

Influence of Nonlinear Fluid Viscous Dampers on Seismic Response of RC Elevated Storage Tanks

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Abstract

The numerical investigation on the seismic response of RC elevated liquid storage tanks installed with viscous dampers is presented. A discrete two-mass model for the liquid and multi-degree of freedom system for staging, installed with the dampers are developed for Reinforced Concrete (RC) elevated liquid storage tanks. The elevated tank is assessed for seismic response reduction when provided with Linear Viscous Damper (LVD) and Nonlinear Viscous Damper (NLVD), installed in the staging. The RC elevated liquid storage tanks are analyzed for two levels of liquid containment in the tank, 100% and 25% of the tank capacity. Three Configurations of placements of dampers viz. dampers at alternate levels (Configuration I and Configuration II) and dampers at all the panels of the staging of the tank (Configuration III) are considered. To study the effect of peak ground acceleration, eight real earthquake time histories with accelerations varying from 0.1 g to 0.93 g are considered. The nonlinearity in the viscous damper is modified by taking force proportional to various velocity exponents. It is found that the nonlinear viscous dampers with lower damping constant result in a comparable reduction in the response of RC elevated liquid storage tank, to that of linear viscous dampers with higher damping constant. A lower damping constant signifies compact the size of the damper.

Keywords: RC Elevated Liquid Storage Tank; Linear Fluid Viscous Damper; Nonlinear Fluid Viscous Damper; State-space; Seismic Analysis.

1. Introduction

The seismic safety of liquid storage tanks is of prime importance, and their response should be controlled using various control strategies. Liquid storage tanks are considered as lifeline structures and should remain functional during and after the earthquakes. Their performance during strong earthquakes is of critical concern. Most of the failures of large tanks during earthquakes are suspected of having resulted from the dynamic buckling caused by overturning moments of seismically induced liquid inertia and liquid surface slosh waves. Due to its complex dynamics and variable liquid levels, behavior of the elevated liquid storage tank cannot be estimated by the similar approaches used in the case of the high-rise buildings.

Several research works reported in the literature, guidelines, and specifications in international codes are available for seismic analysis and design of the liquid storage tanks. Housner (1963) [1] studied the dynamic behavior of ground supported and elevated water tank. Further, Haroun and Housner (1982) [2]; and Haroun [3] carried out vibration studies on ground supported, deformable cylindrical water tanks; and derived parameters of the mechanical model.

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Apart from these studies, many researchers have worked on modeling of sloshing in containers and liquid dynamics. Ibrahim et al. [4] carried out extensive review of recent advances in liquid sloshing dynamics; further, the two equivalent mechanical models for modeling sloshing, namely mass-spring dashpot and pendulum models were discussed [5].

Specifications in international codes such as ACI 350.3 [6], and EN 1998-4 [7] are available for seismic analysis and design of RC liquid storage tanks. Jain and Jaiswal [8] and; Tung and Kiremidjian [9] illustrated the analysis procedure for elevated RC tanks considering two-mass model for liquid and assuming single lumped mass for the staging of the tank. Malhotra [10] carried out studies on ground supported base isolated tanks focusing on base shear, overturning moment, and axial compressive stresses. It was found that convective action does not contribute significantly to the overturning moment. Shenton III and Hampton [11] carried out response spectrum analysis of base isolated steel elevated water tanks, and found that seismic isolation is effective in reducing the tower drift, base shear, overturning moment, and tank wall pressures with a slight increase in convective displacement. Shrimali and Jangid [12], carried out studies on base isolated elevated steel liquid storage tanks considering two positions of isolators; at the top and bottom of the supporting tower structure. Abali and Uckan [13], carried out a parametric study on ground supported base isolated liquid storage tanks using FPS bearings. It was found that FPS would be effective in controlling the response of the slender tank compared to the broad tank. Moslemi et al. [14] used the finite element technique to investigate the seismic response of liquid filled tanks. It was concluded that the current practice of using the lumped mass technique as per ACI 350.3 standard in conjunction with ASCE 7-05, predicts the results with reasonable accuracy. Further, studies are carried out on water tank with different types of isolators viz. lead rubber bearing, variable frequency pendulum isolator and multiple friction pendulum system, by Shrimali and Jangid [15]; Panchal and Jangid [16], and Zhang et al. [17], respectively. Chalhoub and Kelly [18], carried out experimental study on base isolated cylindrical water tank. It was concluded that the low frequency that characterizes the motion of base isolated structures could be close to the sloshing frequencies of the contained fluid and affect the water displacement response. The researchers used two-mass model approach or three-mass model approach for modeling of liquid. The significant difference between these models is the number of lumped masses into which the liquid column is divided. Earthquake response of slender and broad liquid storage steel tanks isolated with variable curvature friction pendulum systems (VCFPS) was investigated by Panchal and Jangid [19]. It was observed that under near-fault ground motions, use of the VCFPS was quite effective in controlling the seismic response of liquid storage tanks. A brief review of the literature, related to the response of base-isolated structures under near-fault earthquakes and representation of near-fault earthquake motion using equivalent pulses, was presented by Saha et al. [20]. It was found that, the response reduction increases with the increase in isolation damping; however, the sloshing displacement was found to be less sensitive to the change in the isolation damping. Studies have also been reported for the ground-supported liquid storage tanks with semi-active dampers [21, 22], and elevated water tank with friction dampers [23].

During the earthquake, forces are induced in the elevated liquid storage tanks, which may lead to their failure. Many times, the conventional seismic resistant design approach without sophisticated vibration control devices cannot provide sufficient protection against the earthquake-induced forces. In aseismic design, either the elevated tanks are increased in their strength or the large mass of liquid is isolated. However, an alternate option is to install dampers in the staging. Supplemental dampers are especially suitable for tall structures which are generally not base-isolated owing to their flexibility, i.e. longer time periods. In order to reduce the seismic response of the liquid storage tanks, base isolation technique is effectively used by several researchers. It was found that the base isolation technique is effective in reducing base shear, while sloshing displacement is marginally increased.

Dampers have been effectively used for retrofitting works [24-26]. Also, in structures with high fundamental time period of vibration dampers have been proved to be very effective [27]. However, viscous dampers have not been examined for their use as seismic response control device for the elevated liquid storage tanks. Also, it is noted that previous researchers have considered staging of the elevated water tank as single lumped mass, which could not replicate the true response of the tank to the dampers, as dampers are to be installed in the staging. Hence, appropriate modeling of the elevated liquid storage tanks incorporating dampers is required to facilitate examining their effectiveness.

The specific objectives of the present study are: (i) to evaluate the seismic response of the RC elevated liquid storage tanks modeled with two- mass model of liquid and multi-degree of freedom system for staging, (ii) to study the influence of the velocity exponent, α on the effectiveness of viscous dampers with increased nonlinearity, (iii) to compare the seismic response of the RC elevated liquid storage tank installed with linear viscous dampers (LVDs) and nonlinear viscous dampers (NLVDs) subjected to eight different real earthquake ground motions; and (iv) to investigate the effect of positions of fluid viscous dampers on the response of the RC elevated liquid storage tanks.

The paper is organized in seven sections. This introduction section is followed by Section 2, which explains in brief the research methodology adopted in the paper. Section 3 describes the modeling of elevated liquid storage tank, where the two-mass model for liquid and multi-degree freedom system for framed staging is explained. Section 4 describes

the modeling of fluid viscous damper. The numerical modelling of the tank installed with fluid viscous damper along with the procedure for solution of governing equation of motion is illustrated in Section 5. Further, Section 6 presents the numerical study and results. Main conclusions of the study are presented in Section 7.

2. Research Methodology

The research methodology is divided into three steps. The first step is mathematical modeling of RC elevated liquid storage tank and Fluid viscous damper. The second step MATLAB code is written for numerical modelling and solution of governing equation of motion by state-space method. In the final step, the seismic response of the RC tank without and with fluid viscous dampers (linear and nonlinear) is obtained. All the steps are discussed in detail in the succeeding sections from Section 3 to Section 6. Figure 1 illustrates the methodology.

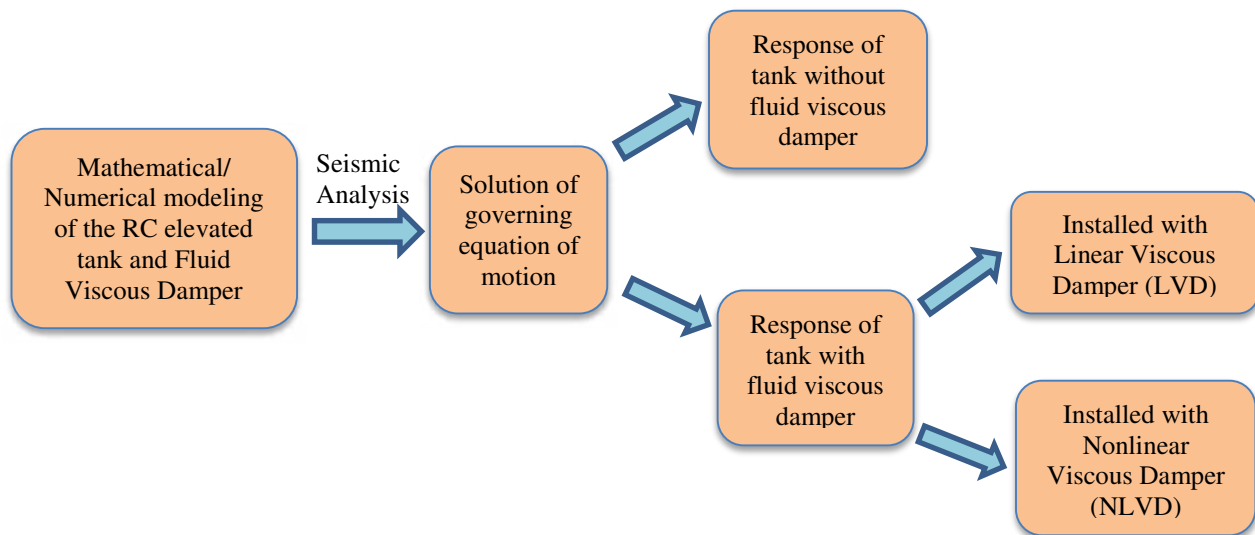


Figure 1. Research methodology

3. Modeling of Elevated Liquid Storage Tank

Previous study by (Jain, 2005) Jain and Jaiswal [8] showed that for analysis of the RC elevated liquid storage tanks, the container is considered rigid. Hence, the two-mass model can be conveniently used, which has also been recommended by the ACI 350.3 [6] and European standards, EN 1998-4 [7]. In the present study, a two-mass model with multi-degree freedom staging for the RC elevated liquid storage tank without and with dampers is presented. The response of tank, wherein fluid idealized as two-mass, is evaluated using the mechanical analog proposed by Housner [1], Haroun and Housner [2], and Housner [3]. In order to include the effect of the hydrodynamic pressure in the analysis, the tank is idealized by an equivalent spring mass model, which takes into account the effect of tank wall-liquid interaction [1, 2, 3, 6, 7]. The following assumptions are made for the structural system under consideration [28]:

- The superstructure, i.e., structure of the tank above ground level, is considered to remain elastic during the earthquake excitation. This is a reasonable assumption, as the supplementary dampers attempt to reduce the earthquake response in such a way that the structure remains within elastic range.
- The tanks are with circular plan geometry, supported on staging, which consists of the inextensible columns providing vertical support and lateral stiffness.
- The system is subjected to a single horizontal component of the earthquake ground motion.
- The effects of soil-structure interaction (SSI) are not taken into consideration.

