INVESTMENT DIVERSIFICATION AS A STRATEGY FOR REDUCING INVESTMENT RISK

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Investment diversification is a widely accepted investment strategy, aimed at reducing investment uncertainty, while simultaneously keeping the expected return on investment unaltered. The development of investment diversification coincided with the development of portfolio theory. At the time when traditional portfolio theory was recognized as the leading portfolio management practice, the simple diversification of investments was the most commonly used strategy; however, due to its inability to recognize the importance of the correlation between returns on different investments, simple diversification was later rejected in modern portfolio theory and replaced with efficient diversification. The research study is aimed at conducting a comparative analysis between the simple and efficient diversifications of investments, together with the inevitable analysis of the optimal number of securities in a portfolio and the testing of the validity of the international diversification of investments. By applying a qualitative research methodology, it is concluded that the benefits of the international diversification of investments are still substantial, and as such outweigh specific limitations, and that the number of securities in a portfolio should be increased as long as its marginal benefits, in the form of reduced investment risk, exceed its marginal costs – in terms of increased portfolio management costs, which also represents the main result of the research.

Keywords: simple diversification, efficient diversification, national diversification, international diversification

JEL Classification: G11

INTRODUCTION

Economic reality undoubtedly confirms the existence of the interrelatedness of and correlation between return and risk as the basic postulates of modern financial theory. Due to the fact that return and risk are interdependent, any rational investor, in addition to estimating a future, expected return, seeks to identify and assess the risk of certain investment alternatives. In this regard, achieving the expected return is the key driver of an investment activity, while its maximization at the given level of risk is the main goal pursued by any investor.
An investor who knows future returns with certainty will invest in only one security, namely the one with the highest future return (Markowitz, 1999). However, being certain about what the future holds is quite an unrealistic assumption that ignores risk and oversimplifies the investment process. Modern investors do not concentrate their wealth in a single security or a single type of securities; they rather invest their assets in different types of securities, thus building a diversified portfolio.

In terms of finance, an investment portfolio is a collection of different types of investments, i.e. a mix of different financial instruments held by investors. Holding a securities portfolio is a part of the investment strategy called the diversification of investments, which is carried out in order to reduce the total variance of a portfolio without changing the expected return. A simpler way to reduce portfolio risk is to allocate a portion of assets to risk-free assets. However, this strategy of risk reduction, quite opposite to diversification, would result in lower expected portfolio returns.

With regard to the above-mentioned, this research focuses on the analysis of the development process of the diversification of investments as an established investment risk reduction strategy.

The aim of the research is to examine the positive and negative aspects of the simple and efficient diversifications of investments, including the ever-present issue related to the selection of the optimal portfolio size and the comparison of the potential benefits and limitations of the international diversification of investments.

In accordance with the subject matter of the research study and the defined research goal, the initial hypothesis set out in this paper reads as follows:

H: The international diversification of investments, compared to the national diversification, achieves the same or a higher level of the expected return, including a further investment risk reduction.

The qualitative research method, based on the analytical description, is used in this study. This methodological toolkit makes it possible for the author to produce relevant conclusions about the research topics, based on the study of the relevant and for the most part foreign literature.

Taking into account the defined subject, goal and hypothesis, after the introductory considerations and the review of the relevant literature, this paper presents the analysis of the differences between the simple and the efficient diversifications of investments, which is followed by the identification of the disadvantages and limitations of diversification as an investment strategy. The paper continues by presenting the potential benefits and limitations of the international diversification of investments. In the last, concluding section of the paper, the opinions about the confirmation of the initial hypothesis are presented and the implications for future research considered.

LITERATURE REVIEW

The common concept of portfolio theory is that by combining different assets one can achieve better results than by simply investing funds in a single asset. The often-cited recommendation in the financial literature on how to allocate one’s funds was written down in the IV century and reads as follows: “put a third in land, a third in merchandise and a third in cash”. Although this idea had been around for centuries, it is during the mid-XX century that it actually took shape. In fact, before the emergence of modern portfolio theory (MPT), investors had used to construct their portfolios without considering the degree of the correlation between returns on different investment assets. The main disadvantage of this type of diversification, known as simple (naive) diversification, is that efficiency decreases as the number of assets in a portfolio increases (Jakšić & Leković, 2015, 32). Being based on the “law of large numbers” - i.e. on holding a large number of securities in a portfolio, simple diversification results in an excessive diversification, which in turn results
M. Lekovic, *Investment diversification as a strategy for reducing investment risk*

High portfolio management costs. According to J. C. Francis and D. Kim (2013), simple diversification can reduce portfolio risk, but cannot minimize it since it ignores the correlation between returns on different assets.

Simple diversification and the application of the law of large numbers were first rejected by H. M. Markowitz (1952). The author points out that a portfolio with 60 different securities from a single industry would not be as well diversified as a same-size portfolio with securities from different industries. According to H. M. Markowitz (1952), if one wants to make the variance small, it is not enough to invest in many securities, but it is necessary to avoid investing in securities with high covariances among themselves instead. Accordingly, H. M. Markowitz (1952, 89) suggests that we should diversify across different industries since companies in different industries, especially the industries with different economic characteristics, have lower covariances than the companies within a single industry. Therefore, H. M. Markowitz (1952) identified the importance of the correlation between the returns of individual securities in a portfolio; in this respect, a lower value of the correlation coefficient implies greater benefits from diversification. The founder of the MPT favors efficient diversification instead of simple diversification, i.e. recommends investing in low-correlated securities.

Unsystematic risk can be eliminated by efficient diversification, while the total investment risk can be reduced to the level of systematic risk. In the case of efficient national diversification, the lower limit in terms of risk reduction is actually the level of national systematic risk. However, in addition to national diversification, investors can also opt for international diversification. H. G. Grubel (1968) first pointed to the importance of international diversification and the possibility of reducing portfolio risk below the level of systematic risk. His viewpoint was supported by B. H. Solnik (1974), H. Levy and Z. Lerman (1988), W. Bailey and R. M. Stulz (1990) and the many others who emphasized the advantages of constructing an internationally diversified portfolio, i.e. the benefits of investing money in foreign securities. Unfortunately, due to the growing international market integration, the benefits of international diversification are being reduced - however, they are still significant and evident. The substantial benefits of international diversification are also supported by the research carried out by K. Li, A. Sarkar and Z. Wang (2003), R. Gupta (2006), W. J. P. Chiou (2009), C. S. Asness, R. Israelov and J. M. Liew (2011), O. Bouslama and O. B. Ouda (2014), G. Mansourfar, H. Didar and S. Jodatnia (2017) and others. K. Li et al. (2003), R. Gupta (2006) and O. Bouslama and O. B. Ouda (2014) point out the fact that although the growing integration of different capital markets reduces the benefits of investing in foreign markets (especially the emerging markets), this does not necessarily mean that it eliminates them. The authors agree that emerging markets still represent an important component of a well-diversified portfolio. P. Christoffersen, V. R. Errunza, K. Jacobs and H. Langlois (2012) came up with the evidence supporting the aforementioned statement. The authors used the weekly rates of return of a large number of countries for the period 1973-2009, and found an increasing correlation between developed markets, as well as between emerging markets; the important conclusion of their research is that investing in emerging markets still brings significant benefits to investors.

In addition to selecting an optimal method for diversification, economists have been trying to determine an optimal number of securities in a portfolio for decades. The first study which measured the effects of an increase in the portfolio size on risk reduction for the purpose of determining the optimal size of a portfolio was carried out by J. L. Evans and S. H. Archer (1968), who found that, eight to ten securities in a portfolio on average are sufficient to achieve the largest number of benefits from diversification. The authors argue that a portfolio consisting of 15 securities is fully diversified, for which reason any further increase in the number of the securities held in that portfolio does not affect risk reduction. M. Statman (1987) rejected the above conclusion based on his research, which showed that an optimally diversified portfolio must include 30 securities at least. J. Y. Campbell, M. Lettau, B. G. Malkiel and Y. Xu (2001) point out that the number of the securities required in order to achieve the
optimal portfolio diversification increases with an increase in unsystematic risk. The authors divided the observed period from 1963 to 1997 into the three sub-periods: 1963-1973, 1974-1985 and 1986-1997. They concluded as follows: in terms of the first two sub-periods, most of the benefits from diversification were achieved by investing in 20 securities, whereas the similar effects of the diversification in the third sub-period were achieved by investing in 50 securities. H. Benjelloun (2010) came to a similar conclusion about the optimal size of a portfolio and an increase in the optimal number of the securities held in a portfolio. He pointed out that, in order to achieve a sufficient diversification of investments, a portfolio must include between 40 and 50 securities.

While examining the efficiency of simple diversification, G. Y. N. Tang (2004) came to a conclusion that a 20-stock portfolio was good enough in terms of eliminating 95% of unsystematic risk, whereas the additional 80 stocks (the 100-stock portfolio) were required for the elimination of the additional 4% of such unsystematic risk (99% of unsystematic risk). M. Statman (2002, 2004) and D. L. Domian, D. A. Lawton and M. D. Racine (2007) argue that the optimal number of stocks in a portfolio has increased from 10 to 15 stocks at the beginning of the 1950s to a hundred and over a hundred shares at the beginning of the XXI century.

