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Intermittent behaviour in the Belousov-Zhabotinsky reaction

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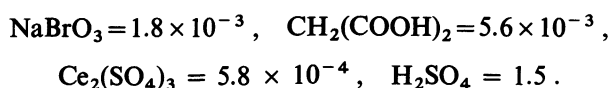
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Résumé. — L'une des routes possibles vers la turbulence est la transition intermittente. Avant la transition vers la turbulence, des oscillations régulières existent et au-dessus des oscillations apparemment régulières sont interrompues au hasard par des bruits de grande amplitude. Ce comportement se manifeste dans la réaction de Belousov-Zhabotinsky. D'autre part une analyse des mesures montre que l'on a affaire dans ce cas à une intermittence de type 1.

Abstract. — One of the possible routes to turbulence is the intermittent transition. Below the onset of turbulence regular oscillations exist, and above the onset seemingly regular oscillations are interrupted randomly by large amplitude bursts. This behaviour shows up in the Belousov-Zhabotinsky reaction. Moreover an analysis of the measurements indicates that a so-called « type 1 » transition takes place in this case.

The possibility of turbulence in chemical kinetics, as suggested by Ruelle [1], has been verified recently [2, 3] for the Belousov-Zhabotinsky (B-Z) reaction. We report here the discovery of an intermittent behaviour in this reaction. Such a behaviour has been seen during the transition to turbulence in thermo-convection experiments [4] and in studies of ordinary equations [5].

In our experiment, the B-Z reaction takes place in an open well stirred tank reactor. Due to stirring, no spatial pattern can develop and the concentrations of the chemical species evolve according to the non linear equations of chemical kinetics, as derived from the mass action law; this deterministic behaviour is sufficient to produce chaos. The experimental conditions are: reacting volume 28 ml, temperature 39.6 °C, concentration of reagents before reaction in mol.l⁻¹ (standard analytical reagent grade without further purification):



A peristaltic pump feeds the reactor at constant adjustable rate. The chemical reaction in the reactor is monitored by the optical density at 340 nm. As this wavelength is absorbed [6] by the Ce⁴⁺ ion only, the signal is a sort of « pure quantity » and has been preferred to the redox potential that depends on the concentration of several chemical species.

As shown in figure 1a, when the mean residence time of chemicals in the reactor is 100 min., the optical density oscillates regularly. At higher fluxes (residence time 76 min. in figure 1b) the time record changes in a specific manner: seemingly stable oscillations exist which are interrupted from time to time and at random by large peaks. Such a transition from stable periodic behaviour to oscillations interrupted by random bursts denotes an intermittent transition to turbulence [5]. The present transition is well described by « type 1 intermittency » [7], shortly described hereafter. Although detailed modelizations of the B-Z kinetics have been proposed [8], we have not tried to relate them to our observations, since most features of the intermittent transition are model independent.

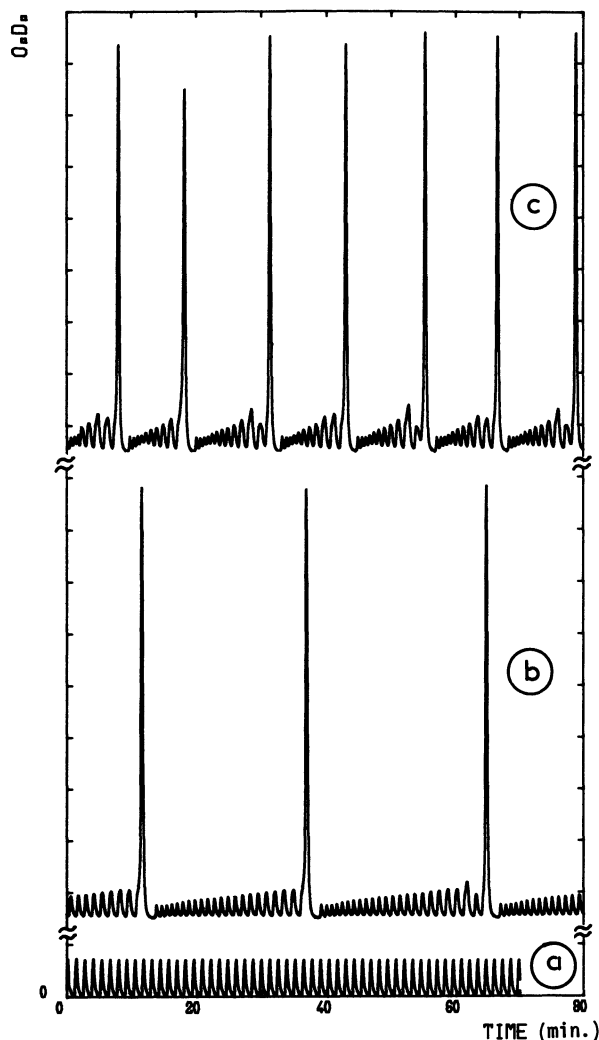


Fig. 1. — $[\text{Ce}^{4+}]$ oscillations recorded as a function of time : a) residence time 100 min. ; b) residence time 76 min. ; c) residence time 35 min.

