

# Investigation of flow control and cooling performance using comb plasma actuators

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## Research Article

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# **Investigation of flow control and cooling performance using comb plasma actuators**

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## 1 **Abstract**

2 This paper proposes a novel comb plasma actuator (CPA) for active flow control.  
3 The effects of the CPA on the tip and the root are investigated to improve the film  
4 cooling effectiveness. Results show that the CPA on the root increases the size of the  
5 counter-rotating vortex pairs (CRVPs) and the agminated body force arches the coolant  
6 air away from the wall. Nevertheless, the scale of the anti-counter rotating vortex pairs  
7 (Anti-CRVPs) induced by CPA on the tip is larger than one of CRVPs, which  
8 significantly weakens the coiling effect of the mainstream on the coolant air. The  
9 maximum velocity of the near-wall fluid with CPA on the tip is 1.2 times that without  
10 a plasma actuator. Compared with plasma off, the wall-averaged film cooling  
11 effectiveness increases by 90.9%, 108.9%, 87.2%, and 38.0%, respectively, under  
12 blowing ratios of 0.25, 0.5, 0.75, and 1.0 when using CPA on the tip. In addition, the  
13 wall-averaged cooling effectiveness increases by 58.7%, 108.9%, and 115.0% when  
14 applied voltages are 6 kV, 12 kV, and 24 kV%, respectively. The diffusing body force  
15 of CPA on the tip increases coolant air distributions along the spanwise direction. When  
16 the blowing ratio increases from 0.25 to 1.0, the spanwise film cooling effectiveness  
17 increases by 62.3%, 103.4%, 164.6%, and 150.5%, respectively, on average.

18 **Keywords:** aerodynamic actuation, comb electrode, film cooling, flow control, plasma,  
19 pressure loss

## 21 NOMENCLATURE

$A$	Amplitude of exposed electrode, mm
$a$	Normal height of the plasma region, mm
$b$	Streamwise length of the plasma region, mm
$D$	Diameter of film cooling hole, mm
$DR$	Coolant air to mainstream density ratio, $\rho_c/\rho_\infty$
$E$	Electric field intensity, kV/cm
$E_b$	Breakdown electric field intensity, kV/cm
$e_c$	Elementary charge, C
$F$	Body force, mN/mm <sup>3</sup>
$f$	Frequency of applied voltage, kHz
$k_1, k_2$	Spatial distribution coefficient of the electric field
$L_1$	Width of exposed electrode, mm
$L_2$	Width of covered electrode, mm
$L_3$	Spanwise length of the electrode, mm
$M$	Blowing ratio, $DR \cdot U_c/U_\infty$
$s$	Spacing between the electrodes, mm
$T$	Local fluid temperature, K
$U$	Streamwise velocity of jet flow, m/s
$W$	Normal velocity of jet flow, m/s
$X, Y, Z$	Coordinate direction distance, mm
<b>Greek symbols</b>	
$\Delta$	Growth rate of film cooling effectiveness
$\Delta t$	Charge time of plasma, $\mu$ s
$\eta$	Film cooling effectiveness
$\Theta$	Dimensionless temperature
$\lambda$	Wavelength of exposed electrode, mm
$\rho_c$	Charge density, C/m <sup>3</sup>
$\varphi$	Applied voltage, kV
<b>Subscripts</b>	
$aw$	Adiabatic wall
$c$	Coolant air
$s$	Value along the spanwise direction
$w$	Value along the wall
$\infty$	Mainstream
<b>Abbreviations</b>	
Anti-CRVPs	Anti-counter rotating vortex pairs
CPA	Comb plasma actuator
DBD	Dielectric barrier discharge

## 1. Introduction

Air pollution caused by conventional thermal power generation is a prominent problem [1]. The proposals for carbon neutrality and peak carbon dioxide emissions have led to a booming opportunity for gas turbines [2]. The cooling air required to cool the hot end components of the gas turbine derives from the compressor. Increasing the utilization of cooling air is conducive to reducing fuel consumption, which has positive implications for alleviating the current energy crisis and environmental degradation [3]. While advanced film cooling technology holds tremendous advantages in reducing the amount of cooling air, it limits cooling capacity [4].

Some researchers have focused on the effect of plasma actuation on flow control. Compared with passive flow control, such as vortex generators [5] and transverse trenches [6], active flow control using plasma actuators shows favorable characteristics, such as quick response [7], small size [8], and low power consumption [9]. Li et al. [10] indicated that the dielectric barrier discharge (DBD) plasma actuation accelerated the near-wall fluid flow. Zhang et al. [11] analyzed the start-up stage of the flow field under plasma actuation using schlieren visualization and particle image velocimetry. It was found that the plasma actuator produced a thin jet in the first stage, and an arched jet escaped from the surface in the second stage. The starting vortex controlled the induced flow field, and the arched jet disappeared in the third stage. In the fourth stage, the wall-jet played a dominant role in the induced flow field, and the deflection angle of the wall-jet was approximately constant. Chen et al. [12] analyzed the flow control effect of annular plasma actuator. Results revealed that the flow state changes from laminar

44 to turbulent in advance due to the rotating vortex ring generated by the annular plasma  
45 actuator in the opposite direction to the external air recirculation. Harinaldi et al. [13]  
46 experimentally studied the effect of plasma on flow control using a delta wing with a  
47  $65^\circ$  sweep angle. It was found that the lift coefficient of the delta wing increased by  
48 0.078, and the drag coefficient decreased by 0.053 under multiple plasma actuators.  
49 Huang et al. [14] investigated the effect of plasma actuators on flow control under a  
50 laminar separation condition. Results showed that compared with plasma off, the flow  
51 energy during one oscillation period was reduced by 726% with a co-current plasma  
52 actuator at the position of 0.6 chord from the leading edge. Plasma actuation effectively  
53 alleviated the pitch instability of laminar separation flutter at a high Reynolds number  
54 of 77,000. Zheng et al. [15] analyzed two flow control principles of alternating current  
55 (AC) plasma and nanosecond plasma both numerically and experimentally. Results  
56 indicated that the wall jet at the AC plasma discharge only affected the fluid flow near  
57 the actuator. In contrast, the flow field downstream the actuator was affected by the  
58 waste heat generated by the nanosecond plasma discharge. Giorgi et al. [16] analyzed  
59 the effect of plasma actuation on flow separation of compressor cascades. Results  
60 showed that the plasma aerodynamic actuation caused 14% reduction of the pressure  
61 loss coefficient and 3% increase in the static pressure.

62 The plasma actuator was arranged on the gas turbine blade based on active flow  
63 control to enhance the film cooling performance [17]. Dai et al. [18] studied effect of  
64 plasma aerodynamic actuation on a circular jet in cross flow field by using Smoke  
65 Visualization technology. Results showed that trend of the circular jet to stick to the

66 wall became obvious with increasing applied voltage. The large arc length of the  
67 exposed electrode at the hole outlet increased the effusion effect of the jet near the wall.  
68 Erfani et al. [19] analyzed the effect of plasma actuator temperature on thermodynamic  
69 performance. Results revealed that the maximum induced velocity of the hot medium  
70 actuator increased by 45.5% compared to that of the cold medium actuator. The shape  
71 of the plasma actuator has immensely affected aerodynamic actuation effect. Li et al.  
72 [20] investigated the effect of a sawtooth plasma actuator (STPA) on the film cooling  
73 using a plasma phenomenological model. Results showed that the film cooling  
74 effectiveness of the STPA on the tip was 65.5% higher than that of STPA on the root.  
75 Durscher and Roy [21] analyzed the disturbance of the flow field by circular and  
76 rectangular plasma actuators using particle image velocimetry. Results showed that the  
77 flow field induced by the two plasma actuators presented a spiral structure.

78 Although many scholars have focused on effect of plasma on active flow control  
79 and film cooling, few of them were related to convective heat transfer enhancement by  
80 using different shapes of plasma actuators. In this work, propose a new comb plasma  
81 actuator (CPA) is proposed and the thermodynamic performance is investigate. Based  
82 on the plasma model proposed in Shyy et al. [22], the electric body force as a source  
83 term is coupled to the momentum equation to achieve the plasma aerodynamic  
84 actuation. This research investigates the effects of the CPA on the tip and the CPA on  
85 the root on flow field disturbances and heat transfer enhancement by analyzing vortex  
86 structures near the film hole. These results create a foundation for improving film  
87 cooling performance based on the plasma actuation for the active flow control.

## 2. Model introduction and validation

This section introduces the computational domain, plasma model, boundary conditions, and governing equations.