Based on the example of the capital markets of the USA, the UK, Japan, Canada and Australia, V. Alexeev and F. Tapon (2013a) proved that the optimal number of securities in a portfolio depended on market conditions, and that this number increased during the periods of the financial and economic crisis. In this regard, the different capital markets have established different optimal portfolio sizes. Based on the survey they had conducted in the capital markets of Australia, V. Alexeev and F. Tapon (2013b), concluded that 24 to 30 shares were sufficient to construct a well-diversified portfolio. In terms of the capital market of Canada, the same authors found that the optimal portfolio size was that exceeding 50 shares (Alexeev & Tapon, 2014). The results of the research carried out by M. R. Sarker (2013) in the capital market of Bangladesh indicate that the optimal portfolio consists of 33 shares, whereas the optimal number of shares in a portfolio in the capital market in Kenya, ranges from 18 to 22 shares, according to a survey conducted by S. E. Kisaka, J. A. Mbithi and H. Kitur (2015).

It should be noted that the research findings referring to the optimal size of a portfolio in the bond market are highly correlated with the findings relating to the stock market. The results of the study carried out by W. R. McEnally and M. C. Boardman (1979) indicate that between eight and 16 securities should be included in a portfolio so as to significantly reduce volatility, whereas recent studies, such as those conducted by W. Dbouk and L. Kryzanowski (2009), suggest that an optimal portfolio should include a greater number of components, which is generally estimated to be between 25 to 40 securities.

THE SIMPLE AND EFFICIENT DIVERSIFICATIONS OF INVESTMENTS

The traditional approach to increasing the number of securities in a portfolio for the purpose of reducing the total risk is known as simple (naive) diversification. According to this approach, investing in 100 different securities is ten times less risky than investing in 10 securities. The simple diversification of investments, based on the law of large numbers, was supported by the proponents of traditional portfolio theory: J. R. Hicks (1935), J. B. Williams (1938), D. H. Leavens (1945) and others, who separately evaluated individual securities, i.e. they did not make investment decisions within the context of a particular portfolio. Furthermore, they were not interested in determining the correlation between returns on individual securities within a portfolio. Traditional portfolio theory and its proponents did not recognize the importance of correlation for a portfolio construction. Correlation is important because it is essential for us to think about and make decisions based on the entire portfolio, rather than on individual securities. According to traditional portfolio theory, if investors want to eliminate risk, they should invest in a large number of securities; therefore, during the period when traditional portfolio theory was considered to
be the most influential concept, portfolio performance was evaluated solely based on the actual return.

In addition to completely ignoring correlation, another important disadvantage of simple diversification is, usually, reflected in an excessive number of securities held in a portfolio. An excessive number of components in an investment portfolio lead to the high transaction costs related to both portfolio construction and portfolio management. Therefore, it can be concluded that simple diversification represents a traditional approach to diversification; however, it is still applied in practice by those investors and portfolio managers who use heuristics (mental shortcuts), such as the application of the 1/N rule.

Unlike traditional portfolio theory and simple diversification as its main characteristic, the MPT has shifted the emphasis from the analysis of the characteristics of the individual securities held in a portfolio to the analysis of the characteristics of the entire portfolio, simultaneously underlining the importance of the correlation between returns on held securities. If investors seek to reduce portfolio risk, they should not invest in a large number of different securities; they should rather invest in low-correlated securities (Jaksic, 2012, 161). H. M. Markowitz (1952) provided the mathematical proof that a proper diversification can indeed minimize the variance of a portfolio for a given level of return. He was the first scientist and author to have formally quantified the return-risk trade-off. Understanding the nature of the correlation between returns on different assets enabled the construction of the sets of the efficient portfolios that minimize risk for a given level of return, i.e. they maximize return for a given level of risk.

According to H. M. Markowitz (1952), efficient diversification implies that investors should avoid securities with high covariances among themselves when constructing their investment portfolios. In an extreme case of perfectly positively correlated securities, diversification has no effect on risk. However, in all other cases, namely in every instance where the correlation between returns on the securities is less than perfectly positive, such a diversification will help reduce risk without sacrificing the expected return. The strongest positive effects of diversification can be achieved if all of the elements of a portfolio are perfectly negatively correlated. However, a perfect negative correlation, i.e. the complete canceling out of the variability of returns on securities against each other is not realistic; this is rather an idealized image of reality. It is difficult to find uncorrelated or negatively correlated securities on financial markets. The most common case is a moderate positive correlation, which moderately adds to reducing portfolio risk.

Figure 1 shows the effect of Markowitz’s efficient diversification for a portfolio composed of two securities: Security B and Security A.

![Figure 1 The effect of Markowitz’s efficient diversification](source)

All the possible combinations of the positively correlated ($\rho = +1$) B and A securities are represented by the straight line BA. Each point on this line marks the portfolio whose characteristics match the weighted characteristics of its components. This means that by combining the perfectly positively correlated A and B securities portfolio risk can be reduced; however, the expected return is also reduced in this manner.
Starting from the point B and moving towards the point A, the expected return and portfolio risk grow due to the fact that the share of the riskier security that offers a higher return also increases. Starting from the opposite direction, i.e. from the point A and moving towards the point B, we see that both the expected return and portfolio risk become reduced. This supports the conclusion that diversification does not produce any benefits in the case of a perfect positive correlation among portfolio components.

On the other hand, all of the combinations of the negatively correlated ($\rho = -1$) B and A securities are distributed along the two straight lines, the one of which (the line BC) is negatively inclined, whereas the other (the line CA) is positively inclined. Moving from the point B towards the point C implies the inclusion of the riskier security A in the portfolio, which results in a decrease in the standard deviation of the portfolio and a concurrent increase in the expected return. If we were to assume an infinite divisibility of the observed securities, portfolio risk should be reduced to zero at the point C. Therefore, portfolio diversification provides the complete stabilization of returns at the point C. This is the ideal situation achieved due to a perfect negative correlation between the elements of a portfolio. By including the additional, riskier security A, portfolio returns continue to grow along the positive slope of the line CA; however, this is accompanied by a certain increase in portfolio risk (Figure 1).

Finally, by connecting the described straight line BA with the lines BC and CA, we obtain a triangle BCA, within which all of the combinations of the imperfectly correlated ($-1 < \rho < +1$) B and A securities represented by the respective BA curves are contained. It is important to note that the curves BA initially have a negative slope due to the fact that the introduction of the riskier security A causes portfolio risk to briefly decrease because the correlation is less than perfectly positive. As the correlation coefficient decreases, the curves BA shift to the left, which actually illustrates an increase in benefits from diversification in terms of the stabilization of portfolio returns. Therefore, in the case of imperfectly correlated securities, portfolio risk is located between the zero value, attained due to the perfect negative correlation, and the maximum value, achieved as a result of an ideal positive correlation among the elements of a portfolio. The general conclusion is that an efficient diversification implies, as well as requires, a low coefficient of correlation (Figure 1).

According to M. Rubinstein (2002), H. M. Markowitz was hardly the first to recognize the desirability of diversification; however, he indeed was the first person to produce a mathematical formalization of the idea of the diversification of investments. H. M. Markowitz (1952, 77) rejects the rule that the investor should maximize discounted expected returns. This rule does not imply diversification, which is why it is rejected both as a hypothesis and as the maximum to guide investment behavior. According to H. M. Markowitz (1999), the existence of uncertainty in terms of investment is the essential point in analyzing the behavior of a rational investor, whereas the diversification of investments is a reasonable and common practice, as it reduces the mentioned uncertainty.

The effect of the efficient diversification on reducing the mentioned uncertainty, i.e. investment risk, can be mathematically interpreted. The general formula used for the portfolio variance calculation is written as follows (Elton, Gruber, Brown & Goetzmann, 2011, 58):

$$\sigma_p^2 = \sum_{i=1}^{n} w_i^2 \sigma_i^2 + \sum_{i=1}^{n} \sum_{j=1, i \neq j}^{n} w_i w_j \sigma_{ij},$$

(1)

where:

$\sigma_p^2$ - the variance of the portfolio $p$,

$w_i$ - the share of the $i$-th security in the portfolio,

$w_j$ - the share of the $j$-th security in the portfolio,

$\sigma_{ij}$ - the covariance between returns on securities $i$ and $j$,

$n$ - the number of the securities held in the portfolio.

