# Joint UAV Hovering Altitude and Power Control for Space-Air-Ground IoT Networks

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Abstract—Unmanned aerial vehicles (UAVs) have been widely used in both military and civilian applications. Equipped with diverse communication payloads, UAVs cooperating with satellites and base stations (BSs) constitute a space-air-ground three-tier heterogeneous network, which are beneficial in terms of both providing the seamless coverage as well as of improving the capacity for increasingly prosperous Internet of Things (IoT) networks. However, cross-tier interference may be inevitable among these tightly embraced heterogeneous networks when sharing the same spectrum. The power association problem in satellite, UAV and macrocell three-tier networks becomes a critical issue. In our paper, we propose a two-stage joint hovering altitude and power control solution for the resource allocation problem in UAV networks considering the inevitable cross-tier interference from space-air-ground heterogeneous networks. Furthermore, Lagrange dual decomposition and concaveconvex procedure (CCP) method are used to solve this problem, followed by a low-complexity greedy search algorithm. Finally, simulation results show the effectiveness of our proposed twostage joint optimization algorithm in terms of UAV network's total throughput.

*Index Terms*—UAV communication networks, IoT network, power control, cross-tier interference, heterogeneous networks, satellite.

# I. Introduction

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IVEN the substantial success of unmanned aerial vehicles (UAVs) in surveillance and monitoring tasks, it has become vitally important to bring drones into wireless communications considering their low cost, fast deployment, fully controllable mobility as well as the line of sight (LOS) communication links. These drones are usually equipped with diverse payloads for receiving, processing and transiting signals, which can be viewed as the aerial mobile base station (AMBS) constituting UAV communication networks [1] [2].

UAV communication networks along with traditional satellite networks and ground cellulars construct a space-air-ground three-tier heterogeneous network, which is capable of both providing seamless coverage as well as of further improving the channel capacity for increasingly prosperous Internet of Things (IoT) networks [3]–[5]. More explicitly, the ground marcocell base station (MBS) provides the basic broad-band information services for the IoT nodes. Small drones act as on-demand aerial access points for the sake of offloading the ground MBS and of constructing emergency links in the context of contingency. Moreover, UAV netowrk can be viewed as a promising solution to support energy-efficient uplink and location in energy-constrained IoT-centric networks [6]. By contrast, the satellite is used for providing a global coverage benefitting from its broadcast services and broad sight [7]. Hence, relying on such three-tier heterogeneous network, the connectivity, capacity and energy efficiency of IoT networks can be significantly improved.

In particular, as a beneficial communication enhancement facilitator, UAV network is characterized by flexility, cost-saving and energy-efficiency. Specifically, in remote regions not seamlessly covered by macrocells on the ground, the UAV network may economically provide information services for IoT nodes compared with the high cost of satellite connections. Furthermore, in crowded places the UAV network may relieve the channel congestion of the macrocell and guarantee the quality of service (QoS) of latency- and throughput-sensitive IoT applications [8] [9]. More importantly, UAVs can help to quickly construct an emergency information system or even act as the IoT sensing nodes, which is beneficial of supporting the disaster relief when a large part of cellular and Internet infrastructures on the ground are destroyed by a calamity [10].

UAV aided hybrid communication techniques have been widely investigated in the literature. Specifically, in [11], Amorim *et al.* presented models for path loss exponents and shadowing of the radio channel between UAVs and cellular networks with the aid of a field measurement. Zeng *et al.* 

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proposed an energy-efficient UAV communication model by optimizing the trajectory of drones, which jointly considered both the energy consumption and the communication throughput in [12]. The energy efficiency of UAV communication was defined as the ratio of total transmitted bits to UAV's energy consumption. Furthermore, an effective dynamic trajectory control mechanism for multi-UAV network was proposed by Fadlullah et al. in [13], which was beneficial in terms of both improving the network throughput as well as of reducing the communication delay. In [14], Mozaffari et al. considered a coexistence between the UAVs and an underlaid device-to-device (D2D) communication network and studied the coverage performance as well as data rate. However, the aforementioned articles mostly focused their attention on how to improve the communication performance such as throughput, delay and coverage, by designing the mobility of drones, while few considered the intra- and inter-interference and cross-tier resource allocation among different networks.

Due to spectrum scarcity, it is possible to sharing the spectrum among different kinds of communication subsystems. More specifically, the C-band, Ku-band and Ka-band have been well utilized for air-to-ground reliable wide-band communications. Particularly, a range of compelling applications of the fifth generation wireless systems (5G) attempt to use higher frequency band for providing low-latency and highthroughput services, such as C-band and Ka-band, which are originally assigned to the airborne communications [15]–[18]. It is worth noting that mmWave communications [19] have been already adopted in both UAV and satellite scenarios [20]-[23]. Hence, a well-implemented network association mechanism of space-air-ground heterogeneous systems is beneficial in terms of both improving the resource utilization as well as of reducing the cross-tier interference [24] [25] [26]. As for the resource allocation problem in heterogeneous networks, Fooladivanda et al. in [27] investigated the user association and resource allocation in heterogeneous cellular networks in terms of orthogonal channel deployment, co-channel deployment as well as partially shared channel deployment. Moreover, they obtained upper bounds of the heterogeneous network's performance. Furthermore, a distributed joint allocation algorithm is proposed for band selection and power allocation in order to maximize total capacity of a multi-mode and multi-band user terminal (MMT) by Choi et al. in [28]. Moreover, considering the aspect of energy efficiency, Xie et al. in [29] formulated an energy-efficient resource allocation problem as a Stackelberg game for heterogeneous cognitive femtocells, followed by a gradient based iteration solution. In [30], Ye et al. focused their attention on the relationship between the user association and load balancing for heterogeneous networks with picocells and femtocells solved by a low-complexity and fast-convergence distributed algorithm. Furthermore, in [31], a mixed-integer programming problem was formulated for allocating subchannel and power resources in orthogonal frequency-division multiple access (OFDMA) hybrid networks with femtocells.

However, these resource allocation mechanisms may not be suitable for the applications for the UAV aided spaceair-ground heterogeneous network, because few of them considered the characteristics of UAVs in designing resource allocation algorithms, such as dynamic topology, flexible deployment, etc. Given a general space-air-ground heterogeneous communication scenario jointly served by the satellite, lowaltitude UAVs and the ground MBS, users served by UAV networks may severely influence or be inevitably affected by the operation of satellite communication systems and macrocells. Therefore, the resource allocation of different kinds of users should take into account the inevitable crosstier interference in space-air-ground hybrid networks [32]. Moreover, as the aerial base stations, UAVs play a critical role in offloading the ground MBS and in enhancing ultra-reliable communication links. Given the coverage of each drone network, frequently changing UAVs' horizontal hovering position in the same altitude may result in server inter-interference between adjacent UAV networks and increase the risk of flight collision. Additionally, considering the power constraint of small drones, it may be unrealistic to make the drone adaptively move around for supporting the bursty traffic of the ground users. Hence, a delicately designed UAVs' hovering altitude distribution is capable of improving the user's QoS by deploying more drones in different hovering altitudes as well as of guaranteeing their flight safety.

Inspired by the above-mentioned open challenges, in this paper, we propose a two-stage joint hovering altitude and power control for UAV networks in the context of a space-air-ground heterogeneous communication network considering diverse user's QoS requirements. Our main contributions can be summarized as follows:

- To the best of our knowledge, this is the first work for resource allocation for UAV networks in the context of space-air-ground heterogeneous communication systems considering the feasible deployment of drones aiming to reduce the cross-tier interference.
- A two-stage joint hovering altitude and power control solution is investigated for our proposed model. Both the Lagrange dual decomposition and concave-convex procedure (CCP) method are used to approximatively solve the relaxed convex problem. Moreover, a low-complexity greedy proportionable power constrained algorithm is proposed for resource allocation in UAV networks.
- Extensive simulations are conducted in order to evaluate
  the performance of our proposed two-stage joint resource
  allocation scheme. Simulation results show that our resource allocation mechanism is beneficial in terms of
  improving UAV network's total throughput considering
  the inevitable cross-tier interference.

The remainder of this article is outlined as follows. The system model and problem formulation are detailed in Section II. A two-stage joint hovering altitude and power control solution for UAV networks is elaborated in Section III. In Section IV, the implementation of the aforementioned two-stage joint iterative algorithm as well as a low-complexity greedy algorithm is presented, including its complexity analysis. In Section V, simulation results are provided for characterizing our proposed uplink resource allocation model for UAV networks, followed by our conclusions in Section VI.

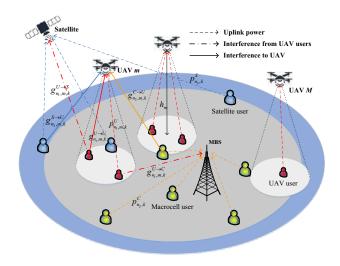


Fig. 1. The structure of satellite, UAV and macrocell three-tier hybrid network

### II. SYSTEM MODEL AND PROBLEM FORMULATION

#### A. System Model

In this paper, as show in Fig. 1, we consider a three-tier hybrid network including a satellite network with a geosynchronous earth orbit satellite (GEO), a macrocell with a MBS and M UAV networks sharing the same channel. Each UAV network is served by a hovering drone. Let  $h_m$  represent the hovering altitude of the m-th drone. The coverage of M UAV networks are overlaid within the coverage of the GEO as well as the macrocell. We focus our attention on the uplink power control of the users in the UAV networks. We assume that the uplink power of both satellite users and of macrocell users is equal.

