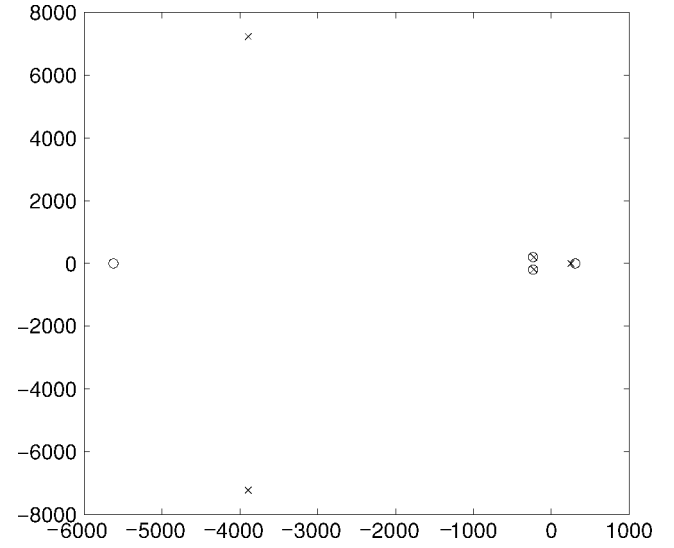


Fig. 19. Pole-zero map of the LQG impedance.

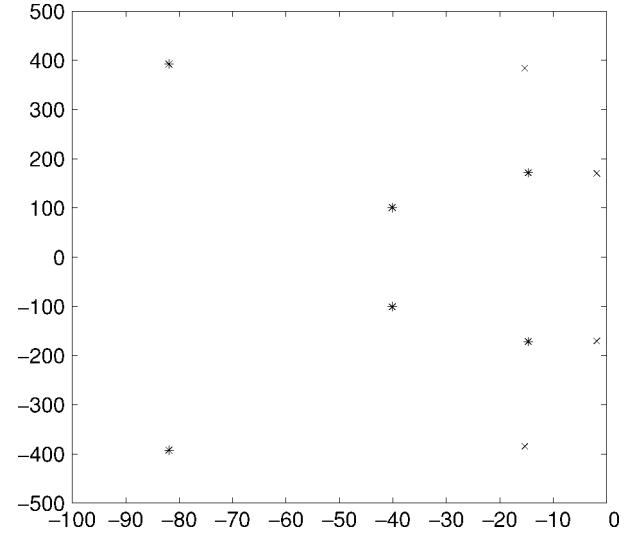


Fig. 20. Open (×) and shunted (*) pole locations. Note that one pair of high-frequency observer poles are not visible within the scope of this plot.

By concatenating the *LQR* gain matrix and Kalman observer, and compensating for the system gains a_3 and a_4 , the actual impedance presented to the shunt transducer can be determined. In Fig. 18, the complex impedance of the resulting controller is plotted together with that of the negated coil impedance. A negative coil impedance connected to the true coil impedance effectively removes the source impedance from the transducer. The *LQG* impedance has a tendency to mimic this impedance over a certain frequency range. The pole-zero map of the *LQG* controller is shown in Fig. 19.

After examining the open- and closed-loop pole locations shown in Fig. 20, it can be appreciated that the controller is clearly acting to increase the system damping. Corresponding mitigation of the transfer function from an applied disturbance to the measured vibration can be seen in both the frequency

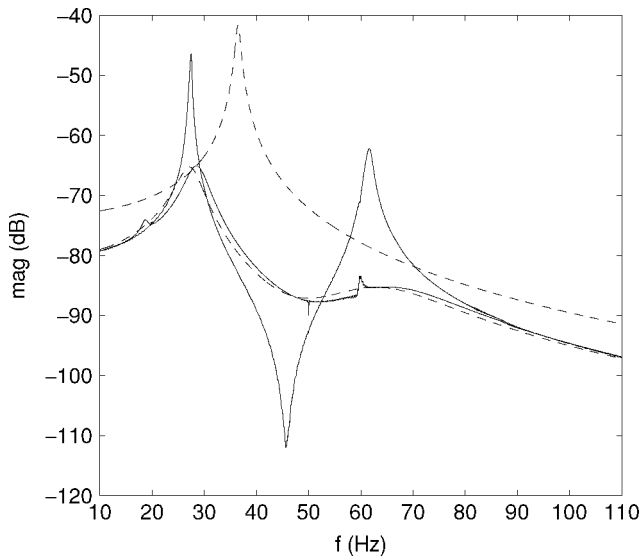


Fig. 21. Single-mass (---), two-mass (—), experimental shunted (—), and simulated shunted (---) magnitude frequency response $d_2(s)/I_d(s)$.