Assuming that all the elements of a portfolio are uncorrelated, i.e. that the covariance between their returns is equal to zero ($\sigma_{ij} = 0$), we rewrite the previous expression as:
\[ \sigma_p^2 = \sum_{i=1}^{n} w_i^2 \sigma_i^2. \]  

(2)

By introducing the additional assumption of the equal amount of the funds invested in each security \( w_i = \frac{1}{n} \), Equation (2) is written as follows:

\[ \sigma_p^2 = \sum_{i=1}^{n} \left( \frac{1}{n} \right)^2 \sigma_i^2 = \frac{1}{n} \sum_{i=1}^{n} \sigma_i^2 = \frac{1}{n} \sigma_i^2. \]  

(3)

The effect of efficient diversification on portfolio risk reduction, represented by the equation \( \sigma_p^2 = \frac{1}{n} \sigma_i^2 \), is evident. It is clear that the portfolio risk expressed by the variance \( \sigma_p^2 \) decreases as the number of the uncorrelated elements of the portfolio \( n \) increases. For an extremely large number of uncorrelated elements in a portfolio, the portfolio variance approximates to zero.

However, in a real market environment, it is impossible to construct a portfolio which only includes uncorrelated securities; therefore, the effects of the diversification of investments are significantly weaker. Uncertainty cannot be completely eliminated solely by diversification. The idea is to eliminate unsystematic risk, thus leaving only systematic risk, which is defined by the beta (Vincent, 2011). If an investor implements effective diversification, his/her portfolio will not contain unsystematic risk (the risk inherent in the issuer’s company, such as insolvency risk, failed promotional activities, labor strikes, etc.), but only systematic risk (the risk inherent in the entire market, such as the interest-rate risk, foreign-exchange risk, inflation risks, etc.). Systematic risk is the risk compensated for by the market itself, whereas unsystematic risk is the risk which cannot be compensated for. Therefore, in terms of appropriately constructed portfolios, systematic risk - the risk that cannot be eliminated by implementing diversification - is the only type of risk considered as relevant.

Some authors, including I. Omisore, M. Yusuf and N. Christopher (2012), have quite interestingly put forward the idea that unsystematic risk can be eliminated by diversification; however, this is followed by an increase in systematic risk. Diversification compels portfolio managers to invest in different types of assets, thereby artificially increasing demand for such assets. In this way, this artificially increased demand drives up the asset prices, which if analyzed individually have a small real value. Therefore, the entire portfolio becomes more expensive, which in turn results in a lower probability of achieving the expected positive return, i.e. leads to an increase in portfolio risk.

Bearing this in mind, it can be concluded that effective diversification is desirable; however, it is not a perfect investment strategy. The benefits of diversification in terms of maintaining the same level of a portfolio’s expected return (while reducing portfolio risk at the same time) achieved by combining assets with low or even negative correlation are evident. However, the problem here is to find negatively correlated assets since the most common type of correlation present in modern financial markets is a positive one. Also, in the conditions of a financial and economic crisis, correlation coefficients are close to 1, thereby reducing or completely eliminating the benefits of diversification. This is the major disadvantage of such an investment strategy because, if diversification does not produce the expected results in a situation when investors need to be protected from risk, the general usefulness of diversification must be considered. A financial and economic crisis and attempts to lower correlation coefficients are the factors that drive investors to invest their available funds not only in securities (primarily stocks and bonds), but also in new assets, such as precious metals, oil, real estate, works of art, and so on, and to include such assets in their portfolios. It should be noted that during financial and economic crises, the optimal number of securities held in a portfolio increases, which imposes higher costs in terms of portfolio management.

Certain empirical studies suggest that in the absence of constraints a simple diversification of investments is a more successful investment strategy in terms of reducing investment risk compared to efficient diversification. Based on the conducted comparative
V. DeMiguel, L. Garlappi and R. Uppal (2009) determined that 14 optimal portfolio strategies showed inferior performance in comparison to the naive 1/N strategy. The authors specify the length of the time period analyzed and the number of assets, i.e. the elements of a portfolio, as the main criteria that determine the level of the success of the optimal portfolio strategies (optimal diversification) and the 1/N strategy (simple diversification), respectively. It is to be expected that optimal portfolio strategies will deliver better results than the 1/N strategy in the case where assessment refers to a long estimation window, and where the number of assets in a portfolio is small. Vice versa, it is expected that simple diversification will exceed optimal diversification if the number of assets in a portfolio is large and if the estimation of the expected return refers to a short estimation window. The key question that should be addressed in this matter is the critical length of the estimation window that would support specific models of the optimal allocation of assets in their achieving better results than the 1/N strategy. The aforementioned research, conducted on the US capital market, found that the critical length of the estimation window was 3000 months for the portfolio consisting of 25 assets, i.e. over 6000 months for the portfolio containing 50 assets. Bearing in mind the fact that the price estimates were generally done on the basis of the short-term sample of 60 to 120 months, the rationale supporting the determined superiority of the 1/N strategy is clear.

M. Kritzman, S. Page and D. Turkington (2010) argue that the application of the 1/N rule is not a viable alternative to the careful optimization of the portfolio, and consider the argumentation on the superiority of the 1/N strategy to be a misconception. The conclusion of their study is that the alleged superiority of the 1/N approach does not rest on the limitations of optimization, but rather on the forecasting based on the short estimation window. The results of the research conducted, based on the long-term estimation window, show that the performance of the optimized portfolios significantly exceeds the performance of the equally weighted 1/N portfolios, meaning that simple diversification thus loses its significance.

Figure 2 The effects of national and international diversifications

Source: Author

Lowering portfolio risk below the level of national systematic risk is made possible thanks to the international diversification of investments. By including foreign securities in a portfolio, one portion of the risk characterized as systematic risk in terms of the national market is transformed into unsystematic risk. The risk that remains after an effectively implemented international diversification is global systematic (market) risk, which cannot be avoided due to the fact that global macroeconomic factors affect all countries of the world. Therefore,
international diversification transforms a portion of national systematic risk into unsystematic risk, thus contributing to a further risk reduction and bringing it to the level of global systematic risk (Figure 2). The conclusion is that the investor can reduce the risk exposure of individual assets by holding a nationally diversified portfolio of assets and lower the exposure to national systematic risk by holding an internationally diversified portfolio as well.

The adequacy of the international diversification of investments predominantly depends on the correlation among the financial markets of different countries. E. J. Elton et al. (2011) calculated the correlation coefficients of the 15 stock indices of different world countries for the period 1990-2007 by using monthly returns data. The correlation among the stock indices of these different countries was 0.48 on average, and was twice smaller than the correlation between various stock indices in terms of a particular country. This illustrates the potential benefits of international diversification because, as a rule, a lower correlation coefficient results in a lower portfolio risk. However, the fact that the correlation between the markets of different countries increases from one year to another is a worrying one. This is confirmed by the calculations performed by the same authors for the previous period 1980-1988, where the value of the average correlation coefficient relating to international stock indices amounted to 0.40. The increase in the correlation in the following period was a result of an increased integration of the world economy and the establishment of the European Monetary Union (EMU), as well as the increased correlation among the markets of the EMU member countries. However, despite this increase, the correlation among the international markets remained lower than the correlation relating to the market of a particular country. Therefore, it is reasonable to expect that international diversification will continue to reduce the total portfolio risk in the future.

The results of the research study analyzing the case of 23 developed countries in the period 1980-2005, conducted by G. Bekaert, R. J. Hordick and X. Zhang (2009), confirm still significant benefits of international diversification. The authors did not find evidence in favor of the increased correlation of returns, except in the case of European capital markets. The study even points out the fact that, in terms of the financial literature, “there is no definitive evidence that cross-country correlations are significantly and permanently higher now than they were, say, 10 years ago.” At the same time, the authors acknowledge that the effects of globalization are obvious and that investors from America and Europe can achieve greater benefits by investing in the Far East; they, however, argue that the globalization process has not led to major and permanent changes in the international correlation yet.

From the viewpoint of Chinese investors, the usefulness of the international diversification of investments was examined and confirmed by C. Jiang, Y. Ma and Y. An (2013). The Chinese capital market has become more strongly integrated with the international capital market, following the implementation of the new foreign-currency exchange system in 2005, which has reduced, but not eliminated, the benefits of international diversification. However, the authors acknowledge that the study did not include transaction costs, which leaves the following question open: if transaction costs were included in the analysis of the benefits of...
international diversification, would these benefits still manage to outperform associated costs?

A number of studies (Ramchand & Susmel, 1997; Kunovac, 2011) analyzing the correlation between the capital markets of different countries have concluded that the international correlation is significantly higher in turbulent periods in comparison with quiet market periods. A turbulent period implies a period of high market volatility (high absolute returns), whereas a quiet period implies a period of low market volatility (low absolute return). L. Ramchand and R. Susmel (1997) found that the correlation between the US and other world capital markets (Japan, the United Kingdom, Germany, Canada) was on average two or three-and-a-half times higher during the turbulent period compared to the quiet market period. Similarly, by analyzing monthly returns, D. Kunovac (2011) determined that the correlation between the Croatian and foreign capital markets was on average more than two times higher in the turbulent period. The mentioned studies confirmed the existence of the phenomenon of asymmetric correlation. In terms of international diversification, the results of these studies suggest that the benefits of international diversification in a turbulent market period are limited and significantly lower than in a quiet period. During a quiet market period, correlation is lower and the benefits of international diversification are greater, whereas turbulent periods are characterized by an increase in correlation and the consequent diminishing of the benefits of diversification.

