

# Kepler-423b: a half-Jupiter mass planet transiting a very old solar-like star<sup>★,★★</sup>

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## ABSTRACT

We report the spectroscopic confirmation of the *Kepler* object of interest KOI-183.01 (Kepler-423b), a half-Jupiter mass planet transiting an old solar-like star every 2.7 days. Our analysis is the first to combine the full *Kepler* photometry (quarters 1–17) with high-precision radial velocity measurements taken with the FIES spectrograph at the Nordic Optical Telescope. We simultaneously modelled the photometric and spectroscopic data-sets using Bayesian approach coupled with Markov chain Monte Carlo sampling. We found that the *Kepler* pre-search data conditioned light curve of Kepler-423 exhibits quarter-to-quarter systematic variations of the transit depth, with a peak-to-peak amplitude of  $\sim 4.3\%$  and seasonal trends reoccurring every four quarters. We attributed these systematics to an incorrect assessment of the quarterly variation of the crowding metric. The host star Kepler-423 is a G4 dwarf with  $M_{\star} = 0.85 \pm 0.04 M_{\odot}$ ,  $R_{\star} = 0.95 \pm 0.04 R_{\odot}$ ,  $T_{\text{eff}} = 5560 \pm 80$  K,  $[M/H] = -0.10 \pm 0.05$  dex, and with an age of  $11 \pm 2$  Gyr. The planet Kepler-423b has a mass of  $M_p = 0.595 \pm 0.081 M_{\text{Jup}}$  and a radius of  $R_p = 1.192 \pm 0.052 R_{\text{Jup}}$ , yielding a planetary bulk density of  $\rho_p = 0.459 \pm 0.083 \text{ g cm}^{-3}$ . The radius of Kepler-423b is consistent with both theoretical models for irradiated coreless giant planets and expectations based on empirical laws. The inclination of the stellar spin axis suggests that the system is aligned along the line of sight. We detected a tentative secondary eclipse of the planet at a  $2\sigma$  confidence level ( $\Delta F_{\text{ec}} = 14.2 \pm 6.6$  ppm) and found that the orbit might have a small non-zero eccentricity of  $0.019^{+0.028}_{-0.014}$ . With a Bond albedo of  $A_B = 0.037 \pm 0.019$ , Kepler-423b is one of the gas-giant planets with the lowest albedo known so far.

**Key words.** planets and satellites: detection – planets and satellites: fundamental parameters – techniques: radial velocities – planets and satellites: individual: Kepler-423b – stars: fundamental parameters – techniques: photometric

## 1. Introduction

We can rightfully argue that space-based transit surveys such as CoRoT (Baglin et al. 2006) and *Kepler* (Borucki et al. 2010)

\* Based on observations obtained with the Nordic Optical Telescope, operated on the island of La Palma jointly by Denmark, Finland, Iceland, Norway, and Sweden, in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias, in time allocated by OPTICON and the Spanish Time Allocation Committee (CAT).

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have revolutionised the field of exoplanetary science. Their high-precision and nearly uninterrupted photometry has opened up the doors to planet parameter spaces that are not easily accessible from the ground, most notably, the Earth-radius planet domain (e.g., Leger et al. 2009; Sanchis-Ojeda et al. 2013; Quintana et al. 2014).

When combined with high-resolution spectroscopy, space-based photometry provides us with the most accurate planetary and stellar parameters, which in turn are essential to investigate planet’s internal structure, migration, and evolution (Rauer et al. 2014). The exquisite photometry from space allows us to detect the eclipse of hot Jupiters even in the visible (e.g., Coughlin & López-Morales 2012; Parviainen et al. 2013). The

eclipse of transiting exoplanets – also known as planet occultation, secondary eclipse, and secondary transit – is a powerful tool for probing their atmospheres, in particular their albedos and brightness temperatures (Winn 2010). The timing and duration of the secondary eclipse, coupled with the timing and duration of the transit, enable us to measure small non-zero eccentricities ( $e \lesssim 0.1$ ) that are not easily detectable with radial velocity (RV) measurements. The eccentricity is an important parameter for the investigation of the star-planet tidal interactions, planet-planet gravitational perturbations, and migration mechanisms of hot Jupiters.

Ever since June 2010 the *Kepler* team has been releasing and updating a list of transiting planet candidates, also known as *Kepler* Objects of Interest (KOI), which as of August 2014 amounts to 7305 objects<sup>1</sup>. Whereas *Kepler* multi-transiting system candidates have a low probability of being false positives (Lissauer et al. 2014; Rowe et al. 2014), the same does not apply for those where a single planet is observed to transit (Santerne et al. 2012; Sliski & Kipping 2014). These require ground-based follow-up observations for validation, such as high-resolution spectroscopy and high-precision RV measurements. The aim of follow-up observations is thus twofold: a) to rule out false-positive scenarios and confirm that the photometric signal is caused by a bona fide transiting planet; b) to characterise the system by exploiting simultaneously both the photometric and spectroscopic data.

In the present paper we report on the confirmation of the *Kepler* transiting planet Kepler-423b (also known as KOI-183.01). We combined the full *Kepler* photometry with high-resolution spectroscopy from FIES at NOT to confirm the planetary nature of the transiting object and derive the system parameters.

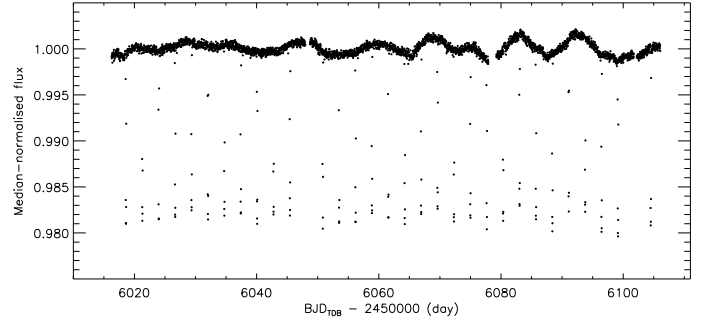
This paper is organised as follows. Section 2 describes the available *Kepler* photometry of Kepler-423, whereas Sect. 3 reports on our spectroscopic follow-up with FIES at NOT. In Sect. 4, we detail how the fundamental parameters of the host star were derived. In Sect. 5, we outline our global Bayesian analysis and report on the quarter-to-quarter instrumental systematics affecting the *Kepler* photometry. Results are discussed in Sect. 6 and conclusions are given in Sect. 7.

## 2. *Kepler* photometry

Kepler-423 – whose main designations, equatorial coordinates, and optical and infrared photometry are listed in Table 2 – was previously identified as a *Kepler* planet-hosting star candidate by Borucki et al. (2011) and Batalha et al. (2013) and assigned the identifier KOI-183.

The *Kepler* photometry<sup>2</sup> of Kepler-423 covers quarters 1–17 (Q<sub>1</sub>–Q<sub>17</sub>), offering four years of nearly continuous observations, from 13 May 2009 to 11 May 2013. The short cadence (SC;  $T_{\text{exp}} = 58.85$  s) data are available for Q<sub>4</sub>–Q<sub>8</sub> and Q<sub>13</sub>, and encompass 190 individual transits. The long cadence (LC;  $T_{\text{exp}} = 1765.46$  s) photometry contains the SC transits and 311 additional LC-only transits observed in Q<sub>1</sub>–Q<sub>3</sub>, Q<sub>9</sub>–Q<sub>12</sub>, and Q<sub>14</sub>–Q<sub>17</sub>.

In this work we used the *Kepler* simple aperture photometry (SAP; Jenkins et al. 2010), as well as the same data processed with the new version of the pre-search data conditioning (PDC) pipeline (Stumpe et al. 2012), which uses a Bayesian maximum



**Fig. 1.** Example section of median-normalised long cadence light curve of Kepler-423. Data are from *Kepler* quarter 13.

**Table 1.** Main identifiers, equatorial coordinates, and optical/infrared magnitudes of the planet-hosting star Kepler-423.

Main identifiers		
KIC	9651668	
KOI ID	183	
GSC2.3 ID	N2JG036249	
USNO-A2 ID	1350-10669726	
2MASS ID	19312537+4623282	
Equatorial coordinates		
RA (J2000)	19 <sup>h</sup> 31 <sup>m</sup> 25 <sup>s</sup> .378	
Dec (J2000)	+46°23′28″.240	
Magnitudes		
Filter ( $\lambda_{\text{eff}}$ )	Mag	Error
<i>g</i> (0.48 $\mu\text{m}$ )	14.729	0.030
<i>r</i> (0.63 $\mu\text{m}$ )	14.225	0.030
<i>i</i> (0.77 $\mu\text{m}$ )	14.102	0.030
<i>z</i> (0.91 $\mu\text{m}$ )	14.028	0.030
<i>J</i> (1.24 $\mu\text{m}$ )	13.142	0.023
<i>H</i> (1.66 $\mu\text{m}$ )	12.847	0.018
<i>Ks</i> (2.16 $\mu\text{m}$ )	12.799	0.031
W1 (3.35 $\mu\text{m}$ )	12.704	0.025
W2 (4.60 $\mu\text{m}$ )	12.771	0.026
W3 (11.56 $\mu\text{m}$ )	12.776 <sup>a</sup>	–
W4 (22.09 $\mu\text{m}$ )	9.536 <sup>a</sup>	–

**Notes.** Equatorial coordinates and optical SDSS-*g*, -*r*, -*i*, -*z* photometry are from the *Kepler* Input Catalogue. Infrared *J*, *H*, *Ks* and W1, W2, W3, W4 data are from the 2MASS (Cutri et al. 2003) and WISE All-Sky Data Release (Wright et al. 2010; Cutri et al. 2012) database, respectively. <sup>(a)</sup> Upper limit.

a posteriori (MAP) approach to remove the majority of instrumental artefacts and systematic trends (Smith et al. 2012). The iterative filtering procedure by Aigrain & Irwin (2004) with a  $5\sigma$  clipping algorithm was applied to both the SAP and the PDC-MAP light curves to identify and reject further outliers. We also performed a visual inspection of the *Kepler* light curves to remove photometric discontinuities across the data gaps that coincide with the quarterly rolls of the spacecraft. The point-to-point scatter estimates for the PDC-MAP SC and LC light curve are 1146 ppm (1.24 mmag) and 292 ppm (0.32 mmag), respectively (Table 5).

