**Research Article** 

# Investigation of temperature-dependent optical properties of TiO<sub>2</sub> using diffuse reflectance spectroscopy



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#### Abstract

Temperature-dependent diffuse reflectance spectroscopy (DRS) measurements have been carried out on the polycrystalline sample TiO<sub>2</sub>. Important values from optical parameters such as band gap ( $E_g$ ), Urbach energy ( $E_U$ ), and Urbach focus ( $E_0$ ) have been estimated in the range of 300–450 K. In order to understand the experimental value of band gap ( $E_g$ ) of TiO<sub>2</sub>, i.e., obtained from DRS, a first-principle calculation has been performed. The dependency of  $E_U$  and the slope of exponential tails ( $\beta_1$ ,  $\beta_2$ ) of the density of states has also been studied which determines the distribution of exponential tails near the valence and conduction bands in semiconducting oxides. The behavior of optical band gap and  $E_U$  has also been investigated with the influence of temperature using Cody model. From the temperature dependence of band gap measurements, the value of thermodynamical parameter such as Debye temperature ( $\theta_D$ ) has also been estimated. Thus it appears that the temperature-dependent optical absorption spectroscopy is very powerful and economical tool to probe the electronic structure near band edge and also to estimate the important thermodynamical parameter.

**Keywords** Diffuse reflectance spectroscopy · Urbach energy · DFT calculations · Temperature-dependent band gap · Debye temperature

# **1** Introduction

Optical properties of titanium dioxide (TiO<sub>2</sub>) have been the central goal of various intensive investigations over the past few years [1–3]. The major objective is to understand the behavior of optical absorption spectra with the application of temperature [4, 5]. Diffuse reflectance spectrometer (DRS) is an effective tool to understand the absorption spectra as a function of doping or temperature. The absorption spectra obtained from DRS contain three possible transitions: (1) main absorption spectra which give the information of optical gap [6, 7], (2) near absorption edge also called Urbach tail showing amount of disorder present in samples [4], and (3) lower absorption spectra which confirm the presence of defect inside the sample [8, 9]. To explore the optical absorption spectra which may be affected from various parameters like temperature, structural transition, doping, etc., an influential work has been done to shape our understanding as to how band gap and disorder varies on semiconducting materials [4, 10]. To understand how the thermal and structural components of the disorder exclusively contribute to the comprehensiveness of the optical absorption tail, Cody et al. [11] accomplished an experimental inquiry of their specific roles.

TiO<sub>2</sub> is well known for its high stability, abundance, nontoxicity, and there has been a tremendous amount of application in semiconducting devices. Keeping this view studies has already been done, extending from their synthesis and characterization to atomic scale, i.e., experimental and theoretical investigations [1–3]. Taking this into the account, our main aim in the manuscript is to understand the variation of disorder and optical band

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gap with the application of temperature via diffuse reflectance spectroscopy (DRS). According to Jalalov et al. [12], the behavior of optical absorption can also be explained by the density of electronic states.

$$\alpha(\hbar\omega) = A \int_{\varepsilon_{0-\hbar\omega}}^{\varepsilon_0} g(\varepsilon) * g(\varepsilon + \hbar\omega) |B|^2 \frac{d\varepsilon}{\hbar\omega}, \qquad (1)$$

where A is the proportionality constant which is independent of the frequency of an absorbed photon;  $\varepsilon_0$  is the energy at the node of the tails on valence and conduction bands;  $|B|^2$  is the dispersion of the matrix element for the electronic transitions; and  $g(\varepsilon)$  and  $g(\varepsilon + \hbar \omega)$  are the distributions of the DOS consistent of initial and final states of electrons involved in optical transitions during absorption of photons with energy  $\hbar \omega$ . For the disordered system, an exponential tail behavior has been seen in the density of states near to valance and conduction edge. Temperature is one of the important constraints which play a key role in producing thermal disorder in semiconducting oxides. The decrease in band gap on semiconducting materials is observed with increasing temperature, and it is expected in general as per the Varshni's [13] relation as follows:

$$E_{\rm q} = E_{\rm q(0)} - \gamma T^2 / (T + \beta), \tag{2}$$

where  $E_g$  is the energy gap which may be direct  $(E_{gd})$  or indirect  $(E_{gi})$ ,  $E_{g(0)}$  is the energy gap at 0 K, and  $\gamma$  and  $\beta$  are constants. It is proposed that the fitting parameter  $\beta$  in Eq. 2 is related to the Debye temperature  $(\theta_D)$  [14] as:

$$\beta = \begin{bmatrix} 3/8 \end{bmatrix}_D. \tag{3}$$

In this case, it is found that  $\beta = \theta/2$  where  $\theta$  is the effective Einstein vibrational frequency in temperature units of the phonon spectrum in the material.

