

# Kinematics of the wire-driven parallel robot MARIONET using linear actuators

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**Abstract**—Wire-driven parallel robots are special types of Gough-Stewart platform in which the rigid extensible legs are substituted by extensible wires. Usually wire length change is obtained by coiling the wire on a drum actuated by a rotary motor. We present here a robot using linear actuator and a pulley system allowing a higher modularity of the actuation system. The kinematics of this redundant system (the system has 7 wires), taking into account the elasticity of the wires, is presented. Inverse kinematics may be solved either by first choosing the wire tensions, the control vector being then a linear function of the tensions or by solving directly a system of non linear equations whose unknowns are the components of the control vector. Forward kinematics is a much more complex issue, involving the solving of a large system. We present a solving approach but this problem remains an open issue.

## I. INTRODUCTION

### A. THE MARIONET ROBOT

Wire-driven parallel robots are special types of Gough-Stewart platform in which the rigid extensible legs are substituted by extensible wires. Although known for some time [1], [11], [13], [15], [21], [22] they are currently extensively studied [2], [3], [5], [7], [9], [18], [19] as they offer a larger workspace and high end-effector velocities. Usually wire length change is obtained by coiling the wire on a drum actuated by a rotary motor (see for example the FALCON [11] or SEGESTA [9] robots). If some accuracy is required this solution has the drawback that a special guide must be manufactured on the drum to get a linear relationship between the rotation of the drum and the length of the coiled wire. As the dimensions of the drum are limited so is the amount of coiled wire and consequently the modularity of the system is reduced.

We have started designing a new robot, called *Marionet*, with modularity as focus point: as the robot performances are highly dependent upon the robot geometry (in a broad sense) we wish to be able to quickly modify it in order to adapt the robot to the task at hand. Being able to change the minimal and maximal wire lengths is an important part of this modularity as these parameters play an important role for the robot workspace, accuracy and maximal velocities.

This has motivated us to consider a new coiling system based on a linear actuator and a pulley system (figure 1). The linear actuator (Copley Motion type M 2506) has a platform that slides along a rod using a single rail stage. The motion of the platform is measured by a linear incremental encoder with an accuracy of 1  $\mu\text{m}$ .

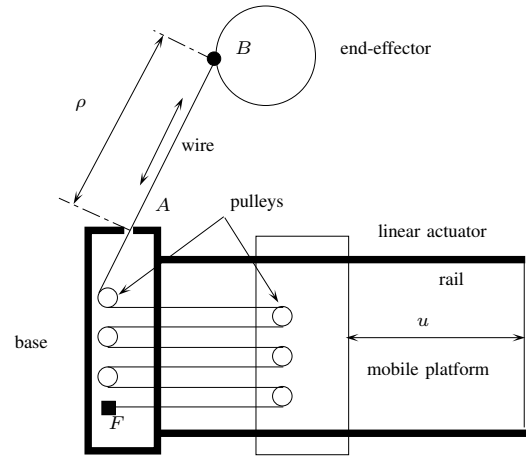


Fig. 1. The wire system used to actuate the Marionet robot. The wire system dimensions have been enlarged compared to the real distance between  $A$  and  $B$ .

One extremity of the wire is attached to a fixed point  $F$  on the base and from this point the wire goes alternately to pulleys that are fixed either on the mobile platform or on the base. The wire goes from a final pulley on the base through a fixed opening, whose location is  $A$ , to the robot end-effector at point  $B$ : the distance between  $A$  and  $B$  will be denoted  $\rho$  and the points  $A, B$  are called the *anchor points* of the robot. Hence the motion of the linear actuator is amplified by the pulleys system by a factor  $K$ , which is an even number. Note that a direct drive may be obtained if an extremity of the wire is connected to the mobile platform and goes directly to the final pulley. We are aware that for large  $K$  the linear actuator will have to provide large force but only experimental tests will show how this may impact the efficiency of the robot.

