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Interpolation-Based QR Decomposition and Channel Estimation Processor for MIMO-OFDM System

Po-Lin Chiu, Member, IEEE, Lin-Zheng Huang, Li-Wei Chai, and Yuan-Hao Huang, Member, IEEE

Abstract—This paper presents a modified interpolation-based QR decomposition algorithm for the grouped-ordering multipleinput multiple-output (MIMO) orthogonal frequency division multiplexing (OFDM) systems. Based on the original research that integrates the calculations of the frequency-domain channel estimation and the QR decomposition for the MIMO-OFDM system, this study proposes a modified algorithm that possesses a scalable property to save the power consumption for interpolation-based QR decomposition in the variable-rank MIMO scheme. Furthermore, we also develop the general equations and a timing scheduling method for the hardware design of the proposed QR decomposition processor for the higher-dimension MIMO system. Based on the proposed algorithm, a configurable interpolation-based QR decomposition and channel estimation processor was designed and implemented using a 90-nm one-poly nine-metal CMOS technology. The processor supports 2×2 , 2×4 and 4×4 QR-based MIMO detection for the 3GPP-LTE MIMO-OFDM system and achieves the throughput of 35.16 MQRD/s at its maximum clock rate 140.65 MHz.

Index Terms—Interpolation, multiple-input multiple-output (MIMO), QR decomposition (QRD).

I. INTRODUCTION

M ORE and more ubiquitous applications of wireless communication in our daily lives have increased demand for high data rate and high-quality wireless access. Thus, wideband communication techniques have been developed to increase the service quality. The adoption of orthogonal frequency division multiplexing with multiple-input multiple-output technology (MIMO-OFDM) promises a significant increase in data rate and spectral efficiency without bandwidth expansion. The spatial multiplexing (SM) technique conveys independent data streams simultaneously via different transmit antennas so as to increase the data rate [1]. Therefore, the MIMO receiver obtains the combinative data stream that suffered from wireless channel effects. Thus, a MIMO detector, that detects the transmitted data

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of each transmit antenna, plays an important role in the MIMO system.

Beside the extremely high-complexity maximum likelihood (ML) MIMO detector, several suboptimal MIMO detection algorithms have been proposed to improve the complexity and detection performance. The iterative detection schemes [2], [3] and the tree-search-based detection schemes [4], [5] are two kinds of the most popular algorithms. The iterative detection algorithm, like successive interference cancellation (SIC), has lower complexity than ML and can be implemented easily. The tree-search-based detection algorithm, like sphere decoding and K-best algorithm, has near-ML performance, but its complexity is also higher than that of the iterative detection algorithm. Both kinds of detection algorithms need the QR decomposition preprocessing to avoid the complicated pseudo-inverse computation of channel matrix. Then, the subsequent detection processes become more simple.

The throughput and complexity are two implementation issues of the QR decomposition, and many researchers [6]–[12] have made their efforts to improve the processing latency and the hardware cost of the QR decomposition. However, most of them considered the single-carrier QR decomposition and these tone-by-tone QR decompositions could not fulfill the requirements of the real-time processing for the multi-carrier MIMO system if the MIMO dimension is very high. The complexity of QR decomposition is $O(n^3)$ for an $n \times n$ matrix, and grows proportionally with the FFT size in the OFDM system. Because the FFT size is usually very large and the MIMO detection must be performed on every subcarrier, the complexity of QR decomposition becomes tremendous in the MIMO-OFDM systems. In order to support much higher data rate, MIMO dimension has an increasing trend in the wireless communication systems. For example, IEEE 802.16e uses 2×2 MIMO scheme [13], and 4×4 MIMO scheme is supported by IEEE 802.11n [14] and 3GPP-LTE [15]. Furthermore, higher MIMO dimension, such as 8×8 , is discussed in IEEE 802.16m [16] and 3GPP LTE-Advanced [17] standard committees. Thus, the increasing complexity of QR decomposition caused by high MIMO dimension is an essential issue for the next generation wireless communication systems.

Accordingly, the interpolation-based QR decomposition (IQRD) algorithms [18], [19] were proposed to mitigate the complexity issue of QR decomposition in the MIMO-OFDM system. The interpolation-based QR decomposition algorithm efficiently combines the calculations of channel estimation in the OFDM system and the QR decomposition in the MIMO detection so as to greatly reduce the overall complexity. The algorithm performs QR decomposition only on the pilot

subcarriers and obtains the mapped QR matrices of the data subcarriers by interpolation. Based on the generic idea, we propose a scalable interpolation-based QR decomposition algorithm for the high-dimension MIMO-OFDM system [20]. The proposed algorithm has better stability than the Gram-Schmidt-based interpolation-based QR decomposition algorithm [18] because the proposed algorithm does not need square root and division operations before the inverse mapping process. Moreover, in this paper, we establish a configurable hardware architecture to support various MIMO configurations according to the MIMO channel rank. In the reduced-rank MIMO channel, the proposed hardware architecture can save computation power by the scalability property of the proposed algorithm. Moreover, we also develop a timing-schedule analysis algorithm based on the proposed hardware architecture so that the hardware architecture and timing schedule can be easily extended to the higher-dimension MIMO scheme.

The remainder of this paper is organized as follows. The signal model and system specifications are defined in Section II. Section III introduces the traditional and the proposed interpolation-based QR decomposition algorithms. In Section IV, we present the timing schedule analysis method for the configurable hardware. Then, the proposed configurable hardware architecture and chip implementation results are shown in Section V. Finally, Section VI makes a brief conclusion.

II. SIGNAL MODEL AND SYSTEM SPECIFICATIONS

A. Signal Model

For the spatial multiplexing MIMO system with N transmit antennas and M receive antennas, where $M \ge N$, the $N \times 1$ data vector $\mathbf{x} \triangleq [x_1 \ x_2 \cdots x_N]^T$ is transmitted via N transmit antennas. Then, the transmitted data is affected by an $M \times N$ MIMO fading channel **H** and an $M \times 1$ additive white Gaussian noise (AWGN) $\mathbf{n} \triangleq [n_1 \ n_2 \cdots n_M]^T$. Hence, the $M \times 1$ signal vector $\mathbf{y} \triangleq [y_1 \ y_2 \cdots y_M]^T$ is received at the receiver side, and the MIMO signal model can be expressed as

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n}$$

Generally, in the MIMO receiver, the channel information is estimated by the channel estimator. The MIMO detector uses the received data and the estimated channel response to detect the transmitted data thereafter. Usually, the channel **H** is assumed perfectly known in the MIMO detector for problem simplification.

In the MIMO-OFDM system, as shown in Fig. 1, signal bandwidth is divided into many subcarriers according to the number of FFT size. The system usually needs to perform $128 \sim 2048$ MIMO detections in one OFDM symbol, thus, the computational complexity is tremendously high. If the antenna number increases, the computation complexity further grows dramatically but the available execution time is still restricted in one OFDM symbol. Therefore, for the QR-based MIMO detector, the QR decomposition and MIMO detection are two essential implementation issues.

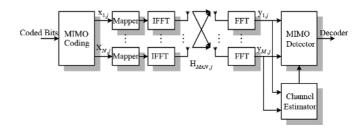


Fig. 1. Block diagram of the MIMO-OFDM system.

