



JEDI: These aren't the JSON documents you're looking for...

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ABSTRACT

The JavaScript Object Notation (JSON) is a popular data format used in document stores to natively support semi-structured data. In this paper, we address the problem of JSON similarity lookup queries: given a query document and a distance threshold τ , retrieve all documents that are within τ from the query document. Different from other hierarchical formats such as XML, JSON supports both ordered and unordered sibling collections within a single document which poses a new challenge to the tree model and distance computation. We propose JSON tree, a lossless tree representation of JSON documents, and define the JSON Edit Distance (JEDI), the first edit-based distance measure for JSON. We develop QuickJEDI, an algorithm that computes JEDI by leveraging a new technique to prune expensive sibling matchings. It outperforms a baseline algorithm by an order of magnitude in runtime. To boost the performance of JSON similarity queries, we introduce an index called JSIM and an effective upper bound based on tree sorting. Our upper bound algorithm runs in $O(n\tau)$ time and $O(n + \tau \log n)$ space, which substantially improves the previous best bound of $O(n^2)$ time and $O(n \log n)$ space (where n is the tree size). Our experimental evaluation shows that our solution scales to databases with millions of documents and JSON trees with tens of thousands of nodes.

CCS CONCEPTS

• Information systems → Semi-structured data; Similarity measures; Database query processing; Proximity search.

KEYWORDS

JSON edit distance, similarity lookup queries, document stores

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1 INTRODUCTION

The JavaScript Object Notation (JSON) has evolved into one of the most prominent data formats. It is used in a large variety of

scenarios, e.g., to publish datasets [20, 54] or as an open-standard data interchange format in mobile and web applications [19]. JSON-like formats are also used in document stores to natively support semi-structured data [1, 6, 39].

As JSON does not enforce a schema, it increases the variety in which a given piece of information can be represented. Consider the following scenario: a web crawler collects movies in JSON format from multiple sources and saves them in a document store. In order to avoid duplicate entries, the crawler queries the database for the existence of the movie to be inserted. However, a query for exact duplicates is not effective since key names or the structure will typically vary. Consider the document in Figure 1a, which was discovered by the crawler. The document in Figure 1b already resides in the database. Both documents represent the same movie, but due to their different representations a query for exact duplicates will fail. Detecting near-duplicate entries remains a challenge.

```

{
  "title" : "Star Wars -
              A New Hope",
  "running time" : 125,
  "cast" : {
    "Han" : "Ford",
    "Leia" : "Fisher"
  }
}
(a)

{
  "cast" : [
    "Ford",
    "Fisher"
  ],
  "running time" : 125,
  "name" : "Star Wars -
              A New Hope",
}
(b)
    
```

Figure 1: Two JSON representations of the same movie.

In this paper, we study the following problem of similarity queries for JSON: given a query document T_q , retrieve all documents T_i from a database of JSON documents that are within a given distance threshold τ from T_q . To answer such queries, a distance function that assesses the similarity of two JSON documents is needed.

JSON similarity queries are poorly supported in many existing systems. Stand-alone tools for JSON differences are either line-based hence ignore the hierarchical information [15, 25], or do not provide any guarantees on the quality of the result [11]. Similarity functions related to JSON in database systems are limited to basic values, e.g., strings and sets, and cannot be used to compute the distance between JSON documents [17, 33, 35, 39, 42]. For other data formats, similarity queries and the related distance measures are well studied, e.g., for XML [16, 21, 32, 37] data, which – like JSON – is a hierarchical data format. Common approaches for XML are based on the well-known tree edit distance [41], which is the minimal difference between two documents respecting both their hierarchical structure and data values. For JSON, assessing a minimal, edit-based difference is still an unsolved problem.

Assessing the edit-based difference between JSON documents is challenging. JSON differs from other hierarchical data formats,



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such as XML, in that it supports both ordered and unordered sibling nodes within a single document. This uniqueness calls (1) for a tree representation that models both types of siblings, and (2) for a distance function that assesses the similarity of the resulting trees. In particular, the support for unordered sibling collections poses a computational challenge: We show that computing the minimal difference between JSON documents is NP-hard when no restrictions are imposed on the standard set of node edit operations, i.e., insertion, deletion, and renaming.

We solve the problem of computing a minimal, edit-based difference between JSON documents. (1) We develop a lossless tree representation of JSON that models both ordered and unordered siblings. (2) We show that the edit distance in its general formulation leads to non-intuitive results. We therefore restrict the edit operations to respect the nested document structure of JSON and propose the first edit-based distance measure for JSON documents, called *JSON Edit Distance (JEDI)*. The function guarantees that the difference is minimal and the document nesting is respected.

We present an algorithm for JEDI, called *QuickJEDI*, which is based on a recursive solution. Compared to previous edit distance algorithms for related problems [59, 60], this algorithm leverages a novel technique, the aggregate size bound, to prune the expensive min-cost matching between sibling sets in each recursive step. This optimization leads to runtime improvements of up to an order of magnitude. We further propose the *JSIM* index that only searches the τ -range around the query document instead of scanning all documents. JSIM is a 4-level tree and each level routes the search into one or more branches. A new technique allows us to reduce the τ -range at each level, thus reducing the total number of explored branches. The documents returned by the index are filtered with a highly effective upper bound based on tree sorting, for which we improve the computational complexity from quadratic to linear.

The main contributions of this paper are:

- We show that the existing formulation of the tree edit distance can lead to non-intuitive results and is NP-hard for JSON. To solve the problem, we introduce JSON trees, a lossless tree representation of JSON documents, and JEDI, the first edit-based distance measure for JSON.
- We develop a new algorithm, QuickJEDI, for computing JEDI in $O(n^2 d \log d)$ time and $O(n^2)$ space for JSON trees of size n and maximum degree d . The algorithm leverages the new aggregate size bound to prune expensive sibling matchings.
- To improve the performance of JSON similarity queries, we introduce (1) a novel index called JSIM; (2) an effective upper bound based on tree sorting, and an algorithm for computing the bound in $O(n\tau)$ time and $O(n + \tau \log n)$ space, which substantially improves the previous best bound of $O(n^2)$ time and $O(n \log n)$ space.
- Our empirical study on 22 JSON datasets suggests that our solution scales to databases with millions of documents and can handle large JSON trees with tens of thousands of nodes.

2 EDIT-BASED DISTANCE FOR JSON TREES

We now introduce a new distance measure that assesses the minimal difference of two JSON documents by a given set of allowable edit operations and a novel tree representation of JSON data. To our

best knowledge, this measure is the first distance for JSON that respects its nested structure and provides quality guarantees, i.e., the difference defining the distance is guaranteed to be minimal.

The JSON Data Format. We recap the definition of the JSON data format (cf. RFC8259 [8]). A JSON document is recursively composed of values, arrays, and objects: (1) A *value* is either a literal (string, number, boolean, or null), an object, or an array. (2) An *array* is an ordered, possibly empty list of *values* enclosed by brackets. (3) An *object* is an unordered, possibly empty collection of key-value pairs enclosed by curly braces. The *keys* (called “names” in [8]) are string literals that are unique within an object.

EXAMPLE 1. *The JSON document in Figure 1a is an object of three key-value pairs. The keys are "title", "running time", and "cast". The value of "cast" is an object, and the other values are string and number literals.*

2.1 JSON Tree Representation

Due to its recursive definition, JSON is hierarchically structured and naturally represented as a tree. The specifics of transforming a JSON document into a tree, however, are not obvious. Previous attempts to model JSON as trees are unsuitable for distances based on a minimal number of node edit operations because either (1) the object and array information is not modelled [34, 46], e.g., $[['A']]$ and $'A'$ are transformed to identical trees such that the structural information is lost; or (2) arrays are modeled as objects with the array index as a key [7, 47], which generates an error of $O(n)$ when a single element in an array of size n is missing. Consider two arrays $['A', 'B', 'C', 'D']$ and $['B', 'C', 'D']$: the array index keys of all identical elements differ due to element $'A'$ that is not present in the second array. Tree models for XML documents are not suitable since XML is ordered by definition; although XML has been modeled as unordered trees to capture the semantics of data-centric XML [2], these models do not support a mix of ordered and unordered siblings.

JSON Tree. We introduce the new concept of a *JSON tree*. The constraints that we impose on JSON trees model all aspects of JSON data and allow for a lossless transformation between JSON documents and JSON trees.

A JSON tree $T = (N, E, \Lambda, \Psi, <_S)$ is a tree with nodes N and edges $E \subseteq N \times N$. The label of node v , $\Lambda(v)$, is a literal value; the labels of array and object nodes are *null*. Function Ψ assigns a type to each node $v \in N$, $\Psi(v) \in \{\text{object}, \text{array}, \text{key}, \text{literal}\}$. The *sibling order*, $<_S$, defines a strict, partial order on the nodes of a tree. Two nodes $x, y \in N(T)$ of a JSON tree are *comparable*, i.e., $x <_S y$ or $y <_S x$, iff one of the following holds:

- (1) x and y are children of the same array node; or
- (2) there is an ancestor x' of x (including x) and an ancestor y' of y (including y) such that x' and y' are comparable.

In the second condition, $x <_S y$ iff $x' <_S y'$. Intuitively, the order among the children of an array node imposes an order on the subtrees rooted in these children; all other nodes are incomparable. The children of an object node (i.e., key nodes) must have unique labels among their siblings.

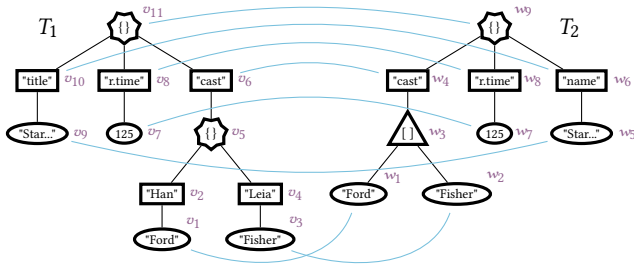


Figure 2: JSON trees of the documents in Figure 1. Object nodes are visualized as stars with symbol $\{ \}$, array nodes as triangles with symbol $[]$, keys as rectangles, and literals as ellipses with their original labels, respectively. Blue lines – depict the JSON edit mapping, and v_i, w_j are node identifiers.

Transformation. A JSON document is transformed into a JSON tree by recursively unnesting the document. Objects become nodes of type object (label *null*) with key node children; a key node (labeled with its name) has a single child subtree that represents its value; an array (label *null*) becomes an array node with the i -th value in its list becoming the i -th child subtree defining the sibling order $<_S$. Literals are leaf nodes of type literal (labeled with the respective literal value).

EXAMPLE 2. Figure 2 shows the JSON tree representation of the two documents in Figure 1.

Notation. With $N(T)$ resp. $E(T)$, we denote the nodes resp. edges of a JSON tree T . $|T| = |N(T)|$ is the size of T , $v \in T$ is shorthand for $v \in N(T)$. The parent of a node $v \in T$ is $p(v)$, the set of its children is $chd(v)$, the degree is $deg(v) = |chd(v)|$; the degree of tree T , $deg(T)$, is the largest degree of a node in T ; $anc(v)$ and $desc(v)$ denote the set of ancestors resp. descendants of v (excluding v). The lowest common ancestor of two nodes v, w is $lca(v, w)$.

$T[v]$ denotes the subtree rooted in node v . The subforest of node v , denoted $F[v]$, is the set of subtrees of its children, $T[v_i], v_i \in chd(v)$. If an order is defined on $chd(v)$, then the subforest $F[v]$ is ordered by the root nodes of its subtrees. We use ϵ to denote the empty node, which is not part of any tree. We define $T[\epsilon]$ to be the empty subtree with $N(T[\epsilon]) = \emptyset$ and $E(T[\epsilon]) = \emptyset$, and $F[\epsilon] = \emptyset$ to be the empty subforest. The postorder traversal recursively visits all children of a node v before visiting v (ordered children in ascending order and unordered children in arbitrary order; $post(v)$ is the position of node v in a given postorder traversal).