Figure 2 (a) shows the idealized schematic diagram of the RC elevated liquid storage tank considered in the study. Figure 2 (b) and Figure 2 (c) show the model of the tank with Configuration I and Configuration II for placement of the fluid viscous dampers installed in the staging. The case of installation of dampers at all the levels of staging is considered as Configuration III (Figure 2 (d)). Figure 2 (d) presents the mathematical model of the RC elevated liquid storage tank installed with the dampers (Configuration III). The parameters of the tanks considered are liquid column height (H), radius (R), and height of staging (H_{st}). The relative convective mass displacement, rigid mass displacement, and displacements at the horizontal bracing levels are denoted by x_c , x_r , and x_1, \dots, x_p , respectively, where p is number of panels in the staging; \ddot{u}_g represents the earthquake ground acceleration. Further, m_1, m_2, \dots, m_p are the lumped masses at the bracing levels of the staging; m_{tb} is the mass of tank base including floor beams; m_{tw} is mass of tank wall

including roof slab, and m is the mass of liquid.

$$m = \pi R^2 H \rho_l \quad (1)$$

In Equation 1, ρ_l is the density of the contained liquid

3.1. Two-mass Model

Two-mass model was originally proposed by Housner [1] and later adopted by several researchers. The modified Housner's model presented in the ACI: 350.03 [6] is used in the present study. Figure 2 shows the schematic diagram of the tank model showing total height of the liquid inside the tank denoted by H and radius for circular tank denoted by R . In this model, the convective mass (m_c) of the liquid is considered to be connected to the solid tank wall with stiffness (k_c) at height H_c from the base of the container, whereas the rigid mass (m_r) is connected rigidly to the tank wall with stiffness (k_i) at a height H_r , while H_{st} denotes the height of the staging. The stiffness of the spring attached to the convective mass (k_c) given by Equation 2, and the natural frequency of convective mass of liquid (ω_c) are given by Equation 3.

$$k_c = \frac{1.84 m_c g}{R} \tanh(1.84 S) \quad (2)$$

$$\omega_c = \sqrt{\frac{k_c}{m_c}} \quad (3)$$

Where, g is the gravitational acceleration and $S = H/R$ is the aspect ratio of the liquid column.

$$C_c = 2 \xi_c m_c \omega_c \quad (4)$$

In Equation 4 C_c is the damping coefficient and ξ_c is the damping ratio of the convective mass. If t_w is the thickness of wall; the spring stiffness attached to the impulsive mass is given by, $k_i = m_i (\omega_i)^2$. The natural frequency of impulsive mass of liquid (ω_i) is obtained through Equations 5 to 7.

$$\omega_i = C_I \frac{1}{H} \sqrt{\frac{10000E}{\rho_c}} \quad (5)$$

$$C_I = C_w \sqrt{\frac{t_w}{10R}} \quad (6)$$

$$C_w = 0.09375 + 0.2039 \left(\frac{H}{2R}\right) - 0.1034 \left(\frac{H}{2R}\right)^2 - 0.1253 \left(\frac{H}{2R}\right)^3 + 0.1267 \left(\frac{H}{2R}\right)^4 - 0.03186 \left(\frac{H}{2R}\right)^5 \quad (7)$$

The sloshing mass (m_c) and mass rigidly connected to the container (m_r) are expressed in terms of the total mass (m) of the liquid as explained in Equations 8 and 9.

$$\gamma_c = \frac{m_c}{m} = \frac{0.46}{S} \tanh(1.84 S) \quad (8)$$

And:

$$\gamma_r = \frac{m_r}{m} = \frac{S}{1.732} \tanh\left(\frac{1.732}{S}\right) \quad (9)$$

Sloshing mass height (H_c) and impulsive mass height (H_r) are given by Equations 10 and 11, respectively.

$$\frac{H_c}{H} = 1 - \frac{\cosh(1.84 S) - 2.01}{(1.84 S) \sinh(1.84 S)} \quad (10)$$

$$\frac{H_r}{H} = \frac{0.866}{S} \coth\left(\frac{1.732}{S}\right) - 0.125 \quad (11)$$

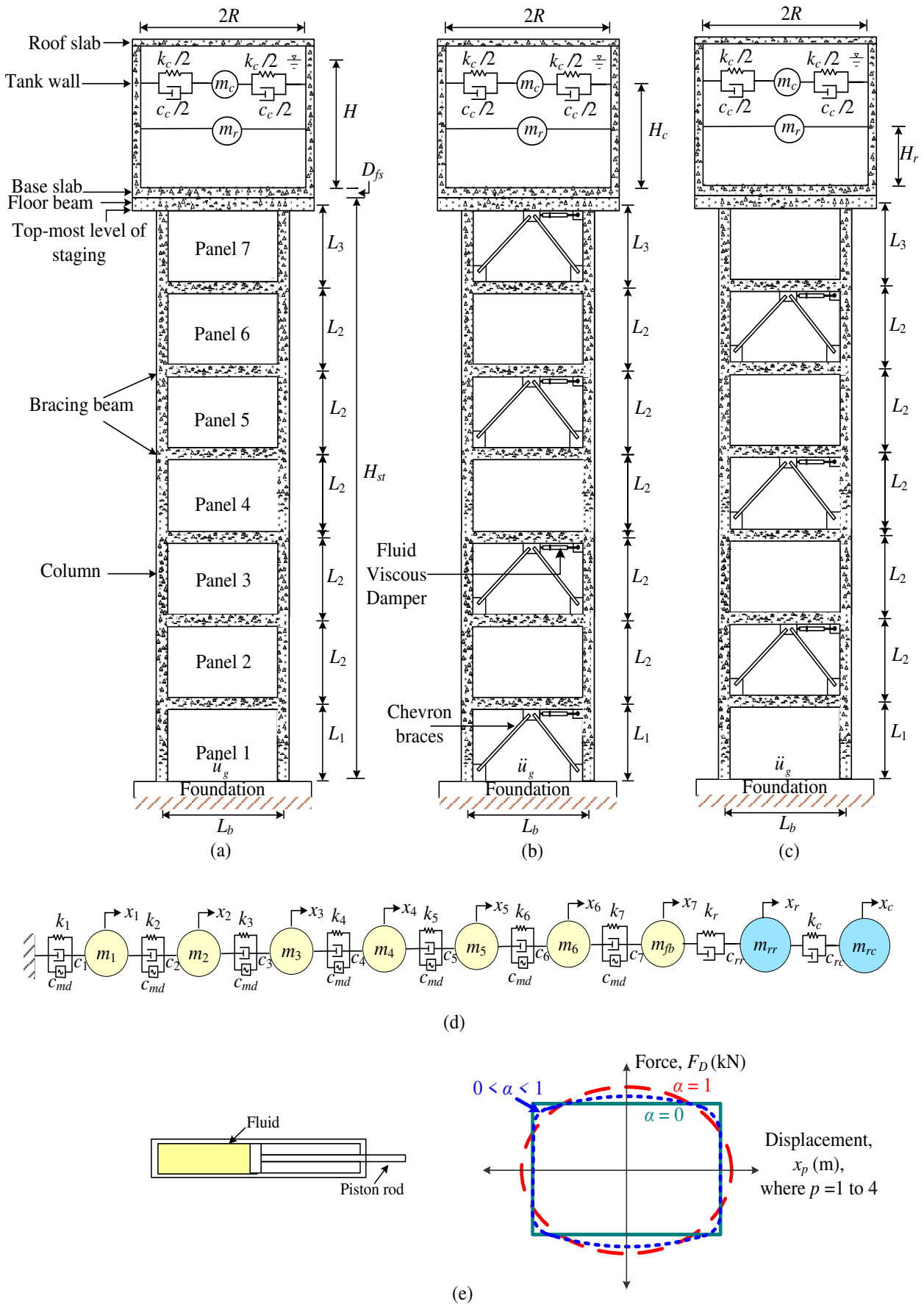


Figure 2. Schematic diagram of (a) the RC elevated liquid storage tank, (b) Configuration I for placement of dampers (c) Configuration II for placement of dampers (d) Mathematical model of the RC elevated liquid storage tank with fluid viscous dampers, and (e) Fluid viscous damper along with force-displacement loops for linear ($\alpha = 1$) and nonlinear ($0 < \alpha < 1$) fluid viscous dampers.

$$m_{fb} = m_{ib} + 0.5m_{top} \quad (19)$$

In Equation 19, m_{fb} is the top-most level mass of the staging; m_{top} is the contribution of mass from the top-most panel of the staging, c_{rr} is the damping associated with k_i and m_{rr} ; while c_{rc} is the damping associated with k_c and m_{rc} .

4. Modeling of Fluid Viscous Damper

Design of the Fluid Viscous Damper (FVD) is based on inertial flows, where non-flammable, non-toxic, environmentally safe, and thermally stable, silicone oil is forced through small orifices at high speeds (more than 200 m/s), generating high damping forces. This allows the damper to operate at relatively high operating pressures [24]. The output of this device is not affected by viscosity changes of the fluid. The control force (F_D), offered by the fluid viscous damper as given by Goel [25] is,

$$F_D = C_{md} |\dot{u}|^\alpha \operatorname{sgn}(\dot{u}) \quad (20)$$

Where, C_{md} is the damping constant associated with every fluid viscous damper depending on its design; \dot{u} is the relative velocity between two ends of the damper; α is the exponent varying between 0 and 1; and $\operatorname{sgn}(\cdot)$ is the signum function. The damper with $\alpha = 1$ is called as linear viscous damper (LVD), in which damping force is directly proportional to the velocity; while, the damper with $\alpha \neq 1$ is called as nonlinear viscous damper (NLVD). A damper with $\alpha = 0$ exhibits rectangular force-displacement loop resembling the friction damper. Figure 2 (e) shows schematic of fluid viscous damper and the force-displacement hysteresis loops for the LVD, NLVD-I, and NLVD-II in accordance with their energy dissipation characteristics.

