Irreversibility on the Level of Single-Electron Tunneling

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We present a low-temperature experimental test of the fluctuation theorem for electron transport through a double quantum dot. The rare entropy-consuming system trajectories are detected in the form of single charges flowing against the source-drain bias by using time-resolved charge detection with a quantum point contact. We find that these trajectories appear with a frequency that agrees with the theoretical predictions even under strong nonequilibrium conditions, when the finite bandwidth of the charge detection is taken into account.

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The second law of thermodynamics states that a macroscopic system out of thermal equilibrium will irreversibly move toward equilibrium driven by a steady increase of its entropy. This macroscopic irreversibility occurs despite the time-reversal symmetry of the underlying microscopic equations of motion. Also, a microscopic system will undergo an irreversible evolution on a long time scale, but, over a sufficiently short observation time τ , both entropy-producing trajectories as well as their timereversed entropy-consuming counterparts occur. It is only because of the statistics of these occurrences that a longterm irreversible evolution is established. This phenomenon is described by the fluctuation theorem [1,2].

Irrespective of the description of the trajectories being system-specific, the fluctuation theorem (FT) relates the probabilities $P_{\tau}(\Delta S)$ for processes that change the entropy of the system by an amount ΔS during an arbitrary time τ by the equation

$$\frac{P_{\tau}(\Delta S)}{P_{\tau}(-\Delta S)} = e^{\Delta S/k_{\rm B}},\tag{1}$$

where k_B is the Boltzmann constant. In a seminal work, Wang *et al.* [3] tested the FT by measuring force trajectories of a micron-scale latex bead in a liquid. Since then, the FT has been tested in other systems [4–6], but all of those earlier experiments were carried out in a classical regime at room temperature. Experiments in the quantum regime [7–9] have long been anticipated, and the use of quantumcoherent mesoscopic conductors may lead to this goal. Subject Areas: Mesoscopics, Statistical Physics

However, at their typical operation temperatures T below 1 K, the requirement to resolve tiny fluctuations on the energy scale $k_{\rm B}T$ becomes an increasingly challenging task. An interesting recent result in this direction has been the verification of exact relations between current and current noise as functions of the source-drain voltage across an Aharonov-Bohm interferometer [10]. These relations are naturally derived from the FT [Eq. (1)], as well as the Onsager-Casimir and fluctuation-dissipation relations [11,12].

As a step toward the direct test of Eq. (1) in the quantum regime, we verify the fluctuation theorem in singleelectron tunneling [13–15] at low temperatures, although our experiment is carried out in the regime of classical charge counting. We employ real-time detection of singleelectron charging [16,17] in quantum dots (QDs). Monitoring the charge state of two QDs that are coupled both in series and to source and drain electrodes (double quantum dot [DQD]) allows us to measure the directionresolved charge flow through this device [18] and consequently the current probability distribution. A recent experiment following this line [19] revealed the importance of the backaction [20] of the charge-sensing device, which was a quantum point contact [21] (QPC). Backaction due to nonequilibrium QPC noise destroys microreversibility in the DQD and leads to an apparent temperature that significantly exceeds the bath temperature [19,22,23]. This sensitivity to the measurement arises because the entropy fluctuations associated with singleelectron tunneling are 3 orders of magnitude smaller than those at room temperature. In order to avoid the spurious backaction, we employ an optimized sample design that combines electron-beam and scanning-probe lithography [24]. It provides the high tunability and electronic stability required for the experiment while maintaining a good QPC-DQD coupling. We observe quantitative

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agreement between our data and theory in the nearequilibrium regime after including a small correction due to finite detector bandwidth [25], which is a technical rather than physical complication and requires no fitting parameter. In the regime far from equilibrium, our results depend on the system details; we find that the FT describes our data correctly in configurations where the DQD dynamics are those of a three-state Markovian system.