Optical spectroscopy is a tool which can tell about not only the optical band gap of semiconducting materials but also the disorder in the form of Urbach energy as well as various defects [8] present in semiconducting materials. Keeping this in view, here we have performed temperature-dependent DRS and report its dependency on optical band gap [4], Urbach energy [10], and Urbach focus on TiO<sub>2</sub> [1, 15, 16]. It is observed that Urbach energy shows opposite behavior from band gap, i.e., with the increase in temperature optical band gap decreases while due to change in optical spectra near absorption tail edge leads to increase disorder present in sample [4]. It is clear from the experimental evidence that Urbach–Martienssen [17, 18] (U–M) tails in the optical absorption spectra showing the variation of disorder produced with the application of temperature as well as variations of band gap with Urbach energy have also been investigated.

## 2 Experimental and theoretical details

#### 2.1 Structural characterizations

Commercial anatase  $TiO_2$  powder of Alfa Aesar with purity 99.999% has been used for characterization. In order to examine the structural phase purity, X-ray diffraction (XRD) experiment has been carried out on Bruker D8 diffractometer equipped with Cu target having LynxEye detector [6, 19–21]. The high-temperature X-ray diffraction measurements were performed to confirm the structural phase transition in the prepared samples. Jobin–Yvon Horiba micro-Raman spectrometer was used for Raman measurements. The micro-Raman spectrometer consists of an argon ion laser as light source.

# 2.2 Temperature-dependent diffuse reflectance spectroscopy (DRS) measurement

The optical band gap of prepared sample has been measured by using DRS measurements [6–8]. These measurements have been taken in the 200–800 nm wavelength range using Cary-60 UV–Vis–NIR spectrophotometer having Harrick Video-Barrelino diffuse reflectance probe in the temperature range of 300–450 K [22].

#### 2.3 Theoretical methods

The first-principles calculations are executed using FP-LAPW [23] approach and implemented in WIEN2k code [8, 24, 25]. The Kohn–Sham equations [26, 27] were solved self-consistently using FP-LAPW method. The generalized gradient approximation (GGA + U) has been used for DFT calculation. In the present studies, we have used structural parameters from experimental X-ray diffraction analysis (experimental data). Keeping this in view, we have not used lattice relaxation for calculation. We have taken generalized gradient approximation (GGA + U) as an exchange–correlation potential with U=5 eV. During calculations, we have used  $R_{MT}K_{max} = 7$ , where  $K_{max}$  is the plane wave cutoff and  $R_{MT}$  is the minimum of all atomic sphere radii (Muffin-tin radii). We have sensibly selected the muffin-tin radii (MT) 1.93 and 1.74 a.u. for Ti and O, respectively. When the total energy of given structure is stable within 10<sup>-3</sup> mRy, it is believed that the self-consistent calculations are converged. The k-mesh size of  $5 \times 5 \times 3$ has been used in calculation.



**Fig. 1** a X-ray diffraction of anatase TiO<sub>2</sub>; indexing has been done using JCPDS No. 00-021-1272. No extra plane in diffraction pattern confirms phase purity. **b** Raman analysis of anatase (A) phase TiO<sub>2</sub> with space group I4<sub>1</sub>/amd

# **3** Results and discussion

#### 3.1 Structural characterization and phase purity

Figure 1a shows the powder X-ray diffraction pattern for the prepared sample. The obtained X-ray diffraction data are indexed considering the space group  $I4_1$ /amd, and no impurity peaks are observed, which confirms the structural phase purity of the prepared sample. Further Raman spectra of anatase TiO<sub>2</sub> have been recorded which is shown in Fig. 1b. It is clear from Raman spectra that  $B_{1g}$ ,  $A_{1g}$ , and  $E_{g}$ modes confirm the presence of anatase phase with space group  $I4_1$ /amd.

