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Investigation of Tolerable Laser Linewidth for Different Modulation Formats in CO-OFDM Systems

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Abstract

The ideal behavior of communication system requires a single frequency carrier. In optical communication system, light is used as a carrier. Practical laser source has a finite linewidth due to variations in the frequency of operation, hence, resulting in undesired phase perturbations in the signal whereas the ideal requirement is the delta function spectral shape at the carrier frequency. The spectral shape gets broadened due to phase noise and is modeled as lorentzian shape. Linewidth is a measure of stability of laser phase noise with time. Coherent Optical Orthogonal frequency division multiplexing (CO-OFDM) along with the spectrally efficient Quadrature Amplitude Modulation (QAM) formats is emerging as one of the best solutions for future high speed fiber transmission systems. Though the coherent, receivers have advantages in terms of sensitivity and selectivity, laser phase noise is the main limitation of such systems as the laser phase noise further causes common phase rotation of all the subcarriers per symbol and also results in inter carrier interference. QAM formats are also susceptible to laser phase noise. Phase noise in coherent systems is governed by laser linewidth. Hence, it is very important to investigate the impact of laser linewidth in CO-OFDM systems. This paper investigates the tolerable laser linewidths for different QAM formats in a 40 Gbps COOFDM system.

1. Introduction

With the tremendous increase in internet usage along with the requirement of high bandwidth applications, high speed and long haul optical communication systems are in great demand. This has compelled the researchers in the related

area to take advantage of multicarrier transmission schemes along with the coherent detection and digital signal processing. Latest technological advancements in microelectronics such as high speed digital signal processors, analog to digital converters and digital to analog converters have made possible the use of digital signal processing in communication systems. This has further led to the development of software defined optical transmission [1]. A number of channel impairments such as chromatic dispersion, phase noise etc. can be mitigated effectively by employing DSP at the receiver or transmitter.

OFDM, a multicarrier transmission scheme is preferred choice for high speed optical communications as it is efficiently implemented using Inverse Fast Fourier Transform (IFFT) and is robust against various channel impairments. Intensity modulation and linear field modulation are the two variants of optical OFDM systems. Coherent detection is used for linear field modulation and direct detection is used for intensity modulation.

Direct Detection optical OFDM system finds applications in inexpensive short haul communication as there is lesser number of components at transmitter and receiver side as compared to coherent optical OFDM. However, there is requirement of frequency spacing between the optical carrier and OFDM band so as to avoid intermodulation distortion present in the diode. On the other hand, CO-OFDM is suitable for high speed long haul optical communication system [2]. High performance of CO-OFDM system requires narrow linewidth transmitter and local oscillator lasers along with the DSP algorithms for phase and frequency estimation at the receiver. Therefore, the hardware and cost involved are more. Digital phase estimation, computationally efficient FFT and IFFT, adaptive data rates due to software defined QAM constellations are the major advantages offered by COOFDM systems [1]. The software defined capability in COOFDM system presents numerous advantages in terms of different modulation formats for different subcarriers, mitigation of various imperfections such as laser drift, channel dispersion, optimization of various OFDM system parameters by monitoring of transmission channel characteristics. Due to these reasons, coherent detection is the most suitable choice for high-speed, high-spectral efficiency, dynamically reconfigurable optical networks suitable for long-distance transmission. By recovering the electric field in the two fiber polarizations, a coherent receiver allows information symbols to be encoded in all the degrees of freedom available in a fiber, leading to improved power and spectral efficiency [3].

Laser linewidth is defined as the width of the power spectral density of the emitted electric field. It is measured in the units of frequency, wavenumber or wavelength. It is typically the full width at half maximum. Coherent detection, OFDM and QAM are all susceptible to phase noise. The phase noise is characterized by laser linewidth. The phase noise results in phase rotation of all the subcarriers and hence leads to inter carrier interference which further results in loss of orthogonality [4]. Narrow linewidth lasers (nearly few kHz) removes the degradation caused by phase noise. QAM modulation formats are very sensitive to the phase of the received symbol. Hence it is necessary to investigate the beha-

vior in terms of Laser linewidth for a COOFDM system.