The previously described statement that correlation increases with an increase in the volatility level, i.e. that it is higher in the case of large absolute returns, was examined by F. Longin and B. Solnik (2001), who concluded that the above-mentioned statement applied in terms of the bear market, but not in terms of the bull market. The results of their research based on using the monthly rates of return in the period 1958-1996 showed that the correlation of the US capital market with the capital markets of Great Britain, France, Germany and Japan was growing in the conditions of the bear market and large negative returns, but was decreasing in the conditions of the bear market and large positive returns. Therefore, the correlation of large negative returns indicates a trend of growth, whereas the correlation of large positive returns indicates a decreasing trend and converges to zero. The authors conclude that correlation does not depend on the level of market volatility, but rather on the market trend. Volatility on its own does not affect correlation. In the context of international diversification, the results of the aforementioned research suggest that the benefits of international diversification in the conditions of the bear market are limited and considerably smaller than in the conditions of the bull market. In the conditions of the bull market, correlation is lower and the benefits of international diversification are greater, whereas the bear market is characterized by an increase in correlation and a consequent reduction in benefits from diversification.

On the example of the US capital market, A. Ang and J. Chen (2002) proved that the phenomenon of correlation asymmetry was not only the characteristic of international capital markets, but also of the capital markets of individual countries. The authors also found that the correlation between individual shares and the overall capital market is significantly higher in the conditions of the bear market compared to the bull market. In their study, they developed a model for measuring the degree of asymmetry and concluded that asymmetry was greater in the following cases: the shares of small companies in comparison with the shares of large ones, the past loser portfolios compared to the past winner portfolios, shares with a lower beta coefficient compared to those with a higher beta coefficient; in addition, the authors determined that there was no relation between the leverage and correlation asymmetries.

As the starting point of scientific papers and empirical studies, the evidence in favor of the phenomenon of correlation asymmetry has been found by L. Yuo and R. T. Daigler (2010), J. Danielsson (2011) and others. The authors reject the constant and linear correlation between returns of financial instruments, noting that the findings on the benefits of the international diversification based on the constant correlation are often misleading and incorrect. Therefore, the adoption of the final position
on the presence or absence of the superiority of the international diversification of investments over national diversification is a difficult task that requires caution. This is supported by the numerous other factors that reduce the usefulness of international investment and international diversification, such as: trade restrictions, political barriers, restrictions on currency exchange, and so on. According to W. F. Sharpe, G. Alexander and J. V. Bailey (1995), investing in a foreign security carries the risk associated with that particular security on its domestic market, plus an additional risk in the form of political and foreign-exchange risks. Political risk refers to the uncertainty regarding the possibilities of investors to convert a foreign currency into the local currency because the government of some foreign country may restrict, tax or completely ban the conversion of one currency to another. On the other hand, foreign-currency risk relates to the uncertainty about the exchange rate at which some foreign currency will be converted to the investor's local currency in the future. In other words, currency risk is expressed as the variability of the portfolio returns caused by fluctuations in the exchange rate, i.e. change in the exchange rates in terms of the domestic and foreign currencies.

Good news is that changes in the currency exchange rates of different countries are not highly correlated, for the reason of which fact exchange-rate risk represents a small part of the total risk of an internationally diversified portfolio. Some authors, such as J. C. Van Horne and J. M. Wachowicz (2007), even argue that currency risk contributes to the success of international diversification, i.e. boosts its effectiveness. In addition, foreign-exchange risk can be reduced or even completely eliminated by hedging it with forwards or futures. The full protection against foreign-exchange risk is possible in the case of risk-free fixed-income securities. On the other hand, it is not possible to completely eliminate the foreign-exchange risk related to the risky investments whose returns vary. Futures contracts can cover the expected cash flow; however, if the actual cash flow is greater than the expected, then a portion of the foreign-currency funds must be converted to local currency at the forward exchange rate. The proponents of hedging warn that the investors who do not implement foreign-exchange risk hedging miss the opportunity to reduce portfolio risk without diminishing portfolio return. They point out that a significant reduction in the variability of portfolio returns can be achieved through hedging. On the other hand, the opponents of hedging opine that the costs of hedging exceed its benefits related to risk reduction. Namely, the total annual hedging costs are estimated at between 0.25% and 0.50% of the value of the hedged assets - this fact is sufficient to persuade the opponents that the hedging of foreign-exchange risk is not profitable (Sharpe et al., 1995, 976). According to B. H. Solnik (1974), if an investor in foreign securities does not protect him-/herself against the exchange rate fluctuations, he/she is in fact intentionally speculating on currencies. Foreign-currency risk, as well as any other financial risks, carries a potential reward; therefore, such a speculation can be quite profitable. The conclusion is that, in addition to reducing the level of risk, international diversification often generates higher returns because it involves a larger choice of investments and provides opportunities to make a profit from exchange-rate fluctuations.

Taking into account the uncertainty regarding the future price movements of foreign securities, as well as the uncertainty about the future exchange rates at which capital gains and dividends will be converted from some foreign currency to the investor's local currency, international investments can be classified as:

- investment in foreign securities and
- investment in a foreign currency.

In this respect, the total return on an international investment includes:

- the returns earned from investing in foreign securities and
- the returns earned from investing in a foreign currency.

The previous statement can be mathematically proved to be true; we start with an algebraic expression for calculating the actual rate of return on shares (Francis & Kim, 2013, 411):
\[ r_{c,it} = \left( \frac{p_{c,it} - p_{c,it-1}}{p_{c,it-1}} \right) + d_{c,it}, \]  
\[ r_{c,it} = \left( \frac{x_{c,t} - x_{c,t-1}}{x_{c,t-1}} \right) \]  
\[ r_{US,it} = r_{c,it} + r_{x,t}, \]  
\[ r_{US,it} = \left( 1 + r_{c,it} \right) \left( 1 + r_{x,t} \right) - 1 = r_{c,it} + r_{x,t} + r_{c,it} r_{x,t}, \]  
\[ \sigma_{US,it} = \sqrt{\sigma_{c,it}^2 + \sigma_{x,t}^2 + 2\sigma_{c,it} \sigma_{x,t}}. \]
internationally are weakly correlated, the total risk which an investor investing in foreign securities is exposed to is smaller than the sum of domestic risk and exchange risk. In this particular example, the standard deviation of the return on foreign stock ($\sigma_{US,\text{it}}$) is smaller than the sum of the standard deviation of the return on this stock in terms of the domestic market ($\sigma_{c,\text{it}}$) and the standard deviation of the return generated by exchange-rate fluctuations ($\sigma_{x,t}$), i.e. $\sigma_{US,\text{it}} < \sigma_{c,\text{it}} + \sigma_{x,t}$. This relationship is a result of the effects of two factors:

- there is a very low correlation between return on stock in terms of the domestic market and the return generated by exchange-rate fluctuations, so the last expression $\sigma_{c,\text{it}} + \sigma_{x,t}$ approximates to zero;
- the root sum square of standard deviations is smaller than their simple sum.

It should be noted that international diversification contributes to a further reduction in portfolio risk; however, its benefits are constantly diminished from one year to another as a result of the international market integration and consequently of the increased correlation between the markets of different countries. The studies based on the data from the 1960s and the 1970s point to a reduction in the variability of returns, i.e. portfolio risk, by about 50%, as a direct result of international diversification, whereas recent studies have shown that international diversification reduces the variability of returns by less than 1%. For example, while analyzing the influence of the international diversification in the period 1990-2007, E. J. Elton et al. (2011) found out that the total investment risk could be reduced by only 0.6% by applying the optimal US and global portfolio mix. In this particular case, the minimal risk is achieved by investing 68% of assets in the US portfolio and the remaining 32% of assets in the global portfolio. The discussion presented in this paper points to the conclusion that although the benefits of the international diversification of investments have been significantly reduced, they still exist.

CONCLUSION

At the time when traditional portfolio theory was a commonly accepted concept, the simple diversification of investments based on the law of large numbers, meaning namely that the correlation among the returns of the individual securities held in a portfolio was ignored, which often resulted in an excessive number of investment portfolio components, and thereby in an excessive cost of portfolio management. Efficient diversification is the new model of investment diversification proposed by the MPT. This type of investment diversification takes into consideration the degree of the correlation among returns on individual securities, thus minimizing investment risk and including an optimal number of securities in a portfolio and also maintaining the same level of the expected return.

The number of securities in a portfolio required in order to achieve the satisfactory effects of diversification depends on the correlation among returns on individual securities. A positive correlation implies a larger number of securities, whereas a negative correlation requires a smaller number of securities to be included in an efficiently diversified portfolio. If there are a very small number of securities in a portfolio, that results in a potentially high unsystematic risk, whereas a large number of securities incur high transaction costs both in terms of creating such a portfolio and in terms of the high costs of portfolio management. The general conclusion is that the number of the securities held in a portfolio should be increased as long as its marginal benefits in the form of reduced investment risk reach the level of its marginal costs in terms of increased portfolio management costs. The equality of the marginal cost and marginal benefits is a condition for maximizing diversification benefits.