Figure 1 shows the median-normalised LC data of Kepler-423 from *Kepler* quarter 13. The  $\sim 1.8\%$ -deep transit signals occurring every 2.7 days are clearly visible, along with a  $\sim 0.5\%$  (peak-to-peak) out-of-transit modulation. Given the spectral type of the planet host star (G4 V; see Sect. 4.1), this variability is likely to be due to magnetic active regions carried around by stellar rotation. Using an algorithm based on the autocorrelation

<sup>1</sup> Available at <http://exoplanetarchive.ipac.caltech.edu/cgi-bin/ExoTables/nph-exotbls?dataset=cumulative>

<sup>2</sup> Available at <http://archive.stsci.edu/kepler>

**Table 2.** FIES radial velocity measurements of Kepler-423.

BJD <sub>TDB</sub> (− 2 450 000)	RV km s <sup>−1</sup>	$\sigma_{RV}$ km s <sup>−1</sup>	Bisector km s <sup>−1</sup>	S/N/pixel @5500 Å
6470.576529	−3.095	0.040	0.045	13
6472.450721	−3.099	0.037	0.001	11
6472.685581	−3.141	0.044	0.049	10
6473.557333	−3.024	0.039	−0.010	15
6473.687627	−3.024	0.037	−0.005	16
6485.482378	−3.026	0.022	0.018	21
6485.632534	−3.039	0.028	0.026	18
6486.453320	−3.122	0.025	0.019	19
6486.635293	−3.117	0.028	0.018	18
6487.476759	−2.958	0.021	0.002	22
6487.640452	−2.927	0.027	−0.002	18
6544.396913	−2.955	0.030	0.032	13

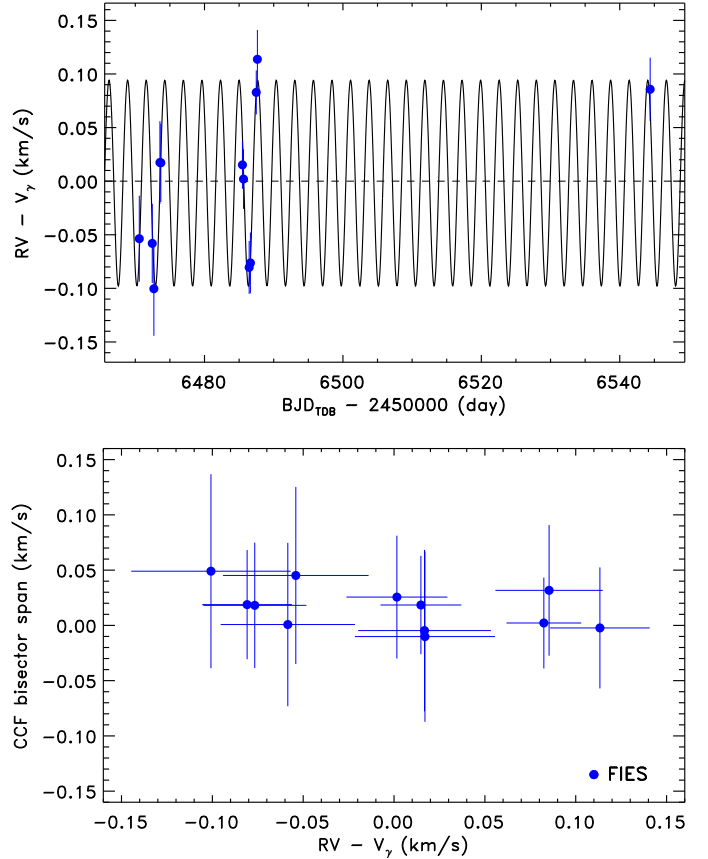
**Notes.** The barycentric Julian dates are provided in barycentric dynamical time (BJD<sub>TDB</sub>). The CCF bisector spans and the S/N per pixel at 5500 Å are listed in the last two columns.

function of the Q<sub>3</sub>–Q<sub>14</sub> time-series, McQuillan et al. (2013) found a stellar rotation period of  $P_{\text{rot}} = 22.047 \pm 0.121$  days.

### 3. High-resolution spectroscopy

The spectroscopic follow-up of Kepler-423 was performed with the Fibre-fed Échelle Spectrograph (FIES; Frandsen & Lindberg 1999; Telting et al. 2014) mounted at the 2.56-m Nordic Optical Telescope (NOT) of Roque de los Muchachos Observatory (La Palma, Spain). The observations were carried out between June and September 2013, under OPTICON and CAT observing programmes 2013A025 and 79-NOT14/13A, respectively. We used the 1.3'' *high-res* fibre, which provides, in conjunction with a 50- $\mu\text{m}$  slit at the fibre exit, a resolving power of  $R = 67\,000$  in the spectral range 3600–7400 Å. Three consecutive exposures of 1200 s were taken per epoch observation to remove cosmic ray hits. Following the observing strategy described in Buchhave et al. (2010), we traced the RV drift of the instrument by acquiring long-exposed ( $T_{\text{exp}} = 15$  s) ThAr spectra right before and after each epoch observation. The data were reduced using a customised IDL software suite, which includes bias subtraction, flat fielding, order tracing and extraction, and wavelength calibration. RV measurements were derived via multi-order cross-correlations technique with the RV standard star HD 182572 – observed with the same instrument set-up as the target object – and for which we adopted an heliocentric RV of  $-100.350$  km s<sup>−1</sup>, as measured by Udry et al. (1999).

The FIES RV measurements are listed in Table 2 along with the observation barycentric Julian dates in barycentric dynamical time (BJD<sub>TDB</sub>, see Eastman et al. 2010), the cross-correlation function (CCF) bisector spans, and the signal-to-noise ratios (S/N) per pixel at 5500 Å. The upper panel of Fig. 2 shows the FIES RVs of Kepler-423 and the Keplerian fit to the data – as obtained from the global analysis described in Sect. 5 – whereas the lower panel displays the CCF bisector spans plotted against the RV measurements, assuming that the error bars of the former are twice those of the latter. We followed the method described in Loyd & France (2014) to account for the uncertainties of our measurements and found that the probability that uncorrelated random datasets can reproduce the observed arrangement of points (null hypothesis) is about 50%. The lack of significant linear correlation between the CCF bisector spans and the RVs indicates that most likely the Doppler shifts observed in



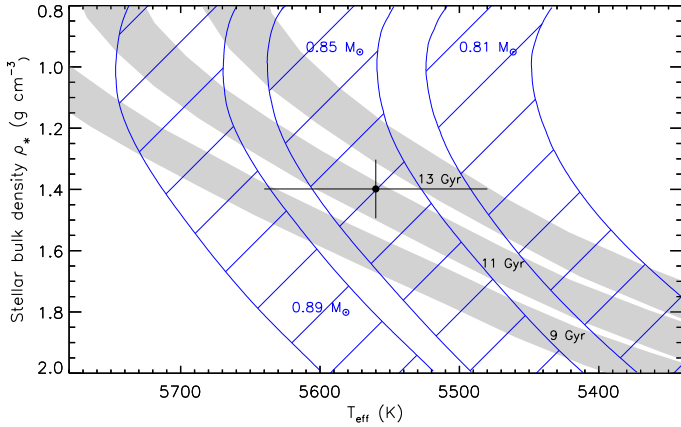
**Fig. 2.** Upper panel: FIES radial velocities of Kepler-423 – after subtracting the systemic velocity  $V_\gamma$  – versus BJD<sub>TDB</sub> and Keplerian fit to the data. Lower panel: bisector spans of the FIES cross-correlation functions versus RV measurements, after subtracting the systemic velocity  $V_\gamma$ . Error bars in the CCF bisector spans are taken to be twice the uncertainties in the RV data.

Kepler-423 are induced by the orbital motion of the companion rather than stellar activity or a blended eclipsing binary (see, e.g., Queloz et al. 2001).

## 4. Properties of the host star

### 4.1. Photospheric parameters

We derived the fundamental photospheric parameters of the host star Kepler-423 using the co-added FIES spectrum, which has a S/N of about 60 per pixel at 5500 Å. Two independent analyses were performed. The first method compares the co-added FIES spectrum with a grid of theoretical models from Castelli & Kurucz (2004), Coelho et al. (2005), and Gustafsson et al. (2008), using spectral features that are sensitive to different photospheric parameters. We adopted the calibration equations for Sun-like dwarf stars from Bruntt et al. (2010) and Doyle et al. (2014) to determine the microturbulent  $v_{\text{micro}}$  and macroturbulent  $v_{\text{macro}}$  velocities, respectively. The projected rotational velocity  $v \sin i_*$  was measured by fitting the profile of several clean and unblended metal lines. The second method relies on the use of the spectral analysis package SME 2.1, which calculates synthetic spectra of stars and fits them to observed high-resolution spectra (Valenti & Piskunov 1996; Valenti & Fischer 2005). It uses a non-linear least squares algorithm to solve for the model atmosphere parameters. The two analysis provided consistent



**Fig. 3.** Modified Hertzsprung-Russell diagram showing the stellar bulk density versus effective temperature. The position of Kepler-423 is overlotted on theoretical evolutionary tracks and isochrones from the Pisa Stellar Evolution Data Base for low-mass stars. The blue hatched areas represent different masses (0.81, 0.85, and 0.89  $M_{\odot}$  from right to left), while the greys represent the age isochrones (9, 11, and 13 Gyr from bottom to top), computed for an initial metal content between  $Z = 0.012$  and  $Z = 0.014$ .

results well within the errors bars. The final adopted values are  $T_{\text{eff}} = 5560 \pm 80$  K,  $\log g = 4.44 \pm 0.10$  ( $\log_{10} \text{cm s}^{-2}$ ),  $[\text{M}/\text{H}] = -0.10 \pm 0.05$  dex,  $v_{\text{micro}} = 1.0 \pm 0.1$  km s $^{-1}$ ,  $v_{\text{macro}} = 2.8 \pm 0.4$  km s $^{-1}$ , and  $v \sin i_{\star} = 2.5 \pm 0.5$  km s $^{-1}$ . Using the [Straizys & Kuriliene \(1981\)](#) calibration scale for dwarf stars, the effective temperature of Kepler-423 translates to a G4 V spectral type.