### 2.1 Geometry and plasma actuator

Fig. 1 shows the three-dimensional computational domain in this research. A film hole with a diameter ( $D$ ) of 12.7 mm has a length of  $4D$  and an inclination angle of  $35^\circ$ . The size of the mainstream channel is  $59D \times 3D \times 10D$ , and the trailing edge of the film hole outlet is  $40D$  away from the mainstream outlet. The coolant chamber has a length of  $6D$ , a width of  $3D$ , and a height of  $6D$ . The origin of coordinates is located at the trailing edge of the film hole outlet. The axes  $X$ ,  $Y$ , and  $Z$  represent the streamwise direction, spanwise direction and normal direction of the airflow.

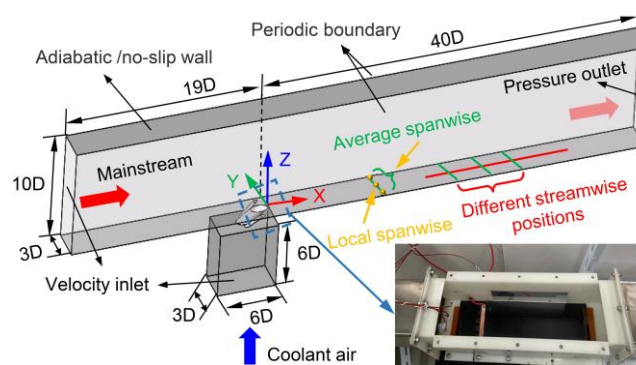


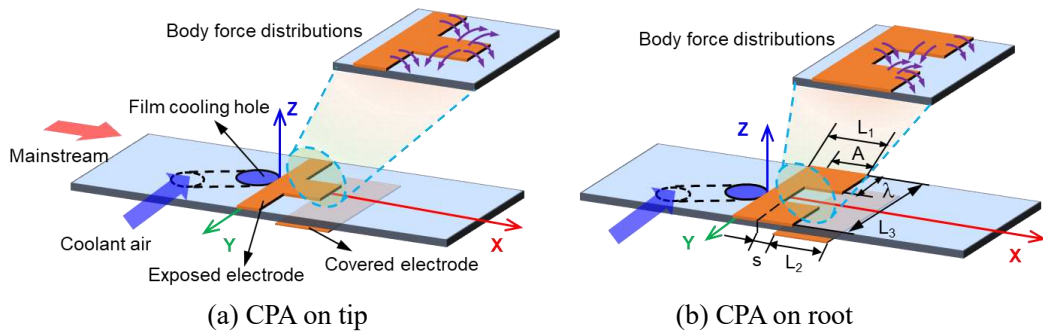
Fig. 1 Three-dimensional computational domain

Fig. 2 shows a schematic diagram of comb plasma actuators on tip and root in the numerical simulation. The exposed and covered electrodes are arranged asymmetrically on both sides of the flat plate. The bottom of the covered electrode is covered with an insulating layer to prevent plasma discharge. Table 1 presents the parameters of the comb plasma actuator. The exposed electrode has a length ( $L_1$ ) of 12 mm, amplitude ( $A$ ) of 8 mm, and wavelength ( $\lambda$ ) of 12.7 mm. The length ( $L_2$ ) of the covered electrode is



107 20 mm, and the width ( $L_3$ ) is 38.1 mm. The distance ( $s$ ) between the exposed and  
 108 covered electrodes is 1 mm, and the thickness is 0.1mm. The plasma region has  
 109 dimensions of 3 mm in height and 6 mm in length.

110 Body force distributions induced by CPA are shown in Fig. 2. The CPA on the tip  
 111 has the expended body force along the spanwise direction, whereas the CPA on the root  
 112 has an agminated body force toward the wall center. According to the plasma  
 113 phenomenological model by Shyy et al. [22], the body force from the actuator is added  
 114 to the momentum equation through user-defined functions (UDFs) in ANSYS Fluent  
 115 software as a source term. The plasma region is located in the triangular prism region  
 116 of the flat plate, and its active flow control is reflected by the acceleration of near-wall  
 117 fluid ejection.



119 (a) CPA on tip  
 120 (b) CPA on root  
 Fig. 2 Arrangements and body force distributions of comb plasma actuators

121 Table 1. Parameters of comb plasma actuators

Parameters	Values
Normal height of the plasma region ( $a$ )	3 mm
Amplitude of exposed electrode ( $A$ )	8 mm
Streamwise length of the plasma region ( $b$ )	6 mm
Applied frequency of plasma actuator ( $f$ )	2 kHz
Width of the exposed electrode ( $L_1$ )	5 mm
Width of the covered electrode ( $L_2$ )	10 mm
Spanwise length of the electrode ( $L_3$ )	38.1 mm
Spacing between the electrodes ( $s$ )	0.5 mm
Wavelength of the exposed electrode ( $\lambda$ )	12.7 mm
Thickness of two electrodes	0.1 mm

## 122 2.2 Boundary conditions

123 Table 2 presents the boundary conditions of the simulations. The mainstream and  
124 the coolant air are assumed to be incompressible ideal gases, and the inlets of the  
125 mainstream channel and coolant chamber are set as velocity inlet boundaries. The inlet  
126 temperature values of the mainstream ( $T_\infty$ ) and the coolant air ( $T_c$ ) are given at 300 K  
127 and 200 K, respectively, and the inlet velocity of the mainstream ( $U_\infty$ ) is 20 m/s. The  
128 density ratio ( $DR$ ) of the mainstream to the coolant air is 1.5. The channel outlet is set  
129 as a pressure outlet boundary with a pressure value of 101,325 Pa. Periodic boundary  
130 conditions are applied for both sides of the mainstream channel and the coolant chamber.  
131 Adiabatic no-slip boundary condition is set on other walls.

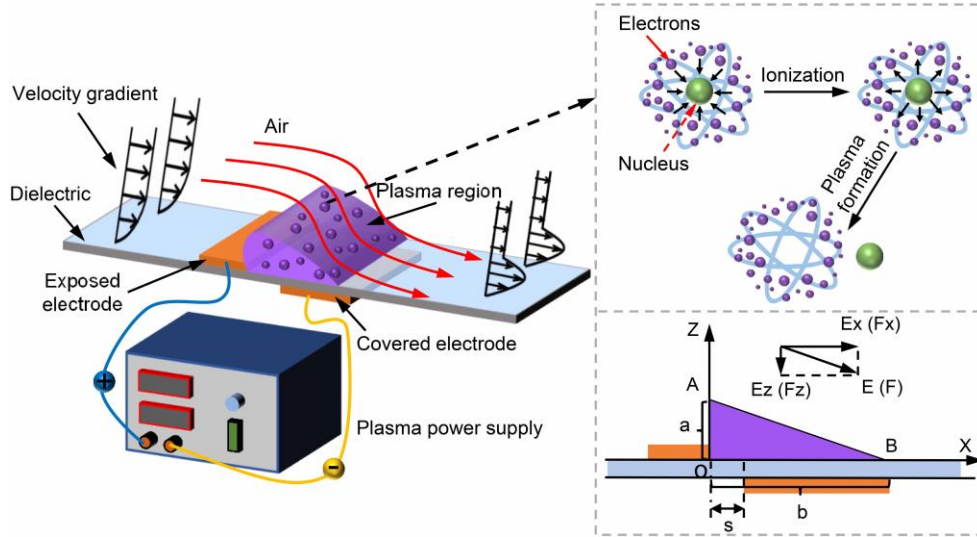
132 Table 2. Boundary conditions of simulations

Parameters	Values
Temperature of mainstream inlet ( $T_\infty$ )	300 K
Inlet velocity of mainstream ( $U_\infty$ )	20 m/s
Outlet pressure ( $P$ )	101,325 Pa
Temperature of coolant air inlet ( $T_c$ )	200 K
Density ratio ( $DR$ )	1.5
Blowing ration ( $M$ )	0.25, 0.5, 0.75, 1.0

## 133 2.3 Governing equations

134 Fig. 3 presents a schematic diagram of the plasma aerodynamic actuation. The  
135 plasma power supply generates an alternating current at high frequency and high  
136 pressure. The air molecules are ionized above the covered electrode. Outer electrons  
137 escape from the nucleus and become free electrons. The plasma consists of positive  
138 nuclei and negative free electrons. The plasma collides with surrounding air molecules  
139 to exchange momentum under the electric field, and the air above the electrode is  
140 constantly ionized [23]. The fluid shows a trend to rush towards the wall under the

141 aerodynamic actuation of the plasma actuators. The electric field intensity in the  
 142 phenomenological model is linearized by Shyy et al. [22]. The plasma is full of the  
 143 triangular region AOB in Fig. 3.



