# "INTEGRATING SCHEDULING WITH BATCHING AND LOT-SIZING: A REVIEW OF ALGORITHMS AND COMPLEXITY ${ }^{n}$ 

by
Luc VAN WASSENHOVE *
and
C.N. POTTS**
$\mathbf{N}^{\circ} 91 / 10 / T M$

* Professor of Operations Management and Operations Research, INSEAD, Boulevard de Constance, Fontainebleau 77305 Cedex, France.
** Faculty of Mathematical Studies, University of Southampton, Southampton, England.

Printed at INSEAD, Fontainebleau, France.

## INTEGRATING SCHEDULING WITH

## BATCHING AND LOT-SIZING:

 A REVIEW OF ALGORITHMS AND COMPLEXITYC.N. Potts

Faculty of Mathematical Studies, University of Southampton, U.K.

L.N. Van Wassenhove<br>INSEAD, Fontainebleau, France

In many practical situations, batching of similar jobs to avoid set-ups is performed whilst constructing a schedule. On the other hand, each job may consist of many identical items. Splitting a job often results in improved customer service or in reduced throughput time. Thus, implicit in determining a schedule is a lot-sizing decision which specifies how a job is to be split. This paper proposes a general model which combines batching and lot-sizing decisions with scheduling. A review of research on this type of model is given. Some important open problems for which further research is required are also highlighted.

Key words: algorithms, batching, complexity, lot-sizing, scheduling

## INTRODUCTION

Throughout this paper, we refer to batching as the decision of whether or not to schedule similar jobs contiguously: On the other hand, lot-sizing refers to the decision on when and how to split a production lot of identical items into sublots.

Batching of similar jobs is mainly done to avoid set-up times or set-up costs. Picture, for example, a production line for colour plastics. Customer orders for several hundred different colour shades may await production. These orders can be divided into major colour groups, such as reds, blues, etc., and within a colour group, say red, they may range from very light to dark red. Set-up times between colours from the same group are small, since it would be usual for: production to graduate from lighter to darker shades. However, a large set-up is required when production switches from reds to blues, for example, since a thorough cleaning of the production line is necessary between the current colour (dark red) and the next colour (light blue). Because of these time-consuming and costly set-ups between different colour groups, production line efficiency is maximized by choosing a long run-length for each colour group. On the other hand, consider the orders for reds and blues, some of which may not be urgent, whereas others are due imminently. Customer service may then be improved by having smaller batches; for example, instead of producing a single large batch of reds in the current month and a single large batch of blues next month, it may be preferable to produce smaller batches of reds and blues in the current month to accommodate urgent orders and to process the remaining orders next month. Note that smaller batches tend to reduce average inventory levels.

Batching problems also occur in other environments, such as mechanical parts
manufacturing. In the latter, it is common to adopt principles of group technology ${ }^{1}$, whereby the factory layout is such that machines are grouped into cells. Each group technology cell then produces several families of jobs with similar production requirements. No machine set-ups are needed between two consecutively scheduled jobs from the same family, although a set-up is required between jobs of different families. In group technology, it is conventional to schedule contiguously all jobs from the same family. As shown in our colour plastics example above, this is not necessarily the best strategy. It may be better to partition each family of jobs into several batches, where all jobs of a batch are scheduled contiguously, and then schedule the batches. Solving these types of problems, therefore, requires both batching and scheduling.

We now concentrate on situations in which a job or lot consists of many identical items. Most scheduling models assume that no shipment of items is possible until the entire job is completed. However, in this case, the customer may be out of stock while awaiting delivery. Assume, for example, that a customer has a low inventory of some product and places a replenishment order consisting of a number of pallets to cover expected demand for the next few months. It may take several weeks to process the complete order. However, customer service is improved, firstly by producing a few pallets in the near future to cover the customer's demand during the current month, and then by satisfying the remaining part of the order at some later date. It is now apparent that if items or sublots may be shipped immediately upon completion, decomposing a job into sublots may improve customer service.

In multi-stage systems such as flow-shops, open-shops or job-shops, the creation of sublots permits the overlapping of different operations on the same job
and may therefore reduce throughput time. Most scheduling models allow a job to be transferred to the next machine only when it is completed on the current machine. In a model which allows lot-sizing, however, a sublot can be transferred to the next machine and processed, while other items from the same job, but of a different sublot, are processed on the current machine. We refer to this process of allowing overlaps through the creation of sublots as lot-streaming. Thus, when the decomposition of jobs is allowed, a solution procedure requires the creation of sublots through lot-sizing or lot-streaming, as well as the scheduling of sublots.

There is a vast body of literature dealing with batching and lot-sizing ${ }^{2,3}$, on the one hand, and with scheduling ${ }^{4}$, on the other. However, both worlds seem to be very much apart. The scheduling literature nearly always assumes that batching and lot-sizing decisions are already taken. Similarly, research on batching and lotsizing seldom considers sequencing issues. There are surprisingly few publications that contain elements of both fields. From the discussion above, however, it should be clear that batching, lot-sizing and scheduling decisions are strongly inter-related. Moreover, in the advent of CIM (Computer Integrated Manufacturing), batching, lot-sizing and scheduling decisions will have to be taken concurrently, i.e., they will be integrated and computer-controlled. Our motivation for studying the integration of scheduling with batching and lot-sizing should now be apparent.

This paper reviews research on scheduling which, additionally, involves an element of batching or lot-sizing. The next section describes a general model which requires both batching and lot-sizing decisions to be taken; this is followed by a discussion of applications of the model. The general model allows all trade-offs to be considered when integrating batching, lot-sizing and scheduling in a complex
environment. An ultimate aim is to tackle this general model. Since solving the general model is beyond the scope of current methodology, subsequent sections survey research on submodels that integrate scheduling with batching and lot-sizing respectively. The paper concludes with some suggestions for further research.

## A GENERAL MODEL

We now give a description of a general model which captures the notions of batching and lot-sizing. In all of the problems considered, jobs are to be scheduled on one or more machines.

Firstly, we describe a single machine problem. There are $N$ jobs, each of which is assigned to one of $F$ families. Each job $j(j=1, \ldots, N)$ becomes available for processing at time zero and requires a processing time $p_{j}$ on the machine. Furthermore, job $j$ contains $q_{j}$ identical items (each requiring a processing time $p_{j} / q_{j}$ ). Implicit in a schedule is a partition of a job into sublots; all items of a sublot are scheduled contiguously. We distinguish between discrete sublots for which the processing requirement for a sublot is $p_{j} / q_{j}$ times the (integer) number of items in a sublot, and continuous sublots where any split of the processing time $p_{j}$ defines the sublots of job $j$. In the latter case, a sublot with processing time $p$, where $0<p \leq p_{j}$, contains $p q_{j} / p_{j}$ items, irrespective of whether this quantity is an integer. The continuous sublots model provides a good approximation to the discrete sublots case when $q_{\text {j }}$ is large and is often much easier to analyze.

We now extend our model to the case where there are $M$ machines. It is possible for different sublots of the same job to be processed concurrently on different machines. However, at any time, a sublot can be processed on at most one machine.

A parallel machines problem requires $p_{j}$ units of processing of each job $j$ to be performed; the machines are identical, so there is no requirement that the processing must be scheduled on a particular machine. The more general uniform and unrelated parallel machine models in which processing times depend on the assignment of sublots to machines are not discussed here.

Our model for multi-stage systems is now explained. A flow-shop requires each sublot to be processed on machines $1, \ldots, M$ in that order. In an open-shop, each sublot is processed once on each machine, but the machine routing, which can differ between sublots, forms part of the decision process. In a flow-shop and open-shop, the processing time $p_{j m}$ of each job $j$ on each machine $m(m=1, \ldots, M)$ is specified. Different sized sublots are allowed on different machines, although in the flow-shop, no processing of a sublot on machine $m(m=2, \ldots, M)$ is allowed until all sublots containing items from this machine- $m$ sublot are completed on machine $m-1$. The more general job-shop problem in which different machine routings are prescribed for different jobs is not discussed here.

In all problems, each machine can process at most one sublot at a time. A schedule specifies sublot sizes, indicates which sublots are scheduled on which machine and defines a processing order for the relevant sublots on each machine. Machine set-ups for single and parallel machine problems are necessary as follows. If a sublot of a job from family $g$ is sequenced first on a machine, a major set-up requiring time $s_{0 g}$ is needed. Also, after a sublot of a job from family $f$ is scheduled, a major set-up requiring time $s_{f}$, is needed before a sublot of a job from family $g$ ( $g \neq f$ ) is processed next. No major set-up is necessary between sublots of jobs belonging to the same family, however. Additionally, a minor set-up time $t_{j}$ is re-
quired immediately before a sublot of job $j$ is processed. If for each family $g$ we have that $s_{f g}$ is independent of $f$ for $f \neq g$, i.e., if $s_{0_{g}}=s_{f g}=s_{g}$ for all families $f$ and $g$, where $f \neq g$, then set-up times are sequence independent; otherwise they are sequence dependent. We have defined a set-up time model in which no processing can occur on a machine while it is undergoing a set-up. A set-up cost model replaces these set-up times with set-up costs: $c_{0_{g}}, c_{f}$ and $b_{j}$ are costs corresponding to $s_{0_{g}}$, $s_{f g}$ and $t_{j}$ respectively. We make the reasonable assumption that set-up times and costs satisfy the triangle inequality, i.e., $s_{f h} \leq s_{f g}+s_{g h}$ and $c_{f h} \leq c_{f g}+c_{g h}$, for all distinct families $f, g$ and $h$ including the case $f=0$. For flow-shop and open-shop problems where the machines are not identical, set-ups may vary between machines; hence an additional index $m$ may be necessary to specify set-up times and costs on machine $m(m=1, \ldots, M)$.

For each job $j$, we define a due date $d_{j}$ which is applicable to each item $i$ of job $j$, i.e., $d_{i}=d_{j}$. Furthermore, a positive (importance) weight $w_{j}$ is divided equally over all $q_{j}$ items of job $j$, i.e., $w_{i}=w_{j} / q_{j}$ for each item $i$ of job $j$. Consider a typical item $i$ of job $j$ which belongs to sublot $k$ in some schedule. In an item completion time model, item $i$ is deemed to be completed immediately after its processing is finished. Alternatively, it may be assumed that item $i$ is completed only when the processing of sublot $k$ is finished or when the processing of job $j$ is finished. These cases define sublot completion time and job completion time models respectively. Thus, having specified the model, the completion time $C_{i}$ of each item $i$ is easily determined for any schedule. Also, for each item $i$, its lateness

$$
L_{i}=C_{i}-d_{i}
$$

$$
T_{i}=\max \left\{C_{i}-d_{i}, 0\right\}
$$

and

$$
U_{i}= \begin{cases}1 & \text { if } C_{i}>d_{i} \\ 0 & \text { otherwise }\end{cases}
$$

can be found. Possible objectives to be minimized are the maximum completion time $C_{\max }=\max _{i}\left\{C_{i}\right\}$, the maximum lateness $L_{\max }=\max _{i}\left\{L_{i}\right\}$, the total (weighted) completion time $\sum_{i}\left(w_{i}\right) C_{i}$, the total (weighted) tardiness $\sum_{i}\left(w_{i}\right) T_{i}$, or the (weighted) number late $\sum_{i}\left(w_{i}\right) U_{i}$, where each maximum and each summation is over all items $i$. For set-up cost models, the total set-up cost is added to the appropriate scheduling objective function to give an overall cost to be minimized.