In this paper five different modulation formats are investigated 4-QAM, 16-QAM, Circular 4-QAM, Circular 16-QAM and optimized C16-QAM. As the order of modulation format increases, the phase noise affects the system performance more because the number of distinct phases to be identified is more as the order of modulation format is increased. One possible solution to resolve the issue of linewidth is by using a pilot tone having sufficient guard bandwidth so that the phase difference between transmitter's laser and local oscillator's laser can be detected [5]. Other methods include pilot aided phase noise compensation techniques.

The linewidth of the lasers used as well as the capability of the DSP to recover the constellation at extremely low SNR will further limit what constellation type that can be used in practice. The higher the order of the modulation format, the harder it is to perform phase tracking which put constraints on the linewidth of the lasers [6]. This paper investigates the phase noise effects arising from finite transmitter and local oscillator linewidth. The performance is investigated in terms of Symbol Error Rate as the laser linewidth varies at different OSNRs. From the graphs drawn, the values of tolerable linewidths for various modulation formats at different OSNRs are obtained for a target SER of 1e−3.

2. Theoretical Details

Mathematical model of a COOFDM system is given by [7]

$$y_{ik} = x_{ik} h_k e^{j\varnothing_i^c} + \in_{ik} + n_{ik} \tag{1}$$

$$e^{j\varnothing_i^c} \triangleq \frac{1}{N_{sc}} \sum_n e^{j\varnothing(n)} \tag{2}$$

x_{ik} and y_{ik} are the mQAM modulated data of the kth subcarrier in i^{th} OFDM symbol before and after transmission, h_k is the transmission channel impulse response at k^{th} subcarrier, n_{ik} is the complex white gaussian noise, $\in_{ik}$ is the intercarrier interference, $\varnothing_i^c$ represents the common phase error cause by laser phase drift or phase noise during optical fiber transmission, $\varnothing(n)$ is the laser phase noise.

The laser phase noise $\varnothing(n)$ is modeled as a random-walk process where $\varnothing_i's$ are independent, identically distributed Gaussian random variables with zero mean and variance (σ^2) given by

$$\sigma^2 = 2\pi\Delta f T_s \tag{3}$$

where Δf is the combined laser linewidth and T_s is the symbol period. The two main techniques to combat phase noise are Pilot aided phase noise compensation technique and RF pilot tone based phase noise compensation technique.

3. Details of Simulation Set up

The block diagram of simulation set up is shown in Figure 1. An OFDM signal with a data rate of 40 Gb/s is generated from a pseudorandom binary sequence (PRBS) generator.
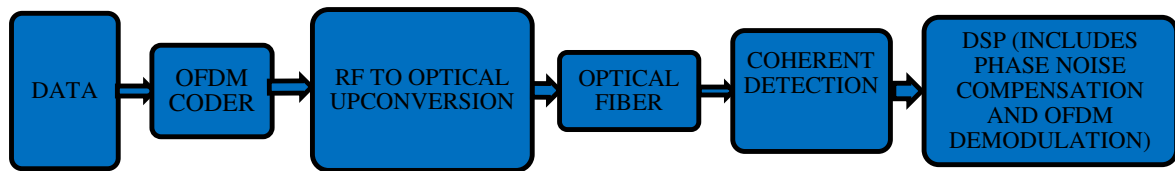
Figure 1. Block diagram of coherent optical communication system.

OFDM coder generates the electrical OFDM signal. The steps involved in OFDM coder are serial to parallel conversion, mapping, training symbols insertion, pilot carrier insertion, IFFT. An IFFT/FFT size of 128 is used. A Cyclic Prefix having 6.5% of the symbol length is added. A laser with 100 kHz linewidth is used to generate a continuous signal at 193.1 THz. This is modulated with the OFDM signal in a null-biased IQ-Mach Zehnder Modulator (MZM) for CO-OFDM, an MZM up-convert the electrical OFDM signal into optical domain.

Optical Signal is then transmitted through a single mode fiber of length 3200 km. Dispersion compensation is done in optical domain.

