

# Investigation on the Small Signal Characteristic Based on the LLC Hybrid Hysteretic Charge Control

Richard (Hua) Yang, Brent A. McDonald, and Yalong Li

**Abstract**—In this paper, an analytical small-signal model applied for hybrid hysteretic charge (HHC) control has been proposed and analyzed with the advantages over direct frequency control (DFC). Based on the approach of extended describing function method and average concept, for the first time, the systematical analytical open loop transfer functions from control to output, input to output, output impedance and the closed transfer functions of the overall loop, audio susceptibility and output impedance are proposed and verified through simulation. Additionally, some important physical insights have been extracted, analyzed and verified. Finally, the experiments on a design example of 12 VDC&12 A output power are conducted and verified. It shows that the calculations match well with the results from both the simulation and experiment, which reveals the proposed analytical transfer functions are very useful for the practical power design to achieve good prediction result.

**Index Terms**—Analytical small signal model, hybrid hysteretic charge (HHC), hybrid hysteretic charge control, LLC, UCC25630.

## I. INTRODUCTION

WITH the increasing requirement on power efficiency and power density, the LLC topology has become into one of the most popular topologies of the isolated power converters. Numerous articles [1]–[6] have been created to show the best design optimization methods. However, there are the challenges for the conventional DFC LLC converter regarding the control design and loop optimization when input voltage and output voltage have been specified strictly to be within a varied range, in which the task of loop design is hard to be optimized. As for the small signal modeling on PWM converters, the state-space approach based on the average concept proposed by Middlebrook and Cuk [7] is accurate within a limited frequency bandwidth. Later R. Ridley [8] had proposed an improved methodology with the concept of the three-terminal switch, on which the good prediction result in many PWM converters are achieved [9], [10], [11], [12]. In recent years, the advanced describing function method has been successfully applied to most of current control converters with the accurate analytical transfer functions up to the switching frequency in [13]–[14]. However, all these methodologies are hard to obtain a good result if applying to the resonant converter where the switching frequency components and its harmonics have been turned into

the dominant variable part and the beat frequency dynamics has occurred. Then the extended describing function method proposed by E. X. Yang [15]–[16] had been successfully applied to the resonant converter to predict the beat frequency dynamic behavior accurately.

To work out the model of LLC converter, lots of researches [17]–[20] based on the extended describing function or other similar averaged modeling concept [21] have been employed and the results are proved to be accurate to predict the beat frequency dynamics. However, the models are still hard to meet the practical engineering design due to its lack of analytical transfer functions for the physical insight extraction and most precise modes are only based on the simulation in which the physical insight is hard to yield. It is not until recent years that S. Tian [22]–[23] simplified the model from the 5th order to a 3th one with a result of an analytical transfer function for both SRC and LLC converter. Followed by this, Y. Hsieh has employed a novel rotating coordinate modeling concept to the SRC converter and achieved the most precise prediction results based on the describing transfer function [24]–[25], in which the best accurate analytical transfer function has also been extracted but it is still expected to extend to the LLC converter. As a conclusion, there is the challenge for the conventional DFC LLC control to apply to most of the applications due to its not good transient performance by the intrinsic loop characteristic.

To solve this problem, several new LLC loop control schemes have been proposed in recent years. The first one is the average current control [26]–[27], in which the tank current has been sensed and scaled and then participate in the loop control, it is proved to be with the advantages over the DFC control on input ripple cancellation but still owns the room for the further improvement in terms of the load transient performance. The second one is the charge control [28], which compares the total input charge with the control voltage to modulate the switching frequency, then an inner current loop is offered to yield the fast-transient response. Another hysteretic charge control [29]–[30] can also achieve the good dynamic load performance by sensing the current of tank current or voltage of resonant capacitor, but the DC gain of control to output is with a little big variation during the full load range which will bring the difficulty of loop design at light load. However, there are not the detail analytical transfer functions to describe the whole physical insight regarding their small signal characteristics.

In view of the mentioned above issues, the HHC control, with the combination of charge current control and hysteretic charge control, is proposed to achieve the best-in-class

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transient performance by overcoming the disadvantage of charge control and avoiding unstable condition by adding into the frequency compensation ramp [31]–[33]. It has changed the plant transfer function to an equivalent first order system characterized by a relatively stable cross frequency and small variation of DC gains, which has made the loop design easy to compensate.

In this paper, the small signal model for new LLC converter will be proposed firstly, which is not purely depend on the approach of extended describing function and the related superposition theorem, but the improved results of a third order transfer function from this theorem. In Section II, the transfer functions of the proposed model are derived and simplified for the purpose of physical insight investigation. Different from the conventional DFC control, the proposed model replaces the small signal variable of  $F_s$  by that from feedback control. In Section III and IV, the derived analytical transfer functions regarding the open loop of control to output, input to output, output impedance and that of the closed loop are verified through simulation, in which, the detail physical insight analysis are provided. In section V, the experiment of practical design is conducted to verify the proposed transfer functions. Section VI summarizes the paper.

## II. SMALL-SIGNAL MODEL FOR HHC CONTROL

As shown in Fig.1, the key difference between HHC and the conventional DFC is the added feedback signal of VCR, which is a combination of the internal current ramp part and the divided scaling part from the voltage of the resonant capacitor  $C_s$  [31]–[32]. Refer to Fig. 1, VHS is the input voltage of the half bridge LLC tank, VTL and VTH come from the compensation voltage  $V_{comp}$ , they are symmetrical based on a reference voltage VCM (for example 3 V) and then will be compared with VCR. So  $v_{cr1}$  and  $v_{crh}$  are produced henceforth to provide the input signal for the S/R latch, therefore, the final drive signal Gate\_L and Gate\_H can be produced based on another deadtime control signal for the S/R latch. As shown in Fig. 2,  $v_{cr1}$  will turn high and then pull Gate\_L low when VTL crosses VCR at time of  $t_0$ , then the VHS begin to rise, when the rising of VHS completes or the dead time elapses at  $t_1$ , Gate\_H will turn high. At the next time of  $t_2$  when VTH has crossed VCR,  $v_{crh}$  will turn high and then pull Gate\_H low, then the VHS begins to decrease, when VHS finishes this process or the dead time has been elapsed at  $t_3$ , Gate\_L will turn high.

### A. Small Signal Model for LLC HHC Control

For a conventional DFC control, the simplified analytical transfer functions have been proposed [22]–[23], in which the capacitor small signal model has turned into an inductor small signal model. So, the original small signal model of LLC tank has been simplified greatly from an above fifth-order equivalent circuit into a third-order equivalent circuit. This has provided the great possibility to extend this result

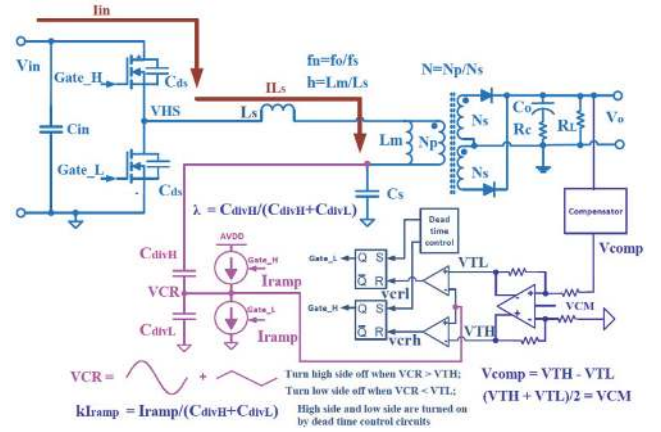


Fig. 1. The proposed HHC control used in LLC HB converter.

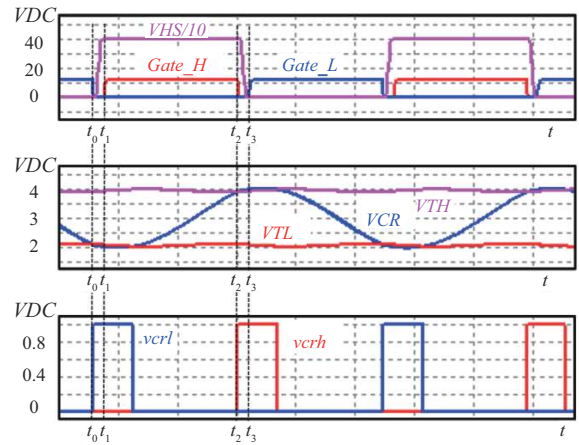


Fig. 2. Proposed hybrid hysteresic control used in LLC converter.

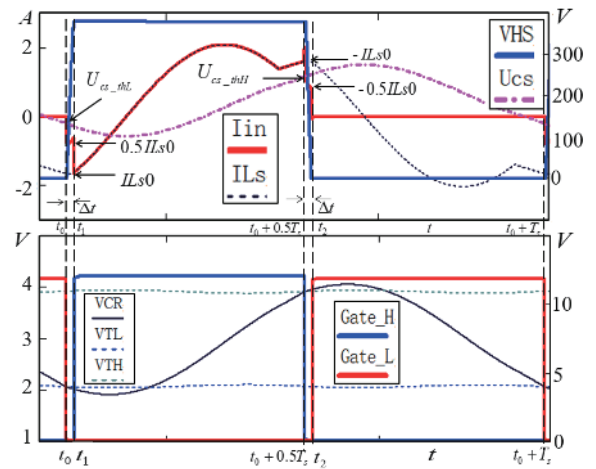


Fig. 3. Waveforms between the tank part and the VCR part for HHC control.

to other kinds of LLC control topology.

As for HHC, it is critical to investigate the key difference compared with DFC, which is the scaling voltage sense of the resonant capacitor voltage. Fig. 3 shows the key waveforms between input current  $I_{in}$ , tank current  $I_{Ls}$ , voltage of resonant capacitor  $U_{cs}$ , tank input voltage VHS, High side Gate drive Gate\_H, low side Gate drive Gate\_L, VCR, VTH

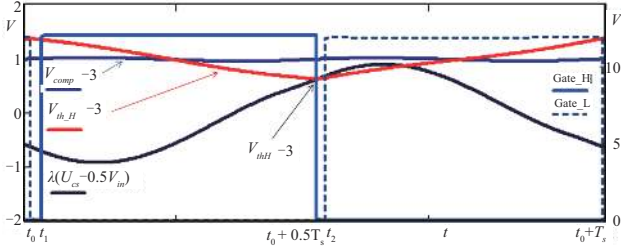


Fig. 4. Operation principle of TI HHC control with ramp current.

and VTL.