5. Numerical Modeling and Solution

In this section, numerical modeling procedure and solution of governing differential equations for time history analysis of the RC elevated liquid storage tank, with staging modeled as multi-degree of freedom system, installed with the viscous damper is illustrated.

5.1. Equation of Motion

The governing differential equation of motion under earthquake excitation, with added supplemental viscous dampers, is given by Equation 21.

$$[M]\{\ddot{X}(t)\} + [C]\{\dot{X}(t)\} + [K]\{X(t)\} = \{F_e(t)\} + [L]\{f_c(t)\} \quad (21)$$

Where, $[M]_{n \times n}$ is mass matrix; $[K]_{n \times n}$ is stiffness matrix; and $[C]_{n \times n}$ is damping matrix. The control force distribution matrix; $[L]_{n \times n}$ is given by Equation 22.

$$[L] = \begin{bmatrix} 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (22)$$

Where, $\{F_e(t)\} = \{F_1(t), F_2(t) \dots F_n(t)\}^T$ is a vector such that $\{F_e(t)\} = -[M]\{r\}\ddot{u}_g(t)$ where, $\{r\} = \{1, 1, \dots, 1\}^T$ is the influence coefficient vector. Here, the degrees of freedom are: $n = 9$. Also, $\{f_c(t)\} = \{F_{D1}(t), F_{D2}(t), \dots, F_{Dn}(t)\}^T$ is a vector containing the control force exerted by the dampers corresponding to each degree of freedom, n . Moreover, $\{X(t)\}$ is the vector of displacement of the masses relative to the ground, expressed as:

$$\{X(t)\} = \{x_1(t) \quad x_2(t) \quad \dots \quad x_r(t) \quad x_c(t)\}^T \quad (23)$$

In Equation 23, $x_1 = (d_1 - u_g)$, $x_2 = (d_2 - u_g)$, ..., $x_r = (d_r - u_g)$, $x_c = (d_c - u_g)$; u_g is the ground displacement; and d_c , d_r , and $d_p \dots, d_1$ are the absolute displacements at the level of convective mass level, rigid mass level, and bracing level masses, respectively.

The hydrodynamic forces are imparted on the tank wall, which transmits forces on the staging underneath. The seismic forces induced in the staging are controlled using the fluid viscous dampers. Therefore, the effectiveness of such supplementary damping system is assessed in terms of the reduction of displacements, base shear, and overturning moment generated in the staging of the elevated tank during earthquake. The base shear, V_b (Equation 24) and the overturning moment, M_o (Equation 25) in the staging at the foundation level are expressed as:

$$V_b = m_{rc} a_c + m_{rr} a_r + \dots + m_3 a_3 + m_2 a_2 + m_1 a_1 \tag{24}$$

$$M_o = m_{rc} a_c (H_c + D_{fs} + H_{st} + \frac{D_{fb} - D_{fs}}{2}) + m_{rr} a_r (H_r + D_{fs} + H_{st} + \frac{D_{fb} - D_{fs}}{2}) + \dots + m_3 a_3 (2L_2 + L_1) + m_2 a_2 (L_2 + L_1) + m_1 a_1 L_1 \tag{25}$$

Where, the height of the staging, $H_{st} = L_1 + (p - 2)L_2 + L_3$, D_{fs} is the depth of floor slab, and D_{fb} is the depth of floor beam. The absolute accelerations at the different level of masses are denoted by $a_c, a_r, a_p, \dots, a_2, a_1$.

5.2. State-space Solution

In the state-space method, the response of the system is analyzed using both; displacement and velocity, as independent variables, called as states [30]. Vector, $z(t)$ is defined to represent both states viz. displacement and velocity of the system. These two independent response variables in the present study are expressed as Equation 26:

$$z(t) = \begin{Bmatrix} X(t) \\ \dot{X}(t) \end{Bmatrix} \tag{26}$$

Every degree of freedom is associated with two states, viz. displacement and velocity. Thus, if the degree of freedom of a structure is n , then there will be $2n$ states, first n for the displacement and remaining n for the velocity. It follows that Equation 21 can be written in the equivalent state-space form presented in Equation 27.

$$\dot{z}(t) = \begin{Bmatrix} \dot{X}(t) \\ \ddot{X}(t) \end{Bmatrix} = \begin{bmatrix} \mathbf{0} & \mathbf{I} \\ -\mathbf{M}^{-1}\mathbf{K} & -\mathbf{M}^{-1}\mathbf{C} \end{bmatrix} \begin{Bmatrix} X(t) \\ \dot{X}(t) \end{Bmatrix} + \begin{Bmatrix} \mathbf{0} \\ \mathbf{M}^{-1}\mathbf{F}_e(t) \end{Bmatrix} + \begin{Bmatrix} \mathbf{0} \\ \mathbf{M}^{-1}\mathbf{L}f_c(t) \end{Bmatrix} \tag{27}$$

Where, $\mathbf{0}$ and \mathbf{I} are respectively null matrix with all zero elements and identity matrix. Equation 27 can be simplified as,

$$\dot{z}(t) = \mathbf{A}z(t) + \mathbf{F}(t) \tag{28}$$

Where,

$$\mathbf{A} = \begin{bmatrix} \mathbf{0} & \mathbf{I} \\ -\mathbf{M}^{-1}\mathbf{K} & -\mathbf{M}^{-1}\mathbf{C} \end{bmatrix} \tag{29}$$

$$\mathbf{F}(t) = \begin{Bmatrix} \mathbf{0} \\ \mathbf{M}^{-1}(\mathbf{F}_e(t) + \mathbf{L}f_c(t)) \end{Bmatrix} \tag{30}$$

Equation 28 is the first-order linear differential equation, called as continuous state-space equation of motion. If t_0 represents the time when the initial displacement and velocity are given, the solution to above equation for any time $t > t_0$ can be written as,

$$z(t) = e^{\mathbf{A}(t-t_0)} z(t_0) + e^{\mathbf{A}t} \int_{t_0}^t e^{-\mathbf{A}s} \mathbf{F}(s) ds. \tag{31}$$

To integrate the forcing function $F(s)$ in Equation 31, the method of numerical integration is used. If $t_{k+1} = t$, $t_k = t_0$, $\Delta t = t - t_0$, and $t_k \leq s \leq t_{k+1}$, using delta forcing function Equation 31 can be written as,

$$z_{k+1} = e^{\mathbf{A}\Delta t} z_k + \Delta t e^{-\mathbf{A}t} \mathbf{F} \tag{32}$$

Equation 32 leads to the displacement and velocity at time step $k + 1$, while the acceleration is obtained through Equation 28. Time history analysis is carried out, and response quantities viz. displacements, base shear, overturning moment, and damper force are obtained.

For the elevated RC liquid storage tank with linear viscous dampers installed in its staging, the seismic response reduction is quantified as compared to the uncontrolled response, i.e., staging without dampers. Percentage reduction of the peak seismic response quantities for the cylindrical elevated RC tanks is calculated. For example, the percentage reduction in the convective displacement in x -direction (x_c) is calculated as,

$$\% \text{ Reduction in } x_c = \left(\frac{(x_c)_{uc} - (x_c)_c}{(x_c)_{uc}} \right) \times 100 \quad (33)$$

Where, $(x_c)_{uc}$ is the response quantity without fluid viscous dampers, $(x_c)_c$ is the response quantity with fluid viscous dampers installed in the staging of the elevated tank. Evidently, negative values of the percentage reduction signify seismic response magnification.

6. Numerical Study

The numerical study is conducted to evaluate the seismic response of the elevated liquid storage tanks installed with viscous dampers. A code has been written in MATLAB [31], for conducting time history analyses of the RC elevated liquid storage tank subjected to eight different real earthquake ground motions. Two types of tanks, with different slenderness, are considered. The slenderness of the cylindrical tanks is defined using aspect ratio, $S = H/R$, and two aspect ratios, viz. $S = 0.5$ and 2.0 are considered. The influence of damping constant and nonlinear velocity exponent (α) is studied by varying α from 0 to 1, increasing at an interval of 0.1. Further, the effectiveness of using the three types of dampers, viz. linear viscous damper (LVD) and nonlinear viscous dampers, NLVD-I ($\alpha = 0.5$), and NLVD-II ($\alpha = 0$), with three configurations of placement of dampers in the staging of the elevated liquid storage tank is investigated.

Table 1 shows the geometric properties of the tank considered in the numerical study. The following are the geometric and material properties used in the numerical study: (i) height of liquid in the container (H) is 5.05 m for tank full condition; inner diameter ($2R$) of the container is 5.06 m; (ii) the contained liquid is considered as water with mass density = 1,000 kg/m³; (iii) volume of the liquid is considered as 100% ($S = 2$, i.e., tank full) and 25% ($S = 0.5$) of the tank capacity - excluding freeboard; (iv) for the RC staging, modulus of elasticity, $E = 25 \times 10^6$ kN/m², number of columns are four, the damping ratio of the RC staging, $\zeta_r = 5\%$; (v) the damping ratio for convective mass, $\zeta_c = 0.5\%$; and (vi) two fluid viscous dampers, each with damping constant as, $C_{md} = 10$ kN-s/m, 40 kN-s/m, 80 kN-s/m, 120 kN-s/m, and 140 kN-s/m (with varying α), with Configuration III placement of dampers, are installed in the staging of the RC elevated tank. The highest value of C_{md} is selected such that for the damper capacity does not exceed 130 kN, and the response of the tank is not increased. It is assumed that all dampers in the staging have the same damping constant and nonlinear exponent.

The dynamic properties of the tank modeled herein are presented in Table 2, which are obtained by conducting free vibration analysis. The details of the earthquake ground motion time histories considered are given in Table 3. The coupled differential equations of motion for the system (Equation 28) are derived and solved by the state-space method. The seismic response quantities, viz. convective displacement (x_c), rigid mass displacement (x_r), displacements at the bracing levels of the RC staging (x_1, x_2, \dots, x_p), normalized base shear, $F_b = V_b / W$, overturning moment (M_o) are obtained, each for two different aspect ratios of the tank. Here, $W = (M_t) g$ is the total weight of the tank, where M_t is the total mass, considering bracing level masses, rigid mass, and convective mass. Further, seismic response of RC elevated liquid storage tank with fluid viscous dampers ($C_{md} = 80$ kN-s/m), LVD ($\alpha = 1$) and NLVD-I ($\alpha = 0.5$), and NLVD-II ($\alpha = 0$), installed in the staging, is compared with the corresponding response of the tanks without dampers.