Due to the fact that the correlation among the financial markets of different countries is lower than the correlation in terms of a particular country and its market, investors are advised to opt for international diversification as an optimal investment strategy. Indeed, the effect of international diversification on risk reduction is diminished
due to globalization and an increasing economic integration of countries. However, any risk reduction is significant; furthermore, if we also include the possibility of earning higher returns, which may be achieved based on a wider investment horizon (especially by investing in emerging markets) and favorable exchange-rate fluctuations, the benefits of international diversification are real and more than evident. By converting one part of national systematic risk into unsystematic risk, the international diversification of investments reduces the level of investment risk from the level of national systematic risk to the level of global systemic risk, simultaneously maintaining or even increasing the expected return on investment. Therefore, compared to national diversification, international diversification provides a better portfolio performance, which confirms the validity of the hypothesis.

A large number of studies argue that the benefits of the international diversification of investments are still substantial; however, many authors warn that the only way to come to a valid conclusion is to include a realistic assumption of asymmetric correlations. In this regard, a conclusion has been drawn that the benefits of international diversification in a quiet market period are greater than those in the period of market turbulence. Furthermore, it is concluded that during a turbulent period it is important that a distinction between the sub-periods of the bear market and the sub-periods of the bull market should be made because, in terms of the bull market, the benefits of international diversification are significantly higher compared to those in the bear market conditions. In short, the benefits of the diversification of international investments are the smallest in the conditions of the bear market since the correlation of large negative returns indicates the tendency of growth.

The empirical analysis of the benefits of the simple, efficient, national and international diversifications of investments followed by a corresponding comparative analysis was not carried out in this study, nor was the empirical analysis of the optimal size of a portfolio in terms of the Serbian capital market conducted, either, which is the key limitation of this paper. Simultaneously, however, it makes an interesting suggestion for future research.

The opinions presented in this paper are aimed at emphasizing the importance of diversification as an investment strategy, as well as the importance of its advantages, disadvantages and limitations. By identifying the shortcomings and limitations, their significance is diminished, whereas the importance of diversification as an investment practice is improved. A particularly interesting fact is that, in the contemporary world, the optimal number of portfolio components exceeds 100; some investors, however, still hold three to four securities in their investment portfolios. This suggests the direction of future research: to try to analyze this issue, which is referred to as the diversification puzzle in the financial literature, which should include the elements of behavioral portfolio theory.

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DIVERSIFIKACIJA KAO INVESTITICIONA STRATEGIJA SMANJENJA RIZIKA ULAGANJA

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Diversifikacija je opšteprihvaćena investiciona strategija koja ima za cilj smanjenje neizvesnosti ulaganja uz zadržavanje nepromjennog očekivanog prinosa ulaganja. Razvoj diversifikacije ulaganja odvija se paralelno sa razvojem portfolio teorije. U vreme važenja tradicionalne portfolio teorije, primjenjava ne je prosta diversifikacija ulaganja koja je, usled zanemarivanja korelacije među prinosima različitih investicionih plasmana, sa pojavom savremene portfolio teorije odbačena i zamenjena efikasnom diversifikacijom. Svrsu istraživanja je upoređenje promjena prošte i efikasne diversifikacije ulaganja, uz neizbježno analiziranje optimalnog broja hartija od vrednosti u sastavu portfolija i ispitivanje opravdanosti primene međunarodne diversifikacije ulaganja. Primjenom kvalitativne metodologije istraživanja zaključeno je da su koristi od međunarodne diversifikacije ulaganja još uvijek rezpektabilne i da nadmašuju prateća ograničenja, kao i da broj hartija od vrednosti u sastavu portfolija treba povećavati sve dok se marginalne koristi od diversifikacije, u vidu smanjenog rizika ulaganja, ne izjednače sa marginalnim troškovima, u smislu povećanih troškova upravljanja portfoliom, što predstavlja glavni rezultat istraživanja.

Ključne reči: prosta diversifikacija, efikasna diversifikacija, nacionalna diversifikacija, međunarodna diversifikacija

JEL Classification: G11

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Investitor koji sa sigurnošću poznaje buduće prinose investiraće samo u jednu hartiju od vrednosti - onu koja ima najveći budući prinos (Markowitz, 1999).
Međutim, sigurna budućnost je nerealna pretpostavka koja zanemaruje rizik i suviše pojednostavljuje proces investiranja. Savremeni investitori ne koncentrišu svoje bogatstvo u jednu hartiju od vrednosti ili jednu vrstu hartija od vrednosti, već investiraju raspoloživa sredstva u različite vrste vrednosnih papira, kreirajući diversifikovani portfolio.

U finansijama, portfolio predstavlja skup investicija različitih vrsta i karakteristika, tj. kombinaciju različitih finansijskih instrumenata u posedu investitora. Držanje portfolija hartija od vrednosti je deo investicijske strategije koja se naziva diversifikacija ulaganja, a koja se sprovodi sa ciljem redukovanja ukupne varijacije sredstava, uz nepromjenjeno očekivani prinos portfolija. Jednostavniji način za smanjenje rizika portfolija je preusmeravanje dela sredstava u bezrizičnu aktivu. Međutim, takav način smanjenja rizika, za razliku od diversifikacije, rezultirao bi smanjenjem očekivanog prinosa portfolija. Imajući u vidu napred navedeno, predmet istraživanja je analiza razvojnog procesa diversifikacije kao ustaljene strategije smanjenja rizika ulaganja.

Cilj istraživanja je ispitivanje pozitivnih i negativnih aspekata proste i efikasne diversifikacije ulaganja, uz uvek aktuelni izbor optimalne veličine portfolija i upoređivanje potencijalnih koristi i ograničenja međunarodne diversifikacije ulaganja. Shodno opredeljenom predmetu i postavljenom cilju istraživanja, osnovna hipoteza rada je: H: Međunarodna diversifikacija ulaganja, u poredenju sa nacionalnom diversifikacijom, omogućava ostvarenje istog, ali visokog prinos za smanjenje rizika ulaganja.

Vodeći računa o opredeljenom predmetu, cilju i definisanoj hipotezi, u radu će nakon uvodnih razmatranja i pregleda relevantne literature biti analizirane razlike između proste i efikasne diversifikacije ulaganja, uz neizbežno navođenje nedostataka i problema sa kojima se suočava diversifikacija kao investicijska strategija. Potom će biti predstavljene potencijalne koristi i ograničenja međunarodne diversifikacije ulaganja. U poslednjem, zaključnom delu rada se stavovi o ispunjenosti osnovne hipoteze i sagledaće se otvorena pitanja značajna za buduća istraživanja.

PREGLED LITERATURE

U portfolio teoriji je poznata ideja da se kombinovanjem različitih aktivara mogu postići bolji rezultati nego plasiranjem finansijskih sredstava samo u jednu aktivu. Predlog alokacije finansijskih sredstava zapisan u IV-om veku i često navođen u finansijskoj literaturi glasi: „pojedinac treba trećinu sredstava da uloži u zemlju, trećinu u robu i trećinu da drži u gotovini“. Iako je ova ideja vekovima poznata, ona je tek polovinom prošlog veka uobličena. Naime, pre nastanka savremene portfolio teorije (Modern Portfolio Theory - MPT) investitori su konstruisali portfolio ne vodeći računa o stepenu korelacije među prinosima različitih investicionih plasmana. Osnovni nedostatak takvog načina diversifikacije, poznatog kao prosta (naivna) diversifikacija, jeste nepoštovanje efikasnosti sa povećanjem broja hartija od vrednosti koje ulaze u portfolij (Jaksić i LeKović, 2015, 32).


Prostu diversifikaciju i upotrebu zakona velikih brojeva načinio je opredijeljen metod kvalitativne ekonomske analize, zasnovan na analitičkoj o podaci. Ovaj metodološki instrumentar omogućava da se proučavaju relevantne, dominantne i inostrane literature formušu validni zaključak o istraživanoj problematični sistem.
hartija od vrednosti iste industrije nije podjednako dobro diversifikovan kao portfolio sastavljen od istog broja hartija od vrednosti različitih industrija. Prema H. M. Markowitz-u (1952, 89), da bi se smanjila varijansa portfolija nije dovoljno investirati u veliki broj hartija od vrednosti, već je neophodno izbaci

investiranje u hartije od vrednosti sada smanjenja rizika ulaganja. Prema H. M. Markowitz-u (1952, 89), da bi se smanjila varijansa portfolija nije dovoljno investirati u veliki broj hartija od vrednosti, već je neophodno izbaci

investiranje u hartije od vrednosti sa međusobno visokom kovarijanskom. Imajući u vidu navedeno, on predlaže diversifikaciju između različitih industrija, jer preduzeca iz različitih industrija, naročito industrija sa različitim ekonomskim karakteristikama, imaju manju kovarijansu nego preduzeća iz iste industrije. Dakle, H. M. Markowitz (1952) je uočio važnost korelacije među prinosima pojedinačnih hartija od vrednosti u sastavu portfolija, pri čemu niži koeficijent korelacije implicira veće koristi od diversifikacije. Utome


PROSTA I EFKASNA DIVERSIFIKACIJA ULAGANJA

Traidicionalni pristup povećavanja broja hartija od vrednosti u sastavu portfolija u funkciji smanjenja ukupnog rizika portfolija poznat je kao prosta (naivna) diversifikacija. Prema ovom pristupu investicija u sto različitih hartija od vrednosti nosi deset puta niži rizik od investicije u deset takvih hartija od vrednosti. Prekomeran broj komponenti portfolija uzrokuje visoke transakcione troškove prilikom kreiranja takvog portfolija i visoke troškove upravljanja portfoliom. Može se zaključiti da prosta diversifikacija predstavlja tradicionalni pristup diversifikaciji, ali se još uvek pojavljuje u investicionej praksi i primenjuje od strane onih investitora i portfolio menadžera koji se služe heuristikama (mentalnim prečicama), poput primene pravila 1/N.