It should be noted that we do not discuss preemption in our general model. As pointed out above, preemption of sublots is not allowed. However, an item can be split between different sublots under our continuous sublots model (although whether this corresponds to item preemption in the conventional sense depends on which objective function is assumed).

We conclude this section by adapting the three-field problem descriptor of Lawler et al. ${ }^{4}$ to our general model. In this three-field notation, a problem type is represented by $\alpha|\beta| \gamma$, where $\alpha$ represents the machine environment, $\beta$ defines the job characteristics and $\gamma$ is the objective function. Let o denote the empty symbol. The first field takes the form $\alpha=\alpha_{1} \alpha_{2}$, where $\alpha_{1}$ and $\alpha_{2}$ are interpreted as follows.

- $\alpha_{1} \in\{o, P, F, O\}:$
- $\alpha_{1}=0$ : a single machine;
- $\alpha_{1}=P:$ identical (parallel) machines;
- $\alpha_{1}=F:$ a flow-shop;
- $\alpha_{1}=O:$ an open-shop.
- $\alpha_{2} \in\{o, M\}$ :
- $\alpha_{2}=0$ : the number of machines is arbitrary;
- $\alpha_{2}=M$ : there are a fixed number of machines $M$.

We note that for a single machine problem $\alpha_{1}=0$ and $\alpha_{2}=1$, whereas $\alpha_{1} \neq 0$ and $\alpha_{2} \neq 1$ for other problem types. The second field $\beta \subseteq\left\{\beta_{1}, \beta_{2}, \beta_{3}\right\}$ indicates job characteristics as follows.

- $\beta_{1} \in\left\{o, s_{f}, s_{f}\right\}$ :
- $\beta_{1}=0$ : there are no major set-up times;
- $\beta_{1}=s_{f}$ : families are specified, each having a major sequence independent set-up time on each machine;
- $\beta_{1}=s_{f g}$ : families are specified, each having a major sequence dependent set-up time on each machine.
- $\beta_{2} \in\left\{o, q_{j}(\lambda, \mu)\right\}:$
- $\beta_{2}=0$ : each job contains a single item;
- $\beta_{2}=q_{j}(\lambda, \mu)$ : jobs containing several items may be split into sublots.
- $\lambda \in\{c, d, *\}:$
- $\lambda=c$ : jobs are split into continuous sublots;
- $\lambda=d$; jobs are split into discrete sublots;
- $\lambda=*:$ refers to both problems types $\lambda=c$ and $\lambda=d$.
- $\mu \in\{j, i, s, *\}:$
- $\lambda=j:$ job completion times;
- $\lambda=i$ : item completion times;
- $\lambda=s$ : sublot completion times;
- $\lambda=*:$ refers to the three problem types $\lambda=j, \lambda=i$ and $\lambda=s$.
- $\beta_{3} \in\left\{o, t_{j}\right\}:$
- $\beta_{3}=0$ : there are no minor set-up times;
- $\beta_{3}=t_{j}:$ for each job, a minor set-up time is incurred for each of its sublots on each machine.

Lastly, the third field defines the objective in the form $\gamma=\gamma_{1}+\gamma_{2}+\gamma_{3}$, where

- $\gamma_{1} \in\left\{C_{\max }, L_{\max }, \sum C_{i}, \sum w_{i} C_{i}, \sum T_{i}, \sum w_{i} T_{i}, \sum U_{i}, \sum w_{i} U_{i}\right\}$;
while $\gamma_{2}$ and $\gamma_{3}$ define any major and minor set-up costs as follows.
- $\gamma_{2} \in\left\{o, \sum c_{f}, \sum c_{f}\right\}$ :
- $\gamma_{2}=0$ : there are no major set-up costs;
- $\gamma_{2}=\sum c_{\rho}:$ families are specified, each having a major sequence independent set-up cost on each machine;
- $\gamma_{2}=\sum c_{f g}:$ families are specified, each having a major sequence dependent set-up cost on each machine.
- $\gamma_{3} \in\left\{o, \sum b_{j}\right\}:$
- $\gamma_{3}=0$ : there are no minor set-up costs;
- $\gamma_{3}=\sum b_{j}$ : for each job, a minor set-up cost is incurred for each of its sublots on each machine.

To illustrate the three-field descriptor, we present three examples.
$1\left|s_{f}\right| L_{\text {max }}$ is the problem of scheduling families of jobs on a single machine to minimize the maximum lateness, where each job contains a single item. Major sequence independent set-up times are necessary when the machine switches to processing jobs from a different family, but there are no minor set-ups.
$P \| \sum C_{i}$ is the problem of scheduling jobs on an arbitrary number of identical parallel machines to minimize the total completion time. Each job contains a single item and no machine set-ups are necessary.
$F 2\left|q_{j}(c, s)\right| C_{\max }+\sum b_{j}$ is the problem of scheduling jobs, each containing several items, in a two-machine flow shop. Jobs may be split into continuous sublots and sublot completion times are assumed. There are no major set-ups, although a minor set-up cost is incurred whenever a sublot is processed on a machine. The objective is to minimize the maximum completion time plus the total set-up cost.

## DISCUSSION OF THE MODEL

From the description above, it is clear that standard non-preemptive scheduling models which do not allow jobs to be split into sublots and which do not consider set-ups are special cases of our general model. Lawler et al. ${ }^{4}$ present an excellent review of standard scheduling theory. Polynomial-time algorithms are known for some standard non-preemptive problems. For a single machine, the maximum lateness problem $1\left|\mid L_{\max }\right.$ is solved by the earliest due date (EDD) rule of Jackson ${ }^{5}$, the total weighted completion time problem $1 \| \sum w_{i} C_{i}$ is solved by the shortest weighted processing time (SWPT) rule of Smith $^{6}$ and the number late problem $1 \mid \sum U_{i}$ is solved by the algorithm of Moore. ${ }^{7}$ For parallel machines, the total completion time problem $P \| \sum C_{\mathrm{i}}$ is solved by Conway et al. ${ }^{8}$ using a generalization of the SPT rule. Finally, for two machines, maximum completion time problems for the flow-shop $F 2\left|\mid C_{\max }\right.$ and open-shop $\left.O 2\right| \mid C_{\text {max }}$ are solved by algorithms of Johnson ${ }^{9}$ and Gonzales and Sahni ${ }^{10}$ respectively. This collection of problems is of primary concern in this paper. Most other standard non-preemptive problems, in-
cluding the single machine weighted number late and the total (weighted) tardiness problems (1\| $\left|\mid w_{i} U_{i}\right.$ and $\left.1 \| \sum\left(w_{i}\right) T_{i}\right)$, the parallel machine maximum completion time and total weighted completion time problems $\left(P \| C_{\max }\right.$ and $\left.P \| \sum w_{i} C_{i}\right)$, the maximum lateness and total completion time problems for the two-machine flowshop $\left(F 2 \| L_{\max }\right.$ and $\left.F 2 \| \sum C_{i}\right)$ and open-shop $\left(O 2 \| L_{\max }\right.$ and $\left.O 2 \| \sum C_{i}\right)$, and the maximum completion time problem for the three-machine flow-shop ( $F 3 \| C_{\max }$ ) and open-shop $\left(O 3\left|\mid C_{\max }\right)\right.$, are NP-hard. ${ }^{10-16}$ Each problem in this latter collection is clearly NP-hard under our more general model.

We note that some special cases of our general model reduce essentially to a problem involving batching or to a problem involving lot-sizing. More precisely, if every job consists of a single item (and continuous sublots are not allowed), then we have a batching problem. On the other hand, a lot-sizing problem results if every family contains a single job. Below, we discuss some applications of the batching and lot-sizing problems.

Applications of the batching problem are varied. Machines which use different colours of paint provide an obvious instance where sequence dependent set-ups are necessary. Alternatively, consider the scheduling of tasks in a computer system. Each task has a requirement for a particular compiler to be resident in the computer's memory before it can be executed. If the appropriate compiler is resident, then the task may start immediately; otherwise a set-up is incurred to bring the relevant compiler into memory. In this example, a sequence independent set-up time is necessary to load the compiler into memory since this operation does not depend on which compiler is previously resident. A final example occurs when labour is a limiting resource. ${ }^{17}$ Before a job can be processed on a particular machine, it
may be necessary to switch an operator from another machine, thereby incurring a set-up.

We now discuss the practical relevance of our lot-sizing model. In the sublot completion time model, the completion times of the selected sublots define when deliveries occur. It may be argued that a sublot completion time model with set-up costs is of special interest: in effect, the set-up costs represent the extra delivery costs when shipping small quantities in a Just-In-Time environment. Also, the usefulness of lot-streaming in multi-stage systems should be clear from the increased industrial interest in smaller throughput times and the emphasis that recent production scheduling systems place on the desirability of overlapping operations.

The next two sections review research on batching and lot-sizing models respectively. The literature dealing with multi-machine models is sparse since most research has focused on single machine scheduling. Nevertheless, single machine scheduling algorithms are commonly used to schedule bottleneck machines in various production environments. Furthermore, results derived for single machine models often provide the basis for heuristic methods which are used to schedule more complex systems.

## BATCHING MODELS

In this section, we review results on the batching model. Recall that for the batching model, every job consists of a single item which cannot be split. A major set-up time or cost is incurred when a machine switches from processing a job in one family to a job in another. There are no minor set-ups in a batching model. Throughout the discussion below, set-ups are assumed to refer to major set-ups.

Our main aim is to describe algorithms and state the computational complexity for the various problems of interest. A summary of results for sequence independent set-ups is shown in Table 1. (Where available, corresponding results for sequence dependent set-ups are given in the text.) Entries in Table 1 are listed according to whether the group technology assumption that all jobs within a family are scheduled contiguously is imposed, to whether a set-up time or set-up cost model is assumed and to whether the number of families $F$ is fixed or arbitrary. It should be understood that both set-up times and costs are implicit under group technology, whereas either times or costs (but not both) are assumed for other entries in Table 1.