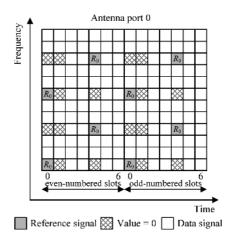


Fig. 2. Pilot locations for the first transmit antenna in the 3GPP-LTE system.

B. System Specification

In this paper, we follow the specification of 3GPP-LTE Release 8 [15] to perform the analysis, simulation, and implementation. The 3GPP-LTE supports a maximum 2048-point FFT size at 20-MHz bandwidth and has three MIMO configurations, 2×2 , 2×4 , and 4×4 . In order to facilitate the operation of these MIMO configurations, 3GPP-LTE specifies the pilot pattern within an unit of resource block (RB) which contains twelve concatenated subcarriers. Fig. 2 shows an example of the pilot pattern in every RB of a subframe at the first antenna port, but the location may be shifted in frequency domain for different subframes. In the simulation of this paper, we use reference channel models specified by 3GPP-LTE [21] including Extended Vehicular A (EVA), Extended Pedestrian A (EPA), and Extended Typical Urban (ETU) channel models.

III. INTERPOLATION-BASED QR DECOMPOSITION

In general, the traditional tone-by-tone QR decomposition in a MIMO-OFDM system estimates the channel matrices by interpolation firstly and then performs the QR decomposition on each subcarrier as shown in Fig. 3(a), in which H_1 , H_7 and H_{13} are the MIMO channel matrices for pilot subcarriers. The computational complexity of this brute-force QR decomposition is extremely high for the large number of subcarriers and the high-dimension MIMO scheme. Thus, the interpolation method [18] was proposed to avoid computing the QR decomposition on every subcarrier so as to greatly reduce the overall complexity.

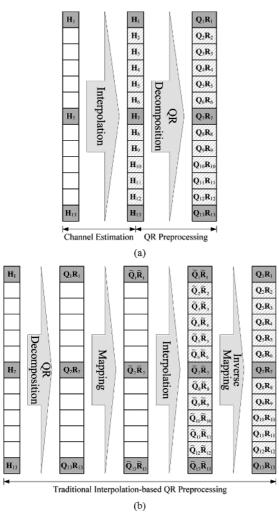


Fig. 3. (a) Traditional tone-by-tone QR decomposition algorithm. (b) Traditional interpolation-based QR decomposition algorithm in the MIMO-OFDM system.

A. Traditional Interpolation-Based QRD

The generic interpolation-based QR decomposition algorithm [18] is a Gram-Schmidt-based algorithm. The Gram-Schmidt orthogonalization is an iterative process expressed by

$$\mathbf{u}_{k} = \mathbf{h}_{k} - \sum_{j=1}^{k-1} \mathbf{q}_{j}^{H} \mathbf{h}_{k} \mathbf{q}_{j}, \quad \mathbf{u}_{1} = \mathbf{h}_{1}$$
$$\mathbf{q}_{k} = \frac{\mathbf{u}_{k}}{\|\mathbf{u}_{k}\|} \quad \mathbf{r}_{k}^{T} = \mathbf{q}_{k}^{H} \mathbf{H}$$
(1)

where k = 1, ..., N. The \mathbf{h}_k and \mathbf{q}_k are the *k*th column vectors of \mathbf{H} and \mathbf{Q} , respectively, and the \mathbf{r}_k^T is the *k*th row vector of \mathbf{R} . The superscripts of H and T represent the Hermitian and transpose of a matrix respectively. The interpolation-based QR decomposition [18] verifies that only the Laurent polynomial (LP) matrices can be interpolated. This algorithm is conceptually depicted in Fig. 3(b). Instead of estimating the channel matrices of all subcarriers, the algorithm only needs the channel matrices of the pilot subcarriers, \mathbf{H}_1 , \mathbf{H}_7 , and \mathbf{H}_{13} , and computes their corresponding \mathbf{Q} and \mathbf{R} matrices. Because the \mathbf{Q}

and **R** matrices are not LP matrices, the polynomial interpolation technique can not be applied straightforward. Therefore, an invertible mapping function \mathcal{M} was introduced to obtain the mapped LP matrices $\left(\tilde{\mathbf{Q}}, \tilde{\mathbf{R}}\right) = \mathcal{M}(\mathbf{Q}, \mathbf{R})$; consequently, the interpolation of $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ matrices becomes applicable. Then, the **Q** and **R** matrices of data subcarriers are obtained by the inverse mapping \mathcal{M}^{-1} from their interpolated $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ matrices. The mapping and inverse mapping functions are formulated by

$$\mathcal{M}: \tilde{\mathbf{Q}} = \mathbf{Q} \boldsymbol{\Delta} \quad \tilde{\mathbf{R}} = \boldsymbol{\Delta} \mathbf{R} \tag{2}$$

$$\mathcal{M}^{-1}: \mathbf{Q} = \tilde{\mathbf{Q}} \boldsymbol{\Delta}^{-1} \quad \mathbf{R} = \boldsymbol{\Delta}^{-1} \tilde{\mathbf{R}}$$
(3)

and

$$\Delta_1 = r_{1,1} = \sqrt{\tilde{r}_{1,1}}$$
$$\Delta_i = r_{i,i} \cdot \prod_{j=1}^{i-1} r_{j,j}^2 = \sqrt{\tilde{r}_{i,i}\tilde{r}_{i-1,i-1}}, \quad i \ge 2.$$

B. Proposed Interpolation-Based QRD

The traditional Gram-Schmidt-based interpolation-based QR decomposition requires square root and division operations (1) and the mapping function. Thus, we try to further reduce these calculations by exploring (1) in a 2×2 MIMO system as an example. The 2×2 QR decomposition is written as

$$\begin{split} \mathbf{H} &= \begin{bmatrix} \mathbf{h}_1 & \mathbf{h}_2 \end{bmatrix} \\ &= \begin{bmatrix} \mathbf{q}_1 & \mathbf{q}_2 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} \\ 0 & r_{22} \end{bmatrix} \\ &= \begin{bmatrix} \frac{\mathbf{h}_1}{\|\mathbf{h}_1\|} & \frac{\mathbf{h}_2 - \mathbf{q}_1^H \mathbf{h}_2 \mathbf{q}_1}{\|\mathbf{h}_2 - \mathbf{q}_1^H \mathbf{h}_2 \mathbf{q}_1\|} \end{bmatrix} \begin{bmatrix} \|\mathbf{h}_1\| & \mathbf{q}_1^H \mathbf{h}_2 \\ 0 & \|\mathbf{h}_2 - \mathbf{q}_1^H \mathbf{h}_2 \mathbf{q}_1\| \end{bmatrix}. \end{split}$$