2.2 JSON Edit Distance (JEDI)

Given two JSON trees, our goal is to assess their similarity. We aim for a similarity measure that captures fine-grained differences, allows an intuitive interpretation of the similarity value, and guarantees the minimality of the similarity value. A well-known approach that satisfies these requirements is the edit distance, which has been applied to strings [58], trees [41], and graphs [23].

The edit distances for general, rooted, labeled trees [48, 61], however, are not applicable to JSON trees since they can only deal with either ordered or unordered trees, but not with a mix of the two. In JSON trees, the order of array children must be respected,

whereas the order of object children must be ignored. Note that all nodes in subtree $T[c_i]$ appear before the nodes in $T[c_j]$ if $c_i <_S c_j$, i.e., the order imposed by an array is propagated to the subtrees rooted in the children. We are the first to define an edit distance that can deal with both ordered and unordered siblings in a single tree. Further, we respect the node types of JSON, e.g., a literal value should not be aligned to a key node.

Similar to the edit distance for other data types, we define the JSON edit distance (JEDI) as the minimum number of edit operations required to transform one tree to the other. Allowable operations include: *delete* node v and connect its children to the parent of v ; *insert* a new node w between an existing node v and a possibly empty subset of v 's children; and *rename* the label of node v .

JSON Edit Mapping. Following previous works, we formally define the JSON edit distance using the concept of an edit mapping. The edit mapping aligns the nodes of the input trees, T_1 and T_2 , and must respect some constraints to be valid. The interpretation is as follows: nodes in T_1 that are not mapped are deleted, nodes in T_2 that are not mapped are inserted, and nodes that are mapped are renamed. The constraints imposed on the mapping control which edit operations are allowable depending on the tree context; they are discussed in detail below.

DEFINITION 1 (JSON EDIT MAPPING). A mapping $M \subseteq N(T_1) \times N(T_2)$ is a JSON edit mapping from T_1 to T_2 iff the following constraints hold for any node pairs $(v, w), (v', w'), (v'', w'') \in M$:

- (1) $v = v'$ iff $w = w'$ [one-to-one],
- (2) v is an ancestor of v' iff w is an ancestor of w' [ancestor],
- (3) $type(v) = type(w)$ [type],
- (4) if $v <_S v'$ and w is comparable to w' in $<_S$, then $w <_S w'$ [array-order],
- (5) $lca(v, v')$ is a proper ancestor of v'' iff $lca(w, w')$ is a proper ancestor of w'' [document-preserving].

A mapping $M' \subseteq M$ between two subforest $F_1[v]$ and $F_2[w]$ is an edit mapping iff M' is an edit mapping from $T_1[v]$ to $T_2[w]$.

The cost of all edit operations is one except for rename: if the labels of the mapped nodes are identical, then the cost is zero. The cost of an edit mapping, $\gamma(M)$, is the total cost of all edit operations. The edit distance is defined as the cost of the edit mapping with the lowest cost.

EXAMPLE 3. Figure 2 shows a JSON edit mapping between two JSON trees. The cost of the mapping is 5: delete nodes "Han", "Leia", and $\{ \}$ from the left tree; insert $[]$ into the right tree; rename "title" to "name". There is no mapping with a lower cost, thus JEDI is 5.

Constraints (1) and (2) of the edit mapping ensure that the node mapping can be interpreted as a set of edit operations. Constraint (3) ensures that labels can only be renamed between nodes of the same type. This prevents that nodes with identical labels but different types (e.g., a key and a literal value may have identical labels) are mapped at zero cost, thus ignoring their difference. Note that it is still possible to substitute (delete and insert) a node of one type by a node of another type, but the cost is higher than for rename. The array-order constraint (4) uses the partial order $<_S$ defined on JSON trees to enforce the order imposed by array nodes; children of object nodes are not restricted and can be arbitrarily mapped.

Document-Preserving Constraint. The recursive definition of JSON gives rise to its nested document structure. A nested document (e.g., representing the cast of a movie) often is meaningful only in the context of the enclosing document (in the example, the movie the cast belongs to). Constraint (5), the *document-preserving* constraint, forces the edit mappings to respect the nested document structure of JSON and leads to more intuitive mappings. In particular, shortcuts that delete the root nodes of subtrees (thus disassembling the documents they root), rearrange their nested subtrees, and recombine the nested subtrees into new documents by inserting new subtree roots are prevented. We illustrate the effect of this constraint in Example 4.

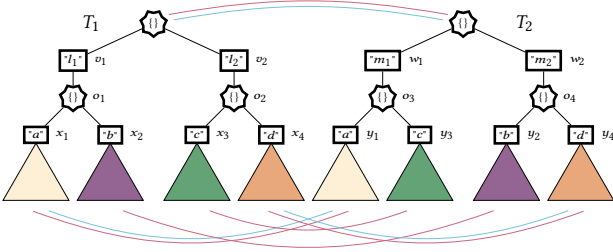


Figure 3: Edit mappings with and without the document-preserving constraint.

EXAMPLE 4. Consider the schematic illustration of the two JSON trees T_1 and T_2 in Figure 3. Each tree consists of two subtrees $T_1[v_1]$, $T_1[v_2]$ resp. $T_2[w_1]$, $T_2[w_2]$, which in turn are composed of an object node and two smaller subtrees $T_1[x_i]$ resp. $T_2[y_j]$ each, $i, j \leq 4$. The subtree pairs $T_1[x_i]$ and $T_2[y_j]$, $i = j$, are identical (same color in the figure) and are all of size n . Any two subtrees $T_1[v_i]$ and $T_2[w_j]$, $i \neq j$, are different with an edit mapping of cost $O(n)$.

The minimum-cost edit mapping (with document-preserving constraint) will delete $T_1[x_2]$ and $T_1[x_3]$, and insert their identical counterparts $T_2[y_2]$ and $T_2[y_3]$ since they belong to different documents in T_2 . An edit mapping that does not respect the document-preserving constraint, however, has only cost 8: delete nodes v_1, v_2, o_1, o_2 , insert o_3 as parent of y_1, y_3 ; o_4 as parent of y_2, y_4 ; w_1 as parent of o_3 ; and w_2 as parent of o_4 . Without the document-preserving constraint, rearranged subtrees form new documents, which is not desired for JSON trees.

As a pleasant side effect, the document-preserving constraint substantially reduces the search space for the minimal cost mapping and allows for faster algorithms. In fact, we show that finding a minimum JSON edit mapping that ignores the document-preserving constraint is an NP-hard problem [30]. The proof is by reducing the problem of exact cover by 3-sets (X3C).

THEOREM 1. Without the document-preserving constraint, the problem of computing the JSON edit distance between two JSON trees is NP-hard.

3 AN EFFICIENT ALGORITHM FOR JEDI

Next, we introduce QuickJEDI, an efficient algorithm for computing the JSON edit distance. We first discuss a baseline solution, analyze its performance bottlenecks, and finally propose effective techniques to address these bottlenecks.

3.1 A Baseline Algorithm

None of the previous algorithms that computes the minimum edit distances between trees is applicable in our scenario due to the type and the array-order constraints in the JSON edit mapping (cf. Definition 1). Our baseline extends two algorithms for the so-called *constrained tree edit distance*. These algorithms compute minimal edits under the document-preserving constraint (constraint (5) in the JSON edit mapping) for ordered [59] resp. unordered trees [60]. Since a single JSON tree may include both ordered and unordered siblings, neither of the two algorithms is applicable; also, these algorithms deal with generic trees and do not consider node types.

We recap the solutions for the constrained tree edit distance and show how they can be extended to compute the JSON edit distance. Both algorithms are based on a recursive solution that is implemented using dynamic programming.

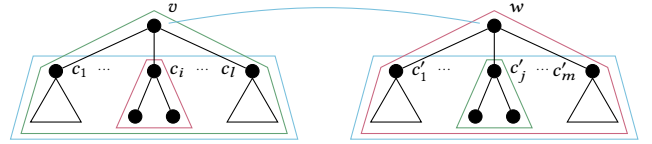


Figure 4: Recursive decomposition of two trees; pairs of subtrees resp. subforests of the same color form the subproblems required to compute the distance btw. $T[v]$ and $T[w]$.

Recursive Solution. The recursive solution decomposes two trees T_1 and T_2 with root nodes $v \in T_1$ and $w \in T_2$ into subtrees and subforests as illustrated in Figure 4. The distance between T_1 and T_2 is computed from the distances between the subproblems resulting from their decomposition. With $dt(v, w)$ we denote the *tree distance* between subtrees $T_1[v]$ and $T_2[w]$, and $df(v, w)$ denotes the *forest distance* between subforests $F_1[v]$ and $F_2[w]$. Then, the recursive solution is defined as follows:

$$df(\epsilon, \epsilon) = 0; dt(\epsilon, \epsilon) = 0$$

$$df(v, \epsilon) = \sum_{c \in \text{chd}(v)} dt(c, \epsilon); dt(v, \epsilon) = df(v, \epsilon) + \gamma(v, \epsilon) \quad (1)$$

$$df(\epsilon, w) = \sum_{c' \in \text{chd}(w)} dt(\epsilon, c'); dt(\epsilon, w) = df(\epsilon, w) + \gamma(\epsilon, w)$$

$$df(v, w) = \min \begin{cases} df(\epsilon, w) + \min_{c' \in \text{chd}(w)} \{df(v, c') - df(\epsilon, c')\} & (2a) \\ df(v, \epsilon) + \min_{c \in \text{chd}(v)} \{df(c, w) - df(c, \epsilon)\} & (2b) \\ \text{Min-cost-matching}(\text{chd}(v), \text{chd}(w)) & (2c) \end{cases}$$

$$dt(v, w) = \min \begin{cases} dt(\epsilon, w) + \min_{c' \in \text{chd}(w)} \{dt(v, c') - dt(\epsilon, c')\} & (3a) \\ dt(v, \epsilon) + \min_{c \in \text{chd}(v)} \{dt(c, w) - dt(c, \epsilon)\} & (3b) \\ df(v, w) + \gamma(v, w) & (3c) \end{cases}$$

The tree distance, $dt(v, w)$, is the minimum cost of three scenarios (cf. Figure 4 and Eq. 3), each of which represents an edit operation: (3a) w is *inserted*, hence the nodes in subtree $T_1[v]$ are mapped to the nodes of one of w 's children $T_2[c'_j]$ (green), (3b) v is *deleted*, hence the nodes of subtree $T_2[w]$ are mapped to the nodes of one of v 's children $T_1[c_i]$ (red), and (3c) v is mapped to w with *rename* cost $\gamma(v, w)$, hence also the subtrees of their children are mapped (blue); $\gamma(v, \epsilon)$ and $\gamma(\epsilon, w)$ denote the cost of deleting resp. inserting a node. The cost of matching the children of nodes v and w in scenario (3c)

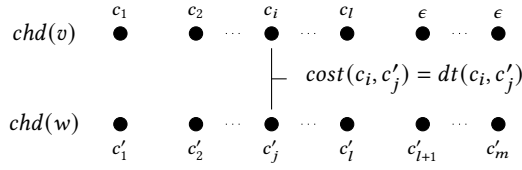


Figure 5: Bipartite graph for the nodes $chd(v)$ and $chd(w)$.

is equivalent to their forest distance $df(v, w)$. The *base cases* of the recursion are shown in Eq. 1. The forest distance, $df(v, w)$, (cf. Eq. 2) is computed analogously for insertion (2a) and deletion (2b). In the third scenario (2c), a minimum-cost matching between the subtrees rooted in $chd(v)$ and $chd(w)$ is established.

The *minimum-cost matching* \mathcal{M} is one-to-one and models the subtrees rooted in $chd(v)$ and $chd(w)$ as nodes of a bipartite graph (cf. Figure 5); the cost of an edge between two subtrees rooted in $c_i \in chd(v)$ and $c'_j \in chd(w)$ is their tree distance, $dt(c_i, c'_j)$. In the unordered case [60], the minimum-cost bipartite graph matching, $M_{BPM(v,w)}$, with cost $\gamma(M_{BPM(v,w)}) = BPM(v, w)$ must be computed (e.g., using a min-cost max-flow algorithm [50]). In the ordered case [59], the subtree sequence edit distance matching, $M_{SED(v,w)}$, with cost $\gamma(M_{SED(v,w)}) = SED(v, w)$ must be computed.

