# Key-Dependent S-Box Generation in AES Block Cipher System 

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#### Abstract

Advanced Encryption Standard (AES) block cipher system is widely used in cryptographic applications. A nonlinear substitution operation is the main factor of the AES cipher system strength. The purpose of the proposed approach is to generate the random S-boxes changing for every change of the secret key. The fact that the S-boxes are randomly key-dependent and unknown is the main strength of the new approach, since both linear and differential cryptanalysis require known S-boxes. In the paper, we briefly analyze the AES algorithm, substitution S-boxes, linear and differential cryptanalysis, and describe a randomly key-dependent S-box and inverse S-box generation algorithm. After that, we introduce the independency measure of the S-box elements, and experimentally investigate the quality of the generated $S$-boxes.


Keywords: advanced encryption standard, key-dependent S-boxes, generation algorithm.

## 1. Introduction

Cryptography has an important role in the security of data transmission and is the best method of data protection against passive and active fraud. The growing number communication users has led to increasing demand for security measures to protect data transmitted over open channels (Chen et al., 2008; Li et al., 2007; Sakalauskas, 2005). A cipher system is a set of reversible transformations from the set M of a plaintext into the set C of a ciphertext. Each transformation depends on a secret key and the ciphering algorithm. In the block cipher system, the plaintext is divided into the blocks and the ciphering is carried out for the whole block (El-Ramly et al., 2001).

Two general principles of block ciphers are diffusion and confusion. Diffusion is spreading of the influence of a one plaintext bit to many ciphertext bits with intention to hide the statistical structure of the plaintext. Confusion is transformation that change dependence of the statistics of ciphertext on the statistics of plaintext. In most cipher systems the diffusion and confusion is achieved by means of round repetition. Repeating a single round contributes to cipher's simplicity (Masuda et al., 2006). Modern block ciphers consist of four transformations: substitution, permutation, mixing, and key-adding (Schneier, 1996; Menezes et al., 1997).

Cryptographic objects are private key algorithms, public key algorithms and pseudorandom generators. Block ciphers transform usually the 128 or 256 bits string to a string
of the same length under control of the secret key. Private key cryptography, such as DES (DES, 1977), 3DES, and Advanced Encryption Standard (AES) (AES, 2001), uses the same key for the sender and receiver to encrypt the plaintext and decrypt the ciphertext. Private key cryptography is more suitable for the encryption of a large amount of data. Public key cryptography, such as the Rivest-Shamir-Adleman (RSA) or Elliptic Curve algorithms, uses different keys for encryption and decryption. The AES algorithm defined by the National Institute of Standards and Technology of the United States has been accepted to replace DES as the new private key encryption algorithm. AES overpass DES in improved security because of larger key sizes. AES is suitable for 8 bit microprocessor platforms and 32 bit processors (Su et al., 2003).

Block cipher systems depend on the S-boxes, which are fixed and have no relation with the secret key. So only changeable parameter is the secret key. Since the only nonlinear component of AES is S-boxes, they are an important source of cryptographic strength.

The use of key-dependent S-boxes in block cipher design has not been widely investigated in the literature. Research into S-box design has focused on determination of S-box properties which yield cryptographically strong ciphers, with the aim of selecting a small number of good S-boxes for use in a block cipher DES and CAST (Menezes et al., 1997). Some results have demonstrated that a randomly chosen S-box of sufficient size will have several of these desirable properties with high probability (Keliher, 2003).

This paper outlines the work of the authors' investigation into the design of a new pseudo-randomly generated key-dependent S-boxes. Other systems using key-dependent S-boxes have been proposed in the past, the most well-known is Blowfish (Schneier, 1996) and Khufu (Merkle, 1991). Each of these two systems uses the cryptosystem itself to generate the S-boxes. Preliminary results show, that our proposed algorithm has good cryptographic strength, with the added benefit that is resistant to linear and differential cryptanalysis, which require that the S-boxes be known.

A new method to generate pseudo-random S-boxes as a function of the secret key will be presented. In the next section, we briefly introduce the AES algorithm. In the following two sections, we analyze AES S-boxes, differential and linear cryptanalysis. A central part of the paper describes the pseudo-randomly key-dependent S-box and inverse S-box generation algorithm. After that, the paper discusses experimental results and gives conclusions.