Then, according to (2), the mapped $\hat{\mathbf{Q}}$ and $\hat{\mathbf{R}}$ matrices become

$$\mathbf{Q} = \mathbf{Q}\boldsymbol{\Delta}$$

$$= \begin{bmatrix} \frac{\mathbf{h}_{1}}{\|\mathbf{h}_{1}\|} & \frac{\mathbf{h}_{2}-r_{12}\mathbf{q}_{1}}{\|\mathbf{h}_{2}-r_{12}\mathbf{q}_{1}\|} \end{bmatrix} \begin{bmatrix} \|\mathbf{h}_{1}\| & 0\\ 0 & \|\mathbf{h}_{1}\|^{2} \|\mathbf{h}_{2}-r_{12}\mathbf{q}_{1}\| \end{bmatrix}$$

$$= \begin{bmatrix} \mathbf{h}_{1} & (\mathbf{h}_{2}-r_{12}\mathbf{q}_{1}) \|\mathbf{h}_{1}\|^{2} \end{bmatrix}$$

$$= \begin{bmatrix} \mathbf{h}_{1} & (\mathbf{h}_{1}^{H}\mathbf{h}_{1}) \mathbf{h}_{2} - (\mathbf{h}_{1}^{H}\mathbf{h}_{2}) \mathbf{h}_{1} \end{bmatrix}$$
(4)

and

$$\mathbf{R} = \Delta \mathbf{R}$$

$$= \begin{bmatrix} \|\mathbf{h}_{1}\| & 0 \\ 0 & \|\mathbf{h}_{1}\|^{2} \|\mathbf{h}_{2} - r_{12}\mathbf{q}_{1}\| \end{bmatrix} \begin{bmatrix} \|\mathbf{h}_{1}\| & \mathbf{q}_{1}^{H}\mathbf{h}_{2} \\ 0 & \|\mathbf{h}_{2} - r_{12}\mathbf{q}_{1}\| \end{bmatrix}$$

$$= \begin{bmatrix} \|\mathbf{h}_{1}\|^{2} & \|\mathbf{h}_{1}\| \|\mathbf{q}_{1}^{H}\mathbf{h}_{2} \\ 0 & \|\mathbf{h}_{1}\|^{2} \|\mathbf{h}_{2} - r_{12}\mathbf{q}_{1}\|^{2} \end{bmatrix}$$

$$= \begin{bmatrix} \mathbf{h}_{1}^{H}\mathbf{h}_{1} & \mathbf{h}_{1}^{H}\mathbf{h}_{2} \\ 0 & (\mathbf{h}_{1}^{H}\mathbf{h}_{1}) (\mathbf{h}_{2}^{H}\mathbf{h}_{2}) - (\mathbf{h}_{2}^{H}\mathbf{h}_{1}) (\mathbf{h}_{1}^{H}\mathbf{h}_{2}) \end{bmatrix}.$$
(5)

We found that all entries in the Q and R matrices have no square root and division operations and all product terms in the

 $\hat{\mathbf{Q}}$ and $\hat{\mathbf{R}}$ can be found in the entries of \mathbf{H} and its Hermitian matrix \mathbf{A} , where

$$egin{aligned} \mathbf{A} &= \mathbf{H}^H \mathbf{H} \ &= egin{bmatrix} \mathbf{h}_1^H \mathbf{h}_1 & \mathbf{h}_1^H \mathbf{h}_2 \ & egin{matrix} \mathbf{h}_1^H \mathbf{h}_2 \end{pmatrix}^* & \mathbf{h}_2^H \mathbf{h}_2 \end{bmatrix} \end{aligned}$$

This property exists in any MIMO dimensions. Accordingly, we propose a modified interpolation-based QR decomposition (MIQRD) algorithm which computes the Hermitian matrix of the channel matrix before performing the QR decomposition. Then, the $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ matrices are computed directly from the entries of channel matrix and its corresponding Hermitian matrix with only multiplication and addition. After the $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ matrices are calculated by this one-step processing, the subsequent processes are the same as the traditional interpolation-based QR decomposition algorithm such as interpolation and inverse mapping. The proposed algorithm can be illustrated in Fig. 4(a).

Furthermore, we extend the proposed algorithm to the 4×4 QR decomposition to show its scalable property. The proposed one-step processing is divided into several micro steps according to the number of transmit antennas, and these micro steps are performed sequentially as follows:

Initial :

$$\mathbf{H}^{H}\mathbf{H} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{12}^{*} & a_{22} & a_{23} & a_{24} \\ a_{13}^{*} & a_{23}^{*} & a_{33} & a_{34} \\ a_{14}^{*} & a_{24}^{*} & a_{34}^{*} & a_{44} \end{bmatrix}$$
(6a)

Micro-step 1 :

$$① \begin{cases} \tilde{\mathbf{q}}_1 = \mathbf{h}_1 \\ \tilde{r}_{1i} = a_{1i}, & i = 1, 2, \dots, 4 \end{cases}
 \tag{6b}$$

Micro-step 2:

$$\hat{\mathbf{q}}_{2} = a_{11}\mathbf{h}_{2} - a_{12}\mathbf{h}_{1} \\ \tilde{r}_{22} = a_{11}a_{22} - a_{12}a_{21} \\ \hat{\mathbf{s}}_{23} = a_{11}a_{23} - a_{13}a_{21} \\ t_{1} = a_{12}a_{23} - a_{13}a_{22} \\ \hat{\mathbf{s}}_{24} = a_{11}a_{24} - a_{14}a_{21} \\ t_{2} = a_{12}a_{24} - a_{14}a_{22} \\ t_{3} = a_{13}a_{24} - a_{14}a_{23}$$

$$(6c)$$

Micro-step 3 :

$$\begin{array}{l}
\textcircled{3} \left\{ \begin{array}{l} \tilde{\mathbf{q}}_{3} = \tilde{r}_{22}\mathbf{h}_{3} - \tilde{r}_{23}\mathbf{h}_{2} + t_{1}\mathbf{h}_{1} \\ \tilde{r}_{33} = \tilde{r}_{22}a_{33} - \tilde{r}_{23}a_{32} + t_{1}a_{31} = c_{4} \\ \end{matrix} \right. \\
\textcircled{4} \left\{ \begin{array}{l} \tilde{r}_{34} = \tilde{r}_{22}a_{34} - \tilde{r}_{24}a_{32} + t_{2}a_{31} = c_{3} \\ c_{2} = \tilde{r}_{23}a_{34} - \tilde{r}_{24}a_{33} + t_{3}a_{31} \\ c_{1} = t_{1}a_{34} - t_{2}a_{33} + t_{3}a_{32} \\ \end{matrix} \right. \\
\overbrace{} \text{(6d)} \\ \overbrace{} \text{(icro-step 4)}^{i} :
\end{array}$$

Micro-step 4 :

$$\textcircled{4} \begin{cases} \tilde{\mathbf{q}}_4 = c_4 \mathbf{h}_4 - c_3 \mathbf{h}_3 + c_2 \mathbf{h}_2 - c_1 \mathbf{h}_1 \\ \tilde{r}_{44} = c_4 a_{44} - c_3 a_{43} + c_2 a_{42} - c_1 a_{41}. \end{cases}$$
 (6e)

These sequential processes are similar to the order of Gram-Schmidt algorithm. The first column \tilde{q}_1 of the \tilde{Q} and the first row \tilde{r}_1 of the \tilde{R} are computed firstly. Then, the second column \tilde{q}_2 and the second row \tilde{r}_2 are computed by utilizing the results of the previous micro-step. The other columns and rows of the \tilde{Q} and \tilde{R} can also be deduced by analogy.

