

The Adam Hilger Series on Optics and Optoelectronics

Laser Resonators and the Beam Divergence Problem

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