Seven such wire systems are fixed on standard beams that constitutes the frame of the robot (figure 2). The robot is controlled by a PC under Linux including electronic boards that are connected to power amplifiers. Potential applications that will be considered for this robot are:

- rehabilitation: we will use the robot to measure the motion of human joints and establish various models according to the patient. Then force feedback may be used to implement a rehabilitation protocol or for sport training [16], [17]
- service robotics: in this domain we intend to explore the use of *Marionet* as a windows washing machine for large buildings (the wire systems will be strategically located on the front of the building) or as an assistant

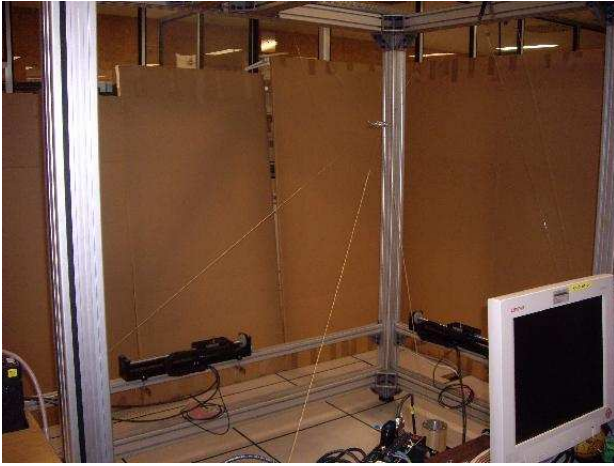


Fig. 2. The Marionet robot

device for elderly people [10]

- entertainment robotics: we intend to explore the use of the robot for movie maker (allowing new angles of view for cameras and unusual actors motion) and fast scenic changes in opera and theaters
- rescue robotics: we intend to use the robot as an independent, portable crane for assisting rescuer during major natural catastrophe [20]
- industrial robotics: Marionet will allow extremely fast motion of the end-effector that may be convenient for pick-and-place operations

In all these applications modularity is extremely important and Marionet combines both a modular mechanical system and a design software that will allow to determine what is the best geometry of the robot for the task at hand.

Still the development of a new robot has to go through the study of basic problems and we address in this paper the kinematics issues. Apart of the original mechanical structure of the wire system our contribution will be to take into account the wire elasticity in the inverse and forward kinematics. Note that others mechanical elements or our system, such as the pulleys, may exhibit elasticity but their stiffness is much higher than the wires one. The influence of cable sag in the inverse kinematics has been addressed in [12] but the length of the wires in our system are sufficiently small to neglect this effect.

## II. KINEMATICS

Currently the wires of the robot are standard fishing wires with high elasticity. This elasticity may be modeled with Hooke's law: if  $L_0$  is the length of the unloaded wire and  $L$  its length under tension, then the tension  $\tau$  in the wire may be calculated as

$$\tau = k \frac{L - L_0}{L} \quad (1)$$

where  $k$  characterizes the material of the wire. The total length of the wire may be written as

$$L = \rho + V + Ku \quad (2)$$

where  $u$  is the actuator position with respect to a given point on the actuator axis and  $V$  is the fixed length of the wire between  $A$  and  $F$ . We may assume that  $L_0, V, K$  are known constants. If we assume a small velocity of the end-effector the tension  $\tau$  in the wires are related to the wrench  $\mathcal{F}$  exerted on the platform by

$$\mathcal{F} = \mathbf{H}\tau \quad (3)$$

where  $\mathbf{H}$  is the transpose of the inverse jacobian matrix of the robot, which is pose dependent. The elements of  $\mathbf{H}$  are known analytical functions of the pose parameters. We define a reference frame  $\mathcal{R} = (O, \mathbf{x}, \mathbf{y}, \mathbf{z})$  and uses the coordinates in  $\mathcal{R}$  of a point  $C$  on the platform to parameterize the position of the end-effector. A mobile frame  $\mathcal{C}$ ,  $\mathbf{x}_m, \mathbf{y}_m, \mathbf{z}_m$  is attached to the platform and the Euler angles are used to represent the orientation of the platform. If  $\mathbf{n}_i$  is the unit vector giving the direction of wire  $i$ , then the  $i$ -th column  $H_i$  of  $\mathbf{H}$  may be written as

$$H_i^T = ((\mathbf{n}_i \quad \mathbf{CB}_i \times \mathbf{n}_i)) \quad (4)$$

### A. INVERSE KINEMATICS

In this section we will exhibit a method to calculate a control  $u$  that lie in the linear actuator motion range while ensuring that the wire tension will be positive and lower than a fixed threshold.