The bandwidth of the channel is B, which is divided into K subchannels. The channel fading between the MBS and users on the ground is the frequency-selective Reyleigh fading, while the communication channel between the hovering drone and users is dominated by the line of sight (LoS) path. The channel fading between the GEO and users on the ground is the Rice fading.

Let  $N_S$  and  $N_C$  denote the number of active users served by the GEO and by the MBS in a macrocell, respectively. Moreover,  $N_U$  is the number of active users camping on each UAV network. We assume that the satellite users and the macrocell users are uniformly distributed in each coverage area. In our model, two kinds of users with different QoS requirements are served in each UAV network. Specifically, the number of QoS-sensitive users requiring a high transmission rate of  $R_h$  is  $N_{uh}$ , while the number of QoS-tolerant users with a low transmission rate requirement of  $R_l$  is  $N_{ul}$ , where  $N_{uh} + N_{ul} = N_U$ . Let  $\mathbb{N}_{uh}$  and  $\mathbb{N}_{ul}$  represent the set of QoS-sensitive users and QoS-tolerant users, respectively. Then, we have  $|\mathbb{N}_{uh}| = N_{uh}$  and  $|\mathbb{N}_{ul}| = N_{ul}$ , and  $|\mathbb{N}_{uh}| \cap \mathbb{N}_{ul} = \emptyset$ .

have  $|\mathbb{N}_{uh}| = N_{uh}$  and  $|\mathbb{N}_{ul}| = N_{ul}$ , and  $\mathbb{N}_{uh} \cap \mathbb{N}_{ul} = \emptyset$ . Let  $g_{n_1,m,k}^{U \to S}, g_{n_1,m,k}^{U \to C}$  and  $g_{n_1,m,k}^{U \to U}$  denote the channel gains on k-th subchannel from user  $n_1$  in m-th UAV network to the GEO, to the MBS and to the hovering drone, respectively, where  $n_1 \in \{1,2,\ldots,N_U\}, m \in \{1,2,\ldots,M\}$  and  $k \in \{1,2,\ldots,K\}$ . In our model,  $g_{n_1,m,k}^{U \to S}$  can be viewed as a constant because the UAV users locate far away from the GEO satellite, while  $g_{n_1,m,k}^{U \to C}$  depends the channel state and the distance between each UAV user and the MBS. For the sake of analysis, we assume that the service radius of each drone can be neglected compared with its altitude, and hence  $g_{n_1,m,k}^{U \to U}$  is only sensitive to the hovering altitude  $h_m$  of the m-th drone, which can be formulated as:

$$g_{n_1,m,k}^{U\to U} = \frac{\kappa}{h_m^2},\tag{1}$$

where  $\kappa$  denotes the unit power gain in terms of the reference distance  $h_r=1$ m. Furthermore, let  $g_{n_2,m,k}^{C\to U}$  represent the channel gain on k-th subchannel from user  $n_2$  in the macrocell to the m-th hovering drone, while  $g_{n_3,m,k}^{S\to U}$  denotes the channel gain on k-th subchannel from user  $n_3$  in the satellite network to the m-th hovering drone, where  $n_2\in\{1,2,\ldots,N_C\}$  and  $n_3\in\{1,2,\ldots,N_S\}$ . Moreover, let  $p_{n_2,k}^C$  and  $p_{n_3,k}^S$  represent the uplink transmission power of user  $n_2$  in the macrocell and of user  $n_3$  in the satellite network on k-th subchannel, respectively, while  $p_{n_1,m,k}^U$  is the uplink transmission power of user  $n_1$  in the m-th UAV network on k-th subchannel. In our model, we define  $\mathbf{P}_{N_U\times M\times K}$  as the power allocation matrix for the users served by total M UAV networks, and we have  $|\mathbf{P}|_{n_1,m,k} = p_{n_1,m,k}^U$ .

 $[\mathbf{P}]_{n_1,m,k}=p^U_{n_1,m,k}.$  Here, we define a channel indicator matrix as  $\mathbf{A}_{N_U\times M\times K}$ , where  $[\mathbf{A}]_{n_1,m,k}=a_{n_1,m,k}.$  To elaborate,  $a_{n_1,m,k}=1$  represents that the k-th subchannel is occupied by user  $n_1$  in the m-UAV network, otherwise,  $a_{n_1,m,k}=0.$  We consider the additive white Gaussian noise (AWGN) with the variance of  $\sigma^2$ . Hence, as for the m-th UAV network, the received signal-to-interference-plus-noise ratio (SINR) of the hovering drone from user  $n_1$  accessing the k-th subchannel can be calculated by:

$$\gamma_{n_1,m,k} = \frac{p_{n_1,m,k}^U g_{n_1,m,k}^{U \to U}}{g_{n_2,m,k}^{C \to U} p_{n_2,k}^C + g_{n_2,m,k}^{S \to U} p_{n_2,k}^S + \sigma^2},$$
 (2)

where  $g_{n_2,m,k}^{C \to U} p_{n_2,k}^C$  is the interference from the user in the macrocell sharing the same sub-channel, while  $g_{n_3,m,k}^{S \to U} p_{n_3,k}^S$  is the interference caused by the user in the satellite network occupying the k-th sub-channel. Remarkably, at most one user is capable of accessing the same subchannel at one moment in the macrocell, in the satellite network as well as in a UAV network. For the sake of simplification, in our model we assume that the users served by the drones are equipped with a directional antenna and the co-interference between different UAV networks is negligible compared with the crosstier interference from the macrocell and the satellite network.

Relying on the Shannon formula [33], the uplink capacity of m-th UAV network from its user  $n_1$  on k-th subchannel can be calculated by:

$$C_{n_1,m,k} = \frac{B}{K} \log_2 (1 + \gamma_{n_1,m,k}).$$
 (3)

#### B. Problem Formulation

In this section, we will formulate the uplink resource allocation problem for the UAV network. Furthermore, we

assume that the channel state information (CSI) as well as the result of uplink resource allocation can be forwarded to the users by the hovering drone based on the channel reciprocity.

- 1) Constraints: In our uplink resource allocation problem, our objective is to maximize the total capacity in M UAV networks under the following constraints:
  - UAV user's power constraint: the users in each UAV network have a maximum transmission power limit of  $P_{max}^U$ . Hence, for  $\forall n_1 \in \{1, 2, \dots, N_U\}$  and  $\forall m \in \{1, 2, \dots, M\}$ , we have:

$$\sum_{k=1}^{K} a_{n_1,m,k} p_{n_1,m,k}^U \le P_{\max}^U. \tag{4}$$

Furthermore, the non-negativity of power yields  $p_{n_1,m,k}^U \geq 0$ . • UAV safety flight and hovering altitude constraint: In

• UAV safety flight and hovering altitude constraint: In order to guarantee the safety of M cooperated drones, we consider a hierarchical deployment of these drones with different hovering altitudes. Moreover, the hovering altitudes of them are distributed within a specified safe range of  $[h_{\min}, h_{\max}]$  and subjects to:

$$\sum_{i,j\in\mathbb{M},i\neq j} (h_i - h_j)^2 \ge \chi^2,\tag{5}$$

where  $\chi^2$  is the minimal variance of the altitude of M drones for safety flight and hovering, while  $\mathbb{M}$  represents the set of M hovering drones. Moreover, for  $\forall i, j \in \mathbb{M}$ , we have  $h_{\min} \leq h_i, h_j \leq h_{\max}$ .

QoS guarantee: For the QoS-sensitive users, the requirement of a high transmission rate of R<sub>h</sub> can be expressed as:

$$\sum_{k=1}^{K} a_{n_{uh},m,k} C_{n_{uh},m,k} \ge R_h, \tag{6}$$

where  $\forall n_{uh} \in \mathbb{N}_{uh}$  and  $\forall m \in \{1, 2, ..., M\}$ . By contrast, for the QoS-tolerant users, we have:

$$\sum_{k=1}^{K} a_{n_{ul},m,k} C_{n_{ul},m,k} \ge R_l, \tag{7}$$

where  $\forall n_{ul} \in \mathbb{N}_{ul}$  and  $\forall m \in \{1, 2, \dots, M\}$ .

• Interference constraint of macrocell: UAV networks share the same frequency with the macrocell. Hence, the macrocell may suffer a cross-tier interference from M UAV networks. Let  $I_k^C$  denote the threshold of the interference on the k-th subchannel and  $\forall k \in \{1, 2, \ldots, K\}$ , i.e.

$$\sum_{m=1}^{M} \sum_{n_1=1}^{N_U} a_{n_1,m,k} p_{n_1,m,k}^U g_{n_1,m,k}^{U \to C} \le I_k^C. \tag{8}$$

• Interference constraint of satellite network: Similar to the interference constraint of macrocell, let  $I_k^S$  represent the threshold of the interference from UAV networks to the satellite network on the k-th subchannel. Thus, we have:

$$\sum_{m=1}^{M} \sum_{n_1=1}^{N_U} a_{n_1,m,k} p_{n_1,m,k}^U g_{n_1,m,k}^{U \to S} \le I_k^S, \tag{9}$$

where  $\forall k \in \{1, 2, ..., K\}$ .