## 2. The AES Algorithm

The AES is a private key block cipher that processes data blocks of 128 bits with key length of 128,192 , or 256 bits. The AES algorithm's operations are performed on a 2-D array of 4 times 4 bytes called the State. The initial State is the plaintext and the final State is the ciphertext. The State consists of 4 rows of bytes. As the block length is 128 bits, each row of the State contains 4 bytes. The four bytes in each column form a 32 bit word. After an initial round key addition, a round function consisting of four transformations - SubBytes, ShiftRows, MixColumns, and AddRoundKey is applied to
each data block. The round function is applied 10,12 , or 14 times depending on the key length. AES-128 applies the round function 10 times, AES-192 - 12 times, and AES-256 - 14 times. The transformations are reversible linear and non-linear operations to allow decryption using their inverses. Every transformation affects all bytes of the State. The transformation SubBytes is a nonlinear byte substitution that operates on each byte of the State using a table (S-box). The numbers of the table is computed by a finite field inversion followed by an affine transformation. The resulting table is called an S-box. The ShiftRows transformation is a circular shifting operation, which rotates the rows of the State with different numbers of bytes (offsets). The offset equals to the row index: the second row is shifted one byte to the left, the third row - two bytes to the left, the fourth row - three bytes to the left, and first row - four bytes to the left. MixColumns transformation mixes the bytes in each column by multiplying the State with the polynomial modulo $x^{4}+1$. The State bytes are the coefficients of the polynomial. The AddRoundKey transformation is an XOR operation that adds the round key to the State in each round. The round keys are generated during the key expansion process. The initial round key equals to secret key (Zhang and Parhi, 2002; Su et al., 2003; Hsiao et al., 2005; Feldhofer et al., 2005).

## 3. Substitution S-Boxes

Substitution is a nonlinear transformation which performs confusion of bits. A nonlinear transformation is essential for every modern encryption algorithm and is proved to be a strong cryptographic primitive against linear and differencial cryptanalysis. Nonlinear transformations are implemented as lookup tables (S-boxes). An S-box with $p$ input bits and $q$ output bits is denoted $p \rightarrow q$. The DES uses eight $6 \rightarrow 4$ S_boxes. S-boxes are designed for software implementation on 8-bit processors. The block ciphers with $8 \rightarrow 8$ S-boxes are SAFER, SHARK, and AES. For processors with 32-bit or 64-bit words, Sboxes with more output bits provide high efficiency. The Snefru, Blowfish, CAST, and SQUARE use $8 \rightarrow 32$ S-boxes. The S-boxes can be selected at random as in Snefru, can be computed using a chaotic map, or have some mathematical structure over a finite Galois field. Examples of the last approach are SAFER, SHARK, and AES. S-boxes that depend on key values are slower but more secure than key independent ones (Schneier, 1996). Use of key independent chaotic S-boxes are analyzed in (Jakimovski and Kocarev, 2001), in which the S -box is constructed with a transformation $F((X+K) \bmod M)$, where $K$ is the key (Masuda et al., 2006).

In the AES, the S-box generate two transformations in the Galois fields $\operatorname{GF}(2)$ and $\mathrm{GF}\left(2^{8}\right)$. S-box is a nonlinear transformation where each byte of the State is replaced by another byte using the substitution table. The first transformation: S-box finds the multiplication inverse of the byte in the field $\operatorname{GF}\left(2^{8}\right)$. Since it is a algebraic expression, it is possible to mount algebraic attacks. Hence, it is followed by an affine transformation. The affine transformation is chosen in order to make the SubBytes a complex algebraic
expression while preserving the nonlinearity property. The both S-box transformations can be expressed in a matrix form as (Hsiao et al., 2005; Hsiao et al., 2006)

$$
\begin{equation*}
S^{\prime}=M \bullet S^{-1}+C, \tag{1}
\end{equation*}
$$

where the sign - is multiplication and the sign + is addition in the field $\operatorname{GF}\left(2^{8}\right)$. The $8 \times 1$ vector $S^{\prime}$ denotes the bits of the output byte after the S -box transformations. The inverse S-box transformation can be get by multiplying both sides of equation (1) by $M^{-1}$ and it performs the inverse affine transformation followed by the multiplicative inverse in $\mathrm{GF}\left(2^{8}\right)$ :

$$
\begin{equation*}
S^{-1}=M^{-1} \bullet S^{\prime}+M^{-1} \bullet C . \tag{2}
\end{equation*}
$$