Adaption to JSON. In Lemma 1, we show how previous solutions can be extended to compute JEDI between two JSON trees.

LEMMA 1. Given two JSON trees T_1 and T_2 , the recursive formulas (1), (2), and (3), compute the JSON edit distance between T_1 and T_2 , $JEDI(T_1, T_2) = dt(\text{root}(T_1), \text{root}(T_2))$ with the following extensions:

- (1) The minimum-cost matching $\mathcal{M} \subseteq chd(v) \times chd(w)$ observes the node type:

$$\mathcal{M} = \begin{cases} M_{SED(v,w)} & \text{if } type(v) = type(w) = array \\ M_{BPM(v,w)} & \text{otherwise} \end{cases} \quad (4)$$

- (2) The rename cost must be redefined as follows:

$$\gamma'(v, w) = \begin{cases} \gamma(v, w) & \text{if } type(v) = type(w) \\ \gamma(v, \epsilon) + \gamma(\epsilon, w) & \text{otherwise} \end{cases} \quad (5)$$

Dynamic Programming Implementation. Algorithm 1 implements the recursive solution of Lemma 1. The results for subproblems are stored in two matrices, dt and df , each of size $(|T_1| + 1) \times (|T_2| + 1)$. The distance between subtrees $T_1[v]$ and $T_2[w]$ is stored in row v and column w , and we refer to the value as $dt(v, w)$; similarly, $df(v, w)$ stores the distance between subforests $F_1[v]$ and $F_2[w]$. Table 1 shows examples of a forest and a tree distance matrix.

Initialization: The first row and column of each matrix are initialized in lines 1-8. Mapping two empty trees has cost 0; for all other nodes, the cost results from summing up the deletion resp. insertion costs of their child subtrees, e.g., $dt(v_6, \epsilon) = 6$ (cf. Table 1) is the cost of deleting the subtree of node "cast" in Figure 2.

Distance Computation: The algorithm processes the tree nodes bottom-up in postorder and the distance matrices are filled row by row. We label the three cases in Eq. 2 (forest distance) with *insF* (2a), *delF* (2b), and *renF* (2c); the cases in Eq. 3 (tree distance) are labeled *insT* (3a), *delT* (3b), *renT* (3c). Due to the postorder traversal, all values required to compute $dt(v, w)$ and $df(v, w)$ are available in the distance matrices. To compute *renF*, a min-cost matching \mathcal{M}

among the children must be established. If both v and w are array nodes (ordered case), the edit distance between ordered sequences of siblings establishes the min-cost matching (line 16), in all other cases a bipartite graph matching must be computed (line 18). The distance between T_1 and T_2 results in the lower right corner of the tree distance matrix, e.g., $dt(\text{root}(T_1), \text{root}(T_2)) = 5$ in Table 1.

Complexity: The *space complexity* is dominated by the distance matrices of size $O(|T_1||T_2|)$. The runtime is dominated by the bipartite graph matching, which for a node pair v, w with degrees $d_v = deg(v)$ and $d_w = deg(w)$ is computed in time $O(d_v \times d_w \times (d_v + d_w) \times \log(d_v + d_w))$ using a min-cost max-flow algorithm [50]. For the overall algorithm (cf. Algorithm 1), the *runtime complexity* is $O(|T_1| \times |T_2| \times (deg(T_1) + deg(T_2)) \times \log(deg(T_1) + deg(T_2)))$ [60].

| df | ϵ | w_1 | w_2 | ... | w_6 | w_9 | dt | ϵ | w_1 | w_2 | ... | w_6 | w_9 |
|------------|------------|-------|-------|-----|-------|-------|------------|------------|-------|-------|-----|-------|-------|
| ϵ | 0 | 0 | 0 | ... | 1 | 8 | ϵ | 0 | 1 | 1 | ... | 2 | 9 |
| v_9 | 0 | 0 | 0 | ... | 1 | 8 | v_9 | 1 | 1 | 1 | ... | 1 | 8 |
| v_{10} | 1 | 1 | 1 | ... | 0 | 7 | v_{10} | 2 | 2 | 2 | ... | 1 | 8 |
| ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| v_6 | 5 | 5 | 5 | ... | 5 | 8 | v_6 | 6 | 5 | 5 | ... | 6 | 8 |
| v_{11} | 10 | 10 | 10 | ... | 9 | 5 | v_{11} | 11 | 10 | 10 | ... | 10 | 5 |

Table 1: Forest and tree distance matrices df and dt for the JSON trees in Figure 2.

3.2 Avoiding the Expensive Min-Cost Matching

JEDI must compute the min-cost matching between the child subtrees of each node pair of the input trees. This step is expensive and dominates the overall runtime. In this section, we show that the expensive min-cost computation can be avoided in many cases, thus substantially improving the runtime of the distance computation.

The key idea is that the min-cost matching in Eq. (2) is the minimum of three values. Two of them are efficient to compute, one is the expensive matching. If we can show that the cost of the matching is higher than one of the other two values, the exact cost of the matching is irrelevant and the computation can be skipped.

We are the first to follow this approach. The challenge is to identify a lower bound on the min-cost matching that is both effective and can be computed efficiently. Efficiency is crucial since the lower bound filter will be evaluated *in addition* to the min-cost matching whenever the filter cannot avoid the matching computation. The min-cost matching is a bipartite graph matching in the unordered case and a sequence edit distance computation in the ordered case. Since the sequence edit distance cannot be smaller than the bipartite graph matching cost, we focus on the bipartite graph matching.

Figure 5 illustrates the bipartite graph for the nodes $chd(v)$ and $chd(w)$. The edge cost $cost(c_i, c'_j)$ between two nodes $c_i \in chd(v)$ and $c'_j \in chd(w)$ is the tree distance between the subtrees rooted in these nodes, $dt(c_i, c'_j)$. To simplify the presentation, we assume $l = deg(v) < deg(w) = m$, i.e., $k = m - l$ subtrees will be matched to the empty tree. We denote the cost of the bipartite matching between the children of two nodes v, w with $BPM(v, w)$.

Aggregate Size Bound. To establish a lower bound on the bipartite graph matching cost, we leverage the specific characteristics of the edge costs in our scenario. Since the edge costs are given by the respective subtree distances, we can bound the cost

Algorithm 1: JEDI-baseline(T_1, T_2)

Input: JSON trees T_1 and T_2 .
Result: JSON Edit Distance: JEDI(T_1, T_2).

```

/* Initialization. */
1 dt(0, 0) = 0 /* Tree distance matrix of size  $T_1 + 1 \times T_2 + 1$ . */
2 df(0, 0) = 0 /* Forest distance matrix of size  $T_1 + 1 \times T_2 + 1$ . */
3 for v in N( $T_1$ ) do
4   df(v, 0) =  $\sum_{c \in \text{chd}(v)} \text{dt}(c, 0)$ 
5   dt(v, 0) = df(v, 0) +  $\gamma(v, \lambda)$ 
6 for w in N( $T_2$ ) do
7   df(0, w) =  $\sum_{c' \in \text{chd}(w)} \text{dt}(0, c')$ 
8   dt(0, w) = df(0, w) +  $\gamma(\lambda, w)$ 
/* Distance computation. */
9 for v in N( $T_1$ ) do /* In postorder. */
10  for w in N( $T_2$ ) do /* In postorder. */
11    /* Cost for inserting node w. */
12    insF = df(0, w) +  $\min_{c' \in \text{chd}(w)} \{\text{df}(v, c') - \text{df}(0, c')\}$ 
13    insT = dt(0, w) +  $\min_{c' \in \text{chd}(w)} \{\text{dt}(v, c') - \text{dt}(0, c')\}$ 
14    /* Cost for deleting node v. */
15    delF = df(v, 0) +  $\min_{c \in \text{chd}(v)} \{\text{df}(c, w) - \text{df}(c, 0)\}$ 
16    delT = dt(v, 0) +  $\min_{c \in \text{chd}(v)} \{\text{dt}(c, w) - \text{dt}(c, 0)\}$ 
17    /* Cost for renaming node v to node w. */
18    if type(v) == type(w) == array then
19      renF = SED(v, w)
20    else
21      renF = BPM(v, w)
22    df(v, w) = min{insF, delF, renF}
23    renT = df(v, w) +  $\gamma'(v, w')$ 
24    dt(v, w) = min{insT, delT, renT}
25 return dt(root( $T_1$ ), root( $T_2$ ))

```

by the size difference of the subtrees, $\text{cost}^*(c_i, c'_j) = (|T[c_i]| - |T[c'_j]|) \leq \text{cost}(c_i, c'_j)$. A minimal matching $\text{BPM}^*(v, w)$ that uses $\text{cost}^*(c_i, c'_j)$ cannot be more expensive than the original matching, $\text{BPM}^*(v, w) \leq \text{BPM}(v, w)$. We leverage this fact to derive a novel lower bound based on subtree sizes. We define the *sorted aggregate size* between start s and end e in a subforest $F[v]$ as

$$\text{SAS}(v, s, e) = \sum_{i=s}^e |T[c_i]|, \quad c_i \in \text{chd}(v), \quad (6)$$

where c_i is the i -th smallest subtree in $F[v]$ (ties broken arbitrarily).

The intuition of our bound is as follows: There exists a matching with cost $\text{BPM}(v, w)$, $\text{deg}(v) < \text{deg}(w)$, that matches the $k = \text{deg}(w) - \text{deg}(v)$ smallest subtrees to the empty tree, inducing cost $\text{SAS}(w, 1, k)$. The matching cost between the remaining subtrees is no larger than the difference of their aggregate subtree sizes.

THEOREM 2 (AGGREGATE SIZE BOUND). *Given two JSON tree nodes $v \in T_1, w \in T_2$. Let $d_v = \text{deg}(v)$, $d_w = \text{deg}(w)$, $k = d_w - d_v$, and $d_v \leq d_w$, then:*

$$\text{BPM}(v, w) \geq |\text{SAS}(v, 1, d_v) - \text{SAS}(w, k+1, d_w)| + \text{SAS}(w, 1, k).$$

EXAMPLE 5. *For the root nodes of the JSON trees in Figure 2, $\text{BPM}(v_{11}, w_9) = 5$ and the aggregate size bound is 2 ($\text{SAS}(w_9, 1, k) = 0$ since both nodes have the same degree, i.e., $k = 0$). In Figure 6,*

$k = 1$ and the aggregate subtree bound is 9: $\text{SAS}(w, 1, k) = 5$ and $|\text{SAS}(v, 1, d_v) - \text{SAS}(w, k+1, d_w)| = 4$. Note that our aggregate size bound performs much better than a simple subtree size difference bound, which is $|\text{SAS}(v, 1, d_v) - \text{SAS}(w, 1, d_w)| = 1$ in this example.

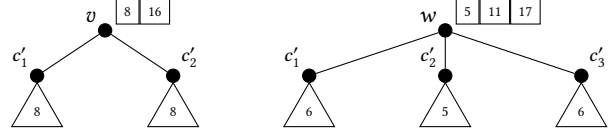


Figure 6: SAS arrays for the aggregate size bound.

Efficient Computation of Aggregate Size Bound. The aggregate size bound requires us to compute sums of subtree sizes. Since the bound is computed $O(|T_1||T_2|)$ times (for all pairs of parent nodes), computing these sums is too expensive. We precompute an array SAS_v of size $\text{deg}(v)$ for each node $v \in T_1$ with $\text{SAS}_v[i] = \text{SAS}(v, 1, i)$ (cf. Eq. (6)); analogously SAS_w for all $w \in T_2$ is computed. Thanks to the SAS arrays we can compute the bound in constant time:

$$|\text{SAS}(v, 1, d_v) - \text{SAS}(w, k+1, d_w)| + \text{SAS}(w, 1, k) = |\text{SAS}_v[d_v] - \text{SAS}_w[d_w] + \text{SAS}_w[k]| + \text{SAS}_w[k] \quad (7)$$

EXAMPLE 6. $\text{SAS}_{w_9} = [2, 4, 8]$ for root node w_9 in Figure 2. Figure 6 shows the SAS arrays for the root nodes v and w of the example trees.