 Subchannel allocation constraint: In each UAV network, one subchannel can be allocated to at most one user, which can be formulated by:

$$\sum_{n_1=1}^{N_U} a_{n_1,m,k} \le 1,\tag{10}$$

where  $\forall k \in \{1, 2, ..., K\}$  and  $\forall m \in \{1, 2, ..., M\}$ . Moreover, the channel indicator variable  $a_{n_1, m, k} \in \{0, 1\}$ .

2) Uplink Resource Allocation Formulation: The total capacity of M UAV networks can be given by:

$$C_{total} = \sum_{m=1}^{M} \sum_{n_1=1}^{N_U} \sum_{k=1}^{K} a_{n_1,m,k} C_{n_1,m,k}.$$
 (11)

Hence, the uplink resource allocation problem can be formulated as:

$$\max_{\{a_{n_1,m,k},p_{n_1,m,k}^U,h_m\}} \sum_{m=1}^M \sum_{n_1=1}^{N_U} \sum_{k=1}^K a_{n_1,m,k} C_{n_1,m,k}$$
s.t.  $(12a): \sum_{k=1}^K a_{n_1,m,k} p_{n_1,m,k}^U \leq P_{\max}^U, \forall n_1, m,$ 

$$(12b): p_{n_1,m,k}^U \geq 0, \forall n_1, m, k,$$

$$(12c): \sum_{i,j \in \mathbb{M}, i \neq j} (h_i - h_j)^2 \geq \chi^2,$$

$$(12d): h_{\min} \leq h_m \leq h_{\max}, \forall m,$$

$$(12e): \sum_{k=1}^K a_{n_{uh},m,k} C_{n_{uh},m,k} \geq R_h, \forall n_{uh}, m,$$

$$(12f): \sum_{k=1}^K a_{n_{ul},m,k} C_{n_{ul},m,k} \geq R_l, \forall n_{ul}, m,$$

$$(12g): \sum_{m=1}^M \sum_{n_1=1}^{N_U} a_{n_1,m,k} p_{n_1,m,k}^U g_{n_1,m,k}^{U \to C} \leq I_k^C, \forall k,$$

$$(12h): \sum_{m=1}^M \sum_{n_1=1}^{N_U} a_{n_1,m,k} p_{n_1,m,k}^U g_{n_1,m,k}^{U \to S} \leq I_k^S, \forall k,$$

$$(12i): \sum_{n_1=1}^N a_{n_1,m,k} \leq 1, \forall m, k,$$

$$(12j): a_{n_1,m,k} \in \{0,1\}, \forall n_1, m, k.$$

To elaborate further, (12a) and (12b) in problem (12) are users' power constraints, while (12c) and (12d) are hovering altitude constraints. As for the QoS constraints (12e) and (12f), considering the QoS-tolerant users with a low transmission rate requirement of  $R_l$ , where  $0 < R_l \ll R_h$ , hence we can neglect the constraint (12f) in problem (12) without loss of generality. Furthermore, (12g) and (12h) are interference constraint from macrocell and satellite network, respectively. Finally, the subchannel allocation constraints are given by (12i) and (12j). Unfortunately, however, our optimization objective is a function of  $(a_{n_1,m,k},\ p_{n_1,m,k}^U,\ h_m)$ , and the form of  $a_{n_1,m,k}C_{n_1,m,k}$  is not concave in  $(a_{n_1,m,k},\ p_{n_1,m,k}^U,\ h_m)$ . Moreover, the hovering altitude constraint of (12c) and the

integer programming constraint of (12j) are not convex as well. In the following, we will reformulate the optimization problem (12) as a convex optimization problem with the aid of relaxing the integer constraints and provide its solution relying on a two-stage joint optimization.

# III. TWO-STAGE JOINT HOVERING ALTITUDE AND POWER CONTROL SOLUTION

In this section, we propose a two-stage joint optimization algorithm for our uplink resource allocation problem. Since there are a total of three kinds of optimization variables in problem (12), i.e  $a_{n_1,m,k},\ p_{n_1,m,k}^U$  and  $h_m$ , it is prohibitive to find the globally optimal solution and thus a near optimal algorithm with low computational complexity is desirable. In the following, we first fix the hovering altitude  $h_m=h_m^0, m\in\mathbb{M}$  and search the optimal joint subchannel and power control scheme in Stage 1. Then, relying on the result of Stage 1, we try to find the optimal hovering altitude of each drone in Stage 2.

# A. Stage 1: Joint Subchannel and Power Control

1) Constraint Relaxation: Here, we first study the joint subchannel and power control problem with given hovering altitude, where the initial  $h_m^0$  constitutes a arithmetic progression ranging from  $h_{\min}$  to  $h_{\max}$ . In the following, we convert the non-convex problem (12) into a tractable convex problem [31] [34] [35]. First of all, we relax the inter programming constraint  $a_{n_1,m,k} \in \{0,1\}$  in (12j) to a continuous convex constraint  $a_{n_1,m,k} \in [0,1]$ .

continuous convex constraint  $a_{n_1,m,k} \in [0,1]$ . Furthermore, let us introduce the auxiliary variable  $\rho_{n_1,m,k} = a_{n_1,m,k} p_{n_1,m,k}^U$ , and hence the uplink capacity of Eq. (3) can be converted to:

$$\hat{C}_{n_{1},m,k} = \frac{B}{K} \log_{2} \left( 1 + \frac{\rho_{n_{1},m,k} g_{n_{1},m,k}^{U \to U}}{a_{n_{1},m,k} \left( g_{n_{2},m,k}^{C \to U} p_{n_{2},k}^{C} + g_{n_{3},m,k}^{S \to U} p_{n_{3},k}^{S} + \sigma^{2} \right)} \right),$$
(13)

where  $g_{n_1,m,k}^{U \to U} = \frac{\kappa}{h_m^2}$  and  $h_m \triangleq h_m^0, m \in \mathbb{M}$ . Now we introduce Lemma 1 to show the concavity of our objective function.

**Lemma 1.** Assume f(x) is a concave function of x when  $x \in [0, X]$ . Let us introduce a variable a as a = tx,  $t \in [0, 1]$ . Then, g(t, a) = tf(a/t) is concave in (t, a) when  $t \in [0, 1]$  and  $\forall a \in [0, tX]$ .

*Proof.* Since f(x) is a concave function,  $f''(x) \leq 0$ . The Hessian matrix of g(t,a) can be calculated as:

$$\nabla^2 g(t,a) = \frac{f^{''}(a/t)}{t^3} \left[ \begin{array}{cc} a^2 & -at \\ -at & t^2 \end{array} \right].$$

Furthermore, for  $\forall x, y \in \mathbb{R}$  and  $t \in [0, 1]$ , we have:

$$\left[\begin{array}{cc} x & y\end{array}\right] \nabla^2 g(t,a) \left[\begin{array}{c} x \\ y\end{array}\right] = \frac{f^{''}(a/t)}{t^3} (ax-yt)^2 \leq 0.$$

Hence, the Hessian matrix  $\nabla^2 g(t,a)$  is a negative semidefinite matrix. Thus, g(t,a) = tf(a/t) is a concave function [36] [37].

Relying on **Lemma 1**, our optimization objective  $a_{n_1,m,k}\hat{C}_{n_1,m,k}$  is concave in  $(a_{n_1,m,k}, \rho_{n_1,m,k})$ , based on which our joint subchannel and power control problem can be reformulated as:

$$\max_{\{a_{n_1,m,k},\rho_{n_1,m,k}^U\}} \sum_{m=1}^M \sum_{n_1=1}^{N_U} \sum_{k=1}^K a_{n_1,m,k} \hat{C}_{n_1,m,k}$$
 s.t. 
$$(14a) : \sum_{k=1}^K \rho_{n_1,m,k} \le P_{\max}^U, \quad \forall n_1, m,$$
 
$$(14b) : \rho_{n_1,m,k} \ge 0, \quad \forall n_1, m, k,$$
 
$$(14c) : \sum_{k=1}^K a_{n_{uh},m,k} \hat{C}_{n_{uh},m,k} \ge R_h, \quad \forall n_{uh}, m,$$
 
$$(14d) : \sum_{m=1}^M \sum_{n_1=1}^{N_U} \rho_{n_1,m,k} g_{n_1,m,k}^{U \to C} \le I_k^C, \quad \forall k,$$
 
$$(14e) : \sum_{m=1}^M \sum_{n_1=1}^{N_U} \rho_{n_1,m,k} g_{n_1,m,k}^{U \to S} \le I_k^S, \quad \forall k,$$
 
$$(14f) : \sum_{n_1=1}^N a_{n_1,m,k} \le 1, \quad \forall m, k,$$
 
$$(14g) : a_{n_1,m,k} \in [0,1], \quad \forall n_1, m, k.$$

Obviously, our joint subchannel and power control problem in (14) is a convex optimization problem.