Osim zanemarivanja korelacije, važan nedostatak proste diversifikacije se ogleda u neretko prekomernom broju hartija od vrednosti u sastavu portfolija. Prekomeran broj komponenti portfolija uzrokuje visoke transakcione troškove prilikom kreiranja takvog portfolija i visoke troškove upravljanja portfoliom. Može se zaključiti da prosta diversifikacija predstavlja tradicionalni pristup diversifikaciji, ali se još uvek pojavljuje u investicionej praksi i primenjuje od strane onih investitora i portfolio menadžera koji se služe heuristikama (mentalnim prečicama), poput primene pravila 1/N.

Nasuprot tradicionalnoj portfolio teoriji i prostoj diversifikaciji kao njenoj karakteristici, MPT je pomerila akcenat sa analize karakteristika pojedinačnih hartija od vrednosti na analizu karakteristika portfolija, ističući značaj korelacije među prinosima komponentnih hartija od vrednosti. Ukoliko investitori nastoje da smanje rizik portfolija, nije dovoljno da investiraju u veliki broj različitih hartija od vrednosti, već je potrebno da investiraju u hartije od vrednosti čiji prinosi imaju nisku korelaciju (Jakšić, 2012, 161). H. M. Markowitz (1952) je dao matematički dokaz da odgovarajuća diversifikacija može minimizirati varijansu portfolija za dati nivo prinosa. On je prvi formalno kvantifikovao supstipiciju (trade off) između prinosa i rizika. Obraćanje pažnje na to kako su prinosi aktive korelirani sa ostalom aktivom, omogućilo je kreiranje seta efikasnih portfolija koji minimiziraju rizik za dati nivo prinosa, odnosno, maksimiraju prinos za dati nivo rizika.

Prema H. M. Markowitz-u (1952), efikasna diversifikacija zahteva od investitora da prilikom formiranja portfolija izbegava hartije od vrednosti sa visokom korelacijom. U ekstremnom slučaju savršeno pozitivno koreliranih hartija od vrednosti, efekti

Na Slici 1 prikazan je efekat Markowitz-eve efikasne diversifikacije, za slučaj portfolija sastavljenog od dve hartije od vrednosti B i A.

Slika 1 Efekat Markowitz-eve efikasne diversifikacije

Izvor: Autor, na osnovu: Francis & Kim, 2013, 39

Sve moguće kombinacije savršeno pozitivno korelisanih ($\rho = +1$) hartija od vrednosti B i A predstavljene su pravom linijom BA. Svaka tačka na ovoj pravoj označava portfолio čije se karakteristike podudaraju sa ponderisanim karakteristikama njegovih komponenata. To znači da se kombinovanjem savršeno pozitivno korelisanih hartija B i A ne može poštici smanjenje rizika portfolija, koje nije praćeno istovremenim smanjenjem očekivanog prinsosa. Krećući se od tačke B ka tački A očekivani prinos i rizik portfolija rastu, jer raste učestveno rizičnije hartije od vrednosti koja nosi i veći prinos. U obrnutom slučaju, krećući se od tačke A ka tački B očekivani prinos i rizik portfolija se smanjuju. Navedeno potvrđuje izostanak koristi od diversifikacije u slučaju perfektno pozitivne korelacije između komponenti portfolija.

S druge strane, sve kombinacije savršeno negativno korelisanih ($\rho = -1$) hartija od vrednosti B i A raspoređuju se duž dve prave linije, od kojih je jedna linija negativnog nagiba (linija BC), a druga pozitivnog nagiba (linija CA). Kretanje od tačke B ka tački C podrazumeva uključivanje rizičnije hartije od vrednosti A u portfolio, koje rezultira smanjivanjem standardne devijacije portfolija, uz istovremenim rast očekivanog prinsosa. Ukoliko bi pretpostavili beskonačnu deljivost posmatranih hartija od vrednosti, rizik portfolija bi bilo moguće svesti na nulu u tački C. U tački C diversifikacija portfolija obezbeđuje potpunu stabilizaciju njegov prinsosa. U pitanju je optimalna situacija, postignuta zahvaljujući perfektnoj negativnoj korelacji između elemenata portfolija. Dodatnim uključivanjem rizičnijeg vrednosnog papira A, duž linije pozitivnog nagiba CA, nastavlja se povećavanje očekivanog prinsosa portfolija, ali po ceni rastućeg rizika (Slika 1).

Konačno, spajanjem opisane prave linije BA sa pravim linijom BC i CA, dobija se trokut BCA, u čijem prostoru se nalaze sve kombinacije nesavršeno korelisanih ($-1 < \rho < +1$) hartija od vrednosti B i A, predstavljene krivim linijama BA. Važno je primetiti da su krive linije BA u početku negativnog nagiba, jer se uključivanjem rizičnije hartije od vrednosti A rizik portfolija nakratko smanjuje zahvaljujući činjenici da je korelacija manje nego savršeno pozitivna. Kako se koeficijent korelacije smanjuje, tako krive linije BA sve više tendaraju u levo, što govori o povećavanju koristi od diversifikacije u smislu stabilizacije prinsosa portfolija. Dakle, u slučaju nesavršeno korelisanih hartija od vrednosti, rizik portfolija se nalazi između nulte vrednosti postignute zahvaljujući savršeno negativnoj korelacji i maksimalne vrednosti ostvarene kao posledica savršeno pozitivne korelacije.
između elemenata portfolija. Generalni zaključak je da efikasna diversifikacija podrazumeva i zahteva niske koeficijente korelacije (Slika 1).


Uticaj efikasne diversifikacije na smanjenje rizika portfolija, predstavljen jednačinom $\sigma_p^2 = \frac{1}{n} \sigma_i^2, (3)$ je očigledan. Jasno je da se sa povećanjem broja nekoreliranih elemenata portfolija ($n$), rizik portfolija iskazan varijansom ($\sigma_p^2$) smanjuje. Za ekstremno veliki broj nekoreliranih elemenata portfolija, varijansa portfolija se približava nuli. Međutim, u realnom tržišnom ambijentu je nemoguće kreirati portfolio sastavljen od nekoreliranih vrednosnih papira, pa su i efekti diversifikacije ulaganja znatno manji. Namera je da se diversifikacijom eliminiše nesistemski rizik, ostavljajući samo sistemski rizik, definisan beta koeficijentom (Vincent, 2011). Ukoliko investitor sprovede efikasnu diversifikaciju, portfolio neće posedovati nesistemski rizik (rizik svojstven za kompaniju emitenta, poput rizika nelikvidnosti, neuspešne promotivne aktivnosti, štrajka radnika i sl.), već samo sistemski rizik (rizik svojstven za celokupno tržište, poput kamatnog, deviznog, inflacionog rizika i sl.). Sistemski rizik je rizik koji tržište kompenzuje, a nesistemski rizik je rizik koji se ne može otkloniti diversifikacijom. Pojedini autori, poput I. Omisore-a, M. Yusuf-a i N. Christopher-a (2012), intrigantno tvrde da diversifikacija eliminise nesistemski rizik, ali po cenu podizanja sistemskog rizika. Diversifikacija primorava portfolio menadžere da investiraju u različite vrste aktiva, čime se veštaci povećava tražnja za njima. Ova veštaci povećana tražnja uzrokuje rast cene aktive koja bi, analizirana individualno, imala malu osnovnu vrednost. Rezultat je da ukupan portfolio
postaje skuplji, što za posledicu ima smanjenu verovatnoću ostvarenja očekivanog pozitivnog prinosa, odnosno, rast portfolio rizika.

