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Influence of temperature and/or field dependences of the E – J power law on trapped magnetic field in bulk YBaCuO

K. Berger, J. L ev eque, D. Netter, B. Douine, and A. Rezzoug

Abstract— Temperature, current density and magnetic field distributions in YBCO bulk superconductor during a pulsed-field magnetization (PFM) process are calculated using the finite difference method. Simulations are based on the heat diffusion equation with account of the heat produced by flux motion, and Maxwell's equations. A power law with temperature and magnetic field dependent parameters is used to characterize the electromagnetic behavior of the superconducting material. We analyze how the stored magnetic energy W_m depends on the temperature and field dependences of the power law.

Index Terms— bulk YBaCuO, stored magnetic energy, thermal coupling, magnetization, modelling.

I. INTRODUCTION

THE recent developments in preparing melt-textured high-temperature superconductor (HTS) bulk parts with high critical current density, close to 10^9 A·m² at 77 K, make this material particularly promising for use as cryo-permanent magnets [1], [2].

To magnetize the HTS, pulsed field magnetization (PFM) process is often used because it is considered to be the most practical method. However, this process leads to a strong temperature rise in the superconductor produced by flux motion and it is found experimentally that trapped flux reaches a maximum at some optimal value B_{opt} of the maximal applied field B_m , and decreases for larger B_m [3].

In this paper, numerical simulations are performed to obtain and understand electromagnetic and thermal phenomena in an YBCO bulk part during PFM. The coupled magneto-thermal problem to be solved is 2D-axisymmetrical and strongly nonlinear. Simulations are based on the Finite Difference Method and allow for the calculation of the magnetic field, current density and temperature distributions in the superconductor during all the stages of the PFM process.

In order to have a more global idea of the trapped field inside the HTS part, we chose to study the stored magnetic

energy in the superconductor. We will show that only the taking into account of the heat generation can reproduce experimental results showing a maximum in the stored magnetic energy.

II. NUMERICAL ANALYSIS METHOD

A. Magnetization process

In the PFM experiment, a cylindrical bulk YBCO (Fig. 1) is magnetized by using a pulsed Cu coil which, together with a capacitor, form a resonant circuit. The resulting applied field $B_a(t)$ in the z direction can be expressed as:

$$B_a(t) = B_m \frac{t}{\tau} \exp\left(1 - \frac{t}{\tau}\right), \quad (1)$$

with B_m the maximal applied field at $t = \tau$, and τ the time constant of the system. In order to simulate a PFM process, we chose a time constant τ of 1 ms. Fig. 2 shows the temporal evolution of the applied magnetic field $B_a(t)$.

B. Model description

The electromagnetic behavior of a superconductor is governed by the Maxwell's equations. When quasi-static approximation is taken (no displacement currents are considered and $\nabla \cdot \mathbf{J} = 0$), the supplement of the constitutive

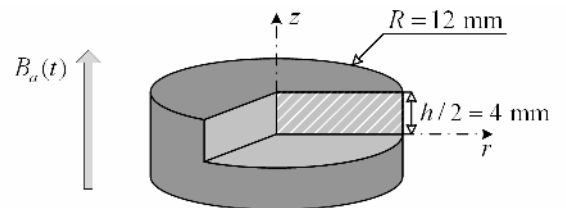


Fig. 1. Sample geometry: compact cylinder with 12 mm of outer radius and 8 mm of height. Due to symmetry only one half of the sample is modeled (hatched part).

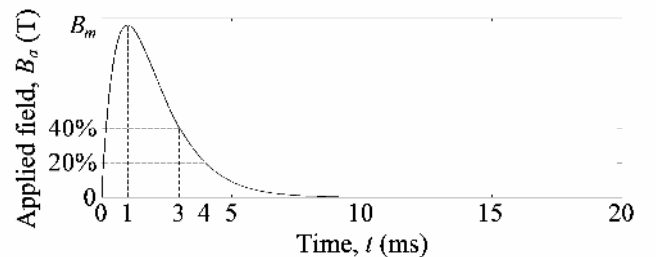


Fig. 2. Temporal evolution of the applied magnetic field $B_a(t)$.