#### 1) INVERSE KINEMATICS ALGORITHMS:

For the inverse kinematics the pose of the end-effector is known and we will consider one wire to determine what should be its control  $u$ . First the length  $\rho$  may be determined: indeed the pose of the end-effector allows one to determine the coordinates of  $B$  in the reference frame, while the coordinates of  $A$  in the same frame are known. Hence the components of the vector  $\mathbf{AB}$  can be determined and  $\rho$  is the norm of this vector.

If the end-effector is submitted to known forces/torques it is possible to solve the linear system (3) in  $\tau$  using methods that are classical for wire-driven robot [4], [5], [9] ensuring that all elements of  $\tau$  are positive to avoid having slack wires. The control  $u$  is then calculated using (1,2) as

$$u = \frac{kL_0}{K(k - \tau)} - \frac{\rho + V}{K} \quad (5)$$

The drawback of this approach is that both  $u$  and  $\tau$  have limits (the linear actuator has a limited stroke and the  $\tau$  must be positive and also lower than a fixed threshold to avoid breaking the wire). With this method we may ensure that the limits on  $\tau$  are verified but cannot guarantee that the limits on  $u$  are also satisfied.

We may note that the wire tension may be expressed as

$$\tau = \frac{k(\rho + V - L_0 + Ku)}{\rho + V + Ku} \quad (6)$$

The constraints  $\tau < \tau_{max}$  may thus be written as  $Ku(k - \tau_{max}) < \tau_{max}(\rho + V) - k(\rho + V - L_0)$ . Usually  $k$  will much larger than  $\tau_{max}$  and hence  $k - \tau_{max}$  will be positive.

Consequently we may determine an upper bound for  $u$  as  $(\tau_{max}(\rho + V) - k(\rho + V - L_0))/(k - \tau_{max})$ . The same approach used for the constraint  $\tau > \tau_{min}$  allows one to determine a lower bound for  $u$ .

Using equations (1,2) equations (3) is now a non-linear system of 6 equations in the seven unknowns  $u$ , from which we must determine the solutions that are included between the lower and upper bounds that have been determined in the previous paragraph.

Inverse kinematics may be used in two cases:

- to move the robot from its current pose to another one, far from the current one. In that case the control  $u$  may be quite different from its current value
- during a robot motion in which case we are looking for solutions that are close to the current values of  $u$ . Here computation should be real time

The number of methods for solving a non-linear system are limited and we are using interval analysis with the library ALIAS that is developed in our laboratory. This approach allows one to determine solutions of a system which are included in a pre-defined domain and its computation time decreases with the size of the domain. These properties make the method appropriate for addressing the two above issues.

Different strategies may be used to solve the system (3):

- **Algorithm 1:** we consider (3) as an under-constrained system of 6 equations in the 7  $u_i$ . The ranges for the  $u_i$  will be either the actuator stroke or small intervals centered at the last known values for real time use and we will stop the algorithm as soon as a solution is found.
- **Algorithm 2:** we fix the value of one of the  $u_i$  and consider (3) as a square system of equations. The value of the fixed  $u_j$  may be determined by using the new value of  $\rho_j$  and equation (5) with a fixed value for  $\tau_j$  within the range  $[\tau_{min}, \tau_{max}]$ . Up to now we have not been able to determine if this system may have multiple solutions.

## 2) NUMERICAL EXAMPLES:

We are considering two possible designs of MARIONET with the anchor point coordinates presented in table I. The second design which differs only by the coordinates of the  $B$  points (indicated in parenthesis) and is called *T-platform* (also called 3-2-1 [8]). In this design there are only 3 different anchor points: one hosting three wire extremities and two attached each with 2 wires. More precisely wires (1,4,5) are connected at  $B_1$ , (2,6) at  $B_2$  and (3,7) at  $B_3$ .

We have identified the value of  $k$  by applying various known loads on a single wire and measuring its length. This has shown that Hooke's law was real close from the wire behavior and have obtained  $k = 383N$ . The amplification ratio of the actuator was  $K = 2$  and the mass of the platform is 0.02 kg. The allowed range for  $u$  is  $[-20,20]$  and is identical for all actuators.