The proposed algorithm features a scalability property for different MIMO schemes. In the practical MIMO-OFDM system,

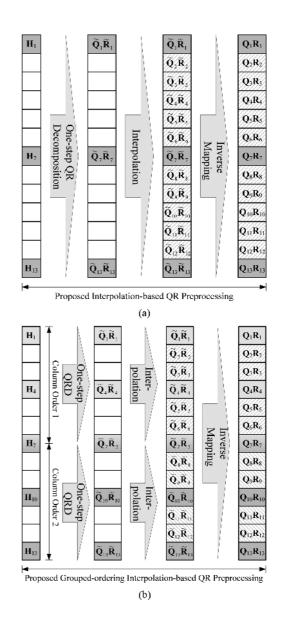


Fig. 4. Proposed interpolation-based QR decomposition for (a) the same column order and (b) the grouped column order.

the equivalent channel matrix may be not square because of non-full-rank channel or system deployment. For example, for a 4×3 channel matrix, the dimension of corresponding Hermitian matrix is 3×3 . Therefore, calculations for (6e) and a_{i4} or a_{4i} , where $i = 1, \ldots, 4$, in (6b)–(6e) can be eliminated. In summary of (6b)–(6e), for the scalable $4 \times N$ channel matrix and $N \in \{1, \ldots, 4\}$, (1)–(4) represent the calculations for N = 4, (1)-(3) for N = 3, (1) and (2) for N = 2, and (1) for N = 1. Without loss of generality, if the **Q** and **R** of an $M \times M$ channel matrix are computed, all the Q and R matrices of other $K \times L$ channel matrices, where $K \in \{1, \ldots, M\}$ and $L \in \{1, \ldots, K\}$, can be obtained without extra calculations in the proposed algorithm. Thus, the proposed algorithm features the scalability property that saves the hardware energy consumption while limited antenna resource is assigned in the system.

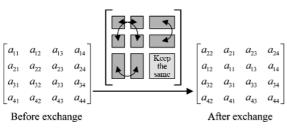


Fig. 5. Hermitian matrix before and after exchanging order of h_1 and h_2 .

TABLE I Relationships of Exchanging h_1 and h_2

Micro-step 1	Micro-step 2
$ \tilde{\mathbf{q}}'_{1} = \mathbf{h}_{2} \\ \tilde{r}'_{1i} = a_{2i}, i = 1, 2, 3, 4 $	
**	$\tilde{r}_{23}^{22} = -\tilde{t}_1$
	$\begin{array}{c}t_1^{\gamma} = -\tilde{r}_{23}\\\tilde{r}' = -t_2\end{array}$
	$t_{2'}^{\prime} = -\tilde{r}_{24}$
	$t_{3}' = -t_{3}$
Micro-step 3	Micro-step 4
	$ \tilde{\mathbf{q}}'_4 = \tilde{\mathbf{q}}_4 $ $\tilde{r}'_{44} = \tilde{r}_{44} $
$\ddot{r}'_{33} = \ddot{r}_{33} = c'_4$ $\ddot{a}' = \ddot{a}_{33} = c'_4$	$\tilde{r}'_{44} = \tilde{r}_{44}$
$\tilde{r}_{34}^{\prime r} = \tilde{r}_{34} = c_3^{\prime}$ $c_2^{\prime} = -c_1$	
$c_1^2 = -c_2$	

C. Application to Sorted QR Decomposition

In the QR-based MIMO detection, sorted QR decomposition is usually applied to improve the detection performance. However, the traditional interpolation-based OR decomposition becomes inapplicable in this situation because $(\tilde{\mathbf{Q}}_1, \tilde{\mathbf{R}}_1), (\tilde{\mathbf{Q}}_7, \tilde{\mathbf{R}}_7)$ and $(\tilde{\mathbf{Q}}_{13}, \tilde{\mathbf{R}}_{13})$ have different column orders. In order to solve this ordering problem, we propose a grouped-ordering modified interpolation-based QR decomposition (GO-MIORD) algorithm. We divide all subcarriers into several groups and the subcarriers in one group have the same column order. Fig. 4(b) shows an example of two groups. The traditional algorithm must perform the QR decompositions of the pilot subcarrier twice at the group boundary, such as subcarrier 7, for two different column orders; thus, the computational complexity doubles.

Nevertheless, the proposed algorithm can obtain the Q and R matrices of two different column orders by sharing the Hermitian matrix entries and a few additional computations. For example, if h_1 and h_2 of one channel matrix **H** are exchanged as the channel matrix of the other column order, all entries of Hermitian matrix for the second column order are the same as those for the original column order except that their indices are exchanged, as shown in Fig. 5. If we compute the (6b)-(6e) for the index-exchanged Hermitian matrix, the order-exchanged $(\tilde{\mathbf{Q}}', \tilde{\mathbf{R}}')$ pertaining to the original $(\tilde{\mathbf{Q}}, \tilde{\mathbf{R}})$ can be calculated as listed in Table I. In this best case, only $\tilde{\mathbf{q}}_2'$ needs to be re-computed, and $\left(\tilde{\mathbf{Q}},\tilde{\mathbf{R}}\right)$ and $\left(\tilde{\mathbf{Q}}',\tilde{\mathbf{R}}'\right)$ share the same Hermitian matrix. Therefore, the computational complexity can be greatly reduced. Assume that there are G groups in an OFDM symbol and P pilots in each group. The GO-MIQRD algorithm is summarized in the following.

1) Set $q \leftarrow 1$.

2) Determine the column order of group g.

3) Set $p \leftarrow 1$.

- 4) If q > 1, change the column order of the pilot p = P in group g-1 to the column order of group g, and go to step 6 by using sharing property. Otherwise, go to the next step.
- 5) Calculate Hermitian matrix $\mathbf{A} = \mathbf{H}^H \mathbf{H}$ of pilot p.
- 6) Set $k \leftarrow 1$.
- 7) Calculate the kth column of $\hat{\mathbf{Q}}$ and the kth row of $\hat{\mathbf{R}}$
- 8) If k = N, go to the next step. Otherwise, set $k \leftarrow k + 1$ and go back to step 7.
- 9) If p = P, go to the next step. Otherwise, set $p \leftarrow p+1$ and go back to step 5.
- 10) Interpolate the Qs and Rs of these P pilots to obtain the \mathbf{Qs} and \mathbf{Rs} of other subcarriers in group q.
- 11) If g = G, go to the next step. Otherwise, set $g \leftarrow g + 1$ and go back to step 2.

12) For each subcarrier, apply $\mathcal{M}^{-1}: \left(\tilde{\mathbf{Q}}, \tilde{\mathbf{R}}\right) \to (\mathbf{Q}, \mathbf{R})$. For an $M \times N$ channel matrix, the complexity \mathcal{C}_{tr} of computing the \mathbf{Q} and \mathbf{R} matrices in the traditional algorithm [18], [22] is

$$\begin{aligned} \mathcal{C}_{\rm tr} &= \mathcal{C}_{\rm GR} + \mathcal{C}_{\mathcal{M}} \\ \mathcal{C}_{\rm GR} &= \frac{3}{2} (MN^2 + M^2N) - N^3 - \frac{1}{2}M^2 + 2MN \\ &- \frac{3}{2}N^2 + \frac{1}{2}M - \frac{1}{2}N \\ \mathcal{C}_{\mathcal{M}} &= M(N-1) + \frac{N(N+1)}{2} + N - 1 \end{aligned}$$

where C_{GR} is the number of complex multiplications for computing Givens-rotation-based QR decomposition, and $C_{\mathcal{M}}$ denotes the cost of mapping function \mathcal{M} . Furthermore, the complexity of the proposed algorithm for the same result is

$$\mathcal{C}_{\text{one-step}} = \frac{N(N+1)}{2}M + \sum_{step=2}^{N} \left[(\mathbf{C}_{step}^{N} + M) \times step \right].$$

The computational complexity of the traditional and the proposed algorithms for various MIMO configurations are compared in Fig. 6. The proposed algorithm has a lower complexity than the traditional algorithm especially for the grouped-ordering scheme and the amount of reduced complexity varies depending on the column order. In Fig. 6(b), although the complexity of the worst case is higher than that of the traditional algorithm in 8×8 MIMO, the average cost still approximates that of the traditional algorithm. Most important of all, the proposed algorithm has much lower complexity than the traditional algorithm for the lower-rank MIMO schemes due to its scalability property.