#### 4.2. Stellar mass, radius, and age

Stellar mass, radius, and age were determined using the effective temperature  $T_{\text{eff}}$  and metallicity  $[\text{M}/\text{H}]$ , as derived from the spectral analysis (Sect. 4.1), along with the stellar bulk density  $\rho_{\star}$ , as obtained from the modelling of the transit light curve (Sect. 5). We compared the position of Kepler-423 on a  $\rho_{\star}$ -versus- $T_{\text{eff}}$  diagram with a grid of ad hoc evolutionary tracks (Fig. 3).

We generated stellar models using an updated version of the *FRANEC* code ([Degl'Innocenti et al. 2008](#); [Tognelli et al. 2011](#)) and adopting the same input physics and parameters as those used in the Pisa Stellar Evolution Data Base for low-mass stars<sup>3</sup> (see, e.g., [Dell'Omodarme et al. 2012](#), for a detailed description). To account for the current surface metallicity of Kepler-423 ( $[\text{M}/\text{H}] = -0.10 \pm 0.05$  dex) and microscopic diffusion of heavy elements towards the centre of the star, we computed evolutionary tracks assuming an initial metal content of  $Z = 0.010$ ,  $Z = 0.011$ ,  $Z = 0.012$ ,  $Z = 0.013$ ,  $Z = 0.014$ , and  $Z = 0.015$ . The corresponding initial helium abundances, i.e.,  $Y = 0.268$ ,  $0.271$ ,  $0.273$ ,  $0.275$ ,  $0.277$ , and  $0.279$ , were determined assuming a helium-to-metal enrichment ratio  $\Delta Y/\Delta Z = 2$  ([Jimenez et al. 2003](#); [Casagrande 2007](#); [Gennaro et al. 2010](#)) and a cosmological  $^4\text{He}$  abundance  $Y_p = 0.2485$  ([Cyburt 2004](#); [Peimbert et al. 2007a,b](#)). For each chemical composition, we generated a very fine grid of evolutionary tracks in the mass domain  $M_{\star} = 0.70$ – $1.10 M_{\odot}$ , with step of  $\Delta M_{\star} = 0.01 M_{\odot}$ , leading to a total of 246 stellar tracks.

We found that evolutionary tracks with initial metal content between  $Z = 0.012$  and  $Z = 0.014$  have to be used to reproduce the current photospheric metallicity of Kepler-423. We derived

a mass of  $M_{\star} = 0.85 \pm 0.04 M_{\odot}$  a radius of  $R_{\star} = 0.95 \pm 0.04 R_{\odot}$  and an age of  $t = 11 \pm 2$  Gyr (Table 5). Mass and radius imply a surface gravity of  $\log g = 4.41 \pm 0.04$  ( $\log_{10} \text{cm s}^{-2}$ ), which agrees with the spectroscopically derived value  $\log g = 4.44 \pm 0.10$  ( $\log_{10} \text{cm s}^{-2}$ ).

Using pre-main sequence (PMS) evolutionary tracks would lead to consistent results in terms of stellar mass and radius, but would also yield an age of  $25 \pm 5$  Myr. Given the relatively rapid evolutionary time-scale of PMS stars, we note that the likelihood of finding Kepler-423 still contracting towards the zero-age main sequence (ZAMS) is about 600 times lower than the probability for the star to be found in the post ZAMS phase. Moreover, such a young scenario is at odds with: *a*) the distance from the galactic plane, which amounts to  $166 \pm 17$  pc (given the spectroscopic distance of  $725 \pm 75$  pc – see below – and galactic latitude of  $+12.92^{\circ}$ ); *b*) the relatively long rotation period of the star ( $P_{\text{rot}} = 22.047 \pm 0.121$  days); *c*) the absence of high magnetic activity level (the peak-to-peak photometric variation is  $\sim 0.5\%$ ); *d*) the lack of detectable Li I  $\lambda 6708 \text{ \AA}$  absorption line in the co-added FIES spectrum. Short rotation period ( $P_{\text{rot}} \lesssim 5$  days), coupled with high magnetic activity and strong Li I  $\lambda 6708 \text{ \AA}$  absorption line ( $EW_{\text{Li}} \gtrsim 300 \text{ m\AA}$ ), are usually regarded as youth indicators in PMS low-mass stars (see, e.g., [Marilli et al. 2007](#); [Gandolfi et al. 2008](#)).

#### 4.3. Interstellar extinction and distance

We followed the method described in [Gandolfi et al. \(2008\)](#) to derive the interstellar extinction  $A_v$  and spectroscopic distance  $d$  of the system. We simultaneously fitted the available optical and infrared colours listed in Table 2 with synthetic theoretical magnitudes obtained from the *NextGen* model spectrum with the same photospheric parameters as the star ([Hauschildt et al. 1999](#)). We excluded the *W3* and *W4* WISE magnitudes, owing to the poor photometry ([Cutri et al. 2012](#)). Assuming a normal extinction ( $R_v = 3.1$ ) and a black body emission at the star's effective temperature and radius, we found that Kepler-423 suffers a negligible interstellar extinction of  $A_v = 0.044 \pm 0.044$  mag and that its distance is  $d = 725 \pm 75$  pc (Table 5).

## 5. Bayesian and MCMC global analysis

### 5.1. Approach

We estimated the system parameters, i.e., stellar, planetary, and orbital parameters for which inference can be made based on photometry and RVs, using a Bayesian approach where the photometric and RV data are modelled simultaneously, similarly to the work described in [Gandolfi et al. \(2013\)](#) and [Parviainen et al. \(2014\)](#). The model describes the primary transits, secondary eclipses, and RV variations. The significance of a possible secondary eclipse signal (Sect. 6.2) was assessed separately using a method based on Bayesian model comparison ([Parviainen et al. 2013](#)).

We obtained an estimate of the model posterior distribution using the Markov chain Monte Carlo (MCMC) technique. The sampling was carried out using *emcee*<sup>4</sup> ([Foreman-Mackey et al. 2012](#)), a Python implementation of the Affine Invariant Markov chain Monte Carlo sampler ([Goodman & Weare 2010](#)). We used *PyDE*<sup>5</sup>, a Python implementation of the differential evolution algorithm for global optimisation, to generate an initial population

<sup>4</sup> Available at [github.com/dfm/emcee](http://github.com/dfm/emcee)

<sup>5</sup> Available at [github.com/hpparvi/PyDE](http://github.com/hpparvi/PyDE)

<sup>3</sup> Available at <http://astro.df.unipi.it/stellar-models/>

of parameter vectors clumped close to the global posterior maximum used to initialise the MCMC sampling. The sampling was carried out with 500 simultaneous walkers (chains). The sampler was first run iteratively through a burn-in period consisting of 20 runs of 500 steps each, after which the walkers had converged to sample the posterior distribution. The chains were considered to have converged to sample the posterior distribution after the ensemble properties of the chains did not change during several sets of 500 iterations, and the results from different walker subsets agreed with each other. The final sample consists of 1500 iterations with a thinning factor of 50 (chosen based on the average parameter autocorrelation lengths to ensure that we had independent samples), leading to 15 000 independent posterior samples.

## 5.2. Dataset

The dataset consists of the 12 FIES RVs (Sect. 3), subsets of the SC and LC data for the transit modelling, and subsets of the LC data for the secondary eclipse modelling.

The photometric data for the transit modelling included 12 h of data around each transit, where each segment was detrended using a second-order polynomial fitted to the out-of-transit points. We preferred short time cadence light curves when available, and excluded the LC transits for which SC data was available. The final SC and LC transit light curves contain about 138 400 and 12 100 points, respectively. We chose not to use PDC-MAP data because of the issues in the crowding metric correction applied by the pipeline, but used the PDC-MAP cotrended fluxes instead (see Sect. 5.4).

The eclipse model was evaluated using LC data alone. We included about 18 h of data centred on half-phase from each individual orbit – enough to allow for eccentricities up to 0.2 – and did not detrend the individual data segments (we used Gaussian processes to model the baseline instead). We rejected 69 subsets of LC data because of clear systematics and performed the secondary eclipse modelling using 447 LC segments.

## 5.3. Log-posterior probability density and parametrisation

The non-normalised log-posterior probability density is described as

$$\begin{aligned} \log P(\theta|D) = & \log P(\theta) \\ & + \log P(F_{\text{SC}}|\theta) + \log P(F_{\text{LC}}|\theta) \\ & + \log P(F_{\text{EC}}|\theta) \\ & + \log P(RV|\theta), \end{aligned} \quad (1)$$

where  $F_{\text{SC}}$  and  $F_{\text{LC}}$  are the short- and long-cadence photometric data for the primary transit,  $F_{\text{EC}}$  is the long cadence photometric data for the secondary eclipse,  $RV$  corresponds to the FIES RV data,  $\theta$  is the parameter vector containing the parameters listed in Table 3, and  $D$  the combined dataset. The first term in the right-hand side of Eq. (1), namely  $\log P(\theta)$ , is the logarithm of the joint prior probability, i.e., the product of individual parameter prior probabilities, and the four remaining terms are the likelihoods for the RV and light curve data.

The likelihoods for the combined RV and photometric dataset  $D$  follow the basic form for a likelihood assuming independent identically distributed errors from normal distribution

$$\begin{aligned} \log P(D|\theta) = & -\frac{N_{\text{D}}}{2} \log(2\pi) - N_{\text{D}} \log(\sigma_{\text{D}}) \\ & - \frac{1}{2} \sum_{i=1}^{N_{\text{D}}} \left( \frac{D_i - M(t_i, \theta)}{\sigma_{\text{D}}} \right)^2, \end{aligned} \quad (2)$$

**Table 3.** Model parametrisation used in the basic system characterisation.

Model parameter	Notation
Planetary orbital period	$P_{\text{orb}}$
Planetary mid-transit epoch	$T_0$
Bulk stellar density	$\rho_{\star}$
Impact parameter	$b$
Orbit eccentricity	$e$
Argument of periastron	$\omega$
Planet-to-star area ratio	$R_{\text{p}}^2/R_{\star}^2$
Planet-to-star surface brightness ratio <sup>a</sup>	$f$
Linear limb-darkening coefficient	$u_1$
Quadratic limb-darkening coefficient	$u_2$
Kepler LC data scatter	$\sigma_{\text{LC}}$
Kepler SC data scatter	$\sigma_{\text{SC}}$
Systemic radial velocity	$V_{\gamma}$
Radial velocity semi-amplitude	$K$
Quarterly crowding metric	$C_i$ , with $i \in [1..17]$

**Notes.** <sup>(a)</sup> We defined the planet-to-star surface brightness ratio  $f$  as the flux ratio per projected unit area (instead of as eclipse depth). The eclipse depth is thus  $\Delta F_{\text{ec}} = f \times R_{\text{p}}^2/R_{\star}^2$ .

where  $D_i$  is the single observed data point  $i$ ,  $M(t_i, \theta)$  the model explaining the data,  $t_i$  the centre time for a data point  $i$ ,  $N_{\text{D}}$  the number of data points, and  $\sigma_{\text{D}}$  the standard deviation of the error distribution (see, e.g., Gregory 2005).