Using Algorithm 1 and the range  $[-20,20]$  for all seven  $u$  we find a solution in 14 seconds on a Dell D620. If we restrict the range for the  $u$  to be centered at the last measured

TABLE I  
COORDINATES IN CENTIMETER OF THE ANCHOR POINTS  $A$  AND  $B$  WITH  
RESPECT TO THE REFERENCE AND MOBILE FRAME

	x	y	z
$A_1$	0	60	0
$A_2$	180	120	0
$A_3$	180	0	0
$A_4$	20	0	180
$A_5$	20	120	180
$A_6$	180	120	180
$A_7$	180	0	180
$B_1$	-10(-10)	-5(0)	0
$B_2$	10 (10)	-5 (10)	0
$B_3$	0 (10)	10 (-10)	0
$B_4$	-5 (-10)	-10 (0)	10 (0)
$B_5$	-5 (-10)	10 (0)	10 (0)
$B_6$	5 (10)	10	10 (0)
$B_7$	5 (10)	-10	10 (0)

value and fix their width to 1 mm, then a solution is found in 2 seconds, which is still too large for real time use.

For algorithm 2 we choose a value of  $u_1$  so that the wire tension is the middle of the allowed range for the tension. If the range for all  $u$  is  $[-20,20]$  the algorithm find a solution in 12 milliseconds. If we restrict the range for the  $u$  to be centered at the last measured value and fix the width of the range to 1 mm, then a solution is found in 2 milliseconds which is compatible with a real-time use.

Using a continuation method we may calculate the solution in  $u_j, j > 1$  for a varying  $u_1$ . For example we have considered a planar version of MARIONET with only 4 wires and we have calculated the solutions in  $u_2, u_3, u_4$  when  $u_1$  was varying from 0.1 to 10 cm (figure 3): it may be seen that the solutions are roughly linearly dependent upon  $u_1$ . This linear dependency was expected. Indeed the solution in

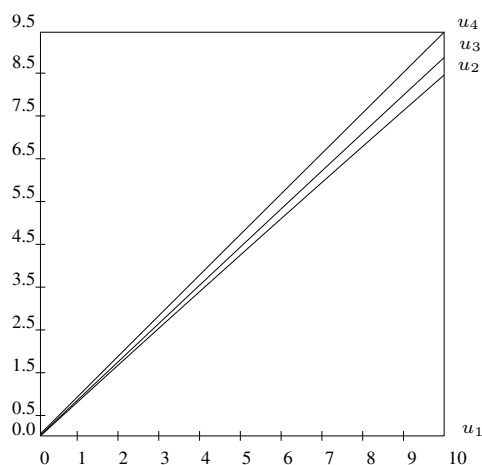


Fig. 3. Solution of the inverse kinematics for the control vector of a planar version of MARIONET when  $u_1$  is changing

$\tau_j, j > 1$  of equation (3) will be linear in  $\tau_1$ . Considering now equation (6) it may be seen that in the denominator we

have  $W = \rho + V \gg Ku$  and consequently we may write

$$\begin{aligned}\tau &= \frac{k(\rho + V - L_0 + Ku)}{W(1 + Ku/W)} \\ &\approx \frac{k(\rho + V - L_0 + Ku)}{W}\end{aligned}$$

Although  $\rho + V - L_0$  is a function of  $u$  it may be assumed that the change in the wire length will be sufficiently small so that this term will be approximately constant and consequently  $\tau$  will be a linear function of  $u$ . Hence  $\tau_j$  is a linear function of  $u_j$  but also of  $\tau_1$  which is linear in  $u_1$ : consequently  $u_j$  will be approximately linear in  $u_1$  as observed. Using this linear approximation we may update the search domain for the  $u_j$  to find a solution for an arbitrary  $u_1$ .

### III. FORWARD KINEMATICS

Being given the control vector  $u$  the unknowns are the seven  $\rho$  and the six pose parameters. We have six equations coming from the force/torque equilibrium (3) and seven equations relating the  $\rho$  to the pose parameters (i.e. the inverse kinematic equations of a classical parallel robots). Hence the forward kinematics is obtained as the solution of a square system of 13 non-linear equations. We may already assume that solving this system will not be an easy task as it amounts to solve at the same time the forward kinematics of a Gough platform (an already difficult task) and in addition the static equilibrium equations with elastic elements, a problem known to be difficult [6].