2) Lagrangian Dual Decomposition Method: In this subsection, we use the Lagrangian dual decomposition method to solve our joint subchannel and power control problem in (14) [38]. Let  $L(\mathbf{A}, \boldsymbol{\rho}, \boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\nu}, \boldsymbol{\omega}, \boldsymbol{\xi})$  be the Lagrangian function, which can be written as:

$$L(\mathbf{A}, \boldsymbol{\rho}, \boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\nu}, \boldsymbol{\omega}, \boldsymbol{\xi})$$

$$= \sum_{m=1}^{M} \sum_{n_{1}=1}^{N_{U}} \sum_{k=1}^{K} a_{n_{1},m,k} \hat{C}_{n_{1},m,k}$$

$$+ \sum_{m=1}^{M} \sum_{n_{1}=1}^{N_{U}} \lambda_{n_{1},m} \left( P_{\max}^{U} - \sum_{k=1}^{K} \rho_{n_{1},m,k} \right)$$

$$+ \sum_{m=1}^{M} \sum_{n_{uh}=1}^{N_{uh}} \mu_{n_{uh},m} \left( \sum_{k=1}^{K} a_{n_{uh},m,k} \hat{C}_{n_{uh},m,k} - R_{h} \right)$$

$$+ \sum_{k=1}^{K} \nu_{k} \left( I_{k}^{C} - \sum_{m=1}^{M} \sum_{n_{1}=1}^{N_{U}} \rho_{n_{1},m,k} g_{n_{1},m,k}^{U \to C} \right)$$

$$+ \sum_{k=1}^{K} \omega_{k} \left( I_{k}^{S} - \sum_{m=1}^{M} \sum_{n_{1}=1}^{N_{U}} \rho_{n_{1},m,k} g_{n_{1},m,k}^{U \to S} \right)$$

$$+ \sum_{m=1}^{M} \sum_{k=1}^{K} \xi_{m,k} \left( 1 - \sum_{n_{1}=1}^{N_{U}} a_{n_{1},m,k} \right), \tag{15}$$

where  $\lambda$ ,  $\mu$ ,  $\nu$ ,  $\omega$  and  $\xi$  are the Lagrange multipliers associated with the corresponding constraints, while  $\mathbf{A} = \{a_{n_1,m,k}\}$  and  $\boldsymbol{\rho} = \{\rho_{n_1,m,k}\}$ . The constraints of (14b) and (14g) will be considered after obtaining the optimal solution of  $a_{n_1,m,k}$ .  $\rho_{n_1,m,k}$ .

Hence, the Lagrangian dual function can be expressed as:

$$g(\lambda, \mu, \nu, \omega, \xi) = \sup_{\mathbf{A}, \rho} L(\mathbf{A}, \rho, \lambda, \mu, \nu, \omega, \xi).$$
(16)

The Lagrangian dual problem can be formulated as:

$$\min_{\boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\nu}, \boldsymbol{\omega}, \boldsymbol{\xi}} g(\boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\nu}, \boldsymbol{\omega}, \boldsymbol{\xi})$$
s.t.  $\boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\nu}, \boldsymbol{\omega}, \boldsymbol{\xi} \succeq 0$ .

Eq. (15) can be reorganized as:

$$L(\mathbf{A}, \boldsymbol{\rho}, \boldsymbol{\lambda}, \boldsymbol{\mu}, \boldsymbol{\nu}, \boldsymbol{\omega}, \boldsymbol{\xi}) = \sum_{m=1}^{M} \sum_{k=1}^{K} \boldsymbol{\Phi} + \boldsymbol{\Psi}, \quad (18)$$

where

$$\Phi = \sum_{n_{1}=1}^{N_{U}} a_{n_{1},m,k} \hat{C}_{n_{1},m,k} - \sum_{n_{1}=1}^{N_{U}} \lambda_{n_{1},m} \rho_{n_{1},m,k} 
+ \sum_{n_{uh}=1}^{N_{uh}} \mu_{n_{uh},m} a_{n_{uh},m,k} \hat{C}_{n_{uh}} - \sum_{n_{1}=1}^{N_{U}} \nu_{k} \rho_{n_{1},m,k} g_{n_{1},m,k}^{U \to C} 
- \sum_{n_{1}=1}^{N_{U}} \omega_{k} \rho_{n_{1},m,k} g_{n_{1},m,k}^{U \to S} - \sum_{n_{1}=1}^{N_{U}} \xi_{m,k} a_{n_{1},m,k},$$
(19)

and

$$\Psi = \sum_{m=1}^{M} \sum_{n_1=1}^{N_U} \lambda_{n_1,m} P_{\text{max}}^U - \sum_{m=1}^{M} \sum_{n_{uh}=1}^{N_{uh}} \mu_{n_{uh},m} R_h 
+ \sum_{k=1}^{K} \nu_k I_k^C + \sum_{k=1}^{K} \omega_k I_k^S + \sum_{m=1}^{M} \sum_{k=1}^{K} \xi_{m,k}.$$
(20)

Relying on Eq. (18), the dual problem can be divided into  $(M \times K)$  parallel subproblems. Let  $a_{n_1,m,k}^*$  and  $\rho_{n_1,m,k}^*$  represent the optimal solutions of maximizing the Eq. (19). Take the partial derivative of Eq. (19) with respect to  $a_{n_1,m,k}$ and  $\rho_{n_1,m,k}$ , and for the QoS-sensitive user  $i \in \mathbb{N}_{uh}$ , we have:

$$\frac{\partial \Phi}{\partial \rho_{i,m,k}} = \frac{B}{K \ln 2} \left( \frac{a_{i,m,k} g_{i,m,k}^{U \to U} + \mu_{i,m} a_{i,m,k} g_{i,m,k}^{U \to U}}{a_{i,m,k} \Delta + \rho_{i,m,k}^* g_{n_1,m,k}^{U \to U}} \right) - \Theta_i,$$
(21)

while for the QoS-tolerant user  $j \in \mathbb{N}_{ul}$ , i.e

$$\frac{\partial \mathbf{\Phi}}{\partial \rho_{j,m,k}} = \frac{B}{K \ln 2} \left( \frac{a_{j,m,k} g_{j,m,k}^{U \to U}}{a_{j,m,k} \Delta + \rho_{j,m,k}^* g_{j,m,k}^{U \to U}} \right) - \Theta_j, \qquad (22)$$

where  $\Delta=g_{n_2,m,k}^{C\to U}p_{n_2,k}^C+g_{n_3,m,k}^{S\to U}p_{n_3,k}^S+\sigma^2$  and  $\Theta_{n_1}=\lambda_{n_1,m}+\nu_kg_{n_1,m,k}^{U\to C}+\omega_kg_{n_1,m,k}^{U\to S}, n_1\in\{1,2,\ldots,N_U\}$ . Considering the constraint of (14b), as  $\Phi$  is also a concave function, the optimal solution  $\rho_{n_1,m_k}^*, \forall n_1, m, k$  obeys:

$$\begin{cases} \rho_{n_{1},m,k}^{*} = 0 & \text{and} & \frac{\partial \mathbf{\Phi}}{\partial \rho_{n_{1},m,k}} \mid_{\rho_{n_{1},m,k}=0} < 0, \\ \rho_{n_{1},m,k}^{*} > 0 & \text{and} & \frac{\partial \mathbf{\Phi}}{\partial \rho_{n_{1},m,k}} \mid_{\rho_{n_{1},m,k}=\rho_{n_{1},m,k}^{*}} = 0. \end{cases}$$
(23) 
$$\nu_{k}^{(i+1)} = \left[ \nu_{k}^{(i)} - \alpha_{3}^{(i)} \left( I_{k}^{C} - \sum_{m=1}^{M} \sum_{n_{1}=1}^{N_{U}} \rho_{n_{1},m,k} g_{n_{1},m,k}^{U \to C} \right) \right]^{+}$$

Then, the optimal solution of the power allocation  $p_{n_1,m,k}^{U*} =$  $\rho_{n_1,m,k}^*/a_{n_1,m,k}$  in m-th UAV network on the k-th subchannel for user  $n_1$  can be given by:

$$p_{n_{1},m,k}^{U*} = \left\{ \begin{array}{l} \max\left\{0, \ \frac{B(1+\mu_{i,m})}{K\ln 2 \times \Theta_{n_{1}}} - \frac{\Delta}{g_{j,m,k}^{U \to U}}\right\}, \ n_{1} \in \mathbb{N}_{uh}, \\ \max\left\{0, \ \frac{B}{K\ln 2 \times \Theta_{n_{1}}} - \frac{\Delta}{g_{j,m,k}^{U \to U}}\right\}, \ n_{1} \in \mathbb{N}_{ul}. \end{array} \right.$$
(24)

Similarly, considering  $a^*_{n_1,m,k} \in [0,1]$  in  $(14\mathrm{g})$ , the optimal solution  $a^*_{n_1,m,k}, \forall n_1,m,k$  are given by:

$$\begin{cases} a_{n_1,m,k}^* = 0 & \text{and} \quad \frac{\partial \mathbf{\Phi}}{\partial a_{n_1,m,k}} \mid_{a_{n_1,m,k}=0} < 0, \\ a_{n_1,m,k}^* \in (0,1) & \text{and} \quad \frac{\partial \mathbf{\Phi}}{\partial a_{n_1,m,k}} \mid_{a_{n_1,m,k}=a_{n_1,m,k}^*} = 0, \\ a_{n_1,m,k}^* = 1 & \text{and} \quad \frac{\partial \mathbf{\Phi}}{\partial a_{n_1,m,k}} \mid_{a_{n_1,m,k}=1} > 0, \end{cases}$$
(25)

where for the QoS-sensitive user  $i \in \mathbb{N}_{uh}$ ,

$$\frac{\partial \mathbf{\Phi}}{\partial a_{i,m,k}} = (1 + \mu_{i,m}) \frac{B}{K} \log_2 \left( 1 + \frac{p_{i,m,k}^{U*} g_{i,m,k}^{U \to U}}{\Delta} \right) 
- (1 + \mu_{i,m}) \frac{B p_{i,m,k}^{U*} g_{i,m,k}^{U \to U}}{K \ln 2 \times (\Delta + p_{i,m,k}^{U*} g_{i,m,k}^{U \to U})} - \lambda_{i,m} p_{i,m,k}^{U*} 
- \nu_k p_{i,m,k}^{U*} g_{i,m,k}^{U \to C} - \omega_k p_{i,m,k}^{U*} g_{i,m,k}^{U \to S} - \xi_{m,k},$$
(26)

and for the OoS-tolerant user  $j \in \mathbb{N}_{nl}$ , we have:

$$\frac{\partial \Phi}{\partial a_{j,m,k}} = \frac{B}{K} \log_2 \left( 1 + \frac{p_{j,m,k}^{U*} g_{j,m,k}^{U \to U}}{\Delta} \right) \\
- \frac{B p_{j,m,k}^{U*} g_{j,m,k}^{U \to U}}{K \ln 2 \times (\Delta + p_{j,m,k}^{U*} g_{j,m,k}^{U \to U})} - \lambda_{j,m} p_{j,m,k}^{U*} \\
- \nu_k p_{j,m,k}^{U*} g_{j,m,k}^{U \to C} - \omega_k p_{j,m,k}^{U*} g_{j,m,k}^{U \to S} - \xi_{m,k}.$$
(27)