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law $\mathbf{B} = \mu_0 \mathbf{H}$ gives:

$$\nabla \times \nabla \times \mathbf{E} = -\mu_0 \partial \mathbf{J} / \partial t. \quad (2)$$

Because the superconductor is subjected to a non-stationary external magnetic field $B_a(t)$, a heat per unit volume is produced:

$$Q = \mathbf{E} \cdot \mathbf{J}. \quad (3)$$

The temperature change due to the heat generation is described by the heat diffusion equation:

$$\gamma C \frac{\partial T}{\partial t} - \nabla \cdot (\kappa \nabla T) = Q, \quad (4)$$

where T is the temperature, γ the density, C the specific heat capacity, and κ the thermal conductivity.

The heat transfer is considered essentially by convection between the superconductor and the liquid nitrogen bath. In this liquid, the convective heat transfer coefficient h^* is approximately 400 W/(m²·K) according to [4].

In axially symmetric problems the electric field \mathbf{E} and the current density \mathbf{J} have only a non-zero component in the θ direction, E and J . Then the fundamental equations on the axisymmetric coordinate (r, z) are as follows:

$$\frac{1}{r} \frac{\partial E}{\partial r} + \frac{\partial^2 E}{\partial r^2} - \frac{E}{r^2} + \frac{\partial^2 E}{\partial z^2} = \mu_0 \frac{\partial J}{\partial t}, \quad (5)$$

$$\gamma C \frac{\partial T}{\partial t} = \frac{\kappa}{r} \frac{\partial T}{\partial r} + \kappa \frac{\partial^2 T}{\partial r^2} + \kappa \frac{\partial^2 T}{\partial z^2} + Q. \quad (6)$$

The power law model is used to describe the nonlinear E - J characteristic of the superconductor,

$$E = E_c (J / J_c)^n, \quad (7)$$

where J_c is the critical current density, E_c the critical electrical field, and n the index of the power law. The parameters J_c and n can also depend on the temperature T and the magnetic flux density \mathbf{B} . In Kim's model [5] the flux density dependence of J_c is considered as:

$$J_c(\mathbf{B}) = J_{c0} \frac{1}{1 + \|\mathbf{B}\| / B_0}, \quad (8)$$

where J_{c0} is J_c for $\|\mathbf{B}\| = 0$ and B_0 a constant. The field dependence model of the n -value is taken as:

$$n(\mathbf{B}) = n_1 + \frac{n_0 - n_1}{1 + \|\mathbf{B}\| / B_0}, \quad (9)$$

where n_0 and n_1 are respectively n -value for $\|\mathbf{B}\| = 0$ and $\|\mathbf{B}\| \gg B_0$.

On the basis of Anderson's excitation creep model, the index n can be identified with $U_{0a} / k_B T$, where U_{0a} is the apparent pinning potential [7], and k_B the Boltzmann's constant. Measurements of J_c as a function of T have successfully been fitted to linear model in [7]. The following expressions are used:

$$J_c(T) = J_{c0} \frac{1 - T / T_c}{1 - T_0 / T_c}, \quad (10)$$

$$n(T) = n_0 T_0 / T \text{ with } n_0 = U_{0a} / k_B T_0. \quad (11)$$

Here T_0 is the liquid nitrogen bath temperature, J_{c0} and n_0 are respectively the critical current density and the n -value for the case $T = T_0$.