The likelihood for the secondary eclipse data was calculated using Gaussian processes (GPs) to reduce our sensitivity to systematic noise (Rasmussen & Williams 2006; Gibson et al. 2012). We modelled the residuals as a GP with an exponential kernel, with the kernel hyper-parameters fixed to values optimised to the data.

The RV model follows from equation

$$RV = V_{\gamma} + K[\cos(\omega + \nu) + e \cos \omega], \quad (3)$$

where  $V_{\gamma}$  is the systemic velocity,  $K$  the RV semi-amplitude,  $\omega$  the argument of periastron,  $\nu$  the true anomaly, and  $e$  the eccentricity.

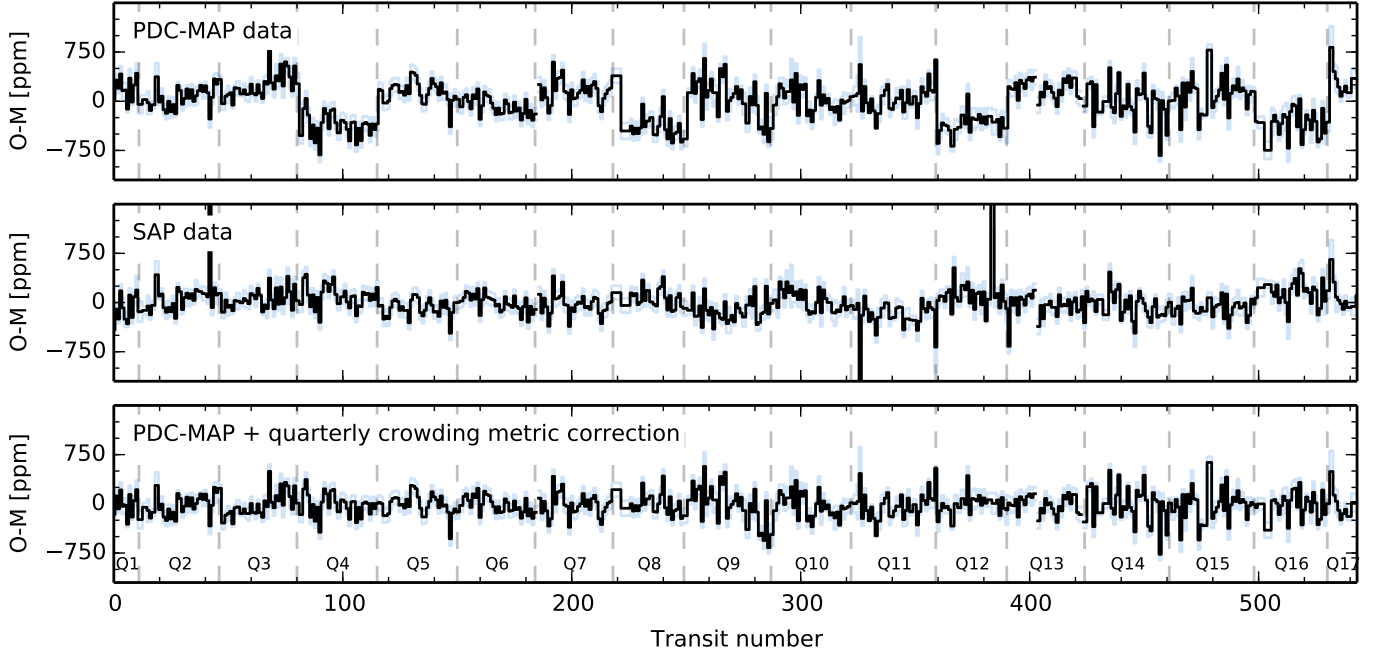
The transit model used PyTransit, an optimised implementation of the (Giménez 2006) transit shape model<sup>6</sup>. The long-cadence and planetary eclipse models were super-sampled using 8 subsamples per LC exposure to reduce the effects from the extended integration time (Kipping 2010).

We defined the planet-to-star surface brightness ratio  $f$  as the flux ratio per projected unit area (instead of as eclipse depth). The eclipse depth is thus  $\Delta F_{\text{ec}} = f \times R_{\text{p}}^2/R_{\star}^2$ .

## 5.4. Systematic effects in the Kepler photometric data: quarterly transit depth variation

Van Eylen et al. (2013) recently observed systematic depth variations in the *Kepler* transit light curves of HAT-P-7, which were found to be related to the 90-degree rolling of the spacecraft occurring every quarter (i.e., every ~90 days). They proposed four possible causes for the variations, i.e., unaccounted-for light contamination, too small aperture photometric masks, instrumental non-linearities, and colour-dependence in the pixel response function, but noted that it is not possible to choose the most likely cause based on *Kepler* data alone.

<sup>6</sup> Available at [github.com/hpparvi/PyTransit](https://github.com/hpparvi/PyTransit)



**Fig. 4.** *Upper panel:* average, observed–modelled ( $O - M$ ) flux residual of the photometric points encompassing the second ( $T_2$ ) and third transit contact ( $T_3$ ) as a function of the transit numbers for the PDC-MAP data, assuming that the *Kepler* contamination metric has been properly estimated. The light blue lines show the standard error of the mean for each transit. The beginning of each *Kepler* quarter is marked with dashed grey vertical lines. *Middle panel:* as in the upper panel, but for the SAP data. *Lower panel:* same as before, but for the PDC-MAP cotrended data, following our quarterly crowding metric correction constrained by an informative prior (see text for more details).

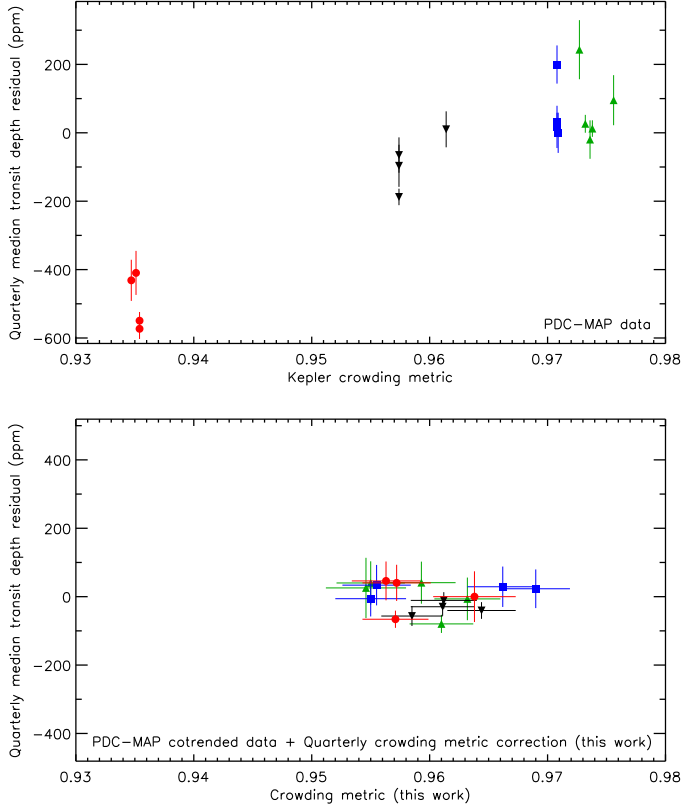
We searched for similar instrument systematics in the *Kepler* light curve of Kepler-423 by subtracting, from each PDC-MAP and SAP transit light curve, the corresponding best-fitting transit model obtained using simultaneously all the *Kepler* segments (Sect. 5.2). The upper panel of Fig. 4 displays the transit depth residual as a function of the transit number for the PDC-MAP data. We found a significant ( $\sim 16\sigma$ ) quarter-to-quarter systematic variation of the transit depth, with a seasonal trend reoccurring every four quarters and with the  $Q_4$ ,  $Q_8$ ,  $Q_{12}$ , and  $Q_{16}$  data yielding the deepest transit light curves. The peak-to-peak amplitude is about 800 parts per million (ppm), which corresponds to  $\sim 4.3\%$  of the mean transit depth.

Intriguingly, there is no significant ( $\sim 2\sigma$ ) quarter-to-quarter variation of the transit depth in the SAP data, as shown in the middle panel of Fig. 4. The SAP residuals exhibit, however, intra-quarter systematic trends that might result from the motion of the target within its photometric aperture due to telescope focus variation, differential velocity aberration, and spacecraft pointing (Kinemuchi et al. 2012). The PDC-MAP data are corrected for these effects using cotrending basic vectors generated from a suitable ensemble of highly-correlated light curves on the same channel (Stumpe et al. 2012). Because different behaviours of the *Kepler* detectors would most likely cause systematics visible in both PDC-MAP and SAP data, we can safely exclude the channel-to-channel non-linearity difference as the source of the quarter-to-quarter transit depth variation. Moreover, the *Kepler* CCD non-linearity is reported to be 3% over the whole dynamic range (Caldwell et al. 2010) and the systematic variations are at least one order of magnitude larger than the expected non-linearity effect at the transit depth signal.

This leaves the crowding metric correction performed by the PDC-MAP pipeline as the most plausible explanation. The crowding metric is defined as the fraction of light in the photometric aperture arising from the target star. Since apertures are

defined for each quarter – to account for the redistribution of target flux over a new CCD occurring at each roll of the spacecraft – the crowding metrics are computed quarterly for each target. The excess flux due to crowding within the photometric aperture is automatically removed by the PDC-MAP pipeline from the SAP light curve. The upper panel of Fig. 5 shows the quarterly median transit depth residuals – as derived from the PDC-MAP light curve – plotted against the crowding metrics – as extracted from the header keyword CROWDSAP listed in the *Kepler* data (Table 4, second column). We found a significant correlation between the two quantities, with a null hypothesis probability of only 0.15%. The lack of significant quarter-to-quarter transit depth variation in the SAP data (Fig. 4, middle panel) suggests that the crowding metric variation among quarters is most likely overestimated, i.e., the excess flux arising from nearby contaminant sources is very likely to be almost constant from quarter to quarter.