Using (1,2) we may calculate  $\rho$  as a function of  $\tau$ :

$$\rho = \frac{kL_0}{k - \tau} - V - Ku \quad (7)$$

Being given the limits  $[0, \tau_{max}]$  on  $\tau$  we may deduce a range for  $\rho$  from this equation. The orientation angles are naturally bounded while the coordinates of  $C$  should be such that  $C$  lie within the hull of the  $A$  anchor points.

#### A. Planar case

We may consider an almost planar case in which the planar end-effector is attached to the frame with only four wires and moves roughly within an horizontal plane. The motion of the end-effector will not be exactly planar as the compensation of gravity requires that the wires do not all lie in an horizontal plane. Furthermore with 4 wires we can control only 3 pose parameters and therefore cannot compensate the motion of the end-effector along the vertical direction.

Using a minimal parameter set for the pose we have 6 unknowns (the 3 coordinates of  $C$  and the rotation angles) and 4 equations for the inverse kinematics that involve the 4  $\rho$ . Mechanical equilibrium provides 6 additional equations and we end up with a system of 10 equations in 10 unknowns.

#### B. Spatial case

For the spatial case the system of equations may be transformed into a system of algebraic equations in order to apply classical solving algorithms such as Groebner basis or the continuation method. However these methods have a complexity which grows exponentially with the number of

unknowns and we know that they were already at their limits when studying the forward kinematics of classical Gough platform. As we are considering a much more complex problem it appears that these methods may not be appropriate without a difficult in-depth analysis of the system. Another method, that has been successful for the Gough platform [14], is based on interval analysis which requires to restrict the solving problem to determine solution within a bounded domain, which is the case as already mentioned.

However it has been shown that the chosen set of pose parameters was not the most appropriate for using interval analysis [14]. A better set of pose parameters is to use as unknowns the coordinates of 4 of the  $B$  points i.e. 12 unknowns, leading to a total of 19 unknowns (the 12 coordinates and the 7  $\rho$ ). If we assume that the selected set of  $B$  points is  $B_1, B_2, B_3, B_4$  (assuming that they are not coplanar) we know that we can find a set of 4 scalar constants  $l_1^j, l_2^j, l_3^j, l_4^j$  such that  $l_1^j + l_2^j + l_3^j + l_4^j = 1$  and with

$$OB_j = l_1^j OB_1 + l_2^j OB_2 + l_3^j OB_3 + l_4^j OB_4 \quad (8)$$

Hence the 7 inverse kinematic equations are functions only of the 12 coordinates of  $B_1, B_2, B_3, B_4$  while the 6 equations of (3) are functions of the same unknowns and of the  $\rho$ . Six additional equations may be obtained by writing that the distances between pairs of points in the set  $\{B_1, B_2, B_3, B_4\}$  are known scalars and we end up with a square system of 19 equations in 19 unknowns. Note that this method does not require to measure the tension in the wires, which is always a difficult task.

For the  $T$ -platform the pose parameters may be reduced to the 9 coordinates of  $B_1, B_2, B_3$  and we obtain a reduced system of 16 equations in 16 unknowns. Note that this system may be further simplified by considering the two inverse kinematic equations for two wires sharing the same anchor points  $B_i$ . These equations may be written as  $(x_i - xa_i)^2 + (y_i - ya_i)^2 + (z_i - za_i)^2 = \rho_i^2$  where  $x_i, y_i, z_i$  are the coordinates of  $B_i$  and  $xa_i, ya_i, za_i$  the coordinates of the anchor point on the base. The difference between these two equations is linear in  $x_i, y_i, z_i$  and as 4 independent pairs of such equations may be considered, we may solve them to determine 4 unknowns, thereby reducing the number of unknowns to 12. However in the numerical examples we have not considered this reduced system.