Our measurements were performed in a ${}^{3}\text{He}/{}^{4}\text{He}$ dilution refrigerator on the sample shown in Fig. 1(a). The dark parts in the atomic-force micrograph correspond to the conductive (nondepleted) parts of a two-dimensional electron gas located 34 nm below the surface of a GaAs/Al_{0.3}Ga_{0.7}As heterostructure (sheet density $n_S = 4.9 \times 10^{15} \text{ m}^{-2}$, mobility $\mu = 33 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$, as determined at T = 4.2 K). Confinement is achieved in one part with Ti/Au gates (the upper half of the image), which are biased with negative voltages. The thin vertical finger gates are only slightly biased in order to maintain a small tunneling coupling between the two QDs (white disks) and the source and drain leads. The horizontal lines are created by local anodic oxidation; they electrically separate the DQD from the charge detector QPC in the lower half of the image. The detector's conductance G_{OPC} is sensitive to the charge on the DQD and abruptly decreases if an elec-

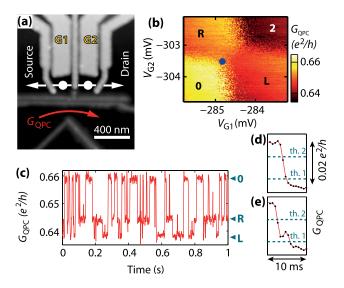


FIG. 1. (a) Atomic-force micrograph of the sample. Electrons can travel between the source and drain via the two quantum dots marked by disks. The conductance $G_{\rm QPC}$ of the quantum point contact serves to read out the charge state of the quantum dots. (b) By using the two gates G1 and G2, the charge state of the sample is controllably switched between empty (0), singly occupied [left (L), right (R)], and doubly (2) occupied. These four states are visible as panels of distinct $G_{\rm QPC}$ in the plot. (c) Time dependence of $G_{\rm QPC}$ close to the charge-degeneracy point marked by a dot in (b), displaying fluctuations between three levels: L, R, and 0. (d) and (e): $G_{\rm QPC}$ time segments showing examples (d) of a direct transition from 0 to L, and (e) of a transition from 0 to L via R.

tron is loaded to either of the two QDs. Figure 1(b) shows a color plot of the time-averaged QPC conductance as a function of the two gate voltages V_{G1} and V_{G2} , which control the number of electrons on the DQD [26]. Four regions of stable charge are visible as regions of constant QPC conductance, up to a background that is linear in V_{G1} and V_{G2} . We estimate that each QD holds about 80 electrons, but for ease of notation we consider only the number of excess electrons and denote the four relevant charge states of the DQD as empty (0), singly occupied (L, R), and doubly occupied (2). At the borders of these regions, thermal fluctuations of the charge occur.

In particular, at the charge-degeneracy point marked by a dot in the color plot, the OPC conductance fluctuates rapidly between three levels corresponding to the states 0, L, and R, as shown in Fig. 1(c). By counting the number of transitions between L and R, we can determine the total number n of electrons that pass through the center barrier of the DOD during an acquisition time τ . If τ is large compared to the typical dwell time of an electron inside the DQD, the electron passing through the center barrier will typically reach one of the leads, where it equilibrates with the thermal bath at temperature T. The entropy change ΔS will then be equal for all charge fluctuations with equal n [9,12,15]. The change can be either positive or negative, depending on the direction of the charge flow with respect to the bias direction. As the dissipated heat neV_{DOD} is determined by the source-drain voltage across the DQD, ΔS is given by neV_{DOD}/T , and the FT for our system is

$$\frac{P_{\tau}(n)}{P_{\tau}(-n)} = e^{neV_{\text{DQD}}/k_{\text{B}}T}.$$
(2)

The OPC is biased with a voltage of 300 μ V, and its conductance is recorded by using a room-temperature current-to-voltage converter and digitizer. The signal is then filtered by software at a bandwidth of 0.4 kHz, further resampled at 1.5 kHz, and stored for analysis. Two conductance thresholds are defined in the middle between neighboring conductance levels. In the algorithm that determines the chronological sequence of DQD states, we build in the requirement that at least three successive data points must lie in the same conductance interval for the DQD state to be accepted. The reason for this choice becomes clear when we take a closer look at the G_{OPC} time traces provided in Figs. 1(d) and 1(e). The G_{OPC} signal in panel (d) exhibits a direct transition from level 0 to level L. Because of the finite rise time, two of the sampled data points happen to lie between thresholds 1 and 2. If these were to be assigned to level R, a false transition from R to L would be counted, which would reduce the net flow n in the corresponding time segment by 1. In comparison, the signal in panel (e) shows a short, yet clear, dwell time in the level R.