Kinemuchi et al. (2012) quoted the completeness of the *Kepler* input catalogue (KIC) as possible source of contamination error. However, from a comparison with the POSS II image centred around Kepler-423, we noted that all nearby faint stars up to *Kepler* magnitude  $K_p < 20$  mag are included in the KIC. We therefore considered the *Kepler* crowding metric values to be generally correct, but not their variations among quarters. The crowding metric correction is the last data processing step performed by the PDC-MAP pipeline on the cotrended *Kepler* light curve (Smith et al. 2012; Stumpe et al. 2012). To account for the quarterly systematics, we carried out the parameter estimation with the PDC-MAP cotrended data. The latter were obtained by removing the *Kepler* crowding metric correction from the pipeline-generated PDC-MAP data. The parameter estimation was then performed including a per-quarter contamination metric to the model with informative prior based on the average crowding metric derived by the *Kepler* team (Fig. 4, lower



**Fig. 5.** *Upper panel:* quarterly median transit depth residuals, as derived from the *Kepler* PDC-MAP light curve of Kepler-423, against *Kepler* crowding metrics. Error bars are the median absolute deviations. Quarters sharing the same *Kepler* observing season are plotted with the same symbol and colour: Q<sub>1</sub>, Q<sub>5</sub>, Q<sub>9</sub>, Q<sub>13</sub>, and Q<sub>17</sub> (upward green triangles); Q<sub>2</sub>, Q<sub>6</sub>, Q<sub>10</sub>, and Q<sub>14</sub> (downward black triangles); Q<sub>3</sub>, Q<sub>7</sub>, Q<sub>11</sub>, and Q<sub>15</sub> (blue squares); Q<sub>4</sub>, Q<sub>8</sub>, Q<sub>12</sub>, and Q<sub>16</sub> (red circles). *Lower panel:* same as before, but for the PDC-MAP cotrended data, following our quarterly crowding metric correction constrained by an informative prior. The x-axis reports our estimates of the quarterly crowding metrics (Table 4).

panel). Thus, our approach also yielded fitted estimates for the quarterly crowding factor.

### 5.5. Priors

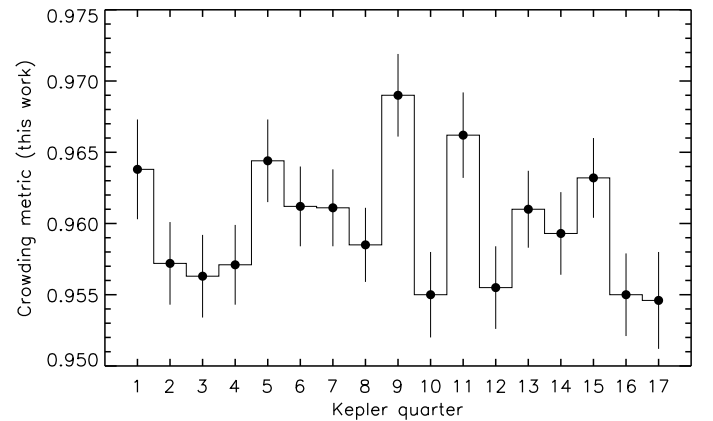
The final joint model has 31 free parameters, listed in Table 3. We used uninformative priors (uniform) on all parameters except the 17 crowding metrics, for which we used normal priors centred on 0.96 with a standard deviation of 0.01, based on the crowding metrics estimated by the *Kepler* team. While reducing the objectivity of the analysis, setting an informative prior on the quarterly crowding metrics was a necessary compromise, since the shape of the transit light curve alone cannot constrain totally free contamination.

We considered two cases for the secondary eclipse. For model comparison purposes, we carried out the sampling for a model with a delta prior forcing the planet-to-star surface brightness ratio to zero (no-eclipse model), and with a uniform prior based on simple modelling of expected flux ratios. We estimated the allowed range for the planet-to-star surface brightness ratio using a Monte Carlo approach by calculating the flux ratios for 50 000 samples of stellar effective temperature, semi-major axis, heat redistribution factor, and Bond albedo. The effective temperature and semi-major axis distributions are based

**Table 4.** *Kepler* quarterly crowding metrics (second column), and our estimates and uncertainties (last two columns).

Quarter (Q <sub>i</sub> )	<i>Kepler</i> crowding metric	Derived crowding metric (C <sub>i</sub> )	σ <sub>C<sub>i</sub></sub>
Q <sub>1</sub>	0.9756	0.9638	0.0035
Q <sub>2</sub>	0.9614	0.9572	0.0029
Q <sub>3</sub>	0.9708	0.9563	0.0029
Q <sub>4</sub>	0.9354	0.9571	0.0028
Q <sub>5</sub>	0.9738	0.9644	0.0029
Q <sub>6</sub>	0.9574	0.9612	0.0028
Q <sub>7</sub>	0.9708	0.9611	0.0027
Q <sub>8</sub>	0.9354	0.9585	0.0026
Q <sub>9</sub>	0.9736	0.9690	0.0029
Q <sub>10</sub>	0.9574	0.9550	0.0030
Q <sub>11</sub>	0.9709	0.9662	0.0030
Q <sub>12</sub>	0.9347	0.9555	0.0029
Q <sub>13</sub>	0.9732	0.9610	0.0027
Q <sub>14</sub>	0.9574	0.9593	0.0029
Q <sub>15</sub>	0.9708	0.9632	0.0028
Q <sub>16</sub>	0.9351	0.9550	0.0029
Q <sub>17</sub>	0.9727	0.9546	0.0034

**Notes.** Our estimates of the crowding metrics with their 1σ uncertainties from the MCMC posterior sampling are listed in the last two columns.



**Fig. 6.** Quarterly crowding metric estimates rederived from our analysis and their 1σ uncertainties (Table 4) versus quarter numbers. The posterior crowding estimates are a product of transit modelling using the PDC-MAP cotrended data and informative priors based on the *Kepler* crowding estimates.

on estimated values (Table 5), the heat distribution factor values are drawn from uniform distribution  $U(1/4, 2/3)$  and the Bond albedo values from uniform distribution  $U(0, 0.5)$ . The resulting distribution is nearly uniform, and extends from 0.0 to 0.012 (99th percentile), and thus we decided to set a uniform prior  $U(0, 0.012)$  on the surface brightness ratio.

## 6. Results and discussions

We list our results in Table 5. The system's parameter estimates were taken to be the median values of the posterior probability distributions. Error bars were defined at the 68% confidence limit. We show the phase-folded transit and RV curves along with the fitted models in Figs. 7 and 8, respectively.

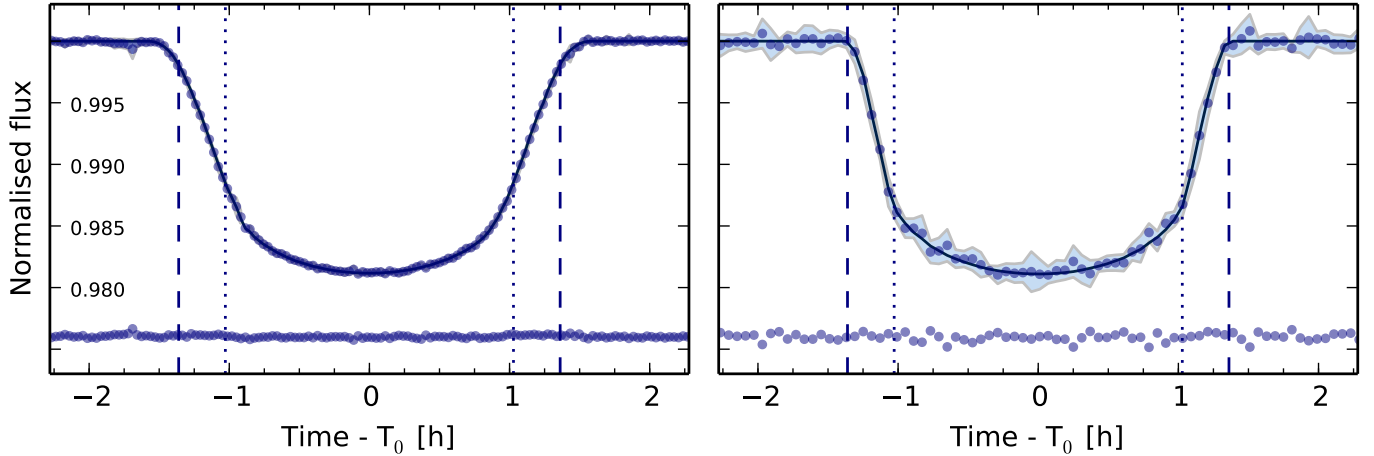
The quarterly correction estimates, along with their 1σ uncertainties, are listed in Table 4. For the sake of illustration, they are also plotted in Fig. 6. We found no significant correlation