Table 1. Geometric properties of cylindrical RCC elevated liquid storage tank

Sr. No.	Component	Dimension (mm)
1.	Thickness of roof slab	120
2.	Thickness of tank wall (t_w)	200
3.	Tank wall height including freeboard	5300
4.	Inner radius of the tank (R)	2530
5.	Thickness of floor slab (D_{fs})	250
6.	Floor beam ($B \times D_{fb}$)	250 × 600
7.	Bracing beams ($B \times D$)	400 × 400
8.	Length of bracing beams (L_b)	3500
9.	Column diameter	500
10.	Height of bottom panel (L_1)	2500
11.	Height of intermediate panel (L_2)	3000
12.	Height of top panel (L_3)	2500

Table 2. Dynamic properties of RCC elevated liquid storage tank

$S = H/R$	$S = 0.5$		$S = 2.0$	
	$H_{st} = 20 \text{ m}$		$H_{st} = 20 \text{ m}$	
	$T \text{ (s)}$	$f \text{ (Hz)}$	$T \text{ (s)}$	$f \text{ (Hz)}$
Mode 1	5.06	0.20	3.68	0.27
Mode 2	1.12	0.89	2.18	0.46
Mode 3	0.57	1.76	0.58	1.73
Mode 4	0.19	5.34	0.19	5.34
Mode 5	0.11	9.19	0.11	9.19
Mode 6	0.08	12.63	0.08	12.63
Mode 7	0.07	15.22	0.07	15.22
Mode 8	0.06	17.00	0.06	17.00
Mode 9	0.05	21.33	0.05	21.33
$H_r \text{ (m)}$	2.04		2.5	
$H_c \text{ (m)}$	1.99		3.81	

Table 3. Details of earthquake ground acceleration time histories

Sr. No.	Earthquake (Event Date)	Recording Station	Notation	Component	Peak Ground Acceleration (PGA) (g)	Number of Data Points (Δt)
1.	Imperial Valley, 1940 (18/05/1940)	El-Centro	Imperial Valley	S00E	0.34	2688 (0.02s)
2.	Tabas, 1978 (16/09/1978)	Tabas	Tabas	344	0.93	2500 (0.02 s)
3.	Loma Prieta, 1989 (18/10/1989)	LPGC	Loma Prieta	000	0.57	5001 (0.005 s)
4.	Turkey, 1992 (13/03/1992)	Erzican	Turkey	EW	0.50	4156 (0.005 s)
5.	Northridge, 1994 (17/01/1994)	Sylmar County	Sylmar	360	0.84	3000 (0.02 s)
6.	Kobe, 1995 (16/01/1995)	JMA	Kobe	90	0.59	2400 (0.02 s)
7.	Chi-Chi, 1999 (20/09/1999)	Chiayi-086	Chi-Chi	N	0.21	18000 (0.005 s)
8.	Bhuj, 2001 (26/01/2001)	Ahmedabad	Bhuj	N78E	0.11	26706 (0.005 s)

6.1. Influence of Nonlinear Exponent α

Figure 3 shows the effect of damping constant, nonlinear exponent, α on the response of the elevated liquid storage tanks ($S = 2$) subjected to Tabas, 1978 (0.93 g), Loma Prieta, 1989 (0.57 g), and Chi-Chi, 1999 (0.21 g) earthquakes. It is observed that the response of the tank reduces with a reduction in the nonlinear exponent, $1 > \alpha > 0$, is true only for fluid viscous dampers with low damping constant and when the RC tank is subjected to ground excitations of low PGA. It is noted that when the RC tank is installed with the NLVDs with $C_{md} \geq 40 \text{ kN-s/m}$, the performance of the NLVDs, degrades with a reduction in the nonlinear exponent beyond a certain limit (indicated by a dotted line). It is also seen that the effect of damping constant is more in case of the RC tanks subjected to near field ground motions, than that of the far-field ground motions.

Further, it is observed that use of the NLVDs with higher damping constant (120 kN-s/m) gives maximum reduction in base shear response at $\alpha = 0.8$ (Tabas, 1978, PGA = 0.93 g), $\alpha = 0.3$ (Loma Prieta, 1989, PGA = 0.57 g), and $\alpha = 0.5$ (Chi-Chi, 1999, PGA = 0.21 g). This behavior indicates that the response of the RC tank does not depend only upon the damper characteristics and PGA of the ground motion, but also on, site-specific characteristics of the ground motion. Promisingly, for lower damping ratio, $C_{md} = 10 \text{ kN-s/m}$, maximum base shear, overturning moment, and displacement response reduction is observed to be at $\alpha = 0$. Hence, it is concluded that for low damping constants, as α changes from 1 to zero, the performance of the dampers enhances, and it is superior at $\alpha = 0$. It is also interesting to note that for the tank subjected to ground motions of higher PGA, the use of the fluid viscous dampers with a higher value of damping constant, with $\alpha < 0.6$, showed an increase in the displacement response. It is observed that when the elevated tanks subjected to high PGA events (Tabas, 1978) are installed with fluid viscous dampers in the staging of the tank, linear viscous dampers ($\alpha = 1$) with high damping constant are more advantageous; whereas for low PGA ground motions, NLVDs are beneficial.

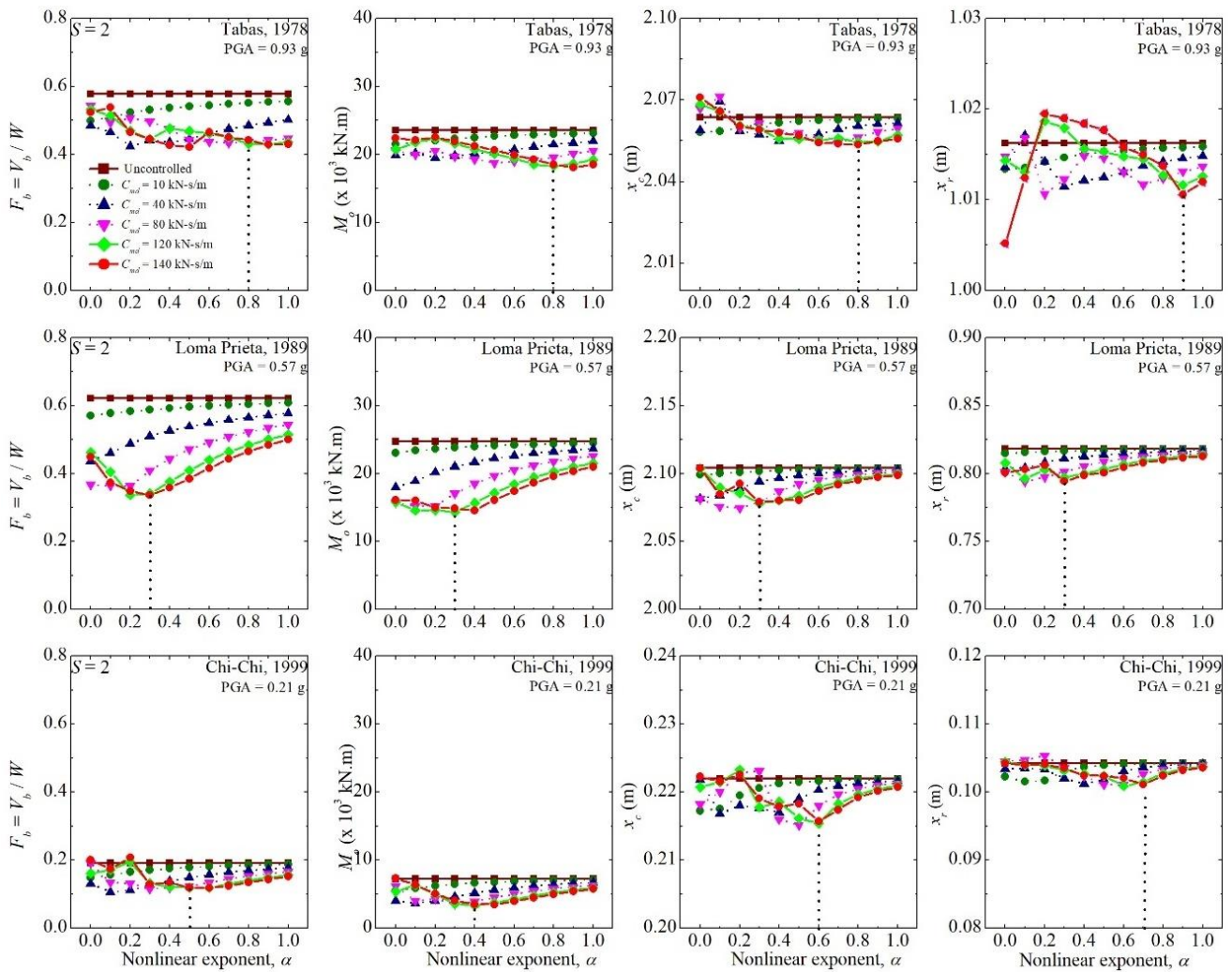


Figure 3. Effect of damping constant C_{md} , and nonlinear exponent α on the response of the RC elevated liquid storage tanks ($S = 2$) installed with fluid viscous dampers, under Tabas, 1978, Loma Prieta, 1989, and Chi-Chi, 1999, earthquake

Figure 4 presents time variation of peak normalized base shear (F_b), overturning moment (M_o), convective mass displacement (x_c) and rigid mass displacement (x_r), for RC elevated liquid storage tank ($S = 2$) installed with fluid viscous dampers ; constant $C_{md} = 80$ kN-s/m ($\alpha = 1, 0.5$, and 0), and varying C_{md} as 40 kN-s/m with $\alpha = 0.5$ and $C_{md} = 10$ kN-s/m with $\alpha = 0$, under Loma Prieta, 1989 earthquake. The figure shows the effectiveness of the fluid viscous dampers for controlling the response of the RC elevated liquid storage tank. Further, the figure highlights the effectiveness of the NLVD ($\alpha = 0.5$ and $\alpha = 0$) having lower damping constant. It is observed that the NLVD with lower damping constant gives a comparable reduction in response to that of LVD with higher damping constant. It is observed that the effectiveness of fluid viscous dampers, LVD ($C_{md} = 80$ kN-s/m, $\alpha = 1$), NLVD ($C_{md} = 40$ kN-s/m, $\alpha = 0.5$), and NLVD ($C_{md} = 10$ kN-s/m, $\alpha = 0$) is same in controlling the displacements at all the considered levels. Lower damping constant signifies the reduction in the size of the damper.