Na osnovu navedenog, zaključuje se da je efikasna diversifikacija poželjna, ali ne i savršena investiciona strategija. Koristi od diversifikacije, u smislu zadržavanja očekivanog prinosa portfolio uz smanjeni rizik portfolio, postignute kombinovanjem aktive sa niskom ili još bolje negativnom korelacijom, su evidentne. Međutim, problem je pronalazak negativno korelisanih aktiva, budući da je pozitivna korelacija najčešći slučaj korelativne veze na savremenim finansijskim tržištima. Takođe, u uslovima finansijsko-ekonomskih kriza, koeficijenti korelacije teže jedinici, zbog čega se smanjuju ili potpuno nestaju prednosti diversifikacije. Ovo je ujedno i najveći nedostatak ove investiciono strategije, jer ukoliko diversifikacija ne daje rezultate onda kada je investitorima najpotrebnija zaštita od rizika, postavlja se pitanje njene generalne upotrebljivosti. Upravo su finansijsko-ekonomskie krize i namera da se smanje koeficijenti korelacije podstakli investitore da pored hartija od vrednosti (primarno akcija i obveznica) tragaju za novom aktivom, poput plemenitih metala, nafte, nekretnina, umetničkih dela i sl, i da je uključuju u portfolio. Treba istaći i da u vreme finansijski-ekonomskih kriza povećava optimalan broj hartija od vrednosti u sastavu portfolio, što implicira i veće troškove upravljanja portfolio.

Pojedina empirijska istraživanja sugerišu da je u odsustvu ograničenja trgovanja prostas diversifikacija ulaganja uspešnija investiciona strategija smanjenja rizika ulaganja od efikasne diversifikacije. V. DeMiguel, L. Garlappi i R. Uppal (2009) su uporednom analizom utvrdili lošije performanse četvrtog optimalnih portfolio strategija u odnosu na naivnu 1/N strategiju. Kao osnovne kriterijume od kojih zavisi utvrđeni nivo uspešnosti optimalnih portfolio strategija (optimalne diversifikacije) i 1/N strategije (proste diversifikacije), autori navode dužinu analiziranog vremenskog perioda i broj aktiva, tj. elemenata portfolio. Za očekivati je da optimalne portfolio strategije donesu bolje rezultate od 1/N strategije, ukoliko je procenom obuhvaćen dug vremenski period (long estimation window) i ukoliko je broj aktiva u sastavu portfolio mali. I obrnuto, za očekivati je da prosta diversifikacija nadmaši optimalnu diversifikaciju ukoliko je broj aktiva u sastavu portfolio veliki i ukoliko se procena očekivanog prinosa odnosi na relativno kratak vremenski period. Ovde se, kao ključno, postavlja pitanje kritične dužine vremenskog perioda koji treba da bude obuhvaćen procenom (critical length of the estimation window), da bi modeli optimalne alokacije aktive doneli bolje rezultate od 1/N strategije. U opisanom istraživanju, sprovedenom na američkom tržištu kapitala, utvrđeno je da kritična dužina iznosi 3000 meseci za portfolio sastavljen od dvadeset pet aktiva, odnosno, više od 6000 meseci za portfolio koji sadrži pedeset aktiva. Imajući u vidu činjenicu da se procene u praksi obično vrše na osnovu kratkoročnog uzorka od šesdeset ili stotinu meseci, više nego jasan je razlog utvrđene superiornosti 1/N strategije.


POTENCIJALNE KORISTI I OGRANIČENJA MEĐUNARODNE DIVERSIFIKACIJE ULAGANJA

Kombinovanjem različitih vrsta vrednosnih papira finansijskog tržišta jedne zemlje, koji nisu savršeno pozitivno korelisan, redukse se ukupna varijansa, tj. ukupan rizik portfolio. Donja granica smanjenja ukupnog rizika portfolio, postignutog zahvaljujući nacionalnoj diversifikaciji ulaganja, jeste sistemski rizik nacionalnog tržišta. Naralna diversifikacija
putem smanjivanja nesistemskog rизika, svodi ukupан rизик портфолија на ниво националног sistemског rизика (Слика 2).

Dodатно smanjenje rизика портфолија испод нивоа националног sistemског rизика omogućava međunarodna diversifikacija ulaganja tako što, uključivanjem straniх hartija od vrednosti u portfolio, jedан deo rизика koji je на националном тржишту okarakterisan као sistemски transformише у nesистемски. Rизик koji постоjeјe најен ефикасно sprovedene međunarodne diversifikacije ulaganja jeste глобални sistemski (тржишни) rизик, koji se не може избећи je rизик противопостављен као система rизика на ниво глобалног sistemског rизика (Слика 2). Заклjučuje se да инвеститор може smanjiti izloženost rизiku pojединачне активе držanjем национално diversifikованог портфолија, али и изloženost sistemском rизику националног тржишта držanjем međunarodno diversifikованог портфолија.

Slika 2 Efekat nacionalne i međunarodne diversifikacije

Izvor: Autor


Rezultati istraživanja koje су на примеру dvadesetтри razvijene zemlje sveta, за period 1980-2005, sproveli G. Bekaert, R. J. Hordick и X Zhang (2009), potvrđuju јeшћu uvek značajne koristi od međunarodne diversifikacije. Они nisu pronašli dokaze у korist trenda rasta...
korelacije prinosa, osim u slučaju evropskog tržišta kapitala. U studiji se čak ističe da u finansijskoj literaturi „ne postoje konačni dokazi da je korelacija među zemljama značajno i permanentno veća sada nego pre deset godina“. Istovremeno, priznaju da su efekti globalizacije očigledni i da investitori iz Amerike i Evrope mogu ostvariti veće benefite ulaganjem sredstava u zemlje Dalekog istoka, ali tvrde da proces globalizacije još uvek nije doveo do velikih i trajnih promena u međunarodnoj korelaciji.


Imajući u vidu neizvesnost budućih cena stranih vrednosnih papira, kao i neizvesnost budućeg deviznog kursa po kome će se kapitalni dobici i dividende konvertovati iz strane u domaću valutu investitora, međunarodna investicija se može podeliti na:

- investiciju u strane hartije od vrednosti, i
- investiciju u stranu valutu.

Saglasno navedenom, ukupan prinos od međunarodne investicije se sastoji od:

- prinosa koji donosi investiranje u strane hartije od vrednosti, i
- prinosa koji donosi investiranje u stranu valutu.

Prethodna tvrdnja se može i matematički dokazati, a polazna tačka je algebarski izraz za stvarnu stopu prinos na akcije (Francis & Kim, 2013, 411):
Diversifikacija kao investiciona strategija smanjenja rizika ulaganja

\[ r_{c,it} = \frac{(p_{c,it} - p_{c,it-1}) + d_{c,it}}{p_{c,it-1}} \]  \hspace{1cm} (4)

gde su:

- \( r_{c,it} \) - stvarna stopa prinosa na akcije preduzeća i lociranog u zemlji \( c \) u vremenu \( t \),
- \( p_{c,it} \) - cena akcije preduzeća i lociranog u zemlji \( c \) u vremenu \( t \),
- \( p_{c,it-1} \) - cena akcije ovog preduzeća u vremenu \( t-1 \),
- \( d_{c,it} \) - dividenda po akciji ovog preduzeća.

Međutim, iz ugla američkog investitora, stvarna stopa prinosa na akcije pomenutog preduzeća se dobija primenom sledeće formule:

\[ r_{US,it} = \frac{(p_{c,it} + d_{c,it})(x_{c,t}) - (p_{c,it-1})(x_{c,t-1})}{p_{c,it-1}(x_{c,t-1})} \]  \hspace{1cm} (5)

gde su:

- \( r_{US,it} \) - ukupna stopa prinosa koju američkom investitoru donosi akcija \( i \),
- \( x_{c,t} \) - devizni kurs između valute zemlje \( c \) i američkog dolara u vremenu \( t \), izražen u dolarima po jedinici strane valute,
- \( x_{c,t-1} \) - devizni kurs između valute zemlje \( c \) i američkog dolara u vremenu \( t-1 \).

Simplifikovanjem dalje sledi:

\[ r_{US,it} = \left[ \left(1 + r_{c,it}\right) \left(1 + r_{x,t}\right) \right] - 1 = r_{c,it} + r_{x,t} + r_{c,it} r_{x,t} \]  \hspace{1cm} (6)

gde su:

- \( r_{c,it} \) - stopa prinosa koju bi investitor zaradio ako bi kao građanin zemlje \( c \) kupio deo akcija preduzeća i u vremenu \( t - 1 \), i prodao ih u vremenu \( t \) (domaći prinos aktive, tj. prinos aktive u okviru domaćeg tržišta),
- \( r_{x,t} \) - stopa prinosa koju donose promene u deviznom kursu,
- \( r_{c,it} r_{x,t} \) - efekat koji promena deviznog kursa ima na kapitalni dobitak (gubitak) i dividende.

Poslednji izraz u gornjoj jednačini \( (r_{c,it}, r_{x,t}) \) može se izostaviti, pošto je znatno manji od prethodna dva (jednak je njihovom proizvodu, a oni su po pravilu manji od 1,0), tako da je približno (Elton et al, 2011, 211):

\[ r_{US,it} = r_{c,it} + r_{x,t} \]  \hspace{1cm} (7)

Na ovaj način, dokazano je da se prinos od međunarodne investicije sastoji od:

- prinosa koji donosi investiranje u stranu aktivu (prinos aktive u okviru njenog domaćeg tržišta na kome je izdata), i
- prinosa koji donosi investiranje u stranu valutu.