## Single machine problems

We first discuss problems with sequence independent set-up times and costs under the group technology assumption that all jobs within a family are scheduled contiguously. For the maximum lateness and total weighted completion time problems, jobs within a family are sequenced in EDD order (non-decreasing order of $d_{j}$ ) and SWPT order (non-decreasing order of $p_{j} / w_{j}$ ) respectively. Furthermore, scheduling of families is straightforward if each family is treated as a single composite job. ${ }^{19}$ Assume, without loss of generality, that jobs from the same family $f(f=1, \ldots, F)$ are numbered consecutively as $j, \ldots, k$. Furthermore, for the maximum lateness problem, assume that this numbering is consistent with an EDD ordering, i.e., $d_{j} \leq \ldots \leq d_{k}$. For both problems, the composite job corresponding to family $f$ has processing time $s_{j}+\sum_{h=j}^{k} p_{h}$. The due date of the composite job corresponding to family $f$ in the maximum lateness problem is $\min _{j^{\prime} \in\{j, \ldots, k]}\left\{d_{j^{\prime}}+\sum_{h=j^{\prime}+1}^{k} p_{h}\right\}$ and in the total weighted completion time problem the weight of the composite job is

Table 1. Complexity of batching problems with sequence independent set-ups

| Problem | Group <br> Technology | Set-up Times |  | Set-up Costs |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Fixed $F$ | Arbitrary $F$ | Fixed $F$ | Arbitrary $F$ |
| $1\left\|s_{\rho}\right\| L_{\text {max }}+\sum c_{\rho}$ | $O(N \log N)$ | $O\left(F^{2} N^{2 F}\right)$ | NP-hard | $O\left(F^{2} N^{2 F}\right)$ | NP-hard |
| $1\left\|s_{j}\right\| \sum C_{i}+\sum c_{j}$ | $O(N \log N)$ | $O\left(F^{2} N^{F}\right)$ | open | $O\left(F^{2} N^{F}\right)$ | open |
| $1\left\|s_{j}\right\| \sum w_{i} C_{i}+\sum c_{j}$ | $O(N \log N)$ | $O\left(F^{2} N^{2 F}\right)$ | open | $O\left(F^{2} N^{F}\right)$ | open |
| $1\left\|s_{j}\right\| \sum U_{i}+\sum c_{j}$ | open | $O\left(F^{2} N^{F+1}\right)$ | NP-hard | $O\left(F^{2} N^{2 F+1}\right)$ | NP-hard |
| $P\left\|s_{j}\right\| \sum C_{i}+\sum c_{j}$ | open | open | open | open | open |
| $F 2\left\|s_{j}\right\| C_{\max }+\sum c_{j}{ }^{*}$ | $O(N \log N)$ | $O\left(F^{2} N^{2 F}\right)$ | open | $O\left(F^{2} N^{2 F}\right)$ | open |
| $O 2\left\|s_{j}\right\| C_{\text {max }}+\sum c_{j}$ | open | open | open | open | open |

[^0]$\sum_{h=j}^{k} w_{h}$. For the maximum lateness problem composite jobs are sequenced in EDD order, whereas for the total weighted completion time problem composite jobs are sequenced in SWPT order. These algorithms for the maximum lateness and total weighted completion time problems both require $O(N \log N)$ time. Unfortunately, the composite job approach does not extend to the number late problem.

We now turn our attention to the more general set-up time problem in which the group technology assumption is not imposed. Monma and Potts ${ }^{18}$ derive results about the ordering of jobs within a family for single machine problems with sequence dependent set-up times; these results remain valid if set-up costs are additionally introduced. For the maximum lateness problem, jobs within each family are sequenced in EDD order, whereas they are sequenced in SWPT order for the total weighted completion time problem. Furthermore, on-time jobs in the weighted number late problem are sequenced in EDD order. Using the methodology of Lawler and Moore ${ }^{20}$, a dynamic programming algorithm is derived by Monma and Potts for $1\left|s_{f_{g}}\right| L_{\max }$ and $1\left|s_{f_{g}}\right| \sum w_{i} C_{i}$. State variables indicate the number of jobs of each family that are scheduled (from which the set of scheduled jobs is deduced, since the order of jobs within each family is known), the number of times each of the $F^{2}$ types of set-up is used and the family to which the last scheduled job belongs. The completion time of the last scheduled job is easily computed from these state variables which enables objective function contributions to be evaluated. Using these algorithms, the time requirement for $1\left|s_{f g}\right| L_{\max }$ and $1\left|s_{f_{g}}\right| \sum w_{i} C_{i}$ is $O\left(F^{2} N^{\left.F^{2}+F\right)}\right.$ and for $1\left|s_{j}\right| L_{\text {max }}$ and $1\left|s_{j}\right| \sum w_{i} C_{i}$ is $O\left(F^{2} N^{2 F}\right)$. For $1\left|s_{f}\right| \sum C_{i}$, Ahn and Hyun ${ }^{21}$ observe that objective function contributions can be evaluated without explicitly computing the completion time of the last scheduled job. Their dynamic program-
ming algorithm avoids state variables which indicate the number of times each type of set-up is used, thereby yielding the time complexity for $\left.1\right|_{s_{g}} \mid \sum C_{i}$ as $O\left(F^{2} N^{F}\right)$. A modified dynamic programming approach is needed for $1\left|s_{f}\right| \sum w_{i} U_{i}$ because the presence of late jobs stops the computation of the completion time of the last scheduled on-time job from the number of jobs of each family scheduled and the number of each type of set-up. The algorithm of Monma and Potts assumes that each weight is an integer and uses as state variables the number of jobs of each family that are scheduled, the weighted number of late jobs amongst those considered and the family to which the last on-time job belongs; the minimum completion time of the last on-time job is stored as a function value. Using this algorithm, $1\left|s_{f}\right| \sum w_{i} U_{i}$ and $1\left|s_{f_{g}}\right| \sum w_{i} U_{i}$ are solved in $O\left(F^{2} N^{F} W\right)$ time, where $W$ is the sum of all job weights. This time complexity becomes $O\left(F^{2} N^{F+1}\right)$ for $1\left|s_{j}\right| \sum U_{i}$ and $1\left|s_{f}\right| \sum U_{i}$ in which $W=N$.

The recursions of Monma and Potts ${ }^{18}$ can be modified to provide corresponding algorithms, with identical time complexities, for the maximum lateness and total weighted completion time problems in which set-up costs replace set-up times. Moreover, for $1 \| \sum w_{i} C_{i}+\sum c_{\rho g}$ the state variables representing numbers of times each type of set-up is used are not needed: set-up cost contributions are added to the objective function when a job is scheduled. The time complexity is therefore reduced to $O\left(F^{2} N^{F}\right)$, even for sequence dependent set-up costs. We note that this approach for the total weighted completion time problem is essentially equivalent to applying the algorithm of Baker and Schrage ${ }^{22}$, where each precedence constraint chain corresponds to enforcing the SWPT sequence on the jobs of a family. For $1\left|\mid \sum w_{i} U_{i}+\sum c_{f}\right.$ and 1$| \mid \sum w_{i} U_{i}+\sum c_{f g}$, we require additional state
variables indicating the number of times each type of set-up is used. This leads to a dynamic programming algorithm with a time complexity of $O\left(F^{2} N^{F^{2}+F} W\right)$ for $1\left|\mid \sum w_{i} U_{i}+\sum c_{\rho,}\right.$ and of $O\left(F^{2} N^{2 F} W\right)$ for 1$| \mid \sum w_{i} U_{i}+\sum c_{\rho}$.

Reviewing the complexities of $1\left|s_{f g}\right| L_{\max }, \quad 1| | L_{\max }+\sum c_{f g}, 1\left|s_{f g}\right| \sum w_{i} C_{i}$, $1\left|\left|\sum w_{i} C_{i}+\sum c_{f g}, \quad 1\right| s_{f g}\right| \sum U_{i}$ and $1\left|\mid \sum U_{i}+\sum c_{f g}\right.$, we observe that each is polynomially solvable when $F$ is fixed. When $F$ is arbitrary, results of Bruno and Downey ${ }^{23}$ show that $1\left|s_{f}\right| L_{\max }, 1| | L_{\max }+\sum c_{f}, 1\left|s_{f}\right| \sum U_{i}$ and $1\left|\mid \sum U_{i}+\sum c_{f}\right.$ are NP-hard. The complexity of $1\left|s_{f}\right| \sum\left(w_{i}\right) C_{i}, 1\left|s_{f}\right| \sum\left(w_{i}\right) C_{i}, \quad 1| | \sum\left(w_{i}\right) C_{i}+\sum c_{f}$ and $1 \| \sum\left(w_{i}\right) C_{i}+\sum c_{f g}$ for arbitrary $F$ remains open, however.

Zdrzalka ${ }^{24}$ proposes heuristic methods for $1\left|s_{f}=1\right| L_{\max }$ in which there are unit set-up times. To facilitate worst-case analysis, he assumes that all due dates are non-positive. When all jobs of a family are scheduled contiguously (as in the group technology assumption), the resulting schedule is shown to have a maximum lateness which does not exceed twice the optimal value. He also suggests an improvement which allows each family to be split into at most two batches. At each iteration of this procedure, a job is shifted from the first to the second batch of its family, after which the resulting batches are resequenced. This improved heuristic requires $O\left(N^{2}\right)$ time and generates a schedule for which the maximum lateness does not exceed $5 / 3$ times that of an optimal schedule.

Mason and Anderson ${ }^{25}$ propose a branch and bound algorithm for $1\left|s_{f}\right| \sum w_{i} C_{i}$. By incorporating various dominance rules to restrict the search, their algorithm is able to solve problems with up to 30 jobs. Gupta ${ }^{26}$ and Ahn and Hyun ${ }^{21}$ present heuristic methods for $1\left|s_{f g}\right| \sum C_{i}$. Gupta's method constructs partial schedules using the earliest completion time rule: the job which is appended to the current
partial sequence is chosen so that its completion time is as small as possible. Ahn and Hyun suggest an improvement heuristic which attempts to reduce the total completion time of the current sequence by shifting contiguously scheduled jobs from the same family to another position. Computational results show that this improvement heuristic generates superior solutions to those obtained using Gupta's method.

## Parallel machine problems

Following the approach of Monma and Potts ${ }^{18}$, it is possible to derive dynamic programming algorithms for various parallel machine problems. Unfortunately, the resulting algorithms are of little practical interest because of their enormous space and time requirements. The complexity of $P\left|s_{f}\right| \sum C_{i}, \quad P\left|s_{f}\right| \sum C_{i}$, $P \| \sum C_{i}+\sum c_{j}$ and $P \| \sum C_{i}+\sum c_{f g}$ is open.

Under the assumption that all items have a common due date, $\mathrm{So}^{27}$ proposes three heuristic methods for the following variant of $P\left|s_{f}, q_{j}(d, i), t_{j}\right| \sum w_{i} U_{i}$. (Although this model involves lot-sizing in addition to batching, it is appropriate to discuss it in this section.) The $q_{j}$ items of job $j(j=1, \ldots, N)$ are not identical, although, within each job, item weights are assumed to be' 'agreeable': items of each job can be listed so that their processing times are non-decreasing and their weights are non-increasing. Two of the heuristics employ pseudopolynomial dynamic programming procedures to generate a schedule. The first schedules the machines sequentially with a view to maximizing the total weight of scheduled items at each stage, while the second solves a single machine problem obtained by aggregating capacities and then assigns the scheduled jobs to the original machines. The third
heuristic is a greedy method which, at each iteration, selects and schedules several items of a job on a machine so that they are on time: the items and the machine are chosen so that the ratio of total weight to total processing plus (major and minor) set-up time is as large as possible. Computational tests indicate that the schedules generated by the greedy method are usually at least comparable with those given by the computationally more expensive heuristics which use dynamic programming.