The response of the RC elevated liquid storage tank, with and without fluid viscous dampers (Configuration III) is presented in Table 4 and Table 5 for $S = 0.5$ and $S = 2$, respectively. From the table it is very interesting to note that NLVD-I ($C_{md} = 80$ kN-s/m, $\alpha = 0.5$) is superior in controlling the displacement response in all the considered earthquakes than the LVD ($C_{md} = 80$ kN-s/m, $\alpha = 1$) and NLVD-II ($C_{md} = 80$ kN-s/m, $\alpha = 0$). Though the energy dissipation capacity of the NLVD-II is more than the LVD and NLVD-I, as seen in Figure 5.

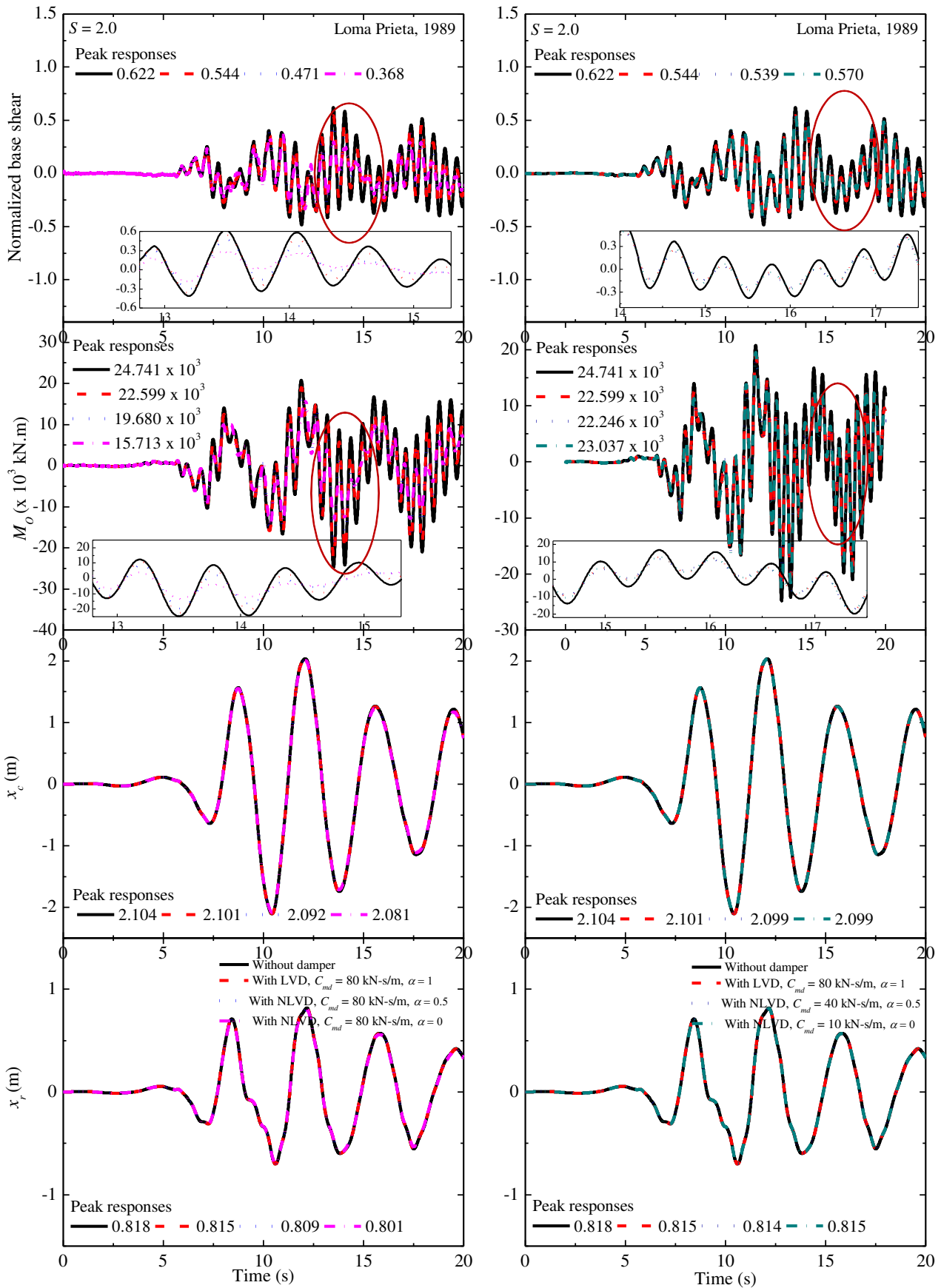


Figure 4. Time variation of response quantities, peak normalized base shear (F_b), overturning moment (M_o), convective mass displacement (x_c) and rigid mass displacement (x_r), for the RC elevated liquid storage tank ($S = 2$) installed with fluid viscous dampers; constant $C_{md} = 80$ kN-s/m ($\alpha = 1, 0.5$, and 0), and varying C_{md} ($C_{md} = 40$ kN-s/m with $\alpha = 0.5$, and $C_{md} = 10$ kN-s/m with $\alpha = 0$), under Loma Prieta, 1989 earthquake.

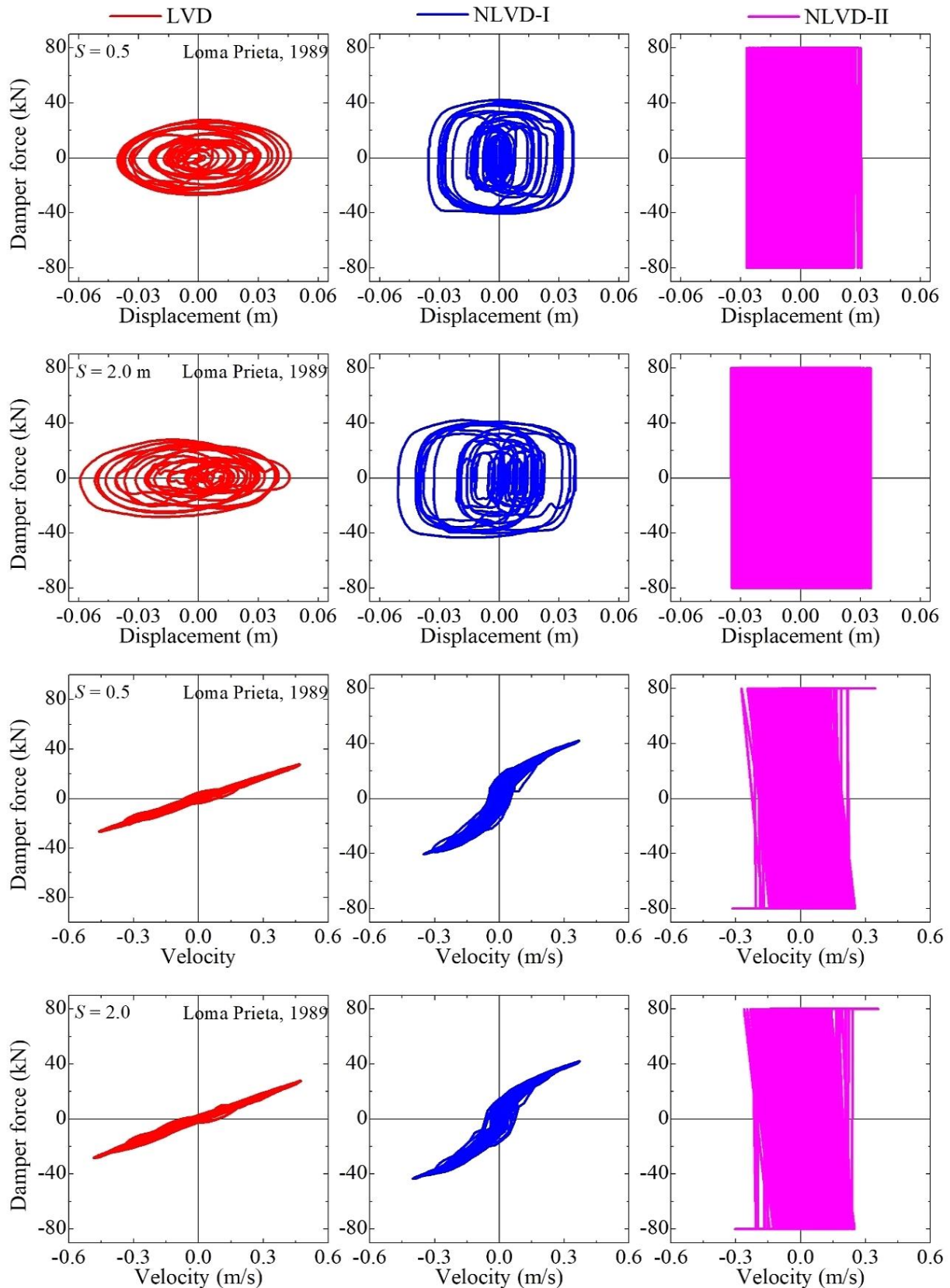


Figure 5. Force displacement loops for linear and nonlinear viscous dampers (LVD, NLVD-I, and NLVD-II) installed in RC elevated liquid storage tank under Loma Prieta, 1989 earthquake

6.2. Displacement-damper Force Relationship

Figure 5 shows the relationship between the damper force and displacement obtained for RC elevated liquid storage tank, installed with fluid viscous dampers (LVD, NLVD-I, and NLVD-II), under Loma Prieta, 1989 earthquake. The figure clearly portrays the energy dissipation characteristics of the dampers. For linear viscous damper (LVD),

damping force is directly proportional to the displacement; for NLVD-I the force-displacement is slightly nonlinear; while for NLVD-II the force-displacement relation is rectangular, as seen in case of friction dampers. Further, the bigger size of the force-deformation loop signifies the more energy dissipation. From Figure 5, it is clear that NLVDs dissipate more energy than the LVDs, highlighting the efficiency of nonlinear viscous dampers over linear viscous dampers. As the dampers are installed in the staging of the elevated tank, the present approach of considering a multi-degree freedom system for staging is a powerful tool for assessing the performance of the tank installed with dampers.