As shown in Fig. 1, the scaling voltage part in VCR is obtained from the divided voltage of  $C_s$  by the capacitors  $C_{divH}$  and  $C_{divL}$ . The scaling down coefficient can be defined as:

$$\lambda = \frac{C_{divH}}{C_{divL} + C_{divH}} \quad (1)$$

It is generally assumed the dead time  $\Delta t$  of the gate drives to be equal. Fig. 3 shows the details regarding the  $I_{in}$  and VHS, and then the average input current can be obtained as:

$$I_{in,avg} = \frac{\int_{t_0}^{t_0+0.5T_s} i_{LS}(t)dt - 0.5 \int_{t_0}^{t_1} i_{LS}(t)dt + 0.5 \int_{t_0+0.5T_s}^{t_2} i_{LS}(t)dt}{T_s} \quad (2)$$

If defining the voltage of  $U_{cs}$  at  $t_0$  and  $t_0 + 0.5T_s$  as  $U_{cs\_thL}$  and  $U_{cs\_thH}$ , and the tank current as  $I_{Ls0}$  at  $t_0$ , then (2) can be re-written as:

$$\begin{aligned} I_{in,avg} &= \frac{\int_{t_0}^{t_0+0.5T_s} i_{LS}(t)dt + 2|0.5I_{Ls} \ 0| \Delta t}{T_s} \\ &= \frac{\int_{t_0}^{t_0+0.5T_s} i_{LS}(t)dt + 2C_{ds}V_{in}}{T_s} \\ &= F_s(C_s(U_{cs\_thH} - U_{cs\_thL}) + 2C_{ds}V_{in}) \end{aligned} \quad (3)$$

It shows the minimum dead time is considered from (3), so the input power under steady status can be finally written as:

$$P_{in} = V_{in}F_sC_s(2U_{cs\_thH} - V_{in}) + 2C_{ds}F_sV_{in}^2 \quad (4)$$

In the configuration of HHC method products such as TI UCC25630X series, the quantity of  $U_{cs\_thH}$  can be sensed by the voltage of VCR pin even though there is another combination of ramp current by the internal frequency compensation. Shown as in Fig. 4, the scaling voltage  $\lambda(U_{cs} - 0.5V_{in})$  will cross the quantity of  $V_{thH} - VCM$  (the combined quantity of feedback and ramp current) with a value of  $V_{thH} - VCM$  when Gate\_H turns off, the operation principle will be elaborated by the formulas (5)–(7).

From the operation principle of HHC control, the compensation part in terms of integrating frequency control into VCR voltage is paramount for the investigation, if we define the internal coefficient for the ramp compensation as:

$$k_{Iramp} = \frac{I_{ramp}}{C_{divL} + C_{divH}} \quad (5)$$

Then the following equations can be obtained as:

$$V_{comp} - \frac{0.25k_{Iramp}}{F_s} = V_{thH} \quad (6)$$

$$\lambda(U_{cs\_thH} - 0.5V_{in}) + VCM = V_{thH} \quad (7)$$

If we define the conversion efficiency from primary side to secondary side as  $\eta$ ,  $V_f$  as the average forward voltage for a rectifier on the output side,  $I_{sec}$  as the LLC tank's output current,  $I_o$  as the external load current, and  $Z(s)$  as the LLC output impedance, then the following equation can be obtained if the formulas of (5)–(7) are combined into (4).

$$I_{sec} = \frac{\eta \left( V_{in}F_sC_s \frac{2(V_{thH} - VCM)}{\lambda} + 2C_{ds}F_sV_{in}^2 \right)}{V_o + V_f} = I_o + \frac{V_o}{Z(s)} \quad (8)$$

In above (8), there are four variables  $V_o$ ,  $V_{in}$ ,  $V_{thH}$  and  $I_o$ , which are mainly with DC components but not include the switching frequency components and its harmonics, then the conventional average concept [1] can be applied to derive the related small signal small equation. For the theoretical manipulation, we can ignore the quantities of  $V_f$  and  $\eta$ . Perturbing on the above formula (8) with the quantities of  $V_o$ ,  $V_{in}$ ,  $V_{thH}$  and  $I_o$  by  $\hat{v}_o$ ,  $\hat{v}_{in}$ ,  $\hat{v}_{thH}$ ,  $\hat{i}_o$  respectively, we can obtain the following small signal equations:

$$\hat{v}_o = Z(s) \left( -\frac{\hat{v}_o}{R_L} + k_{th}\hat{v}_{thH} + \left( \frac{V_o}{R_LF_s} + \frac{2C_{ds}V_{in}^2}{V_o} \right) \hat{f} + k_{in}\hat{v}_{in} - \hat{i}_o \right), \quad (9)$$

where:

$$Z(s) = \frac{R_L(1 + sR_cC_o)}{1 + sR_LC_o} \quad k_{in} = \frac{V_o}{R_LV_{in}} - \frac{2C_{ds}V_{in}F_s}{V_o} \quad k_{th} = \frac{2C_{ds}V_{in}F_s}{V_o\lambda}$$

Refer to Fig. 4, the small signal average concept can also be employed based on (6). Perturbing on the variables of  $V_{comp}$ ,  $F_s$  and  $V_{thH}$  by  $\hat{v}_{comp}$ ,  $\hat{f}$ ,  $\hat{v}_{thH}$ , then we can obtain the following:

$$\hat{v}_{comp} + \frac{0.25k_{Iramp}}{F_s^2} \hat{f} = \hat{v}_{thH} \quad (10)$$

Combining (10) into (9), we have:

$$\begin{aligned} \hat{v}_o / Z(s) &= k_v\hat{v}_o + k_{th}\hat{v}_{thH} + k_f\hat{f} + k_{in}\hat{v}_{in} - \hat{i}_o \\ k_f &= \frac{V_o}{R_LF_s} + \frac{2C_{ds}V_{in}^2}{V_o} + \frac{0.5V_{in}C_sI_{ramp}}{V_oF_sC_{divH}} \end{aligned} \quad (11)$$

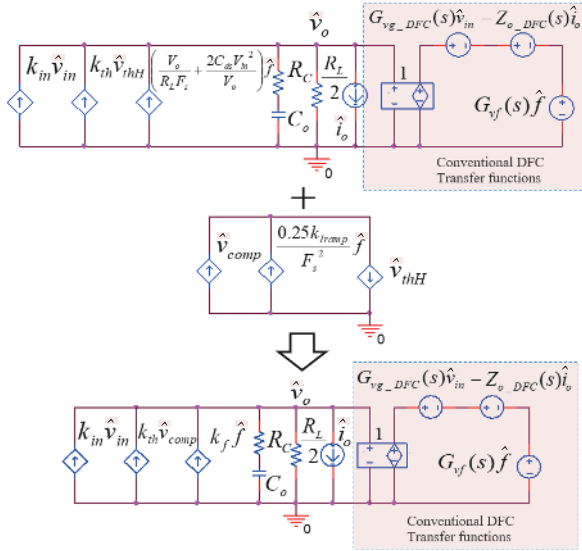


Fig. 5. Small signal equivalent circuit for the LLC HHC control.

So, the correlation in terms of small signal variables among input voltage, output voltage, compensation voltage, operation (7) frequency and external output current have been built by (11).

### B. Implementation of the Analytical HHC Small Signal Transfer Function

Equation (11) shows that the small signal perturbation of the output  $V_o$  has one more of the small signal variable  $V_{comp}$  than the conventional DFC control due to the characteristic of HHC control, where the compensation feedback signal is only directly related to  $V_{comp}$  but not  $F_s$  from the control block. It is taken for granted that only one variable  $V_{comp}$  is incorporated into the open loop of control to output finally, then the small signal variable of  $F_s$  is required to be cancelled in the final control block. However, it is not straightforward to implement such a behavior in the control block directly; therefore, it is required to make a mathematic manipulation from the conventional DFC control to replace the small signal variable of  $F_s$  provided that the analytic small transfer function is given. Refer to the simplified analytic transfer functions applied for a DFC control [23], the perturbation of  $V_o$  can be expressed by the open loop transfer functions of input to output  $G_{vg\_DFC}(s)$ , control to output  $G_{vf}(s)$  and output impedance  $Z_{o\_DFC}(s)$ , which is shown as:

$$\hat{v}_o = G_{vg\_DFC}(s)\hat{v}_{in} + G_{vf}(s)\hat{f} - Z_{o\_DFC}(s)\hat{i}_o \quad (12)$$

Fig. 5 shows the small signal equivalent circuit for the LLC HHC control.

Even the concept of extended describing function proposed by Dr. E. Yang has been used widely for the small signal analysis both for SRC, LLC and other types of resonant converters [16], most of the models are accurate enough to make a good prediction regarding the small signal characteristic over a wide frequency range. However, most of them are featured by complicated mathematics expressions or the circuit simulation-oriented way, their analytical based

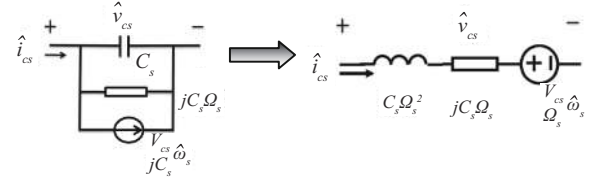


Fig. 6. Simplified equivalent small signal model for the resonant capacitor proposed by S. Tian.

formulas are still hard to be derived due to the higher order of the model. To simplify the order of the model, Shown in Fig. 6. Tian had tried to propose a simplified model successfully by turning the equivalent signal model circuit of the resonant capacitor into an equivalent model featuring inductor behavior [22]–[23], then the original small signal circuit of LLC tank has been simplified greatly from the original fifth-order equivalent circuit into a third-order one, which has provided the great possibility to obtain the analytical expression.