144  
 145 Fig. 3 Schematic diagram of the plasma aerodynamic actuation

146 According to Ref. [22], the electric field intensity decreases linearly along the  
 147 coordinate axis, and it is calculated by:

$$148 \quad E(X, Z) = |\vec{E}| = E_0 - k_1 X - k_2 Z \quad (1)$$

$$149 \quad k_1 = \frac{E_0 - E_b}{b} \quad (2)$$

$$150 \quad k_2 = \frac{E_0 - E_b}{a} \quad (3)$$

151 where  $E_0$  represents the ratio of applied voltage ( $\varphi_0$ ) to electrode gap ( $s$ ).  $k_1$  and  $k_2$  are  
 152 spatial distribution coefficients of the electric field intensity, which refers to the spatial  
 153 distribution gradient of the electric field intensity. In the present simulation, the  
 154 breakdown electric field intensity  $E_b$  is 30 kV/cm. The components of the electric field  
 155 in the directions  $X$  and  $Z$  are defined as:

$$156 \quad E_x(X, Z) = \frac{E(X, Z)k_2}{\sqrt{k_1^2 + k_2^2}} \quad (4)$$

157 
$$E_z(X,Z) = \frac{E(X,Z)k_1}{\sqrt{k_1^2 + k_2^2}} \quad (5)$$

158 where the body force components in the directions  $X$  and  $Z$  are given by:

159 
$$F_x = \rho_c e_c f \Delta t E_x \quad (6)$$

160 
$$F_z = \rho_c e_c f \Delta t E_z \quad (7)$$

161 there the charge density  $\rho_c$  is  $10^{17}$  C/m<sup>3</sup>, and elementary charge  $e_c$  is  $1.6 \times 10^{-19}$  C. The  
 162 applied frequency ( $f$ ) is 2 kHz, and duration of plasma actuation ( $\Delta t$ ) is 67  $\mu$ s. Other  
 163 detailed parameters can be found in Ref. [22].

164 In the book by Versteeg and Malalasekera [24] the mass conservation equation,  
 165 momentum equation, and energy equation are presented as follows:

166 
$$\frac{\partial}{\partial x_i}(\rho u_i) = S_m \quad (8)$$

167 
$$\frac{\partial}{\partial x_i}(\rho u_i u_j) = -\frac{\partial P}{\partial x_j} + \frac{\partial}{\partial x_i}(\tau_{ij} - \overline{\rho u_i u_j}) + \rho g + F_j \quad (9)$$

168 
$$\frac{\partial}{\partial x_i}(\rho c_p u_i T) = \frac{\partial}{\partial x_i}(\lambda \frac{\partial T}{\partial x_i} - \rho c_p \overline{u_i T}) + \mu \phi + S_h \quad (10)$$

169 where  $S_m$ ,  $F_j$ , and  $S_h$  are source terms in the mass, momentum, and energy equations.  $F_j$   
 170 represents the electric field force induced by the plasma actuator. As a source term of  
 171 the steady body force,  $F_j$  is added to the momentum equation through the user-defined  
 172 functions (UDFs) in the software ANSYS Fluent 18.0. The electric field strength and  
 173 the body force are stored in the user-defined memories (UDMs) for post-processing.

174 According to Goldstein et al. [25], the blowing ratio is defined by:

175 
$$M = \frac{\rho_c U_c}{\rho_\infty U_\infty} = DR \frac{U_c}{U_\infty} \quad (11)$$

176 where  $DR$  is the density ratio of coolant air to the mainstream.  $\rho$  is density, and  $U$  is  
 177 flow velocity.  $c$  represents coolant air, and  $\infty$  represents mainstream. The film cooling  
 178 effectiveness is calculated by:

$$179 \quad \eta = \frac{T_{\infty} - T_{aw}}{T_{\infty} - T_c} \quad (12)$$

180 where  $T_{\infty}$  and  $T_c$  represent the inlet temperature of mainstream and coolant air,  
 181 respectively.  $T_{aw}$  means adiabatic wall temperature. Spanwise-averaged film cooling  
 182 effectiveness ( $\bar{\eta}_s$ ) and wall-averaged film cooling effectiveness ( $\bar{\eta}_w$ ) are given by:

$$183 \quad \bar{\eta}_s = \frac{T_{\infty} - \overline{T_{s-aw}}}{T_{\infty} - T_c} \quad (13)$$

$$184 \quad \bar{\eta}_w = \frac{T_{\infty} - \overline{T_{w-aw}}}{T_{\infty} - T_c} \quad (14)$$

185 where  $\overline{T_{s-aw}}$  and  $\overline{T_{w-aw}}$  mean spanwise-averaged wall temperature and wall-averaged  
 186 temperature. Dimensionless film cooling effectiveness ( $\eta_{ratio}$ ) and dimensionless  
 187 average cooling effectiveness ( $\bar{\eta}_{ratio}$ ) are defined as:

$$188 \quad \eta_{ratio} = \frac{\bar{\eta}}{\eta_0} \quad (15)$$

$$189 \quad \bar{\eta}_{ratio} = \frac{\frac{1}{n} \sum_{i=0}^{i=n} \bar{\eta}}{\frac{1}{n} \sum_{i=0}^{i=n} \eta_0} \quad (16)$$

190 where  $\bar{\eta}_0$  is the average film cooling effectiveness, and  $i$  is the point along the  
 191 streamwise direction. The growth rate of wall-averaged cooling effectiveness is given  
 192 as:

$$193 \quad \Delta = \frac{\bar{\eta}_w - \bar{\eta}_0}{\eta_0} \times 100\% \quad (17)$$

194 The dimensionless temperature is calculated by:

195 
$$\theta = \frac{T_{aw}}{T_\infty} \quad (18)$$

196 The streamwise velocity gradient and the normal velocity gradient are expressed  
197 as:

198 
$$U^* = \frac{U}{U_\infty} \quad (19)$$

199 
$$W^* = \frac{W}{U_\infty} \quad (20)$$

200 where  $U$  and  $W$  are streamwise velocity and normal velocity of airflow, respectively.

201 To display vortices in a flow field, the equation for the  $Q$  criterion is given as [26]:

202 
$$Q = -\frac{1}{2} \left[ \left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial y} \right)^2 + \left( \frac{\partial w}{\partial z} \right)^2 \right] - \frac{\partial u}{\partial y} \frac{\partial v}{\partial x} - \frac{\partial u}{\partial z} \frac{\partial w}{\partial x} - \frac{\partial v}{\partial z} \frac{\partial w}{\partial y} \quad (21)$$

203 where  $\partial u_i / \partial x_j$  is a gradient of velocity in space. Streamwise gauge pressure and spanwise  
204 gauge pressure are calculated by:

205 
$$P_f = P_{(f,i)} - P_0 \quad (22)$$

206 
$$P_s = P_{(s,i)} - P_0 \quad (23)$$

207 where  $P_0$  is atmospheric pressure, and  $P$  is actual pressure.  $f$  is a streamwise value, and  
208  $s$  is a spanwise value.

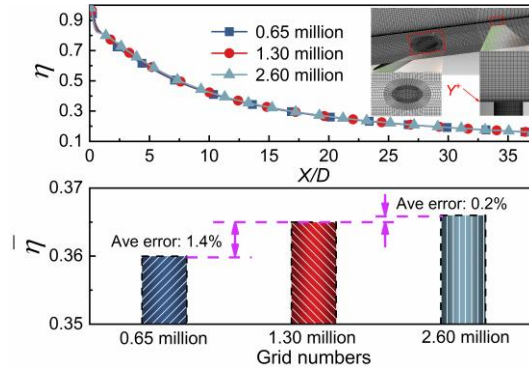
## 209 **2.4 Model validation**

210 This section conducts an analysis of grid independence and validations of the  
211 turbulence model and the plasma model.

### 212 **2.4.1 Grid independence analysis**

213 Structural grids are used to set up the computational domain. The grids near the  
214 wall and film hole are refined to capture the complex flow phenomenon in the near-  
215 wall region. The  $y^+$  value close to side walls is close to 1. With the plasma off, a minor  
216 difference in wall film cooling effectiveness is found among the cases with 0.5 million,  
217 0.65 million, 1.30 million, and 2.60 million grids. Compared with the case with 1.30

218 million grids, the average deviations of cooling effectiveness for the cases with 0.65  
 219 million and 2.60 million grids are 1.4% and 0.2%, respectively, as shown in Fig. 4.  
 220 Based on these facts, the number of 1.30 million grids is used for all simulations.

