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## Permalink

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## Journal

Physical review. B, Condensed matter, 47(13)
ISSN
0163-1829

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## Publication Date

1993-04-01
DOI
10.1103/physrevb.47.8156

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Peer reviewed

# Internal magnetic field in $\mathrm{La}_{2-x} \mathbf{S r}_{x} \mathbf{C u O}_{4}$ :Gd observed by electron paramagnetic resonance 

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(Received 27 August 1992)


#### Abstract

We have measured the electron paramagnetic resonance (EPR) of $\mathrm{Gd}^{3+}$ in single crystals of $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4+\delta}$, as a function of temperature $T$, magnetic-field angle, oxygen content, microwave frequency, and Sr concentration ( $0 \leq x \leq 0.024$ ). For temperatures larger than the antiferromagnetic ordering temperature of the Cu lattice, $T_{N}$, we have identified four different sites of $\mathrm{Gd}^{3+}$ as expected for twinned crystals and we are able to fit the data for all directions of the magnetic field. Samples annealed under vacuum or oxygen show only small changes on their crystal-field parameters and $g$ values. For temperatures smaller than $T_{N}$, the EPR lines are further split due to the internal magnetic field acting at the Gd site associated with the antiferromagnetic ordering of the Cu lattice. The temperature dependence of the splitting of the resonance lines allow us to calculate the moment per Cu ion. A value of $\sim 0.6 \mu_{B}$ per Cu ion at $T=0 \mathrm{~K}$ is inferred, with the Cu moments lying in the $b c$ plane about $5^{\circ}$ from the $c$ axis. The data only can be fit for all the directions of the applied magnetic field if other mechanisms such as a Heisenberg type of exchange between the Cu and Gd moments or a distortion of the lattice below $T_{N}$ are included.


## I. INTRODUCTION

There have been many suggestions that magnetic interactions play an important role in the high- $T_{c}$ superconductors. ${ }^{1,2}$ A number of experimental studies of the magnetic properties of these materials have been reported in an attempt to clarify the nature of the magnetism of the $\mathrm{Cu}-\mathrm{O}$ lattice, and its possible relationship to the mechanism of superconductivity. ${ }^{1,2}$ These studies include dc and ac magnetization, ${ }^{3}$ neutron scattering, ${ }^{4}$ $\mu^{+}$SR, ${ }^{5}$ NMR and nuclear quadrupole resonance (NQR), ${ }^{6}$ and two-magnon Raman. ${ }^{7}$ Many of them have focused on the $\mathrm{La}_{2} \mathrm{CuO}_{4}\left(T\right.$ phase) and $R_{2} \mathrm{CuO}_{4}$ ( $R=\mathrm{Pr}, \mathrm{Nd}, \mathrm{Sm}, \mathrm{Eu}, \mathrm{Gd}$ ) ( $T^{\prime}$ phase) host systems, due to their relatively simple structure. It turns out that these host systems, even without electron or hole dopants, have remarkably complex magnetic features. ${ }^{3}$ Despite the difficulties this complexity entails, it is essential to obtain a detailed understanding of all the magnetic properties of
these host systems because, once known, even subtle differences in the superconducting versions may prove to be a route to obtain the key insights into the role of magnetism in high- $T_{c}$ superconductivity. In this paper, we use EPR of dilute local moments, which are placed as probes at the La sites, to clarify the subtle and complex magnetic features of these systems.

Related experiments, in which a local moment (Gd) is substituted for the $R$-site atom ( $R \equiv \mathrm{Eu}$ ), have been reported separately. ${ }^{8}$ While there are certain features in common between the La and $R$ hosts, there are also significant differences in the crystal and magnetic structures of these systems which warrant separate consideration and analysis.

We have measured the EPR spectra of $\mathrm{Gd}^{3+}$ (doped at $0.1 \%-1 \%$ ) in single crystals of $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4 \pm \delta}$, as a function of temperature, $T$, magnetic-field angle, oxygen content, microwave frequency, and Sr concentration ( $0 \leq x \leq 0.024$ ). We interpret these data and obtain infor-
mation about the magnetic ordering of the Cu-O system and the internal magnetic field acting at the rare-earth site. We determine the crystal-field parameters for the $\mathrm{Gd}^{3+}$ ion, and identify the nonequivalent $\mathrm{Gd}^{3+}$ sites and their point group symmetry. We also address the problem which arises when working with twinned single crystals and crystals having different oxygen contents. ${ }^{9}$

In Sec. II, the details of sample preparation and experimental techniques are given. In Sec. III, we analyze the point symmetry of the La sites in the $\mathrm{La}_{2} \mathrm{CuO}_{4}$ crystal structure and present an appropriate spin Hamiltonian for $\mathrm{Gd}^{3+}$ ions substituting for $\mathrm{La}^{3+}$ ions at the different sites. In Sec. IV, we present our experimental results. In Sec. V, an analysis of the data is given, and in Sec. VI our conclusion are presented.

## II. SAMPLE PREPARATION AND EXPERIMENTAL TECHNIQUES

The samples used were single crystal grown in air from CuO -rich flux by slow cooling in Pt crucibles. Their oxygen content has been modified by annealing them under vacuum ( $\sim 10^{-6} \mathrm{~mm}$ ) or oxygen pressure ( $\sim 150 \mathrm{~atm}$ ) at $T \simeq 800 \mathrm{~K}$. We note that EPR, unlike other techniques, does not require large samples, crystals of $1 \mathrm{~mm}^{3}$ or less in volume are sufficient. The EPR measurements were made with conventional spectrometers operating at 9 and 35 GHz , at temperatures between 1.5 and 300 K .