Figure 2(a) shows an example of a $P_{\tau}(n)$ distribution measured at an electron-bath temperature of 330 mK and

with $V_{\text{DQD}} = 0 \ \mu \text{V}$. It is based on the counting analysis of 3000 G_{QPC} time segments, each with length $\tau = 2$ s. The choice of τ is such to minimize the combined error that originates both from the imperfect long-time limit [9,12,15,19] (favoring large τ) and from statistics (favoring small τ). The distribution is symmetric about n = 0, i.e., there is no net charge flow in equilibrium, as expected. The amount of charge flow at zero DQD bias (compared to the charge flow at finite DQD bias) is a sensitive measure for the strength of residual QPC backaction. Because of left-right asymmetries in the DQD, such as a nonzero level detuning, QPC backaction generically leads to nonequilibrium charge flow in a ratchet-type effect [27,28].

When V_{DQD} is increased to 20 μ V, the distribution shifts toward positive *n*, as shown in Fig. 2(b), and, on average, an electron number of $\langle n \rangle = 2.5$ is transferred. Still, for some of the time segments, the charge flow is against the applied bias (n < 0), which results in a temporary decrease of the system entropy. Similar measurements are carried out at temperatures of 500 mK and 700 mK [29]. These are shown in Figs. 2(c)–2(e), where the data points are the logarithm of the left-hand side of Eq. (2), measured at $V_{\text{DOD}} = 0 \ \mu$ V and $V_{\text{DOD}} = 20 \ \mu$ V, respec-

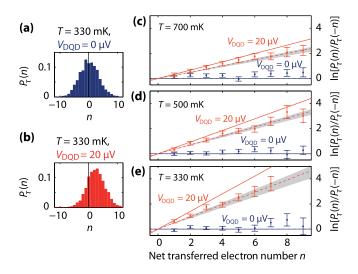


FIG. 2. (a), (b): Experimental probability distributions for the net electron number n transferred through the DQD during time $\tau = 2$ s for two different DQD source-drain voltages V_{DOD} . (c), (d), and (e): Comparison of experimental data with theory for three different bath temperatures. The data points correspond to the left-hand side of Eq. (2) and describe the probability ratio of forward (+n, entropy-producing) and backward (-n, entropy-)consuming) processes for a given n. The solid lines mark the expected exponential behavior $\exp(neV_{\text{DQD}}/k_{\text{B}}T)$ for the two source-drain voltages 0 μ V (dark blue, horizontal) and 20 μ V (red, inclined). If the finite bandwidth of the detector is taken into account [25,30] (dashed lines), experiment and theory agree within the statistical uncertainty of the data. (Error bars indicate the estimated standard deviation. The gray bands around the dashed lines indicate the uncertainty in the finite-bandwidth correction.)

tively. The expression $\ln[P_{\tau}(n)/P_{\tau}(-n)]$ follows the expected linear behavior close to the theoretical curve $neV_{\text{DOD}}/k_{\text{B}}T$ (solid lines).

In the nonzero-bias case, there is a systematic deviation of 20% to 30% in the slope. This deviation can be understood by taking into account the limited bandwidth of the charge detection. A charge-switching event in the DQD is detected in the QPC only after a reaction time of $1/\Gamma_{det}$, which in our case is determined both by the rise time of the measurement electronics and by the rejection of short events built into the analysis algorithm. If the charge state switches back too fast, the event is missed. Following the ideas presented in Ref. [30], Utsumi et al. [25] calculated the effect of the finite bandwidth. They found that, up to order $1/\Gamma_{det}$, the finite bandwidth has the same effect as a prefactor $\alpha_{\rm BW} < 1$ to the term $eV_{\rm DQD}/k_{\rm B}T$, just as we have observed in our experiment. The factor $\alpha_{BW} =$ $k_{\rm B}T \ln w^*/eV_{\rm DQD}$ is expressed in terms of the six transition rates Γ_{ii} between the states i, j = L, R, 0,

$$w^* \approx w + \frac{1 - w}{\Gamma_{det}} \left(\frac{\Gamma_{L0} \Gamma_{0R}}{\Gamma_{LR}} + \frac{\Gamma_{RL} \Gamma_{L0}}{\Gamma_{R0}} + \frac{\Gamma_{0R} \Gamma_{RL}}{\Gamma_{0L}} \right), \quad (3)$$