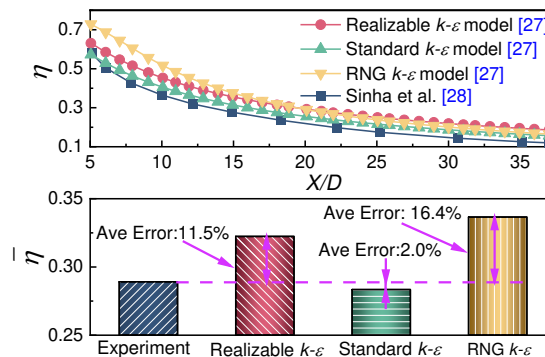


221  
 222

Fig. 4 Grid distributions near the film hole and analysis of grid independence

### 223 2.4.2 Validation of turbulence model

224 In a previous study [27], numerical results were conducted using the standard  $k-\varepsilon$   
 225 turbulence model, realizable  $k-\varepsilon$  turbulence model, and RNG  $k-\varepsilon$  turbulence model  
 226 compared to experimental results by Sinha et al. [28]. The cooling effectiveness  
 227 distributions on the wall centerlines for three turbulence models have the same trend as  
 228 reported by Sinha et al. [28]. A minimum error of 2% is observed between the standard  
 229  $k-\varepsilon$  turbulence model and experimental results as shown in Fig. 5. The errors between  
 230 other turbulence models and experimental results are above 10%. Accordingly, the  
 231 standard  $k-\varepsilon$  turbulence model is used in the present simulations.

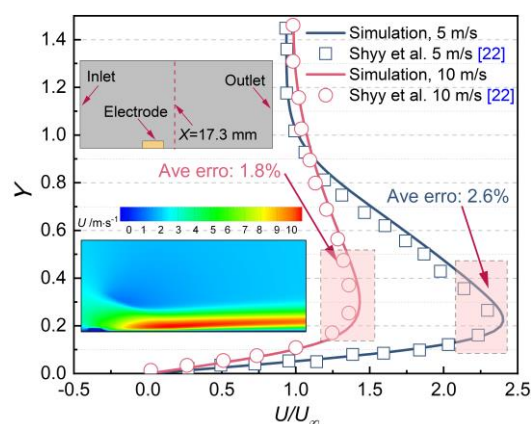


232  
 233

Fig. 5 Validation of turbulence models

### 234 2.4.3 Validation of plasma actuation model

235 The computational domain for the model validation has dimensions of 21.5 mm ×  
 236 10 mm. The plasma actuators are under an applied voltage of 4 kV and an applied  
 237 frequency of 3 kHz. Under the plasma actuation, the near-wall fluid downstream the  
 238 actuator is speeded up. Deviations between simulation results and data in Shyy et al.  
 239 [22] are 2.6% and 1.8% at inlet velocities of 5 m/s and 10 m/s, respectively, as shown  
 240 in Fig. 6. These results indicate that the plasma actuation model in the present paper is  
 241 reliable and acceptable.



243 Fig. 6 Validations of plasma actuation model at various inlet velocities

### 244 3. Results and discussion

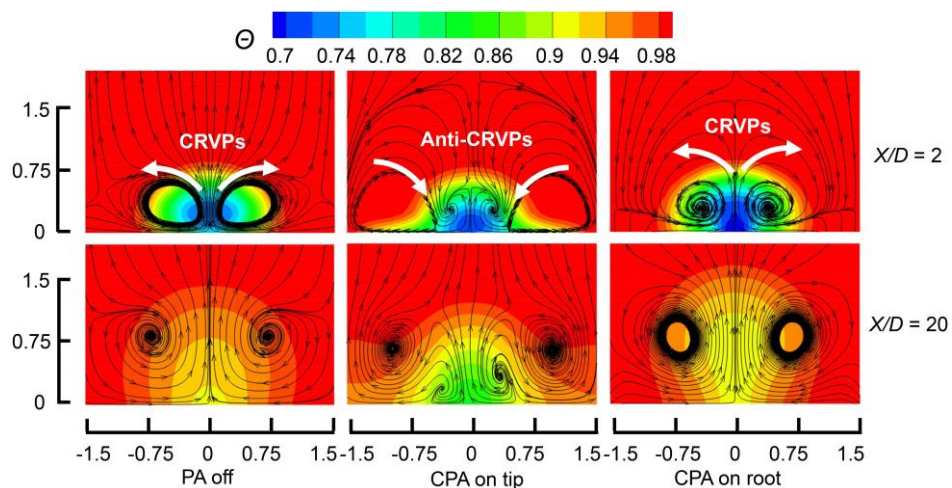
245 This section provides discussions about effects of comb plasma actuator (CPA) on  
 246 tip and CPA on root on flow field, film cooling, and pressure loss.

#### 247 3.1 Flow field characteristics

248 Fig. 7 presents dimensionless temperature distributions and streamlines at the  
 249 streamwise planes  $2D$  and  $20D$  (in direction  $x$ ). The low-temperature zone in the cross-  
 250 section is concentrated in the spanwise range from  $-0.75$  to  $0.75$ . This zone decreases  
 251 downstream the wall, and the temperature value increases under plasma off. Counter-  
 252 rotating vortex pairs (CRVPs) emerge, and the coolant air is carried away from the wall  
 253 and mixed with the high-temperature mainstream. This is the reason why the film



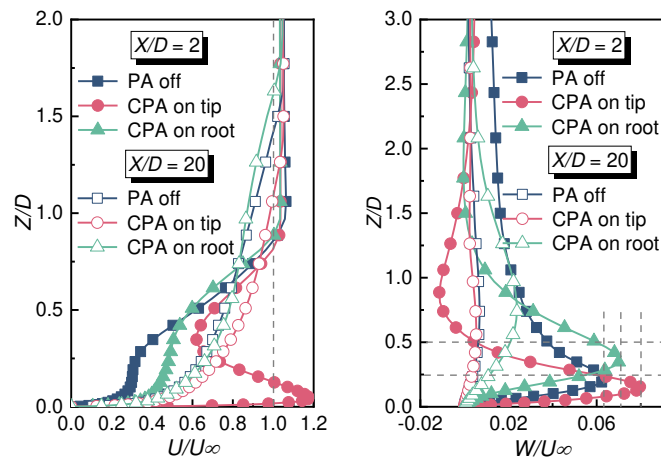
254 cooling performance is significantly weakened. The core height of CRVPs increases  
 255 along the streamwise direction, which enhances the enrolling effect of the mainstream  
 256 on the coolant air. When the CPA is applied to the tip, the low-temperature zone is  
 257 distributed in the whole spanwise direction. The low-temperature zone downstream the  
 258 wall is enlarged compared to that under plasma off. The CPA on the tip produces anti-  
 259 counter rotating vortex pairs (Anti-CRVPs), with a scale much larger than that of  
 260 CRVPs. Anti-CRVPs weaken the strength of CRVPs, and the coolant air over the wall  
 261 center diffuses to both sides. The distribution of spanwise film cooling is changed.  
 262 Compared with plasma off, the temperature in the central region is lower in the case  
 263 with the CPA on the tip. For the CPA on the root, the low-temperature zone downstream  
 264 the wall is smaller than for the other two cases. It is observed that the core height of  
 265 CRVPs for the CPA on the root is higher than that without plasma actuation. This  
 266 indicates that the shape of the plasma actuator has a significant effect on the flow field  
 267 distribution.



268 Fig. 7 Dimensionless temperature contours and streamlines at planes of  $X = 2D$  and  $20D$   
 269

270 Fig. 8 shows dimensionless streamwise velocity distributions and dimensionless  
 271 normal velocities at the streamwise planes  $2D$  and  $20D$  (in direction  $x$ ). Compared with

272 the results under plasma actuation, the velocity boundary layer and the streamwise  
 273 velocity become thicker and smaller under the plasma off. The streamwise fluid  
 274 velocity near the wall increases under plasma actuation. The maximum velocity for the  
 275 CPA on the tip is 1.2 times the mainstream velocity, which indicates that the near-wall  
 276 fluid flow accelerates due to the presence of the plasma actuator. The flow velocity for  
 277 the CPA on the root has a slight difference from that without plasma actuation. In  
 278 contrast, the flow velocity for the CPA on the tip is significantly higher than that without  
 279 plasma actuation. It is concluded that the CPA on the root shows a weak aerodynamic  
 280 actuation effect on the flow field. The velocity boundary layer for the CPA on the tip is  
 281 significantly thinner than for plasma off. The coolant air is pulled down to the wall due  
 282 to the CPA on the tip. The maximum normal velocity for the CPA on the root has the  
 283 largest height, which means the coolant air under the action of the CPA on the root  
 284 shows a solid penetration to the mainstream.