Local Greedy Lower Bound. The local greedy lower bound on $\text{BPM}(v, w)$ matches each node by following the lowest cost edge. The result may violate the one-to-one requirement and therefore may not be a valid matching. Similar bounds have been used before (e.g., [45]). Since this bound is as expensive as the sequence edit distance (quadratic in the node degrees as all edge costs must be checked), it is only useful for the bipartite graph matching.

LEMMA 2 (LOCAL GREEDY LOWER BOUND). *Let T_1, T_2 be JSON trees, $v \in T_1, w \in T_2$. Let $GM_v \subseteq \text{chd}(v) \times \text{chd}(w)$ map $c_i \in \text{chd}(v)$ to some $c_j \in \text{chd}(w)$ such that $\text{dt}(c_i, c_j)$ is minimal; $GM_w \subseteq \text{chd}(w) \times \text{chd}(v)$ is defined analogously:*

$$\text{BPM}(v, w) \geq \max\{\gamma(GM_v), \gamma(GM_w)\}$$

We show how to compute GM_v and GM_w with low overhead: While we build the bipartite graph and retrieve all edge costs between the children of two nodes v, w , we maintain the minimum cost edge for each node $c_i \in \text{chd}(v)$ and $c'_j \in \text{chd}(w)$. In a single pass over the nodes, we get GM_v and GM_w with linear overhead.

An interesting opportunity arises when GM_v or GM_w is one-to-one: In this case, we can skip the bipartite graph matching since $\text{BPM}(v, w) = \max\{\gamma(GM_v), \gamma(GM_w)\}$ and we know the exact costs.

3.3 The QuickJEDI Algorithm

We present QuickJEDI, our efficient algorithm for computing the JSON edit distance. QuickJEDI extends JEDI-baseline (Algorithm 1) with the results in Section 3.2. While the baseline must compute the expensive min-cost matching between the children of each node pair (v, w) , QuickJEDI checks the aggregate size bound (cf. Th. 2) to assess whether the matching is required. The aggregate size bound

is a lower bound for both types of min-cost matchings: the sequence edit distance, $SED(v, w)$, for pairs of array nodes, and the bipartite graph matching, $BPM(v, w)$, which is applied otherwise. Only if the lower bound is smaller than both $insF$ and $delF$ (line 2), the min-cost matching must be computed. Before computing $BPM(v, w)$, we also check the local greedy lower bound (cf. Lemma 2).

We further avoid the min-cost matching for two special cases (omitted in Algorithm 2 for brevity): if both v and w are key nodes, they have only one child each (c_v resp. c_w), and $renF = dt(c_v, c_w)$. If both v and w are literal values, they are leaves, and $renF = 0$.

Algorithm 2: QuickJEDI(T_1, T_2)

Input: JSON trees T_1 and T_2 .

Result: JSON Edit Distance: JEDI(T_1, T_2).

```

/* Lines 1-14 from Algorithm 1 */
1 AggSizeBd = |SASv[dv] - SASw[dw] + SASw[k]| + SASw[k]
2 if AggSizeBd < min{insF, delF} then
3   if type(v) == type(w) == array then
4     renF = SED(v, w)
5   else
6     LocalGreedyBd = max{γ(GMv), γ(GMw)}
7     if LocalGreedyBd < min{insF, delF} then
8       renF = BPM(v, w)
/* Lines 19-21 from Algorithm 1 */
9 return dt(root(T1), root(T2))

```

4 THE JEDIORDER FILTER

In this section, we propose *JediOrder*, a highly effective upper bound filter on the JSON edit distance. In a JSON similarity query, the upper bound is evaluated before JEDI: if the upper bound is within the similarity threshold τ , the expensive JEDI needs not be computed.

We discuss Wang's algorithm [55], the fastest known algorithm that (with some adaptations to JSON trees) computes *JediOrder*. Wang's algorithm is faster than JEDI (quadratic vs. cubic) and requires less space. It turns out, however, that Wang's algorithm is still too slow to be used as an upper bound filter. The upper bound is computed for all tree pairs, but can only avoid the JEDI computation when the upper bound is within the threshold τ . Whenever the upper bound is larger than τ (including the cases when the true distance is larger), JEDI must be computed *in addition* to *JediOrder*.

To pay off, the upper bound filter must incur very low cost compared to the computation of the exact distance. To this end, we develop a new algorithm, called *JOFilter*, that takes the similarity threshold τ into account. *JOFilter* only assesses whether *JediOrder* is within threshold τ (which is enough for the filter purpose) and avoids computing the exact *JediOrder* value otherwise. With a clever tree traversal that considers only relevant node pairs, we achieve linear runtime (vs. quadratic runtime of Wang's algorithm).

4.1 Tree Sorting and Upper Bound Guarantee

JediOrder sorts the children of object nodes in a JSON document lexicographically by their keys; recall that the keys are string literals that are unique within an object. The result is an *ordered* JSON tree in which all sibling collections are totally ordered (cf. Figure 7).

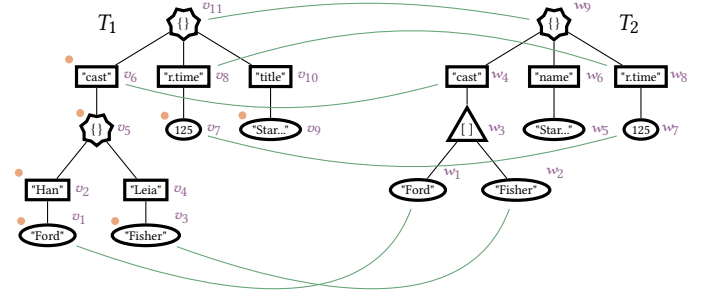


Figure 7: Sorted JSON trees from Figure 2 including the ordered JSON edit mapping \rightarrow , postorder numbers v_i and w_j , and favorable children \bullet .

JediOrder computes the minimal, edit-based distance between sorted JSON trees. Thanks to the order, *JediOrder* does not need to compute a bipartite graph matching, $BPM(v, w)$, between the children of two nodes v and w ; instead, the cheaper sequence edit distance, $SED(v, w)$, is evaluated (cf. Section 3.1). Formally, *JediOrder* is defined as the cost of the min-cost mapping that satisfies Definition 2.

DEFINITION 2 (ORDERED JSON EDIT MAPPING). A JSON edit mapping M is ordered iff for any node pairs $(v, w), (v', w') \in M$:

- v is to the left¹ of v' iff w is to the left of w' [order].

EXAMPLE 7. Considering the (ordered) JSON edit mappings in Figures 2 and 7, $JEDI(T_1, T_2) = 5$ vs. $JediOrder(T_1, T_2) = 8$. Due to the lexicographical order of the key nodes in Figure 7, the node pairs (v_9, w_5) and (v_{10}, w_6) violate the order constraint and are not in the minimum-cost ordered JSON edit mapping.

The order constraint in Definition 2 subsumes the array-order in Definition 1, thus *JediOrder* provides an upper bound for JEDI.

THEOREM 3 (JEDIORDER UPPER BOUND). Given JSON trees T_1, T_2 , then $JediOrder(T_1, T_2) \geq JEDI(T_1, T_2)$.

4.2 JediOrder Baseline: Wang's Algorithm

JediOrder is based on sorted, hence, ordered trees. As a baseline algorithm for *JediOrder*, we adapt the state-of-the-art constraint tree edit distance algorithm by Wang and Zhang [55], which runs in $O(|T_1||T_2|)$ time and $O(|T_2| \log |T_1|)$ space, to JSON trees.

Recursive Solution: The recursive solution discussed in Section 3.1 (cf. Eq. 1-3 and Lemma 1) also holds for *JediOrder*. Due to the total order among siblings, the minimum-cost matching in Eq. 2c is always computed by the sequence edit distance (rather than the more expensive bipartite graph matching). Zhang [59] shows the correctness of the recursion.

Memory Efficient Implementation: Similar to Algorithm 1, Wang's algorithm uses dynamic programming and a nested loop over all node pairs of the input trees T_1 and T_2 . To reduce the memory complexity, Wang implements two key ideas: (1) The deletion and rename costs of a node $v \in T_1$ ($delF/delT$ and $renF/renT$ in Algorithm 1) w.r.t. all nodes $w \in T_2$ (inner loop) are computed *incrementally* while the children of v are processed (in the outer loop).

¹ v is to the left of v' if v is not a descendant of v' and precedes v' in postorder.

The required cost arrays of size $|T_2|$ are maintained with each node v ; they are allocated when the first child of v is processed and are released after processing v . (2) The nodes of T_1 (outer loop) are processed in *favorable child order*, a postorder traversal that visits the so-called favorable child (defined as the child with the largest subtree) first and all other children in the usual left-to-right order. This traversal guarantees that only $\log |T_1|$ nodes $v \in T_1$ maintain their cost arrays concurrently, thus reducing the memory complexity from quadratic to $O(|T_2| \log |T_1|)$. In Figure 7, the favorable children of T_1 are marked with an orange bullet \bullet .

We will reuse these concepts and in addition leverage the similarity threshold to evaluate the JediOrder filter in linear time.

4.3 Leveraging the Distance Threshold

In the similarity lookup scenario, we are only interested in assessing whether JediOrder is within the similarity threshold τ . Hence, we do not need to consider mappings M_{JO} with a cost larger than τ .

On top of the two optimizations of Wang's algorithm (cf. Section 4.2), we add a third key idea: (3) leverage the user-defined similarity threshold τ in combination with the postorder lower bound (cf. Lemma 3) to reduce the number of *relevant node pairs*.

LEMMA 3 (POSTORDER LOWER BOUND [31]). *Given an ordered JSON edit mapping M_{JO} with cost $\gamma(M_{JO})$, for every node pair $(v, w) \in M_{JO}$ the following holds: $|\text{post}(v) - \text{post}(w)| \leq \gamma(M_{JO})$.*

In similarity queries, the distance is bounded by the threshold τ . Therefore, Lemma 3 implies that there are only $2\tau + 1$ eligible mapping partners $w \in T_2$ for a given node $v \in T_1$ such that the cost of the overall ordered JSON edit mapping is within τ . We refer to the eligible nodes $w \in T_2$ as the τ -range of a node $v \in T_1$.

EXAMPLE 8. *Consider the JSON trees in Figure 7 and a threshold $\tau = 2$. Any ordered JSON edit mapping that maps v_6 to a node in T_2 and has a cost of at most τ must map node v_6 to a node in its τ -range, i.e., w_4, w_5, w_6, w_7 , or w_8 .*

Our goal is to apply the τ -range in Wang's algorithm to avoid the nested loop over all node pairs. In particular, we strive to replace the inner loop over all nodes of T_2 by a constant τ -range of $2\tau + 1$ nodes. This has an impact on the computation of the tree, the forest, and the sequence edit distance (SED) matrices.

In the tree and forest distance matrix, at most $2\tau + 1$ cells are filled per row. The other cells are guaranteed to exceed the threshold due to the τ -range and do not need to be computed. Whenever these cells appear in a minimum computation, their value is considered to be infinite. If the overall mapping cost is within the threshold, the matrices store the correct JediOrder values. The correctness proof for the tree and the forest distance matrix is similar to the proof for the SED matrix, which we discuss in detail below.

We leverage the τ -range also for SED, which is used to compute the minimum-cost matching between the ordered children of two nodes. A sequence edit matching must satisfy Definition 3.

DEFINITION 3 (SEQUENCE EDIT MATCHING). *Matching $M_{SED(m,n)} \subseteq \text{chd}(m) \times \text{chd}(n)$, $m \in T_1$ and $n \in T_2$, is a sequence edit matching iff for any pairs $(v, w), (v', w') \in M_{SED(m,n)}$ the following holds:*

- $v = v'$ iff $w = w'$ [one-to-one],
- v is to the left of v' iff w is to the left of w' [order].

Restricting SED to the τ -range results in τ -restricted SED matchings and the corresponding τ -sequence edit distance (τ SED).