In our model, at most one user is allowed to access the same subchannel at one moment in a UAV network. In order to maximize the Lagrangian function, we have:

$$n_1^* = \arg\max_{n_1} \frac{\partial \mathbf{\Phi}}{\partial a_{n_1, m, k}}, \quad \forall m, k,$$
 (28)

where  $a_{n_1^*,m,k}^*=1$  represents the suboptimal channel indicator

3) The Update of Lagrangian Multipliers: Since the Lagrangian dual function in Eq. (16) is not differentiable, we use the subgradient method to update the Lagrangian multipliers  $\lambda$ ,  $\mu$ ,  $\nu$ ,  $\omega$  and  $\xi$  [39] [40] [41]. The Lagrangian multipliers can be updated as follows:

$$\lambda_{n_1,m}^{(i+1)} = \left[\lambda_{n_1,m}^{(i)} - \alpha_1^{(i)} \left(P_{\text{max}}^U - \sum_{k=1}^K \rho_{n_1,m,k}\right)\right]^+, \forall m, n_1,$$
(29)

$$\mu_{n_{uh},m}^{(i+1)} = \left[\mu_{n_{uh},m}^{(i)} - \alpha_2^{(i)} \left(\sum_{k=1}^K a_{n_{uh},m,k} \hat{C}_{n_{uh},m,k} - R_h\right)\right]^+, \forall m, n_{uh},$$
(30)

$$\nu_k^{(i+1)} = \left[\nu_k^{(i)} - \alpha_3^{(i)} \left(I_k^C - \sum_{m=1}^M \sum_{n_1=1}^{N_U} \rho_{n_1,m,k} g_{n_1,m,k}^{U \to C}\right)\right]^+, \forall k,$$
(31)

$$\omega_k^{(i+1)} = \left[ \omega_k^{(i)} - \alpha_4^{(i)} \left( I_k^S - \sum_{m=1}^M \sum_{n_1=1}^{N_U} \rho_{n_1, m, k} g_{n_1, m, k}^{U \to S} \right) \right]^+, \forall k,$$
(32)

where i is the indicator of the iteration, and  $\alpha$  represents the step size, while  $[\cdot]^+ = \max\{0, \cdot\}$ . Moreover, to guarantee the convergence of the subgradient method, the step sizes should satisfy:

$$\sum_{i=1}^{\infty} \alpha^{(i)} = \infty, \quad \text{and} \quad \lim_{i \to \infty} \alpha^{(i)} = 0.$$
 (33)

In order to speed up the convergence, an adaptive step size is set as  $\alpha=1/I$ , where I represents the iteration index. Relying on Eq. (24)-Eq. (33), we can obtain the optimal solution  $\left\{a_{n_1,m,k}^*, p_{n_1,m,k}^{U*}\right\}$  of joint subchannel and power control for each users in UAV networks considering a fixed deployment altitude of hovering drones. Denote the obtained total capacity of UAV networks as  $C_{total}(a_{n_1,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h})$ , where  $\mathbf{h} \triangleq [h_1, h_2, \ldots, h_M]^T$ .

## B. Stage 2: Hovering Altitude Optimization

1) Difference of Convex Programming Based Hovering Altitude Formulation: As mentioned before, in Stage 1, we fix the deployment altitude of each hovering drone and search for the optimal joint subchannel and power control mechanism for each user in UAV network, denoted as  $\left\{a_{n_1^*,m,k}^*, p_{n_1,m,k}^{U^*}\right\}$ , where  $n_1 \in \{1,2,\ldots,N_U\}$ ,  $m \in \{1,2,\ldots,M\}$  and  $k \in \{1,2,\ldots,K\}$ . In the following, we try to determine the optimal hovering altitude of each drone based on the results obtained from Stage 1. Considering the safety hovering altitude constraints of (12c) and (12d) in our original problem formulation in (12), we have:

$$\max_{\{h_m\}} \sum_{m=1}^{M} \sum_{n_1=1}^{N_U} \sum_{k=1}^{K} a_{n_1^*,m,k}^* \frac{B}{K} \log_2 \left( 1 + \frac{\kappa p_{n_1,m,k}^{U*}}{h_m^2 \Delta} \right) 
\text{s.t.} \quad (34a) : \sum_{i,j \in \mathbb{M}, i \neq j} (h_i - h_j)^2 \ge \chi^2,$$

$$(34b) : h_m \le h_{\text{max}}, \quad \forall m, 
(34c) : h_m \ge h_{\text{min}}, \quad \forall m.$$
(34)

The hovering altitude optimization problem in (34) can be reformulated as a difference of convex (DC) programming [42] [43], which can be given by:

$$\min_{\mathbf{h}} \quad 0 - g_0(\mathbf{h}) 
s.t. \quad (35a) : \chi^2 - g_1(\mathbf{h}) \le 0, 
\quad (35b) : h_m \le h_{\max}, \quad \forall m, 
\quad (35c) : h_m \ge h_{\min}, \quad \forall m.$$
(35)

where the objective function can be expressed as:

$$g_0(\mathbf{h}) = \sum_{m=1}^{M} \sum_{n_1=1}^{N_U} \sum_{k=1}^{K} a_{n_1^*, m, k}^* \frac{B}{K} \log_2 \left( 1 + \frac{\kappa p_{n_1, m, k}^{U*}}{h_m^2 \Delta} \right),$$
(36)

and  $g_1(\mathbf{h})$  can be given by:

$$g_1(\mathbf{h}) = \sum_{i,j \in \mathbb{M}, i \neq j} (h_i - h_j)^2. \tag{37}$$

# **Algorithm 1:** CCP aided Iterative Algorithm for Optimal Hovering Altitude

- 1: Initialize an initial feasible  $\mathbf{h}^{*(0)}$ , and a stopping threshold  $\delta$ .
- 2: Set iteration indicator n := 0.
- 3: repeat
- 4: Calculate  $g_0(\mathbf{h}^{*(n)})$ .
- 5:  $\hat{g}_0(\mathbf{h}; \mathbf{h}^{*(n)}) \triangleq g_0(\mathbf{h}^{*(n)}) + \nabla g_0(\mathbf{h}^{*(n)})^T (\mathbf{h} \mathbf{h}^{*(n)}).$
- 6:  $\hat{g}_1(\mathbf{h}; \mathbf{h}^{*(n)}) \triangleq g_1(\mathbf{h}^{*(n)}) + \nabla g_1(\mathbf{h}^{*(n)})^T(\mathbf{h} \mathbf{h}^{*(n)}).$
- 7: Solve the convex subproblem in (41).
- 8: Obtain  $\mathbf{h}^{*(n+1)}$  and calculate  $g_0(\mathbf{h}^{*(n+1)})$ .
- 9: Update iteration indicator n := n + 1.
- 10: **until**  $g_0(\mathbf{h}^{*(n)}) g_0(\mathbf{h}^{*(n-1)}) \le \delta$  is satisfied.
- 11: Set  $\mathbf{h}^* \stackrel{\triangle}{=} \mathbf{h}^{*(n)}$ .

Specifically,  $g_1(\mathbf{h})$  is a quadratic form, which can be rewritten as  $g_1(\mathbf{h}) = \mathbf{h}^T \mathbf{Q} \mathbf{h}$ , where  $\mathbf{Q} = diag(M) - 1$ . Moreover, diag(M) denotes a diagonal matrix with all diagonal elements equaling M and  $\mathbf{1}$  is an  $M \times M$  matrix with all elements being 1. Hence, both  $g_0(\mathbf{h})$  and  $g_1(\mathbf{h})$  in (35) are convex functions. Hence, we can use the CCP method to solve the problem in (35), where we are capable of achieving the locally optimal result of the non-convex problem through solving a series of iterative convex subproblems as shown in Algorithm. 1.