However, the ESR of the output capacitors is neglected due to the practical use of ceramic capacitors as far as the analytical small signal transfer function is concerned [23]. For the scenarios of using electrolytic capacitors, the ESR shall be considered. Shown in Table I, the analytical transfer functions have been modified to achieve this. The combination of the formulas (11)–(13) will result in a final small signal transfer function shown as below:

$$\begin{aligned} \hat{v}_o(s) & \left( \frac{1}{Z(s)} - \left( \frac{k_f}{G_{vf\_DFC}(s)} - \frac{1}{R_L} \right) \right) \\ & = k_{th}\hat{v}_{comp}(s) + \left( k_{in} - \frac{k_f G_{vg\_DFC}(s)}{G_{vf\_DFC}(s)} \right) \hat{v}_{in}(s) + \left( \frac{k_f Z_o(s)}{G_{vf\_DFC}(s)} - 1 \right) \hat{i}_o \end{aligned} \quad (13)$$

Then the transfer function of LLC HHC control can be obtained as follows:

$$\hat{v}_o = G_{vg\_HHC}(s)\hat{v}_{in} + G_{vc\_HHC}(s)\hat{v}_{vc} - Z_{o\_HHC}(s)\hat{i}_o \quad (14)$$

where:

$$G_{vc\_HHC}(s) = \frac{k_{in}Z(s)}{1 - Z(s)\left(\frac{k_f}{G_{vf\_DFC}(s)} - \frac{1}{R_L}\right)}$$

$$G_{vg\_HHC}(s) = Z(s)\left(k_{in} - k_f \frac{G_{vg\_DFC}(s)}{G_{vf\_DFC}(s)}\right) \left/ \left( 1 - Z(s)\left(\frac{k_f}{G_{vf\_DFC}(s)} - \frac{1}{R_L}\right) \right) \right.$$

$$Z_{o\_HHC}(s) = Z(s)\left(k_{in} - k_f \frac{Z_{o\_DFC}(s)}{G_{vf\_DFC}(s)}\right) \left/ \left( 1 - Z(s)\left(\frac{k_f}{G_{vf\_DFC}(s)} - \frac{1}{R_L}\right) \right) \right.$$

If we define  $G_{DC\_vg}$  as the DC gain of  $G_{vg\_DFC}(s)$ ,  $G_{DC\_dm}$  and  $G_{DC\_cm}$  as the DC gain of  $G_{vf\_DFC}(s)$  under the conditions of  $f_n \leq 1$  and  $f_n \geq 1$  respectively ( $f_n$  is the normalized operation frequency), then the transfer functions of open control to output loop  $G_{vc\_HHC}(s)$ , open input to output loop  $G_{vg\_HHC}(s)$ , open output impedance  $Z_{o\_HHC}(s)$  can be simplified into the analytical formula expression after the mathematic manipulations [33], which is also shown in Table II.

TABLE I  
TRANSFER FUNCTIONS FOR CONVENTIONAL LLC HB CONVERTER

| Transfer Functions for the Conventional DFC LLC Converter                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $G_{DC_{cm}}$<br>( $f_n \geq 1$ )                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | $\frac{V_{in} f_n h}{2F_s N} \frac{\left(\frac{1}{f_n^2} - f_n^2\right) \left(\frac{\pi^2 Q_r h}{8}\right)^2 - \left(h + 1 - \frac{1}{f_n}\right) \frac{2}{f_n^2}}{\left[\sqrt{\left(h + 1 - \frac{1}{f_n^2}\right)^2 + \left(\left(\frac{1}{f_n} - f_n\right) \frac{\pi^2 h Q_r}{8}\right)^2}\right]^3}$                                                                                                                                                                                                                                                                                                           |
| $G_{DC_{dm}}$<br>( $f_n \leq 1$ )                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | $\frac{V_{in} f_n h}{2N} \frac{\left(\frac{1}{f_n^2} - f_n^2\right) \left(\frac{\pi^2 Q_r h}{8}\right)^2 - \left(h + 1 - \frac{1}{f_n}\right) \frac{2}{f_n^2}}{2N} \frac{1}{f_n \sin\left(\frac{\pi f_n}{2}\right)} \frac{1}{\left[\sqrt{\left(h + 1 - \frac{1}{f_n^2}\right)^2 + \left(\left(\frac{1}{f_n} - f_n\right) \frac{\pi^2 h Q_r}{8}\right)^2}\right]^3} \frac{\pi \cos\left(\frac{\pi f_n}{2}\right)}{2 \sin^2\left(\frac{\pi f_n}{2}\right)} - \frac{V_{in} f_n h}{2N} \frac{1}{\sqrt{\left(h + 1 - \frac{1}{f_n^2}\right)^2 + \left(\left(\frac{1}{f_n} - f_n\right) \frac{\pi^2 h Q_r}{8}\right)^2}}$ |
| $G_{vL_{DFC}}(s)$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | $G_{DC_{cm}} \frac{(1 + sR_c C_o)(R_{eq}^2 + X_{eq}^2)}{(s^2 L_e^2 + sL_e R_{eq} + X_{eq}^2)(1 + sR_L C_o) + R_{eq}(sL_e + R_{eq})(1 + sR_c C_o)} \quad (f_n \geq 1)$<br>$G_{DC_{dm}} \frac{1 + sR_c C_o}{1 + \frac{s}{Q_p \omega_p} + \frac{s^2}{\omega_p^2}} \quad (f_n \leq 1)$                                                                                                                                                                                                                                                                                                                                  |
| $G_{DC_{vg}}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | $\frac{1}{2N} \frac{1}{\sqrt{\left(h + 1 - \frac{1}{f_n^2}\right)^2 + \left(\left(\frac{1}{f_n} - f_n\right) \frac{\pi^2 h Q_r}{8}\right)^2}} \quad (f_n \geq 1)$<br>$\frac{1}{2N \sin\left(\frac{\pi f_n}{2}\right)} \frac{h}{\sqrt{\left(h + 1 - \frac{1}{f_n^2}\right)^2 + \left(\frac{1}{\sin\left(\frac{\pi f_n}{2}\right)} \left(\frac{1}{f_n} - f_n\right) \frac{\pi^2 h Q_r}{8}\right)^2}} \quad (f_n \leq 1)$                                                                                                                                                                                              |
| $G_{vg_{DFC}}(s)$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | $G_{DC_{vg}} \frac{(1 + sR_c C_o)(sL_e R_{eq} + R_{eq}^2 + X_{eq}^2)}{(s^2 L_e^2 + sL_e R_{eq} + X_{eq}^2)(1 + sR_L C_o) + R_{eq}(sL_e + R_{eq})(1 + sR_c C_o)} \quad (f_n \geq 1)$<br>$G_{DC_{vg}} \frac{1 + sR_c C_o}{1 + \frac{s}{Q_p \omega_p} + \frac{s^2}{\omega_p^2}} \quad (f_n \leq 1)$                                                                                                                                                                                                                                                                                                                    |
| $Z_{o_{DFC}}(s)$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | $R_L \frac{(1 + sR_c C_o)(s^2 L_e^2 + sL_e R_{eq} + X_{eq}^2)}{(s^2 L_e^2 + sL_e R_{eq} + X_{eq}^2)(1 + sR_L C_o) + R_{eq}(sL_e + R_{eq})(1 + sR_c C_o)} \quad (f_n \geq 1)$<br>$\frac{\pi^2 L_e}{8N^2} \frac{s(1 + sR_c C_o)}{1 + \frac{s}{Q_p \omega_p} + \frac{s^2}{\omega_p^2}} \quad (f_n \leq 1)$                                                                                                                                                                                                                                                                                                             |
| $L_e = \begin{cases} L_s \left(1 + \frac{1}{f_n}\right) & (f_n \geq 1) \\ L_s \left(1 + \frac{1}{f_n}\right) + L_m (1 - f_n) & (f_n \leq 1) \end{cases} \quad \omega_p = \sqrt{\frac{8N^2}{L_c C_o \pi^2 \left(1 + \frac{\pi R_c}{\sqrt{8} R_L}\right)}} \quad R_{eq} = \frac{8N^2 R_L}{\pi}$<br>$h = \frac{L_m}{L_s}$<br>$Q_p = \sqrt{R_L + \frac{\pi R_c}{\sqrt{8}}} \cdot \frac{8\pi N \sqrt{L_e C_o R_L}}{16\sqrt{2} N^2 R_L C_o R_c + \pi^3 L_e} \quad X_{eq} = 2\pi F_s C_s - \frac{1}{2\pi F_s C_s} \quad Q_r = \sqrt{\frac{L_s}{C_s}} \frac{1}{R_L N^2} \quad f_n = \frac{F_s}{F_o}$ |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |

TABLE II  
TRANSFER FUNCTIONS FOR LLC HHC HB CONVERTER

| Open Loop Transfer Functions for the HHC LLC Converter                                                                                                                                                                                            |                                                                                                                                                                                                                                                                                                                                                                          |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $G_{vc\_HHC}(s)$                                                                                                                                                                                                                                  | $\frac{\frac{k_{th}}{R_L} - \frac{k_f}{G_{DC\_dm}}}{1 + s \frac{C_o \left(1 + \frac{R_c}{R_L}\right) - \frac{k_f}{G_{DC\_dm} Q_p \omega_p} + \frac{s^2}{\omega_p^2 \left(1 - \frac{2G_{DC\_dm}}{R_L k_f}\right)}} \frac{1 + sR_c C_o}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_dm}}} \quad (f_n \leq 1)$                                                                        |
|                                                                                                                                                                                                                                                   | $\frac{\frac{k_{th}}{R_L} - \frac{k_f}{G_{DC\_cm}}}{1 + \frac{s}{\omega_1} + \frac{s^2}{\omega_2} + \frac{s^3}{\omega_3}} \frac{1 + sR_c C_o}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_cm}}} \quad (f_n \geq 1)$                                                                                                                                                                |
| $G_{vg\_HHC}(s)$                                                                                                                                                                                                                                  | $\frac{k_{in} - k_f \frac{G_{DCVg}}{G_{DC\_dm}}}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_dm}}} \frac{1 + sR_c C_o}{1 + s \frac{C_o \left(1 + \frac{R_c}{R_L}\right) - \frac{k_f}{G_{DC\_dm} Q_p \omega_p} + \frac{s^2}{\omega_p^2 \left(1 - \frac{2G_{DC\_dm}}{R_L k_f}\right)}} \quad (f_n \leq 1)$                                                                           |
|                                                                                                                                                                                                                                                   | $\frac{\left(k_{in} - k_f \frac{G_{DCVg}}{G_{DC\_cm}}\right) (1 + sR_c C_o) \left(1 + s \frac{G_{DCVg} L_e R_{eq} k_f}{(R_{eq}^2 + X_{eq}^2) (k_f G_{DCVg} - k_{in} G_{DC\_cm})}\right)}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_cm}}} \frac{1 + \frac{s}{\omega_1} + \frac{s^2}{\omega_2} + \frac{s^3}{\omega_3}}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_cm}}} \quad (f_n \geq 1)$ |
| $Z_{o\_HHC}(s)$                                                                                                                                                                                                                                   | $\frac{1}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_dm}}} \frac{(1 + sR_c C_o) \left(1 + s \frac{(-k_f) L_e \pi^2}{8N^2}\right)}{1 + s \frac{C_o \left(1 + \frac{R_c}{R_L}\right) - \frac{k_f}{G_{DC\_dm} Q_p \omega_p} + \frac{s^2}{\omega_p^2 \left(1 - \frac{2G_{DC\_dm}}{R_L k_f}\right)}} \quad (f_n \leq 1)$                                                               |
|                                                                                                                                                                                                                                                   | $\frac{\left(1 - \frac{k_f R_L X_{eq}^2}{G_{DC\_cm} (R_{eq}^2 + X_{eq}^2)}\right) (1 + sR_c C_o) \left(1 + \frac{s}{\omega_4} + \frac{s^2}{\omega_5}\right)}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_cm}}} \frac{1 + \frac{s}{\omega_1} + \frac{s^2}{\omega_2} + \frac{s^3}{\omega_3}}{\frac{2}{R_L} - \frac{k_f}{G_{DC\_cm}}} \quad (f_n \geq 1)$                             |
| $\omega_1 = \frac{(R_{eq}^2 + X_{eq}^2) \left(\frac{2G_{DC\_cm}}{R_L k_f} - 1\right)}{\left(1 + \frac{R_c}{R_L}\right) \frac{G_{DC\_cm} C_o}{k_f} (R_{eq}^2 + X_{eq}^2) - 2R_{eq} L_e - R_L C_o X_{eq}^2 - R_c C_o R_{eq}}$                       |                                                                                                                                                                                                                                                                                                                                                                          |
| $\omega_2 = \frac{(R_{eq}^2 + X_{eq}^2) \left(1 - \frac{2G_{DC\_cm}}{R_L k_f}\right)}{L_e^2 + L_e R_L C_o R_{eq} + R_{eq} L_e R_c C_o} \quad \omega_3 = \frac{(R_{eq}^2 + X_{eq}^2) \left(1 - \frac{2G_{DC\_cm}}{R_L k_f}\right)}{L_e^2 R_c C_o}$ |                                                                                                                                                                                                                                                                                                                                                                          |
| $\omega_4 = \frac{G_{DC\_cm} (R_{eq}^2 + X_{eq}^2) - k_f R_L X_{eq}^2}{R_{eq} L_e R_L (-k_f)} \quad \omega_5 = \frac{G_{DC\_cm} (R_{eq}^2 + X_{eq}^2) - k_f R_L X_{eq}^2}{L_e^2 R_L (-k_f)}$                                                      |                                                                                                                                                                                                                                                                                                                                                                          |
| $k_{th} = \frac{2C_s V_{in} F_s}{V_o \lambda} \quad k_{in} = \frac{V_o}{R_L V_{in}} - \frac{2C_{ds} V_{in} F_s}{V_o} \quad k_f = \frac{V_o}{R_L F_s} + \frac{2C_{ds} V_{in}^2}{V_o} + \frac{0.5V_{in} C_s I_{ramp}}{V_o F_s C_{divH}}$            |                                                                                                                                                                                                                                                                                                                                                                          |

### III. VERIFICATION ON THE ANALYTICAL TRANSFER FUNCTIONS

The small signal characteristic of LLC HHC converter will be fully verified and investigated in this section through simulation based on a design example with major power stage parameters setting by:  $V_{in} = 370 \text{ VDC} - 410 \text{ VDC}$ ,  $V_o = 24 \text{ VDC}$ ,  $R_L = 2 \Omega$ ,  $L_m = 330 \mu\text{H}$ ,  $L_s = 50 \mu\text{H}$ ,  $C_s = 44 \text{ nF}$ ,  $C_o = 470 \mu\text{F} \times 4$ ,  $R_c = 24 \text{ m}\Omega/4$ ,  $N = N_p/N_s = 25/3$ . The related SIMPLIS simulation is used based on the circuits shown as in Fig. 7.

#### A. Verification and Analysis on the Transfer Function of Open Control to Output

Based on the transfer functions presented in Table I and Table II, the open loop transfer functions for the HHC control for the UCC25630X products can be verified further by using the same approach, in which the related small signal plots regarding the open control to output under the scenarios of  $f_n > 1$  and  $f_n < 1$  are obtained through calculation. To have a contrast, the simulation is conducted. As shown in Fig. 8, the results between SIMPLIS simulation and calculation are given under the input condition of 370 VDC and 410 VDC with the output being 24 VDC & 12 A. The dashed lines show the simulation results and the solid lines show the calculation results.

It is shown from Fig. 8 that the calculation results match well with the simulation results in both the conditions. However, the calculation results do not match the simulation results well when frequency increases up to half of the operation frequency due to the simplified third-order of the model and the incorporated average concept, but it does not have any impact on the practical prediction.

In order to investigate the characteristic of HHC and the advantage over the conventional hysteretic control, the DC gain of  $G_{vc}(s)$  for these two approaches are analyzed. Refer to Table I, the DC gain of  $G_{vc}(s)$  can be simplified as:

$$G_{dc_{vc\_HHC}} = \frac{\frac{2C_s V_{in} F_s}{V_o \lambda}}{\frac{2}{R_L} - \left( \frac{V_o}{R_L} + \frac{V_{in}}{V_o} k_{I_{ramp}} \right) \frac{1}{G_{DC_{vf}} F_o f_n}} \cdot \frac{4NC_s F_o f_n}{G_{DC_{vg}} \lambda} = \frac{2}{R_L} + \left( \frac{V_o}{R_L} + \frac{2k_{I_{ramp}} N}{G_{DC_{vg}}} \right) \frac{1}{(-G_{DC_{vf}}) F_o f_n} \quad (15)$$

While

$$G_{DC_{vf}} = \begin{cases} G_{DC_{cm}} & (f_n \geq 1) \\ G_{DC_{dm}} & (f_n \leq 1) \end{cases} \quad k_{I_{ramp}} = \frac{C_s \cdot 10^{-3}}{C_{divH}}$$

For the HHC, the DC Gain will be inversely proportional to  $\lambda$  from (15), another variable is  $k_{I_{ramp}}$ , in which the variable

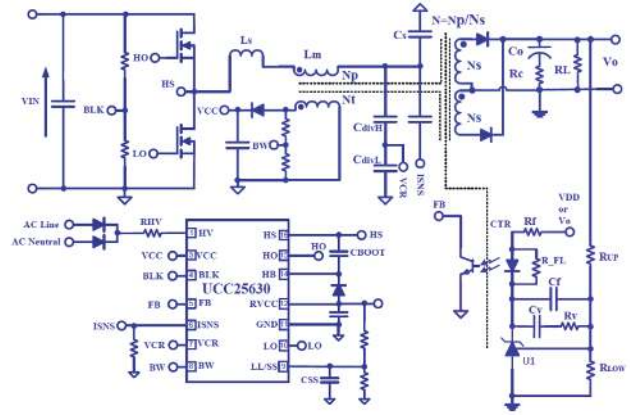


Fig. 7. Circuit for the simulation verification (dead time is set as 200 ns).

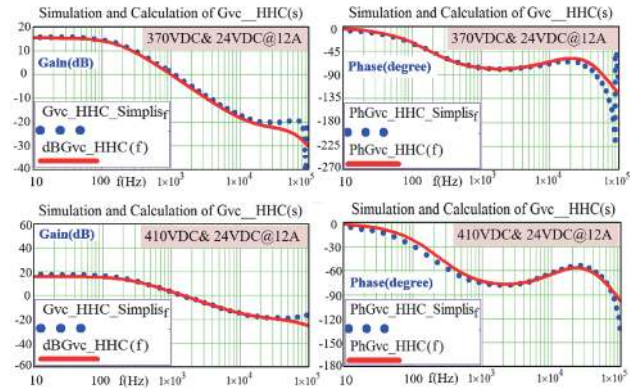


Fig. 8. Plot comparison of control to output between simulation and calculation under the condition of 370 VDC@24 VDC&12 A ( $f_n = 0.82$ ) and 410 VDC ( $f_n = 1.08$ )@24 VDC&12 A.

of  $I_{ramp}$  has been incorporated. However, it is not the case for the conventional charge control. So, the difference can be found through the approximate DC gain plot referring to the variables of  $R_L$  and  $f_n$ . Shown in (16), the normal constant of  $k_{I_{ramp}}$  can be removed and the DC gain for the conventional charge control can be obtained.

$$G_{dc_{vc\_HHC}}(R_L, f_n) = \frac{\frac{4NC_s F_o f_n}{G_{DC_{vg}}(R_L, f_n) \lambda}}{\frac{2}{R_L} + \left( \frac{V_o}{R_L} + \frac{2k_{I_{ramp}} N}{G_{DC_{vg}}(R_L, f_n)} \right) \frac{1}{(-G_{DC_{vf}}(R_L, f_n)) F_o f_n}} \quad (16)$$

With the incorporation of  $G_{DC_{vg}}(R_L, f_n)$  and  $G_{DC_{vf}}(R_L, f_n)$  shown in Table I, the approximate DC gain plot between the HHC control and the conventional hysteretic charge (HC) control can be illustrated in Fig. 9. To have the investigation on the DC gain over a practical design input voltage range, the plotting under different output load for HHC control is shown in the left part of Fig. 9, where three items of the curve tendency can be observed: firstly, the overall DC gain is proportional to  $V_{in}$  under a certain output load even though there is a special case when  $f_n$  is below 1, in which the gain will not decrease at once but it will decrease finally with respect to the decreasing of  $f_n$ . Secondly, the

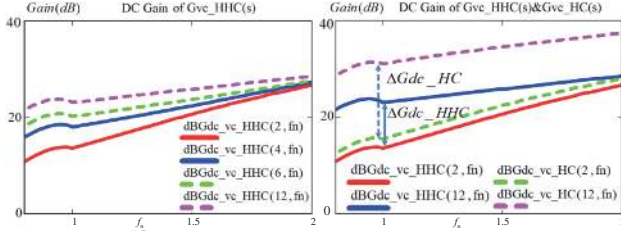


Fig. 9. DC gain plot comparison between the HHC and the conventional hysteretic charge control.