D. High-Dimensional Extension

As described in Section III-B, the proposed algorithm can be extended to any MIMO dimensions. For the proposed one-step process, the straightforward method expands (1) and (2) similar to (4) and (5). Then, each micro step, such as (6b) and (6c), of the one-step process can be determined from these deduced forms. However, in the higher-dimension MIMO system, the equation expansion becomes very complicated and the micro

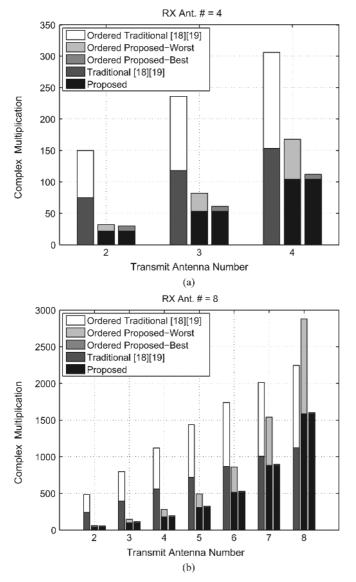


Fig. 6. Computational complexity comparisons of the traditional method and the proposed one-step method for (a) four receiving antennas and (b) eight receiving antennas.

steps of the proposed one-step algorithm are difficult to be derived correctly. Thus, we further present an iterative algorithm that can efficiently derive the micro steps and make the proposed algorithm more useful.

As mentioned in Section III-B, the down-scalability describes that $\tilde{\mathbf{Qs}}$ and $\tilde{\mathbf{Rs}}$ for $(M-1) \times (M-1)$, $(M-2) \times (M-2)$, etc., can be derived from $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ for an $M \times M$ channel matrix. From a reverse viewpoint, it is very possible that the up-scalability should be applicable such that $\tilde{\mathbf{Qs}}$ and $\tilde{\mathbf{Rs}}$ for $(M+1) \times (M+1)$, $(M+2) \times (M+2)$, etc., can also be derived from $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ for an $M \times M$ channel matrix. By investigating the results for 2×2 , 3×3 and 4×4 in (6b)–(6e), we found that \tilde{r}_{22} includes $a_{11}a_{22}$ and $a_{12}a_{21}$ terms, \tilde{r}_{23} includes $a_{11}a_{23}$ and $a_{13}a_{21}$ terms, and \tilde{r}_{24} includes $a_{11}a_{24}$ and $a_{14}a_{21}$ terms. Therefore, we deduce that \tilde{r}_{25} for 5×5 QR matrices should include $a_{11}a_{25}$ and $a_{15}a_{21}$ terms and so on. According to these rules, we can derive a generalized method to compute the $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ matrices for any MIMO dimensions. 1) Definition III.1: For a set $s \triangleq \{s_1, s_2, \ldots, s_k\}, \forall s_i \in \{1, 2, \ldots, N\}$ where $i = 1, 2, \ldots, k$, there exists a function f_d which is defined as

$$f_d(\mathbf{s}) = \sum_{i=1}^k (-1)^{k-i} f_d(\mathbf{s} \setminus \{s_i\}) a_{ks_i},$$

and
$$f_d(\{\phi\}) = 1$$

where $s \setminus \{s_i\}$ means s_i element is excluded in the set s.

Definition III.2: For an $M \times M$ channel matrix, the entries of $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ are defined as

$$\tilde{\mathbf{q}}_{k} = f_{d} \left(\{1, \dots, k\} \setminus \{k\}\right) \mathbf{h}_{k} - f_{d} \left(\{1, \dots, k\} \setminus \{k-1\}\right) \mathbf{h}_{k-1} + \cdots + (-1)^{k-1} f_{d} \left(\{1, \dots, k\} \setminus \{1\}\right) \mathbf{h}_{1} \tilde{r}_{kk} = f_{d} \left(\{1, \dots, k\} \setminus \{k\}\right) a_{kk} - f_{d} \left(\{1, \dots, k\} \setminus \{k-1\}\right) a_{k(k-1)} + \cdots + (-1)^{k-1} f_{d} \left(\{1, \dots, k\} \setminus \{1\}\right) a_{k1} = f_{d} \left(\{1, \dots, k\}\right),$$
and

 $\tilde{r}_{ij} = f_d\left(\{1,\ldots,j\}\setminus\{i,\ldots,j-1\}\right)$

where i, j, k = 1, 2, ..., M and $i < j \le M$.

According to Definition III.1 and Definition III.2, (6b)–(6e) can be summarized as

.4

Micro-step 2 :

$$\begin{array}{l}
\textcircled{i}{2} \left\{ \begin{array}{l} \widetilde{\mathbf{q}}_{2} = f_{d}\left(\{1\}\right) \mathbf{h}_{1} - f_{d}\left(\{2\}\right) \mathbf{h}_{2} \\ \widetilde{r}_{22} = f_{d}\left(\{1,2\}\right) \\ \\
\textcircled{i}{3} \left\{ \begin{array}{l} \widetilde{r}_{23} = f_{d}\left(\{1,3\}\right) \\ t_{1} = f_{d}\left(\{2,3\}\right) \\ t_{2} = f_{d}\left(\{2,4\}\right) \\ t_{3} = f_{d}\left(\{3,4\}\right) \\ \end{array} \right. \end{matrix} \right\}$$

Micro-step 3:

$$\widehat{\mathbf{3}} \begin{cases} \widetilde{\mathbf{q}}_{3} = f_{d}\left(\{1,2\}\right)\mathbf{h}_{3} - f_{d}\left(\{1,3\}\right)\mathbf{h}_{2} + f_{d}\left(\{2,3\}\right)\mathbf{h}_{1} \\ \widetilde{r}_{33} = f_{d}\left(\{1,2,3\}\right) \\ \\ \widehat{\mathbf{4}} \end{cases} \begin{cases} \widetilde{r}_{34} = f_{d}\left(\{1,2,4\}\right) \\ c_{2} = f_{d}\left(\{1,3,4\}\right) \\ c_{1} = f_{d}\left(\{2,3,4\}\right) \end{cases}$$

Micro-step 4:

$$(4) \begin{cases} \tilde{\mathbf{q}}_4 = f_d\left(\{1,2,3\}\right)\mathbf{h}_4 - f_d\left(\{1,2,4\}\right)\mathbf{h}_3 \\ + f_d\left(\{1,3,4\}\right)\mathbf{h}_2 - f_d\left(\{2,3,4\}\right)\mathbf{h}_1 \\ \tilde{r}_{44} = f_d\left(\{1,2,3,4\}\right). \end{cases}$$

Similarly, all entries of the $\mathbf{\hat{Q}}$ and $\mathbf{\hat{R}}$ for other MIMO dimensions can be derived quickly by these two definitions.