where $w = \exp(eV_{\text{DOD}}/k_{\text{B}}T)$. Qualitatively, the effect can be understood as follows. At a nonzero bias, transitions directed toward the drain occur with faster rates (Γ_{L0}, Γ_{RL} , Γ_{0R}) than those directed toward the source (Γ_{0L} , Γ_{LR} , Γ_{R0}). It is therefore more likely that the detector misses a charge flowing toward the drain than toward the source. In short, the ratio $P_{\tau}(n)/P_{\tau}(-n)$ becomes underestimated for n > 0. It is important to stress that, despite the similar phenomenology, the correction we employ here has a very different quality than the effective temperature due to the QPC backaction introduced in Ref. [19]. QPC backaction implies excitation of degrees of freedom in the microscopic system of interest, whereas the effect of finite bandwidth is a matter of the imperfect room-temperature electronics and leaves the microscopic system unperturbed. Additional data on the dependence of $P_{\tau}(n)$ on QPC bias voltage is presented in the Supplemental Material to this article.

In the finite-bandwidth model, Γ_{det} plays the role of a mean inverse reaction time of the detector. We use a simulation to determine this parameter for our particular detection scheme. A square pulse of duration τ_p is filtered and resampled the same way as the experimental signal. Our value of $\Gamma_{det} = (0.59 \pm 0.12)$ kHz is then defined as the inverse of the minimum τ_p for which at least three sampled points reach 50% of the square-pulse amplitude. The dashed lines in Figs. 2(c)–2(e) show the theoretical expectation calculated with this value for Γ_{det} and the experimentally determined Γ_{ij} [18], and indeed agree much better with the experiment. The gray shaded areas indicate the uncertainty in the slope which is mainly determined by the uncertainty in Γ_{det} . We emphasize that this analysis does not involve any free parameters.

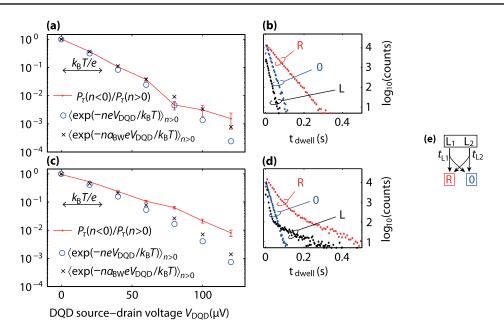


FIG. 3. (a) The red data points show the V_{DQD} dependence of the left-hand side of Eq. (4), which is the ratio of entropy-consuming vs entropy-producing cycles, with error bars that indicate its estimated standard deviation. The blue circles show the right-hand side, which is the average of the Boltzmann factor among the entropy-consuming cycles. The FT [Eq. (4)] is satisfied if the finite detector bandwidth is taken into account in the form of a correction factor α_{BW} to the exponent in Eq. (4) (shown as crosses). The uncertainty in the finite-bandwidth correction is comparable to the error in $P_{\tau}(n < 0)/P_{\tau}(n > 0)$ for all bias voltages. (b) Dwell-time distributions of the G_{QPC} signal in the states L, R, and 0, as extracted from the data set in (a) at the point $V_{DQD} = 0 \ \mu V$. (c) and (d) Same as (a) and (b), but measured at a slightly different gate-voltage configuration. In this case, the dwell times at zero bias (d) are nonexponentially distributed for the states L and R. The finite-bandwidth model [the crosses in (c)] is not valid for this case but plotted for comparison. (e) Diagram of the decay of a single-charge state L (black rectangle) that consists of two internal QD states L1 and L2. Such a process can lead to nonexponentially distributed charge-dwell times as shown in (d).

The DQD voltage of 20 μ V used in the temperaturedependence measurements is comparable with the thermal voltage $k_{\rm B}T/e = 28...58 \ \mu$ V, so the system is not too far from thermal equilibrium. The FT also applies far away from equilibrium, however. To test its predictions in this regime, we have also performed bias-dependence measurements with $V_{\rm DQD}$ up to 120 μ V, i.e., about 4.3 \times $k_{\rm B}T/e$ at T = 330 mK. The data are shown in Fig. 3 and are based on the analysis of 2000 $G_{\rm QPC}$ time segments of length $\tau = 2$ s for each DQD voltage. For clarity and to reduce the statistical error for large voltages, we plot an integrated version of the FT relating the total fractions of entropy-producing and entropy-consuming cycles:

$$\frac{\sum_{n<0} P_{\tau}(n)}{\sum_{n>0} P_{\tau}(n)} = \frac{\sum_{n>0} P_{\tau}(n) e^{-neV_{\text{DQD}}/k_{\text{B}}T}}{\sum_{n>0} P_{\tau}(n)}.$$
 (4)