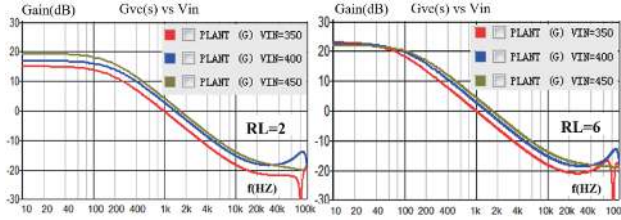


Fig. 10. Loop simulation of control to output when the input voltage varies.

gain will decrease when more of the output current is loaded, which means it will increase under a light load condition. To the third, the delta value of DC gain under those two different load conditions will decrease when  $f_n$  is increased. As shown in the right part of Fig. 9, we can obtain the comparison results between proposed HHC control and conventional hysteretic charge control: firstly, it is concluded that the gain in HC control is with the similar operation discipline, it will increase when  $f_n$  increases under a certain output current, but the delta value of DC gain under those two conditions is different. Refer to right part of Fig. 9, the solid line and the dashed line represent the plot curves of HHC control and HC control respectively, it shows the DC gain of HC control nearly approaches that of HHC control under full load condition, but it increases more under light load condition. As a conclusion, the control design for a conventional hysteretic charge control still faces some challenges if compared to HHC control.

To verify this conclusion, the simulation is conducted under two different output load conditions of  $R_L = 2 \Omega$  and  $6 \Omega$  when input voltage is varied from 350 VDC to 450 VDC. Shown as in Fig. 10, it can be observed that the DC gain follows the similar operation discipline concluded above: the gain will decrease as output load increases from  $R_L = 6 \Omega$  to  $R_L = 2 \Omega$ , the delta value of the gain under a same varied input range will decrease as output load decreases from  $R_L = 2 \Omega$  to  $R_L = 6 \Omega$ .

Fig. 11 shows another investigation when the output varies under a certain input, it can be concluded that the DC gain of the  $G_{vc}(s)$  has some small variation under the rated output load, the lower the input voltage is, the lower the gain can be obtained. From another point of review, the DC gain will decrease with the increase of output load under these two input conditions, the delta value of the gain under a same varied output load range will decrease with the increase of input voltage.

It shows from Figs.10–11 that the cross frequency for the closed loop shall be below the zero of output electrolytic capacitors and also required to avoid the impact range of high frequency dynamics occurring behavior. In order

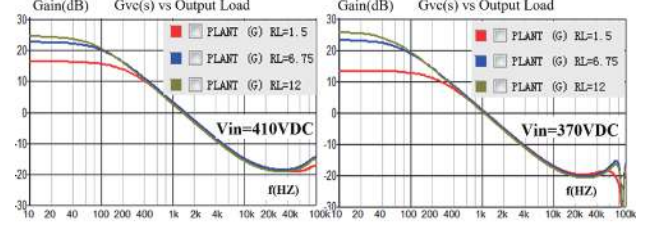


Fig. 11. Sweep of control to output when output current varies.

to yield an easy design for the compensation circuit, the transfer function of open control to output is required to be simplified. Take the scenario of  $f_n \geq 1$ , for example, if the high order poles shown in  $G_{vc}(s)$  are neglected, then the transfer function of open control to output can be simplified further as follows:

$$G_{vc\_HHC\_design}(s) \approx \frac{k_{th}}{R_L} \frac{1 + sR_c C_o}{2 - \frac{k_f}{G_{DC\_cm}} \left(1 + \frac{s}{\omega_1}\right)} \quad (f_n \geq 1) \quad (17)$$

The cross frequency can be approximated as:

$$f_{c\_Gvc} = \frac{\omega_1}{2\pi} \frac{k_{th}}{R_L} \frac{1}{2 - \frac{k_f}{G_{DC\_cm}}} = \frac{1}{2\pi} \frac{k_{th}/k_f}{\frac{C_o}{k_f} - \frac{2R_{eq}L_c + R_L C_o X_{eq}^2}{G_{DC\_cm}(X_{eq}^2 + R_{eq}^2)}} \quad (18)$$

The above (18) can be further simplified as:

$$f_{c\_Gvc} = \frac{1}{2\pi} \frac{k_{th}}{k_f} \frac{1}{\frac{C_o}{k_f} - \delta(R_L, f_n)} \quad (19)$$

$$\delta(R_L, f_n) = \frac{R_L L_s f_n h \left( \frac{16N^2}{\pi^2} + \frac{C_o}{C_s} \left( f_n - \frac{1}{f_n} \right)^2 \right)}{2V_o \left( \frac{L_s}{C_s} \left( f_n - \frac{1}{f_n} \right)^2 + R_L^2 \left( \frac{8N^2}{\pi^2} \right)^2 \right)}$$

The investigation regarding the cross frequency on (19) has been revealed that the factor  $\delta(R_L, f_n)$  is much smaller than the value of the variable  $C_o/k_f$  in the practical application, then the cross frequency can be simplified further as:

$$f_{c\_Gvc} \approx \frac{1}{2\pi} \frac{k_{th}}{C_o} = \frac{C_s V_{in} F_s}{\pi \lambda V_o C_o} \quad (20)$$

Equation (20) shows that the cross frequency for the open control to output is firmly related to the operation frequency no matter whatever the output load is, which can be verified from the results shown in Fig. 11, where the cross frequency is proved not to be affected by the output load directly.



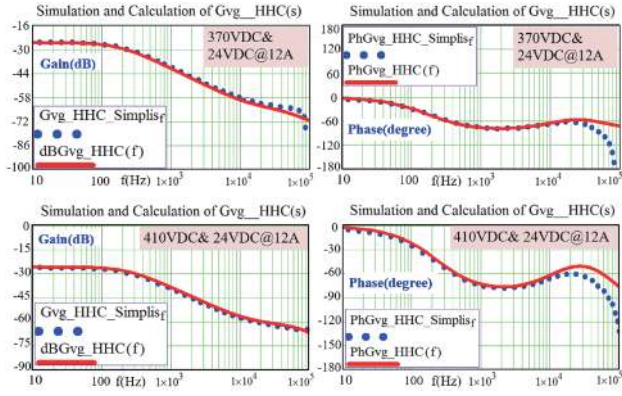


Fig. 12. Plot comparison of input to output between simulation and calculation under the condition of 370 VDC@24 VDC&12 A ( $f_n = 0.82$ ) and 410 VDC ( $f_n = 1.08$ ) @24 VDC&12 A.

Another scenario of  $f_n \leq 1$  can also be verified by using the same approach mentioned above. With this characteristic, it is concluded that the compensation circuit can be easily designed for the HHC control.

### B. Verification and Analysis on the Analytical Transfer Function of Audio Susceptibility

To investigate the audio susceptibility, the plot of open transfer function of the input to output is carried out. Fig. 12 illustrates such a result comparison between simulation and calculation in both the input condition of 370 VDC and 410 VDC. It is revealed that the mathematical calculation results match well with the simulation results except the occurrence of the error when the frequency goes up to half of the operation frequency.

As shown in Fig. 12, it can be seen the gain decreases more after the first poles  $\omega_T$  ( $f_n \leq 1$ ) and  $\omega_1$  ( $f_n \geq 1$ ). As for the practical applications where the ripple frequency of PFC is around 100 Hz, the closed audio acceptability shall be firmly related to the DC gain of the transfer function. Equation (21) shows the formulas of the DC gain based on the variables of output load and the normalized frequency, the approximated gain can be obtained by (22) at the operation condition of the resonant frequency. As for the conventional HC control, the DC gain can be obtained by setting  $k_{ramp}$  as zero based on (21)–(22).

$$G_{DC\_vg\_HHC}(R_L, f_n) = \frac{G_{DC\_vg}(R_L, f_n)}{2N \cdot R_L} - \left( \frac{V_o}{R_L} + \frac{2k_{ramp}N}{G_{DC\_vg}(R_L, f_n)} \right) \cdot \frac{G_{DC\_vg}(R_L, f_n)}{2f_n F_o N G_{DC\_vf}(R_L, f_n)}$$

$$\frac{2}{R_L} + \left( \frac{V_o}{R_L} + \frac{2k_{ramp}N}{G_{DC\_vg}(R_L, f_n)} \right) \frac{1}{(-G_{DC\_vf}(R_L, f_n)) f_n F_o} \quad (21)$$

$$DC_{Gvg\_HHC\_fo} \approx \frac{V_o + \left( V_o + \frac{V_{in} k_{ramp}}{I_o} \right) \frac{h}{2}}{2V_{in} + N \left( V_o + \frac{V_{in} k_{ramp}}{I_o} \right) h} \quad (22)$$

Fig. 13 illustrates the operation principle regarding the DC

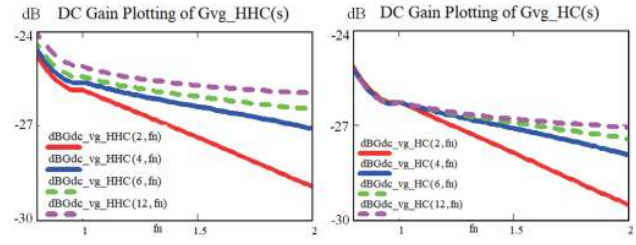


Fig. 13. DC gain plot of input to output under HHC control and conventional HC control.