2) CCP Aided Iterative Solation: To elaborate a litter further, let  $\hat{g}_0(\mathbf{h})$  and  $\hat{g}_1(\mathbf{h})$  approximatively be the first-order Taylor expansion of  $g_0(\mathbf{h})$  and  $g_1(\mathbf{h})$ , respectively, i.e.

$$\hat{g}_0(\mathbf{h}; \mathbf{h}^{(n)}) \triangleq g_0(\mathbf{h}^{(n)}) + \nabla g_0(\mathbf{h}^{(n)})^T (\mathbf{h} - \mathbf{h}^{(n)})$$

$$= g_0(\mathbf{h}^{(n)}) + \Gamma(\mathbf{h}^{(n)})^T (\mathbf{h} - \mathbf{h}^{(n)}),$$
(38)

and

$$\hat{g}_{1}(\mathbf{h}; \mathbf{h}^{(n)}) \triangleq g_{1}(\mathbf{h}^{(n)}) + \nabla g_{1}(\mathbf{h}^{(n)})^{T}(\mathbf{h} - \mathbf{h}^{(n)})$$

$$= \mathbf{h}^{(n)T}\mathbf{Q}\mathbf{h}^{(n)} + (2\mathbf{Q}\mathbf{h}^{(n)})^{T}(\mathbf{h} - \mathbf{h}^{(n)}),$$
(39)

where  $\mathbf{h}^{(n)}$  is the value of  $\mathbf{h}$  in the n-th iteration. Moreover, the  $M \times 1$  vector  $\Gamma = \frac{\mathrm{d}g_0(\mathbf{h})}{\mathrm{d}\mathbf{h}}$ , and the m-th element of  $\Gamma$  can be calculated as:

$$\Gamma_m = -\sum_{n_1=1}^{N_U} \sum_{k=1}^K \frac{2\kappa B a_{n_1^*,m,k}^* p_{n_1,m,k}^{U*}}{K \ln 2 \times \left( h_m^3 \Delta + h_m \kappa p_{n_1,m,k}^{U*} \right)}.$$
(40)

Thus, the value of  $\mathbf{h}^{(n+1)}$  can be achieved from solving the following series of convex linear-constraint subproblems:

$$\min_{\mathbf{h}} 0 - \hat{g}_0(\mathbf{h}) 
\text{s.t.} (41a) : \chi^2 - \hat{g}_1(\mathbf{h}; \mathbf{h}^{(n)}) \le 0.$$
(41)

Note that, the constrains of (35b) and (35c) in problem (35) will be considered in solving above-mentioned convex sub-problem. The stopping criterion of the iteration can be given by:

$$g_0(\mathbf{h}^{(n+1)}) - g_0(\mathbf{h}^{(n)}) \le \delta, \tag{42}$$

where  $\delta$  is the stopping threshold.

Here, we also use the Lagrangian dual decomposition method to solve the convex problem (41). The Lagrangian function can be given by:

$$L(\mathbf{h}, \psi) = -\hat{q}_0(\mathbf{h}) + \psi(\chi^2 - \hat{q}_1(\mathbf{h})), \tag{43}$$

where  $\psi$  is the Lagrangian multiplier. Hence, the Lagrangian duality function is denoted as:

$$z(\psi) = \inf_{\mathbf{h}} -\hat{g}_0(\mathbf{h}) + \psi(\chi^2 - \hat{g}_1(\mathbf{h})). \tag{44}$$

Then, the Lagrangian duality problem can be formulated as:

$$\max_{\psi} z(\psi)$$
s.t.  $\psi \ge 0$ . (45)

Take the derivative of Eq. (51) against hovering altitude vector **h**, and we have:

$$\frac{\mathrm{d}L(\mathbf{h},\psi)}{\mathrm{d}\mathbf{h}} = -\Gamma(\mathbf{h}^{(n)}) - 2\psi \mathbf{Q}\mathbf{h}^{(n)}.$$
 (46)

For  $\forall m = \{1, 2, \dots, M\}$ , we have:

$$\frac{\mathrm{d}L(h_m)}{\mathrm{d}h_m} = 2\psi \left( \sum_{i=1, i \neq m}^{M} h_i^{(n)} - (M-1)h_m^{(n)} \right) + \sum_{n_1=1}^{N_U} \sum_{k=1}^{K} \frac{2\kappa B a_{n_1^*, m, k}^* p_{n_1, m, k}^{U*}}{K \ln 2 \times \left( h_m^{3(n)} \Delta + h_m^{(n)} \kappa p_{n_1, m, k}^{U*} \right)}, \tag{47}$$

where  $h_m^{(n)}$  is the value of  $h_m$  in the *n*-th iteration. Hence, considering the fact that  $L(h_m)$  is a convex function, we have:

$$h_m^{(n+1)} = \begin{cases} h_{\min}, & \text{if } \frac{dL(h_m)}{dh_m} > 0, \\ h_{\max}, & \text{if } \frac{dL(h_m)}{dh_m} < 0. \end{cases}$$
(48)

Given that the dual function  $z(\psi)$  is not differentiable, the Lagrangian multiplier  $\psi$  can be updated by:

$$\psi^{(n+1)} = [\psi^{(n)} + \beta^{(n)}(\chi^2 - \hat{g}_1(\mathbf{h}^n)]^+, \tag{49}$$

where  $\beta^{(n)}$  is the step size of Lagrangian multiplier.

Then, we can achieve the optimal  $h_{(n+1)}$  for the convex subproblem in (41). Hence, relying on the CCP aided iterative algorithm, given fixed  $\{a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*}\}$ , we obtain the optimal hovering altitude vector represented by h\*. Moreover, for the sake of reducing computational complexity, numerous Boolean optimization algorithms can also be invoked in order to solve the near optimum of h. Thus, the total capacity of UAV networks can be recalculated as  $C_{total}(a_{n_1,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h}^*)$ . However, the pseudo-optimal capacity  $C_{total}(a_{n_1,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}^*)$  is not the final optimal capacity of our proposed uplink resource allocation problem in (12), namely  $C^*_{total}$ . In the following, we will combine the aforementioned two stages in order to search for the optimal network capacity jointly considering the hovering altitude and the subchannel and power control<sup>1</sup>.

# Algorithm 2: Joint Hovering Altitude and Power Control

- 1: Initialize an initial feasible  $\mathbf{h}^{(0)}$ , and a stopping threshold  $\Lambda$ .
- 2: Set iteration indicator i := 0.
- 3: repeat
- Update iteration indicator i := i + 1. 4:
- Obtain  $\{a_{n_1^*,m,k}^*, p_{n_1,m,k}^{U*}\}^{(i)}$  by solving (14) in
- Calculate  $C_{total}^{(i)}(a_{n_1^*,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h})$ . Obtain  $\mathbf{h}^{*(i)}$  by solving (35) in Stage 2. 6:
- Calculate  $C_{total}^{(i)}(a_{n_1^*,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h}^*)$ .
- 9: **until**  $C_{total}^{(i)}(a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}^*)$   $C_{total}^{(i-1)}(a_{n_1,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h}^*) \leq \Lambda$  is satisfied.  $\begin{array}{c} \text{10: Set } C^*_{total} \overset{n_1,m,k}{=} \overset{r}{\sim} n_{1,m,k}, & \mathbf{n} \ ) \leq \Lambda \text{ is satisfied.} \\ \text{10: Set } C^*_{total} \overset{\triangle}{=} C^{(i)}_{total} (a^*_{n^*_1,m,k}, p^{U*}_{n_1,m,k}, \mathbf{h}^*). \\ \text{11: Set } \{a^*_{n^*_1,m,k}, p^{U*}_{n_1,m,k}\} \overset{\triangle}{=} \{a^*_{n^*_1,m,k}, p^{U*}_{n_1,m,k}\}^{(i)}. \\ \text{12: Set } \mathbf{h}^* \overset{\triangle}{=} \mathbf{h}^{*(i)}. \end{array}$

# C. Joint Hovering Altitude and Power Control

1) Two-Stage Joint Resource Allocation: In Section III-A and Section III-B, we have studied the optimization problem of both the power control (Stage 1) and the hovering altitude (Stage 2). In this subsection, we combine these two stages and jointly optimize the hovering altitude and power control scheme. Specifically, in the i-th iteration, the optimal subchannel and power control of  $\{a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*}\}^{(i)}$  can be achieved in Stage 1 based on fixed  $\mathbf{h}^{(i-1)}$ , yielding the total capacity of UAV networks of  $C_{total}^{(i)}(a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}).$ Then, relying on given subchannel and power control of  $\{a_{n_1^*,m,k}^*, p_{n_1,m,k}^{U*}\}^{(i)}$ , in Stage 2, we can obtain the optimal hovering altitude vector  $\mathbf{h}^{*(i)}$  and the pseudo-optimal capacity  $C_{total}^{(i)}(a_{n_1^*,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h}^*)$  in the *i*-th iteration of the two-stage joint resource allocation algorithm. In return, we conduct the optimization in Stage 1 based on the latest  $\mathbf{h}^{*(i)}$  and update the  $\{a_{n_{1}^{*},m,k}^{*},p_{n_{1},m,k}^{U*}\}^{(i+1)}$  as well as  $C_{total}^{(i+1)}(a_{n_{1}^{*},m,k}^{*},p_{n_{1},m,k}^{U*},\mathbf{h})$ . Then, relying on Stage 2, we can obtain the  $\mathbf{h}^{*(i+1)}$  and the pseudo-optimal capacity  $C_{total}^{(i+1)}(a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}^*).$ 

Let  $\Lambda$  be the stopping threshold of our two-stage resource allocation scheme. If the following condition is satisfied:

$$C_{total}^{(i+1)}(a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}^*) - C_{total}^{(i)}(a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}^*) \leq \Lambda,$$
(50)

the final optimal uplink total capacity of M UAV networks can be given by:

$$C_{total}^* \triangleq C_{total}^{(i+1)}(a_{n_*^*,m,k}^*, p_{n_1,m,k}^{U*}, \mathbf{h}^*),$$
 (51)

where the optimal subchannel and power control result is given by  $\{a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*}\} \triangleq \{a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*}\}^{(i+1)}$  as well as the optimal hovering altitude  $\mathbf{h}^* \triangleq \mathbf{h}^{*(i+1)}$ . The procedure of the two-stage joint hovering altitude and power control optimization scheme for UAV networks is summarized in Algorithm. 2.