E. Interpolation Scheme

The \mathbf{Q} and \mathbf{R} matrices of data subcarriers are generated by interpolation and then delivered to subsequent MIMO detector after inverse mapping. Hence, the accuracy of the interpolated

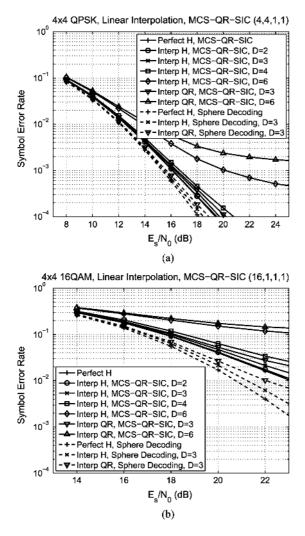


Fig. 7. SER performance results by utilizing different interpolation intervals and MCS-QR-SIC MIMO detectors for the (a) QPSK (4,4,1,1) case and (b) 16QAM (16,1,1,1) case.

Q and **R** affects the final detection performance. In order to choose a proper interpolation scheme, we evaluate the detection performance by utilizing the MCS-QR-SIC MIMO detector [23] under the ETU channel model because the ETU model has the longest tap delay in the 3GPP-LTE channel models. In the simulation, we used 1024×1000 data symbols and evaluated (4,4,1,1) and (16,1,1,1) cases in the 4×4 MCS-QR-SIC MIMO detector for the QPSK and 16QAM modulations, respectively. The pilot subcarrier interval in 3GPP-LTE is six subcarriers as illustrated in Fig. 2. In Fig. 7, we can see that there is a large performance gap between the perfect channel case and interpolated channel case especially in the high-order constellation even for the traditional channel estimation method.

Because the ETU channel is very frequency selective, shortening interpolation interval is a possible method to improve the accuracy of interpolation. In Fig. 7, the symbol error rate (SER) performances of utilizing different interpolation intervals D show that the detection performance is improved with a shorter interpolation interval. Thus, we can perform timedomain interpolation first to generate additional pseudo-pilot channels, and then the pilot subcarrier interval in the frequency-

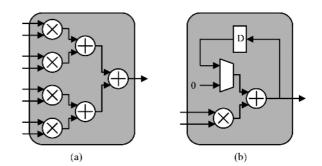


Fig. 8. Basic processing elements (a) norm and (b) MAC.

domain interpolation can be shortened from six to three subcarriers. The simulation shows that the performance degradation is small by using linear polynomial interpolation scheme when E_s/N_0 is around 16 dB and 20 dB for the QPSK and 16 QAM modulations, respectively.

IV. TIMING SCHEDULE ANALYSIS

The proposed one-step process [see (6a)-(6e)] has two special properties. The first property is that all computations are composed of addition and multiplication operations. Thus, two basic hardware elements, norm and multiplication-and-accumulation (MAC), are proposed to implement these operations, as shown in Fig. 8. The norm element calculates the inner product and the MAC element accumulates the products. According to the complexity analysis in Section III-C, many norm and MAC elements are required to realize parallel implementation, especially in the high-dimension MIMO system. The second property is that there exists data dependency between each micro step in the one-step process. Therefore, we must carefully partition the algorithm into several subparallel computations on the norm and MAC elements. The most important design issue is to balance the tradeoff between the hardware complexity and the computation cycle count with an appropriate subparallel hardware architecture and an efficient timing schedule of all operations.

We use α norms and β MACs, that is $\alpha M + \beta$ complex multipliers for M receive antennas, to approach the cycle bound, so that the hardware efficiency can approach 100%. As the M increases, the design complexity grows enormously because there is a large number of the norm and MAC combinations, and scheduling their operations for the optimal $A \times T$ product, where A is the hardware complexity defined as the number of complex multipliers and T is the computational cycle count, becomes very difficult.

Therefore, we propose a method to obtain the optimal timing schedule by programming. First, in order to apply the scalability property to the timing schedule, we construct a dependency tree to determine the output order of entries of $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$, as shown in Fig. 9. Then, we can further expand the tree for \tilde{r}_{ij} according to the Definition III.1 and Definition III.2. Fig. 10 shows the expanded tree structure for \tilde{r}_{44} . We can find that all computations in one-step process can be covered by all possible $\mathbf{s} \triangleq \{s_1, s_2, \ldots, s_k\}$, where $s_i \in \{1, 2, \ldots, M\}$, $i = 1, 2, \ldots, k$ and $k \in \{1, 2, \ldots, M\}$. Thus, we use an *M*-bit binary variable *Sk* to represent the s. For each bit, "1" means

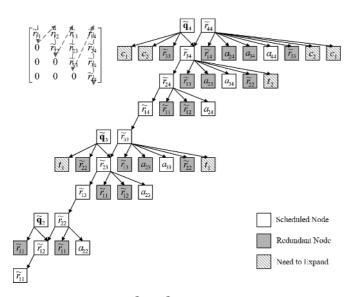


Fig. 9. Output order tree of $\tilde{\mathbf{Q}}$ and $\tilde{\mathbf{R}}$ for 4 × 4 channel matrix.

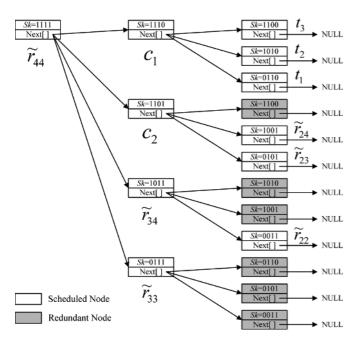


Fig. 10. Dependency tree of \tilde{r}_{44} for 4×4 channel matrix.

the existence of the corresponding s_i , and "0" represents its absence. For example, "0101" represents {1, 3} and "1110" represents {2, 3, 4}. Then, a dependency tree can be built up based on the data dependency of the micro-steps. For a given combination of the norms and MACs, we can traverse the dependency tree to schedule the operations of the proposed algorithm on the norms and MACs. One node must be scheduled after all of its child nodes have been scheduled. Note that because the computation of Hermitian matrix has the highest priority, we schedule dedicated norm elements to perform Hermitian matrix calculations to reduce the computational cycle count. After the Hermitian matrix computation is finished, the norm elements are then shared by other calculations. The MAC elements are almost scheduled for \tilde{q} vectors because each of them occupies

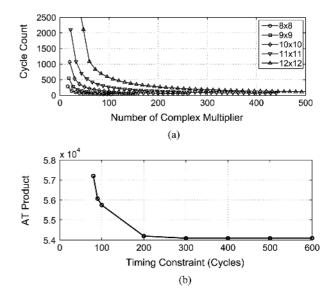


Fig. 11. (a) Timing schedule results for different MIMO configurations. (b) Scheduled smallest AT product values for 12×12 channel matrix under different timing constraints.

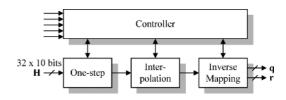


Fig. 12. Proposed MIQRD hardware architecture.