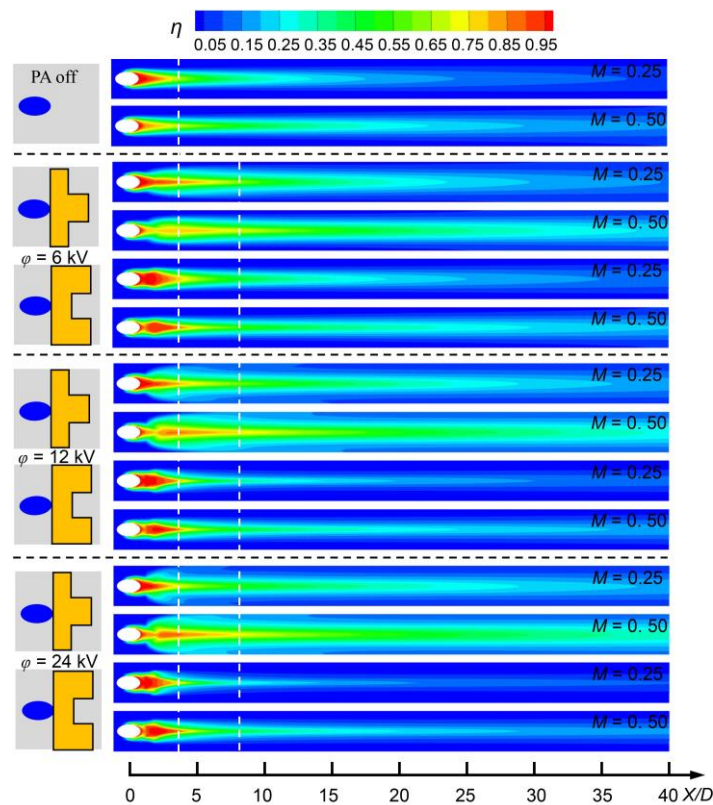
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Fig. 8 Dimensionless velocity distributions at streamwise planes of  $X = 2D$  and  $20D$

### 287 3.2 Film cooling effectiveness

288 Fig. 9 presents the film cooling effectiveness distributions under different applied  
 289 voltages at two low blowing ratios of 0.25 and 0.50. Compared with plasma off, film  
 290 cooling effectiveness with the CPA on the tip has higher lateral distributions along the  
 291 streamwise and spanwise directions. The body force for the CPA on the tip spreads the

292 coolant air across the flat plate. The film cooling effectiveness of the CPA on the root  
 293 is concentrated along the centerline close to the film hole. The body force from the CPA  
 294 on the root extends the coolant air from the wall. For the CPA on the tip at the blowing  
 295 ratio of 0.25, the widest film cooling effectiveness distribution is observed under an  
 296 applied voltage of 12 kV. The film cooling effectiveness increases with the increase of  
 297 applied voltage. A small difference under a blowing ratio of 0.50 is observed between  
 298 the cooling effectiveness distributions at applied voltages of 12 kV and 24 kV. These  
 299 results indicate that the CPA on the tip provides the best film cooling performance under  
 300 an applied voltage of 12 kV at the low blowing ratios of 0.25 and 0.50. For the CPA on  
 301 the root, the film cooling effectiveness distribution decreases along the streamwise  
 302 direction with increasing applied voltage. High cooling effectiveness is mainly  
 303 concentrated near the hole outlet, indicating that the CPA on the root improves the local  
 304 film cooling performance close to the film hole at low blowing ratios.

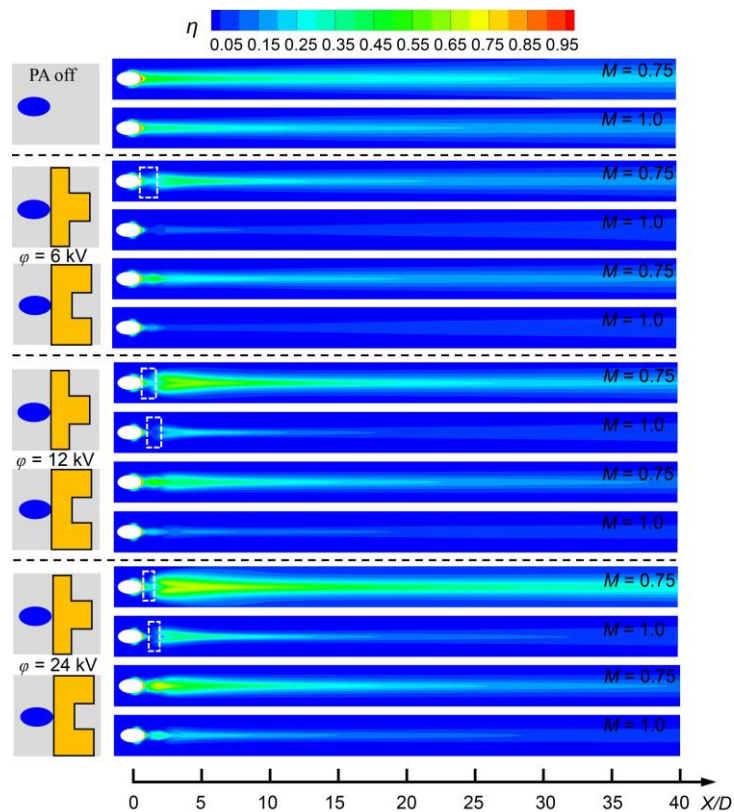


305  
 306 Fig. 9 Film cooling effectiveness distributions downstream the wall at low blowing ratios and  
 307 applied voltages of 0, 6 kV, 12 kV, and 24 kV

308 Film cooling effectiveness distributions under different applied voltages are  
309 presented at high blowing ratios of 0.75 and 1.0 in Fig. 10. With the increase of the  
310 applied voltage, the cooling effectiveness distribution for the CPA on the tip increases  
311 along the streamwise and spanwise directions. The film cooling effectiveness is  
312 improved and covers the whole wall under the blowing ratios of 0.75 and applied  
313 voltage of 24 kV. A small area with less film cooling distributions appears near the hole  
314 outlet for the CPA on the tip at blowing ratios of 0.75 and 1.0. The coolant air has a  
315 considerable outlet momentum under high blowing ratios. The body force induced by  
316 the plasma actuator effectively weakens the suction effect of the mainstream on the  
317 coolant air under a high voltage of 24 kV. This indicates that the plasma actuator has a  
318 wall-jet impact on the airflow. The cooling effectiveness distribution near the film hole  
319 (until 7.5D) for the CPA on the root is improved compared to that without plasma  
320 actuation. The film cooling downstream the wall deteriorates under high blowing ratios.  
321 The results clearly indicate that the CPA on the root is not suitable for improving the  
322 overall film cooling performance.

323 Comparisons of spanwise-averaged film cooling effectiveness are conducted  
324 under different applied voltages and are provided in Fig. 11. The spanwise-averaged  
325 cooling effectiveness for the CPA on the tip is higher than that with plasma off at low  
326 blowing ratios (such as 0.25 and 0.5). The CPA on the tip under applied voltages of 6  
327 kV, 12 kV, and 24 kV shows 1.53-1.67 times, 1.88-1.94 times, and 1.77-2.01 times film  
328 cooling effectiveness for plasma off. The flat plate obtains the best overall film cooling  
329 performance for the CPA on the tip at an applied voltage of 12 kV, but minor  
330 enhancement of cooling effectiveness is observed under the high applied voltage of 24  
331 kV. The CPA on the root is 1.16-1.27 times the cooling effectiveness for plasma off at  
332 the applied voltage of 6 kV and low blowing ratios (0.25 and 0.5). Accordingly, it is

333 proved that the CPA on the root increases the film cooling performance under low  
 334 blowing ratio and low applied voltage. The CPA on the tip at the high blowing ratios of  
 335 0.75 and 1.0 shows 0.95-1.20 times, 1.36-1.78 times, and 2.01-2.16 times the film  
 336 cooling effectiveness for the plasma off under applied voltages of 6 kV, 12 kV, and 24  
 337 kV. The increase in applied voltage enhances the aerodynamic actuation effect. Strong  
 338 aerodynamic induction effectively weakens the considerable outlet momentum of the  
 339 coolant air and the entrainment of high-temperature mainstream to the coolant air. The  
 340 film cooling downstream the wall deteriorates for the CPA on the root at high blowing  
 341 ratios. The film cooling effectiveness is significantly improved by placing the CPA on  
 342 the tip, while the CPA on the root has a poor effect on cooling performance under low  
 343 blowing ratios. The reduction of overall momentum enhances the mixing degree  
 344 between mainstream and coolant air.