## III. Gd $^{3+}$ SITE SYMMETRY

 AND ITS SPIN HAMILTONIANAt high temperature, the crystals of $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}$ form in a tetragonal phase with $14 / \mathrm{mmm}$ symmetry. Each Cu ion is surrounded by an elongated oxygen octahedra and the La ions are surrounded by an array of nine oxygens atoms with a $C_{4 v}$ point symmetry. When cooled below $\sim 500 \mathrm{~K}$ the structure changes to an orthorhombic phase of Cmca symmetry with a staggered tilt $\left(\sim 4^{\circ}\right)$ of the $\mathrm{CuO}_{6}$ octahedra, as shown in Fig. 1. In this crystal structure the La ions occupy ( $8 f$ ) positions in which their local point symmetry is reduced to $C_{1 h}$. The eight La ions can be grouped into two equivalent sets of four ions that differ only by a translation within the unit cell, and the La ions are still surrounded by nine oxygen neighbors. For $\mathrm{Gd}^{3+}$ ions substituting for the $\mathrm{La}^{3+}$ ions, an appropriate spin Hamiltonian can be written as ${ }^{10}$

$$
\begin{equation*}
H=\mu_{B} \mathbf{S} \cdot \underline{g} \cdot \mathbf{H}+\sum_{n=2,4,6} \sum_{m=0}^{n} b_{n}^{m} \boldsymbol{O}_{n}^{m} \tag{1}
\end{equation*}
$$

where $\underline{g}$ is the giromagnetic-tensor, $O_{n}^{m}$ are the Stevens operators, and $b_{n}^{m}$ are the corresponding crystal-field parameters (CFP). We have defined a coordinate system in which $(x, y, z)$ are the components of the electron vector position, measured along the $a,-c$, and $b$ crystallographic axes, respectively. The four possible magnetically nonequivalent Gd sites within each unit cell are surrounded by local configurations of atoms differing by a symmetry operation. The spin Hamiltonian for each site can be derived from Eq. (1) by the following transformation in crystal-field terms: $\left(S_{x}, S_{y}, S_{z}\right)$ to ( $\pm S_{x}, \pm S_{y}, \pm S_{z}$ ). The


FIG. 1. $\mathrm{La}_{2} \mathrm{CuO}_{4}$ unit cell showing the eight La atoms which can be grouped into two equivalent sets. Each $\mathrm{La}(\mathrm{Gd})$ atom is surrounded by nine nearest oxygen neighbors.
point symmetry $C_{1 h}$ (with the reflection symmetry plane being the $x z$ plane) implies that only $b_{2}^{0}, b_{2}^{1}(s)$, and $b_{2}^{2}(c)$ can be different from zero in Eq. (1), corresponding to the operators $O_{2}^{0}, O_{2}^{1}(s)$, and $O_{2}^{2}(c)$. For simplicity we discuss only the terms with $n=2$, a similar analysis applies for $n=4,6$. The eight Gd sites will have the same values of $b_{2}^{0}$ and $b_{2}^{2}(c)$ but four will have positive values for $b_{2}^{1}(s)$, and the other four have $b_{2}^{1}(s)$ negative.

Furthermore, we know that $\mathrm{La}_{2} \mathrm{CuO}_{4}$ grows as a twinned crystal, that is, with the $a$ axis of the orthorhombic crystal structure being coincident with either the $x$ or the $y$ axis of the reference frame fixed to the macroscopic crystal. The Hamiltonian for the Gd sites in the twinned phase may be obtained by interchanging ( $S_{x}, S_{y}$ ) for ( $S_{y},-S_{x}$ ) in the crystal-field terms of Eq. (1). Thus, for the other component of the twin phase, $b_{2}^{0}$ remains unchanged, $b_{2}^{2}(c)$ changes sign, $b_{2}^{1}(s)$ is zero, and $b_{2}^{1}(c)$ plays the role of $b_{2}^{1}(s)$, changing sign for different Gd sites. As a result we expect four superimposed EPR spectra with the following sets of crystal-field parameters: $\left[b_{2}^{0}, \pm b_{2}^{1}(s), b_{2}^{2}(c)\right] \quad$ and $\quad b_{2}^{0}, \pm b_{2}^{1}(c),-b_{2}^{2}(c) \quad$ with $\left|b_{2}^{1}(s)\right|=\left|b_{2}^{1}(c)\right|$. The above also apply for the smaller, but non-negligible, terms with $n=4$ and 6 .

It has recently been reported that nonstoichiometric superoxygenated $\mathrm{La}_{2} \mathrm{CuO}_{4 \pm \delta}$ undergoes a phase separation into two closely related orthorhombic phases at a temperature near $270 \mathrm{~K} .{ }^{9}$ We have not determined the oxygen content of our samples, although the preparation method allows us to estimate that $\delta \leq 0.01$. Samples superoxygenated at 150 bars for two days at 800 K suggest
a phase separation. At room temperature their EPR spectra indicate the presence of a new Gd site. These data will be the subject of a future publication. ${ }^{11}$

The ground state of $\mathrm{Gd}^{3+}$ is ${ }^{8} S_{7 / 2}$. Thus, each EPR spectrum consists of seven "allowed" fine-structures lines with $\Delta M= \pm 1$ for each site. Since there are four inequivalent sites for a twinned sample, at certain orientations of the applied magnetic field it may be possible to resolve as many as 28 allowed fine-structure lines in the EPR spectrum. $\mathrm{Gd}^{3+}$ in $\mathrm{La}_{2} \mathrm{CuO}_{4}$ has unusually large crystal-field splittings, so the relative intensities of the allowed and the forbidden fine-structure lines are comparable at 9 GHz . With the additional complication of multiple split lines, the analysis of the data is particularly difficult at this frequency. For this reason, most of the data and all of the analysis were performed at 35 GHz , where the relative intensity of the forbidden transitions is diminished.