Table 4. Peak values of bracing level displacement responses and the damper forces in the RC elevated liquid storage tank (S = 0.5) installed with the fluid viscous dampers (LVD, NLVD-I, and NLVD-II): Configuration III

Earthquake	Response quantity	x ₁ (m)	x ₂ (m)	x ₃ (m)	x ₄ (m)	x ₅ (m)	x ₆ (m)	x ₇ (m)	F _{D1} (kN)	F _{D2} (kN)	F _{D3} (kN)	F _{D4} (kN)	F _{D5} (kN)	F _{D6} (kN)	F _{D7} (kN)
Imperial Valley, 1940	Without damper	0.01	0.03	0.05	0.06	0.08	0.09	0.09	---	---	---	---	---	---	---
	With LVD	0.01	0.02	0.04	0.06	0.07	0.08	0.08	4.21	14.15	12.12	12.40	11.90	11.23	0.67
	With NLVD-I	0.01	0.02	0.04	0.05	0.06	0.07	0.08	31.42	49.35	47.71	48.81	46.52	47.68	27.95
	With NLVD-II	0.01	0.03	0.05	0.07	0.08	0.09	0.09	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Tabas, 1978	Without damper	0.01	0.05	0.08	0.11	0.15	0.18	0.18	---	---	---	---	---	---	---
	With LVD	0.01	0.04	0.08	0.11	0.14	0.16	0.16	13.58	44.31	29.58	27.71	28.30	28.25	2.02
	With NLVD-I	0.01	0.04	0.07	0.10	0.12	0.14	0.14	36.85	57.09	50.32	49.51	51.48	49.50	29.30
	With NLVD-II	0.01	0.04	0.08	0.10	0.13	0.15	0.15	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Loma Prieta, 1989	Without damper	0.02	0.06	0.10	0.13	0.16	0.18	0.18	---	---	---	---	---	---	---
	With LVD	0.01	0.05	0.08	0.11	0.13	0.15	0.15	10.02	27.69	25.59	22.67	18.60	15.83	2.46
	With NLVD-I	0.01	0.04	0.06	0.08	0.10	0.12	0.12	25.31	42.13	40.61	39.03	36.85	35.03	13.12
	With NLVD-II	0.01	0.03	0.05	0.06	0.08	0.09	0.09	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Turkey, 1992	Without damper	0.01	0.03	0.05	0.07	0.08	0.09	0.10	---	---	---	---	---	---	---
	With LVD	0.01	0.03	0.04	0.06	0.07	0.08	0.08	5.11	14.07	13.25	12.28	12.61	11.18	1.51
	With NLVD-I	0.01	0.02	0.03	0.04	0.04	0.05	0.05	16.95	28.59	27.39	27.96	26.48	24.07	10.56
	With NLVD-II	0.01	0.02	0.03	0.04	0.05	0.06	0.06	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Sylmar, 1994	Without damper	0.01	0.05	0.08	0.11	0.14	0.16	0.16	---	---	---	---	---	---	---
	With LVD	0.01	0.04	0.07	0.10	0.13	0.15	0.15	9.12	29.43	22.23	20.70	19.47	18.30	1.19
	With NLVD-I	0.01	0.04	0.07	0.10	0.12	0.14	0.14	32.95	54.46	49.74	51.39	50.68	49.87	28.41
	With NLVD-II	0.02	0.04	0.07	0.10	0.13	0.15	0.16	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Kobe, 1995	Without damper	0.01	0.04	0.07	0.10	0.12	0.14	0.14	---	---	---	---	---	---	---
	With LVD	0.01	0.04	0.06	0.09	0.10	0.12	0.12	6.58	22.85	18.49	16.90	13.71	12.20	0.81
	With NLVD-I	0.01	0.03	0.06	0.08	0.10	0.11	0.11	34.34	53.16	49.59	50.35	49.11	47.43	28.34
	With NLVD-II	0.01	0.04	0.07	0.09	0.11	0.13	0.14	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Chi-Chi, 1999	Without damper	0.01	0.02	0.04	0.05	0.07	0.08	0.08	---	---	---	---	---	---	---
	With LVD	0.01	0.02	0.03	0.04	0.05	0.06	0.06	4.48	12.24	11.10	9.76	8.17	6.34	0.89
	With NLVD-I	0.00	0.01	0.02	0.03	0.03	0.04	0.04	14.48	25.22	23.58	22.24	20.29	18.69	10.93
	With NLVD-II	0.01	0.02	0.03	0.04	0.05	0.06	0.06	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Bhuj, 2001	Without damper	0.00	0.01	0.02	0.02	0.03	0.03	0.03	---	---	---	---	---	---	---
	With LVD	0.00	0.01	0.01	0.02	0.02	0.03	0.03	1.72	4.08	3.78	3.68	3.52	3.00	0.47
	With NLVD-I	0.00	0.01	0.01	0.01	0.02	0.02	0.02	11.59	15.50	15.87	13.54	15.92	13.14	9.48
	With NLVD-II	0.00	0.01	0.02	0.02	0.03	0.03	0.03	80.00	80.00	80.00	80.00	80.00	80.00	80.00

Table 5. Peak values of bracing level displacement responses and the damper forces in the RC elevated liquid storage tank (S = 2.0) installed with the fluid viscous dampers (LVD, NLVD-I, and NLVD-II): Configuration III

Earthquake	Response quantity	x_1 (m)	x_2 (m)	x_3 (m)	x_4 (m)	x_5 (m)	x_6 (m)	x_7 (m)	F_{D1} (kN)	F_{D2} (kN)	F_{D3} (kN)	F_{D4} (kN)	F_{D5} (kN)	F_{D6} (kN)	F_{D7} (kN)
Imperial Valley, 1940	Without damper	0.01	0.03	0.05	0.07	0.08	0.09	0.09	---	---	---	---	---	---	---
	With LVD	0.01	0.03	0.04	0.06	0.07	0.08	0.08	4.52	14.92	12.93	13.13	12.63	12.11	0.78
	With NLVD-I	0.01	0.03	0.04	0.06	0.07	0.08	0.08	31.21	49.89	47.61	49.28	46.50	48.28	27.95
	With NLVD-II	0.01	0.03	0.05	0.06	0.07	0.08	0.08	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Tabas, 1978	Without damper	0.02	0.06	0.10	0.14	0.18	0.21	0.22	---	---	---	---	---	---	---
	With LVD	0.01	0.05	0.09	0.12	0.16	0.18	0.19	12.89	44.74	30.65	29.12	29.98	30.26	2.20
	With NLVD-I	0.01	0.05	0.08	0.11	0.14	0.17	0.17	38.44	56.94	50.53	49.47	51.64	50.51	29.24
	With NLVD-II	0.02	0.05	0.09	0.13	0.16	0.18	0.19	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Loma Prieta, 1989	Without damper	0.02	0.07	0.11	0.15	0.19	0.22	0.22	---	---	---	---	---	---	---
	With LVD	0.02	0.06	0.10	0.14	0.17	0.20	0.20	10.51	28.25	25.86	22.85	19.49	17.42	2.75
	With NLVD-I	0.02	0.05	0.09	0.12	0.15	0.17	0.17	26.25	43.44	41.22	39.02	37.51	35.73	13.64
	With NLVD-II	0.01	0.04	0.06	0.08	0.10	0.12	0.13	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Turkey, 1992	Without damper	0.01	0.04	0.06	0.08	0.10	0.12	0.12	---	---	---	---	---	---	---
	With LVD	0.01	0.03	0.05	0.07	0.09	0.10	0.10	6.51	17.90	14.99	15.44	15.62	14.09	2.14
	With NLVD-I	0.01	0.02	0.04	0.05	0.06	0.07	0.08	19.19	32.59	30.89	31.59	30.72	29.20	11.24
	With NLVD-II	0.01	0.03	0.04	0.06	0.07	0.08	0.09	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Sylmar, 1994	Without damper	0.01	0.04	0.07	0.09	0.12	0.14	0.14	---	---	---	---	---	---	---
	With LVD	0.01	0.03	0.06	0.08	0.10	0.12	0.13	8.55	28.56	23.30	23.16	21.77	20.87	1.41
	With NLVD-I	0.01	0.03	0.05	0.08	0.10	0.12	0.12	33.93	53.63	48.58	50.99	52.11	48.50	28.84
	With NLVD-II	0.01	0.04	0.06	0.09	0.11	0.13	0.14	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Kobe, 1995	Without damper	0.01	0.04	0.07	0.09	0.11	0.12	0.13	---	---	---	---	---	---	---
	With LVD	0.01	0.04	0.06	0.09	0.10	0.12	0.12	7.71	23.28	18.49	17.29	14.81	12.86	0.58
	With NLVD-I	0.01	0.04	0.06	0.08	0.10	0.11	0.11	35.07	52.39	50.77	48.69	49.55	46.99	28.15
	With NLVD-II	0.01	0.05	0.07	0.10	0.12	0.13	0.13	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Chi-Chi, 1999	Without damper	0.01	0.02	0.04	0.05	0.06	0.07	0.07	---	---	---	---	---	---	---
	With LVD	0.01	0.02	0.03	0.04	0.05	0.06	0.06	4.24	11.64	10.88	9.86	8.35	6.54	0.92
	With NLVD-I	0.00	0.01	0.02	0.03	0.04	0.04	0.04	14.71	26.50	24.86	23.69	21.91	20.26	10.27
	With NLVD-II	0.01	0.02	0.03	0.04	0.05	0.06	0.06	80.00	80.00	80.00	80.00	80.00	80.00	80.00
Bhuj, 2001	Without damper	0.00	0.01	0.02	0.02	0.03	0.03	0.03	---	---	---	---	---	---	---
	With LVD	0.00	0.01	0.01	0.02	0.02	0.03	0.03	1.58	4.25	3.91	3.64	3.26	2.74	0.42
	With NLVD-I	0.00	0.01	0.01	0.01	0.02	0.02	0.02	10.94	14.92	16.74	13.10	16.56	12.92	9.64
	With NLVD-II	0.00	0.01	0.02	0.02	0.03	0.03	0.03	80.00	80.00	80.00	80.00	80.00	80.00	80.00

6.3. Effect of Placement of Damper

Figures 6 and 7 present peak percentage reduction in base shear and the overturning moment when the RC elevated tank is installed with the fluid viscous dampers (LVD, $\alpha = 1$, NLVD-I, $\alpha = 0.5$ and NLVD-II, $\alpha = 0$), for $S = 0.5$ and $S = 2$, respectively, subjected to eight different earthquake ground motions (refer Table 1 for earthquake numbers). Furthermore, figures show the variation on maximum damper force induced at different levels in the elevated tank, with Configuration I, Configuration II and Configuration III placement of fluid viscous dampers. From figures, it is observed that with the installation of NLVDs in the staging of the tank, Configuration I and Configuration II are more effective in reducing the base shear response of the tank, than the Configuration III. However, the damper force induced in the damper is more in Configuration III. Maximum reduction of 80% and 75% in base shear and overturning moment, respectively, is achieved with the installation of NLVDs in the RC elevated liquid storage tank ($S = 0.5$). Further, the peak response reduction of 70% and 65%, in base shear response and overturning moment response is achieved with NLVDs ($S = 2.0$).