Flow-shop and open-shop problems

Firstly, we concentrate on the maximum completion time problem in a flowshop with sequence independent set-ups under the group technology assumption that all jobs of a family are scheduled contiguously. For two machines, Sekiguchi ${ }^{28}$ shows that jobs within each family are sequenced according to Johnson's rule ${ }^{9}$ and he derives a composite job approach to schedule families. This yields an algorithm which requires $O(N \log N)$ time for set-up times and costs. Vakharia and Chang ${ }^{29}$ perform a computational comparison of various heuristic methods on problems with more than two machines. They find that a simulated annealing heuristic provides good quality solutions at reasonable computational expense.

When the group technology assumption is not imposed, it is straightforward to construct two-job instances of $F 2\left|s_{f g}\right| C_{\max }$ and $F 2\left|\mid C_{\max }+\sum c_{f g}\right.$ for which no optimal schedule has identical processing orders on each machine. However, for $F 2\left|s_{f}\right| C_{\max }$ and $F 2\left|\mid C_{\max }+\sum c_{f}\right.$, it is unclear whether processing orders on both machines may be assumed identical. If the permutation flow-shop is considered in which processing orders are constrained to be identical, then it can be shown that jobs within a family are sequenced by Johnson's rule for $F 2\left|s_{f}\right| C_{\max }+\sum c_{f g}$. Fur-
thermore, using the same state variables as for $1\left|s_{f g}\right| L_{\max }$ and $1\left|s_{f}\right| \sum w_{i} C_{i}$, the dynamic programming approach of Monma and Potts ${ }^{18}$ can be employed. The completion time of the last scheduled job on the first machine is easily computed from the state variables and its completion time on the second machine is stored as a function value. The resulting algorithm requires $O\left(F^{2} N^{F^{2}+F}\right)$ time for $F 2\left|s_{f g}\right| C_{\text {max }}$ and $F 2 \| C_{\max }+\sum c_{f g}$, and requires $O\left(F^{2} N^{2 F}\right)$ time for $F 2\left|s_{f}\right| C_{\max }$ and $F 2 \| C_{\max }+\sum c_{f}$, where the permutation flow-shop is assumed in each case. For arbitrary $F$, however, the complexity of $F 2\left|s_{f}\right| C_{\max }$ and $F 2\left|\mid C_{\max }+\sum c_{f}\right.$ is open.

No results are currently available for the maximum completion time in a twomachine open-shop. A key issue concerns the existence, or otherwise, of an optimal solution of $O 2\left|s_{f}\right| C_{\max }$ and $O 2\left|\mid C_{\max }+\sum c_{f}\right.$ in which all jobs within a family are scheduled contiguously, i.e., the group technology assumption is satisfied.

## LOT-SIZING MODELS

We survey results on lot-sizing models in this section. Recall that for the lotsizing model, every family consists of a single job. There are no major set-ups between sublots of different jobs, although minor set-ups between sublots may be necessary. Thus, throughout this section, a set-up is assumed to refer to a minor set-up.

As in the previous section, we describe algorithms and state the computational complexity for the various problems of interest. Table 2 summarizes results for the job, item and sublot completion time models. Even though there are minor differences in approach in some cases, the results of Table 2 are valid irrespective of whether a set-up time or a set-up cost model is adopted and of whether discrete

Table 2. Complexity of lot-sizing problems

|  | Completion Times |  |  |
| :--- | :--- | :--- | :--- |
| Problem | Job: $\mu=j$ | Item: $\mu=i$ | Sublot: $\mu=s$ |
| $1\left\|q_{j}(*, \mu), t_{j}\right\| L_{\max }+\sum b_{j}$ | $O(N \log N)$ | $O(N \log N)$ | $O(N \log N)$ |
| $1\left\|q_{j}(*, \mu), t_{j}\right\| \sum\left(w_{i}\right) C_{i}+\sum b_{j}$ | $O(N \log N)$ | $O(N \log N)$ | open |
| $1\left\|q_{j}(*, \mu), t_{j}\right\| \sum U_{i}+\sum b_{j}$ | NP-hard | NP-hard | NP-hard |
| $P\left\|q_{j}(*, \mu), t_{j}\right\| \sum C_{i}+\sum b_{j}$ | NP-hard | NP-hard | NP-hard |
| $F 2\left\|q_{j}(*, \mu), t_{j}\right\| C_{\max }+\sum b_{j}$ | open | open | open |
| $O 2\left\|q_{j}(*, \mu), t_{j}\right\| C_{\max }+\sum b_{j}$ | $O(N)$ | $O(N)$ | $O(N)$ |
| $* 1\left\|q_{j}(c, s)\right\| \sum\left(w_{i}\right) C_{i}+\sum b_{j}$ is solvable in $O(N \log N)$ time. |  |  |  |

or continuous sublots are assumed.

Single machine problems

We concentrate first on job completion time models for a single machine. A simple interchange argument shows that for the objective functions considered in this paper, there is no advantage in splitting a job into sublots (although if jobs have different release dates, splitting may be beneficial). Thus, standard scheduling algorithms may be useful. For instance, $1\left|q_{j}(*, j), t_{j}\right| L_{\max }+\sum b_{j}$ is solved by sequencing jobs in EDD order and $I\left|q_{j}(*, j), t_{j}\right| \sum w_{i} C_{i}+\sum b_{j}$ is solved by sequencing jobs in mon-decreasing order of $\left(t_{j}+p_{j}\right) / w_{j}$. However, $1\left|q_{j}(*, j)\right| \sum U_{i}$ is equivalent to $1 \| \sum w_{i} U_{i}$ (where the weight in the latter problem corresponds to the number of items in a job in the former problem $)$. Thus, $1\left|q_{j}(*, j)\right| \sum U_{i}$ is NP-hard.

Next, item completion time models are considered. Again, an interchange argument shows that for $1\left|q_{j}(*, i), t_{j}\right| L_{\max }+\sum b_{j}$ and $1\left|q_{j}(*, i), t_{j}\right| \sum w_{i} C_{i}+\sum b_{j}$, there is an optimal solution in which no jobs are split (Santos ${ }^{30}$ proves this for the maximum lateness problem and Dobson et al. ${ }^{31}$ prove it for the total weighted completion time problem). Solution procedures for these two problems, therefore, are identical with those for the job completion time model. For $1\left|q_{j}(*, i), t_{j}\right| \sum U_{i}+\sum b_{j}$, it is easily verified that jobs are split into at most two sublots which contain on-time and late items respectively. It can also be shown that $1\left|q_{j}(*, i), t_{j}\right| \sum U_{i}$ is NP-hard when all jobs have a common due date and that $1\left|q_{j}(*, i)\right| \sum U_{i}+\sum b_{j}$ is NP-hard (for arbitrary due dates). ${ }^{32}$

Finally, we concentrate on the sublot completion time model. It is easily verified that $1\left|q_{j}(*, s), t_{j}\right| L_{\max }+\sum b_{j}$ is again solved by sequencing jobs in EDD order,
without splitting into sublots. Furthermore, identical reductions to those used for the item completion time model can be employed to show that $1\left|q_{j}(*, s), t_{j}\right| \sum U_{i}$ and $1\left|q_{j}(*, s)\right| \sum U_{i}+\sum b_{j}$ are NP-hard. The problem $1\left|q_{j}(c, s)\right| \sum w_{i} C_{i}+\sum b_{j}$ is solved in $O(N \log N)$ time as follows. Firstly, sublots are sequenced in SWPT order which indicates that all sublots of the same job are scheduled contiguously. Secondly, it can be shown that all sublots of the same job should contain the same number of items. Lastly, the number of sublots for job $j(j=1, \ldots, N)$ is either $\left\lfloor\sqrt{p_{j} w_{j} /\left(2 b_{j}\right)}\right\rfloor$ or $\left\lceil\sqrt{p_{j} w_{j} /\left(2 b_{j}\right)}\right\rceil$ ( $\lfloor x\rfloor$ is the largest integer which is less than or equal to $x ;\lceil x\rceil$ is the smallest integer which is greater than or equal to $x$ ); the one which yields the smaller overall cost is selected. For the case of a single job, $1\left|q_{j}(*, s), t_{j}\right| \sum\left(w_{i}\right) C_{i}$ is analyzed by Dobson et al., Santos and Magazine ${ }^{33}$ and Naddef and Santos. ${ }^{34}$ For $1\left|q_{j}(c, s), t_{j}\right| \sum\left(w_{i}\right) C_{i}$, Dobson et al. show that the job should be divided into $k$ sublots, where $k=\lceil\sqrt{(t+8 p) /(4 t)}-1 / 2\rceil$ (since there is a single job, the subscripts on $t, q$ and $p$ are dropped), where sublot $h(h=1, \ldots, k)$ contains $x_{h}=q / k+t q(k+1) /(2 p)-h t q / p$ items. They also propose constructive and improvement heuristics for the $N$-job problem. Naddef and Santos derive analogous results the single-job problem $1 \backslash q_{j}(d, s), t_{j} \mid \sum\left(w_{i}\right) C_{i}$. They propose an algorithm in which, firstly, $k$ sublots are considered and sublot sizes $\left\lfloor x_{1}\right\rfloor, \ldots,\left\lfloor x_{k}\right\rfloor$ are set. Remaining items are assigned to sublots using a greedy approach. The entire procedure is repeated with the value of $k$ reduced by one and the better of the two solutions is selected. Naddef and Santos also propose a heuristic for the corresponding $N$-job problem. For every job, their method schedules all its sublots contiguously. In spite of these results for a single job, the complexity of the $N$-job problem $1\left|q_{j}(*, s), t_{j}\right| \sum\left(w_{i}\right) C_{i}$ is open.

We claim that $P 2\left|q_{j}(*, *), t_{j}\right| \sum C_{i}$ and $P 2\left|q_{j}(*, *)\right| \sum C_{i}+\sum b_{j}$ are NP-hard (irrespective of whether discrete or continuous sublots are considered or of whether a job, item or sublot completion time model is assumed). Arguing informally, by assigning large set-up costs, jobs will not be split into sublots. Similarly, a large set-up time relative to the processing time will also prevent a split. Thus, given an instance of the NP-hard problem $P 2\left|\mid \sum w_{i} C_{i}\right.$ with integer weights, it is possible to construct an equivalent instance of $P 2\left|q_{j}(*, *), t_{j}\right| \sum C_{i}$ or $P 2 \nmid q_{j}(*, *) \mid \sum C_{i}+\sum b_{j}$ in which the number of items in a job corresponds to the weightin $P 2 \| \sum w_{i} C_{i}$.