Coherent Detection at the receiver is carried out by two to four Quadrature Optical Hybrid. It combines the received optical signal and a local oscillator reference signal to generate four optical signals with a 90 degrees phase difference. Hence the in phase and quadrature components of RF baseband signal are obtained. After that DSP is applied to the I/Q components. The steps performed includes phase noise compensation, Cyclic prefix removal, Serial to parallel conversion, FFT, QAM demapping and finally parallel to serial conversion so as to retrieve the original data.

RF Pilot Tone based laser phase noise followed by pilot based equalization is used to remove the laser phase noise effects [8] in which RF pilot is added at the middle of OFDM band and subsequently used at the receiver to reverse the phase noise impairments. The residual phase noise left due to RF pilot getting distorted by OFDM subcarriers is removed by pilot carriers.

4. Results and Discussion

To use the bandwidth efficiently advanced and spectrally efficient modulation formats are used. In this paper, modulation formats used are Rectangular 4-QAM, Rectangular 16-QAM, Circular 4-QAM, Circular 16-QAM and optimized C-16 QAM. Circular-QAM schemes are widely employed in satellite broadcasting systems. Smaller amplitude fluctuation in circular QAM as compared to rectangular-QAM, which results in fewer amplitude levels [9] has created the research interest for their usage in optical communication systems as well.

In this paper laser linewidth requirements are investigated for the mentioned modulation formats and SER floors for different laser linewidth and different modulation formats are investigated. **Figure 2** shows the symbol error rate versus Laser linewidth for 4 QAM modulation format. The graph has been plotted for different OSNRs ranging from 10 dB to 40 dB.

It is observed from the graph in **Figure 2** that with the increase in Laser linewidth, the performance of the system deteriorates in terms of Symbol Error Rate

(SER). For 4-QAM format, the performance in terms of SER is almost consistent up to 100 KHz. After that SER starts increasing. The system starts having significant deterioration at 500 kHz and becomes more severe at 1 MHz. Hence for the systems using 4-QAM format the tolerable laser linewidth as obtained from the graph is 2.3 MHz at 15 dB OSNR, 5.2 MHz at 20 dB OSNR, 5.8 MHz for 25 dB and higher. These values are for target SER 1e−3 at a distance of 3200 km.

Figure 3 shows the SER floor for 16 QAM modulation format by increasing the laser linewidth. It is observed that the same trend follows here also as in 4 QAM but now the SER is consistent up to 10 kHz, starts deteriorating at 50 kHz
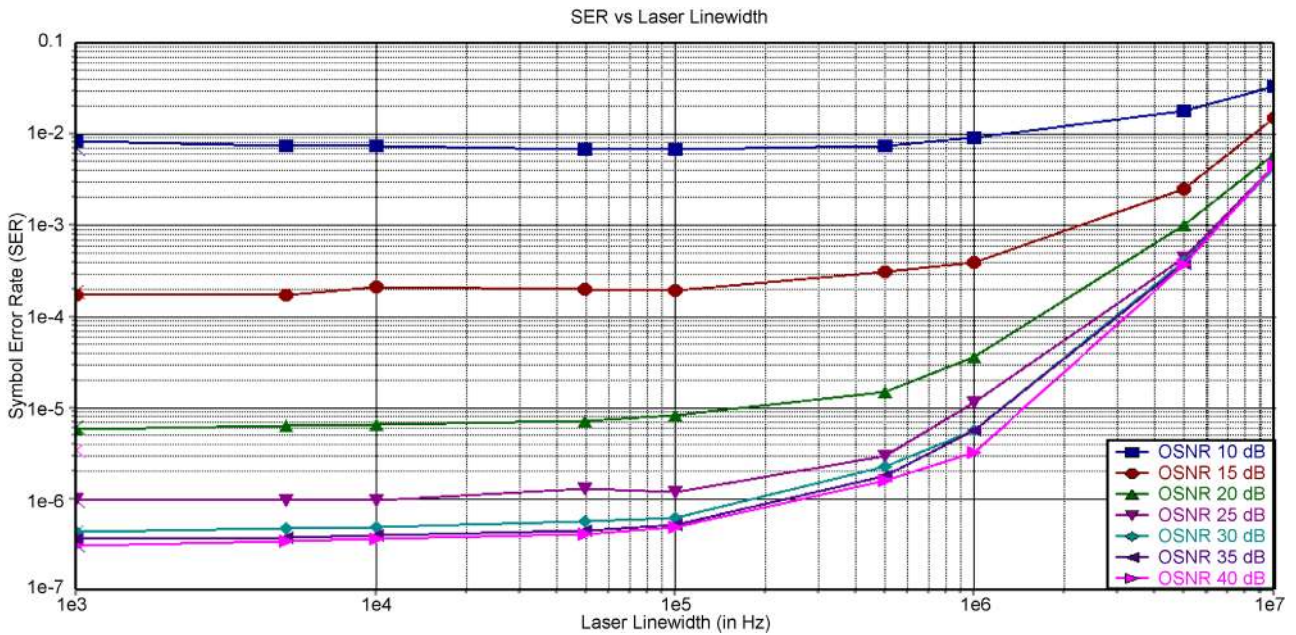