## IV. EXPERIMENTAL RESULTS

It is well documented that as-grown $\mathrm{La}_{2} \mathrm{CuO}_{4}$ undergoes an antiferromagnetic transition with a Néel temperature, $T_{N} \sim 200-320 \mathrm{~K}$. Below the Néel temperature Yamada et al. ${ }^{4}$ found that the Cu spins align antiferromagnetically (AF) along the $c$ axis, with a spin canting of $\sim 0.2^{\circ}$ out of the ( $a, c$ ) plane. The spin arrangement for the Cu ions is illustrated in Fig. 2. We have found that the $\mathrm{Gd}^{3+}$ EPR spectra change at a characteristic temperature $T_{0}$ which we identify with $T_{N}$. We have studied samples of $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}$, with $x=0,0.009$, and 0.024 and find $T_{0}$ values of about 250,200 , and 20 K , respectively, which we attribute to the suppression of $T_{N}$ by the addition of Sr . Measurements of the EPR on single crys-


FIG. 2. Orthorhombic structure (space group Cmca) of $\mathrm{La}_{2} \mathrm{CuO}_{4}$. The $\mathrm{CuO}_{6}$ octahedra are staggered tilt by $\sim 4^{\circ}$ and the Cu spins canted from the CuO planes by $\sim 0.2^{\circ}$ according to the neutron data (from Ref. 4).


FIG. 3. Low-field $\mathrm{La}_{2} \mathrm{CuO}_{4}:$ Gd EPR spectra at $T=300 \mathrm{~K}$ ( $>T_{0}$ ) for (a) $\mathbf{H}_{0} \| \mathbf{b}$ axis, (b) $\mathbf{H}_{0}$ at $25^{\circ}$ from the $b$ axis in a plane containing the [101] axis.
tals of $\mathrm{La}_{0.993} \mathrm{Gd}_{0.007} \mathrm{CuO}_{4 \pm \delta}$ subject to different annealings also have been made. By annealing under vacuum $\left(\sim 10^{-6} \mathrm{~mm}\right)$ for temperatures up to $800-900 \mathrm{~K}$ and 48 $\mathrm{h}, T_{0}$ increased from $\sim 250$ to $\sim 315 \mathrm{~K}$. The value of $T_{0}$ is reduced to $\sim 195 \mathrm{~K}$ when annealed under 150 atm of oxygen at 800 K for 24 h . These values of $T_{0}$ are in good agreement with the values of $T_{N}$ obtained by dc magnetization measurements performed on samples from the same batch. This is consistent with previous studies on the effect of oxygen content on $T_{N}$. ${ }^{9}$ The EPR spectra obtained above and below $T_{0}$ can be summarized as follows.
(a) Paramagnetic region $\left(T>T_{0}\right)$. We have found that for $T>T_{0}$ the EPR spectra can be interpreted as being the result of the superposition of lines from four magnetically nonequivalent $\mathrm{Gd}^{3+}$ crystallographic sites for a twinned crystal. At room temperature the individual lines are broad ( $300-400 \mathrm{G}$ ) relative to their spacing and


FIG. 4. Angular dependence of the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition at $T=300 \mathrm{~K}\left(>T_{0}\right)$, when $\mathbf{H}_{0}$ is rotated from the $b$ axis to an arbitrary plane (see inset).


FIG. 5. $\mathrm{La}_{2} \mathrm{CuO}_{4}:$ Gd EPR spectra for $\mathrm{H}_{0} \|[101]$ axis at (a) $T \sim 253 \mathrm{~K}\left(>T_{0}\right)$, (b) $T \sim 189 \mathrm{~K}\left(<T_{0}\right)$, and (c) $T \sim 77 \mathrm{~K}$ ( $<T_{0}$ ).
hence the spectra are only well resolved for certain field orientations. Each of the seven allowed fine-structure lines splits into as many as four components. In particular, when the magnetic field $H_{0}$ is applied parallel to the $b$ and [101] axes, the four spectra coalesce into one and each spectral line splits into its four components when $H_{0}$ is rotated away from these axes in an arbitrary plane. The four components coalesce into two or three lines when $H_{0}$ lies in certain high-symmetry crystallographic planes. In Fig. 3 are shown the spectra with $H_{0}$ making angles of $0^{\circ}$ and $25^{\circ}$ with the $b$ axis and moving in the


FIG. 6. $\mathrm{La}_{2} \mathrm{CuO}_{4}$ :Gd EPR spectra for $\mathrm{H}_{0} \| c$ (or $a$ ) axis at (a) $T=290 \mathrm{~K}\left(>T_{0}\right)$ and (b) $T=77 \mathrm{~K}\left(<T_{0}\right)$. The assignments of the resonances corresponding to the fine structure for $\mathbf{H}_{0} \| a$ are labeled.


FIG. 7. Angular dependence of the $\mathrm{La}_{2} \mathrm{CuO}_{4}: \mathrm{Gd}$ EPR spectra at $T=300 \mathrm{~K}\left(>T_{0}\right)$ for the five lower transitions when $\mathbf{H}_{0}$ is rotated in the ( $a, c$ ) plane. The solid lines represent the best fitting of the data obtained by using the parameters listed in Table I.
plane containing the [101] axis (we use the [abc] notation). Notice that each line splits into only two components. In Fig. 4, we present the angular dependence of the ( $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ ) transition line, showing the full evolution of the fourfold degeneracy when the magnetic field is rotated from the $b$ axis to the ( $a, c$ ) plane, for the orientation shown in the inset. Because of the complicated spectra, its rapid angular variation, and the considerable linewidth, it is difficult to resolve the individual lines of


FIG. 8. Angular dependence of the $\mathrm{La}_{2} \mathrm{CuO}_{4}: \mathrm{Gd}$ EPR spectra at $T=300 \mathrm{~K}\left(>T_{0}\right)$ for the lower transitions, when $\mathbf{H}_{0}$ is rotated in the (101) plane.