Four E - J laws with or without thermal and magnetic field

TABLE I
RELATIONSHIPS BETWEEN E, J, \mathbf{B} AND T

Symbol	Equation
E - J	$E = E_c \left(\frac{J}{J_c} \right)^n$
E - J - T	$E = E_c \left(\frac{J}{J_c(T)} \right)^{n(T)}$ with $J_c(T) = J_{c0} \frac{1 - T / T_c}{1 - T_0 / T_c}$ and $n(T) = n_0 \frac{T_0}{T}$
E - J - \mathbf{B}	$E = E_c \left(\frac{J}{J_c(\mathbf{B})} \right)^{n(\mathbf{B})}$ with $J_c(\mathbf{B}) = \frac{J_{c0}}{1 + \ \mathbf{B}\ / B_0}$ and $n(\mathbf{B}) = n_1 + \frac{n_0 - n_1}{1 + \ \mathbf{B}\ / B_0}$
E - J - \mathbf{B} - T	$E = E_c \left(\frac{J}{J_c(\mathbf{B}, T)} \right)^{n(\mathbf{B}, T)}$ with $J_c(\mathbf{B}, T) = \frac{J_{c0}}{1 + \ \mathbf{B}\ / B_0} \times \frac{1 - T / T_c}{1 - T_0 / T_c}$ and $n(\mathbf{B}, T) = \left(n_1 + \frac{n_0 - n_1}{1 + \ \mathbf{B}\ / B_0} \right) \times \frac{T_0}{T}$

TABLE II
SIMULATION PARAMETERS

Symbol	Quantity	Value
γ	density	5.4 g/cm ³
C	specific heat	150 J/(kg·K)
κ	thermal conductivity	5 W/(m·K)
h^*	convective heat transfer coefficient	400 W/(m ² ·K)
T_c	critical temperature	92 K
T_0	operating temperature (liquid nitrogen)	77.3 K
E_c	critical electrical field	1 μV/cm
J_{c0}	critical current density at 77.3 K and $\ \mathbf{B}\ = 0$	500 A/mm ²
n_0	n -exponent at 77.3 K and $\ \mathbf{B}\ = 0$	21
n_1	n -exponent at 77.3 K when $\ \mathbf{B}\ \gg B_0$	5
B_0	constant used in magnetic field dependences	0.5 T

dependences are chosen for studying the electromagnetic and thermal phenomena in the bulk YBCO during PFM (Table I).

III. RESULTS

We present the results of the calculations assuming a sample (Fig. 1) characterized by parameters resumed in Table II, which are typical values for YBa₂Cu₃O_{7-δ} crystal. Due to symmetry, results are only shown in the hatched part of the sample.

Magnetic field and current density distributions obtained using the different E - J laws are compared at different times in Fig. 3 and Fig. 4 respectively. From $t = 0$ to 1 ms, the applied field B_a increases up to $B_m = 5$ T and screening currents are induced from the edge of the superconductor (Fig. 4). Because B_m is lower than the full penetration field $B_p = \mu_0 J_c R \approx 7.5$ T, the magnetic field doesn't penetrate to the center of the YBCO cylinder in the case E - J . On the contrary, the other laws with thermal or magnetic field dependence lead to a faster penetration of the field and, consequently, smaller current-free region in the center.

From 1 to 20 ms, B_a decreases down to zero and areas with opposite current appear. At $t = 3$ ms, the applied field is about 40 % of B_m , i.e. 2 T.

From 20 ms to 200 s, the applied magnetic field does not change anymore. However, we can see that trapped magnetic

field and current density distributions change. The first reason for E - J - T and E - J - \mathbf{B} - T laws is that thermal effects are considered and the displacement of the hot spot creates region with lower current density. The second reason is not thermal, the change of the electromagnetic quantities are due to relaxation phenomena generated by the power law $E(J)$.

The main difference between E - J and E - J - \mathbf{B} laws is that the saturating current density in the latter is varying with the local field amplitude – the higher the local field, the lower the current density. This is also true for E - J - \mathbf{B} - T law but thermal effects have to be considered too.