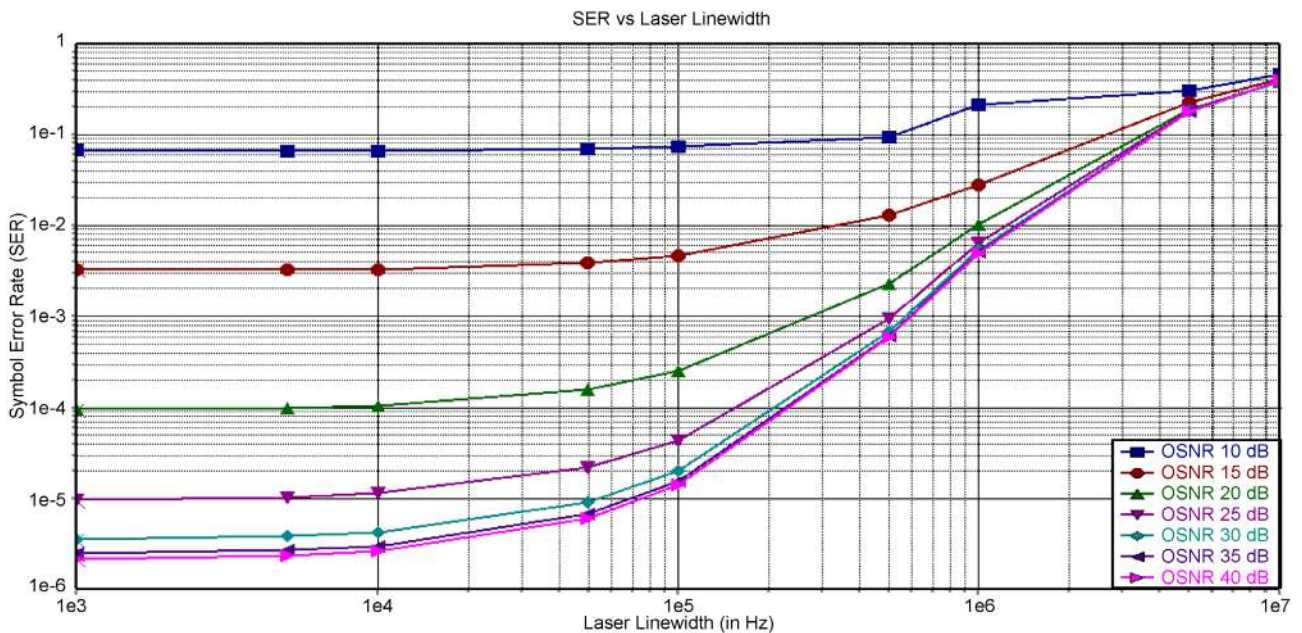Figure 2. SER vs. laser linewidth (4 QAM).

Figure 3. SER vs. laser linewidth (16 QAM).

which becomes faster at 100 kHz. Hence for the systems using 16-QAM format the tolerable laser linewidth is 300 kHz at 20 dB OSNR, 550 kHz for 25 dB OSNR, 600 KHz for 30 dB and higher. Also it is to mention that 15 dB OSNR is not sufficient to have SER < 1e−3 at a distance of 3200 km. In case of 16 QAM modulation format graphs for different OSNRs exhibit the same performance at 10 MHz whereas it is not so in the case of 4 QAM.