## 4. Linear and Differential Cryptanalysis

Linear and differential cryptanalysis uses the input-output correlation and the difference propagations of the cipher in order to extract partial or whole bits of the secret key. Linear cryptanalysis exploits a cipher's weakness expressed in terms of "linear expressions". In Matsui's terminology (Matsui, 1994) a linear expression for one round is an equation for a certain modulo two sum of round input bits and round outputs bits as a sum of round key bits. The expression should be satisfied with probability much more than 0.5 to be useful (Jakimovski and Kocarev, 2001).

In 1991 was introduced a cryptoanalytic technique known as differential cryptanalysis (Biham and Shamir, 1991). It was successfully applied to attack a variety of SPNs, including DES. Differential cryptanalysis requires knowledge of the XOR tables of S-boxes. For an $n \times n$ S-box, $S$, the XOR table has rows and columns indexed by $0,1, \ldots, 2^{n}-1$, and the table entries are defined as follows: if $i, j \in\left\{0,1, \ldots, 2^{n}-1\right\}$, position $(i, j)$ in the XOR table contains value $\left|\left\{X \in\{0,1\}^{n}: S(X) \oplus S(X \oplus i)=j\right\}\right|$, where $i$ and $j$ are $n$ bits strings. The essential part of every block cipher is an S-box. To secure the cipher against these attacks, the nonlinearity of the S-box should satisfy: the maximum input-output correlation and the difference propagation probability should be minimum (Keliher and Meijer, 1997).

There are two ways to fight against linear and differential cryptanalysis. One is built S-boxes with low linear and differential probabilities. The other is to design the round transformation so that only trails with many active S-boxes occur. The round transformation must be designed in such a way that differential steps with few active $S$-boxes are followed by differential steps with many active S-boxes (Masuda et al., 2006).

The object of this proposal is an AES cipher using key-dependent S-boxes. The fact that the S-boxes are unknown is one of the main strength of our cipher system, since both linear and differential cryptanalysis require known S-boxes. If the S-boxes are generated from the key in sufficiently random fashion, each S-box has a high probability of being complete, possessing fairly high nonlinearity. It is not apparent that the pseudorandom nature of the S -boxes introduces any weakness into the system. Ideal randomness
of S-box cannot be achieved. Ideal randomness is not mathematically possible for the following reasons: the value of all elements in the S-box difference table should be even, since $a \oplus b=b \oplus a$. Since the S-box is bijective, the input difference of 0 will lead to an output difference of 0 . So the element corresponding to row $=0$ and column $=0$ at the difference table will be $2^{n}$ and all other elements in row $=0$ and column $=0$ will be 0 (Sakthivel, 2001).

## 5. A Randomly Key-Dependent S-Box and Inverse S-Box Generation Algorithm

A randomly key-dependent S-box and inverse S-box is constructed by composing two transformations: key pseudo-expansion and key-dependent S-box and inverse S-box generation.

### 5.1. Key Pseudo-Expansion

The key pseudo-expansion transformation takes the 16,24 , or 32 bytes secret key, use round constant rcon and generates a 176 byte long key pseudo-schedule $b$, which we use in the second transformation. The bytes of the secret key are row-wise rearranged into a $4 \times 4$ size key matrix. The method of the key pseudo-expansion is an element-wise XOR of the row of key matrix and the row four rows up. In every fourth row, before applying the XOR, the initial row is cyclically rotated and XOR-ed with constant rcon (AES, 2001).

```
Algorithm 1. Key pseudo-expansion
Input: key, rcon.
Output: key-dependent 176 bytes \(b\).
\(b=(\text { reshape }(\text { key }, 4,4))^{\prime}\)
for \(i=5, \ldots, 44\) do
    laik \(=b(i-1,:)\)
        if \(i \bmod 4=1\)
            \(\operatorname{laik}=\operatorname{laik}\left(\left[\begin{array}{lll}2 & 3 & 1\end{array}\right]\right)\)
            \(v=\operatorname{rcon}((i-1) / 4,:)\)
            \(l a i k=\operatorname{XOR}(l a i k, v)\)
            end if
        \(b(i,:)=\operatorname{XOR}(b(i-4,:)\), laik \()\)
    end for
```