In our measurements of the V_{DQD} dependence, we keep the gate voltages V_{G1} and V_{G2} fixed. The choice of V_{G1} and V_{G2} determines the level arrangement of the DQD with respect to the electrochemical potentials of the leads and is *a priori* not relevant for the validity of Eq. (4). In our measurements, we observe a rather strong effect of this choice, which is not fully understood. Thus, we plot in Figs. 3(a) and 3(c) the data of two representative measurements. The differing gate-voltage configurations in the two measurements result in differing relative arrangements of the electrochemical potentials of source, drain, left, and right QD (denoted by $\mu_{\rm S} = eV_{\rm DQD}/2$, $\mu_{\rm D} = -eV_{\rm DQD}/2$, $\mu_{\rm L}$, and $\mu_{\rm R}$, respectively). In measurement (a), we have $\mu_{\rm L} - \mu_{\rm R} \approx 80 \ \mu eV$ and $(\mu_{\rm L} + \mu_{\rm R})/2 \approx 10 \ \mu eV$, whereas in measurement (b), we have $\mu_{\rm L} - \mu_{\rm R} \approx 55 \ \mu eV$ and $(\mu_{\rm L} + \mu_{\rm R})/2 \approx -5 \ \mu eV$, as determined by finite-bias spectroscopy.

The red data points in Fig. 3(a) plot the left-hand side of Eq. (4) as a function of the source-drain voltage. The quantity rapidly decreases with the voltage, as charge transfer against the bias occurs less and less frequently. Measurements at even higher DQD voltages are eventually limited by the necessary, exponentially increasing measurement time. The blue circles plot the right-hand side, calculated without the finite-bandwidth correction. Similar to the low-bias case, there is a systematic deviation. For the black crosses, the exponent in Eq. (4) is replaced with the bandwidth-corrected version $\alpha_{BW}neV_{DQD}/k_BT$, and we see that the observed deviation can entirely be attributed to this measurement issue.

In the second measurement shown in Fig. 3(c), there is a larger discrepancy between the two sides of Eq. (4) which goes beyond the effect of the finite detector bandwidth. We

observe that this discrepancy coincides with the presence of nonexponential distributions of the random dwell times in the three DOD charge states. Figs. 3(a) and 3(d) show the histograms of the signal dwell times in L, R, and 0, measured at $V_{\text{DOD}} = 0 \ \mu \text{V}$ for the two configurations. In configuration (a), the dwell times follow exponential distributions with a single lifetime. This is not the case in configuration (c), where the states L and R are not characterized by a single lifetime. This is indicative of the population of additional (excited) states in the DQD [32]. When we consider the example of the left QD, a nonzero population p_{L2} of a long-lived excited state L2 means that the charge state L can no longer be identified with the QD ground state L1. The QPC, which monitors the dynamics of the charge states, sees a dwell time t in the state L distributed according to $p_{L1}t_{L1}^{-1}\exp(-t/t_{L1}) +$ $p_{L2}t_{L2}^{-1}\exp(-t/t_{L2})$, where t_{L1} and t_{L2} are the decay times of the two QD states into R and 0 [cf. Fig. 3(e)]. In configuration (c), the QD energies are lower than those in configuration (a), and this fact makes population of excited states more probable. Although the precise level arrangement cannot be reconstructed from our data, the measurement in Fig. 3(c) demonstrates the sensitivity of such a test of the FT to the details of the DOD level structure.

In conclusion, we have presented an extensive quantitative test of the fluctuation theorem for electron transport through a DQD, covering different temperatures and strong nonequilibrium transport conditions. Our results validate the theory in the near-equilibrium regime with a good accuracy. A remaining discrepancy is very well explained with a master-equation model of the finite-bandwidth detection. This agreement proves the usefulness of this corrective approach in compensating for a slow detector. In the regime far from equilibrium, our results display a strong dependence on the internal DQD level structure controlled by gate voltages. In configurations where our system is well described as a three-state Markovian system, we observe a good agreement with theory, demonstrating the potential of the DQD as a model system for the study of nonequilibrium thermodynamics. Our results anticipate the test of the FT in quantum-coherent electron transport, which requires the measurement of thermal fluctuations on a sub-Kelvin energy scale.

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