**Table 5.** Kepler-423 system parameters.

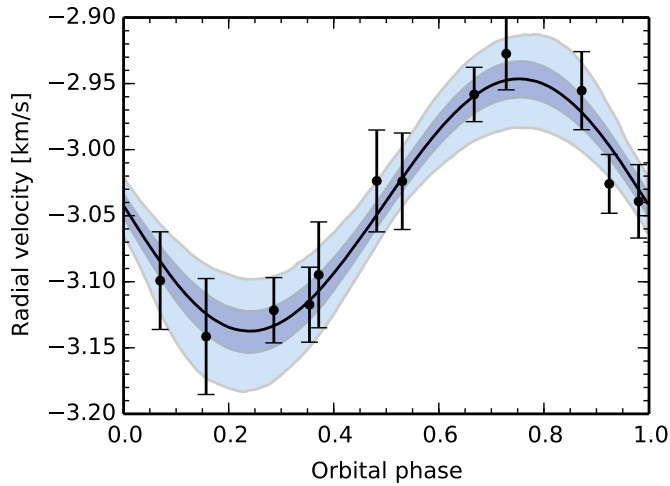
Model parameters	
Planet orbital period $P_{\text{orb}}$ (day)	$2.68432850 \pm 0.00000007$
Planetary mid-transit epoch <sup>a</sup> $T_0$ (BJD <sub>TDB</sub> -2 450 000 day)	$4966.35480997 \pm 0.00002124$
Planet-to-star area ratio $R_p^2/R_\star^2$	$0.015872 \pm 0.000062$
Planet-to-star surface brightness ratio $f$	$(8.93 \pm 4.13) \times 10^{-4}$
Impact parameter $b$	$0.3006 \pm 0.0100$
Bulk stellar density $\rho_\star$ ( $\text{g cm}^{-3}$ )	$1.398 \pm 0.096$
Linear limb-darkening coefficient $u_1$	$0.4650 \pm 0.0100$
Quadratic limb-darkening coefficient $u_2$	$0.1518 \pm 0.0228$
Radial velocity semi-amplitude $K$ ( $\text{km s}^{-1}$ )	$0.0967 \pm 0.0118$
Systemic radial velocity $V_\gamma$ ( $\text{km s}^{-1}$ )	$-3.0410 \pm 0.0081$
Orbit eccentricity $e$	$0.019^{+0.028}_{-0.014}$
Argument of periastron $\omega$ (degree)	$120.26^{+77.01}_{-33.88}$
Kepler LC data scatter $\sigma_{\text{LC}}$ (ppm)	$292.2 \pm 2.4$
Kepler SC data scatter $\sigma_{\text{SC}}$ (ppm)	$1145.7 \pm 2.1$
Derived parameters	
Planet-to-star radius ratio $R_p/R_\star$	$0.12599 \pm 0.00024$
Planetary eclipse depth $\Delta F_{\text{ec}}$ (ppm)	$14.2 \pm 6.6$
Scaled semi-major axis of the planetary orbit $a_p/R_\star$	$8.106^{+0.117}_{-0.259}$
Semi-major axis of the planetary orbit $a_p$ (AU)	$0.03585^{+0.00052}_{-0.00114}$
Orbital inclination angle $i_p$ (degree)	$87.828 \pm 0.126$
Planetary transit duration $T_{14}$ (h)	$2.7220 \pm 0.0019$
Transit ingress and egress duration $T_{12} = T_{34}$ (h)	$0.3330 \pm 0.0024$
Stellar fundamental parameters	
Effective temperature $T_{\text{eff}}$ (K)	$5560 \pm 80$
Surface gravity <sup>b</sup> $\log g$ ( $\log_{10} \text{ cm s}^{-2}$ )	$4.44 \pm 0.10$
Surface gravity <sup>c</sup> $\log g$ ( $\log_{10} \text{ cm s}^{-2}$ )	$4.41 \pm 0.04$
Metallicity [M/H] (dex)	$-0.10 \pm 0.05$
Microturbulent velocity <sup>d</sup> $v_{\text{micro}}$ ( $\text{km s}^{-1}$ )	$1.0 \pm 0.1$
Macroturbulent velocity <sup>d</sup> $v_{\text{macro}}$ ( $\text{km s}^{-1}$ )	$2.8 \pm 0.4$
Projected stellar rotational velocity $v \sin i_\star$ ( $\text{km s}^{-1}$ )	$2.5 \pm 0.5$
Spectral type <sup>e</sup>	G4 V
Star mass $M_\star$ ( $M_\odot$ )	$0.85 \pm 0.04$
Star radius $R_\star$ ( $R_\odot$ )	$0.95 \pm 0.04$
Star age $t$ (Gyr)	$11 \pm 2$
Star rotation period <sup>f</sup> $P_{\text{rot}}$ (day)	$22.047 \pm 0.121$
Interstellar extinction $A_V$ (mag)	$0.044 \pm 0.044$
Distance of the system $d$ (pc)	$725 \pm 75$
Planetary fundamental parameters	
Planet mass <sup>g</sup> $M_p$ ( $M_{\text{Jup}}$ )	$0.595 \pm 0.081$
Planet radius <sup>g</sup> $R_p$ ( $R_{\text{Jup}}$ )	$1.192 \pm 0.052$
Planet density $\rho_p$ ( $\text{g cm}^{-3}$ )	$0.459 \pm 0.083$
Equilibrium temperature $T_{\text{eq}}$ (K)	$1605 \pm 120$
Brightness temperature <sup>h</sup> $T_{\text{br}}$ (K)	$1950 \pm 250$
Geometric albedo <sup>h</sup> $A_g$	$0.055 \pm 0.028$
Bond albedo <sup>h</sup> $A_B$	$0.037 \pm 0.019$

**Notes.** <sup>(a)</sup> BJD<sub>TDB</sub> is the barycentric Julian date in barycentric dynamical time. <sup>(b)</sup> Obtained from the spectroscopic analysis. <sup>(c)</sup> Obtained from  $T_{\text{eff}}$ , [M/H], and  $\rho_\star$ , along with the Pisa Stellar Evolution Data Base for low-mass stars. <sup>(d)</sup> Using the calibration equations of Bruntt et al. (2010) and Doyle et al. (2014). <sup>(e)</sup> With an accuracy of  $\pm 1$  sub-class. <sup>(f)</sup> From McQuillan et al. (2013). <sup>(g)</sup> Radius and mass of Jupiter taken as  $6.9911 \times 10^9$  cm and  $1.89896 \times 10^{30}$  g, respectively. <sup>(h)</sup> Assuming  $A_g = 1.5 \times A_B$  and heat redistribution factor between 1/4 and 2/3.





**Fig. 7.** Phase-folded transit light curves of Kepler-423, best fitting model, and residuals. LC data are shown on the *left panel*, SC on the *right panel*, both binned at  $\sim 1.9$  min. The shaded area corresponds to the  $3\sigma$  errors in the binned fluxes. The dashed lines mark the  $T_{14}$  limits, and the dotted lines the  $T_{23}$  limits. The blurring of the transit shape – due to the long integration time – is obvious in the LC plot (*left panel*).

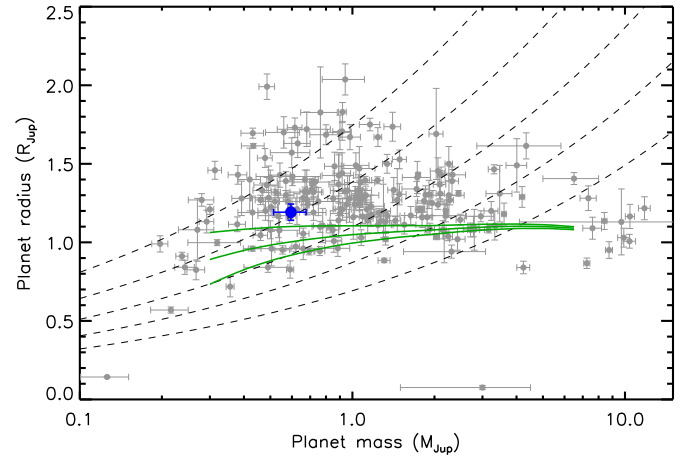


**Fig. 8.** Radial velocity data with the median and 68% and 99% percentile limits of the posterior predictive distribution.

(51% null hypothesis probability) between the quarterly transit depth residuals – as derived from the PDC-MAP cotrended light curve, following our correction for contamination factor – and our estimates of the quarterly crowding metrics, as displayed in the lower panel of Fig. 5. We note that neglecting the quarter-to-quarter transit depth variation leads to a significant ( $7\sigma$ ) underestimate of the planet-to-star radius ratio by about 1.5% and doubles its uncertainty.

### 6.1. Planet properties

The planet Kepler-423b has a mass of  $M_p = 0.595 \pm 0.081 M_{\text{Jup}}$  and a radius of  $R_p = 1.192 \pm 0.052 R_{\text{Jup}}$ , yielding a planetary bulk density of  $\rho_p = 0.459 \pm 0.083 \text{ g cm}^{-3}$ . We show in Fig. 9 how Kepler-423b compares on a mass-radius diagram to all other known transiting hot Jupiters ( $P_{\text{orb}} < 10$  days;  $0.1 < M_p < 15 M_{\text{Jup}}$ ). With a system age of 11 Gyr, the radius of Kepler-423b is consistent within  $1.5\sigma$  with the expected theoretical value for an irradiated coreless gas-giant planet (Fortney et al. 2007). Alternatively, the planet might have a core and be inflated because of unaccounted-for heating source, atmospheric enhanced opacities, and reduced interior heat transport

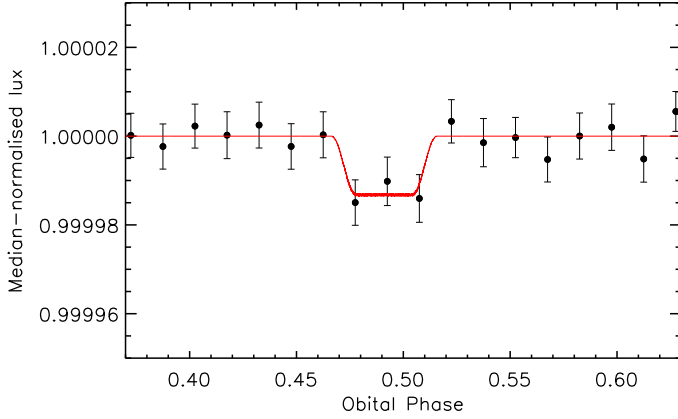


**Fig. 9.** Mass-radius diagram for transiting hot Jupiters (grey circles;  $P_{\text{orb}} < 10$  days and  $0.1 < M_p < 15 M_{\text{Jup}}$ , from the Extrasolar Planet Encyclopedia at <http://exoplanet.eu/>, as of 15 September 2014). Kepler-423b is marked with a thicker blue circle. The Fortney et al. (2007) isochrones for a planet core mass of 0, 25, 50  $M_{\oplus}$  – interpolated to the solar equivalent semi-major axis of Kepler-423b and extrapolated to an age of 11 Gyr – are overplotted with thick green lines from top to bottom. Isodensity lines for density  $\rho_p = 0.25, 0.5, 1, 2,$  and  $4 \text{ g cm}^{-3}$  are overlaid with dashed lines from left to right.