FIG. 9. Angular dependence of the $\mathrm{La}_{1.976} \mathrm{Sr}_{0.024} \mathrm{CuO}_{4}: \mathrm{Gd}$ EPR spectra at $T=300 \mathrm{~K}\left(>T_{0}\right)$, when $\mathbf{H}_{0}$ is rotated in the (101) plane.
the other allowed transitions for an arbitrary orientation of the magnetic field. It is also difficult to resolve the spectra when the magnetic field is in the ( $a, c$ ) plane because the overall splitting is only about half that found when the field is along the $b$ axis. For $\mathbf{H}_{0} \|[101]$ and $T=253 \mathrm{~K}$, Fig. 5(a) shows a resolved spectra with the seven fine-structure lines. Figure 6(a) shows a partially resolved spectra for $\mathbf{H}_{0} \| c$ (or $a$ ) and $T=290 \mathrm{~K}$, note that we are working with twinned crystals. The assignments of the resonances corresponding to the fine structure for $\mathbf{H} \| \mathbf{a}$ are labeled. Figure 7 shows the angular variation in


FIG. 10. $\mathrm{La}_{1.993} \mathrm{Gd}_{0.007} \mathrm{CuO}_{4} \mathrm{EPR}$ spectra at $T=90 \mathrm{~K}\left(<T_{0}\right)$ when $\mathbf{H}_{0}$ is rotated in a plane containing the $b$ and [101] axes, (a) $\mathbf{H}_{0}$ along the $b$ axis, (b) $\mathbf{H}_{0}$ at $10^{\circ}$ from the $b$ axis, and (c) $\mathbf{H}_{0}$ at $20^{\circ}$ from the $b$ axis.


FIG. 11. $\mathrm{La}_{1.993} \mathrm{Gd}_{0.007} \mathrm{CuO}_{4} \mathrm{EPR}$ spectra for the lowest transitions at (a) $T=304 \mathrm{~K}\left(>T_{0}\right)$ and (b) $T=90 \mathrm{~K}\left(<T_{0}\right)$ for $\mathbf{H}_{0} \| b$ axis. The inset shows the splitting of the $-\frac{1}{2} \leftrightarrow \frac{1}{2}$ transition. This sample has been superoxygenated at 150 atm and its $T_{N}$ has been reduced to $\sim 190 \mathrm{~K}$.
the ( $a, c$ ) plane at $T=300 \mathrm{~K}$ for the lower transitions. Due to the twinning of our crystals the spectra in this plane appears to have a $90^{\circ}$ symmetry.

Data obtained for $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}$ :Gd with $x=0.009$ and 0.024 are similar to those found for $x=0$. In Figs. 8 and 9 we present the angular variation of the measured spectra, with $\mathbf{H}_{0}$ being rotated away from the $b$ axis in the (101) plane, for $\mathrm{La}_{2} \mathrm{CuO}_{4}$ : Gd and $\mathrm{La}_{1.976} \mathrm{Sr}_{0.024} \mathrm{CuO}_{4}$ :Gd, respectively. As in Fig. 3, the data for this orientation of the field show the Gd sites grouped into two lines.
(b) Antiferromagnetic region ( $T<T_{0}$ ). As we lower the temperature below $\sim 250,200$, or 20 K for $x=0$,


FIG. 12. Temperature dependence of the splitting $\delta H$ of the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition for $\mathbf{H}_{0} \| b$ in $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}: \mathrm{Gd}(x=0$, 0.009 , and 0.024). Notice the sharp increase in $\delta H$ for $x=0.009$ at $\sim 20 \mathrm{~K}$.
0.009 , and 0.024 , respectively, each of the EPR lines observed for $T>T_{0}$ are further split. A similar behavior is observed for the annealed samples of $\mathrm{La}_{2} \mathrm{CuO}_{4}$ : Gd , where the extra splitting occurs at a temperature near the value of $T_{N}$ measured by dc magnetization. Fortunately the linewidths decrease, so we are able to resolve the spectra despite the added complexity. This further splitting is basically independent of the microwave frequency used (9 and 35 GHz ) and increases as the temperature is lowered. In Fig. 10, we show the spectra for $\mathrm{La}_{1.993} \mathrm{Gd}_{0.007} \mathrm{CuO}_{4}$ measured at $T \sim 90 \mathrm{~K}, v=35.5 \mathrm{GHz}$, with $\mathbf{H}_{0}$ making angles of $0^{\circ}, 10^{\circ}$, and $20^{\circ}$ with the $b$ axis, and moving in the plane containing the [101] axis. Here, each of the lines that was observed above $T_{0}$ is further split into two components. Note that this splitting even occurs for $0^{\circ}$, i.e., with $\mathbf{H}_{0}$ along the $b$ axis. Figure 11 shows these splittings


FIG. 13. Temperature dependence of the linewidth $\Delta H_{p p}$ for $\mathrm{H}_{0} \| b$ in $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}: \mathrm{Gd}(x=0,0.009$, and 0.024) (a) $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition at 35 GHz and (b) $-\frac{3}{2} \leftrightarrow-\frac{1}{2}$ transition at 9.2 GHz.


FIG. 14. Temperature dependence of the linewidth $\Delta H_{p p}$ for the $-\frac{1}{2} \leftrightarrow \frac{1}{2}$ transition and $\mathrm{H}_{0} \| b$ in $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}: \mathrm{Gd}(x=0$, 0.009 , and 0.024), (a) 35 GHz and (b) 9.2 GHz .
for a superoxygenated sample of $\mathrm{La}_{2} \mathrm{CuO}_{4}: \mathrm{Gd}$ with $T_{N} \sim 190 \mathrm{~K}$; the inset shows the splitting for the $-\frac{1}{2} \leftrightarrow \frac{1}{2}$ transition for $T=90 \mathrm{~K}$.