Monma and Potts ${ }^{18}$ show that $P 2\left|q_{j}(c, *), t_{j}\right| C_{\max }$ is NP-hard. A straightforward modification of this reduction shows that $P 2\left|q_{j}(c, *)\right| C_{\max }+\sum b_{j}$ is also NP-hard. Note that $P 2\left|q_{j}(d, *)\right| C_{\max }$ is NP-hard since it is equivalent to $P 2\left|\mid C_{\max }\right.$ when each job contains a single item. Monma and Potts ${ }^{35}$ also propose a heuristic which is applicable to $P\left|q_{j}(c, *), t_{j}\right| C_{\max }$. In its first phase, the heuristic applies list scheduling to jobs listed in non-increasing order of set-up times; i.e., the procedure of assigning the first unscheduled job on the list to the machine with the least load is applied until all jobs are scheduled. Provided it leads to a decrease in maximum completion time, the second phase splits the last job assigned to the most heavily loaded machine into two sublots and reschedules one of these sublots in the first position on the least heavily loaded machine. Sublot sizes are chosen so that this pair of machines become equally loaded. A different machine pair is selected similarly and the splitting procedure is repeated until $\lfloor M / 2\rfloor$ pairs are considered or until no reduction in completion time is possible. The procedure requires $O(N \log N)$ time and generates a schedule which has a maximum completion time which does not
exceed $5 / 3-1 / M$ if $M \geq 4,5 / 4$ if $M=2$, or $11 / 8$ if $M=3$, times that of an optimal schedule. These results are also extended to $P\left|s_{f}, q_{j}(c, *)\right| C_{m a x}$.

## Flow-shop and open-shop problems

Firstly, we review the lot-streaming problems $F\left|q_{j}(c, *)\right| C_{\text {max }}$ for which the job, item and sublot completion time models are equivalent. Our discussion assumes an identical number of sublots on each machine. Potts and Baker ${ }^{36}$ show that it is sufficient to consider sublot sizes which are the same on the second machine as they are on the first machine and which are the same on machine $M$ as they are on machine $M-1$. When sublot sizes do not vary between machines they are consistent. Thus, consistent sublots solve problems with two or three machines. Potts and Baker also derive sublot sizes for $F 2\left|q_{j}(c, *)\right| C_{\max }$ when there is a single job containing $q$ items. Let $\rho=\beta / \alpha$, where $\alpha$ and $\beta$ are the processing times of the job on the first and second machines respectively. If $k$ sublots are allowed on each machine, then sublots containing $\rho^{h-1} q /\left(1+\rho+\ldots+\rho^{k-1}\right)$ items for $h=1, \ldots, k$ yield the minimum value $M_{k}=\alpha\left(1+\rho^{k} /\left(1+\rho+\ldots+\rho^{k-1}\right)\right)$ of the maximum completion time. If there are set-up costs $b_{1}$ and $b_{2}$ on the machines, then a search for a value of $k$ which minimizes the overall cost $M_{k}+\left(b_{1}+b_{2}\right) k$ can be performed. For the case that there is a single job and two sublots are allowed on each machine, Baker and Pyke ${ }^{37}$ describe an $O(M)$ algorithm which finds consistent sublot sizes for $F\left|q_{j}(c, *)\right| C_{\max }$. No results are currently available for the lot-streaming of an arbitrary number of jobs: even $F 2\left|q_{j}(c, *)\right| C_{\text {max }}$ is open.

We now analyze $O 2\left|q_{j}(c, *)\right| C_{\max }+\sum b_{j}$. Let $b_{j m}$ denote the set-up cost incurred for each sublot of job $j(j=1, \ldots, N)$ on machine $m(m=1,2)$. Let
$P_{m}=\sum_{j=1}^{N} p_{j m}$ and $B_{m}=\sum_{j=1}^{N} b_{j m}$ for $m=1,2$. If $p_{j 1}+p_{j 2} \leq \max \left\{P_{1}, P_{2}\right\}$ for all jobs $j$, then applying the $O(N)$ algorithm of Gonzales and Sahni, without splitting jobs, yields an optimal solution with a minimum overall cost ( $C_{\max }$ plus total set-up cost) of $\max \left\{P_{1}, P_{2}\right\}+B_{1}+B_{2}$. Alternatively, if $p_{j 1}+p_{j 2}>\dot{\max }\left\{P_{1}, P_{2}\right\}$ for some job $j$, then the Gonzales and Sahni algorithm produces a schedule with an overall cost of $p_{j} 1+p_{j} 2+B_{1}+B_{2}$. If job $j$ is split into sublots of equal size on both machines, then the overall cost becomes $\max \left\{P_{1}, P_{2}\right\}+B_{1}+B_{2}+b_{j 1}+b_{j 2}$. Since no further reduction in the maximum completion time is possible, an optimal solution is selected from these two alternatives on the basis of overall cost. Clearly, to apply this procedure requires $O(N)$ time. A similar, although slightly more complicated algorithm, which also allows just two sublots of the longest job to be created, solves $O 2\left|q(c, *), t_{j}\right| C_{\max }+\sum b_{j}$ in $O(N)$ time.

## CONCLUDING REMARKS

We have described a model which, in its most general form, requires decisions to be taken on batching and lot-sizing whilst a schedule is constructed. Very little research appears to have been undertaken on this general model. The limited research on special cases, where either batching or lot-sizing decisions are made, is reviewed in the previous sections. In view of the practical importance of the general model and of the theoretical interest in many of the special cases, it is rather surprising that this area has not received more attention. Some interesting areas for future research are outlined below.

In the area of batching models, one of the most vexing issues is the complexity of $1\left|s_{\jmath}\right| \sum\left(w_{i}\right) C_{i}$ and $1 \| \sum\left(w_{i}\right) C_{i}+\sum c_{\jmath}$. Other open problems in batching
include the complexity of the $F 2\left|s_{f}\right| C_{\max }, \quad F 2| | C_{\max }+\sum c_{\rho}, \quad O 2\left|s_{f}\right| C_{\max }$ and $O 2\left|\mid C_{\max }+\sum c_{\rho}\right.$. The derivation of a branch and bound algorithm and the design and worst-case analysis of heuristic methods for $1\left|s_{f}\right| L_{\max }$ are also the subject of our current research.

Some of the more interesting problems that arise in lot-sizing and lot-streaming are, at best, only satisfactorily solved for a single job. For instance, although $1\left|q_{j}(*, s), t_{j}\right| \sum\left(w_{i}\right) C_{i}$ is well-understood for a single job, no complexity result is available for an arbitrary number of jobs. Even less is known about lot-streaming in flow-shops. Attempts should be made to extend the preliminary results of Potts and Baker ${ }^{36}$ so that set-up times can be incorporated and so that more than one job and more than two machines can be handled. An extension of lot-streaming to objectives other than the maximum completion time would also form an interesting research topic.

Finally, we mention the investigation of preemption penalties as a research topic in preemptive scheduling. Conventionally, in the literature on preemptive scheduling, there is no penalty when a job is preempted. In practice, however, it is rather unusual for a machine to be able to operate on a job immediately after processing on the previous job is terminated: it is more likely that some machine idle time is incurred which can be represented by a set-up. This situation can be handled by adopting continuous sublots in our lot-sizing model. Using this approach, Monma and Potts ${ }^{35}$ study the worst-case performance of heuristics for $P\left|q_{j}(c, *), t_{j}\right| C_{\max }$. There is also scope for research on the effect of preemption penalties in single machine problems when jobs have release dates.

## ACKNOWLEDGEMENT

This research was partially support by NATO Collaborative Research Grant 0224/88.

## REFERENCES

1. I. Ham, K. Hitomi and T. Yoshida (1985) Group Technology: Applications to Production Management. Kluwer-Nijhoff, Boston.
2. K.R. Baker (1990) Lot-sizing procedures and a standard data set: a reconciliation of the literature. J. Manufacturing Oper. Mgmt 2, 199-221.
3. J. Maes and L.N. Van Wassenhove (1988) Multi-item single-level capacitated dynamic lot-sizing heuristics: a general review. J. Opl Res. Soc. 39, 991-1004.
4. E.L. Lawler, J.K. Lenstra, A.H.G. Rinnooy Kan and D. Shmoys (1989) Sequencing and scheduling: algorithms and complexity. Report 8934/A, Econometric Institute, Erasmus University, Rotterdam.
5. J.R. Jackson (1955) Scheduling a production line to minimize maximum tardiness. Research Report 43, Management Science Research Project, University of California, Los Angeles.
6. W.E. Smith (1956) Various optimizers for single-stage production. Nav. Res. Logist. Q. 3, 59-66.
7. J.M. Moore (1968) An $n$ job, one machine sequencing algorithm for minimizing the number of late jobs. Mgmt Sci. 15, 102-109.
8. R.W. Conway, W.L. Maxwell and L.W. Miller (1967) Theory of Scheduling. Addison-Wesley, Reading, MA.
9. S.M. Johnson (1954) Optimal two- and three-stage production schedules with
setup times included. Nav. Res. Logist. Q. 1, 61-68.
10. T. Gonzales and S. Sahni (1976) Open shop scheduling to minimize finish time. J. Assoc. Comput. Mach. 23, 665-679.
11. R.M. Karp (1972) Reducibility among combinatorial problems. In Complexity of Computer Computations (R.E.Miller and J.W. Thatcher, Eds), Plenum Press, New York.
12. J. Du and J.Y.-T. Leung (1990) Minimizing total tardiness on one machine is NP-hard. Math. Opns Res. 15, 483-495.
13. J.K. Lenstra, A.H.G. Rinnooy Kan and P. Brucker (1977) Complexity of machine scheduling problems. Ann. Discrete Math. 1, 343-362.
14. J. Bruno, E.G. Coffman, Jr., and R. Sethi (1974) Scheduling independent tasks to reduce mean finishing time. Comm. ACM 17, 382-387.
15. M.R. Garey, D.S. Johnson and R. Sethi (1976) The complexity of flowshop and jobshop scheduling. Math. Opns Res. 1, 117-129.
16. J.O. Achugbue and F.Y. Chin (1982) Scheduling the open shop to minimize mean flow time. SIAM J. Comput. 11, 709-720.
17. V.K. Sahney (1972) Single-server, two-machine sequencing with switching time. Opns Res. 20, 24-36.
18. C.L. Monma and C.N. Potts (1989) On the complexity of scheduling with batch set-up times. Opns Res. 37, 798-S04.
19. E.L. Lawler (1978) Sequencing to minimize total weighted completion time subject to precedence constraints. Ann. Discrete Math. 2, 75-90.
20. E.L. Lawler and J.M. Moore (1969) A functional equation and its application to resource allocation and sequencing problems. Mgmt Sci. 16, 77-84.
21. B.-H. Ahn and J.-H. Hyun (1990) Single facility multi-class job scheduling. Computcrs Opns Res. 17, 265-272.
22. K.R. Baker and L.E. Schrage (1978) Finding an optimal sequence by dynamic programming: an extension to precedence-related tasks. Opns Res. 26, 111120.
23. J. Bruno and P. Downey (1978) Complexity of task sequencing with deadlines, set-up times and changeover costs. SIAM J. Comput. 7, 393-404.
24. S. Zdrzalka (1990) Approximation algorithms for single machine sequencing with delivery times and unit batch set-up times. European J. Opnl Res., to appear.
25. A.J. Mason and E.J. Anderson (1991) Minimizing flow time on a single machine with job classes and setup times. Nav. Res. Logist., to appear.
26. J.N.D. Gupta (1988) Single facility scheduling with multiple job classes. European J. Opnl Res. 33, 42-45.
27. K.C. So (1990) Some heuristics for scheduling jobs on parallel machines with setups. Mgmt Sci. 36, 467-475.
28. Y. Sehiguchi (1983) Optimal schedule in a GT-type flow-shop under seriesparallel precedence constraints. J. Opns Res. Soc. Japan 26, 226-251.
29. A.J. Vakharia and Y.-L. Chang (1990) A simulated annealing approach to scheduling a manufacturing cell. Nav. Res. Logist. 37, 559-577.
30. C. Santos (1984) Batching and sequencing decisions under lead time considerations for single machine problems. M.Sc. thesis, Department of Management Sciences, University of Waterloo, Waterloo.
31. G. Dobson, U.S. Karmarkar and J.L. Rummel (1987) Batching to minimize
flow times on one machine. Mgmt Sci. 33, 784-799.
32. M.Y. Kovalyov, C.N. Potts and L.N. Van Wassenhove (1990) Single machine scheduling with set-ups to minimize the number of late items. Report, Econometric Institute, Erasmus University, Rotterdam.
33. C. Santos and M. Magazine (19S5) Batching in single operation manufacturing systems. Opns Res. Lett. 4, 99-103.
34. D. Naddef and C. Santos (1988) One-pass batching algorithms for the one machine problem. Discrete Appl. Math. 21, 133-145.
35. C.L. Monma and C.N. Potts (1991) Analysis of heuristics for preemptive parallel machine scheduling with batch set-up times. Opns Res., to appear.
36. C.N. Potts and K.R. Baker (1989) Flow shop scheduling with lot streaming. Opns Res. Lett. 8, 297-303.
37. K.R. Baker and D.F. Pyke (1990) Solution procedures for the lot-streaming problem. Decision Sci. 21, 475-491.