Note that equation (8) may also be used in the planar case with a total of 13 unknowns (the 9 coordinates of the  $B_i$  and the four  $\rho$ ) and a total of 13 equations (4 from the inverse kinematics, 6 from the mechanical equilibrium and 3 from the distances between  $B_1, B_2, B_3$ ).

#### 1) NUMERICAL EXAMPLES:

In a first part of our experiment we have considered the problem of finding all the solutions of the forward kinematic problem. It appears quickly that the solving time was heavily sensitive on the bounds given for the  $\rho$  and hence on the allowed  $\tau_{max}$ . We have considered as possible value for  $\tau_{max}$  either 10N or 20N. Various tests were performed with

different values for the  $u_i$ .

**Spatial case**

The ranges for the  $x_i, y_i, z_i$  were fixed respectively to  $[30,160], [30,110], [0, 170]$ . For the T-platform with the bounds for  $\tau$  fixed to  $[0,10]$  N we get a single solution for the forward kinematics in about 10 minutes while for  $\tau$  in  $[0,20]$  two solutions are found in about one hour. These solutions are presented in figure 4, 5. It may be seen that the

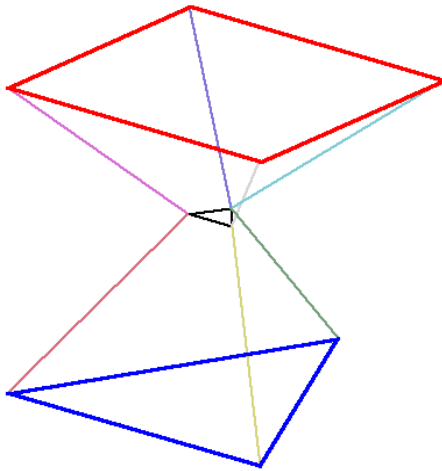


Fig. 4. First solution of the forward kinematics for the T-platform

main transformation between the two solutions is a rotation around the main branch of the "T" although a translation of the anchor point  $B_1$  with 3 wires is also observed. For the first solution the coordinates of this are (85.14, 54.78, 100.36) and (93.45, 55.65, 101.6) for the second solution.

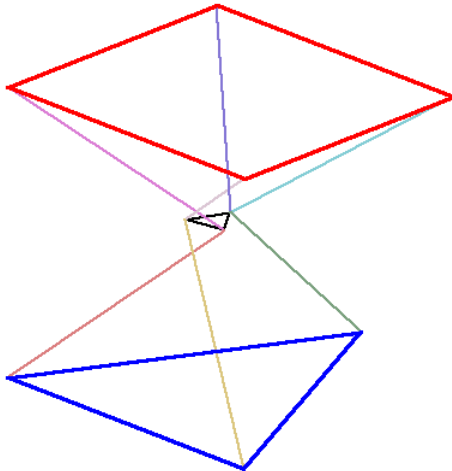


Fig. 5. Second solution of the forward kinematics for the T-platform

For the general platform and  $\tau_{max} = 10N$  we have been able to show that there was a single solution. For  $\tau_{max} = 20N$  we have shown that there was at least 2 solutions (presented in figure 6, 7) but we have been unable