(Guillot 2008; Baraffe et al. 2014). It is worth noting that the radius of Kepler-423b agrees within  $1\sigma$  to the empirical radius relationship for Jupiter-mass planets from Enoch et al. (2012), which predicts a radius of  $1.28 \pm 0.14 R_{\text{Jup}}$ , given the planetary mass  $M_p$ , equilibrium temperature  $T_{\text{eq}}$ , and semi-major axis  $a_p$  listed in Table 5.

### 6.2. Secondary eclipse and planet albedo

We detected a tentative secondary eclipse of Kepler-423b in the *Kepler* long cadence light curve and measured a depth of  $14.2 \pm 6.6$  ppm (Fig. 10). The eclipse signal is relatively weak and could in theory be due to random instrumental or astrophysical events. We set to verify the eclipse signal and assessed its significance using a method based on Bayesian model selection, as described by Parviainen et al. (2013). We introduced some additional improvements that we briefly describe in the following



**Fig. 10.** Secondary eclipse light curve of Kepler-423, phase-folded to the orbital period of the planet. *Kepler* data are median-binned in intervals of 0.015 cycles in phase ( $\sim 1$  h). The  $1\sigma$  error bars are the median absolute deviations of the data points inside the bin, divided by the square root of the number of points. The best fitting transit model is overlotted with a red line.

paragraph<sup>7</sup>. The Bayesian evidence integration could be carried out using simple Monte Carlo integration because of the low dimensionality of the effective parameter space.

We considered two models, one without an eclipse signal ( $M_0$ ) and one with an eclipse signal ( $M_1$ ), and assigned equal prior weights on both models. We calculated the Bayes factor in favour of  $M_1$  cumulatively for each orbit, i.e., we calculated the Bayesian evidence for both models separately for every individual 18 h-long data segment. Since we assumed that the model global likelihoods – or Bayesian evidence – are independent from orbit to orbit, the final global likelihood is the product of the model likelihoods for each orbit – or a sum of the model log-likelihoods. A real eclipse signal that exists from orbit to orbit leads to a steadily increasing Bayes factor in favour of  $M_1$ <sup>8</sup>. In contrast, a signal from an individual event mimicking an eclipse would be visible as a jump in the cumulative Bayes factor trace.

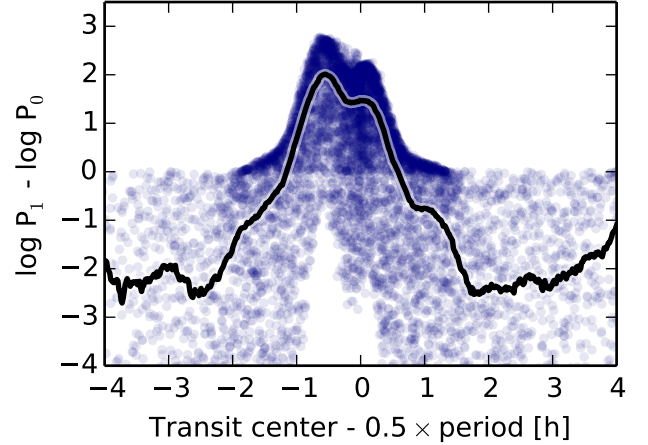
The Bayes factor in favour of the eclipse model was found to depend strongly on our choice of priors on eccentricity and surface brightness ratio. Assuming a uniform prior on eccentricity between 0 and 0.2 and a Jeffreys prior on surface brightness ratio encompassing all physically plausible values for planetary albedos up to 0.5 (i.e., flux ratios between 0 and 0.008) results in a Bayes factor only slightly higher than unity. Lowering the maximum eccentricity to 0.05 and maximum surface brightness ratio to 0.0015 (based on our MCMC posterior sampling, which is going to the grey area of Bayesian model selection) yielded a Bayes factor of  $\sim 2.6$ , corresponding to positive support for the eclipse model.

We show the log posteriors sample differences and the Bayes factor in favour of the eclipse model mapped as a function of eclipse centre – itself a function of the eccentricity and argument of periastron – in Fig. 11, and the cumulative Bayes factor in Fig. 12.

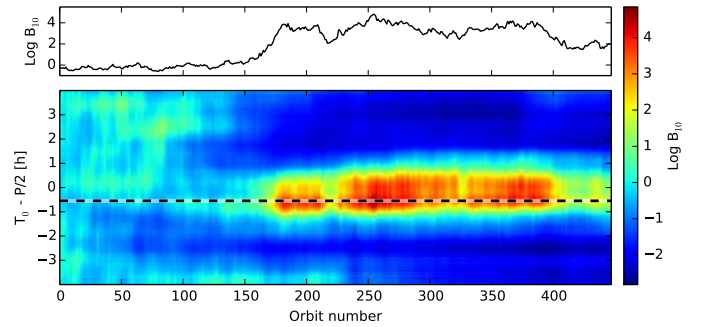
The Bayes factor map is used as an expository tool to probe the Bayes-factor space as a function of our prior assumptions, and in this case shows that a) the tentative eclipse found near 0.5 phase is the only eclipse-like signal inside the sampling

<sup>7</sup> For a detailed explanation, see Parviainen et al. (in prep.).

<sup>8</sup> We stress that this is a slight simplification, as the cumulative Bayes factor behaves more as a directed random walk, especially for weak signals.



**Fig. 11.** Differences between the individual posterior samples for the eclipse model ( $M_1$ ) and no-eclipse model ( $M_0$ ) plotted against the eclipse centre (light blue circles), mapped from the sampling space that uses eccentricity and argument of periastron. Only 447 LC segments are used for the modelling (see Sect. 5.2). A Bayes factor map produced by sliding a uniform prior with a width of 15 min along the transit centre is overlaid with a black thick line.



**Fig. 12.** The cumulation of  $\log B_{10}$  as a function of increasing data. The plot shows only the 447 orbits used for the secondary eclipse modelling (see Sect. 5.2). The *upper plot* shows the trace for the maximum  $\log B_{10}$  case (identified as a slashed line in the *lower plot*), and the *lower plot* shows  $\log B_{10}$  mapped as a function of a sliding prior on the eclipse centre (as in Fig. 11) on the *y*-axis, with the amount of data (number of orbits included) increasing on the *x*-axis.

volume constrained by our priors; b) while the Bayes factor is only moderately in favour of the eclipse model, it is against the eclipse model for eclipse signals occurring away from the identified eclipse (with a peak-to-peak log Bayes factor difference being  $\sim 4$ ). However, the Bayes factor trace (Fig. 12) shows that the support for the eclipse-model is mostly from a small continuous subset of orbits (but not from a single orbit that would indicate a jump in the data). Thus, we must consider the detected eclipse signal to be only tentative.

The depth of the planetary eclipse would imply a planet-to-star surface brightness ratio of  $f = (8.93 \pm 4.13) \times 10^{-4}$ , allowing us to constrain the geometric  $A_g$  and Bond  $A_b$  albedo of the planet. From the effective stellar temperature, eccentricity, and scaled semi-major listed in Table 5, and assuming  $A_g = 1.5 \times A_b$  and heat redistribution factor between 1/4 and 2/3, we found tentative values of  $A_g = 0.055 \pm 0.028$ ,  $A_b = 0.037 \pm 0.019$ , and a planet brightness temperature of  $T_{br} = 1950 \pm 250$  K. This would make Kepler-423b one of the gas-giant planets with lowest Bond albedo known so far (see, e.g., Angerhausen et al. 2014).

### 6.3. Tidal interaction and non-zero eccentricity

The RV data alone constrain the eccentricity to  $e < 0.16$  (99th percentile of the posterior distribution). The inclusion of the photometric data and the tentative detection of the planet occultation give a small non-zero eccentricity of  $0.019^{+0.028}_{-0.014}$ . We stress that ignoring the planet eclipse signal and imposing a circular orbit have a negligible effect on the values of the derived planetary parameters.

We estimated the tidal evolution time-scales of the system using the model of [Leconte et al. \(2010\)](#), which is valid for arbitrary eccentricity and obliquity. However, instead of using a constant time lag  $\Delta t$  between the tidal bulge and the tidal potential, we recast their model equations using a constant modified tidal quality factor  $Q'$ , for an easy comparison with results for other planetary systems usually given in terms of  $Q'$ . Specifically, we assumed that  $\Delta t = 3/(2k_2nQ')$ , where  $k_2$  is the potential Love number of the second degree and  $n$  the mean orbital motion. This approximation is the same as, e.g., in [Mardling & Lin \(2002\)](#) and is justified for a first estimate of the time-scales in view of our limited knowledge of tidal dissipation efficiency inside stars and planets.

The rotation period of the star is longer than the orbital period of the planet, therefore tides act to reduce the semi-major axis of the orbit  $a$  and to spin up the star. Assuming  $Q'_* = 10^6$  for the star, we obtained a tidal decay time-scale  $|(1/a)(da/dt)|^{-1} \sim 4$  Gyr, while the time-scales for spin alignment and spin up are both  $|(1/\Omega)(d\Omega/dt)|^{-1} \sim 10$  Gyr, all comparable to the age of the system. This suggests that a substantial orbital decay accompanied by a spin up of the star could have occurred during the main-sequence evolution of the system. Applying standard gyrochronology to the star ([Barnes 2007](#)), we estimated an age of  $\sim 3.7$  Gyr for the observed rotation period of 22.046 days, which supports the conclusion that stellar magnetic braking is counteracted by the planet. The expected rotation period is  $\sim 40$  days for an age of 11 Gyr, i.e., the star is rotating about 1.8 times faster than expected. The present orbital angular momentum is about 2.5 times the stellar spin angular momentum. If the angular momentum of excess rotation comes from the initial orbital angular momentum, its minimum value was  $\sim 1.25$  the present orbital angular momentum, corresponding to an initial orbital period of at least 4.9 days for a planet of constant mass. If the stellar tidal quality factor  $Q'_* \gtrsim 10^7$ , as suggested by [Ogilvie & Lin \(2007\)](#) for non-synchronous systems as in the case of Kepler-423, the orbital decay and the stellar spin up would have been negligible during the main-sequence evolution of the host and the excess rotation could be associated with a reduced efficiency of the stellar wind due to the magnetic perturbations induced by the planet ([Lanza 2010; Cohen et al. 2010](#)).

Separately, if the orbital eccentricity is indeed non-zero and equal to its most likely value  $0.019^{+0.028}_{-0.014}$ , we estimated that this would require  $Q'_* \geq 10^7$  and  $Q'_p \geq 10^8$ . The latter is consistent with the tidal quality factor estimated by [Goodman & Lackner \(2009\)](#) for coreless planets.