M complex multipliers over several cycles. We performed the scheduling program using different combinations of norms and MACs based on these rules, and obtained the scheduled cycle count versus the hardware complexity ($\alpha M + \beta$ multipliers) for various MIMO configurations, as shown in Fig. 11(a). If the one-step processing module must meet the throughput requirement of the system, we can use Fig. 11(a) to obtain the minimum hardware complexity under the constrained cycle time. On the other hand, the AT product versus timing constraint is plotted in Fig. 11(b). If the energy cost is the design constraint, the optimal hardware combination can be determined by choosing the smallest timing constraint that approximates the AT lower-bound, that is, 200 cycles for the example of 12×12 channel matrix in Fig. 11(b).

V. HARDWARE ARCHITECTURE AND CIRCUIT IMPLEMENTATION

Based on the proposed interpolated-QR decomposition algorithm and the timing schedule program, we designed and implemented the QR decomposition processor for 3GPP-LTE MIMO-OFDM system. The proposed QR decomposition processor consists of one-step processing, interpolation and inverse mapping, as shown in Fig. 12.

A. One-Step Processing

In the system, the pilot channel matrix is updated every three cycles of the system clock f_{sys} and four q or r vectors must be

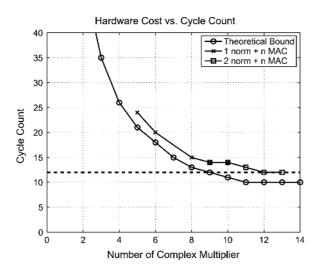


Fig. 13. Computation cycle counts for different combinations of the norm and the MAC in a 4×4 MIMO system.

cycle	1	2	3	4	5	6	7	8	9	10	11	12
norm1	<i>a</i> ₁₁	<i>a</i> ₂₂	<i>a</i> ₂₃	t_1	\widetilde{r}_{23}	\widetilde{r}_{33}	a34	t_2	\widetilde{r}_{34}	c_2	\widetilde{r}_{44}	
norm2	a_{12}	a_{13}	<i>a</i> ₃₃	\widetilde{r}_{22}	<i>a</i> ₁₄	<i>a</i> ₂₄	a_{44}	\widetilde{r}_{24}	t ₃	c_1		
MACI		\tilde{q}	12		\square	\widetilde{q}_{13}	\supset		\square	\tilde{q}	14	\supset
MAC2		(ĝ	22			$\widetilde{q}_{\scriptscriptstyle 23}$)		$\left(\right)$	\widetilde{q}_{i}	24	\supset
MAC3		\widetilde{q}	32		\square	\widetilde{q}_{33})			\widetilde{q}_{i}	34	\supset
MAC4		\tilde{q}	42		(\widetilde{q}_{43})		$\left(\right)$	\widetilde{q}	44	\supset

Fig. 14. Timing schedule of 4×4 one-step with two norms and four MACs.

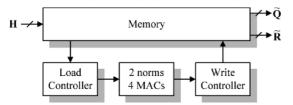


Fig. 15. Block diagram of one-step process with two norms and four MACs.

generated within four cycles for a 4×4 channel matrix. Therefore, in order to generate the $\tilde{\mathbf{Qs}}$ and $\tilde{\mathbf{Rs}}$ for three data subcarriers, the timing processing constraint for the one-step processing module is twelve cycles of the operating $f_{clk} = 4 \times f_{sys}$. Then, two norms and four MACs are selected in the one-step processing module according to Fig. 13, and the final timing schedule can be derived from the scheduling program, as shown in Fig. 14. For 2×2 and 4×2 channel matrices, one-step processing requires only four cycles so that doubled clock rate is enough. The top-level block diagram of the proposed one-step process is illustrated in Fig. 15. The memory stores five temporal complex values $(t_1, t_2, t_3, c_1, c_2)$ and 4×4 complex matrices, including $\mathbf{H}, \tilde{\mathbf{Q}}, \tilde{\mathbf{R}}$, and Hermitian matrix.

B. Interpolation

In 3GPP-LTE, the locations of pilot subcarriers in an OFDM symbol may be shifted in frequency domain for different subframes, and therefore the pilots may be not located at the edge of

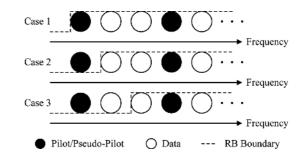


Fig. 16. Three possible pilot locations at the resource block boundary.

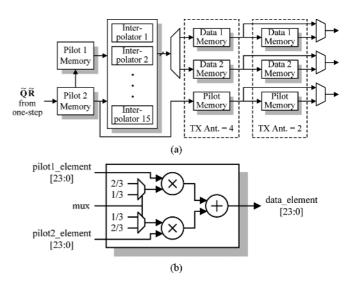


Fig. 17. (a) Interpolation architecture of $\tilde{\mathbf{Qs}}$ and $\tilde{\mathbf{R}}$ and (b) the linear real-valued interpolator.

resource block. Three possible locations of the pilot and pseudopilot (estimated by time-domain interpolation) are summarized in Fig. 16. In 3GPP-LTE, the user equipment (UE) only receives the data located in the assigned resource blocks. In case 2 and case 3, the first pilot is not located in the resource block. In order to design a regular hardware architecture of the interpolation module, the first pilot channel is extrapolated by the channel estimator.

The architecture of the \mathbf{Q} and \mathbf{R} interpolation is shown in Fig. 17(a), in which linear real-valued interpolators are utilized, as shown in Fig. 17(b). Because the proposed MIQRD is designed to output one column of $\tilde{\mathbf{Q}}$ and one row of $\tilde{\mathbf{R}}$ per cycle, it requires fifteen real-valued interpolators, eight for $\tilde{\mathbf{Q}}$ and seven for $\tilde{\mathbf{R}}$ calculations. The memories after the interpolators store the results for inverse mapping. If the pilot is a pseudo-pilot, it needs to be de-mapped so its result must also be stored. Besides, for 4×2 and 2×2 channel matrices, additional memories are required to wait for the processing of inverse mapping since the processing time of one-step module is shorter than that of the 4×4 case.

C. Inverse Mapping

Fig. 18(a) shows the block diagram of the inverse mapping module and it is composed of the demapping factor $(1/\Delta_i)$ calculation and the demapper. In order to simplify the clock design,

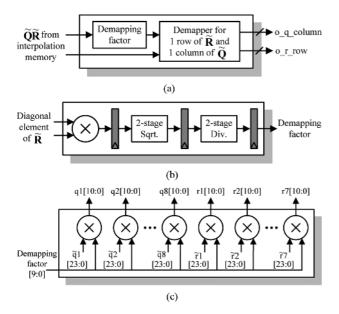


Fig. 18. Block diagram of (a) the inverse mapping, (b) the demapping factor calculation, and (c) the parallel multiplications of demapper.