#### 3.2 Diffuse reflectance spectroscopy (DRS)

We have investigated the optical absorption spectra for TiO<sub>2</sub> using DRS technique. The spectra acquired from DRS enlightened through Kubelka–Munk [28, 29] equation.

$$F(R_{\infty}) = \frac{(1 - R_{\infty})^2}{2R_{\infty}},$$
(4)

where  $F(R_{\infty})$  is the Kubelka–Munk function. Expression of Kubelka–Munk function can be written as:

$$F(R_{\infty}) \propto \alpha \propto \frac{(h\nu - E_{\rm g})^{1/n}}{h\nu},$$
 (5)

In order to estimate the  $E_{g}$ , the obtained absorption coefficient is altered into Tauc equation [30, 31] and plotted in Fig. 2.

$$(\alpha h\nu)^n = A(h\nu - E_g), \tag{6}$$



Fig. 2 Tauc plot to determine the band gap of TiO<sub>2</sub> at 300 K

Here in Eq. 6 we have used the values of n = 1/2 for an indirect transition [4, 7, 10] to determine the optical gap of TiO<sub>2</sub> as it is proposed to be an indirect band gap material. Using Tauc fitting [30], we have obtained experimental bandgap of TiO<sub>2</sub> is 3.21 eV.

#### 3.2.1 First-principle investigation (DFT calculations)

To confirm the type (direct or indirect) of band gap present in anatase TiO<sub>2</sub>, we have performed DFT calculations, and from band structure, it is clear that anatase phase of TiO<sub>2</sub> shows indirect band gap of 3.21 eV shown in Fig. 3. As DRS shows experimental optical band gap  $E_g$ =3.21 eV, to confirm this, we have performed first-principle calculations using WIEN2k code with GGA + U (U=5 eV). We have taken experimental structural parameters and used them



**Fig. 3** Band structures of TiO<sub>2</sub> using GGA + U (U = 5 eV) calculations showing indirect band gap of 3.21 eV



Fig. 4 Total and partial density of states for  $TiO_2$  shows gap between valance band maxima (VBM) and conduction band minima (CBM) of 3.21 eV

directly for the band gap calculations. As per calculated experimental band gap, which is around 3.21 eV, and to match this value of band gap, we have taken U = 5 eV. For a real system, the value of Coulombic interaction (U) is generally avoided in case of GGA calculation (i.e., U = 0), and hence, the value of experimental band gap of the real system does not match. However, in terms of GGA + U, the value of Coulombic interaction also tells about the behavior of a real system. Figure 4 shows partial density of states (PDOS) of TiO<sub>2</sub> showing gap between valance band maxima (VBM) and conduction band minima (CBM) of 3.21 eV, i.e., band gap ( $E_g$ ), which matches with experimental DRS results. In case of pure



**Fig. 5** Varshni's fitting of anatase phase of  $TiO_2$ . Inset shows plot between Kubelka–Munk function and energy of  $TiO_2$  sample at various temperatures (300–450 K)

 $TiO_{2^{\prime}}$  the states near Fermi level are dominated by the O-2p and Ti-3d orbitals.

#### 3.2.2 Temperature-dependent band gap

The optical band gap of semiconductors tends to decrease as the increased in temperature [4, 13]. Figure 5 shows the variation of band gap as a function of temperature. From Fig. 5, it is clear that with the increase in the temperature the band gap of TiO<sub>2</sub> systematically decreases and consistent with earlier reports [1]. We have fitted experimental data with Varshni's relation [13, 32, 33] Using this relation, one can estimate the values of fitting parameters y and  $\beta$  which are functions of thermodynamical quantity like Debye temperature [14, 34]. Inset of Fig. 5 shows the variation of optical spectra (Kubelka-Munk plot) at different temperatures 300-450 K. A relationship between  $\beta$  and  $\theta_{\rm D}$  has been discussed by Manoogian et al. [14, 34] using Varshni's relation. In the intermediate temperature region, the Einstein temperature  $\theta_{\rm F}$  is related to the Debye temperature  $\theta_D$  and  $\beta$  by the relation of  $\theta_E = (3/4)\theta_D$ [14, 34] and  $\beta = \theta_{\rm E}/2$ , respectively. Hence, it is clear that the Varshni's parameter ( $\beta$ ) is related to Debye temperature ( $\theta_D$ ) as follows:  $\beta = (3/8) \theta_D$  [14]. Debye temperature  $(\theta_D) = (8/3)\beta \approx 562$  K, (where  $\beta = 211$  K obtained from fitting).

According to Shojaee et al. [35], Debye temperature of TiO<sub>2</sub> is around 557 K, while using Varshni's fitting obtained from optical spectroscopy, Debye temperature has been found to be very close to reported value [36], which is around 562 K. Hence it is clear that temperature-dependent DRS provide not only the variation in optical properties

but a tool to estimate the thermodynamic properties like Debye temperature.