DEFINITION 4 (τ -RESTRICTED). *Let $M_{\tau SED(m,n)}$, $m \in T_1$ and $n \in T_2$, be a sequence edit matching. $M_{\tau SED(m,n)}$ is τ -restricted iff for any pair $(v, w) \in M_{\tau SED(m,n)}$ the following holds:*

- $|\text{post}(v) - \text{post}(w)| \leq \tau$ [τ -range].

The cost of a minimal SED matching $\gamma(M_{SED(m,n)})$ is identical to the cost of a minimal τ -restricted SED matching $\gamma(M_{\tau SED(m,n)})$ whenever the overall JediOrder value is within the threshold τ (cf. Theorem 4). Otherwise, $\gamma(M_{\tau SED(m,n)})$ provides an upper bound on $\gamma(M_{SED(m,n)})$ and hence an upper bound on $\gamma(M_{JO})$ is computed. However, only tree pairs with $\gamma(M_{JO}) \leq \tau$ have to be considered in a similarity lookup.

THEOREM 4 (EXACT τ SED). *If the minimal ordered JSON edit mapping M_{JO} between T_1 and T_2 has a cost of $\gamma(M_{JO}) \leq \tau$, then $\gamma(M_{\tau SED(m,n)}) = \gamma(M_{SED(m,n)})$ for any node pair $(m, n) \in M_{JO}$.*

Note that τ SED is superior to a simple approach that uses a threshold on the string edit distance [44]. While τ SED prunes based on the postorder positions in the tree, the latter approach prunes based on the position in the string/sequence. Hence, for subtrees of size larger than one, τ SED provides better pruning power than the simple approach, and the same pruning power otherwise.

EXAMPLE 9. *Table 2 shows the SED matrix for the root nodes v_{11} and w_9 of the trees in Figure 7. Consider node v_8 (at sequence position 2 and postorder 8) and a threshold $\tau = 2$. The unrestricted SED must compute all cells of the matrix. The simple threshold-based approach for the string edit distance must compute all cells for nodes with sequence positions 2 ± 2 , i.e., all nodes $w_c \in \text{chd}(w_9)$ must be considered. τ SED, however, only computes the cells in the τ -range of the postorder positions (highlighted in green), e.g., for node v_8 only nodes with postorder positions 8 ± 2 (w_6 and w_8) need to be considered.*

| | | chd(w_9) | | | |
|-----------------|------------|--------------|------------|-------|-------|
| | | SED | ϵ | w_4 | w_6 |
| chd(v_{11}) | ϵ | 0 | 4 | 6 | 8 |
| | v_6 | 6 | 4 | 6 | 8 |
| | v_8 | 8 | 6 | 6 | 6 |
| | v_{10} | 10 | 8 | 7 | 8 |

Table 2: SED(v_{11}, w_9) matrix of the root nodes in Figure 7. For threshold $\tau = 2$, τ SED only computes the cells highlighted in green.

4.4 Challenges of Applying the τ -Range

For the loop variables $v \in T_1$ and $w \in T_2$, Wang computes row v of the SED($p(v), w$) matrix (cf. Algorithm 3). This matrix has a row for each child of $p(v)$ and a column for each child of w .

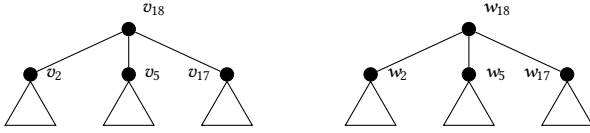
To apply the τ -range in Wang's algorithm, (1) the inner loop over all node pairs must be restricted to the nodes in the τ -range and (2) the SED must be τ -restricted. Unfortunately, extending Wang's algorithm with the τ -range (highlighted in line 2, Algorithm 3) will lead to incorrect results. Consider the matrix of the SED(v_{18}, w_{18}) computation between the two identical JSON trees in Figure 8 with

Algorithm 3: Wang(T_1, T_2, τ)

```

Input: JSON trees  $T_1$  and  $T_2$ , and threshold  $\tau$ .
/* Outline of SED computation in Wang's algorithm. */
1 for  $v$  in  $T_1$  do
2   for  $w$  in  $T_2$  with  $|post(v) - post(w)| \leq \tau$  do
3     for  $c$  in  $chd(w)$  do
4       Compute cell  $(v, c)$  of the SED( $p(v), w$ ) matrix.

```

**Figure 8:** Two identical JSON trees T_1 and T_2 .

$\tau = 2$. Wang's algorithm computes row v_2 while processing v_2 in the outer loop and w_{18} in the inner loop. However, w_{18} is not in the τ -range of v_2 ; hence the node pair (v_2, w_{18}) is not considered in the nested loop, and row v_2 in the SED matrix is not filled.

4.5 The JOFilter Algorithm

We now present a novel algorithm, called *JOFilter*, that assesses whether JediOrder is within a given threshold τ . Our solution is able to leverage all key ideas of the space-efficient algorithm by Wang (incremental cost computation and favorable child order, cf. Section 4.2) and the τ -range introduced in Section 4.3. In the following, we discuss the key challenges that must be addressed and show that JOFilter runs in $O(n\tau)$ time and $O(n + \tau \log n)$ space.

Cost arrays of size τ . Similar to Wang's algorithm, we split the auxiliary matrices into rows and store each row with the relevant nodes $v \in T_1$. A node v maintains the following data: row v of (1) the tree and (2) the forest distance matrix, denoted $v.dt$ and $v.df$, respectively; (3) the tree distance matrix row of v 's favorable child, $v.dt_{fc}$; finally, (4) two rows of the SED(v, w) matrices for all $w \in T_2$, denoted $v.sed_{L_0}$, and $v.sed_{L_1}$, which are sufficient to compute SED [27]. Due to the τ -range, the size of these cost arrays (i.e., matrix rows) can be reduced from $O(|T_2|)$ in Wang's algorithm to $O(\tau)$ in JOFilter. Summarizing, a node $v \in T_1$ stores auxiliary data of size $O(\tau)$. Moreover, the insertion (resp. deletion) costs of node v in the forest, tree, and SED matrices, denoted $v.df_e$, $v.dte$, and $v.sed_e$, are stored in global arrays of size $|T_2|$.

Logarithmic number of active nodes. A node is called *active* while the node and its auxiliary data are held in main memory. A node v becomes active when its favorable child is processed and inactive after v itself was processed. The favorable child order guarantees that at most $O(\log |T_1|)$ nodes are active at any time [55].

Applying the τ -range. We apply the τ -range by replacing the inner loop over all nodes $w \in T_2$ by a constant range of $2\tau + 1$ nodes. As shown in Section 4.4, applying the τ -range in Wang's algorithm leads to incorrect results. We therefore adapt the computation order of the values in the SED computation as shown in Algorithm 4: only a single cell (v, w) of the SED($p(v), p(w)$) matrix is filled in the inner loop rather than an entire matrix row. Since v and w are

Algorithm 4: JOFilter(T_1, T_2, τ)

```

Input: JSON trees  $T_1$  and  $T_2$ , and threshold  $\tau$ .
/* Outline of SED computation in the JOFilter. */
1 for  $v$  in  $T_1$  do
2   for  $w$  in  $T_2$  with  $|post(v) - post(w)| \leq \tau$  do
3     Compute cell  $(v, w)$  of the SED( $p(v), p(w)$ ) matrix.

```

the loop variables, we guarantee that all node pairs in the τ -range are considered in the SED computation.

Algorithm. We present the pseudocode of our solution, JOFilter, in Algorithm 5. Note that $ls(v)$ denotes the left sibling of node v and a dot '.' accesses the data of a given node. The nodes $v \in T_1$ (outer loop) are traversed in favorable child order, while the nodes $w \in T_2$ (inner loop) are traversed in postorder. To avoid the computation between all node pairs, we apply the τ -range (cf. Lemma 3) in the inner loop. Assuming that the rename and deletion costs are given, we first compute the tree and forest distance between nodes v and w (cf. lines 4-9). In the remainder of the algorithm (cf. lines 10-28), the deletion and rename costs for the parent of node v are computed incrementally. After processing all node pairs, the overall distance is stored in the tree distance matrix line of the root node of T_1 , $root(T_1).dt(root(T_2))$. The filter only accepts a tree pair (T_1, T_2) iff $JediOrder(T_1, T_2) \leq \tau$ (cf. line 29).

Complexity. For each node $v \in T_1$ only $2\tau + 1$ nodes $w \in T_2$ are considered (cf. Lemma 3). Therefore, the overall *time* complexity is $O(|T_1|\tau)$. The space complexity is dominated by the global arrays of size $O(|T_2|)$ that store the insertion (resp. deletion) costs of node v in the forest, tree, and SED matrices. Each active node fits in $O(\tau)$ space and there are at most $O(\log |T_1|)$ active nodes at any point in time, leading to an overall space complexity of $O(|T_2| + \tau \log |T_1|)$.

5 JSIM: JSON SIMILARITY INDEX

We now present the *JSIM* index for JSON similarity queries and discuss the use of index and filters in the similarity query context.

The input to the JSIM index over a tree database \mathcal{T} is a query tree T_q and a threshold τ , the output is a *candidate set* $C \subseteq \mathcal{T}$ that is a superset of the query result, $R = \{T_i \in \mathcal{T} \mid JEDI(T_q, T_i) \leq \tau\} \subseteq C$.

Existing indexing techniques for tree similarity queries [31, 49] require ordered trees. They leverage concepts that (due to the missing order of object nodes) are not applicable to JSON, e.g., the postorder position of nodes in the tree [31] or an order-based partitioning of trees into subgraphs [49]. Sorting JSON trees does not solve the problem: The distance between sorted trees may increase w.r.t. JEDI such that the index fails to retrieve relevant trees.

Our JSIM index leverages a novel lower bound for JSON trees, called *JJSON region bound*, that is based on the position of a node in the tree. Based on this lower bound and a node label filter, we build an effective multi-level index that only returns trees $T_i \in \mathcal{T}$ that pass all filters. Moreover, we introduce a technique that decreases the search threshold level by level during the index lookup. This allows us to aggressively prune index branches at deeper index levels.

Algorithm 5: JOFilter(T_1, T_2, τ)

Input: JSON trees T_1 and T_2 , and threshold τ .
Result: *True* if JediOrder(T_1, T_2) $\leq \tau$, *False* otherwise.

```

1 for  $v$  in  $T_1$  do                               /* Favorable child order */
2    $p = p(v)$ 
3   for  $w$  with  $|post(v) - post(w)| \leq \tau$  do /* Postorder */
4     /* Cost for inserting node  $w$ . */
5      $insF = w.df_\epsilon + \min_{c \in chd(w)} \{v.df(c) - c.df_\epsilon\}$ 
6      $insT = w.dt_\epsilon + \min_{c \in chd(w)} \{v.dt(c) - c.dt_\epsilon\}$ 
7     /* Costs for deleting and renaming already computed. */
8      $renF = v.sed_{L_0}(w_t)$  /*  $w$ 's rightmost child  $w_t$ . */
9      $v.df(w) = \min\{insF, v.delF(w), renF\}$ 
10     $renT = v.df(w) + \min\{\gamma(v, w), \gamma(v, \lambda) + \gamma(\lambda, w)\}$ 
11     $v.dt(w) = \min\{insT, v.delT(w), renT\}$ 
12    /* Compute deletion and rename costs for parent. */
13    if  $v$  is favorable child then
14       $p.dt_{fc}(w) = v.dt(w)$ 
15       $p.delF(w) = v.df_\epsilon + v.df(w) - v.df_\epsilon$ 
16       $p.delT(w) = v.dt_\epsilon + v.dt(w) - v.dt_\epsilon$ 
17    else
18       $p.delF(w) = \min\{p.delF(w), p.df(0) + v.df(w) - v.df(0)\}$ 
19       $p.delT(w) = \min\{p.delT(w), p.dt(0) + v.dt(w) - v.dt(0)\}$ 
20    if  $v$  is left-most child then
21       $p.sed_{L_1}(0) = p.sed_{L_0}(0) + v.dt_\epsilon$ 
22       $p.sed_{L_1}(w) = \min\{p.sed_{L_1}(ls(w)) + w.dt_\epsilon, w.sed_\epsilon + v.dt_\epsilon, ls(w).sed_\epsilon + v.dt(w)\}$ 
23    else if  $v$  is not favorable child then
24       $p.sed_{L_1}(0) = p.sed_{L_0}(0) + v.dt_\epsilon$ 
25       $p.sed_{L_1}(w) = \min\{p.sed_{L_1}(ls(w)) + w.dt_\epsilon, p.sed_{L_0}(w) + v.dt_\epsilon, p.sed_{L_0}(ls(w)) + v.dt(w)\}$ 
26    if  $v$  is left sibling of favorable child  $c_f$  then
27       $p.sed_{L_0}(0) = p.sed_{L_1}(0) + p.dt_{fc}(0)$ 
28      for  $w$  with  $|post(v) - post(w)| \leq \tau$  do
29         $p.sed_{L_0}(w) = \min\{p.sed_{L_0}(ls(w)) + w.dt_\epsilon, p.sed_{L_0}(w) + p.dt_{fc}(0), p.sed_{L_0}(ls(w)) + p.dt_{fc}(w)\}$ 
30    else
31       $p.sed_{L_0} = p.sed_{L_1}$ 
32  return  $root(T_1).dt(root(T_2)) \leq \tau$ 