Input of the key pseudo-expansion algorithm is the secret key and round constant rcon. Output of the key pseudo-expansion algorithm is the key pseudo-expanded schedule $b$ (176 bytes). Command reshape in line 1 rearrange the bytes of the secret key into a $4 \times 4$ size matrix. Sign ' means transpose operation. The remaining 160 bytes of the key pseudo-schedule are generated in the for . . . end for cycle (lines 2-10). In line 3 laik is the previous row, which in line 9 is XOR-ed with the row four rows before. If the row index is equal to $5,9, \ldots$, then laik is cyclically rotated and XOR-ed in line 7 with the
round constant rcon. Rotating is done in line 5, where the laik is a row of four bytes and is cyclically permuted by using the new index vector [2 3411 ]. The hexadecimal numbers of the first column of the $10 \times 4$ matrix rcon are $\{01,02,04,08,10,20,40,80,1 \mathrm{~b}, 36\}$. Remaining three columns of the matrix rcon are zero columns.

Note 1. If the secret key length is 192 or 256 bytes, we use only the first 128 bytes of the key.

Note 2. The key pseudo-expansion algorithm don't use the SubByte function and Sbox, while key expansion function in AES uses S-box and SubByte function (AES, 2001).

### 5.2. Key-dependent S-Box and Inverse S-Box Generation

The output of the key pseudo-expansion algorithm is 176 byte long key pseudo-schedule $b$, which is the function of the key. The key pseudo-schedule $b$ is used to generate a randomly key-dependent S-box and inverse S-box.

Algorithm 2. Generation a randomly key-dependent S-box and inverse S-box.
Input: key-dependent 176 bytes $b$ from the output of the key pseudo-expansion algorithm.

Output: integer numbers from the interval [0, 255] of the key-dependent S-box (Sbox) and the inverse S-box (invSbox)

1: Initialization:
$i=0$
$k=1$
$l=1$
2: Compute the first subtotal modulo 256:
$S(1)=(b(1)+b(2)) \bmod 256$
$\operatorname{Sbox}(1)=S(1)$
while $k<256$
$i=i+1$
$m=1+(k+i * l) \bmod 176$
$S(i+1)=(S(i)+b(m)) \bmod 256$
$l=0$
: for $j=1, \ldots, k$ do
Compare subtotal $S(i+1)$ with the elements $\operatorname{Sbox}(j)$ and count the number
$l$ of the S -box elements which are not equal to $S(i+1)$
end for
if $l=j$
$\operatorname{Sbox}(k+1)=S(i+1)$
$k=k+1$
end if
end while
6: for $k=1, \ldots, 256$ do $\operatorname{invSbox}(\operatorname{Sbox}(k)+1)=k-1$
end for

Note 3. Randomness of the key-dependent S-box and inverse S-box is achieved by choosing the index $m$ of the bytes $b$, which depends on the variables $i, k$, and $l$.

## 6. Experimental Results

We introduce the independency measure of the S-box elements:

1) Normalize the S-box elements

$$
\begin{equation*}
y=\frac{x-\operatorname{mean}(x)}{\operatorname{std}(x)} \tag{3}
\end{equation*}
$$

where $\operatorname{mean}(x)=(\max (x)+\min (x)) / 2$, std $(x)=\operatorname{sqrt}\left((\max (x)-\min (x))^{2} / 12\right)$.
2) Compute the correlation function corr of the normalized S-box.
3) Find the maximal value $M A X$ of the correlation function and form a new function CORR, in which the maximal value MAX of the correlation function corr is changed to zero.
4) Calculate the independency measure of the S-box elements

$$
\begin{equation*}
\text { ratio }=\frac{\operatorname{std}(C O R R)}{M A X} \tag{4}
\end{equation*}
$$

Experiment 1. We experimentally checked how the independency measure ratio of the S-box elements depends on the interval length. For the generation of the random integer numbers from some interval we applied Matlab function randperm. We repeated the experiment 500 times and calculated mean and standard deviation of the ratio. The results are given in the Table 1.