It is observed from the results (Figures 3, 6 and 7) that the dampers with $0 < \alpha \leq 1$ help to dissipate the seismic energy more effectively, without contributing towards increasing stiffness; hence, bracing level displacements, rigid

mass displacement, and convective displacement response are effectively reduced by installing fluid viscous damper with $0 < \alpha \leq 1$, under all considered earthquakes. However, as far as the base shear response reduction is concerned, it is observed that the response reduction using the fluid viscous dampers with $\alpha = 0$ and $\alpha = 0.5$ is more, as compared to that with $\alpha = 1$. However, a marginal increase in either (or both) of the base shear and overturning moment response is observed with the NLVD-II ($\alpha = 0$), Configuration III in Imperial Valley, 1940, Sylmar, 1994, Kobe, 1995, Chi-Chi, 1999 and Bhuj, 2001, earthquakes, which is attributed towards the increased stiffness imparted. Further, it is noticed that with the use of fluid viscous dampers, the base shear is substantially reduced under all considered earthquakes. It is observed that typically all the LVDs and NLVDs with appropriate nonlinear exponent α reduce the response of the RC tank; however, the reduction with the NLVDs ($\alpha = 0$ and 0.5) is more than that of the LVD ($\alpha = 1$).

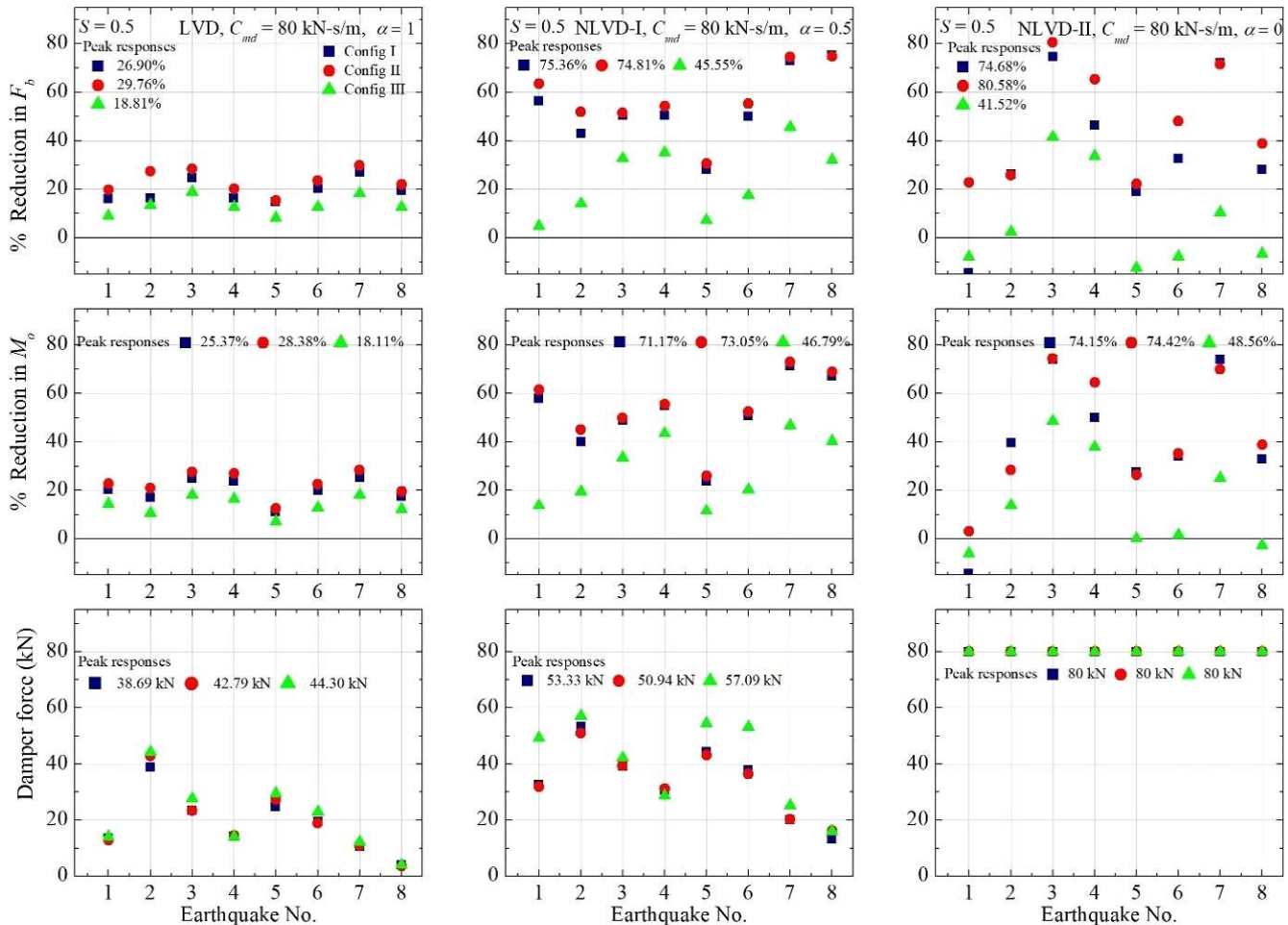


Figure 6. % Reduction in peak seismic response quantities, normalized base shear (F_b), overturning moment (M_o), and the peak damper force induced for the RC elevated liquid storage tank ($S = 0.5$) installed with the LVD, and NLVD ($\alpha = 0.5$ and 0), under different earthquakes.

Figure 8 presents storey shears, overturning moment, and damper force induced at different levels in the elevated tank, with and without fluid viscous dampers (Configuration I, Configuration II, and Configuration III), under Loma Prieta, 1989 earthquake. It is observed that the use of the fluid viscous dampers has helped in reducing the seismic storey shear substantially. Similarly, remarkable reduction in the overturning moment is achieved with the help of the fluid viscous dampers. Further, it is observed that the force induced in the dampers at various levels along the height of the staging of the tank varies. Moreover, it is observed from Figure 8 that at all levels and in all considered placement of dampers, the damper force induced in the NLVD-I is less than that of LVD and NLVD-II. It is a fact that nonlinear viscous dampers absorb high velocity shocks with less damper force. Whereas, in case the NLVD-IIs the damper force is constant for all considered placement configurations. This is because, in case of the NLVD-IIs, with nonlinear exponent, $\alpha = 0$, the damper force is no longer proportional to the velocity and is a function of damping constant only. Additionally, it is very interesting to note that the damper force induced in the first and second level dampers is less than that of the dampers installed in the intermediate panels. Such effectiveness of the dampers based on the nonlinear exponent (α) is anticipated due to the variation of velocities of the masses along the height of the structure.

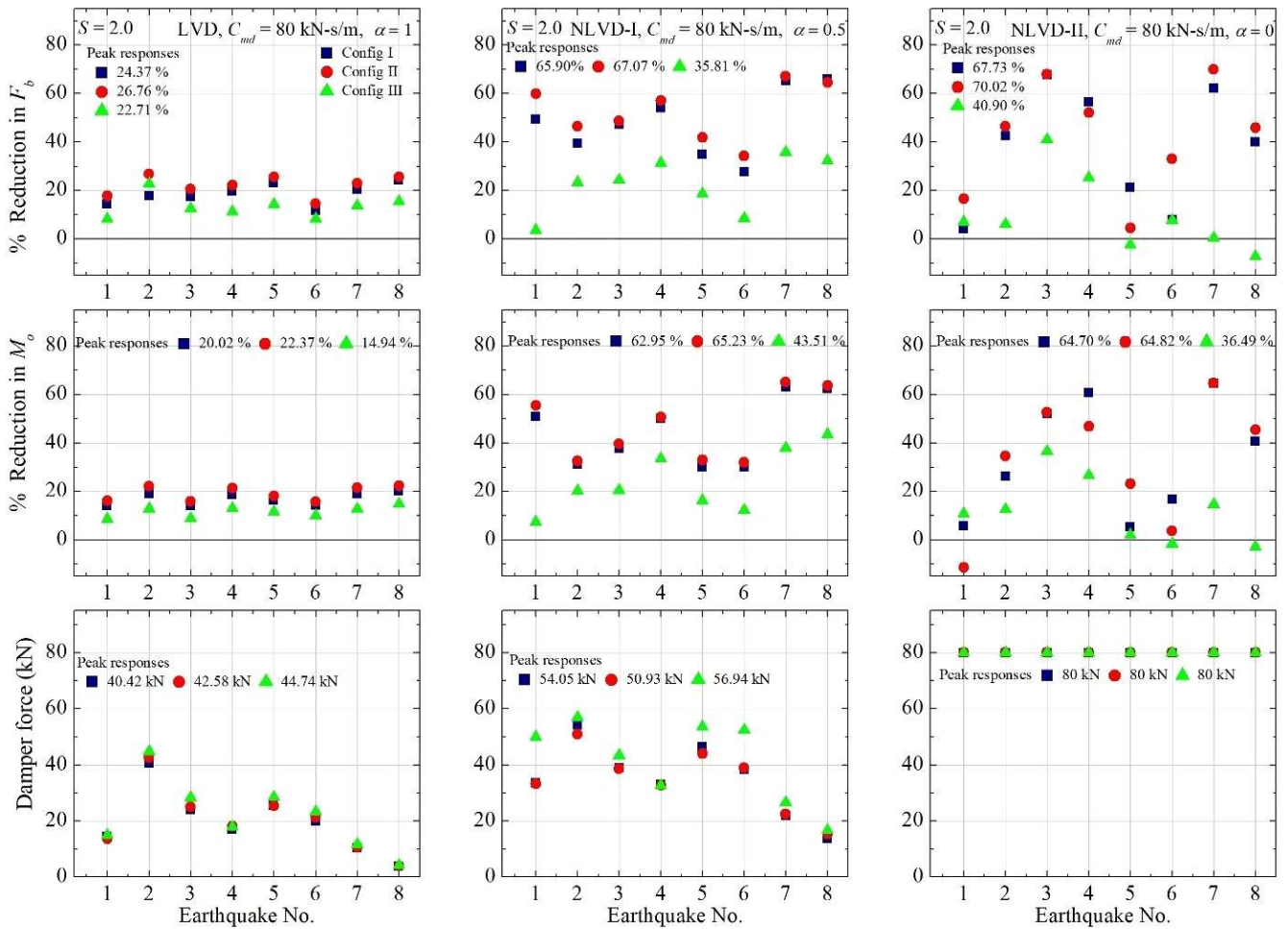


Figure 7. % Reduction in peak seismic response quantities, normalized base shear (F_b), overturning moment (M_o) and the peak damper force induced for the RC elevated liquid storage tank ($S = 2.0$) installed with the LVD, and NLVD ($\alpha = 0.5$ and 0), under different earthquakes.