```

5.1 Leveraging Node Position and Labels

We now present the JSON region bound that is based on the ancestor constraint of the JSON edit mapping in Definition 1. Assume that the node pair (v, w) in Figure 9 is mapped; then, $anc(v)$ must be mapped to $anc(w)$ (red), $desc(v)$ to $desc(w)$ (green), and $lr(v)$ to $lr(w)$ (blue). The left-right nodes $lr(v)$ of node v are all nodes in T_q different from v , $desc(v)$, and $anc(v)$. Intuitively, the size difference of the individual regions imposes a lower bound on the respective mapping cost. For example, the cost of mapping the ancestors in Figure 9 is at least one.

LEMMA 4 (JSON REGION BOUND). *Let T_1, T_2 be JSON trees, M a JSON edit mapping from T_1 to T_2 . For a given similarity threshold τ , if the cost of the mapping is $\gamma(M) \leq \tau$, then for each $(v, w) \in M$:*

$$||desc(v) - desc(w)|| + ||anc(v) - anc(w)|| + ||lr(v) - lr(w)|| \leq \tau.$$

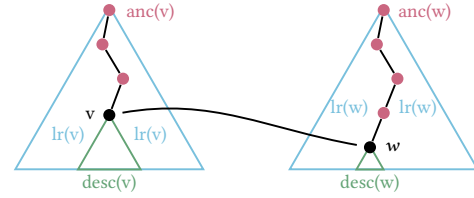


Figure 9: Due to the ancestor constraint, mapping node v to w splits the JSON tree into three regions.

Tightening the Bound. An interesting observation is that when we know one of the size differences in Lemma 4, e.g., $\Delta = ||desc(v) - desc(w)||$, we can tighten the bound for the remaining, unknown differences: $||anc(v) - anc(w)|| + ||lr(v) - lr(w)|| \leq \tau - \Delta$. We leverage this effect to prune branches in our index traversal.

Label Intersection. A well known lower bound is based on the bag intersection of node labels [3]. For JSON trees, we need to replace node labels by *(label, type)* pairs. Then, the following holds:

$$JEDI(T_1, T_2) \geq \max(|N(T_1)|, |N(T_2)|) - |N(T_1) \cap N(T_2)|. \quad (8)$$

5.2 Index Structure and Lookup

We discuss the structure of the JSIM index and our lookup technique that leverages the filters discussed in Section 5.1.

Building the Index. JSIM is a tree with four levels that store (1) node labels, (2) descendant counts, (3) ancestor counts, and (4) left-right node counts, respectively. Each index node is a sorted list of entries that either points to a child node (non-leaf entry) or to a list of indexed trees (leaf entries).

A new tree T_i is inserted $|T_i|$ times into the index, once for each node. Each node adds a constant number of (at most 5) index entries. Therefore, the overall index size is proportional to the aggregated number of nodes of the indexed JSON trees. The insert path for a node $v \in T_i$ is determined by its label, its number of descendants, ancestors, and left-right nodes. New values are inserted into the respective index node, for existing values the child pointer is followed. The process of inserting node $v_8 \in T_1$ from Figure 2 into the index is highlighted in Figure 10a (green). Tree T_1 is inserted with label = "r.time", $|desc(v_8)| = 1$, $|anc(v_8)| = 1$, and $|lr(v_8)| = 8$.

Index Lookup. The lookup for query tree T_q processes $\tau + 1$ nodes $v \in T_q$, and for each node proceeds in two steps: (1) *Label lookup:* Follow the branch for the label of v in the index root node. The index lookup is limited to only $\tau + 1$ nodes since any tree T_i that has more than $\tau + 1$ mismatching labels with T_q cannot be within edit distance τ [31, 38]. (2) *Region traversal:* We leverage Lemma 4 to traverse the remaining levels. At each node, we follow all keys k (i.e., region counts) that fall into the range given by Lemma 4, e.g., $d = ||desc(v) - k|| \leq \tau$ at the descendant count level. Note that each of the three size differences (which are all positive) must be within the threshold τ . At the lower index levels, we leverage the size difference that we know from previous levels, e.g., the threshold for the ancestor level can be decreased to $\tau_a = \tau - d$ and the index verifies all keys k_a with $a = ||anc(v) - k_a|| \leq \tau_a$. The process for the fourth level is similar, we verify all keys k_{lr} with $||lr(v) - k_{lr}|| \leq \tau_{lr}$ against an even further reduced threshold $\tau_{lr} = \tau_a - a$. All trees in

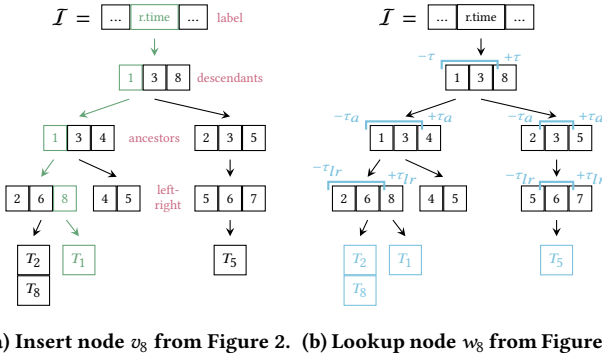


Figure 10: JSIM index: four-level inverted list.

the lists that we reach are candidates and are returned by the index. For example, the lookup of node $w_8 \in T_2$ (Figure 2) is illustrated in Figure 10b (blue) and returns T_2, T_8, T_1, T_5 .

Note that a search may end before reaching a leaf node when no trees in the τ -range are found. This desirable effect is boosted by reducing the τ -range at each level.

5.3 JSON Similarity Lookups

We leverage our techniques (i.e., JSIM, JOFilter, and QuickJEDI) to answer JSON similarity lookup queries as follows: (1) Lookup query tree T_q with threshold τ in the JSIM index to retrieve candidate set C . (2) For each tree $T_i \in C$ check the label intersection lower bound in Eq. (8). (3) For the remaining candidates $T_i \in C'$, if $JediOrder(T_q, T_i) \leq \tau$, then T_i is a result pair. (4) Verify the remaining candidates $T_i \in C''$ by computing $QuickJEDI(T_q, T_i)$.

6 EXPERIMENTS

We experimentally evaluate our solution for JSON similarity lookups on 22 real-world datasets in a unified C++ framework. The source code [29] and the experimental data [28] are publicly available. The experiments are executed single-threaded on an Intel Xeon E5-2630 v3 2.40GHz server with 16 cores and 96GB of RAM (Debian 10).

6.1 Setup

Algorithms: We evaluate various algorithmic combinations. *Scan* denotes a linear scan, *JSIM* denotes our index (cf. Section 5), *Wang* is the state-of-the-art JediOrder algorithm, *JOFilter* is our JediOrder filter (Algorithm 5), *Baseline* refers to the JEDI-baseline (Algorithm 1) and *QuickJEDI* to our optimized version (Algorithm 2).

Datasets: The evaluation is performed on a collection of 22 real-world JSON datasets. We summarize their most important characteristics: *Collection sizes* of up to 8.76 million JSON trees; *JSON tree sizes* of up to 48k nodes; a *type distribution* within a JSON tree of up to 20% objects, 10% arrays, 49% keys, and 49% literals; the *degree of object nodes* is typically less than 20 with the exception of one dataset (104); the *degree of array nodes* is up to 1603 values; one dataset provides a *depth* of 50 (less than 14 for all other datasets).

We briefly describe the datasets used for the experiments in Figures 11 and 12. (1) FENF [22]: FDA enforcement actions, ~14k documents with an average of 49 nodes per document and a depth of 3. (2) Reddit [43]: 25 Reddit articles with an average of 265 nodes

per document. This dataset provides the highest object degree of 104 children. (3) Cards [26]: ~20k Magic cards with an average number of 132 nodes per document. (4) StanDev [53]: question-answering dataset, 48 documents with up to ~18k nodes and an average of 5,379 nodes per document. (5) Movies[40]: TV and movie ratings, ~8.7 million documents with an average of 23 nodes per document. (6) NBA [14]: ~31k NBA games with an average of 977 nodes per document. (7) Device [22]: ~150k FDA enforcement actions with up to 3,264 nodes per document. (8) arXiv [52]: 1.8 million research publications with an average of 53 nodes per publication. (9) Twitter2 [51]: ~19k tweets with an average of 195 nodes per document. (10) DENF [22]: ~7k FDA enforcement actions with an average of 59 nodes per document. (11) Schema [5]: 81k JSON schemas with up to 48k nodes per schema document. (12) SMSen [13]: ~55k SMS messages with an average of 81 nodes per document.

Experimental Setup: For each dataset, we perform JSON similarity lookup queries for three different query trees and four different thresholds. Since the runtime of the distance algorithms depends on the tree sizes, we pick the query trees that are closest to the 25%, 50%, and 75% quantiles of the tree sizes for each dataset (denoted $T_{25\%}$, $T_{50\%}$, and $T_{75\%}$). The goal of similarity lookup queries is to return documents that are similar to the query document, hence useful thresholds depend on the size of the query tree. We experiment with thresholds that are 5%, 10%, 20%, and 30% of the respective query tree size. The timeout for computing the results for all thresholds for a given algorithm and dataset is 24 hours.

Evaluation: We analyze the overall runtime and the effectiveness of the introduced bounds. Each plot in Figure 11 and 12 shows the results of a single experiment, i.e., a given dataset and query tree for varying thresholds on the x-axis. For example, Figure 11a shows the results for dataset FENF and the 50% quantile query tree $T_{50\%}$.

Figure 11 shows the overall lookup runtimes in milliseconds for various algorithm combinations. Figure 12 evaluates the number of trees pruned by the individual filters as well as the number of required verifications. The total height of a bar is the number of documents (i.e., trees) in the dataset, the colors distinguish the tree pairs that are pruned by the JSIM index (orange), the label intersection (red), the upper bound (purple), and the number of verifications (blue). The runtime and effectiveness plots are aligned, e.g., Figures 11a and 12a result from the same experiment.

The overall experiment includes 66 dataset/query combinations. Due to space restrictions, we provide a representative selection that covers the most relevant phenomena (cf. Figures 11 and 12).

6.2 Results

JSIM Index vs. Dataset Scan. We measure the effectiveness of the index by the number of returned candidates (cf. Figure 12). Especially for small thresholds, the returned candidates are orders of magnitude smaller than the collection size (e.g., Figure 12h and 12e).