#### 3.2.3 Determination of band tail width (Urbach energy)

In semiconductors, the fundamental absorption edge below the energy band gap increases exponentially, and the absorption edge is known as the Urbach tail. To understand the behavior of Urbach tails in semiconducting materials, various extensive investigations have already been done over the past few decades. Intensive investigation has been done in studies, i.e., phonons [37, 38], impurities [39], excitons [15], and structural disorders [4], which are associated with the observed exponential tails in optical spectra. Urbach energy ( $E_U$ ) provides the information about the total disorder present in the sample [1, 39–42]. The contributions to the said energy may be due to various types of disorders such as thermal, polar, chemical, and structural defects.

$$F(R) \approx \alpha(E,T) = \alpha_0 \exp\left(\left(E - E_0\right) / E_U\right). \tag{7}$$

In order to find the value of  $E_U$ , we have taken the natural logarithm of F(R) with respect to provided photon energy. After taking natural logarithm of F(R), we will get a straight-line equation which is as follows:

$$\ln \alpha = \ln \alpha_0 + \left[ \left( \left( E - E_0 \right) / E_U \right) \right], \tag{8}$$

and the obtained equation is compared with equation of straight line

$$y = mx + c, \tag{9}$$

where Urbach energy ( $E_U$ ) is equivalent to the inverse of slope of above equation [4, 10]. The distribution of the density of localized states in the tails of the valence and conduction bands has exponential energy dependence [12]:

$$g(\epsilon_{\rm v}) = N(\epsilon_{\rm v}) \exp\left(-\beta_1(\epsilon - \epsilon_{\rm v})\right),\tag{10}$$

$$g(\varepsilon_{\rm c}) = N(\varepsilon_{\rm c}) \exp(-\beta_2(\varepsilon - \varepsilon_{\rm c})), \qquad (11)$$

where  $\beta_1$  and  $\beta_2$  are parameters controlling the slope of an exponential tails of the valence and conduction bands.  $g(\epsilon_v)$  and  $g(\epsilon_c)$  represents as a density of states, and  $N(\epsilon_v)$ and  $N(\epsilon_c)$  are no. of atoms in valence and conduction bands respectively.

According to Jalalov et al. [12], Urbach energy is inversely proportional to the slope of an exponential tail of valance and conduction bands, i.e.,  $\beta_1$  and  $\beta_2$ . Keeping this in view, partial density of states (PDOS) has been calculated to see the variation of conduction band and valance band near Fermi energy using experimental structure parameters.



**Fig. 6 a** Fitting of valence band (obtained from theoretical calculations) at exponential tail of density of states near Fermi energy (valence band tail). **b** fitting of conduction band (obtained from theoretical calculations) at exponential tail of density of states near Fermi energy (conduction band tail)

From room-temperature DRS measurement, the presence of disorder in system has been observed from various reports. Hence, it is quite possible to get exponential tail from theoretical model also. Figure 6a shows fitting of valence band decay for density of states near Fermi energy (valence band tail), and Fig. 6b shows fitting of conduction band decay for density of states near Fermi energy (conduction band tail). Interestingly, it is found that the value of inverse of  $\beta_1$  and  $\beta_2$  has been found in the range of meV which clearly indicates that the Urbach energy is inversely proportional to the slope of an exponential tail of valance and conduction bands. Figure 7 shows a schematic diagram with density of states and photon Energy, and it is clearly seen that disorder states (tail state) arise in between valance bands (VB) and conduction bands (CB). The change in the band gaps with increasing

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**Fig. 7** Diagram between density of states and photon energy, and it is clearly seen that disorder states (tail state) arise in between valance and conduction bands.  $T_1$ ,  $T_2$ , and  $T_3$  represents as transition at various temperatures

temperature can be described by the effect of lattice vibrations on the energy levels in given system. The temperature dependence of the band gap is determined by the density of states [12, 43] of the conduction band and valence band of the semiconductor. Due to the thermal broadening [44] of the density of states near the bottom of the conduction band and valence band reduces the band gap. The temperature dependence of the forbidden states of vibrational level may get allowed near CB and VB, and hence the density of states in the areas of constant edge of the conduction band and valence band has a stepped shape (shown in Fig. 7), i.e., allowed vibrational states near CB and VB for various temperatures like  $T_1$ ,  $T_2$ ,  $T_3$ , etc.