| 88/12 | Spyros MAKRIDAKIS | "Business firms and managers in the 21st century", February 1988 |
| :---: | :---: | :---: |
| 88/13 | Manfred Kets de vries | "Alexithymia in orgauizational life: the organization man revisited", February 1988. |
| 88/14 | Alain NOEL | "The interpretation of strategies: a study of the impact of CEOs on the corporation", March 1988. |
| 88/15 | Anil DEOLALIKAR and Lars-Hendrik RÖLLER | "The production of and returns from industrial inmovation: an econometric analysis for a developing country", December 1987. |
| 88/16 | Gabriel HAWAWINI | "Market efficiency and equity pricing: international evidence and implications for global investing", March 1988. |
| 88/17 | Michael BURDA | "Monopolistic competition, costs of adjustment and the behavior of European employment", September 1987. |
| 88/18 | Michael BURDA | "Reflections on "Wait Unemployment" in Europen, November 1987, revised February 1988. |
| 88/19 | M.J. LAWRENCE and Spyros MAKRIDAKIS | "Individual biss in judgements of conindence", March 1988. |
| 88/20 | Jean DERMINE, Damien NEVEN and J.F. THISSE | "Portfolio selection by mutual funds, an equilibrium model", March 1988. |
| 88/21 | James TEBOUL | "De-industrialize service for quality", March 1988 (88/03 Revised). |
| 88/22 | Lars-Hendrik RŌLLER | ${ }^{\text {MProper }}$ Quadratic Functions with an Application to AT\&T", May 1987 (Revised March 1988). |


| 88/23 | Sjur Didrik FLAM |
| :--- | :--- |
|  | and Georges ZACCOUR |


| 88/24 | B. Espen ECKBO and |
| :--- | :--- |
|  | Herwig LANGOHR |

$88 / 25$

Everette S. GARDNER and Spyros MAKRIDAKIS

88/26 Sjur Didrik FLAM and Georges ZACCOUR
"Equilibres de Nash-Cournot dans le marché européen du gaz: un cas où les solutions en boucle ouverte et en feedback coincident", Mars 1988.
"Information disclosure, means of payment, and takeover premia. Public and Private tender offers in France", July 1985, Sixth revision, April 1988.
"The future of forecasting", April 1988.
"Semi-competitive Cournot equilibrium in multistage oligopolies", April 1988.
"Eatry game with resalable capacity", April 1988.
"The multinational corporation as a network: perspectives from interorganizational theory", May 1988.
"Consumer cognitive complexity and the dimensionality of multidimensional scaling configurations", May 1988.

The financial fallout from Chemsobyl: risk perceptions and regulatory response", May 1988.
"Creation, adoption, and diffusion of innovations by subsidiaries of multinational corporations", June 1988.
"International manufacturing: positioning plants for success", June 1988.
"The importance of flexibility in manufacturing", June 1988.88/35

| 88/34 | Mihkel M. TOMBAK |
| :---: | :---: |
| 88/35 | Mihkel M. TOMBAK |
| 88/36 | Vikas TIBREWALA and Bruce BUCHANAN |
| 88/37 | Murugappa KRISHNAN Lars-Hendrik RÖLLER |
| 88/38 | Manfred KETS DE VRIES |
| 88/39 | Manfred Kets de vries |
| 88/40 | Josef LAKONISHOK and Theo VERMAELEN |
| 88/41 | Charles WYPLOSZ |
| 88/42 | Paul EVANS |
| 88/43 | B. SINCLAIR-DESGAGNE |
| 88/44 | Essam MAHMOUD and Spyros MAKRIDAKIS |
| 88/45 | Robert KORAJCZYK and Claude VIALLET |
| 88/46 | Yves DOZ and Amy SHUEN |
| $88 / 47$ | Alain BULTEZ, Els GUSBRECHTS, |

"Flexihility: an important dimension in manufacturing", June 1988.
"A strategic analysis of investment in flexible manufacturing systems", July 1988.
"A Predictive Test of the NBD Model that Controls for Non-stationarity", June 1988.
"Requlating Price-Liability Competition To Improve Welfare", July 1988.
"The Motivating Role of Envy : A Forgotten Factor in Management", April 88.
"The Leader sas Mirror : Clinical Reflections", July 1988.
"Anomalous price behavior around repurchase tender offers", August 1988.
"Assymetry in the FMS: intentional or systemic?", August 1988.
"Organizational developuent in the transnational euterprise", June 1988.
"Groap decision support systems implement Bayesian rationality", September 1988.
"The state of the art and future directions in combining forecasts", September 1988.
"An empirical investigation of international asset pricing", November 1986, revised August 1988.
"From intent to outcome: a process framework for partnerships", August 1988.
"Asymmetric cannibalism between substitute items listed by retailers", September 1988.

Philippe NAERT and Piet VANDEN ABEELE

Michael BURDA "Reflections on 'Wait unemployment' in
Europe, II", April 1988 revised September 1988.
"Information asymmetry and equity issues", September 1988.
"Managing expert systems: from inception through updating", October 1987.
"Technology, work, and the organization: the impact of expert systems", July 1988.
"Cognition and organizational analysis: who's minding the store?", September 1988
"Whatever happened to the philosopherking: the leader's addiction to power, September 1988.
"Strategic choice of flexible production technologies and welfare implications", October 1988

Method of moments tests of contingent clainas asset pricing models", October 1988.
"Sive-sorted portfolios and the violation of the random walk hypothesis: Additional empirical evidence and inplication for tests of asset pricing models", June 1988.
"Data transferability: estimating the response effect of future events based on historical analogy", October 1988.
"Assessing economic inequality", November 1988.

| 88/59 | Martin KJLDUFF | "The interpersonal structure of decision making: a social comparison approach to organizational choice". November 1988. |
| :---: | :---: | :---: |
| 88/60 | Michael BURDA | "Is mismatch really the problem? Some estimates of the Chelwood Gate II model with US data", Septernber 1988. |
| 88/61 | Lars-Hendrik RÖLLER | "Modelling cost structure: the Bell System revisited", November 1988. |
| 88/62 | Cynthia VAN HULLE, <br> Theo VERMAELEN and <br> Paul DE WOUTERS | "Requiation, taxes and the market for corporate control in Relgium", September 1988. |
| 88/63 | Fernando NASCIMENTO and Wilfried R. VANHONACKER | "Strategic pricing of differentiated consumer durables in a dynamic duopoly: a numerical analysis", October 1988. |
| 88/64 | Kasra FERDOWS | "Charting strategic roles for international factories", December 1988. |
| 88/65 | Arnoud DE MEYER and Kasra FERDOWS | "Quality up, technology down", October 1988 |
| 88/66 | Nathalie DIERKENS | "A discussion of exact measures of information assymetry: the example of Myers and Majluf model or the importance of the asset structure of the firm", December 1988. |
| 88/67 | Paul S. ADLER and Kasra FERDOWS | "The chief technology officer", December 1988. |
| 1989 |  |  |
| 89/01 | Joyce K. BYRER and Tawfik JELASSI | "The impact of language theories on DSS dialog", January 1989. |
| 89/02 | Louis A. LE BLANC and Tawfik JELASSI | "DSS software selection: m multiple criteria decision methodology", January 1989. |