Heat produced by flux motion has been calculated for each

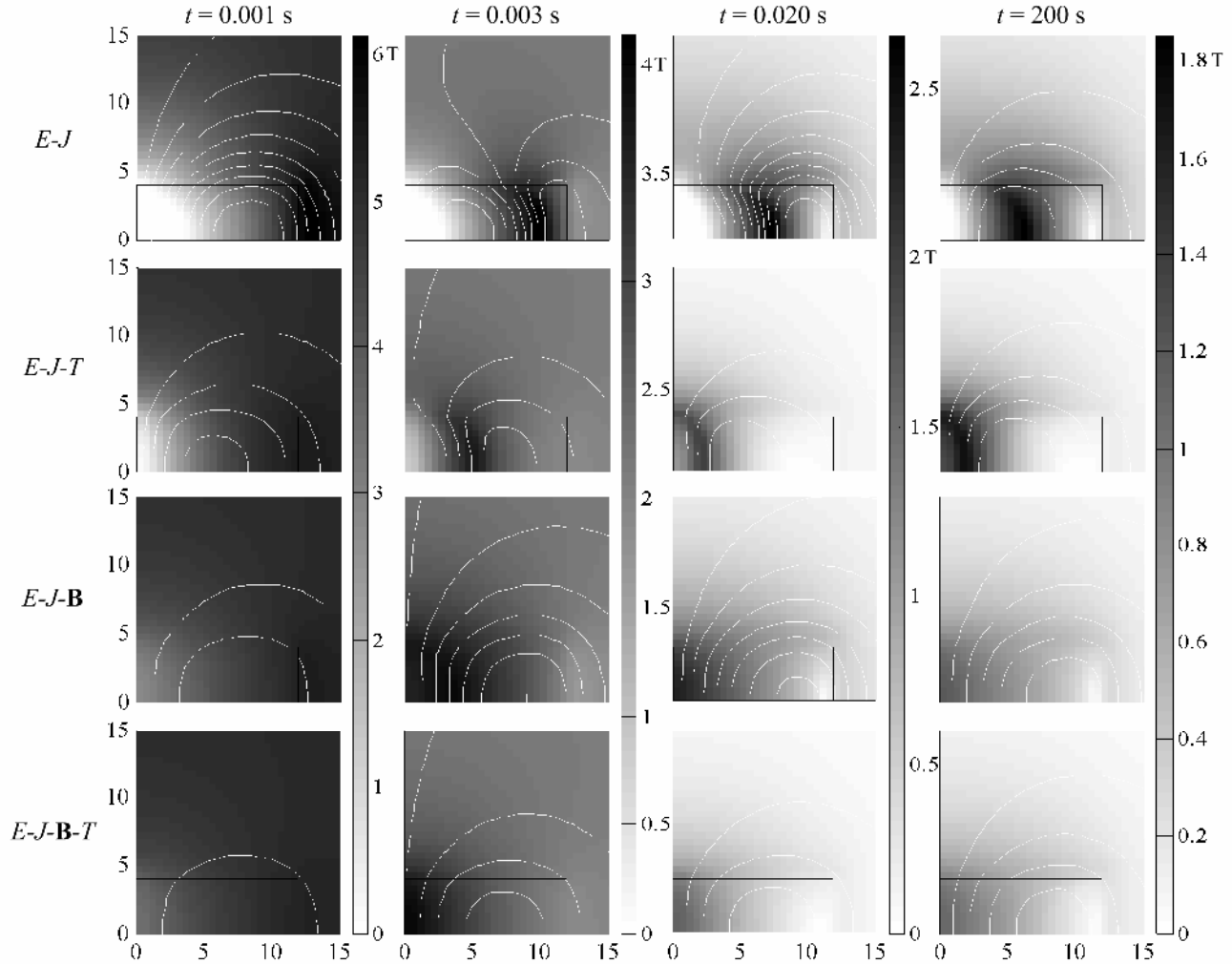


Fig. 3. Comparison of the different E - J laws. Magnetic field distributions $\mathbf{B}(r,z)$ during PFM with $B_m = 5$ T and $\tau = 1$ ms. Due to symmetry, results are shown in the top right half of the sample (Fig. 1). Sample boundaries are situated at $r = 12$ mm and $z = 4$ mm.