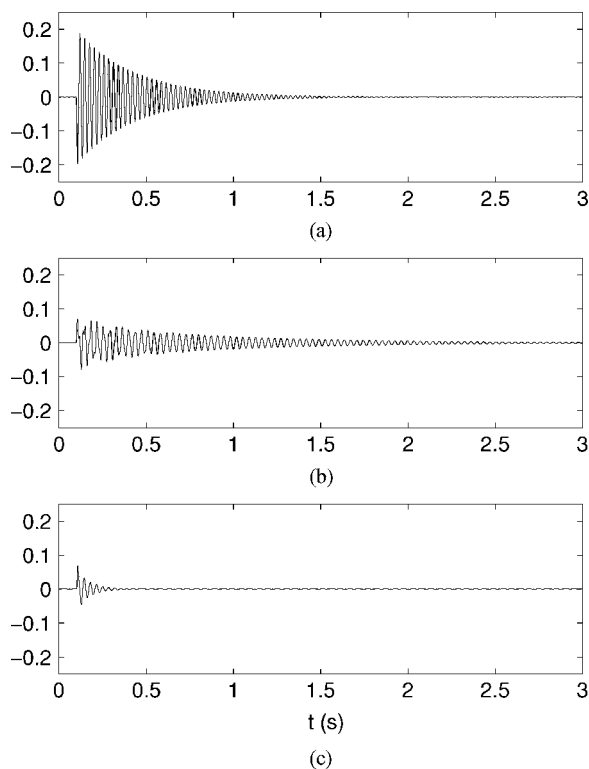


Fig. 22. Single-mass. (a) Two-mass. (b) Shunted two-mass. (c) Velocity response to a 1-A step in I_d .

domain, Fig. 21, and time domain, Fig. 22. The action of the additional mass and electromagnetic shunt acts to reduce the single-mass resonant peak by a minimum of 23.2 dB. The shunted electromagnetic transducer reduces the two-mass first and second resonant peaks by 18.7 and 23.6 dB, respectively.

The reader may note additional dynamics at 20 and 60 Hz in Fig. 21. These dynamics are due to pivot modes of the structure

about the base fixture. The stiffening effect of the controller has a tendency to increase the frequency of low-profile pivot and sway modes. Such modes would be absent in a more rigidly supported inertial drive.

V. CONCLUSION

A technique has been presented for the control of vibration using an electromagnetically actuated inertial drive. By viewing the coil current and voltage as system inputs and outputs, standard synthesis techniques were applied to minimize displacement subject to a penalty on the inertial mass travel and applied terminal voltage. Electromagnetic shunt control requires no external sensors, and thus significantly reduces the cost, complexity, and sensitivity to transducer failure of active vibration control systems.

Experiments were performed on a simple apparatus representing a scenario where the vibration experienced by a host structure is controlled with a suspended absorber mass and electromagnetic coil. In practice, the mass of the absorber is usually limited to about one tenth the host structure. In this regard, the experiment is somewhat unrealistic, as the mass of the absorber is only slightly less than that of the host mass. The available control authority is directly related to both the size of the mass and the available travel.

After adding the absorber mass, the passive dynamics split the original resonant mode into two lightly damped secondary peaks. Then, by designing a suitable control impedance and presenting it to the terminals of the electromagnetic coil, further vibration reduction is achieved by augmenting the passive damping of the secondary modes. As the control design penalizes the absorber mass travel, which increases at low frequencies, the impedance suppresses higher frequency vibration more heavily. The combination of passive and active dynamics reduces the displacement response to a force input by up to 38 dB at the frequency of the original resonance.

Future work includes design for multimode host structures, coupled multidrive multidimensional systems, and restricted impedance design. The *LQG* impedance design contains negative reactive components and is unstable in a systems perspective. Although the connection of the coil and control impedance is stable, an inherently stable controller is desirable. It is presently unclear whether an unstable controller is necessary to result in effective vibration reduction.

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