The reciprocal of the slope of the obtained straight lines leads to determination of the Urbach energy  $E_{\rm U}$ . It is observed that, the values of  $E_{11}$  in TiO<sub>2</sub> were increased from ~100 to 220 meV with temperature range 300-450 K. Increasing  $E_U$  with the application of temperature leads to increase in the disorder present in the sample. The disorder can introduce localized states at the conduction band maxima and valance band minima, which leads to increase the band tail width E<sub>U</sub>. Kranjčec et al. [45] calculated disorder free energy, i.e., Urbach focus  $(E_0)$  and observed that at the structural phase transition the value of the  $E_0$  changes. The  $E_0$  is predicated to be the material constant related to the absorption edge in the absence of any type of disorder in the sample [11, 46]. The detailed discussion on the origin of the  $E_0$  is given by Guerra et al. [47]. Figure 8 shows variation of Urbach energy with the application of temperature with range 300–450 K. The value of Urbach focus [4] represents the disorder free energy (i.e. band gap at 0 K) and shown in the inset of Fig. 8. It is well known that the Urbach energy in solids is used to determine not only thermal disorder, but also structural and compositional disorders in



Fig. 8 Variations in Urbach energy at various temperature ranges (300–450 K) for TiO<sub>2</sub>. Inset of shows Urbach focus across anatase phase of TiO<sub>2</sub>

semiconducting oxides like TiO<sub>2</sub>. Figure 9 shows the linear variation in between band gap and Urbach energy with the application of temperature as suggested by Cody model [11]. According to Cody et al. [11], it is found that band gap  $(E_g)$  and Urbach energy  $(E_u)$  show linear behavior which is as expressed:

$$E_{\rm g}(T,X) = E_{\rm g}(0,0) - \langle \Delta^2 \rangle_0 D \left[ \frac{E_{\rm U}(T,X)}{E_{\rm U}(0,0)} - 1 \right], \tag{12}$$

where  $E_g(0, 0)$  and  $E_U(0, 0)$  are the values of band gap and Urbach energy in a defect-free crystal at 0 K,  $< \Delta^2 >_0$  the zero-point uncertainty [11, 43, 48] in the atomic positions and from fitting the value of the displacement is around



Fig. 9 Plot between  $E_{\rm g}$  and  $E_{\rm U}$  using Cody's model at various temperature ranges (310–450 K)

0.05 Å<sup>2</sup>. It is also important to understand the importance of zero-point uncertainty in the atomic positions, and each real system represents harmonic oscillator model. Using harmonic oscillator, it is easy to estimate minimum oscillator energy (ground vibrational state) [49, 50] as well as  $< \Delta^2 >_0$  as follows:

$$E = \frac{\hbar^2}{8m_{\rm osc}} < \Delta^2 >_0 + \frac{m_{\rm osc}\omega^2 < \Delta^2 >_0}{2'}$$
(13)

Derivative of Eq. 13 will give minimum energy of the oscillator at a particular value of  $\langle \Delta^2 \rangle_0$  is

$$\hbar^2 / 4m_{\rm osc} < \Delta^3 >_0 + m_{\rm osc} \omega^2 < \Delta >_0 = 0,$$
 (14)

$$<\Delta^2>_0=\frac{\hbar^2}{2m_{\rm osc}}\omega$$
(15)

 $E_0 = \hbar \omega / 2, \tag{16}$ 

where  $\hbar = \text{Plank}$  constant,  $m_{\text{osc}} = \text{mass}$  of oscillator,  $< \Delta^2 >_0 = \text{zero-point}$  uncertainty in the atomic position [11],  $E_0 = \text{minimum}$  energy of oscillator and  $\omega$  represents oscillating frequency. Here, D represents the secondorder deformation potential [48], and this has been approximated  $\pm 0.3$  Rydberg/Å<sup>2</sup> (or 4.08 eV/Å<sup>2</sup>) [11]. At zero thermal energy (T = 0 K), the value is nearly zero, and with increase in thermal vibration, the crystal may get deformed. Here  $< \Delta^2 >_0 D$  shows deformation energy [43] which may arise due to the uncertainty of atomic positions (lattice mismatch).

### 4 Conclusion

In summary, the variation of band gap  ${}^{\prime}E_{g}{}^{\prime}$  and Urbach energy  ${}^{\prime}E_{U}{}^{\prime}$  as a function of temperature has been extensively studied. From GGA + U calculations from PDOS, it is clear that the change in behavior of valence band maxima and conduction band minima is due to the overlapping of O-2p (VBM) with Ti-3d (CBM) orbitals, which can vary as disorder increases in sample. Dependency of Urbach energy and the slope of exponential tails ( $\beta_1$ ,  $\beta_2$ ) in density of states have also been studied. In the present investigation, diffuse reflectance spectroscopy used as tools to see the behavior of optical band gap with the influence of temperature and which helps to estimate the thermodynamic parameter like Debye temperature.

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#### **Compliance with ethical standards**

**Conflict of interest** The authors declare that they have no conflict of interest.

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