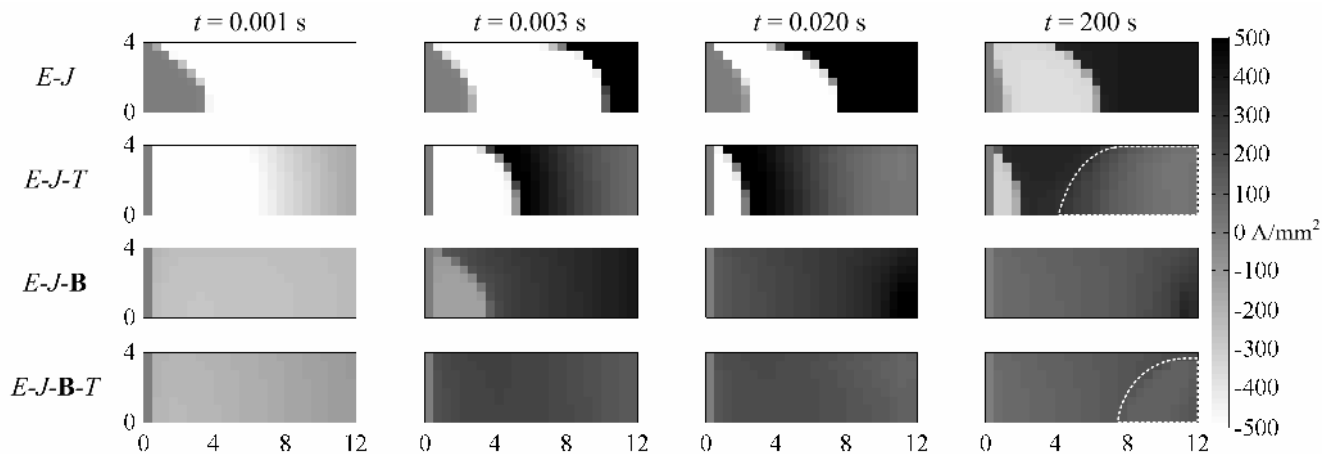


Fig. 4. Comparison of the different E - J laws. Current density distributions $J(r,z)$ during PFM with $B_m = 5$ T and $\tau = 1$ ms. Due to symmetry, results are shown in the top right half of the sample (Fig. 1).

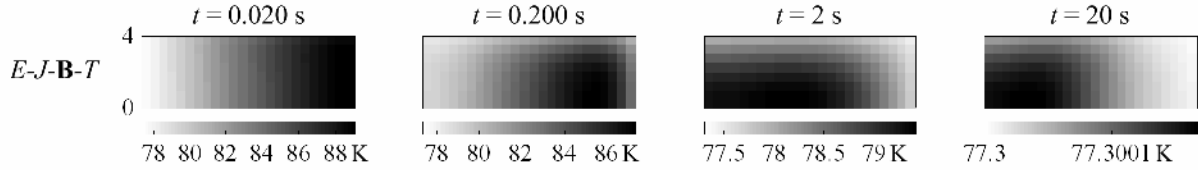


Fig. 5. Displacement of the hot spot. Temperature distributions $T(r,z)$ during PFM with $B_m = 5$ T and $\tau = 1$ ms in the case $E-J-B-T$. Due to symmetry, results are shown in the top right half of the sample (Fig. 1).

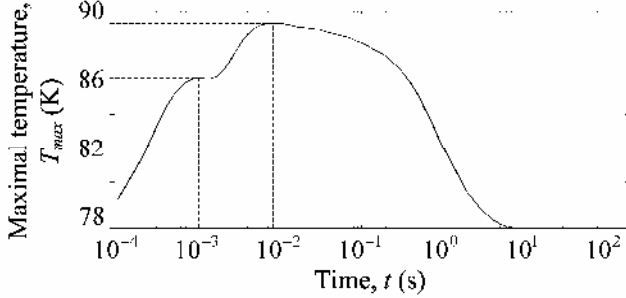


Fig. 6. Maximal temperature in the bulk YBCO as a function of time in the case $E-J-B-T$.

case but only $E-J-T$ and $E-J-B-T$ laws depend on temperature. Temperature distributions with $E-J-B-T$ law are shown in Fig. 5. Approximately the same results have been obtained with $E-J-T$.