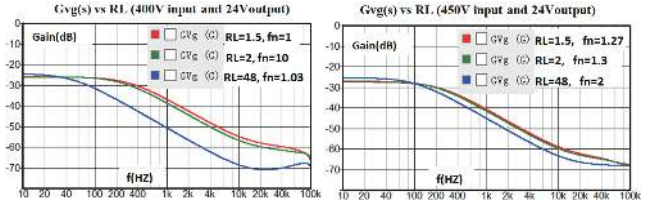


Fig. 14. Plot of input to output under the variation of output load.

gain versus output load for both the conditions under HHC control and HC control. It is revealed that the gain decreases with the increase of  $V_{in}$  or output current for HHC control. As shown in the left part of Fig. 13, the gain is with small variation when LLC operators near the resonant frequency ( $f_n = 1$ ) during the load range of 2 A to 12 A. However, it drops much as the output current increases. As a contrast, the gain nearly remains the same when LLC operates below the resonant frequency point ( $f_n < 1$ ) for the conventional HC control and the overall variation shall be relatively smaller than that in the HHC control.

To verify this principle for HHC control, the simulation is implemented to make load sweep analysis based on the transfer function of  $G_{vg\_HHC}(s)$  when input is 400 VDC and 450 VDC respectively. As shown in Fig. 14, the DC gain increases as output current decreases for both conditions, which matches the result obtained from Fig. 13, the overall variation is small when LLC operates at the resonant frequency point and the gain at 450 VDC is relatively smaller than that of the condition at 400 VDC, which is consistency with the calculation result in (21). With this analysis, we can refer to (22) for the further physical insight analysis regarding the practical design as far as the closed transfer function is concerned.

### C. Close the Voltage Loop

Based on the good match between theoretical calculation and simulation for the open loop control-to-output transfer function, the feedback voltage loop can be constructed for the overall closed loop stabilization. Fig. 15 shows two kinds of compensation circuit regarding the way of  $R_f$ 's power connection, one way is connecting to the output  $V_o$ , another way is connecting to a regulated voltage VDD. In this paper, let's take the second connection way for example, in which only the DC gain of the OPTO is considered to have a simple transfer function derivation for the compensation circuit.

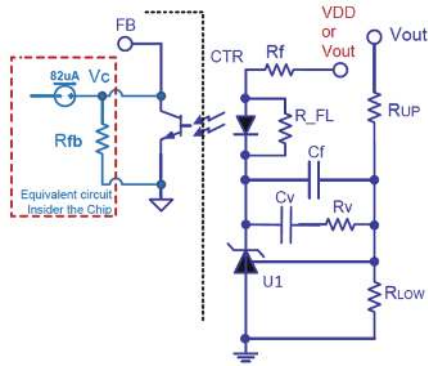
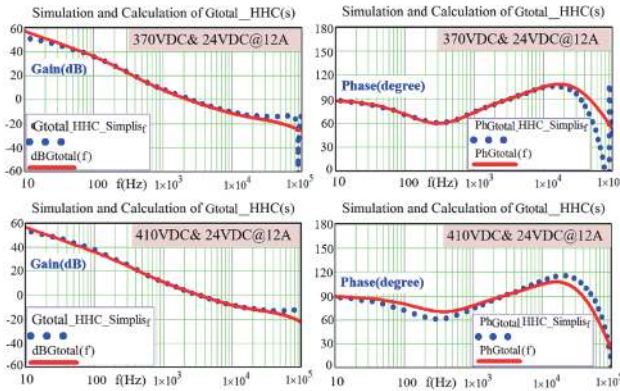


Fig. 15. Feedback circuit for the loop compensation.

Fig. 16. Overall loop plot comparison between simulation and calculation under the condition of 370 VDC@24 VDC&12 A ( $f_n = 0.82$ ) and 410 VDC ( $f_n = 1.08$ )@24 VDC&12 A.

Shown in Fig. 15, the parameters are set by  $R_{up} = 97.7 \text{ k}\Omega$ ,  $R_v = 60 \text{ k}\Omega$ ,  $C_v = 4.7 \text{ nF}$ ,  $R_f = 5 \text{ k}\Omega$ ,  $C_f = 20 \text{ pF}$ , and  $CTR = 0.35$ . Care need to be taken that the additional soft ramp circuit for the purpose of avoiding the output overshoot may be suggested to add in the practical design. As for the UCC25630x series, it is specially noted that the equivalent circuit consist of 82  $\mu\text{A}$  inner current source and  $R_{fb}$  insider the chip shall be considered to form a whole compensation circuit. Since  $V_{comp}$  in  $G_{vc\_HHC}(s)$  is 0.5 times of the voltage on  $R_{fb}$  inside the chip from Table II, we can use this value for the calculation. So, the transfer function for the compensation circuit can be obtained as:

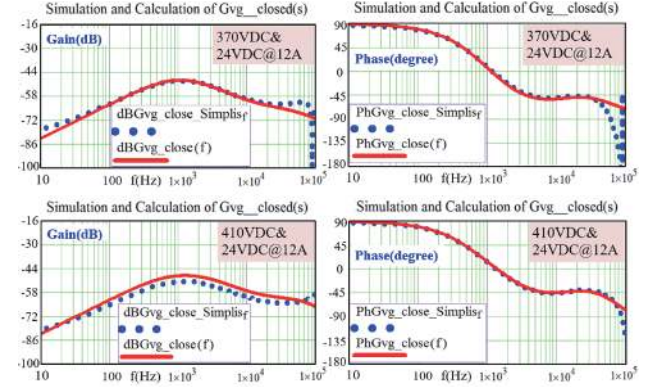
$$G_{cv}(s) = \frac{R_{fb} CTR}{R_f} \frac{1}{(C_v + C_f) \cdot R_{up}} \frac{1 + R_v C_v s}{\left(1 + \frac{s \cdot R_v C_v C_f}{C_v + C_f}\right) s} \quad (23)$$

The overall loop is then obtained as follows:

$$G_{total}(s) = G_{vc\_HHC}(s) G_{cv}(s) \quad (24)$$

Fig. 16 shows the plot comparison of the overall loop between simulation and calculation under the input condition of 370 VDC and 410 DC respectively.

It shows the good matched result between the simulation and calculation can be achieved within a wide range of

Fig. 17. Results comparison of closed audio susceptibility between simulation and calculation under the condition of 370 VDC@24 VDC&12 A ( $f_n = 0.82$ ) and 410 VDC ( $f_n = 1.08$ )@24 VDC&12 A.

frequency, in which both the cross frequency and phase margin are nearly the same. The cross frequency of the closed loop is nearly in proportion to the operation frequency in these two conditions.

#### IV. CHARACTERISTICS UNDER LINE CHANGE AND LOAD CHANGE

##### A. The Closed Audio Susceptibility and Characteristic of AC Ripple Rejection

Based on  $G_{vg\_HHC}(s)$  shown in Table I, the closed audio susceptibility can be obtained as follows:

$$G_{vg\_closed}(s) = \frac{G_{vg\_HHC}(s)}{1 + G_{vc\_HHC}(s) \cdot G_{cv}(s)} \quad (25)$$

To verify the result at the condition of 12 A output, the comparison between simulation and calculation under 370 VDC and 410 VDC can be obtained as shown in Fig. 17.

It can be seen the good matched results can be achieved between the simulation and calculation and then it can be proposed to evaluate converter's line regulation by applying into the time domain.

To characterize the input voltage rejection, the PFC input voltage is applied by a combined value of DC part and AC ripple part. Based on the AC line frequency of  $F_{line}$ , the AC voltage part can be written as:

$$V_{in\_AC}(t) = V_{PFC\_AC} \sin(2\pi F_{line} t) \quad (26)$$

So, the corresponding output voltage can be calculated as:

$$V_{o\_in}(t) = V_{o\_DC} + V_{in\_AC}(t) G_{vg\_closed}(j \cdot 2\pi F_{line}) \quad (27)$$

Take the condition of  $f_n > 1$  for example, when the input varies from 405 V to 425 V based on an AC line frequency of 100 Hz, the calculation result of output from (27) is shown in the right part of Fig. 18, it reveals the average variation of

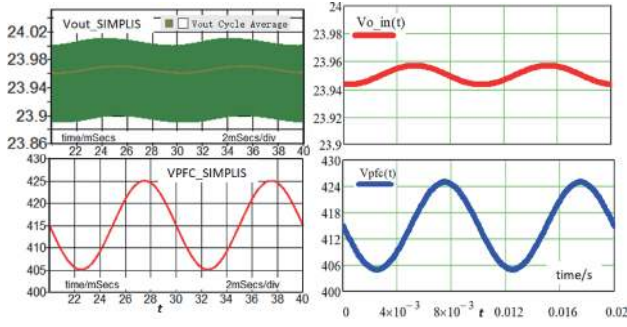


Fig. 18. Comparison of the output between calculation and simulation, in which PFC is with a 20 VAC ripple based on the input of 415 VDC.