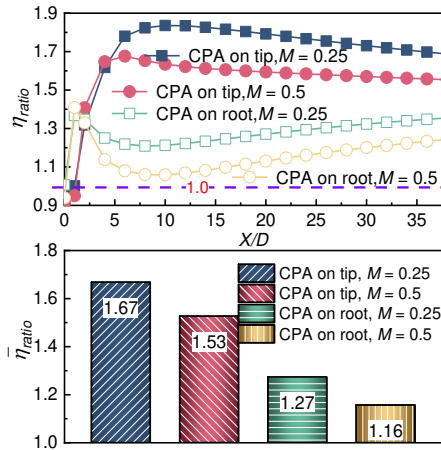
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346 Fig. 10 Film cooling effectiveness distributions downstream the wall at high blowing ratios and

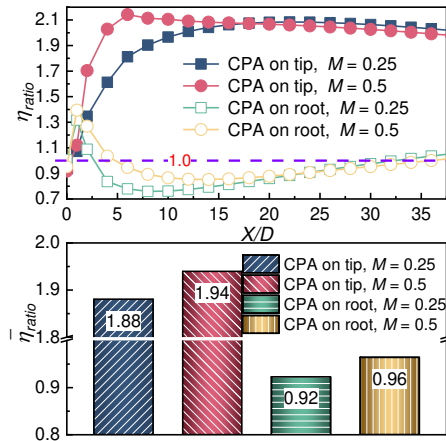
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applied voltages of 0, 6 kV, 12 kV and 24 kV

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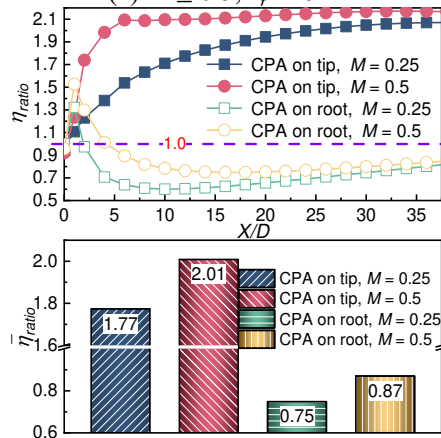


(a)  $M \leq 0.5$ ,  $\phi = 6$  kV

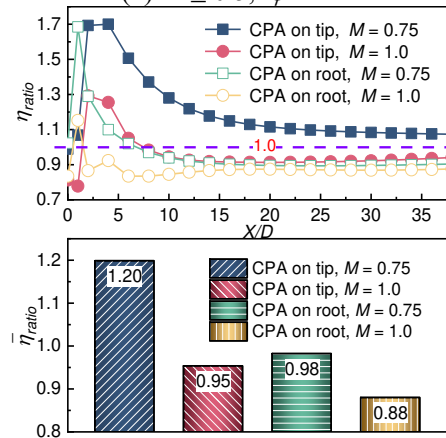


(b)  $M \leq 0.5$ ,  $\phi = 12$  kV

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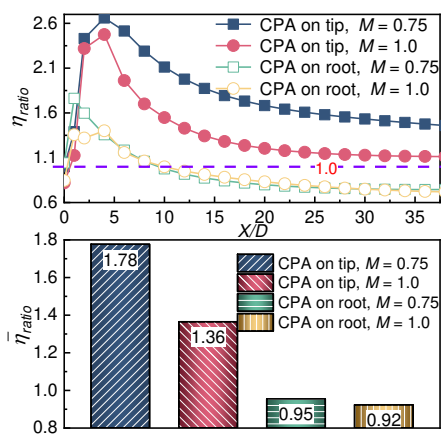


(c)  $M \leq 0.5$ ,  $\phi = 24$  kV

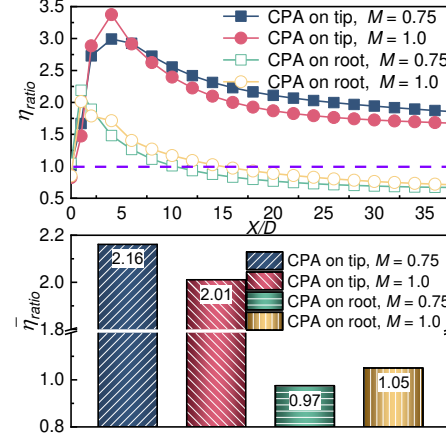


(d)  $M \geq 0.5$ ,  $\phi = 6$  kV

352  
353



(e)  $M \geq 0.5$ ,  $\phi = 12$  kV



(f)  $M \geq 0.5$ ,  $\phi = 24$  kV

354 Fig. 11 Comparisons of spanwise-averaged film cooling effectiveness at different applied voltages

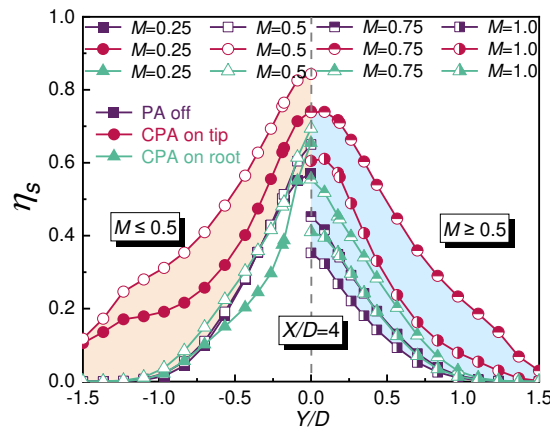
355 Fig. 12 shows spanwise film cooling effectiveness under different blowing ratios.

356 The body force for the CPA on the tip diffuses along the spanwise direction. Table 3

357 provides growth rates of average spanwise film cooling effectiveness for the CPA on

358 the tip. The average spanwise cooling effectiveness of CPA on the tip increases by

359 103.4%, 164.6%, and 150.5% at blowing ratios of 0.5, 0.75, and 1.0. The spanwise film  
 360 cooling effectiveness for the CPA on the root is higher than without plasma only at high  
 361 blowing ratios. The film cooling deteriorates under low blowing ratios, related to the  
 362 body force along the center for the CPA on the root. These results prove that the shape  
 363 of the plasma actuator significantly affects the spanwise film cooling, which provides  
 364 an approach for increasing the inlet temperature of the gas turbine.



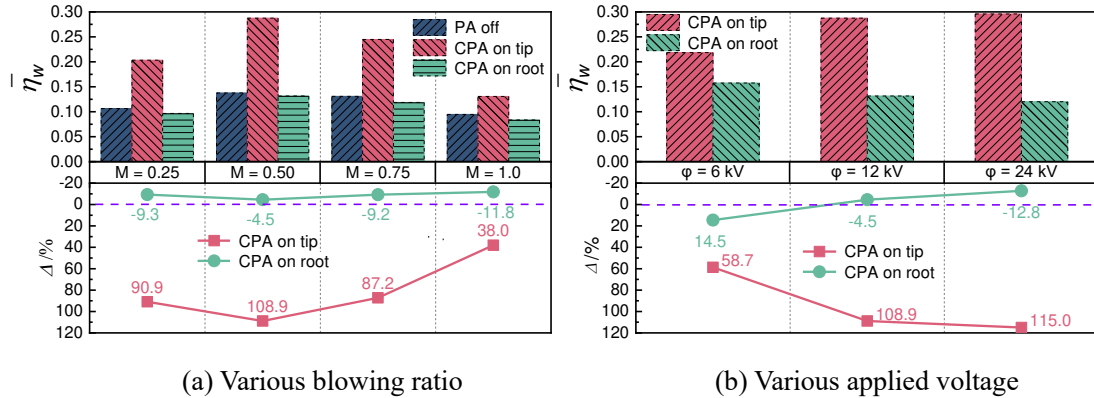
365  
 366 Fig. 12 Comparisons of spanwise film cooling effectiveness at different blowing ratios and applied  
 367 voltage of 12 kV

368 Table 3. Growth rates of average spanwise cooling effectiveness

Case	$M = 0.25$	$M = 0.5$	$M = 0.75$	$M = 1.0$
$\bar{\eta}_s$ of PA off	0.223	0.234	0.161	0.111
$\bar{\eta}_s$ of CPA on tip	0.362	0.476	0.426	0.278
$\bar{\eta}_s$ of growth rate of CPA on tip	62.3%	103.4%	164.6%	150.5%
$\bar{\eta}_s$ of CPA on root	0.188	0.243	0.218	0.157
$\bar{\eta}_s$ of growth rate of CPA on root	-15.75	3.8%	35.4%	41.4%

369 Fig. 13 shows wall-averaged film cooling effectiveness under different factors.  
 370 The arrangement of the CPA on the tip achieves the optimal performance of the overall  
 371 film cooling. Compared with plasma off under blowing ratios of 0.25 and 1.0, the wall-  
 372 averaged cooling effectiveness for the CPA on the tip increases by 38.0% and 108.8%.