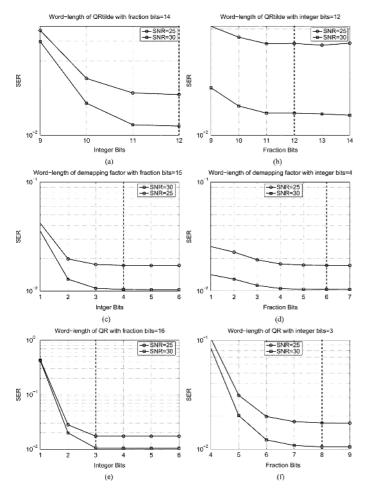


Fig. 19. Fixed-point simulation of MIQRD.

the inverse mapping hardware also operates at a quadruple frequency of the system clock. According to the word-length determined from the fixed-point simulation and the critical time

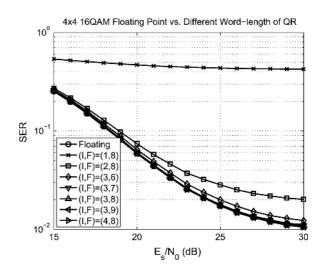


Fig. 20. SER performances of fixed point simulations for different word-lengths of ${\bf Q}$ and ${\bf R}.$

of the synthesis result, both of the square root and division are implemented by two-stage pipelined architecture to meet the timing constraint as depicted in Fig. 18(b). Then, 15 real-valued multipliers are used to de-map one column of $\tilde{\mathbf{Q}}$ and one row of $\tilde{\mathbf{R}}$ to the corresponding \mathbf{Q} and \mathbf{R} , as shown in Fig. 18(c).

D. Fixed-Point Simulation

We use the symbol error rate (SER) as the metric to determine the word-length of the signal in the fixed-point simulation. Because the clipping error has larger impact on the performance of the proposed architecture than the truncation error, we determine the word-length of the integer part for the signal first, and then the fraction part. A fixed-point 2's complement number is represented by (I,F), in which I and F denote the word-lengths of the integer part and the fraction part respectively. According to the fixed point simulation in Fig. 19, the word-length of the signals is chosen to achieve $SER = 10^{-2}$ with QPSK and 16QAM modulations. Fig. 20 shows the SER performances of fixed point simulations for different word-lengths of Q and R in 4×4 16 QAM system. Table II lists the word-length of the signals in the three modules. The word-length for the \mathbf{Q} and \mathbf{R} is larger than those of others and dominates the operating frequency because the dynamic range of \tilde{r}_{NN} grows along with the dimension of channel matrix. The processing time schedules of the whole MIQRD processor for different channel matrices are shown in Fig. 21. The latencies for $M \times 4$ and $M \times 2$ cases are 27 cycles and 15 cycles, respectively, to produce one column/row vector per cycle at the MIQRD output.

E. Circuit Implementation

The proposed interpolation-based QR decomposition processor was designed and implemented using UMC 90-nm one-poly nine-metal CMOS technology. The processor occupies 5.97 mm^2 with 1.61 mm^2 core area. Fig. 22 shows the micrograph of the chip. The function of the chip was verified and the performance measured using a digital test station. The chip consumes 49 mW at its maximum frequency 140.65 MHz. The comparison of the implementation results of the proposed and other QR decomposition processors is summarized in

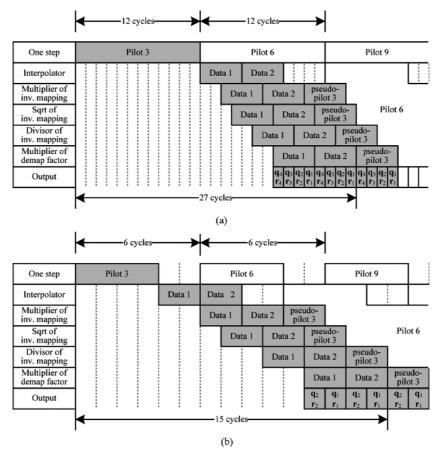


Fig. 21. Processing time of each module in MIQRD for (a) $M \times 4$ channel matrix and (b) $M \times 2$ channel matrix.

Module	Signal	Word-length	(I,F) Number		
One-step	Elements of H	10	(2,8)		
	Elements of Q, R	24	(12,12)		
Interpolation	Coefficient	4	(1,3)		
Inverse	Demapping factor	10	(4,6)		
Mapping	Elements of Q, R	11	(3,8)		

TABLE II WORD-LENGTHS OF THE MODULES IN THE PROPOSED MIQRD ARCHITECTURE

Table III. Since the proposed interpolation-based QR decomposition processor also executes the task of channel estimation, it requires a larger gate count than the other works. However, the throughput of the proposed chip is 35.16 MQRD/s and the normalized throughput of our chip is much higher than those of other works based on the tone-by-tone sole QR decomposition algorithm. Although raw gate-count number is very large in our design, the gate efficiency, either including or excluding the channel estimation, is not the worst as compared to others in the literature. Therefore, this architecture is suitable for designing a high-throughput QR decomposition processor for MIMO-OFDM receiver.

VI. CONCLUSION

This paper proposes a scalable interpolation-based QR decomposition algorithm and a grouped-ordering scheme for the

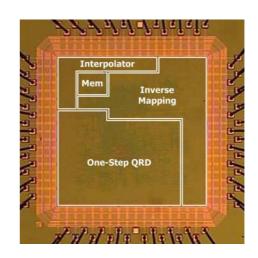


Fig. 22. Chip micrograph.

MIMO-OFDM system. The derived general equations and the proposed timing scheduling method facilitate the architecture design of the proposed algorithm. A configurable interpolation-based QR decomposition processor is also presented in the work. The processor supports 2×2 , 4×2 and 4×4 channel matrices to meet the requirements of the next generation wireless communication system. Meanwhile, it features much higher data throughput at balancing the hardware cost that is very suitable for low-complexity MIMO-OFDM systems.

Algorithm	MMSE GR-SQRD [6]	MGS [7]	MGS [8]	MMSE MGS-SQRD [10]	Givens Rotation Householder [11]	MGS [12]	This work
Matrix	4×4	4×4	4×4	4×4	4×4	4×4	$2 \times 2, 4 \times 2,$
Dimension	Complex	Real	Complex	Complex	Complex	Real	4×4 Complex
Channel Estimation	No	No	No	No	No	No	Yes
Technology	0.25um	0.18um	0.13um	UMC 0.18um	0.13um	TSMC 0.18um	UMC 90nm
	1P/5M CMOS	CMOS	CMOS	1P/6M CMOS	CMOS	CMOS	1P/9M CMOS
Core Area [mm ²]	2.1	-	-	0.997	-	-	1.61
(Gate Count [kGE])	(54)	(72)	(23.2)	(61.8)	(36)	(32.6)	(402.5/317.95 ¹)
Max. f _{clk} [MHz]	125	277	269	162	270	400	140.65
Latency [ns]	640	242	517	642	148	88	192
Processing Cycle	80	67	139	104	40	35	12
(number of QRD)	(1)	(1)	(1)	(1)	(1)	(1)	(3)
Throughput [MQRD/s]	1.56	4.1	1.93	1.56	6.76	11.43	35.16
Normalized Throughput ²	4.33	2.05	2.79	3.12	9.76	5.72	35.16
Gate Efficiency ³	80.25	28.47	120.16	50.49	271.23	175.31	87.35/110.58 ¹

TABLE III Comparison Results

Channel estimation is excluded

² Throughput × (Technology/90nm) / $(64/n^2)$. For an $N \times N$ complex matrix, n = 2N, and n = N for a real matrix.

³ (Normalized Throughput) / (Gate Count)

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