In Fig. 12, we present $\delta H$, the splitting of the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ line, as a function of temperature for $\mathbf{H}_{0}$ parallel to the $b$ axis and $x=0,0.009$, and 0.024. In Fig. 13,


FIG. 15. Normalized linewidth for the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition as a function of temperature for a single crystal of $\mathrm{La}_{2} \mathrm{CuO}_{4+\delta}$ : Gd at 35.5 GHz and $\mathbf{H}_{0} \| \mathbf{b},(\bullet)$ as-grown $T \sim 250 \mathrm{~K}$; (*) vacuum annealed at 800 K for $4 \mathrm{~h}, T_{N} \sim 300 \mathrm{~K}$; ( $\oplus$ ) superoxygenated at 150 bars for 2 days at $800 \mathrm{~K}, T_{N} \sim 190 \mathrm{~K}$. The solid lines is a guide for the eye.


FIG. 16. $\mathrm{La}_{2} \mathrm{CuO}_{4}:$ Gd EPR spectra for the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition in a superoxygenated sample, $T_{N} \sim 190 \mathrm{~K}$, taken at different temperatures.
we show the linewidths of the $-\frac{3}{2} \leftrightarrow-\frac{1}{2}$ and the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transitions with $\mathbf{H}_{0}$ parallel to the $b$ axis, as a function of temperature for $x=0,0.009$, and 0.024 and for $v=9.2$ and 35.5 GHz , respectively. Figure 14 shows, for the same samples and frequencies, the temperature dependence of the linewidth of the $-\frac{1}{2} \leftrightarrow \frac{1}{2}$ transition, with $\mathbf{H}_{0} \| \mathbf{b}$. Figure 15 shows the normalized linewidth for the $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition as a function of temperature with $\mathbf{H}_{0} \| \mathbf{b}$ for a single crystal of $\mathrm{La}_{2} \mathrm{CuO}_{4 \pm \delta}$ subject to different annealings. The crystal as grown shows a maximum in $\Delta H_{p p}$ at $\sim 260 \mathrm{~K}$, after vacuum annealing the temperature of the maximum increases to $\sim 300 \mathrm{~K}$ and when superoxygenated at $\sim 150$ bars it decreases to $\sim 190 \mathrm{~K}$. At low temperatures, when the splittings are well resolved, the plotted linewidth in Figs. 13-15 corresponds to that of a single line, whereas at higher temperatures, when the splittings are unresolved, the composite


FIG. 17. $\mathrm{La}_{2} \mathrm{CuO}_{4}: \mathrm{Gd}-\frac{7}{2} \leftrightarrow-\frac{5}{2}$ transition at $T=90 \mathrm{~K}$ ( $<T_{0}$ ) when $\mathbf{H}_{0}$ is rotated in a plane containing the $v$ axis and the $a$ or $c$ axis (a) $\mathbf{H}_{0}$ along the $b$ axis and (b) $\mathbf{H}_{0} 25^{\circ}$ from the $b$ axis.


FIG. 18. Temperature dependence of the splitting for the various transitions for $\mathbf{H}_{0} \|[$ 101] axis.
width is plotted. This is illustrated in Fig. 16 for the superoxygenated sample of Fig. 15.
The EPR spectra for the transition $-\frac{7}{2} \leftrightarrow-\frac{5}{2}$, for $x=0, T=90 \mathrm{~K}, v=35.5 \mathrm{GHz}$, and for $\mathbf{H}_{0}$ making angles of $0^{\circ}$ and $25^{\circ}$ with the $b$ axis in the plane containing the $a$ or $c$ axis, are shown in Figs. 17(a) and 17(b), respectively. For the latter, note that the three lines observed above $T_{0}$ have split into six lines.

In (a) we presented Fig. 5(a) to illustrate the EPR spectra for $\mathrm{La}_{1.993} \mathrm{Gd}_{0.007} \mathrm{CuO}_{4}$ with $\mathbf{H}_{0}$ parallel to [101], mea-


FIG. 19. Angular dependence of the $\mathrm{La}_{2} \mathrm{CuO}_{4}$ :Gd EPR spectra for the five lowest transitions measured at $T=90 \mathrm{~K}\left(<T_{0}\right)$ and $v=35.4 \mathrm{GHz}$, when $\mathbf{H}_{0}$ is rotated in the ( $a, c$ ) plane. Notice that the data correspond to a twinned crystal.
sured at 35.02 GHz for $T=253 \mathrm{~K}$, i.e., $T>T_{0}$. As mentioned there, the spectra for the four nonequivalent $\mathrm{Gd}^{3+}$ sites coalesce, and only the seven allowed fine-structure lines are observed. As we lower the temperature each of these lines splits into two components, as is shown in Fig. 5 (b) for $T=189 \mathrm{~K}$. As the temperature is lowered further, the splitting increases, and the different components start to overlap, as is shown in Fig. 5(c) for $T=77 \mathrm{~K}$. The splitting of a given transition with $\mathbf{H}_{0} \|[101]$ into its pair of components as a function of temperature between 4 and 300 K is shown in Fig. 18. In Fig. 6, the EPR spectra for $\mathbf{H}_{0}$ parallel to the $a$ or $c$ axis are shown for 290 and 77 K . The assignments of the resonances corresponding to the fine structure for $\mathbf{H}_{0} \|$ a are given. For $T<T_{0}$ it is difficult to identify the lines for $\mathbf{H}_{0} \| \mathbf{c}$ because of our twinned crystals and also because, for this orientation, the line separations due to the crystal field are relatively small and the splittings of the lines are large. This is illustrated in Fig. 19 where the angular variation for the five lower transitions in the ( $a, c$ ) plane at $T=90 \mathrm{~K}$ is plotted for a superoxygenated crystal with $T_{N} \sim 190 \mathrm{~K}$. For convenience, the data in the ( $a, c$ ) plane were taken in a crystal with $T_{N}(\sim 190 \mathrm{~K})$ such that the overlapping of the different split lines is minimized at a temperature easy to stabilize in our experimental setup. That temperature in our case was $T \simeq 90 \mathrm{~K}$. Splitting of lines which are temperature dependent, like those shown in Fig. 18, were also measured for $\mathbf{H}_{0} \| \mathbf{a}$ (or c), but with a more complicated spectra because of the reasons given above.