373 Compared with plasma off, the cooling performance for the CPA on the root deteriorates  
 374 under all blowing ratios. For various working conditions, the film cooling effectiveness  
 375 reaches the highest values under the blowing ratio of 0.5. The wall-averaged cooling  
 376 effectiveness of the CPA on the tip increases by 58.7%, 108.8%, and 115.0% compared  
 377 to that without plasma actuation under applied voltages of 6 kV, 12 kV, and 24 kV. The  
 378 wall-averaged cooling effectiveness at the applied voltage of 12 kV is 31.6% higher  
 379 than that at 6 kV, whereas the value at 24 kV is only 2.9% higher than that at 12 kV.  
 380 These results indicate that the applied voltage has the optimal value for improving film  
 381 cooling effectiveness. With a small amount of coolant air, the best film cooling  
 382 performance of the flat wall is reached under the blowing ratio of 0.5 and the applied  
 383 voltage of 12 kV.



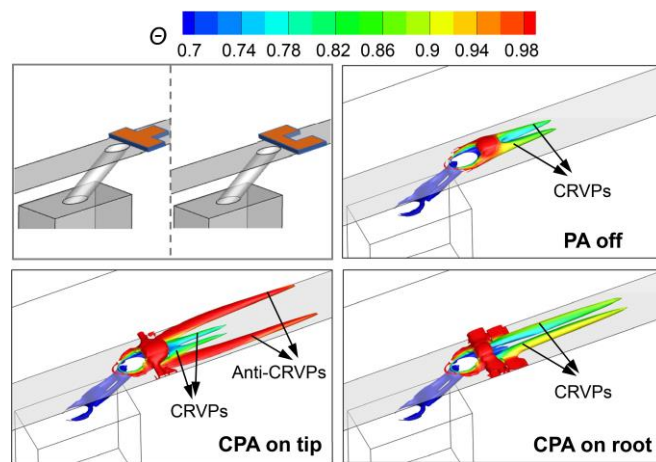
384  
385  
386 Fig. 13 Comparisons of wall-averaged film cooling effectiveness under different factors

### 387 3.3 Pressure loss

388 Three-dimensional vortex structures are displayed with dimensionless temperature  
 389 contours as shown in Fig. 14. Counter rotating vortex pairs (CRVPs) at low temperature  
 390 are presented near the hole outlet, reflecting the mixing degree of the mainstream and  
 391 the coolant air. Anti-counter rotating vortex pairs (anti-CRVPs) at high temperature are  
 392 presented on both sides downstream the hole, reflecting the disturbance effect on the



393 mainstream. The dimension of anti-CRVPs for the CPA on the tip is larger than for  
 394 CRVPs. The presence of the anti-CRVPs improves the diffusion of the coolant air from  
 395 the hole outlet to both sides, which weakens the intensity of the CRVPs. Compared with  
 396 plasma off, the dimension of CRVPs on the wall centerline for the CPA on the tip is  
 397 reduced due to plasma actuation. The vortex dimension of the CPA on the root is larger  
 398 than with plasma off, intensifying the mixing of the mainstream at high temperature  
 399 and the coolant air at low temperature.

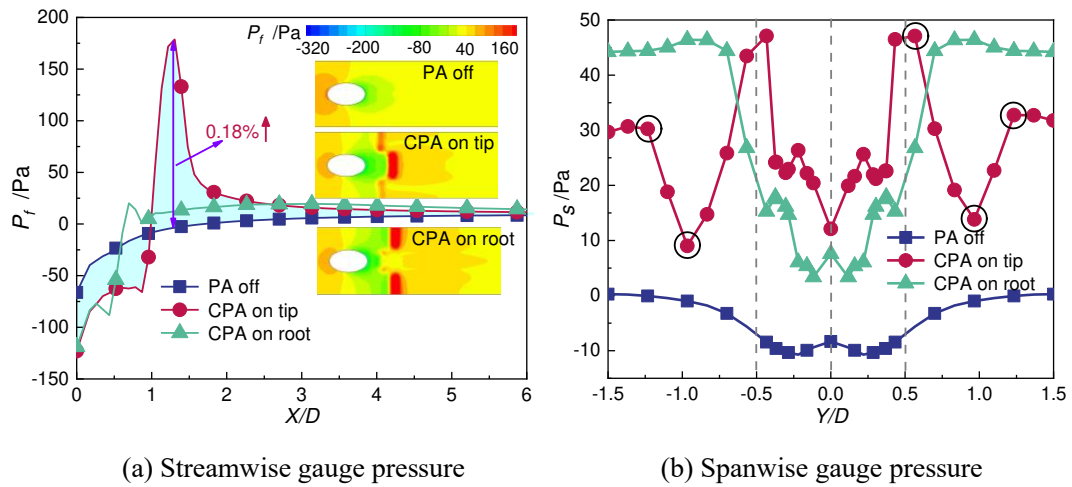


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401 Fig. 14 Three-dimensional vortex structures at blowing ratio of 0.5 and applied voltage of 12 kV  
 402 based on the  $Q$  criterion

403 Fig. 15 presents pressure distributions (gauge pressure) under a blowing ratio of  
 404 0.5 and an applied voltage of 12 kV. Streamwise pressure on the wall surface increases  
 405 dramatically under plasma actuation. The pressure for the CPA on the tip increases by  
 406 0.18% compared to that with plasma off. The airflow is forced down to the wall by the  
 407 plasma aerodynamic actuation. The streamwise pressure variation for the CPA on the  
 408 root is smaller than that for the CPA on the tip, which indicates that the CPA on the root  
 409 has less disturbance on the streamwise airflow. The spanwise pressure on the wall center  
 410 sharply decreases due to the presence of the comb plasma actuator, and the flow velocity  
 411 increases according to the Bernoulli equation. The CPA on the tip has five inflection

412 points between  $-1.5 D$  and  $1.5 D$  along the  $Y$  direction, and the pressure value is lower  
 413 than that of the CPA on the root.



414  
 415  
 416 Fig. 15 Gauge pressure distributions at blowing ratio of 0.5 and applied voltage of 12 kV

## 417 4 Conclusions

418 Effects of applied voltage and actuator shape on the flow field and film cooling  
 419 effectiveness were investigated under blowing ratios of 0.25, 0.5, 0.75, and 1.0. The  
 420 main conclusions are summarized as follows:

421 (1) For the comb plasma actuator (CPA) on the tip, the spanwise expansion of the body  
 422 force causes anti-counter rotating vortex pairs (anti-CRVPs) with a larger scale than  
 423 CRVPs. The anti-CRVPs significantly weaken the lifting effect of the mainstream  
 424 on the coolant air. The aerodynamic actuation of plasma accelerates the near-wall  
 425 fluid flow effectively. The dimension and core height of CRVPs increase due to the  
 426 agminated body force for the CPA on the root. The coolant air causes the arched  
 427 distribution, which deteriorates the film cooling.

428 (2) The CPA on the tip significantly improves the film cooling effectiveness. For the  
 429 CPA on the tip under applied voltages of 12 kV, the wall-averaged values of cooling  
 430 effectiveness are 90.9, 108.8%, 87.2%, and 38.0% higher than those without plasma

431 at blowing ratios of 0.25, 0.5, 0.75, and 1.0. Compared with plasma off, the wall-  
432 averaged values of cooling effectiveness increase by 58.7%, 108.8%, and 115.0%  
433 under applied voltages of 6 kV, 12 kV, and 24 kV. Spanwise film cooling  
434 effectiveness of CPA on tip increases from 62.3% to 164.6% under blowing ratios  
435 from 0.5 to 1.0.

436 (3) The film cooling effectiveness of the CPA on the root increases by 14.5% under 6  
437 kV applied voltage and 0.25 blowing ratio compared with plasma off. The film  
438 cooling performance is improved near the hole outlet for the CPA on the root. The  
439 wall temperature is significantly reduced by optimizing the shape of the plasma  
440 actuator.

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## 449 **References**

450 [1] Kumar R, Ismail M, Zhao W, Noori M, Yadav AR, Chen SB, Singh V, Altabey WA,  
451 Silik AIH, Kumar G, Kumar J, Balodi A (2021) Damage detection of wind turbine  
452 system based on signal processing approach: a critical review. Clean Technol.  
453 Environ. Policy 23: 561-580.