Circular M QAM modulation format has smaller amplitude fluctuation as compared to rectangular-QAM, which results in fewer amplitude levels. This feature of circular QAM modulation format has attracted the interest and its performance is also investigated and compared with rectangular QAM. Figures 4-6 show SER variation with linewidth for Circular 4 QAM, Circular 16 QAM and Optimized C16 QAM respectively.

The performance of circular 4-QAM format follows the same trend as that of rectangular 4-QAM format.SER is nearly consistent up to 100 kHz. After that it starts deteriorating at 500 kHz and SER deterioration becomes fast after 1 MHz (Figure 4).

Similarly for C16-QAM and optimized C16-QAM, SER starts deteriorating rapidly after 100 kHz.

Table 1 shows the tolerable linewidths for different modulation formats for various OSNRs at a distance of 3200 km for a target SER of 1e−3.

The tolerable linewidth values of rectangular 4-QAM format are small as compared to circular 4-QAM format. The difference is 0.2 MHz, 0.3 MHz, 0.4 MHz at 15 dB, 20 dB and 25 dB respectively and after that the performance is same.

For circular 16-QAM format, the tolerable linewidth is increased by nearly 70 kHz, 50 kHz, 90 kHz, 95 kHz, 90 kHz at OSNR values of 20 dB, 25 dB, 30 dB, 35
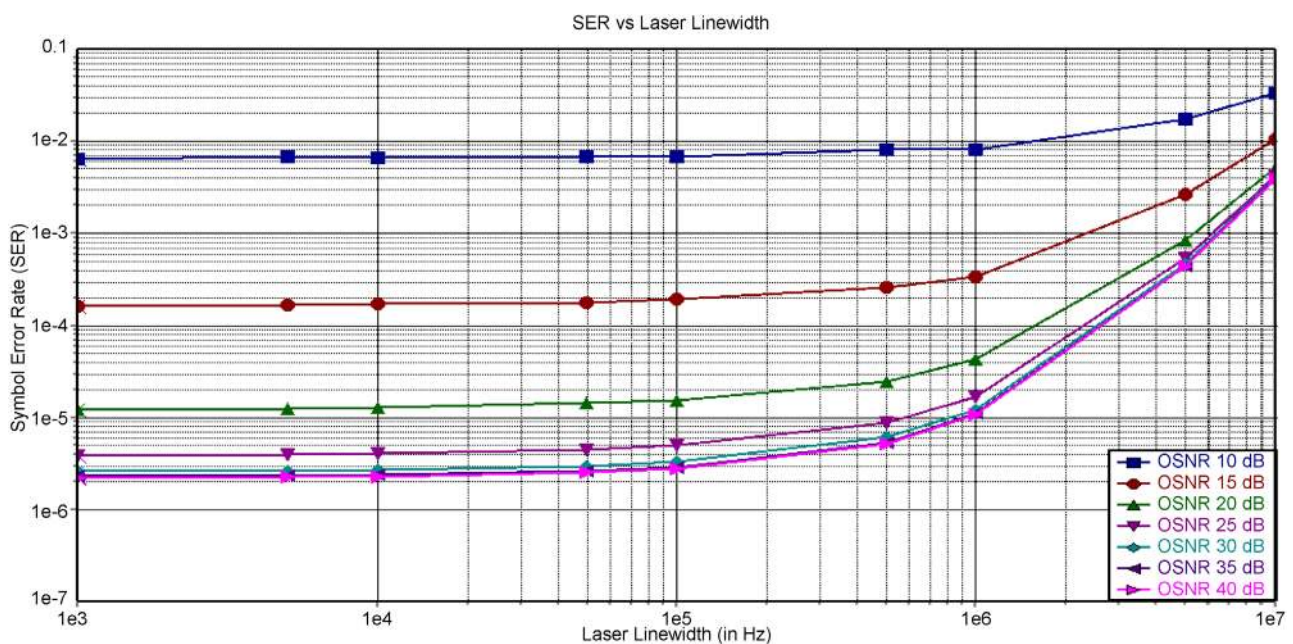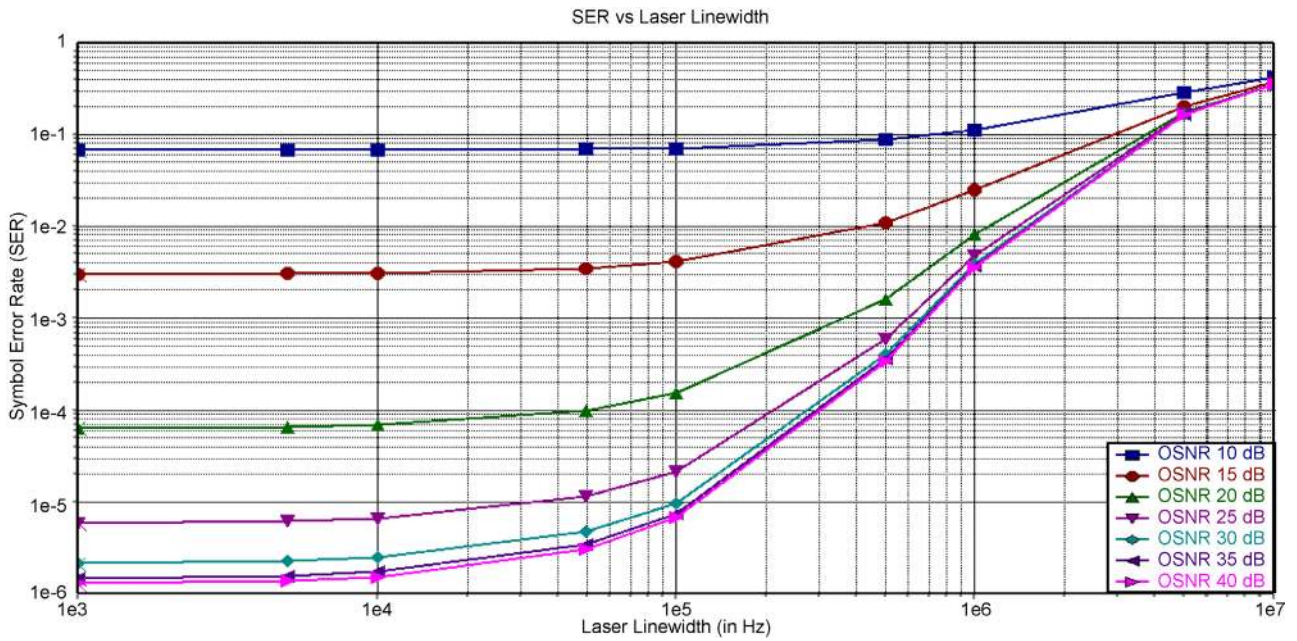

Figure 4. SER vs. laser linewidth (circular 4 QAM).