Figure 9 presents % Reduction in rigid mass displacement (x_r), and convective displacement (x_c) for the RC elevated liquid storage tank ($S = 0.5$ and $S = 2.0$) installed with the LVD, and NLVD ($\alpha = 0.5$ and 0), under different earthquakes. It is observed from the figure that the maximum reduction of rigid mass displacement is 38% ($S = 0.5$, NLVD-I, Configuration I), and convective displacement is reduced by 9% ($S = 2.0$, NLVD-I, Configuration I). Configuration II also has a comparable reduction in displacement response, whereas Configuration III reported the least displacement response reduction. Additionally, it is observed that the NLVD-I is superior in controlling displacement response than the other considered fluid viscous dampers (LVD and NLVD-II). Further, a marginal increase in the displacement response is observed for the RC elevated tank installed with LVD and NLVD-II (Configuration I, Configuration II and Configuration III). Promisingly, no such increase is observed for NLVD-I (Configuration I and Configuration II).

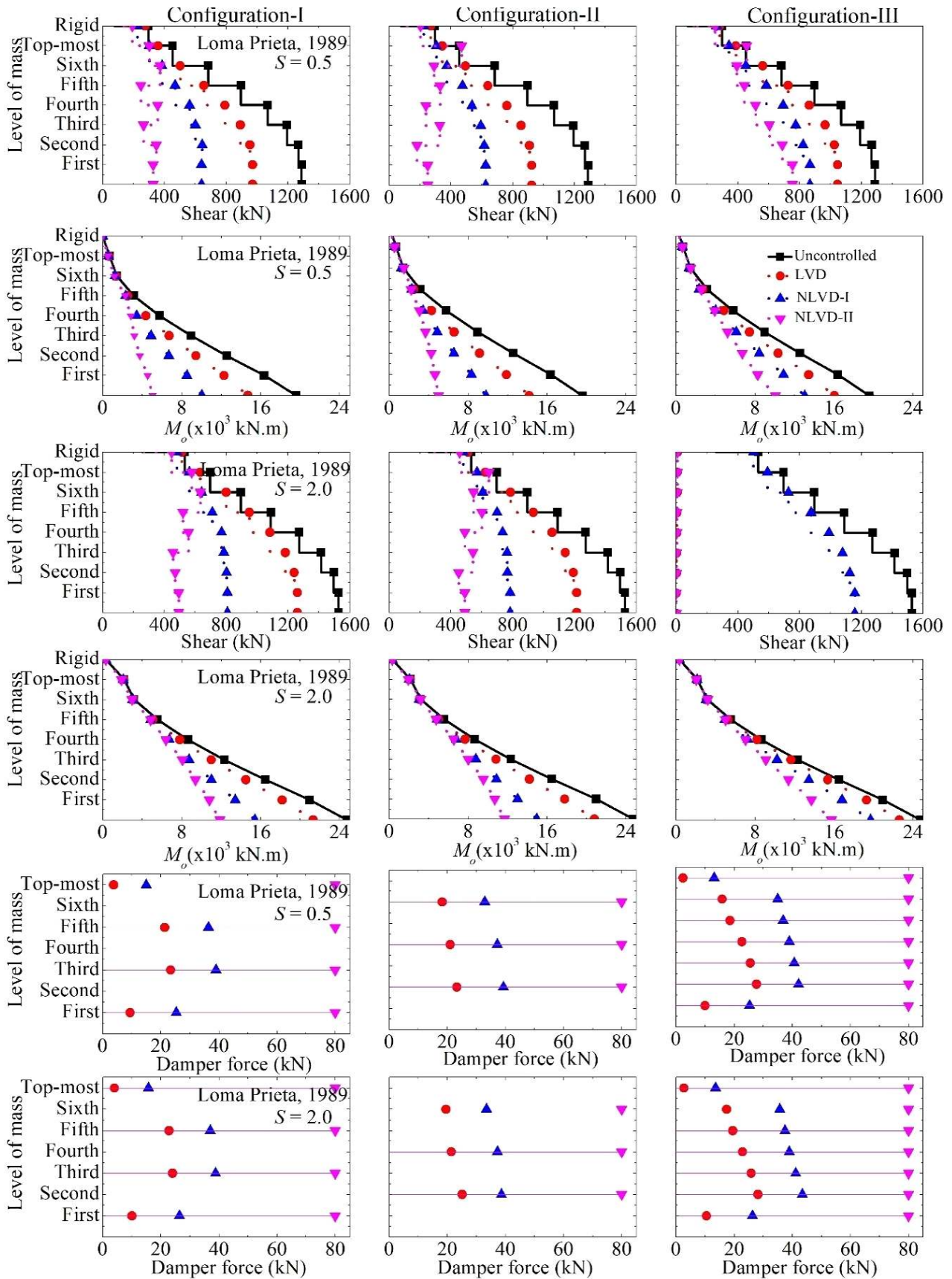


Figure 8. Peak storey shear, overturning moment, and the damper forces, induced at the different level masses of RC elevated water tank with and without fluid viscous dampers (Configuration I, Configuration II, and Configuration III), under Loma Prieta, 1989 earthquake.

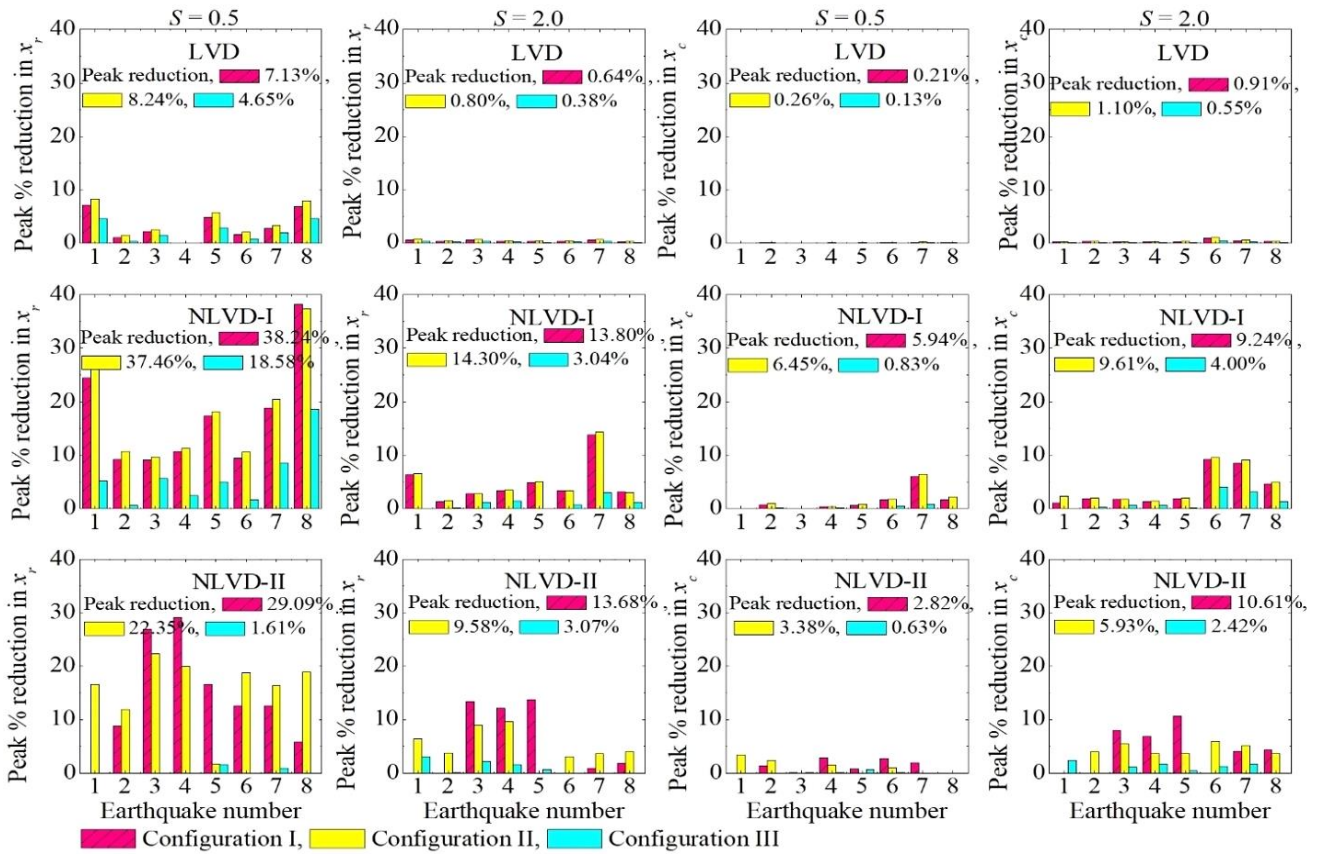


Figure 9. % Reduction in peak seismic response quantities, rigid mass displacement (x_r), and convective mass displacement (x_c) for the RC elevated liquid storage tank ($S = 0.5$ and $S = 2.0$) installed with the LVD ($\alpha = 1$), and NLVD-I ($\alpha = 0.5$) and NLVD-II ($\alpha = 0$), under different earthquakes.

7. Conclusions

The paper illustrates the importance of modeling of the elevated liquid storage tank as two-degrees of freedom system for container and as a multi-degree freedom system for the framed staging of the tank; so as to install dampers in the staging. Seismic response of the RC elevated liquid storage tank with fluid viscous dampers is investigated under eight different real earthquake ground motions. A comparison of the important response quantities, obtained through time history analysis is presented. The following are the major conclusions drawn from the present study.

- Since the dampers are installed in the staging of the elevated tank, the modeling of the multi-degree freedom system for staging provides a better tool while assessing the performance of the tank installed with dampers;
- The nonlinear viscous dampers with lower damping constant results in a comparable reduction in the response of RC elevated liquid storage tank to that of linear viscous dampers with higher damping constant. Lower damping constant signifies the compact size of the damper;
- The seismic response of the tank reduces with a reduction in the nonlinear exponent, α . It is also seen that effect of damping constant increases with an increase in the PGA of earthquake ground motion;
- Typically, all fluid viscous dampers with appropriate selection of parameters, viz. damping constant and nonlinear exponent (α), reduce the response of elevated RC tank. Moreover, effectiveness of the fluid viscous dampers is also affected by the volume of liquid (aspect ratio, S) in the container, as such higher percentage reduction in base shear and overturning moment responses are observed for broad tank;
- The effectiveness of the dampers based on the nonlinear exponent (α) is anticipated due to the variation of velocities of the masses along the height of the staging;
- The effect of the nonlinear exponent on the response reduction favorably increases with an increase in the damping constant. As far as damper force is concerned, it is observed that the effect of nonlinearity in combination with damping constant makes nonlinear viscous dampers more effective than linear viscous dampers.

8. Conflicts of Interest

The authors declare no conflict of interest.

9. References

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