Fig. 6 shows the maximal temperature in the bulk YBCO as a function of time. Because of the thermal time constant, we have to wait several seconds in order to obtain the magneto-thermal steady state. We assume that the superconductor is in steady state at $t = 200$ s.

From 0 to 20 ms, the applied magnetic field varies and temperature distributions present very clear maxima near the sample surface. The reason is obvious as near the surface the flux motion is most intense and the heat release is maximal. In fact, the maximal temperature in the superconductor is observed at the edge of the superconductor at $t = 8$ ms (Fig. 6). After this time, the heat is diffusing from the edge to the center of the bulk YBCO (Fig. 5). Therefore, with $E-J-T$ and $E-J-B-T$ laws at $t = 200$ s, we can see an area (inside the dotted lines in Fig. 4) where the current density is lower.

When τ is given, the key point to magnetize the superconductor is to choose the optimum applied field B_m so that in the remanent state, the trapped magnetic field becomes maximum. The stored magnetic energy defined as,

$$W_m = \frac{1}{2} \iiint_{\mathbb{R}^3} \mathbf{H} \cdot \mathbf{B} \cdot dV = \frac{1}{2} \iiint_{\Omega_s} \mathbf{A} \cdot \mathbf{J} \cdot dV, \quad (12)$$

is plotted in Fig. 7 as a function of B_m . Here, Ω_s is the volume of superconductor, and \mathbf{A} the magnetic vector potential.

With the $E-J$ law, the saturating current density is neither affected by magnetic field nor temperature. Therefore, the predicted stored magnetic energy is the highest with this model. The maximal value (not represented) of 4.7 J is reached for $B_m = 11$ T. When taking into account the magnetic field dependence, the penetration field as well as the current density are lower, which results in a lower maximum of the stored energy. For $E-J-T$ and $E-J-B-T$ laws, the presence of heating leads to reduction of the stored magnetic energy, and a

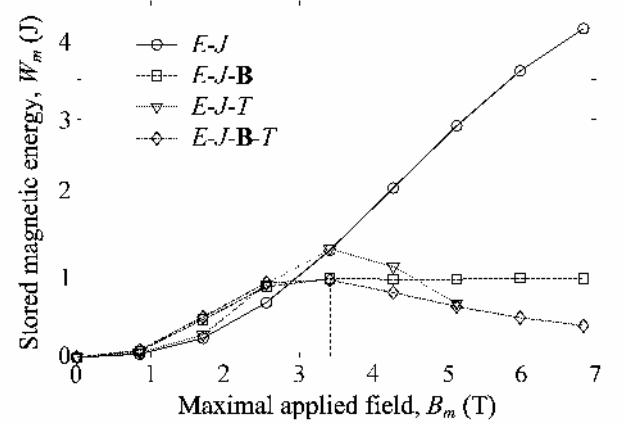


Fig. 7. Comparison of the different $E-J$ laws. Stored magnetic energy W_m as a function of the maximal applied field B_m .

peak in the $W_m(B_m)$ curve appears at $B_m = 3.5$ T.

IV. CONCLUSION

Through this article, the importance of temperature and field dependences of the $E-J$ power law on the superconductor's behavior during a PFM process was shown. The stored magnetic energy W_m with the $E-J-B-T$ law, which reproduces the most realistic behavior, reaches maximum for some optimal maximum field B_{opt} . The value of B_{opt} can be found theoretically, which enables the design of more efficient pulsed system to magnetize cryo-magnets.

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