### 6.4. Spin-orbit alignment along the line of sight

The spin-orbit angle, i.e., the angle between the stellar spin axis and the angular momentum vector of the orbit, is regarded as a key parameter to study planet migration mechanisms (see, e.g., [Winn et al. 2010; Gandolfi et al. 2012; Crida & Batygin 2014](#)). Assuming that a star rotates as a rigid body, one can infer the

inclination  $i_*$  of the stellar spin with respect to the line of sight through

$$\sin i_* = P_{\text{rot}} (v \sin i_*) / 2\pi R_*, \quad (4)$$

where  $P_{\text{rot}}$ ,  $R_*$ , and  $v \sin i_*$  are the stellar rotation period, radius, and projected rotational velocity, respectively. Since a transiting planet is seen nearly edge-on ( $i_p \approx 90^\circ$ ), the inclination of the stellar spin axis can tell us whether the system is aligned along the line of sight or not. However, the method does not allow us to distinguish between prograde and retrograde systems, as  $i_*$  and  $\pi - i_*$  angles provide both the same  $\sin i_*$ .

Using the values reported in Table 5, we found that  $\sin i_* = 1.15 \pm 0.23$ , which implies that  $i_*$  is between  $\sim 70$  and  $90^\circ$  or  $\sim 160$  and  $180^\circ$ . Given the fact that the measurements of the Rossiter-McLaughlin effect have shown that retrograde systems around relatively cool stars ( $T_{\text{eff}} \lesssim 6250$  K) are rare (see, e.g., [Winn et al. 2010; Albrecht et al. 2012; Hirano et al. 2014](#)), our findings are consistent with spin-orbit alignment along the line of sight. Moreover, as seen in Sect. 6.3, the tidal interaction time-scale for the evolution of the obliquity is comparable to the age of the system, implying that any primordial misalignment of the planet has most likely been damped down by tidal forces. This agrees with the general trend observed in systems with short tidal interaction time-scales ([Albrecht et al. 2012](#)).

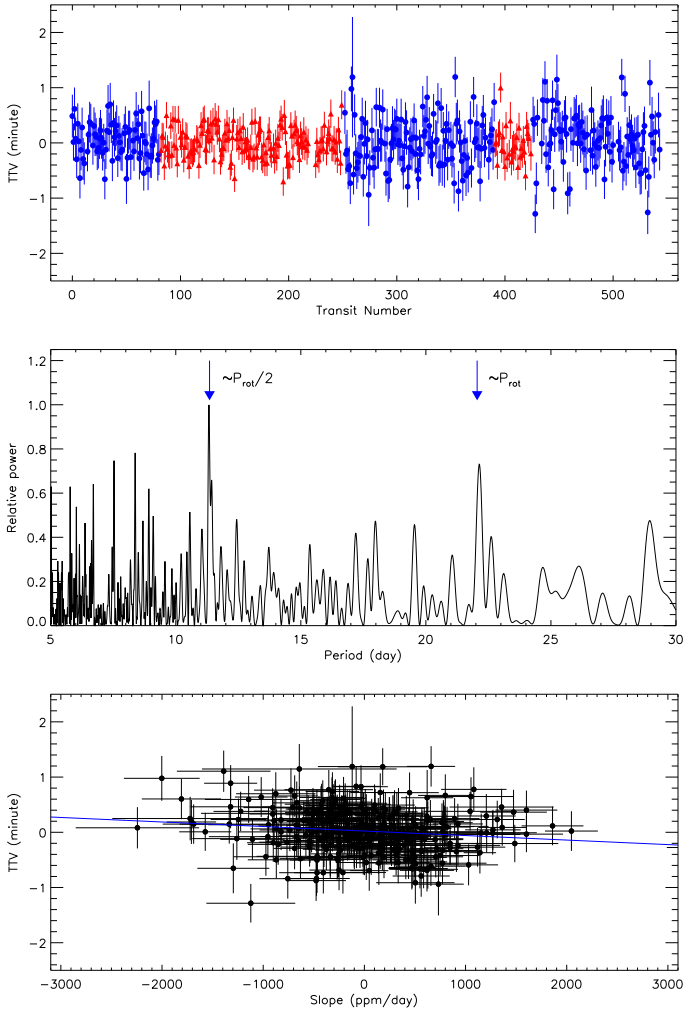
### 6.5. Search for transit timing variations

We carried out a search for additional perturbing objects in the system by looking for gravitationally-induced variations in the transit centre times of Kepler-423b, the so-called transit timing variations (TTVs). The TTV search was carried out using MCMC and exploiting – for the first time – the full *Kepler* light curve of Kepler-423, from  $Q_1$  to  $Q_{17}$ . The transit centre posteriors were estimated by fitting a transit model to the individual transits with parameter posteriors from the main characterisation run used as priors for all the parameters except the transit centre. A wide uniform prior centred on the expected transit centre time, assuming no TTVs, was used for the transit centre.

Our results are shown in the upper panel of Fig. 13. The transit centres do not deviate significantly from the linear ephemeris and the results allow us to rule out TTVs with peak-to-peak amplitude larger than about 2 min. Our finding agrees with those from [Ford et al. \(2011\)](#) and [Mazeh et al. \(2013\)](#), and further confirm the trend that stars hosting hot Jupiters are often observed to have no other close-in planets ([Steffen et al. 2012; Szabó et al. 2013](#)).

The Lomb-Scargle periodogram of the Kepler-423b TTV data shows no peaks with false alarm probability smaller than 1%. However, it is worth noting that there are peaks at the stellar rotation period and its first harmonic (Fig. 13, middle panel), which might be due to the passage of Kepler-423b in front of active photospheric regions (see, e.g., [Oshagh et al. 2013](#)). The peak at half the stellar rotation period might be caused by the occultations of starspots at opposite stellar longitudes. As a matter of fact, the *Kepler* light curve shows also quasi-periodic variations recurring every  $\sim 11$  days (i.e., half the stellar rotation period), which are visible in the second half of the  $Q_{13}$  data plotted in Fig. 1.

As recently suggested by [Mazeh et al. \(2014\)](#), the anti-correlation (correlation) between the TTV and the slope of the light curve around each transit can be used to identify prograde (retrograde) planetary motion with respect to the stellar rotation. The lower panel of Fig. 13 shows that there is no significant correlation (anti-correlation) in our data between TTVs and local



**Fig. 13.** *Upper panel:* differences between the observed and modelled transit centre times of Kepler-423 (TTVs). Transit timing variations extracted from the short cadence data are plotted with red triangles, while long cadence TTVs are shown with blue circles. *Middle panel:* Lomb-Scargle periodogram of the TTV data in the 5–30 day period range. The two arrows mark the peak close to the stellar rotation period and its first harmonic. *Lower panel:* transit timing variation versus local transit slope. The straight blue line marks the linear fit to the data.

photometric slopes, the linear Pearson correlation coefficient and null hypothesis probability being  $-0.16$  and  $13\%$ , respectively.

The lack of TTV-versus-slope correlation (anti-correlation) might imply that there are no detectable spot-crossing events in the TTV data, and that the photometric variation observed in the *Kepler* light curve is mainly dominated by active regions that are not occulted by the planet. Alternatively, there might be spot-crossing events whose signal in the TTV data is just below the noise. As a sanity check, we performed a visual inspection of the SC transits – the only ones in which a spot-crossing event can potentially be identified by eye – and found only one significant event. However, we believe that our data are mainly dominated by noise, because the TTVs are normally distributed around zero with a standard deviation ( $\sim 22$  s) comparable with the average uncertainty of our measurements ( $\sim 19$  s).

## 7. Conclusions

We spectroscopically confirmed the planetary nature of the *Kepler* transiting candidate Kepler-423b. We derived the systems

parameters exploiting – for the first time – the whole available *Kepler* photometry and combined it with high-precision RV measurements taken with FIES at NOT.

We found that the PDC-MAP *Kepler* data are affected by seasonal systematic transit depth variations recurring every 4 quarters. We believe that these systematics are caused by an uncorrected estimate of the quarterly variation of the crowding metric, rather than different behaviours of the *Kepler* detectors (linearity), and treated them as such.

Kepler-423b is a moderately inflated hot Jupiter with a mass of  $M_p = 0.595 \pm 0.081 M_{\text{Jup}}$  and a radius of  $R_p = 1.192 \pm 0.052 R_{\text{Jup}}$ , translating into a bulk density of  $\rho_p = 0.459 \pm 0.083 \text{ g cm}^{-3}$ . The radius is consistent with both theoretical models for irradiated coreless planets and expectations based on empirical laws. Kepler-423b transits every 2.7 days an old, G4 V star with an age of  $11 \pm 2$  Gyr.

The stellar rotation period, projected equatorial rotational velocity  $v \sin i_*$  and star radius  $R_*$  constrain the inclination  $i_*$  of the stellar spin axis to likely lie between  $\sim 70$  and  $90^\circ$ , implying that the system is aligned along the line of sight.

We found no detectable TTVs at a level of  $\sim 22$  s ( $1\sigma$  confidence level), confirming the lonely trend observed in hot Jupiter data. Our tentative detection of the planetary eclipse yields a small non-zero eccentricity of  $0.019^{+0.028}_{-0.014}$ , and geometric and Bond albedo of  $A_g = 0.055 \pm 0.028$  and  $A_b = 0.037 \pm 0.019$ , respectively, placing Kepler-423b amongst the gas-giant planets with the lowest albedo known so far.

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*Note added in proof.* Endl et al. (2014) presented an independent spectroscopic confirmation of the planetary nature of Kepler-423b. While their estimate of the planet radius ( $R_p = 1.200 \pm 0.065 R_{\text{Jup}}$ ) agrees very well with ours, their planetary mass of  $M_p = 0.72 \pm 0.12 M_{\text{Jup}}$  is slightly ( $\sim 1\sigma$ ) higher than our value. This is mainly due to their higher estimate of the stellar mass ( $M_* = 1.07 \pm 0.05 M_\odot$ ), which in turn results from a hotter stellar effective temperature ( $T_{\text{eff}} = 5790 \pm 116$  K) and higher iron content ( $[\text{Fe}/\text{H}] = 0.26 \pm 0.12$  dex).

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