## V. DATA ANALYSIS AND DISCUSSION

Our goals are to interpret the measurements presented in Sec. IV to characterize the nature of different $\mathrm{Gd}^{3+}$ sites, to determine $g$ values, crystal-field parameters, and to obtain information about the magnetic ordering of the $\mathrm{Cu}-\mathrm{O}$ planes. As there are qualitative differences between the spectra obtained above and below $T_{0}$, we again discuss the two temperature regimes separately.

## A. Analysis for $\boldsymbol{T}>\boldsymbol{T}_{\mathbf{0}}$

The analysis presented here is restricted to the data taken at $v \sim 35 \mathrm{GHz}$ and for $x=0$. Other than the reduction in $T_{0}$ there were no substantive differences in the data taken for samples with $x \neq 0$. We found that the set of crystal-field parameters for $x=0$ holds reasonably well for the samples with $x=0.009$ and 0.024 , as well as for


FIG. 20. Best fitting for the data taken in the ( $b,[101]$ ) plane at 290 K using the parameters listed in Table I .
the samples annealed under vacuum or excess of oxygen.
The complicated spectra obtained for an arbitrary orientation of the external magnetic field are simplified, when observed along the $a, b, c$, and [101] directions [see Figs. 3(a), 5(a), 6(a), and 11(a)]. By assuming that the spectra comes from two magnetically nonequivalent $\mathrm{Gd}^{3+}$ sites in the unit cell, and taking into consideration the twinning of the crystals, we were able, using the Hamiltonian of Eq. (1), to fit, better than within half a linewidth, the field for resonance for the allowed transitions observed along all the directions. The best fit of the experimental data yields the $g$ values and crystal-field parameters listed in Table I. Using these parameters and Eq. (1) we have simulated the theoretical angular variation expected for the spectra in different planes. We show the simulation for the ( $b,[101]$ ) plane (see Fig. 20) and in the ( $a, c$ ) plane (see Fig. 7). For simplicity, only part of the experimental data have been included in these two figures. The theoretical curves and the experimental data are in very good agreement.

In summary, the $g$ values and CFP given in Table I applied to the four sites present in a twinned crystal predict a coincident overlapping of the spectra for $\mathbf{H}_{0}$ parallel to the $b$ axis, the splitting of each line into two lines when $\mathbf{H}_{0}$ is rotated toward the [101] axis, into three when mov-

TABLE I. $g$ values and crystal-field parameters at 290 K for a sample of $\mathrm{La}_{2} \mathrm{CuO}_{4}: \mathrm{Gd}^{3+}$ as grown with $T_{N} \sim 250 \mathrm{~K}$.

| $g$ values | $b_{2}^{m}\left(10^{-4} \mathrm{~cm}^{-1}\right)$ | $b_{4}^{m}\left(10^{-4} \mathrm{~cm}^{-1}\right)$ | $b_{6}^{m}\left(10^{-4} \mathrm{~cm}^{-1}\right)$ |
| :---: | :--- | :--- | :--- |
| $g_{x}=1.977 \pm 0.001$ | $b_{2}^{0}=-1378 \pm 5$ | $b_{4}^{0}=-4 \pm 1$ | $b_{6}^{0}=-3 \pm 1$ |
| $g_{y}=1.974 \pm 0.001$ | $b_{2}^{1}=-2013 \pm 10$ | $b_{4}^{1}=-55 \pm 10$ | $b_{6}^{1}=80 \pm 10$ |
| $g_{z}=1.970 \pm 0.001$ | $b_{2}^{2}=-238 \pm 5$ | $b_{4}^{2}=-3 \pm 2$ | $b_{6}^{2}=15 \pm 10$ |
|  |  | $b_{4}^{3}=-10 \pm 5$ | $b_{6}^{3}=-50 \pm 10$ |
|  | $b_{4}^{4}=10 \pm 5$ | $b_{6}^{4}=-10 \pm 10$ |  |
|  |  | $b_{6}^{6}=160 \pm 20$ |  |

ing toward the $a$ or $c$ axis, and into four when rotated to any other axis in the plane. All this is in agreement with the experimental data.

## B. Analysis for $\boldsymbol{T}<\boldsymbol{T}_{\mathbf{0}}$

Dramatic changes in the EPR spectra are observed for $T<T_{0}$. The changes are similar for $x=0,0.009$, and 0.024 , and for the samples as grown they are first observed at $\sim 250,200$, and 20 K , respectively, corresponding approximately to their Néel temperatures.