Due to the smaller number of candidates, the index outperforms the scan in each experiment, e.g., the index is up to five orders of magnitude faster in Figure 11j. For larger datasets (e.g., Figure 11e), the index is needed to answer the query within the timeout. In some scenarios, however, applying an index without further optimizations is not enough: The Reddit dataset used for the experiment

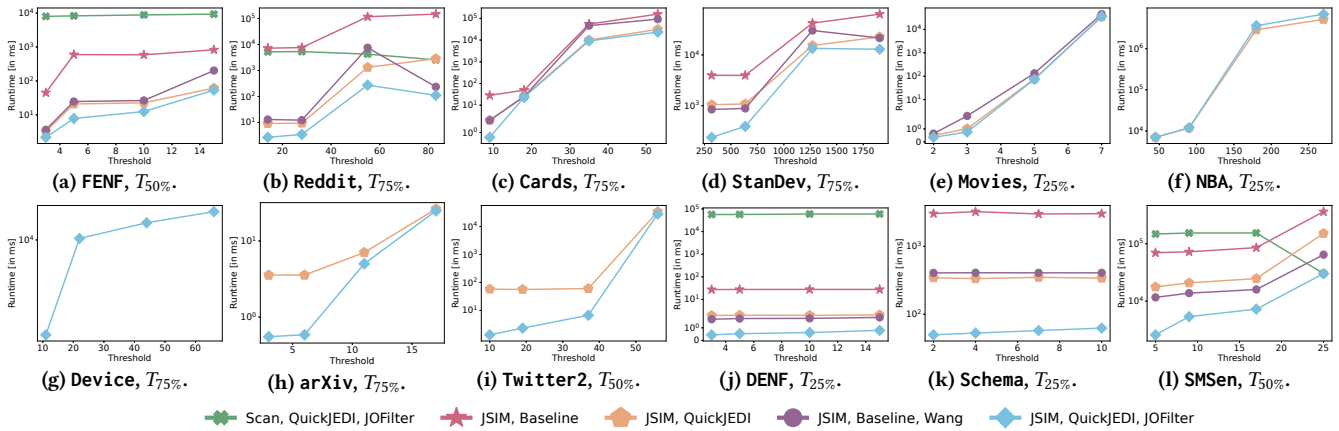


Figure 11: Overall runtime: JSON similarity lookup query.

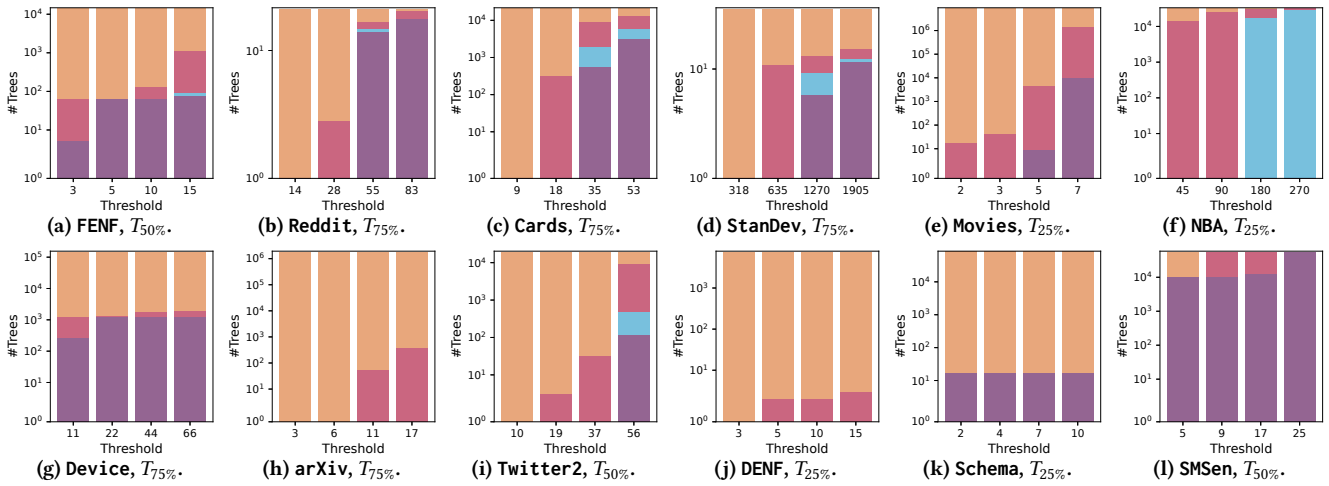


Figure 12: Filter effectiveness: pruned by the JSIM index, label intersection, upper bound, and number of verifications.

in Figure 11b only contains 25 documents; however, due to its object degree of 104, verifying even a single candidate significantly increases the runtime. As a result, scanning Reddit with our optimized algorithms (Scan, QuickJEDI, JOFilter) outperforms the index-based solution with baseline verification (JSIM, Baseline). In some cases, when the lookup result is empty, the query is answered only within the index, i.e., neither the upper bound nor the verification are computed (e.g., Figures 12h and 12j).

Wang vs. JOFilter. Next, we compare the state-of-the-art JediOrder algorithm (Wang) with our optimized algorithm (JOFilter). The experimental results show the behaviour expected based on the runtime complexities of the algorithms. The complexity of JOFilter depends on the threshold. Even for larger thresholds, JOFilter is superior to Wang due to the quadratic complexity of the latter. We compare the runtimes of Wang (purple) and JOFilter (blue) in Figure 11. In Figure 11a, no candidates must be verified except for threshold 15; hence the runtime improves from JOFilter alone. We observe the largest improvements of JOFilter in Figures 11k and 11l, where Wang is up to an order of magnitude slower.

In many scenarios (cf. Figures 12), the upper bound identifies most of the result set and only few trees must be verified (blue bar). However, the upper bound is applied to each candidate and introduces additional overhead which may increase the runtime in cases where the upper bound is not effective (cf. Figure 11f). These results show that an efficient verification algorithm is indispensable.

Baseline Verification vs. QuickJEDI. We also evaluated the effect of the optimized verification algorithm QuickJEDI over the baseline without applying the upper bound (red stars vs. orange pentagons in Figure 11). The complexities of both algorithms heavily depend on the degrees of the trees. QuickJEDI aims at skipping the expensive min-cost matching computation, which substantially reduces the runtime. Consider the measurements for threshold 55 in Figures 11b and 12b: even though only 16 trees have to be verified, the runtime difference between the baseline and QuickJEDI is almost two orders of magnitude. This results from the characteristics of the Reddit dataset, where some documents feature up to 104 unordered key-value pairs per object. Moreover, in 4 out of the 22 datasets the lookup terminated within the timeout only in configurations that include QuickJEDI (e.g., Figures 11f and 11i).

Summary. Overall, the best performance results are achieved by combining the JSIM index, JOFilter, and QuickJEDI. This configuration provides the lowest runtimes for 61 out of our total of 66 experiments and is the only one that is able to process all datasets (e.g., Figure 11g) within 24 hours. Only in cases where the upper bound is ineffective (cf. Figure 11f), QuickJEDI without JOFilter is slightly better. These results are robust even when the characteristics of the datasets vary, e.g., large documents (cf. Figure 11d) and large collections (cf. Figure 11e). In 37 experiments, the query is answered without applying a verification algorithm, i.e., the candidates returned by the index are equivalent to the result and are verified by the upper bound, highlighting the filter effectiveness.

7 RELATED WORK

JSON Tree Representations. There exist multiple tree representations of JSON documents. Bourhis et al. [7] represent keys and the array order as edges and values as leaf nodes; the approach by Shukla et al. [46] is similar, but keys and the array order are inner nodes instead of edges. Similar to our approach, Klettke et al. [34] introduce three different types of nodes (object, array, property) in addition to the label. Spoth et al. [47] use a tree containing atomic values at the leaves and complex values in the inner nodes. These representations either discard the object and the array information or encode the information in the edges of a tree; both choices are unsuitable for node edit operations. Tree representations of XML data (e.g., by Augsten et al. [2]) cannot be applied in the context of JSON since XML siblings are considered to be ordered.

JSON Similarity. To the best of our knowledge, there is only one scientific work on JSON diffs. Cao et al. [11] present an algorithm that computes a JSON patch based on the edit operations defined in RFC6902 [9]. In an experimental study, a comparison to four open source solutions was performed. However, the runtime and space complexity of the presented algorithm was not discussed. Further, the resulting patch is not minimal and therefore unsuitable for similarity queries. Yahia et al. [56] proposed a YAML-based language for describing change-detection strategies on JSON data.

Diff algorithms do exist for other hierarchical data formats. Chawathe et al. [12] present an algorithm that computes minimal diffs for \LaTeX and HTML documents. The following edit operations are considered: insert and delete leaf nodes, update the value of any node, and subtree moves. The XML diffs by Cobena et al. [16] consider insertions and deletions of subtrees, value updates of any node, and moves of a node or a part of a subtree. Both approaches operate on ordered trees and are therefore unsuitable for JSON.

JSON Schema. Most of the scientific work related to JSON deal with schema extraction. Schemas are used as dataset descriptions or to enable optimization techniques in database systems. Durner et al. [18] present a solution to extract multiple local schemas for a single dataset. The schemas are grouped based on the label sets of the keys in a document. Baazizi et al. [4] introduce a parametric and parallel schema inference algorithm. Klettke et al. [34] present a schema extraction algorithm to identify structural outliers based on structure identification graphs. While the goal of schema extraction is different from that of similarity queries, JEDI could be used to identify schemas for similar documents.

Tree Edit Distance. A well-known edit distance for hierarchical data is the tree edit distance (TED). The current best algorithm for ordered trees by Pawlik and Augsten [41] computes TED in cubic time using quadratic memory. Computing TED for unordered trees is NP-hard [61]. Further, TED was applied for different query types, e.g., similarity joins [31] and top-k similarity joins [36]. However, these techniques are not applicable for JSON since JSON trees consist of ordered as well as unordered children. In fact, we showed that a TED adaption for JSON results in an NP-hard problem.

Zhang introduced a constraint TED version which can be computed in time $O(n^2)$ for ordered [59] and $O(|T_1| \cdot |T_2| \cdot (deg(T_1) + deg(T_2)) \cdot \log_2(deg(T_1) + deg(T_2)))$ for unordered trees [60]. Similar to TED, both algorithms are designed for either ordered or unordered trees. We combined both approaches to construct the baseline JEDI algorithm. As shown in our experimental evaluation, we introduce heuristics that decrease the runtime of JEDI often by orders of magnitude. The ordered constraint TED algorithm by Wang et al. [55] using $O(n \log n)$ memory was used as a baseline algorithm for JediOrder. We introduced a novel JediOrder algorithm that improves the complexity to be linear in time and space.

Heuristics for the Unordered Tree Edit Distance. Due to the computational complexity of the unordered TED, a number of heuristics have been presented. Augsten et al. [2] introduced an approximation based on tree decomposition, called windowed pq-grams, that splits a tree into a set of smaller elements which are then compared to the decomposition of another tree. They experimentally showed that windowed pq-grams outperform other tree decomposition algorithms (binary branches [57], path shingles [10], and valid subtrees [24]). Rather than introducing approximations, we defined an exact and minimal JEDI distance.

8 CONCLUSION AND FUTURE WORK

In this paper, we addressed the problem of JSON similarity lookup queries: Given a query document T_q and a distance threshold τ , retrieve all documents from a JSON database \mathcal{T} that are within distance τ from the query. We proposed (a) a lossless tree representation for JSON, (b) JEDI, the first edit-based distance for JSON documents, (c) the efficient QuickJEDI algorithm for JEDI, (d) the JSIM index to efficiently retrieve candidate trees for JSON similarity queries, and (e) JediOrder, an effective upper bound on JEDI. In our experiments, we scaled JSON similarity lookup queries to databases with millions of documents and JSON trees with thousands of nodes.

In an ongoing effort, our solution is being integrated into Apache AsterixDB, an open-source big data management system that uses partitioned-parallel query processing and a JSON-like data format.