 $<sup>^1\</sup>text{Hereafter},$  we use  $C_{total}^{(i)}(a_{n_1^*,m,k}^*,p_{n_1,m,k}^{U*},\mathbf{h}^*)$  to represent the pseudo-optimal capacity of the *i*-th two-stage iterative joint resource association for a more clear expression.

**Algorithm 3:** Two-Stage Joint Resource Allocation (TSJ-RA)

```
1: Initialize K, M, N_U, N_S, N_C, N_{ul} and N_{uh}.
 2: Initialize I_{k}^{C}, I_{k}^{S}, R_{h}, R_{l} and P_{\max}.

3: Initialize g_{n_{1},m,k}^{U \to U}, g_{n_{1},m,k}^{U \to C}, g_{n_{1},m,k}^{U \to S}, g_{n_{2},m,k}^{C \to U}, g_{n_{3},m,k}^{S \to U} and p_{n_{2},k}^{C}, p_{n_{3},k}^{S}.
 4: Initialize Lagrangian variables \pmb{\lambda}^{(0)},\,\pmb{\mu}^{(0)},\,\pmb{
u}^{(0)},\,\pmb{\omega}^{(0)} and
     \psi^{(0)}.
 5: Set the maximum number of iteration indicators i_{
m max}
     and j_{\text{max}}. Let i := 0 and j := 0, respectively.
 6: Initialize hovering altitude \mathbf{h}^{(0)} and subchannel-power
 control \{a_{n_1,m,k}, p_{n_1,m,k}^U\}^{(0)}.
7: Calculate C_{total}^{(0)}(\{a_{n_1,m,k}, p_{n_1,m,k}^U\}^{(0)}, \mathbf{h}^{(0)})
 9:
         j := j + 1.
10:
         repeat
            i := i + 1.
11:
            for k=1 to K do
12:
                for m=1 to M do
13:
14:
                   for n_1 = 1 to N_U do
                       i. Update the power allocation p_{n_1,m_k}^U of
15:
                       QoS-sensitive and QoS-tolerant UAV users
                       relying on Eq. (24).
                       ii. Calculate the partial derivative of Eq. (26)
16:
                       and Eq. (27), respectively.
                   end for
17:
                   Update the subchannel allocation a_{n_1,m,k} of
18:
                    the UAV network relying on Eq. (28).
19:
                end for
             end for
20:
             Update Lagrangian variables \lambda, \mu, \nu and \omega relying
21:
             on Eq. (29), Eq. (30), Eq. (31) and Eq. (32),
             respectively.
         until i = i_{\text{max}} or arrive the convergence.
22:
         Get \{a_{n_1,m,k}, p_{n_1,m,k}^U\}^{(j)}.
23:
         Calculate C_{total}^{(j)}(\{a_{n_1,m,k},p_{n_1,m,k}^U\}^{(j)},\mathbf{h}^{(j-1)}).
24:
         Update the hovering altitude of M UAVs relying on
25:
         Algorithm 1.
         Get \mathbf{h}^{(j)}.
26:
         Calculate C_{total}^{(j)}(\{a_{n_1,m,k},p_{n_1,m,k}^U\}^{(j)},\mathbf{h}^{(j)}).
27:
28: until j = j_{\text{max}} or satisfying Eq. (50).
29: Denote C_{total}^* \triangleq C_{total}^{(j)}(\{a_{n_1^*, m, k}^*, p_{n_1, m, k}^{U*}\}^{(j)}, \mathbf{h}^{*(j)}).
```

# IV. ALGORITHM AND ANALYSIS

## A. Algorithm Implementation

In this section, we will elaborate more on the algorithm implementation of our proposed UAV hovering altitude aided resource allocation mechanism described in Section III, namely TSJ-RA as shown in Algorithm 3 for space-air-ground three-tier heterogenous networks. Furthermore, to reduce the computational complexity we propose a heuristic resource allocation algorithm in Algorithm 4, i.e PPC-RA, which has lower computational complexity compared with the exhaustive search algorithm as well as with TSJ-RA.

# **Algorithm 4:** Proportionable Power Constrained Resource Allocation (PPC-RA)

```
1: Initialize K, M, \overline{N_U, N_S, N_C, N_{ul}} and \overline{N_{uh}}.
 2: Initialize I_k^C, I_k^S, R_h, R_l and P_{\max}.

3: Initialize g_{n_1,m,k}^{U \to U}, g_{n_1,m,k}^{U \to C}, g_{n_1,m,k}^{U \to S}, g_{n_2,m,k}^{C \to U}, g_{n_3,m,k}^{S \to U} and p_{n_2,k}^C, p_{n_3,k}^S.
  4: Set the power allocation scale parameter \theta.
  5: for m=1 to M do
               Let the subchannel set be \mathbb{K} = \{1, 2, \dots, K\}.
  7:
               Let UAV user set be \mathbb{N}_U and the QoS-sensitive user
               set be \mathbb{N}_{uh}.
               while \mathbb{N}_{uh} \neq \emptyset, i \in \mathbb{N}_{uh} do
  8:
                    i. Choose i \in \mathbb{N}_{uh}.
  9:
                   ii. Find k^* = \arg\max_{k \in \mathbb{K}} (g_{i,m,k}^{U \to U}/\Delta).

iii. Set a_{i,m,k^*} = 1, and \mathbb{K} := \mathbb{K} - \{k^*\}.

iv. Set p_{i,m,k^*}^U = \theta(g_{i,m,k^*}^{U \to U}/\Delta).

if Eq. (14c) is satisfied then
10:
11:
12:
13:
                          \mathbb{N}_{uh} := \mathbb{N}_{uh} - \{i\}.
14:
                          \mathbb{N}_U := \mathbb{N}_U - \{i\}.
15:
                    end if
16:
17:
               end while
              while \mathbb{K} \neq \emptyset, n_1 \in \mathbb{N}_U do

i. Find \{n_1, k\}^* = \arg\max_{k \in \mathbb{K}, n_1 \in \mathbb{N}_U} (g_{n_1, m, k}^{U \to U}/\Delta).
18:
19:
                    \begin{array}{l} \text{ii. Set } a_{n_1,m,k}\mid_{\{n_1,k\}=\{n_1,k\}^*}=1.\\ \text{iii. Set } a_{n_1,m,k^*}=1, \text{ and } \mathbb{K}:=\mathbb{K}-\{k^*\}.\\ \text{iv. Set } p_{n_1,m,k^*}^U=\theta(g_{n_1,m,k^*}^{U\to U}/\Delta). \end{array}
20:
21:
22:
23:
24: end for
        Update the power allocation scale parameter \theta relying on
         (14a), (14d) and (14e), i.e.
                              \theta = \min \left\{ \frac{P_{\text{max}}^{U} \Delta}{\sum\limits_{k=1}^{K} a_{n_1, m, k} g_{n_1, m, k}^{U \to U}}, \right.
                                        \frac{I_{k}^{C}\Delta}{\sum_{k=1}^{M}\sum_{n=1}^{N_{U}}a_{n_{1},m,k}g_{n_{1},m,k}^{U\to C}g_{n_{1},m,k}^{U\to U}}
```

26: Update the hovering altitude  $\mathbf h$  of M UAVs relying on Algorithm 1.

 $\left. \frac{I_{k}^{S} \Delta}{\sum_{k=0}^{M} \sum_{n_{1}, m, k}^{N_{U}} a_{n_{1}, m, k} g_{n_{1}, m, k}^{U \to S} g_{n_{1}, m, k}^{U \to U}} \right\}.$ 

27: Denote  $C_{total}^* \triangleq C_{total}(a_{n_1,m,k}, p_{n_1,m,k}^U, \mathbf{h}).$ 

# B. Supplementary Analysis

In this subsection, we provide a further explanation for our proposed two-stage resource allocation scheme in the face of both the optimization algorithm as well as the practical system design. As for solving the optimal power control problem in Eq. (24), the transmission power of both QoS-sensitive users and QoS-tolerant users is related to  $\Delta/g_{n_1,m,k}^{U\to U}$  and  $\Theta_{n_1}$ , where  $\Delta/g_{n_1,m,k}^{U\to U}$  represents the interference level from outside UAV networks, while  $\Theta_{n_1}$  measures the interference

level that the UAV users impose to other networks. We can conclude that the large  $\Delta/g_{n_1,m,k}^{U\to U}$  may result in less power assigned to subchannel k. Furthermore,  $\Theta_{n_1}$  also limits the power allocation for the sake of reducing influence to other communication systems. In contrast to the power allocation for QoS-tolerant users,  $\mu_{n_1,m}$  tends to allocate more power for QoS-sensitive users, which yields a high data transmission rate. As for the subchannel allocation based on Eq. (28), due to the Lagrangian multiplier  $\mu_{n_1,m}$  of Eq. (26), more subchannel resources may be assigned to the QoS-sensitive users. Hence, in practical system design, we should to a large degree use the subchannels having less interference from outside UAV networks and also imposing less interference to other networks, and allocate more such 'clean' subchannels and more power to QoS-sensitive users.