Takođe, zaključuje se i da je prinos koji donosi ista međunarodna investicija različit za investitore različitih zemalja, zbog razlika u deviznim kursevima.

Koristeći prethodnu aproksimaciju, očekivani prinos (\( \bar{r}_{US,it} \)) i standardna devijacija prinosa na stranu akciju (\( \sigma_{US,it} \)) biće (Elton et al, 2011, 211):

\[ \bar{r}_{US,it} = \bar{r}_{c,it} + \bar{r}_{x,t} \]  \hspace{1cm} (8)

\[ \sigma_{US,it} = \sqrt{\sigma_{c,it}^2 + \sigma_{x,t}^2 + 2\sigma_{c,it} \sigma_{x,t} r_{c,it} r_{x,t}} \]  \hspace{1cm} (9)

Pošto su rizici koji prate međunarodno investiranje nisko korelisoni, ukupan rizik investitora koji investira u strane hartije od vrednosti (\( total \ risk \)) je manji od zbira rizika promene cene na tržištu na kome je hartija emitovana (\( domestic \ risk \)) i deviznog rizika (\( exchange \ risk \)). U konkretnom primjeru, standardna devijacija prinosa na stranu akciju (\( r_{US,i} \)) je manja od zbira standardne devijacije prinosa posmatrane akcije
u okviru domaćeg tržišta ($\sigma_{c,it}$) i standardne devijacije prinosa ostvarenog po osnovu promena u deviznom kursu ($\sigma_{x,t}$), odnosno, $\sigma_{US,it} < \sigma_{c,it} + \sigma_{x,t}$. Ovaj odnos proizilazi kao posledica uticaja dva faktora:

- postoji veoma niska korelacija između prinosa akcije u okviru domaćeg tržišta i prinosa ostvarenog po osnovu promene u deviznom kursu, zbog čega poslednji izraz $\sigma_{c,it} x,t$ teži nuli, i
- kvadratni koren zbira kvadrirani standardnih devijacija je manji od njihovog prostog zbira.

Može se zaključiti da međunarodna diversifikacija doprinosi dodatnom smanjenju rizika portfolija, ali se koristi od međunarodne diversifikacije iz godine u godinu smanjuju kao posledica međunarodne tržišne integracije, i posledično, povećane korelacije između tržišta različitih zemalja sveta. Istraživanja zasnovana na podacima iz 1960-tih i 1970-tih godina ukazuju na smanjenje promenljivosti prinosa, odnosno, rizika portfolija za oko 50% kao direktnat rezultat međunarodne diversifikacije, dok novija istraživanja svedoče o smanjenju promenljivosti prinosa za manje od 1%. Primera radi, E. J. Elton i ostali (2011) su, ispitujući uticaj međunarodne diversifikacije u periodu 1990-2007, ustanovili da se optimalnom kombinacijom američkog i svetskog portfolija ukupan rizik ulaganja može smanjiti za svega 0,6%.

U konkretnom slučaju, minimalni rizik je postignut investiranjem 68% sredstava u američki portflio, a preostalih 32% sredstava u svetski portflio. Navedeno govori u prilog značajno smanjenih, ali još uvek prisutnih koristi od međunarodne diversifikacije ulaganja.

ZAKLJUČAK

Prosta diversifikacija ulaganja sprovođena u vreme važenja tradicionalne portfolio teorije se zasnivala na zakonu velikih brojeva, tj. ignorisanju korelacije među prinosima pojedinačnih hartija od vrednosti u sastavu portfolija, rezultirajući neterko prekomernim brojem komponenti portfolija i prekomernim troškovima upravljanja portfoliom. Novi oblik diversifikacije ulaganja koji predlaže MPT je efikasna diversifikacija ulaganja, koja uzimanjem u obzir stepena povezanosti prinosa pojedinačnih hartija od vrednosti omogućava minimiziranje rizika ulaganja, uz optimalan broj hartija od vrednosti u sastavu portfolija i nepromenjen nivo očekivanog prinosa ulaganja.

Broj hartija od vrednosti u sastavu portfolija, potreban da bi se postigli zadovoljavajući efekti diversifikacije, zavisí od korelacije među prinosima hartija od vrednosti. Pozitivna korelacija implicira veći, a negativna korelacija manji zahtevani broj hartija od vrednosti u sastavu efikasno diversifikovanog portfolija. Sviše mali broj hartija od vrednosti u sastavu portfolija ima za posledicu potencijalno visok nesistemski rizik, dok preveliki broj hartija od vrednosti uzrokuje visoke transakcione troškove koji nastaju prilikom kreiranja takvog portfolija i visoke troškove upravljanja portfoliom. Zaključak je da broj hartija od vrednosti u sastavu portfolija treba povećavati sve dok se marginalne koristi od diversifikacije, u vidu smanjenog rizika ulaganja, ne izjednache sa marginalnim troškovima, u smislu povećanih troškova upravljanja portfoliom. Jednakost marginalnih troškova i marginalnih koristi je uslov maksimiranja korisnosti diversifikacije.

Budući da je korelacija među finansijskim tržištima različitih zemalja niža od korelacije unutar jedne zemlje i njenog tržišta, investitorima se predlaže primena međunarodne diversifikacije kao optimalne investicijske strategije. Istini za volju, globalizacija i sve veća ekonomska integracija zemalja nesumnjivo smanjuju učinak međunarodne diversifikacije na polju redukcije rizika. Međutim, i najmanje smanjenje rizika je značajno, a ukoliko se navedenom dodaju i potencijalno viši prinioci, koji mogu biti ostvareni zahvaljujući širem investicionom horizontu (zaradi ulaganjem sredstava u tržišta kapitala zemalja u razvoju) i zahvaljujući povoljnim fluktuacijama deviznog kursa, jasno je da su koristi od međunarodne diversifikacije još uvek realne i više nego očigledne. Međunarodna diversifikacija ulaganja, pretvaranjem dela nacionalnog sistemskog rizika u nesistemski, rezultira smanjenjem rizika ulaganja sa nivoa nacionalnog sistemskog na nivo globalnog sistemskog rizika, uz nepromenjen, ili viši očekivani prinos
ulaganja. Samim tim, međunarodna diversifikacija, u poredenju sa nacionalnom diversifikacijom, obezbeđuje bolje performanse portfolija, čime je potvrđena hipoteza.

U prilog još uvek respektabilnim koristima međunarodne diversifikacije ulaganja govori većina istraživanja, ali mnogi autori upozoravaju da je jedino valjano ono zaključivanje koje je zasnovano na realnoj pretpostavci asimetričnih korelacija. S tim u vezi, zaključeno je da su koristi od međunarodne diversifikacije u mornom tržišnom razdoblju veće u odnosu na turbulentno tržišno razdoblje. Takođe, zaključeno je da je u okviru turbulentnog razdoblja važno izvršiti distinkciju između subperioda opadajućeg i subperioda rastućeg tržišta, jer su koristi od međunarodne diversifikacije u uslovima rastućeg tržišta znatno veće u poredenju sa uslovima opadajućeg tržišta. Ukratko, koristi od međunarodne diversifikacije ulaganja su najmanje u uslovima opadajućeg tržišta, jer korelacija velikih negativnih prinosa pokazuje tendenciju rasta.

U sprovedenom istraživanju nije izvršena empirijska analiza korisnosti proste, efikasne, nacionalne i međunarodne diversifikacije ulaganja praćena odgovarajućom uporednom analizom, niti empirijska analiza optimalne veličine portfolija na tržištu kapitala Republike Srbije, što predstavlja ključno ograničenje rada, ali istovremeno i predlog za buduća istraživanja. Posebno intrigira činjenica da je sadašnji broj komponenta portfolija porastao na preko sto, a da pojedinični investitori u svom portfoliju drže svega tri do četiri hartije od vrednosti. Buduća istraživanja biće usmerena na razmatranje ovog pitanja, poznatog u finansijskoj literaturi pod nazivom diversification puzzle, čemu će poslužiti elementi bihejvioralne portfolio teorije.

REFERENCE


Investment diversification is a widely accepted investment strategy, aimed at reducing investment uncertainty, while simultaneously keeping the expected return on investment unaltered. The development of investment diversification coincided with the development of portfolio theory. At the time when traditional portfolio theory was recognized as the leading portfolio management practice, the simple diversification of investments was the most commonly used strategy; however, due to its inability to recognize the importance of the correlation between returns on different investments, simple diversification was later rejected in modern portfolio theory and replaced with efficient diversification. The research study is aimed at conducting a comparative analysis between the simple and efficient diversifications of investments, together with the inevitable analysis of the optimal number of securities in a portfolio and the testing of the validity of the international diversification of investments. By applying a qualitative research methodology, it is concluded that the benefits of the international diversification of investments are still substantial, and as such outweigh specific limitations, and that the number of securities in a portfolio should be increased as long as its marginal benefits, in the form of reduced investment risk, exceed its marginal costs – in terms of increased portfolio management costs, which also represents the main result of the research.

**Keywords:** simple diversification, efficient diversification, national diversification, international diversification

**JEL Classification:** G11