Following an idea already used [4b] in studying the Rayleigh-Bénard thermoconvection, we consider the peak to peak amplitude of the « regular » oscillations between two bursts ; this gives ordered sequence of numbers $X_1 \dots X_n, X_{n+1} \dots$. In type 1 intermittency, these numbers are connected to each other by a finite difference equation. This reads [7] after suitable choice of normalizations and origins in the generic form :

$$X_{n+1} = X_n + \varepsilon + X_n^2. \quad (1)$$

ε is the control parameter, a smooth function of the residence time. For $\varepsilon < 0$ (in particular for a residence time of 100 min.), $X = \pm (-\varepsilon)^{1/2}$ are two fixed points of the iteration : $-(-\varepsilon)^{1/2}$ (resp. $+(-\varepsilon)^{1/2}$) being stable (resp. unstable). The stable fixed point corresponds to the stable oscillations before the intermittent transition (Fig. 1a). If ε is positive, the fixed points of (1) vanish and a small channel is created [7] between the first bissectrix [in the Cartesian plane (X_n, X_{n+1})] and the representative curve $X_{n+1}(X_n)$. This curve is locally approximated by a parabola, as implied by

equation (1). Far away from the region $X \sim 0$, this local form is no longer valid ; however this large distance behaviour affects the structure of the large bursts only, that we do not consider here.

For $\varepsilon > 0$, starting from a negative X , the successive X_n 's, as given by equation (1), drift slowly through the channel toward positive values. Plotting $X_{n+1}(X_n)$, as given by the time records of the B-Z reaction in the intermittent conditions, one can recognize this drift process (Fig. 2). Furthermore, near $\varepsilon = 0+$, one may replace equation (1) by a differential equation [7], n being taken as continuous. This yields :

$$X(n) \simeq \varepsilon^{1/2} \text{tg}(n\varepsilon^{1/2}).$$

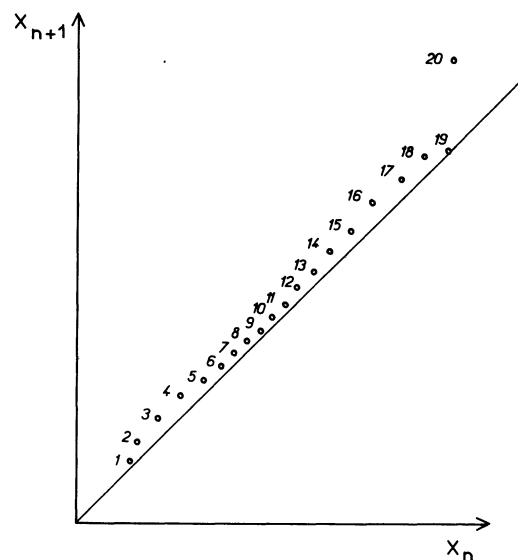


Fig. 2. — Peak to peak amplitude of the « regular » oscillations between two bursts (residence time : 76 min.).

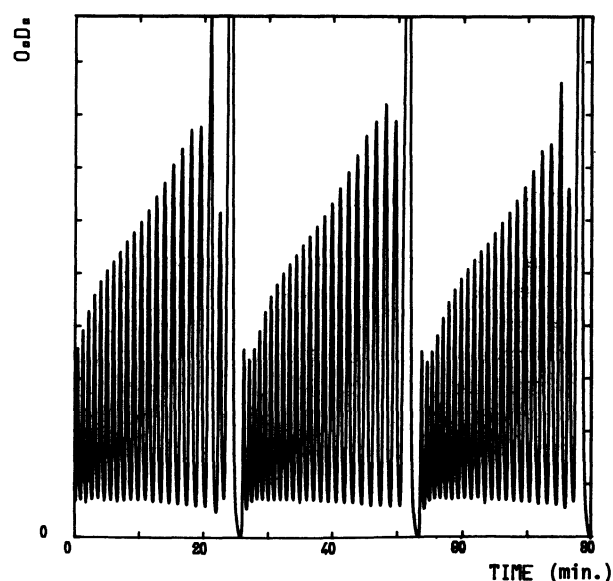


Fig. 3. — Enlarged view of the oscillations (residence time : 76 min.).

This approximation breaks down when $n\varepsilon^{1/2}$ tends to $\pm \pi/2$. However, the tangent like shape of the local maxima can be recognized in the records (Fig. 3).

In real life experiments, it is in principle impossible to conclude surely about the stochastic or non stochastic nature of a process recorded during a finite time. Nevertheless we present hereafter more plausible arguments for our interpretation of this transition :

(i) at values of the residence time still lower than these reported here, the behaviour becomes more and more chaotic. The duration and structure of the oscillations between two bursts fluctuate more and more (Fig. 1c). This agrees with the idea that chaos is already present just beyond the onset of intermittency, even though the records look quite regular then.

(ii) the frequency of occurrence of large bursts does not seem to be locked with the frequency of fast oscillations. The number of oscillations between two bursts varies randomly, with a probability distribution shown in figure 4. This distribution is typical of « type 1 intermittency » : the time needed to drift through the channel is bounded from above. This

time can fluctuate to lower values only. A two dimensional iteration scheme, as the one proposed in references [4, 6] yields a probability distribution similar to the one of figure 4.

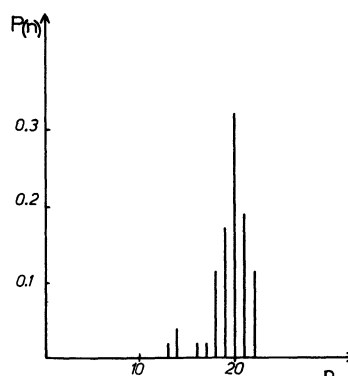


Fig. 4. — Probability distribution of the number of oscillations between two bursts (residence time : 76 min.).

To conclude, all our experimental data are consistent with a transition to turbulence *via* type 1 intermittency.

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