| 89/03 | Beth H. JONES and Tawfik JELASSI | "Negotiation support: the effects of computer intervention and conflict level on bargaining outcome", January 1989. | $89 / 13$ | Manfred KETS DE VRIES | "The impostor syndrome: a disquieting phenomenon in organizational life", February 1989. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 89/04 | Kasra FERDOWS and Amoud DE MEYER | "Lasting improvement in manufacturing performance: In search of a new theory", January 1989. | 89/14 | Reinhard ANGELMAR | "Product innovation: a tool for competitive advantage", March 1989. |
| 89/05 | Martin KILDUFF and Reinhard ANGELMAR | "Shared history or shared culture? The effects of time, culture, and performance on | 89/15 | Reinhard ANGELMAR | "Evaluating a firm's product innovation performance", March 1989. |
|  |  | institutionalization in simulated organizations", January 1989. | 89/16 | Wilfried VANHONACKER, Donald LEHMANN and Fareena SULTAN | "Combining related and sparse data in linear regression models", February 1989. |
| 89/06 | Mihkel M. TOMBAK and B. SINCLAIR-DESGAGNÉ | "Coordinating manufacturing and business strategies: I', February 1989. | 89/17 | Gilles AMADO, Claude FAUCHEUX and | "Changement organisationnel et réalites cuiturelles: contrastes franco-américains", |
| 89/07 | Damien J. NEVEN | "Structural adjustment in European retail banking. Some view from industrial organisation", January 1989. | 89/18 | André LAURENT <br> Srinivasan BALAK- <br> RISHNAN and | March 1989. <br> "Information asymmetry, market faihure and joint-ventures: theory and evidence", |
| 89/08 | Arnoud DE MEYER and Hellmut SCHÜTTE | "Trends in the development of technology and their effects on the production structure in the European Community", January 1989. | 89/19 | Mitchell KOZA <br> Wilfried VANHONACKER, Donald LEHMANN and | March 1989. <br> "Combining related and sparse data in linear regreasion models", Revised March 1989. |
| 89/09 | Damien NEVEN, <br> Carmen MATUTES and | "Brand proliferation and entry deterrence", February 1989. |  | Fareena SULTAN |  |
|  | Mancel CORSTJENS |  | 89/20 | Wilfried VANHONACKER and Russell WINER | "A rational random behavior model of choice", Revised March 1989. |
| 89/10 | Nathalie DIERKENS, Bruno GERARD and Pierre HILLION | "A market based approach to the valuation of the assets in place and the growth opportunities of the firm", December 1988. | 89/21 | Arnoud de MEYER and Kasra FERDOWS | "Influence of manufacturing improvement programmes oa performance", April 1989. |
| 89/11 | Manfred KETS DE VRIES and Alain NOEL | "Understanding the leader-strategy interface: <br> application of the strategic relationship interview method", February 1989. | 89/22 | Manfred KETS DE VRIES and Sydney PERZOW | "What is the role of character in psychoanalysis?" April 1989. |
| $89 / 12$ | Wilfried VANHONACKER | "Estimating dynamic response models when the data are subject to different temporal | 89/23 | Robert KORACZYK and Claude VIALLET | "Equity risk premia and the pricing of foreiph exchange risk" April 1989. |
|  |  | agkregation", January 1989. | 89/24 | Martin KILDUFF and Mitchel ABOLAFIA | "The social destruction of reality: Organisational conflict as social drama" zApril 1989. |


| 89/25 | Roger BETANCOURT and David GAUTSCHI |
| :---: | :---: |
| 89/26 | Charles BEAN, <br> Edmond MALINVAUD, <br> Peter BERNHOLZ, <br> Francesco GIAVAZZI <br> and Charles WYPLOSZ |
| 89/27 | David KRACKHARDT and Martin KILDUFF |
| 89/28 | Martin KILDUFF |
| 89/29 | Robert GOGEL and Jean-Claude LARRECHE |
| 89/30 | Lars-Hendrik ROLLER and Mihkel M. TOMBAK |
| 89/31 | Michael C. BURDA and Stefan GERLACH |
| 89/32 | Peter HAUG and Tawfik JELASSI |
| 89/33 | Bernard SINCLAIRDESGAGNÉ |
| 89/34 | Sumantra GHOSHAL and Nittin NOHRIA |
| 89/35 | Jean DERMINE and Pierre HILLION |

"Two essential characteristics of retail narkets and their economic consequences" March 1989.
"Macroeconomic policies for 1992: the transition and after", April 1989.

Friendship patterns and cuitural attributions: the control of organizational diversity", April 1989.
making: a social comparison approach to organizational choice", Revised April 1989.
"The battlefield for 1992: product strength and geographic coverage", May 1989.
"Competition and Investment in Flexible Technologies", May 1989.
"Intertemporal prices and the US trade balance in durable goods", July 1989
"Application and evaluation of a multicriteria decision support system for the dynamic selection of U.S. manufacturing locations", May 1989.

Design flexibility in monopsonistic industries", May 1989.

Requisite variety versus shared values: managing corporate-division relationships in the M-Form organisation", May 1989.
"Deposit rate ceilings and the market value of banks: The case of France 1971-1981", May 1989.

| 89/49 | Jean DERMINE | "Home country control and mutual recognition", July 1989. | $\begin{aligned} & 89 / 62 \\ & \text { (TM) } \end{aligned}$ | Arnoud DE MEYER | "Technology strategy and international R\&D operations", October 1989. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 89/50 | Jean DERMINE | "The specialization of financial institutions, the EEC model", August 1989. | $\begin{aligned} & 89 / 63 \\ & \text { (TM) } \end{aligned}$ | Enver YUCESAN and <br> Lee SCHRUBEN | "Equivalence of simulations: A graph approach", November 1989. |
| $89 / 51$ | Spyros MAKRIDAKIS | "Siding simulation: a new approach to time series forecasting", July 1989. | $\begin{aligned} & 89 / 64 \\ & \text { (TM) } \end{aligned}$ | Enver YUCESAN and Lee SCHRUBEN | "Complexity of simulation models: A graph theoretic approach", November 1989. |
| $89 / 52$ $89 / 53$ | Arnoud DE MEYER Spyros MAKRIDAKIS | "Shortening developmeat cycle times: a manufacturer's perspective", August 1989. <br> "Why combining works?", July 1989. | 89/65 <br> (TM, AC, FIN) | Soumitra DUTTA and Piero BONISSONE | "MARS: A mergers and mequisitions reasoning system", November 1989. |
| $89 / 54$ | S. BALAKRISHNAN and Mitchell KOZA | "Organisation costs and a theory of joint ventures", September 1989. | 89/66 <br> (TM,EP) | B. SINCLAIR-DESGAGNE | "On the regulation of procurement bids", November 1989. |
| $89 / 55$ | H. SCHUTTE | "Euro-Japanese cooperation in information technology", September 1989. | 89/67 <br> (FIN) | Peter BOSSAERTS and Pierre HILLION | "Market microstructure effects of government intervention in the foreign exchange market", December 1989. |
| 89156 | Wilfried VANHONACKER and Lydia PRICE | "On the practical usefulness of meta-analysis results", September 1989. |  |  |  |
| 89/57 | Taekwon KIM, Lars-Hendrik RÖLLER and Mihkel TOMBAK | "Market growth and the diffusion of multiproduct technologies", September 1989. | $1990$ <br> $90 / 01$ <br> TM/EP/AC | B. SINCLAIR-DESGAGNE | "Unavoidahle Mechanisms", January 1990. |
| $89 / 58$ <br> (EP,TM) | Lars-Hendrik RÖLLER and Mihkel TOMBAK | "Strategic aspects of fiexible production technologies", October 1989. | $\begin{aligned} & 90 / 02 \\ & \text { EP } \end{aligned}$ | Michael BURDA | Monopolistic Competition, Costs of Adjustment, and the Behaviour of European Manufacturing Employment", January 1990. |
| $\begin{aligned} & 89 / 59 \\ & \text { (OB) } \end{aligned}$ | Manfred KETS DE VRIES, <br> Daphna ZEVADI, <br> Alain NOEL and <br> Mihkel TOMBAK | "Locus of control and entrepreneurship: a three-country comparative study", October 1989. | $\begin{aligned} & 90 / 03 \\ & \text { TM } \end{aligned}$ | Arnoud DE MEYER | "Management of Communication in International Research and Development", January 1990. |
| $\begin{aligned} & 89 / 60 \\ & \text { (TM) } \end{aligned}$ | Enver YUCESAN and Lee SCHRUBEN | "Simulation graphs for design and analysis of discrete event simulation models", October 1989. | 90/04 <br> FIN/EP | Gabriel HAWAWINI and Eric RAJENDRA | "The Transformation of the European <br> Finascial Services Industry: From <br> Fragmentation to Integration", January 1990. |
| $\begin{aligned} & \text { 89/61 } \\ & \text { (All) } \end{aligned}$ | Susan SCHNEIDER and Arnoud DE MEYER | "Interpreting and responding to strateaic issues: The impact of national culture", October 1989. | 90/05 <br> FIN/EP | Gabriel HAWAWINI and Bertrand JACQUILLAT | "European Equity Markets: Toward 1992 and Beyond", January 1990. |



| 90/29 <br> FIN/AC | Nathalie DIERKENS | "A Discussion of Correct Measures of Information Asymmetry", January 1990. | $\begin{aligned} & 90 / 40 \\ & \text { OB } \end{aligned}$ | Manfred KETS DE VRIES | "Leaders on the Couch: The case of Roberto Calvi", April 1990. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| 90/30 <br> FIN/EP | Lars Tyge NIELSEN | "The Expected Utility of Portfolios of Assets", March 1990. | 90/41 <br> FIN/EP | Gabriel HAWAWINI, Ituhak SWARY end Ik HWAN JANG | "Capital Market Reaction to the Announcement of Interstate Banking Legislation", March 1990. |
| 90/31 MKT/EP | David GAUTSCHI and Roger BETANCOURT | "What Determines U.S. Retail Margins?", February 1990. | 90/42 <br> MKT | Joel STECKEL and Wilfried VANHONACKER | "Cross-Validating Regression Models in Marketing Research", (Revised April 1990). |
| $\begin{aligned} & \text { 90/32 } \\ & \text { SM } \end{aligned}$ | Srinivasan balak- <br> RISHNAN and <br> Mitchell KOZA | "Information Asymmetry, Adverse Selection and Joint-Ventures: Theory and Evidence", Revised, January 1990. | $\begin{aligned} & 90 / 43 \\ & \text { FIN } \end{aligned}$ | Robert KORAJCZYK and Claude VIALLET | "Equity Risk Premia and the Pricing of Foreign Exchange Risk", May 1990. |
| $\begin{aligned} & 90 / 33 \\ & \text { OB } \end{aligned}$ | Caren SIEHL, <br> David BOWEN and <br> Christine PEARSON | "The Role of Rites of Integration in Service Delivery", March 1990. | $90 / 44$ <br> OB | Gilles AMADO, Claude FAUCHEUX and André LAURENT | "Organisational Change and Cultural <br> Realities: Franco-American Contrasts", April 1990. |
| 90/34 <br> FIN/EP | Jean DERMINE | "The Gains from European Banking Integration, a Call for a Pro-Active Competition Policy", April 1990. | $\begin{aligned} & \text { 90/45 } \\ & \text { TM } \end{aligned}$ | Soumitra DUTTA and <br> Piero BONISSONE | "Integrating Case Based and Rule Based Reasoning: The Possibilistic Connection", May 1990. |
| $\begin{aligned} & \text { 90/35 } \\ & \text { EP } \end{aligned}$ | Jae Won PARK | "Changing Uncertainty and the TimeVarying Risk Premia in the Term Structure of Nominal Interest Rates", December 1988, | $\begin{aligned} & \text { 90/46 } \\ & \text { TM } \end{aligned}$ | Spyros MAKRIDAKIS and Michèle HIBON | "Exponential Smoothise: The Effect of Initial Values and Loss Functions on PostSample Forecasting Accuracy". |
|  |  | Revised March 1990. | $\begin{aligned} & \text { 90/47 } \\ & \text { MKT } \end{aligned}$ | Lydia PRICE and Wilfried VANHONACKER | "Improper Sempling in Natural <br> Experiments: Limitations on the Use of |
| $\begin{aligned} & \text { 90/36 } \\ & \text { TM } \end{aligned}$ | Arnoud DE MEYER | "An Enpirical Investigation of Manufacturing Strategies in European Industry", April 1990. |  |  | Meta-Analysis Results in Bayesian Updating", Revised May 1990. |
| 90/37 <br> TM/OB/SM | William CATS-BARIL | "Executive Information Systews: Developing an Approach to Open the Possibles", April 1990. | 90/48 <br> EP | Jae WON PARK | "The Information in the Term Structure of Interest Rates: Out-of-Sample Forecasting Performance", June 1990. |
| 90/38 MKT | Wilfried VANHONACKER | "Managerial Decision Behaviour and the Estinmation of Dynamic Sales Response | $\begin{aligned} & \text { 90/49 } \\ & \text { TM } \end{aligned}$ | Soumitra DUTTA | "Approximate Reasoning by Analogy to Auswer Null Queries", Junc 1990. |
|  |  | Models", (Revised February 1990). | $\begin{aligned} & 90 / 50 \\ & \text { EP } \end{aligned}$ | Daniel COHEN and Charles WYPLOSZ | "Price and Trade Effects of Exchange Rates Fluctuations and the Design of Policy |
| 90/39 TM | Louis LE BLANC and Tawfik JELASSI | "An Evaluation and Selection Methodology for Expert System Shells", May 1990. |  |  | Coordination", April 1990. |