Table 1
The mean of the ratio of the dependent and independent integer numbers via the interval length

| Interval length | Mean of the ratio of the linearly <br> dependent numbers | Mean of the ratio of the <br> independent numbers |
| :---: | :---: | :---: |
| 8 | $0.362427 \pm 1.6737 \cdot 10^{-16}$ | $0.230258 \pm 0.0627$ |
| 16 | $0.388781 \pm 5.0212 \cdot 10^{-16}$ | $0.166652 \pm 0.0381$ |
| 32 | $0.401525 \pm 4.4632 \cdot 10^{-16}$ | $0.125118 \pm 0.0206$ |
| 64 | $0.407811 \pm 5.0211 \cdot 10^{-16}$ | $0.086057 \pm 0.0118$ |
| 128 | $0.410932 \pm 5.5791 \cdot 10^{-16}$ | $0.062037 \pm 0.0069$ |
| $\mathbf{2 5 6}$ | $\mathbf{0 . 4 1 2 4 8 8} \pm \mathbf{7 . 2 5 2 8} \cdot 10^{-16}$ | $\mathbf{0 . 0 4 4 3 9 0} \pm \mathbf{0 . 0 0 3 2}$ |
| 512 | $0.413264 \pm 7.2528 \cdot 10^{-16}$ | $0.031398 \pm 0.0015$ |
| 1024 | $0.413652 \pm 6.6949 \cdot 10^{-16}$ | $0.022096 \pm 8.3026 \cdot 10^{-4}$ |
| 2048 | $0.413846 \pm 2.7895 \cdot 10^{-16}$ | $0.015646 \pm 4.4133 \cdot 10^{-4}$ |
| 4096 | $0.413942 \pm 5.5791 \cdot 10^{-16}$ | $0.011044 \pm 1.9339 \cdot 10^{-4}$ |
| 40960 | $0.414029 \pm 1.6737 \cdot 10^{-16}$ | $0.003497 \pm 2.0673 \cdot 10^{-5}$ |
| 409600 | $0.414038 \pm 8.9265 \cdot 10^{-16}$ | $0.001105 \pm 2.0026 \cdot 10^{-6}$ |

From Table 1 we can see, that ratio depends on the interval length of the integer numbers. For the AES, the S-box elements are integers from the interval [0, 255]. In that case, the measure ratio for randomly generated elements has value $0.044390 \pm 0.0032$, and ratio has the maximal value $0.4124876 \pm 7.2528 \cdot 10^{-16}$ for linearly dependent elements. If we analyze only the interval $[0,255](16 \times 16$ S-box $)$, and suppose that function randperm permutes the integer numbers "ideally", the ratio $=0.0443904 \pm 0.0032$ can be used as an "ideal" ratio for the random $16 \times 16$ S-box. So, the ratio can be used as the independency measure of the integer numbers from the finite interval. Theoretically, in case the interval of the integer numbers is infinitely long, for the independent integer numbers the ratio is equal to zero.

Experiment 2. The purpose is to verify the proposed S-box and inverse S-box generation algorithm. Consider the 128 bit length secret key in the hexadecimal form:

$$
\begin{equation*}
k e y \_h e x=\{2 f, e 3, c 2, d 3, b f, e 5,56, c 7, f 8,79, d c, c b, 8 c, f d, 6 e, 5 f\} . \tag{5}
\end{equation*}
$$

1) We generate the key-dependent S-box using the transformations described in the paper. The key-dependent S-box is given in the Table 2 . The independency measure ratio of the S-box elements is equal to 0.0432548 and is approximately equal to "ideal" ratio $=$ 0.044390 for independent numbers generated using function randperm. The correlation function of the normalized S-box is in the Fig. 1.
2) We change two bits in the secret key (5), for example, $2 f \rightarrow 1 f$ :

$$
\begin{equation*}
k e y \_h e x=\{1 f, e 3, c 2, d 3, b f, e 5,56, c 7, f 8,79, d c, c b, 8 c, f d, 6 e, 5 f\} \tag{6}
\end{equation*}
$$