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REFERENCES

- [1] Sattam Alsubaiee, Yasser Altowim, Hotham Altwaijry, Alexander Behm, Vinayak Borkar, Yingyi Bu, Michael Carey, et al. 2014. AsterixDB: A Scalable, Open Source BDMS. *Proceedings of the VLDB Endowment* 7, 14, 1905–1916.
- [2] Nikolaus Augsten, Michael Böhlen, Curtis Dyreson, and Johann Gamper. 2012. Windowed pq-grams for approximate joins of data-centric XML. *The VLDB Journal* 21, 4 (2012), 463–488.
- [3] Nikolaus Augsten and Michael H Böhlen. 2013. *Similarity joins in relational database systems*. Vol. 5. Morgan & Claypool Publishers.
- [4] Mohamed-Amine Baazizi, Dario Colazzo, Giorgio Ghelli, and Carlo Sartiani. 2019. Parametric schema inference for massive JSON datasets. *The VLDB Journal* 28, 4 (2019), 497–521.
- [5] Mohamed Amine Baazizi, Dario Colazzo, Giorgio Ghelli, Carlo Sartiani, and Stefanie Scherzinger. 2021. A JSON Schema Corpus. <https://github.com/sdbuni-p/json-schema-corpus>.
- [6] Dipti Borkar, Ravi Mayuram, Gerald Sangudi, and Michael Carey. 2016. Have your data and query it too: From key-value caching to big data management. In *Proceedings of the 2016 International Conference on Management of Data*. ACM, 239–251.
- [7] Pierre Bourhis, Juan L Reutter, Fernando Suárez, and Domagoj Vrgoč. 2017. JSON: data model, query languages and schema specification. In *Proceedings of the 36th Symposium on Principles of Database Systems*. 123–135.
- [8] Tim Bray. 2017. *The JavaScript Object Notation (JSON) Data Interchange Format*. RFC 8259. RFC Editor. <https://www.rfc-editor.org/rfc/rfc8259.txt>
- [9] Paul C Bryan and Mark Nottingham. 2013. *JavaScript Object Notation (JSON) Patch*. RFC 6902. RFC Editor. <https://www.rfc-editor.org/rfc/rfc6902.txt>
- [10] David Buttler. 2004. A short survey of document structure similarity algorithms. *Proceedings of the International Conference on Internet Computing* 1, 3–9.
- [11] Hanyang Cao, Jean-Rémy Falleri, Xavier Blanc, and Li Zhang. 2016. JSON Patch for Turning a Pull REST API into a Push. In *International Conference on Service-Oriented Computing*. Springer, 435–449.
- [12] Sudarshan S Chawathe, Anand Rajaraman, Hector Garcia-Molina, and Jennifer Widom. 1996. Change detection in hierarchically structured information. In *Proceedings of the 1996 International Conference on Management of Data*. ACM, 493–504.
- [13] Tao Chen and Min-Yen Kan. 2013. Creating a live, public short message service corpus: the NUS SMS corpus. *Language Resources and Evaluation* 47, 2 (2013), 299–335.
- [14] Mohamed L. Chouder, Stefano Rizzi, and Rachid Chahal. 2017. JSON Datasets for Exploratory OLAP. <https://doi.org/10.17632/CT8F9SKV97.1>
- [15] Circlecell. 2022. JSON Compare. <https://jsoncompare.com/>. Accessed: 2022-01-12.
- [16] Gregory Cobena, Serge Abiteboul, and Amelie Marian. 2002. Detecting changes in XML documents. In *Proceedings of the 18th International Conference on Data Engineering*. IEEE, 41–52.
- [17] SQL Docs. 2021. Full Text Search. <https://docs.microsoft.com/en-us/sql/relational-databases/search/full-text-search?view=sql-server-ver15>. Accessed: 2022-01-12.
- [18] Dominik Durner, Viktor Leis, and Thomas Neumann. 2021. JSON Tiles: Fast Analytics on Semi-Structured Data. In *Proceedings of the 2021 International Conference on Management of Data*. ACM, 445–458.
- [19] Vincent Emeakaroha, Philip Healy, Kaniz Fatema, and John Morrison. 2013. Analysis of Data Interchange Formats for Interoperable and Efficient Data Communication in Clouds. In *IEEE/ACM 6th International Conference on Utility and Cloud Computing*. 393–398.
- [20] EU. 2021. EU Open Data Portal. <https://data.europa.eu>. Accessed: 2022-01-12.
- [21] Jan P Finis, Martin Raiber, Nikolaus Augsten, Robert Brunel, Alfons Kemper, and Franz Färber. 2013. Rws-diff: flexible and efficient change detection in hierarchical data. In *Proceedings of the 22nd ACM international conference on Information & Knowledge Management*. 339–348.
- [22] US Food and Drug Administration. 2017. FDA Enforcement Actions Dataset. <https://www.kaggle.com/fda/fda-enforcement-actions> Accessed: 2022-01-12.
- [23] Xinbo Gao, Bing Xiao, Dacheng Tao, and Xuelong Li. 2010. A survey of graph edit distance. *Pattern Analysis and Applications* 13 (2010), 113–129.
- [24] Minos Garofalakis and Amit Kumar. 2003. Correlating XML data streams using tree-edit distance embeddings. In *Proceedings of the 22nd Symposium on Principles of Database Systems*. 143–154.
- [25] Zack Grossbart. 2021. JSON Diff. <http://www.jsondiff.com>. Accessed: 2022-01-12.
- [26] Zachary Halpern. 2022. Magic Cards Dataset. <https://mtgjson.com/api/v5/AtomicCards.json>. Accessed: 2022-01-12.
- [27] Daniel S. Hirschberg. 1975. A linear space algorithm for computing maximal common subsequences. *Commun. ACM* 18, 6 (1975), 341–343.
- [28] Thomas Hütter. 2021. <https://github.com/DatabaseGroup/jedi-experiments>: SIGMOD 2022. <https://doi.org/10.5281/zenodo.5807299>
- [29] Thomas Hütter. 2022. <https://github.com/DatabaseGroup/jedi-experiments>: SIGMOD 2022. <https://doi.org/10.5281/zenodo.5881864>
- [30] Thomas Hütter, Nikolaus Augsten, Kirsch Christoph M, Carey Michael J, and Chen Li. 2022. JEDI: These aren't the JSON documents you're looking for... (Extended Version*). *arXiv preprint arXiv:2201.08099* (2022).
- [31] Thomas Hütter, Mateusz Pawlik, Robert Löschinger, and Nikolaus Augsten. 2019. Effective filters and linear time verification for tree similarity joins. In *Proceedings of the 35th International Conference on Data Engineering*. IEEE, 854–865.
- [32] Bumsuk Jang, SeongHun Park, and Young-guk Ha. 2017. A stream-based method to detect differences between XML documents. *Journal of Information Science* 43, 1 (2017), 39–53.
- [33] Taewoo Kim, Wenhai Li, Alexander Behm, Inci Cetindil, Rares Vernica, Vinayak Borkar, Michael J Carey, and Chen Li. 2020. Similarity query support in big data management systems. *Information Systems* 88 (2020), 101455.
- [34] Meike Klettke, Uta Störl, and Stefanie Scherzinger. 2015. Schema extraction and structural outlier detection for JSON-based NoSQL data stores. *Datenbanksysteme für Business, Technologie und Web* (2015), 425–444.
- [35] IBM Knowledge Center. 2022. Fuzzy search. https://www.ibm.com/support/knowledgecenter/SSEPGG_11.5.0/com.ibm.db2.luw.admin.ts.doc/doc/c0058557.html. Accessed: 2022-01-12.
- [36] Daniel Kocher and Nikolaus Augsten. 2019. A scalable index for top-k subtree similarity queries. In *Proceedings of the 2019 International Conference on Management of Data*. ACM, 1624–1641.
- [37] Erwin Leonardi and Sourav S Bhowmick. 2005. Detecting changes on unordered XML documents using relational databases: a schema-conscious approach. In *Proceedings of the 14th ACM International Conference on Information and Knowledge Management*. 509–516.
- [38] Willi Mann, Nikolaus Augsten, and Panagiotis Bouros. 2016. An empirical evaluation of set similarity join techniques. *Proceedings of the VLDB Endowment* 9, 9, 636–647.
- [39] MongoDB. 2020. *White paper: MongoDB Architecture Guide: Overview*. Technical Report. 12 pages. [mongodb.com](https://www.mongodb.com)
- [40] Jianmo Ni, Jiacheng Li, and Julian McAuley. 2019. Justifying Recommendations using Distantly-Labeled Reviews and Fine-Grained Aspects. In *Proceedings of the 2019 Conference on Empirical Methods in Natural Language Processing*. 188–197.
- [41] Mateusz Pawlik and Nikolaus Augsten. 2016. Tree edit distance: Robust and memory-efficient. *Information Systems* 56 (2016), 157–173.
- [42] PostgreSQL Documentation. 2021. Additional Supplied Modules. <https://www.postgresql.org/docs/current/pgtrgm.html>. Accessed: 2022-01-12.
- [43] Reddit. 2021. Reddit Dataset. <https://www.reddit.com/r/science.json>. Accessed: 2022-01-12.
- [44] João Setubal and João Meidanis. 1997. *Introduction to Computational Biology*. PWS Publishing Company.
- [45] Zeyuan Shang, Yaxiao Liu, Guoliang Li, and Jianhua Feng. 2017. K-Join: Knowledge-Aware Similarity Join. In *Proceedings of the 33rd International Conference on Data Engineering*. IEEE, 23–24.
- [46] Dharma Shukla, Shireesh Thota, Karthik Raman, Madhan Gajendran, Ankur Shah, Sergii Ziuzin, Krishnan Sundaram, et al. 2015. Schema-agnostic indexing with Azure DocumentDB. *Proceedings of the VLDB Endowment* 8, 12, 1668–1679.
- [47] William Spoth, Ting Xie, Oliver Kennedy, Ying Yang, Beda Hammerschmidt, Zhen Hua Liu, and Dieter Gawlick. 2018. SchemaDrill: Interactive Semi-Structured Schema Design. In *Proceedings of the Workshop on Human-In-the-Loop Data Analytics*. 1–7.
- [48] Kuo-Chung Tai. 1979. The tree-to-tree correction problem. *J. ACM* 26, 3, 422–433.
- [49] Yu Tang, Yilun Cai, and Nikos Mamoulis. 2015. Scaling similarity joins over tree-structured data. *Proceedings of the VLDB Endowment* 8, 11, 1130–1141.
- [50] Robert Endre Tarjan. 1983. *Data structures and network algorithms*. SIAM.
- [51] Twitter. 2022. Twitter Developer Platform. <https://developer.twitter.com/en/docs.html> Accessed: 2022-01-12.
- [52] Cornell University. 2022. arXiv Dataset. <https://www.kaggle.com/Cornell-University/arxiv> Accessed: 2022-01-12.
- [53] Stanford University. 2019. Stanford QA Dataset. <https://www.kaggle.com/stanfordu/stanford-question-answering-dataset> Accessed: 2022-01-12.
- [54] US. 2021. Open Data US. <https://www.data.gov>. Accessed: 2022-01-12.
- [55] Lusheng Wang and Kaizhong Zhang. 2008. Space efficient algorithms for ordered tree comparison. *Algorithmica* 51, 3 (2008), 283–297.
- [56] Elyas Ben Hadj Yahia, Jean-Rémy Falleri, and Laurent Réveillére. 2017. Polly: A Language-Based Approach for Custom Change Detection of Web Service Data. In *International Conference on Service-Oriented Computing*. Springer, 430–444.
- [57] Rui Yang, Panos Kalnis, and Anthony KH Tung. 2005. Similarity evaluation on tree-structured data. In *Proceedings of the 2005 International Conference on Management of Data*. ACM, 754–765.
- [58] Minghe Yu, Jin Wang, Guoliang Li, Yong Zhang, Dong Deng, and Jianhua Feng. 2017. A unified framework for string similarity search with edit-distance constraint. *The VLDB Journal* 26, 2 (2017), 249–274.
- [59] Kaizhong Zhang. 1995. Algorithms for the constrained editing distance between ordered labeled trees and related problems. *Pattern recognition* 28, 3 (1995), 463–474.
- [60] Kaizhong Zhang. 1996. A constrained edit distance between unordered labeled trees. *Algorithmica* 15, 3 (1996), 205–222.
- [61] Kaizhong Zhang, Rick Statman, and Dennis Shasha. 1992. On the editing distance between unordered labeled trees. *Information processing letters* 42, 3 (1992), 133–139.