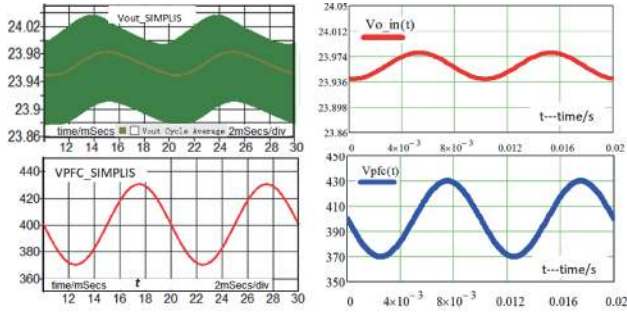


Fig. 19. Comparison of output between calculation and simulation when PFC is with 60 V's AC ripple based on 400 VDC input.

output ripple is only 20 mVDC, which is consistent with the result of simulation shown in the left part of Fig. 18.

To demonstrate the input ripple rejection characteristic further, a big ripple of 60 VAC is applied based on the 400 VDC under the same line frequency, the comparison results between simulation and calculation are obtained as shown in Fig. 19, which is observed that the output variation from the calculation is 38 mV, which matches well with the simulation result.

So, it is concluded that the LLC HHC control has the advantage over the conventional DFC control regarding the input voltage rejection, which means the decreased value of PFC electrolytic capacitors for HHC control will not affect the performance of output characteristic.

### B. The Closed Output Impedance and Dynamic Load Transient Characteristic

Since the transfer function of open output impedance is derived in Table II, it can be used to obtain the closed output impedance, which is shown as:

$$Z_{\text{out\_closed}}(s) = \left. \frac{\Delta v_o}{\Delta i_o} \right|_{\text{closed}} = \frac{-Z_{o\_HHC}(s)}{1 + G_{ve\_HHC}(s)G_{cv}(s)} \quad (28)$$

The comparison between simulation and calculation under the input condition of 370 VDC and 410 VDC and the output condition of 24 VDC&12 A can be obtained from Fig. 20. It shows the results match well over a wide frequency range,

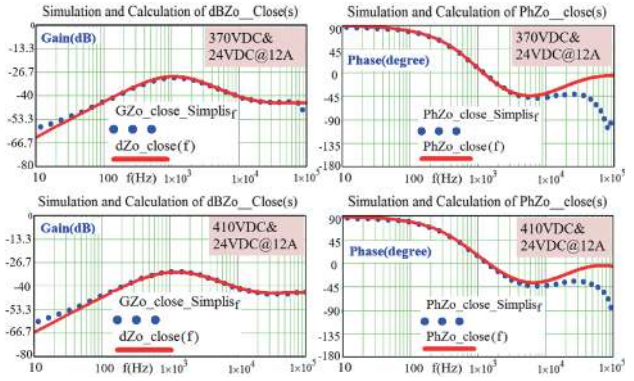


Fig. 20. The plot comparison of closed output impedance between simulation and calculation under the condition of 370 VDC@24 VDC&12 A ( $f_n = 0.82$ ) and 410 VDC ( $f_n = 1.08$ ) @24 VDC&12 A.

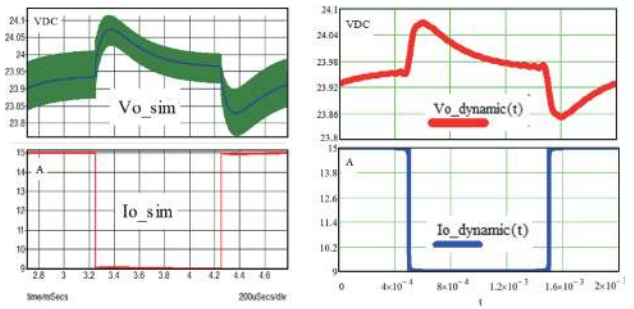


Fig. 21. Results comparison between simulation and calculation under the condition of 410 VDC input and 24 VDC&9 A-15 A-9 A output.

especially for the bode plot. However, there is some variation for the phase comparison when frequency approaches the operation frequency. Further investigation shows it is caused by the non-precise zeros of  $Z_{o\_HHC}(s)$  occurred in the high frequency range due to the averaged concept employing on a simplified LLC tank model [22]–[23], which has been hard for us to obtain the precise high frequency dynamics. However, the phase calculation will match the simulation well if the high frequency zeros are assumed high beyond the operation frequency. Then the closed output load dynamic response can be investigated through the conversion from frequency domain into time domain based on (28).

Since the dynamic step load can be simplified by a squared wave with a certain repetition frequency  $f_{is}$ , the equation for the square wave under the transient frequency  $f_{is}$  can be expressed as a Fourier series, which is given by:

$$i_{o\_dynamic}(t) = \frac{2I_{\text{step}}}{\pi} \cdot \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{2n-1} \cos((2n-1) \cdot 2\pi f_{is} t) \quad (29)$$

where  $I_{\text{step}}$  is the load step and the corresponding output voltage can be calculated as:

$$V_{o\_dynamic}(t) = V_o + i_{o\_dynamic}(t) Z_{\text{out\_closed}}(j \cdot 2\pi f_{is}) \quad (30)$$

Fig. 21 shows the comparison results between simulation and calculation under the input condition of 410 VDC and

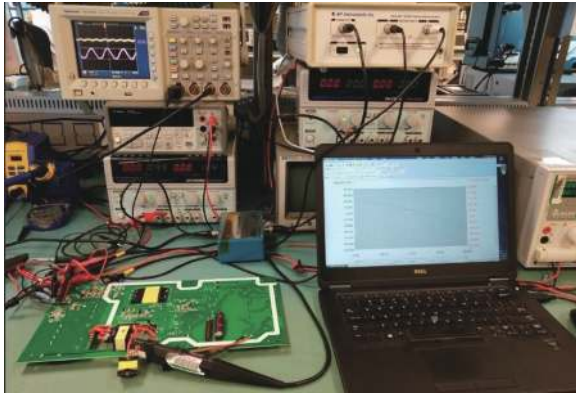


Fig. 22. The loop verification platform based on a TV power board.

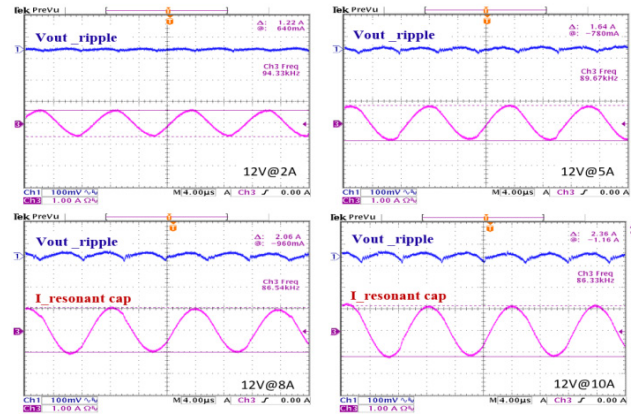


Fig. 23. Waveforms of output ripple and current of resonant tank under the output condition of 12 VDC @2 A, 5 A, 8 A and 10 A.

TABLE III  
PARAMETERS OF LLC CONVERTER FOR THE EXPERIMENT

| Parameter    | Description                                | Value          |
|--------------|--------------------------------------------|----------------|
| $V_{in}$     | Nominal input PFC voltage [VDC]            | 398            |
| $V_o$        | Nominal output voltage [VDC]               | 12             |
| $I_{o\_max}$ | Maximum output current [A]                 | 12             |
| $C_s$        | Resonant Tank capacitor [nF]               | 27             |
| $L_s$        | Resonant Tank conductance [ $\mu$ H]       | 107            |
| $L_m$        | Magnetizing conductance [ $\mu$ H]         | 840            |
| $N$          | Transformer ratio $N_p/N_s$ [ $\mu$ H]     | 32/2           |
| $C_{divH}$   | $U_{CS}$ scaling capacitor (upside) [pF]   | 82             |
| $C_{divL}$   | $U_{CS}$ scaling capacitor (downside) [nF] | 8.2            |
| $C_o$        | Output capacitor [ $\mu$ F]                | 330 $\times$ 5 |
| $R_c$        | ESR of output capacitor [mR]               | 28/5           |
| CTR          | CTR of OPTO                                | 0.4            |

the output load condition of 24 VDC&9 A-15 A-15 A. It can be observed that the result of calculation matches well with the simulation result.

### V. EXPERIMENTAL VERIFICATION

Shown as in Fig. 22, the proposed analytical small signal transfer functions regarding the open control to output loop and the closed overall loop can be verified further through the experiment on a 70"250 W TV power board by using UCC256304, in which, the output is 12 VDC&12 A. The main design parameters are given in Table III.

Based on the dead time setting of 200 ns, the operating frequency on the design board is: 94.3 kHz for 2 A, 90.5 kHz for 4 A, 89.6 kHz for 5 A, 88.5 kHz for 6 A, 86.5 kHz for 8 A and 86.3 kHz for 10 A. The steady operation waveforms are shown in Fig. 23, in which the output ripple and the current through the resonant inductor are given. For the loop measurement, the AP instruments Model 300 is used as shown in Fig. 22. In order to obtain the plant loop, a 50 k $\Omega$  resistor is used to be in series with the lower output side of the OPTO FOD817A for the  $V_c$  pin measurement.