| $\begin{aligned} & \text { 90/51 } \\ & \text { EP } \end{aligned}$ | Michael BURDA and Charles WYPLOSZ | "Gross Labour Market Flows in Europe: Some Stylized Facts", June 1990. | $\begin{aligned} & 90 / 63 \\ & \text { SM } \end{aligned}$ | Sumantra GHOSHAL and Eleanor WESTNEY | "Organising Competitor Analysis Systems", <br> August 1990 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 90 / 52 \\ & \text { FIN } \end{aligned}$ | Lars Tyge NIELSEN | "The Utility of Infinite Menus", June 1990. | $\begin{aligned} & 90 / 64 \\ & \text { SM } \end{aligned}$ | Sumantra GHOSHAL | "Internal Differentiation and Corporate <br> Performance: Case of the Multinational <br> Corporation", August 1990 |
| $\begin{aligned} & 90 / 53 \\ & \text { EP } \end{aligned}$ | Michael Burda | "The Consequences of German Economic and Monetary Union", June 1990. | $\begin{aligned} & 90 / 65 \\ & \text { EP } \end{aligned}$ | Charles WYPLOSZ | "A Note on the Real Exchange Rate Effect of German Unification", August 1990 |
| 90/54 | Damien NEVEN and | "European Financial Requlation: A |  |  |  |
| EP | Colin MEYER | Framework for Policy Analysis", (Revised May 1990). | 90/66 <br> TM/SE/FIN | Soumitra DUTTA and Piero BONISSONE | "Computer Support for Strategic and Tactical Planning in Mergers and Acquisitions", <br> September 1990 |
| $90 / 55$ | Michael BURDA and | "Intertemporal Prices and the US Trade |  |  |  |
| EP | Stefan GERLACH | Balance", (Revised July 1990). | 90/67 <br> TM/SE/FIN | Soumitra DUTTA and Piero BONISSONE | "Integrating Prior Cases and Expert Knowledge In <br> a Mergers and Acquisitions Reasoning System", |
| 90/56 | Damien NEVEN and | "The Structure and Determinants of East-West |  |  | September 1990 |
| EP | Lars-Hendrik RÖLLER | Trade: A Preliminary Analysis of the Manufacturing Sector", July 1990 | 90/68 <br> TM/SE | Soumitra DUTTA | "A Framework and Methodology for Enhancing the Business Impact of Artificial Intelligence |
| $90 / 57$ <br> FIN/EP/ | Lars Tyge NIELSEN | Common Knowiedge of a Multivariate Aggregate Statistic", July 1990 |  |  | Applications", September 1990 |
| TM |  |  | $\begin{aligned} & 90 / 69 \\ & \text { TM } \end{aligned}$ | Soumitra DUTTA | "A Model for Temporal Reasoning in Medical Expert Systems", September 1990 |
| 90/58 <br> FIN/EP/TM | Lars Tyge NIELSEN | "Common Knowledge of Price and Expected Cost in an Otigopolistic Market", August 1990 | $\begin{aligned} & 90 / 70 \\ & \text { TM } \end{aligned}$ | Albert ANGEHRN | "'Triple C': A Visual Interactive MCDSS", September 1990 |
| 90159 | Jean DERMINE and | *Ecomomies of Scale and |  |  |  |
| FIN | Lare-Hendrik RÖLLER | Scope ia the French Mutual Funds (SICAV) Industry", August 1990 | $\begin{aligned} & 90 / 71 \\ & \text { MKT } \end{aligned}$ | Philip PARKER and Hubert GATIGNON | "Competitive Effects in Diffusion Models: An Empirical Anslysis", September 1990 |
| $\begin{aligned} & 90 / 60 \\ & \text { TM } \end{aligned}$ | Peri IZ and <br> Tawfik JELASSI | "An Interactive Group Decision Aid for Multiobjective Problems: An Empirical Assessment", September 1990 | $\begin{aligned} & 90 / 72 \\ & \text { TM } \end{aligned}$ | Enver YŨCESAN | "Analysis of Markov Chains Using Simulation Graph Models", October 1990 |
| $\begin{aligned} & 90 / 61 \\ & \text { TM } \end{aligned}$ | Pankaj CHANDRA and Mihkel TOMBAK | "Models for the Eviauation of Manufacturing <br> Flexibility", Augurt 1990 | $\begin{aligned} & 90 / 73 \\ & \text { TM } \end{aligned}$ | Amoud DE MEYER and Kasra FERDOWS | "Removing the Barriers in Manufacturing", October 1990 |
| $\begin{aligned} & 90 / 62 \\ & \text { EP } \end{aligned}$ | Damien NEVEN and Menno VAN DUK | "Public Policy Towards TV Broodcasting in the Netheriands", Auguat 1990 | $\begin{aligned} & 90 / 74 \\ & \text { SM } \end{aligned}$ | Sumantra GHOSHAL and Nitin NOHRIA | "Requisite Complexity: Organising HeadquartersSubsidiary Relotions in MNCs", October 1990 |


| $\begin{aligned} & 90 / 75 \\ & \text { MKT } \end{aligned}$ | Roger BETANCOURT and David GAUTSCHI | "The Outputs of Retail Activities: Concepts, Measurement and Evidence", October 1990 | 90/87 <br> FIN/EP | Lars Tyge NIELSEN | "Existence of Equilibrium in CAPM: Further Results", December 1990 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { 90/76 } \\ & \text { MKT } \end{aligned}$ | Wilfried VANHONACKER | "Managerial Decision Behaviour and the Estimation of Dynamic Sales Response Models", Revised October 1990 | 90/88 OB/MKT | Susan C. SCHNEIDER and Reinhard ANGELMAR | "Cognition in Organisational Analysis: Who's <br> Minding the Store?" Revised, December 1990 |
| 90/77 MKT | Wilfried VANHONACKER | "Testing the Koyck Scheme of Sales Response to Advertising: An Aggregation-Independent | 90/89 <br> OB | Manfred F.R. KETS DE VRIES | "The CEO Who Couldn't Talk Straight and Other Tales from the Board Room," December 1990 |
|  |  | Autocorrelation Test", October 1990 | 90/90 <br> MKT | Philip PARKER | "Price Elasticity Dynamics over the Adoption <br> Lifecycle: An Empirical Study," December 1990 |
| 90/78 | Michael BURDA and | "Exchange Rate Dynamics and Currency |  |  |  |
| EP | Stefan Gerlach | Unification: The Ostmark - DM Rate", October 1990 |  |  |  |
| 90/79 | Anil GABA | "Inferences with an Unknown Noise Level in a |  |  |  |
| TM |  | Bernoulli Process", October 1990 |  |  |  |
| 90/80 | Anil GABA and | "Using Survey Data in Inferences about Purchase |  |  |  |
| TM | Rober WINKLER | Behaviour", October 1990 | 1991 |  |  |
| 90/81 | Tawfik JELASSI | "Du Present au Futur: Bilan et Orientations des |  |  |  |
| TM |  | Systernes Interactifs d'Aide à la Décision," <br> October 1990 | 91/01 <br> TM/SM | Luk VAN WASSENHOVE, Leonard FORTUIN and Paul Van beek | "Operational Research Can Do More for Managers Than They Think!," <br> January 1991 |
| 90/82 | Charles WYPLOSZ | "Monetary Union and Fiscal Policy Discipline," |  |  |  |
| EP |  | November 1990 | 91/02 <br> TM/SM | Luk VAN WASSENHOVE, Leonard FORTUIN and | "Operational Research and Environment," January 1991 |
| 90/83 | Nathalie DIERKENS and | "Information Asymmetry and Corporate |  | Paul VAN BEEK |  |
| FIN/TM | Bernard SINCLAIR-DESGAGNE | Communication: Results of a Pilot Study", <br> November 1990 | $\begin{aligned} & \text { 91/03 } \\ & \text { FIN } \end{aligned}$ | Pekka HIETALA and Timo LÖYTTYNIEMI | "An Implicit Dividead Increase in Rights Issues: <br> Theory and Evidence," January 1991 |
| 90/84 <br> MKT | Philip M. PARKER | "The Effect of Advertising on Price and Quality: The Optometric Industry Revisited," December 1990 | $\begin{aligned} & \text { 91/04 } \\ & \text { FIN } \end{aligned}$ | Lars Tyge NIELSEN | "Two-Fund Separation, Factor Structure and Robustness," January 1991 |
| $\begin{aligned} & \text { 90/85 } \\ & \text { MKT } \end{aligned}$ | Avijit GHOSH and <br> Vikas TIBREWALA | "Optimal Timing and Location in Competitive <br> Markets," November 1990 | $\begin{aligned} & 91 / 05 \\ & \mathrm{OB} \end{aligned}$ | Susan SCHNEIDER | "Managing Boundaries in Organisations," January 1991 |
| 90/86 <br> EP/TM | Olivier CADOT and Bernard SINCLAIR-DESGAGNE | "Prudence and Success in Politics," November 1990 | $\begin{aligned} & \text { 91/06 } \\ & \text { OB } \end{aligned}$ | Manfred KETS DE VRIES, Danny MILLER and Alain NOEL | "Understanding the Leader-Strategy Interface: Application of the Strategic Relationship Interview Method," January 1990 (89/11, revised April 1990) |

91/08 Charles WYPLOSZ
EP

91/09 Spyros MAKRIDAKIS
TM
"Lending to Insolvent Countries: A Paradoxical Story," January 1991
"Post-Reform East and West: Capital Accumulation and the Labour Mobility Constraint," January 1991
"What can we Learn from Failure?", February 1991


[^0]:    * Results refer to the permutation fiow-shop.