Moreover, the optimal hovering altitude of M drones can be obtained by solving a series of reduced convex problems with the aid of CCP algorithm. According to Eq. (47) and Eq. (48), the optimal hovering altitude must be the boundary value of feasible region. To elaborate,  $\sum_{i=1,i\neq m}^{M} h_i - (M-1)h_m$  in Eq. (47) measures the difference between the hovering altitude of the m-th UAV and the average altitude of others. Our algorithm aims to enlarge the gap between the hovering altitude of the m-th UAV and the average altitude of others.

In terms of the computational complexity, Algorithm 3 combines  $j_{\rm max}$  iterations of the update of power control as well as the update of hovering altitude. Specifically, the computational complexity of the update of power control is  $O(i_{\rm max}KMN_U)$ , while the computational complexity of the update of hovering altitude  $O(n_{\rm max}M)$ , where  $i_{\rm max}$  and  $n_{\rm max}$  are the maximum number of iteration for each step, respectively. Therefore, Algorithm 3 has a computational complexity of  $O(j_{\rm max}(i_{\rm max}KMN_U+n_{\rm max}M))$ . By contrast, Algorithm 4 is a low-complexity greedy scheme aiming to preferentially satisfy the QoS-sensitive users, which gets rid of the update of a range of Lagrange dual. It has a much lower computational complexity of  $O(M(N_U^2+(K-N_U)^2)+n_{\rm max}M)$  compared with Algorithm 3.

# V. SIMULATION RESULTS

In our simulation, three kinds of users are located in a  $500 \,\mathrm{m} \times 500 \,\mathrm{m}$  square region.  $N_C = 10$  macrocell users and  $N_S = 10$  satellite users are randomly distributed in the area. Moreover, the coverage radius of each drone is  $50 \,\mathrm{m}$  and UAV users are randomly distributed in each coverage area. The altitude of GEO is  $36000 \,\mathrm{km}$  and only one MBS is considered in the simulation. The carrier frequency is  $2.4 \,\mathrm{GHz}$  and the total number of the subchannel is K = 128, each of which has a bandwidth of  $15 \,\mathrm{kHz}$ . The AWGN power spectrum density is  $-174 \,\mathrm{dBm/Hz}$ . Furthermore, the channel between users and the MBS follows Rayleigh fading. By contrast, the channels between users and UAVs and the GEO follow Rician fading with  $5 \,\mathrm{dB}$  Rician factor. Let the reference-distance unit power gain be  $\kappa = 1.4 \times 10^{-4}$  [44]. The hovering altitude of drones spans from  $200 \,\mathrm{m}$  to  $400 \,\mathrm{m}$ .

In the following, we consider two scenarios with 4 UAVs and 9 UAVs, respectively. Each drone serves  $N_U=4$  UAV

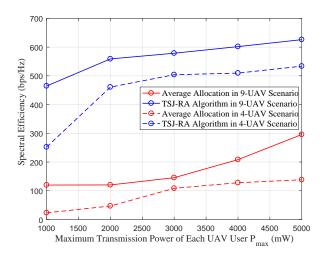


Fig. 2. Spectrum efficiency versus maximum transmission power of UAV users parameterized by different number of UAV networks.

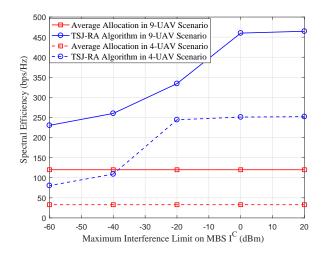


Fig. 3. Spectrum efficiency versus maximum interference limit of the MBS parameterized by different number of UAV networks.

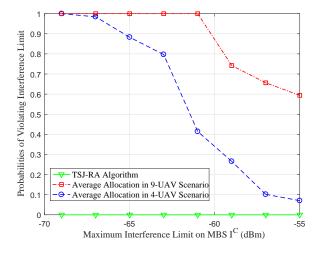


Fig. 4. Probabilities of violating the maximum interference limit on the MBS.

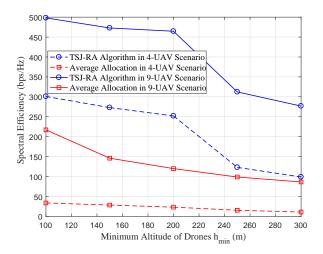


Fig. 5. Spectrum efficiency versus minimum hovering altitude parameterized by different number of UAV networks.

users. In the 4-UAV scenario, there are total 8 QoS-sensitive users and 8 QoS-tolerant users, while there are total 24 QoS-sensitive users and 12 QoS-tolerant users in the 9-UAV scenario. Moreover, the minimum data rate requirement of QoS-sensitive users is  $R_h=30{\rm kbps}$ . We define the spectrum efficiency (SE) of UAV networks to evaluate the effectiveness of our proposed algorithm as:  ${\rm SE}=C_{total}/B$  (bps/Hz).

Fig. 2 shows the impact of the maximum transmission power  $p_{\max}^U$  on the UAV network's SE, where the maximum interference limit of both the MBS and the GEO is 0dBm, i.e.  $I^C = 0$ dBm and  $I^S = 0$ dBm for all subchannels  $k \in \{1, 2, \ldots, K\}$ . It can be observed that our proposed TSJ-RA algorithm outperforms the average resource allocation scheme<sup>2</sup> in terms of the SE. It is because the proposed TSJ-RA algorithm jointly optimizes the altitudes of the drones and transmission power of all users, achieving a decent SE performance and satisfying all the constraints all the time. As a comparison, the comparison algorithm is not aware of system configuration and introduces significant SE loss. Besides, higher SE is obtained with a loose transmission power constraint. Meanwhile, a dense UAV deployment is capable of substantially increasing the network's SE.

Fig. 3 demonstrates the performance of UAV network's SE characterized by the maximum interference limit of the MBS, i.e.  $I^C$ , with respect to  $P^U_{\rm max}=1000{\rm mW}$  and  $I^S=0{\rm dBm}$ . Since the average resource allocation scheme does not rely on the interference limit, the spectrum efficiency is not improved with the increase of MBS's interference limit. As for the TSJ-RA algorithm, a loose interference limit on the MBS yields a high SE of UAV networks to some extent. It is because that with a loose interference limit, UAV users are capable of using higher transmission power, while with a strict interference limit, UAV users have to properly decrease the transmission power to satisfy the preset constraint. Besides, it can seen that when

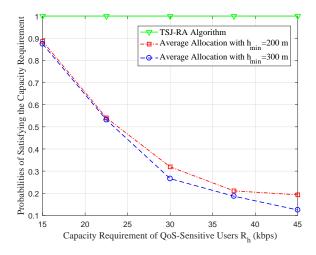


Fig. 6. Probabilities of satisfying capacity requirement of QoS-sensitive users in terms of different minimum hovering altitude of drones.

the interference limit is loose enough, such as  $I^C=0$ dBm for 9-UAV scenario and  $I^C=-20$ dBm for 4-UAV scenario, the SE remains unchanged. It is because with a loose threshold, the pre-set interference constraint can be always satisfied with the given maximum available transmission power. To elaborate a little further, Fig. 4 portrays the probabilities of violating the maximum interference limit on the MBS, which is defined as the ratio of the number of subchannels with interference higher than pre-set maximum limit to the total number of subchannels. We can conclude that our proposed algorithm satisfy the interference limit for all subchannels  $k \in \{1,2,\ldots,K\}$  at all given  $I^C$  values. However, the average algorithm has a high probability of violating the interference limit when the interference requirement is stringent.

In Fig. 5, we evaluate the performance of SE versus different minimum hovering altitudes in different scenarios. It can be seen that a lower minimum hovering altitude is beneficial in terms of improving the SE of the total UAV networks relying on both our proposed TSJ-RA algorithm as well as on the average algorithm. Furthermore, Fig. 6 demonstrates the probabilities of satisfying the pre-set capacity requirement for OoS-sensitive users versus different values of  $R_h$ , which is defined as the ratio of the number of QoSsensitive users with satisfied capacity to the total number of QoS-sensitive users. It can be seen that our proposed algorithm always outperforms the comparison algorithm at all given  $R_h$  values. It is because that our the proposed algorithm considers the capacity requirement of QoS-sensitive users, making the QoS-sensitive users have high priorities to obtain the channels. As a result, the probability of satisfying capacity requirement for QoS-sensitive users equals to 1 all the time. By contrast, the average allocation is not aware of the pre-set capacity constraint. Especially when the capacity requirement is stringent, i.e. 40kbps, only around 10% of QoS-sensitive users can achieve decent capacity higher than the pre-set constraint.

<sup>&</sup>lt;sup>2</sup>In this paper, the average resource allocation scheme means that subchannels as well as power are uniformly allocated to two kinks of users without considering the interference limit of the MBS and the GEO under the constraint of a secure hovering altitude of each drone.

#### VI. CONCLUSIONS

In this paper, we formulated a two-stage joint hovering altitude and power control for UAV networks considering the feasible deployment of drones in the context of a space-airground three-tier heterogeneous network for supporting IoT applications. After appropriate convex relaxation, we used Lagrange dual decomposition and CCP method to provide a near optimal solution for our proposed problem, followed by a low-complexity proportionable power constrained resource allocation algorithm. Finally, extensive simulations were conducted in order to show the performance of our resource allocation mechanism, which yielded an improved UAV network's throughput.

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