- 454 [2] Wang WJ, Tang Q, Gao B (2022) Exploration of CO<sub>2</sub> emission reduction pathways:  
455 identification of influencing factors of CO<sub>2</sub> emission and CO<sub>2</sub> emission reduction  
456 potential of power industry. *Clean Technol. Environ. Policy*. <https://doi.org/10.1007/s10098-022-02456-1>  
457
- 458 [3] Pirkandi J, Khodaparast S, Ommian M, Abbasi Y (2020) Analyzing the  
459 thermodynamic performance of a hybrid system consisting of a gas turbine and two  
460 Stirling engines in series and parallel configurations. *Clean Technol. Environ.*  
461 *Policy* 22: 1385-1403.
- 462 [4] Sun J, Zhang FX, Wang J, Baleta J, Xie GN, Sundén B (2022) Effect of dielectric  
463 barrier discharge plasma on film cooling performance. *Therm. Sci.* 26 (5B): 4157-  
464 4168.
- 465 [5] He J, Deng Q, Feng Z (2021) Film cooling performance enhancement by upstream  
466 V-shaped protrusion/dimple vortex generator. *Int. J. Heat Mass Transfer* 180:  
467 121784.
- 468 [6] Huang X, Pu J, Zhang T, Wang JH, Wu WL, Wu XY (2022) Effect of length-to-  
469 diameter ratio on film cooling and heat transfer performances of simple and  
470 compound cylindrical-holes in transverse trenches with various depths. *Int. J. Heat*  
471 *Mass Transfer* 185: 122328.
- 472 [7] Abdollahzadeh M, Páscoa JC, Oliveira PJ (2014) Modified split-potential model  
473 for modeling the effect of DBD plasma actuators in high altitude flow control. *Curr.*  
474 *Appl. Phys.* 14: 1160-1170.
- 475 [8] Rodrigues FF, Mushyam A, Pascoa JC, Trancossi M (2019) A new plasma actuator  
476 configuration for improved efficiency: the stair-shaped dielectric barrier discharge  
477 actuator. *J. Phys. D: Appl. Phys.* 52: 120317.
- 478 [9] Rodrigues FF, Pascoa JC, Trancossi M (2016) Analysis of innovative plasma  
479 actuator geometries for boundary layer control. In: *Proceedings of the ASME 2016*  
480 *international mechanical engineering congress and exposition, IMECE2016-66495*.
- 481 [10] Li GZ, Zhang HJ, Yan WW (2019) Control of the coherent structure dynamics of a  
482 film cooling flow by plasma aerodynamic actuation. *Int. J. Heat Mass Transfer* 137:  
483 434-445.

- 484 [11] Zhang X, Cui YD, Tay CMJ, Khoo BC (2021) Flow field generated by a dielectric  
485 barrier discharge plasma actuator in quiescent air at initiation stage. *Chin. J.*  
486 *Aeronaut.* 34: 13-24.
- 487 [12] Chen JL, Liao YH (2021) Effects of an annular plasma actuator on a co-flow jet  
488 downstream of a bluff-body. *Appl. Therm. Eng* 192: 116975.
- 489 [13] Harinaldi, Kesuma MD, Irwansyah R, Julian J, Satyadharma A (2020) Flow control  
490 with multi-DBD plasma actuator on a delta wing. *Evergreen: Jt. J. Novel Carbon*  
491 *Resour. Sci. Green Asia Strategy* 7: 602-608.
- 492 [14] Huang G, Dai Y, Yang C, Wu Y, Xia Y (2021) Effect of dielectric barrier discharge  
493 plasma actuator on the dynamic moment behavior of pitching airfoil at low  
494 Reynolds number. *Phys. Fluids.* 33: 043603.
- 495 [15] Zheng JG, Cui YD, Khoo BC (2019) A comparative study of alternating current  
496 and nanosecond plasma actuators in flow separation control. *Int. J. Heat Mass*  
497 *Transfer* 135: 1097-1117.
- 498 [16] Giorgi MGD, Pescini E, Marra F, Ficarella A (2016) Plasma actuator scaling down  
499 to improve its energy conversion efficiency for active flow control in modern  
500 turbojet engines compressors. *Appl. Therm. Eng* 106: 334-350.
- 501 [17] Sun J, Xie GN, Wang J, Sundén B (2022) Enhanced film cooling and flow  
502 disturbance of an AGTB turbine cascade with plasma aerodynamic actuation at  
503 film-holes outlets. *Int. Commun. Heat Mass Transfer*. [https://doi.org/10.1016/j.ich](https://doi.org/10.1016/j.ichmatmasstransfer.2022.106522)  
504 [matmasstransfer.2022.106522](https://doi.org/10.1016/j.ichmatmasstransfer.2022.106522)
- 505 [18] Dai SJ (2015) An experimental study of plasma aerodynamic actuation on a round  
506 jet in cross flow. *AIP Adv.* 5: 037143.
- 507 [19] Erfani R, Zare-Behtash H, Kontis K (2012) Plasma actuator: Influence of dielectric  
508 surface temperature. *Exp. Therm. Fluid Sci.* 42: 258-264.
- 509 [20] Li GZ, Huang YJ, Zhang HJ, Yan WW, Nie DM (2021) Numerical comparison of  
510 saw-tooth plasma actuators for film cooling flow control over a flat plate. *Int. J.*  
511 *Therm. Sci.* 163: 106807.
- 512 [21] Durscher RJ, Roy S (2012) Three-dimensional flow measurements induced from  
513 serpentine plasma actuators in quiescent air. *J. Phys. D: Appl. Phys.* 45: 035202.

- 514 [22] Shyy W, Jayaraman B, Andersson A (2002) Modeling of glow discharge-induced  
515 fluid dynamics. *J. Appl. Phys.* 92: 6434-6443.
- 516 [23] Sun J, Zhang FX, Wang J, Xie GN, Sundé B (2022) Effects of plasma actuation  
517 and hole configuration on film cooling performance. *Propul. Power Res.* <https://doi.org/10.1016/j.jprr.2022.03.005>..
- 519 [24] Versteeg HK, Malalasekera W (1995) An introduction to computational fluid  
520 dynamics: the finite volume method, first edition, Longman, London.
- 521 [25] Goldstein RJ, Eckert ERG, Bljrgcira F (1974) Effects of hole geometry and denstty  
522 on three-dimensional film cooling. *Int. J. Heat Mass Transfer* 17: 595-607.
- 523 [26] Silva CBD, Pereira JCF (2008) Invariants of the velocity-gradient, rate-of-strain,  
524 and rate-of-rotation tensors across the turbulent/nonturbulent interface in jets. *Phys.*  
525 *Fluids.* 20: 055101.
- 526 [27] Wang J, Liu C, Zhao ZM, Baleta J, Sundén B (2020) Effect and optimization of  
527 backward hole parameters on film cooling performance by Taguchi method.  
528 *Energy Convers. Manage* 214: 112809.
- 529 [28] Sinha AK, Bogard DG, Crawford ME (1991) Film-cooling effectiveness  
530 downstream of a single row of holes with variable density ratio. *Trans. ASME: J.*  
531 *Turbomachin.* 113: 442-449.
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533 **Captions of figures and tables**

534 **Fig. 1** Three-dimensional computational domain

535 **Fig. 2** Arrangements and body force distributions of comb plasma actuators

536 **Fig. 3** Schematic diagram of the plasma aerodynamic actuation

537 **Fig. 4** Grid distributions near the film hole and analysis of grid independence

538 **Fig. 5** Validation of turbulence models

539 **Fig. 6** Validations of plasma actuation model at various inlet velocities

540 **Fig. 7** Dimensionless temperature contours and streamlines at planes of  $X = 2D$  and  
541  $20D$

542 **Fig. 8** Dimensionless velocity distributions at streamwise planes of  $X = 2D$  and  $20D$

543 **Fig. 9** Film cooling effectiveness distributions downstream the wall at low blowing  
544 ratios and applied voltages of 0, 6 kV, 12 kV, and 24 kV

545 **Fig. 10** Film cooling effectiveness distributions downstream the wall at high blowing  
546 ratios and applied voltages of 0, 6 kV, 12 kV and 24 kV

547 **Fig. 11** Comparisons of spanwise-averaged film cooling effectiveness at different  
548 applied voltages

549 **Fig. 12** Comparisons of spanwise film cooling effectiveness at different blowing ratios  
550 and applied voltage of 12 kV

551 **Fig. 13** Comparisons of wall-averaged film cooling effectiveness under different  
552 factors

553 **Fig. 14** Three-dimensional vortex structures at blowing ratio of 0.5 and applied voltage  
554 of 12 kV based on the Q criterion

555 **Fig. 15** Gauge pressure distributions at blowing ratio of 0.5 and applied voltage of 12  
556 kV

557 **Table 1** Parameters of comb plasma actuators

558 **Table 2** Boundary conditions of simulations

559 **Table 3** Growth rates of average spanwise cooling effectiveness