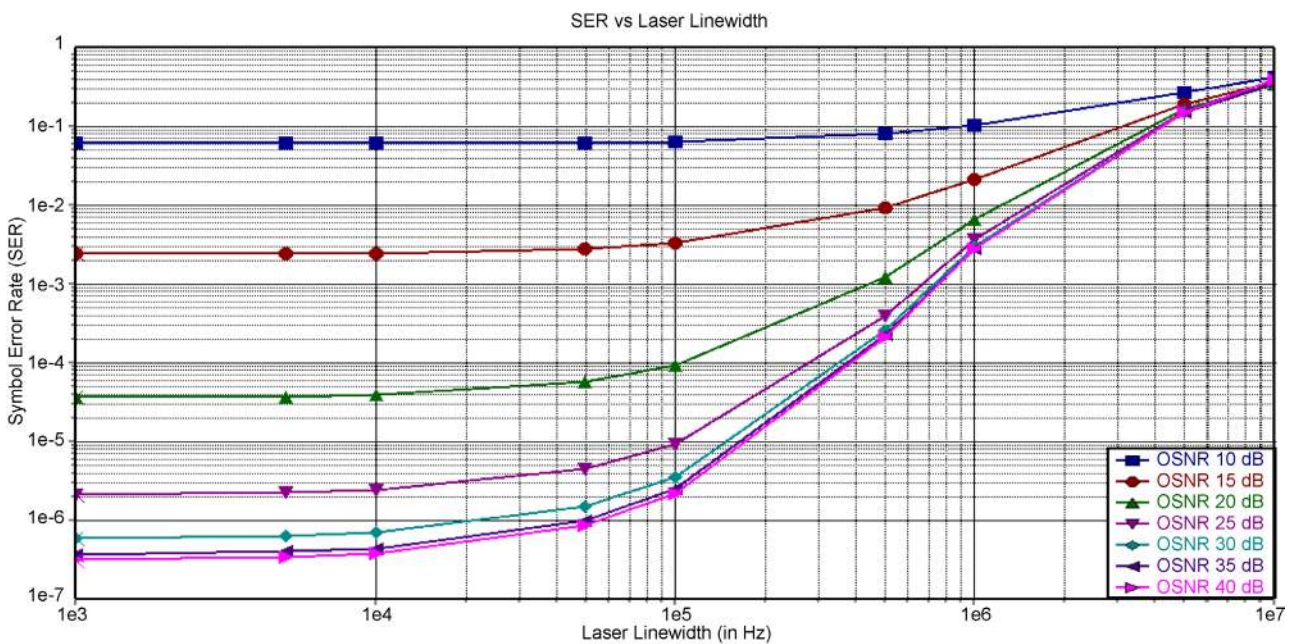**Figure 5.** SER vs. laser linewidth (circular 16 QAM).

Figure 6. SER vs. laser linewidth (optimized C16 QAM).

Table 1. Tolerable linewidth for different modulation formats for various OSNRs.

Modulation Format	OSNR						
	10 dB	15 dB	20 dB	25 dB	30 dB	35 dB	40 dB
4-QAM	Not Achieved	2.3 MHz	5.2 MHz	5.8 MHz	6.5 MHz	6.5 MHz	6.5 MHz
16-QAM	Not Achieved	Not Achieved	300 kHz	550 kHz	600 kHz	605 kHz	610 kHz
C4-QAM	Not Achieved	2.5 MHz	5.5 MHz	6.2 MHz	6.5 MHz	6.5 MHz	6.5 MHz
C16-QAM	Not Achieved	Not Achieved	370 kHz	600 kHz	690 kHz	700 kHz	700 kHz
Optimized C16-QAM	Not Achieved	Not Achieved	500 kHz	700 kHz	780 kHz	790 kHz	800 kHz

dB and 40 dB respectively when compared to rectangular 16-QAM format. For optimized C16-QAM format, this increase is 200 kHz, 150 kHz, 180 kHz, 185 kHz, 190 kHz at 20 dB, 25 dB, 30 dB, 35 dB and 40 dB respectively when compared to rectangular 16-QAM format and is in range 80 - 100 kHz when compared to regular circular 16-QAM format.

Hence it can be concluded that as OSNR is increased, the tolerable linewidth also increases. Also as the order of modulation becomes higher, the tolerable linewidth decreases. However comparing the rectangular QAM and circular QAM formats, it is observed that rectangular 4-QAM format outperforms the circular 4-QAM format whereas circular 16-QAM format outperforms the rectangular 16-QAM format. Optimized C16-QAM format has further better performance.

5. Conclusion

Optical OFDM, Coherent detection and QAM modulation format are affected by phase noise. Phase noise is characterized by Laser linewidth. Hence, laser linewidth requirements are investigated for rectangular and circular 4 and 16 QAM modulation formats. At an OSNR of 25 dB, 4 QAM modulation formats can use lasers of linewidth 5 MHz for SER < 1.0E−3 whereas the required value for 16 QAM modulation format is 500 kHz. OSNR requirements are less for circular QAM as compared to rectangular QAM. Also rectangular 4 QAM outperforms circular QAM whereas circular 16 QAM outperforms rectangular 16 QAM.

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