The open loop of power plant stage can be measured from UCC256304's FB voltage, which is actually located on the terminal of the added 50 k $\Omega$  resistor from the lower output side of FOD817A. Fig. 24 shows the plot comparison results between the measurements and the calculations when it

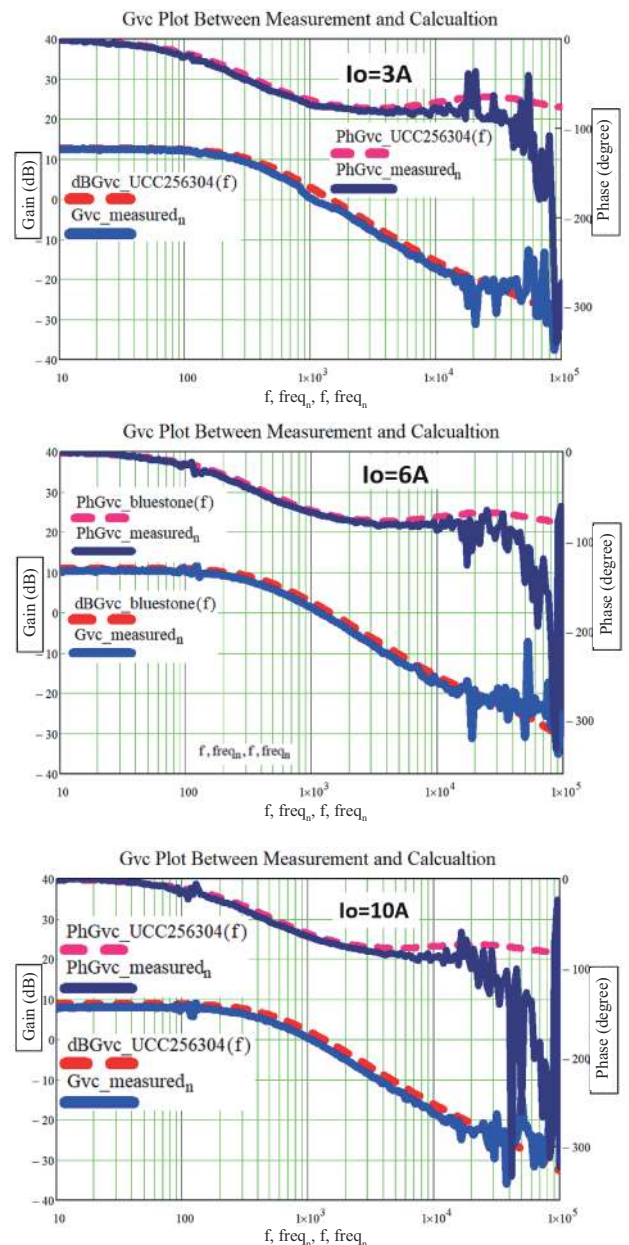


Fig. 24. Control to output plot comparison between measurement and calculation under the steady operation of 3 A, 6 A and 10 A output.

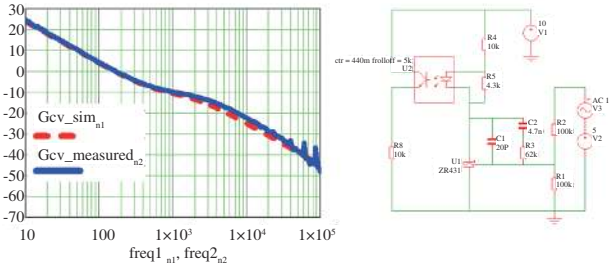


Fig. 25. Compensation plot comparison between simulation and measurement.

operates at 3 A, 6 A and 10 A respectively. The solid green lines represent the measurement results and the red dashed lines represent the calculation results, which show that these results match well practically. Though there may be concerns of dead time, it does not have impact from the prediction of the calculations if the frequency is given correctly. It is obvious to observe that the DC gain decreases with the increase of output current but the variation is relatively small compared to other hysteretic charge LLC converter. The cross frequency nearly remains the same result since the frequency variation is relatively very small.

To verify the transfer function of the overall loop, a practical precise model for the compensation circuit is required for this purpose because the transfer functions (23) is not with the consideration of the roll off frequency for FOD817A and TL431, which is necessary to obtain in practical measurement. Fig. 25 shows such a simulation example by pulling a 10 kΩ resistor at the emitter pin side of the opto-coupler for the rolling off frequency identification, in which the CTR is measured by 0.44 and the roll off frequency is verified to be 5 kHz. Refer to Fig. 15, with the other compensation parameters being set by  $C_v = 4.7$  nF,  $C_f = 20$  pF,  $R_v = 62$  kΩ,  $R_{up} = 100$  kΩ and  $R_f = 10$  kΩ, the open loop plot of output to control can be obtained through simulation and measurement. Shown in Fig. 25, it can be seen the simulation result marked by the dashed red line matches well with the measurement result marked by the green solid line. With this consideration, a roll off pole is therefore added into (23) additionally, so the overall loop can be calculated precisely.

Fig. 26 shows the measurement results for the overall loop under the output of 12 VDC&4 A and 12 VDC&10 A respectively, it can be observed both the cross frequency and phase margin are featured by a very small variation under the two kind of output conditions, which is a special and comforting result characterized by HHC control.

To verify the result of the calculation by (24), the comparison between calculation and measurement are obtained under the output of 12 VDC&6 A. Shown in Fig. 27, the upside figure presents the measurement result and the downside figure shows the comparison under the output of 6 A. It reveals that the measurement result marked by solid line match very well with the calculation result marked by a dashed line up to half of the operating frequency.

In order to verify the characteristic under dynamic load condition, the waveforms of output voltage and resonant

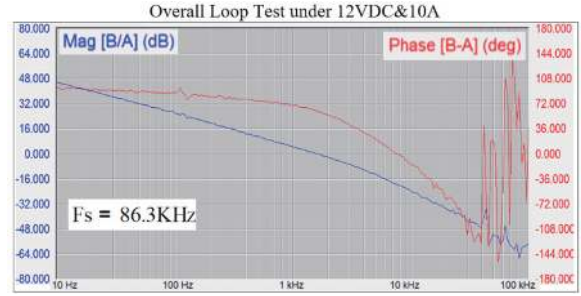
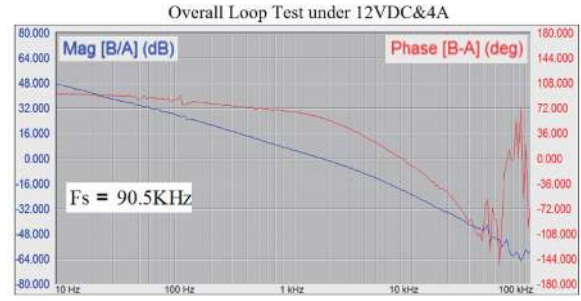


Fig. 26. Measurement results for the overall loop under the output condition of 12 VDC&4 A (upside) and 12 VDC&10 A (downside).

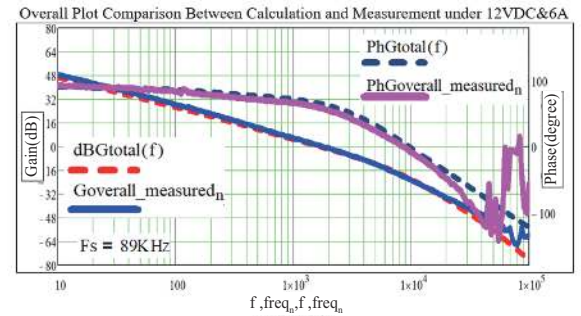
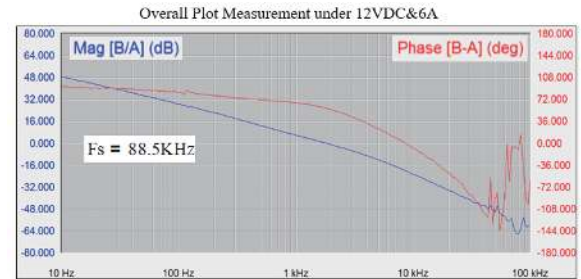


Fig. 27. Overall loop measurement under the output of 12 V&6 A (on the topside) and the related comparison between the measurement and calculation (on the downside).

tank current are measured under the dynamic load condition of 12 VDC&(4 A-8 A-4 A) and 12 VDC&(8 A-12 A-8 A). Shown in Fig. 28, it can be observed the good dynamic performance can be achieved.

To verify the transfer function of closed output impedance given by (28), the dynamic load measurement is conducted based on a step current of 4 A-8 A-4 A with the slew rate setting by 3 A/us and step period-setting by 1 ms. Fig. 29 shows such a comparison between calculation and measurement. It can be observed both results match well, which proves that the closed impedance is with good practical use for the practical design and applications based on LLC HHC control.

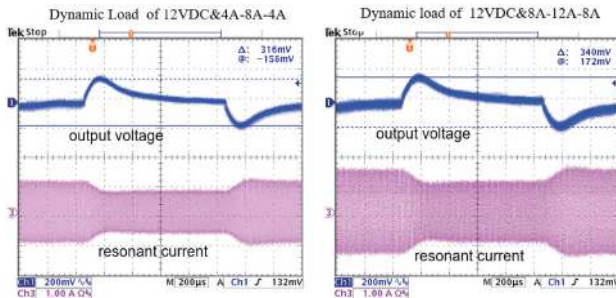


Fig. 28. Measurement of output voltage and resonant tank current.

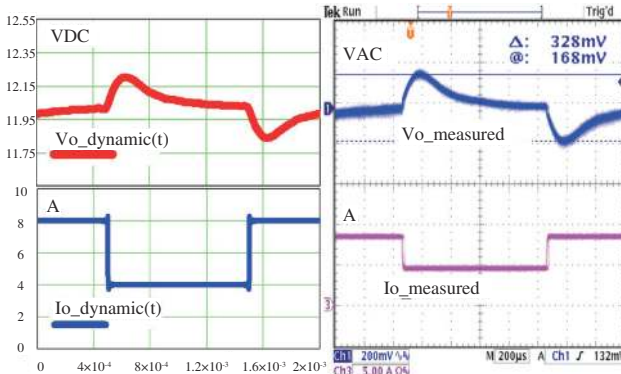


Fig. 29. Dynamic load response between calculation and measurement under the condition of 370 VDC input and 12 VDC&amp;6 A output by 4 A-8 A-4 A.

## VI. CONCLUSIONS

In this paper, the LLC HHC control has been introduced with the advantage of easy loop compensation and good dynamic characteristic compared to the conventional DFC control. The analytical small signal transfer functions applied for this control method have been therefore proposed and illustrated, in which the transfer functions of control to output, input to output, output impedance and the closed overall loop have been elaborated and verified. The overall comparison results based on the proposed transfer functions have been proved to match well with both the results from simulation and measurement in the most part of operating frequency range. More importantly, some physical insights related to the transfer functions are extracted and the design guideline for practical applications has been provided.

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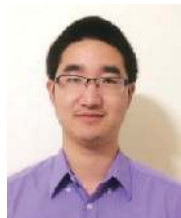
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