Table 2
Key-dependent S-box. Key is as in (5)

| 238 | 111 | 194 | 228 | 165 | 51 | 54 | 157 | 216 | 18 | 202 | 92 | 74 | 129 | 188 | 250 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 230 | 154 | 0 | 72 | 208 | 151 | 125 | 24 | 83 | 146 | 114 | 218 | 121 | 227 | 21 | 2 |
| 185 | 37 | 17 | 8 | 214 | 134 | 220 | 80 | 39 | 181 | 6 | 128 | 207 | 77 | 191 | 231 |
| 10 | 118 | 96 | 79 | 187 | 226 | 50 | 247 | 110 | 15 | 245 | 171 | 86 | 81 | 126 | 224 |
| 234 | 3 | 53 | 108 | 65 | 192 | 35 | 26 | 150 | 14 | 57 | 144 | 167 | 38 | 106 | 91 |
| 236 | 89 | 205 | 88 | 155 | 55 | 104 | 178 | 85 | 215 | 123 | 193 | 76 | 229 | 112 | 56 |
| 75 | 44 | 163 | 97 | 174 | 52 | 199 | 243 | 30 | 133 | 143 | 232 | 137 | 61 | 87 | 211 |
| 179 | 235 | 241 | 223 | 4 | 59 | 201 | 42 | 90 | 225 | 162 | 47 | 22 | 139 | 253 | 13 |
| 136 | 120 | 82 | 170 | 101 | 180 | 102 | 189 | 23 | 78 | 45 | 64 | 63 | 131 | 198 | 153 |
| 183 | 210 | 169 | 251 | 43 | 115 | 173 | 46 | 244 | 164 | 168 | 116 | 20 | 212 | 9 | 33 |
| 200 | 93 | 100 | 36 | 49 | 130 | 109 | 132 | 66 | 248 | 246 | 41 | 124 | 221 | 254 | 141 |
| 28 | 95 | 204 | 252 | 69 | 27 | 209 | 1 | 71 | 242 | 122 | 103 | 213 | 196 | 190 | 67 |
| 182 | 34 | 135 | 219 | 140 | 48 | 147 | 98 | 60 | 177 | 142 | 148 | 237 | 195 | 175 | 99 |
| 5 | 186 | 70 | 166 | 184 | 117 | 7 | 107 | 239 | 217 | 62 | 176 | 159 | 138 | 11 | 113 |
| 68 | 249 | 105 | 149 | 127 | 58 | 73 | 145 | 32 | 19 | 84 | 197 | 94 | 156 | 161 | 160 |
| 172 | 40 | 25 | 158 | 222 | 31 | 16 | 206 | 12 | 255 | 152 | 233 | 29 | 240 | 119 | 203 |

and generate another S-box (Table 3). In that case the ratio is equal to 0.043231 and is approximately equal to "ideal" ratio. The correlation function of the normalized S-box (Table 3) is similar to correlation function of the key (5) (see Fig. 1).


Fig. 1. Correlation function of the normalized S-box (Table 2).

Table 3
Key-dependent S-box. Key is as in (6)