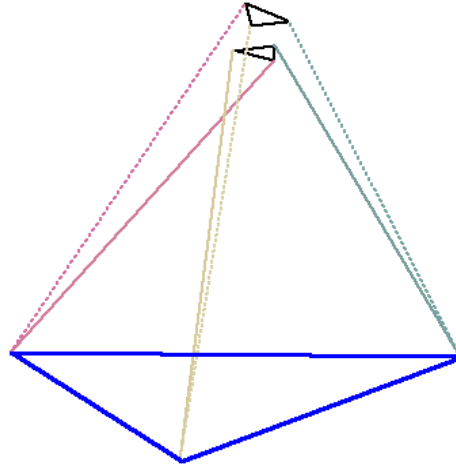


Fig. 6. The location of the 3 lower points of the end-effector

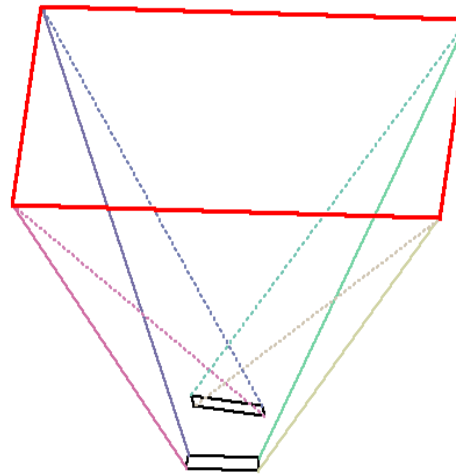


Fig. 7. The location of the 4 upper points of the end-effector

to complete the calculation. For real time calculation we have used the inverse kinematics to determine the control vector for a given pose  $P$  and then we have added to each element of this vector a random perturbation in the range  $[-1,1]$  mm. Assuming that the location of the  $B_i$  points were in a range centered at the location of  $B_i$  for the pose  $P$  with a width of 1 mm we are able to prove that there is a single solution of the forward kinematics in the box in a computation time between 5 and 7 ms. It must be noted that in our trial the Newton scheme was able to converge to the correct solution in less than 1 ms.

**Planar case**

The planar case involves solving a system of 13 equations in 13 unknowns if the full pose of the end-effector has to be determined. If we use a large value of  $\tau_{max}$  we have found an example with 4 solutions (figure 8) that have been determined in 22 minutes. If we restrict  $\tau_{max}$  to 20 and 10 N only 2 solutions are valid and are found in a computation

of 12 minutes and 7 minutes respectively.

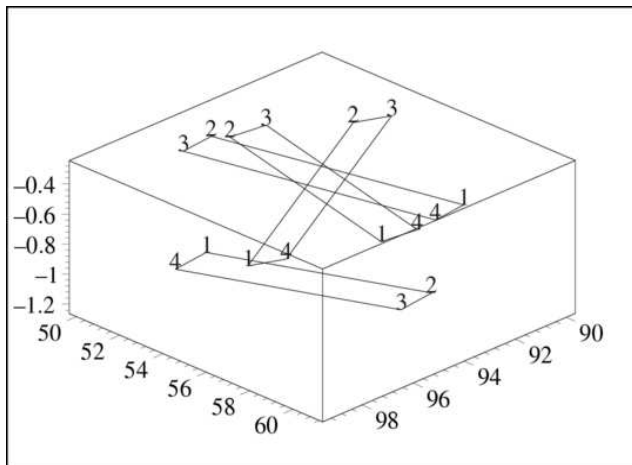


Fig. 8. The four different poses that are solution of a forward kinematics problem for the almost planar robot

The maximal vertical deviation from the manipulator plane is 1.22 mm while the minimal one is 0.38 mm. These small deviations indicate that it may be interesting to look at the full planar case, assuming no motion along the vertical axis. In that case we get a system in 10 unknowns (the 6 coordinates of the three  $B_i$  points and the 4  $\rho$ ) in 10 equations (3 for the distances between the  $B_i$ , 4 for the inverse kinematic and 3 mechanical equilibrium equations). Assuming a large  $\tau_{max}$  4 solutions are found in 1mn 20s while 4 solutions are also found for  $\tau_{max} = 20$  in 29s and 2 solutions for  $\tau_{max} = 10$  in 3s.

If we compare the solutions obtained for the 6D case to the solutions of the planar case in term of mean distances between the four corresponding anchor points of the end-effector we find that the maximal mean distance is 5.3 cm while the minimal one is 0.16 cm. Hence the planar case may be used to define restricted search spaces for the 6D case allowing a lower computation time. Our test have shown that by using this strategy the computation time of the 6D case may be reduced to less than 30 seconds.

#### IV. CONCLUSION

We have considered the kinematic issue regarding a new wire-driven parallel robot having an original actuation scheme, taking into account the elasticity of the wire. Compared to parallel robot with rigid links, kinematics is more complex for wire-driven robot. Inverse kinematics is however still manageable, even in real-time. As for all parallel robot the forward kinematics is much more complex. A real time treatment is possible even in the most general case but finding all solutions is computer intensive. It appears that the solutions exhibit some complicated symmetries and a further understanding of these symmetries may allow to reduce the search space, thereby leading to a large reduction in computation time. The maximal number of solutions is also an open issue while the theoretical results provided in this

paper will be experimentally validated with our prototype in the very near future.

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