It is possible to explain the data below $T_{0}$ by adding to the spin Hamiltonian of Eq. (1) a pseudo-Zeeman energy term associated with an internal magnetic field $H_{i}$, lying approximately in the $(a, c)$ plane. The fact that the splitting appears at $T_{0} \simeq T_{N}$ strongly suggests that the origin of this internal field is associated with the magnetic ordering of the Cu moments. As seen in Fig. 2, below $T_{N}$ the $\mathrm{La}(\mathrm{Gd})$ sites in adjacent unit cells are surrounded by reverse configurations of Cu moments. These spin arrangements create two different $\mathrm{La}(\mathrm{Gd}$ ) sites in the magnetic structure with equal probability of occurrence. The two different La (Gd) sites "see" an internal field $H_{i}$ of the same magnitude but different sign. We calculate the internal field at the $\mathrm{La}(\mathrm{Gd})$ site which arises from the dipolar field of the AF ordered Cu moments. By adding up the contribution of the dipoles around the La (Gd) site from a sphere of 400 A , we have calculated the dipolar field using the magnetic structure proposed by neutron scattering ${ }^{4}$ and $\mu^{+}$SR (Ref. 5) experiments. The measured internal field inferred from our experiments correspond to $\sim 0.6 \mu_{B}$ per Cu ion at 4 K , in good agreement with the value deduced from previous measurements. ${ }^{4,5}$ The $g$ values, CFP, and $H_{i}$ for the best fit of the data at 90 K are given in Table II. The best fit of the data is obtained with $H_{i}$ lying in the ( $b, c$ ) plane, making an angle of $\sim 5^{\circ}$ with the $c$ axis. In Fig. 21, we present the fitting for the ( $b,[101]$ ) plane using the parameters listed in Table II. In Fig. 22, we show the best fit to the data taken at 90 K in the ( $a, c$ ) plane for a superoxygenated sample with $T_{N} \sim 190 \mathrm{~K}$. In that case we use the $g$ values and CFP listed in Table II, but a value of $H_{i}=385$ Oe was used instead of 650 Oe . The difference in $H_{i}$ is because $T_{N}$ for that sample has been reduced from $\sim 250$ to $\sim 190 \mathrm{~K}$ by annealing it in 150 atm of oxygen. In Figs. 21 and 22, for simplicity, we have included just the data corresponding to only one of the twins, simulating the


FIG. 21. Best fitting for the data taken in the ( $b,[101]$ ) plane at 90 K and 35.5 GHz using the parameters listed in Table II. We have included only the data corresponding to one of the twins.
data of an "untwinned" single crystal. The average splitting for the different transitions in the ( $a, c$ ) plane at 90 K for the sample illustrated in Fig. 22 is shown in Fig. 23 as a function of angle. The solid line corresponds to $\delta H=2 H_{i} \sin \theta(\mathrm{Oe})=770 \sin \theta(\mathrm{Oe})$.

The agreement between the data and the simulation is very good in almost all the cases, however, as can be seen in Fig. 21 for the applied magnetic field $H$ making angles of $\sim 30^{\circ}$ or less with the $b$ axis, the data for the lowest transitions cannot be fit within the experimental error. The origin of these differences may result from one of the following mechanisms not considered in our model: (i) A Heisenberg type of exchange between the Gd ions and the Cu moments, of the form $\sum_{k} J_{k} S_{\mathrm{Gd}} S_{\mathrm{Cu}}^{(k)}$. Its contribution to the internal field will depend on the local canting of the Cu moments and, in principle, it will not point in opposite directions for neighboring Gd sites. If so, the internal fields acting on neighboring Gd ions may differ in magnitude and not be perfectly antiparallel, as is the case when they are due only to the dipolar field of the Cu moments. If we allow the internal fields "seen" by the Gd sites to differ $\sim 10 \%$ in magnitude and $\sim 10^{\circ}$ from being

TABLE II. $g$ values, crystal-field parameters and internal magnetic field at 90 K for $\mathrm{La}_{2} \mathrm{CuO}_{4}$ : $\mathrm{Gd}^{3+}$ as grown with $T_{N} \sim 250 \mathrm{~K}$.

| $g$ values | $b_{2}^{m}\left(10^{-4} \mathrm{~cm}^{-1}\right)$ | $b_{4}^{m}\left(10^{-4} \mathrm{~cm}^{-1}\right)$ | $b_{6}^{m}\left(10^{-4} \mathrm{~cm}^{-1}\right)$ | $H_{i}(\mathrm{Oe})$ |
| :---: | :--- | :--- | :--- | :--- |
| $g_{x}=1.976 \pm 0.001$ | $b_{2}^{0}=-1366 \pm 10$ | $b_{4}^{0}=-12 \pm 1$ | $b_{6}^{0}=-1 \pm 1$ | $650 \pm 30$ |
| $g_{y}=1.981 \pm 0.001$ | $b_{2}^{1}=-2040 \pm 10$ | $b_{4}^{1}=-70 \pm 10$ | $b_{6}^{1}=50 \pm 10$ |  |
| $g_{z}=1.982 \pm 0.001$ | $b_{2}^{2}=-335 \pm 5$ | $b_{4}^{2}=-4 \pm 2$ | $b_{6}^{2}=15 \pm 10$ |  |
|  |  | $b_{4}^{3}=140 \pm 20$ | $b_{6}^{3}=3 \pm 3$ |  |
|  | $b_{4}^{4}=25 \pm 5$ | $b_{6}^{4}=-10 \pm 10$ |  |  |
|  |  | $b_{6}^{5}=150 \pm 20$ |  |  |



FIG. 22. Best fitting to the data taken at 90 K and 35.4 GHz , when $\mathbf{H}_{0}$ is rotated in the ( $a, c$ ) plane, using the parameters listed in Table II, but with $H_{i}=385 \mathrm{Oe}$ (see text). For clarity we have used the data corresponding to only one of the twins.
perfectly antiparallel, then the data can be fit for all directions and temperatures within the experimental error. (ii) Another way to explain the observed differences is that the AF ordering in conjunction with the spin canting of the Cu moments may produce shifts in the ionic coordinates within each unit cell and give rise to an internal magnetostriction. Furthermore, the induced ionic displacements within the unit cell could result in changes of the crystal electric field and orbital overlaps. Such changes may give rise to shifts in the position of the finestructure lines of $\mathrm{Gd}^{3+}$, which could also lower the symmetry of the spin site. However, the symmetry at the $\mathrm{Gd}^{3+}$ site is already low, $C_{1 h}$, so we expect to observe