| 222 | 84 | 187 | 195 | 174 | 14 | 78 | 45 | 197 | 181 | 121 | 242 | 129 | 142 | 186 | 90 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 214 | 184 | 21 | 172 | 109 | 83 | 63 | 92 | 244 | 252 | 95 | 238 | 51 | 0 | 249 | 70 |
| 185 | 246 | 18 | 183 | 29 | 196 | 6 | 81 | 162 | 223 | 73 | 221 | 23 | 55 | 126 | 149 |
| 10 | 44 | 139 | 103 | 19 | 67 | 31 | 164 | 251 | 225 | 71 | 76 | 178 | 148 | 191 | 87 |
| 218 | 247 | 156 | 151 | 36 | 153 | 117 | 143 | 171 | 110 | 88 | 182 | 146 | 165 | 39 | 27 |
| 220 | 144 | 175 | 204 | 37 | 239 | 115 | 235 | 79 | 202 | 245 | 135 | 208 | 42 | 253 | 22 |
| 75 | 161 | 188 | 52 | 100 | 17 | 123 | 96 | 133 | 65 | 233 | 82 | 40 | 212 | 48 | 113 |
| 179 | 134 | 206 | 125 | 35 | 25 | 50 | 207 | 190 | 46 | 89 | 154 | 38 | 118 | 102 | 111 |
| 152 | 157 | 227 | 180 | 2 | 114 | 193 | 147 | 250 | 54 | 119 | 105 | 145 | 9 | 32 | 192 |
| 199 | 226 | 229 | 16 | 200 | 49 | 41 | 243 | 13 | 173 | 176 | 4 | 255 | 234 | 205 | 159 |
| 232 | 213 | 241 | 108 | 254 | 47 | 136 | 91 | 15 | 216 | 28 | 7 | 120 | 69 | 94 | 80 |
| 60 | 177 | 248 | 168 | 201 | 170 | 198 | 141 | 194 | 20 | 26 | 85 | 56 | 12 | 231 | 30 |
| 230 | 124 | 3 | 59 | 132 | 203 | 1 | 215 | 66 | 43 | 33 | 127 | 57 | 106 | 237 | 86 |
| 53 | 101 | 62 | 140 | 236 | 99 | 58 | 128 | 240 | 112 | 68 | 189 | 211 | 150 | 77 | 158 |
| 116 | 155 | 166 | 104 | 228 | 130 | 5 | 217 | 167 | 137 | 163 | 72 | 131 | 97 | 98 | 107 |
| 219 | 138 | 209 | 93 | 64 | 24 | 61 | 160 | 11 | 169 | 210 | 8 | 74 | 122 | 224 | 34 |



Fig. 2. Plot of the difference of the S-boxes elements (Table 2 and Table 3).


Fig. 3. Correlation function of the normalized difference between the elements of two S-boxes (Table 2 and Table 3).

We calculate the difference of these two S-boxes (Fig. 2) and mutual independency $r a$ tio $=0.040642$, which is approximately equal to "ideal" independency ratio $=0.044390$, i.e., the mutual dependence of these two S -boxes is insignificant. Correlation of the normalized difference between the elements of S-boxes (Table 2 and Table 3) are given in the Fig. 3.
3) We change only one bit of the secret key (5) ( $2 f \rightarrow 3 f$ ), generate the S-box and calculate difference among the elements of this S-box and the elements of Table 2. The mutual independency ratio of these two S-boxes is 0.0445 , i.e., approximately is equal to "ideal" ratio, so the mutual dependence of these two S-boxes is insignificant.

## 7. Conclusions

We presented a new approach to generate the AES randomly key-dependent S-boxes. The quality of this approach is tested by changing only one bit of the secret key to generate new S-boxes. For that purpose the independency measure ratio based on correlation method was introduced. It was established that for any change of the secret key, the structure of the S-box will be changed essentially. The randomly key-dependent S-boxes make our approach resistant to linear and differential cryptanalysis. This approach will lead to generate more secure block ciphers, solve the problem of the fixed structure S-boxes, and will increase the security level of the AES block cipher system. The main advantage of such approach is that an enormous number of S-boxes can be generated by changing secret key.

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## AES blokinės šifravimo sistemos nuo rakto priklausomu S lenteliu generavimas

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AES blokinè šifravimo sistema plačiai naudojama praktikoje. Šios sistemos atsparumas labai priklauso nuo netiesinés baitụ pakeitimo operacijos. Straipsnio tikslas - pasiūlyti algoritma, kuris generuotu atsitiktines priklausomas nuo rakto baitu pakeitimo $S$ lenteles. Trumpai analizuojamas AES algoritmas, jo pakeitimo $S$ lentelès, tiesinè ir diferencialinè kriptoanalizè bei aprašomas naujas nuo rakto priklausomu atsitiktiniu $S$ lenteliu ir inversiniụ $S$ lenteliu generavimo algoritmas. Pasiūlytas $S$ lenteliụ elementụ nepriklausomumo patikrinimo matas bei tiriama sugeneruotụ $S$ lenteliụ kokybè.