FIG. 23. The angular dependence of the average splitting for the different transitions in the ( $a, c$ ) plane at 90 K for the twin illustrated in Fig. 22. The solid line is the fitting with $\delta H=770 x \sin \theta \mathrm{Oe}$, with $\theta=0^{\circ}$ for $H \|[100]$ and $\theta=90^{\circ}$ for $H \|[001]$ (see text).
changes mainly in the magnitude of the crystal-field parameters. We can improve the fitting of the data if we assign a different set of CFP's to each of the Gd sites created below $T_{0}$, keeping an internal magnetic field of the same magnitude and different sign acting on each of them. A different set of CFP's, below $T_{0}$, for each Gd site may result from an induced internal ionic displacement, if half of the Gd sites sees an expansion, and the other half a contraction of their unit cell, or an equivalent half sees a reduction and the other half an increase of their CFP's. It is interesting to note that below $T_{0}$ and with $H$ making an angle of $\lesssim 30^{\circ}$ with the $b$ axis, the linewidth of the split lines associated with a given transition [see Figs. 10(a), 15(a), and 16(a)] supports a larger distribution of resonance field, that is, larger linewidths, for those sites "having the smaller CFP."

The dependence of $\delta H$ on the Sr concentration, $x$, is similar to that found by NQR by Watanabe et al. ${ }^{6}$ for the ordering of $\mathrm{La}_{2-x} \mathrm{Ba}_{x} \mathrm{CuO}_{4}$ including the abrupt change observed at $\sim 20 \mathrm{~K}$ for $x=0.009$. These authors argued that a possible origin of the increase in the internal field at low temperature may be due to a change from incoherent ordered state to a coherent one.

The large broadening of the linewidths at $T \gtrsim T_{0}$ shown in Figs. 13-16 is observed in all the samples studied. Its origin is possible due to slow magnetic fluctuations present at $T>T_{0}$.

## VI. CONCLUSIONS

For $T>T_{0}$ we have identified four different sites of $\mathrm{Gd}^{3+}$ in $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}$, each with $C_{1 h}$ local point symmetry. The number of nonequivalent $\mathrm{Gd}^{3+}$ observed is that expected for twinned crystals. The crystal-field parameters listed in Table I fit the data within the experimental error, for all the directions of the magnetic field. Samples annealed under vacuum or oxygen, as the one doped with Sr up to $x=0.024$, show only small changes on their CFP's from the values listed in Table I.

For $T<T_{0}$ further splittings of the EPR lines are found. The values of $T_{0}$ are in good agreement with the values of $T_{N}$ determined by dc magnetization for the samples of $\mathrm{La}_{2-x} \mathrm{Sr}_{x} \mathrm{CuO}_{4}, x=0,0.009$, and 0.024 , as for the samples of $\mathrm{La}_{2} \mathrm{CuO}_{4}$ annealed under vacuum or oxygen. The changes in the EPR spectra found at $T<T_{0}$ are associated with the magnetic ordering of the Cu lattice. Several signatures in the EPR spectra that result from this magnetic ordering are observed. One is the presence of an internal field at the Gd site whose origin, at least most of it, is due to the dipolar field associated to the AF ordered Cu moments. The temperature dependence and magnitude of the splitting of the lines implies $\sim 0.6 \mu_{B}$ per Cu ion at $T=0 \mathrm{~K}$, for a magnetic structure with the Cu moments lying in the ( $b, c$ ) plane about $5^{\circ}$ from the $c$ axis, which is in good agreement with the magnetic structure suggested by neutron experiments. ${ }^{4}$

The data below $T_{0}$ can be fitted within the experimental error for all the directions of the applied magnetic field, but for $H$ lying within $\sim 30^{\circ}$ of the $b$ axis. In that case, the difference between the fitting and the data is
about twice the experimental error. It is possible that other mechanisms, such as a Heisenberg type of exchange interacting between the Cu and Gd moment, or a distortion of the lattice below $T_{0}$ due to the AF ordering of the Cu moments can be the origin of the differences found. In fact, we can fit the data within the experimental error, if we allow for an extra contribution to the internal field such that neighboring Gd ions are subject to internal magnetic fields $\sim 10 \%$ different in magnitude and not exactly antiparallel. We also can fit the data within the experimental error keeping an internal field of the same magnitude and different sign acting on neighboring Gd sites, but allowing for different CFP's for each of the Gd sites.

Another interesting feature observed at both frequencies for the samples studied is a well-defined maximum in the linewidth at $\sim T_{0}$ for all the transitions and orientations. Its origin is possible due to slow magnetic fluctuations present above the temperature at which a threedimensional ordering occurs. Finally, it should be mentioned that because our EPR data are observed in a
"foreign" species $\left(\mathrm{Gd}^{3+}\right)$ substituting for $\mathrm{La}^{3+}$ ions, the interpretation of our data should be taken with some reservations.

In summary, our data show that in spite of the difficulties in working with twinned crystals, EPR is a powerful and sensitive technique to further our understanding of the rich and complex magnetic behavior of the planar $\mathrm{CuO}_{2}$ materials.

## ACKNOWLEDGMENTS

We wish to thank Professor D. R. Fredkin and H. Shore for helpful conversations. This research was partially supported at San Diego State University by the Natural Science Foundation (NSF) under Grant Nos. NSF-DMR-9117212 and NSF-INT-9202813, at Los Alamos National Laboratory was performed under the auspices of the United States Department of Energy and at the University of California San Diego by Grant Nos. NSF-DMR-89-15815 and AFOSR-90-0365, DE-AC0476DP00789.
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