# Latin Dances Revisited: New Analytic Results of Salsa20 and ChaCha 

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#### Abstract

In this paper, we propose new attacks on 9-round Salsa20 and 8-round ChaCha. We constructed a distinguisher of double-bit differentials to improve Aumasson's single-bit differential cryptanalysis. We searched for correlations using a PC, and found strong correlations in 9-round Salsa20 and 8-round ChaCha. The complexities of the introduced attacks are $2^{16}$ in 9-round Salsa20 and 2 in 8 -round ChaCha, which are much less than the complexities of an exhaustive key search and existing attacks on those ciphers. The results show that an adversary can distinguish keystream bits from random bits using a few input and output pairs of an initial keys and initial vectors. This method has potential to apply to a wide range of stream ciphers; a double-bit correlation would be found in case that no single-bit correlation is found.


Keywords: Stream cipher, Salsa20, ChaCha, eSTREAM.

## 1 Introduction

Efficient implementations of stream ciphers are useful in any application which requires high-speed encryption, such as SSL[13] and WEP[14]. The stream cipher project of ECRYPT(eSTREAM) [11] was launched to identify new stream ciphers that realizes secure and high-speed encryption. This project ended with a proposal of a list of new eight algorithms in 2008, and one was removed from the list in 2009[2] due to a new vulnerability of the cipher. Four algorithms are assumed to apply to software implementations, and remaining three are for lightweight hardware implementations.

Salsa20, one of algorithms for software implementations, was proposed by Bernstein[5] in 2005, and the cipher is the finalist of the eSTREAM. Salsa20 offers a simple, clean, and scalable design and is suitable for software implementations. Bernstein advocated use of 8,12 and 20 round versions of Salsa20. However, in eSTREAM, the 12 -round version was adopted due to the balance, combining a very nice performance profile with what appears to be a comfortable margin for security.

More recently, he has proposed the ChaCha[3], a new variant of the Salsa20 family. ChaCha follows the same design principles as Salsa20, and a difference between Salsa20 family and ChaCha is the core function; the core function of ChaCha realizes faster diffusion than that of Salsa20 family. ChaCha achieves faster software speed than Salsa20 in some platforms.

Related work. There are many ciphers proposed in eSTREAM, and some have been broken by distinguishing attacks. NLS proposed by Hawkes et al[15], is an extended version of SOBER[16]. NLS is a software-oriented cipher based on simple 32-bit operations (such as 32 -bit XOR and addition modulo $2^{32}$ ), and is related to small fixed arrays. This stream cipher was broken by a distinguishing attack [8] and a Crossword Puzzle Attack [7] which is a variant of the distinguishing attack. LEX[6] has a simple design and based on AES. A variant of the distinguishing attack[10] was found on LEX. Yamb [17] is a synchronous encryption algorithm that allows keys of any length in the range 80-256 bits and allows initial vectors IV of any length in the range 32-128 bits. Yamb was broken by a distinguishing attack proposed by Wu et al.[18]. Some other stream ciphers have been broken by distinguishing attacks [19|20].

Some independent cryptanalyses on Salsa20 have been published, to report keyrecovery attacks for its reduced versions with up to 8 rounds, while Salsa20 has a total of 20 rounds. Previous attacks on Salsa20 used a distinguishing attack exploiting a truncated differential over 3 or 4 rounds. The first attack was presented by Crowley[9], and it was claimed that an adversary could break the 5-round version of Salsa20 within $3^{165}$ trials using a 256-bit key. Later, a four round differential was exploited by Fischer et al.[12] to break 6 rounds in $2^{177}$ trials and by Tsnunoo et al.[21] to break 7 rounds in about $2^{190}$ trials.

The best attack is proposed by Aumasson et al.[22] so far, and it covers the 8 -round version of Salsa20 with an estimated complexity of $2^{251}$. Regarding the 128-bit key, Aumasson proposed key-recovery attacks for reduced versions with up to 7 rounds[22]. Priemuth-Schmid proposed a distinguishing attack using slid pairs[23], but Bernstein showed that time complexity of the attack is higher than brute force attack[4].

For ChaCha, Aumasson attacked the 6 -round version with an estimated complexity of $2^{139}$ and the 7 -round version with an estimated complexity of $2^{248}$ using a 256 -bit key. Regarding the 128-bit key, Aumasson proposed key-recovery attacks for reduced versions with up to 7 rounds with an estimated complexity of $2^{107}$ [22].

These attacks are single-bit differential attacks, a type of correlation attacks. In this method, an adversary chooses the input pair $X, X^{\prime}$ and observes the output pair $Z, Z^{\prime}$, where there is a differential in one bit between $X$ and $X^{\prime}$. Then, the adversary collects many output pairs by changing input pair and observes the one bit differential from the output pair. If the position of the input differential correlates strongly with the position of output differential, the adversary could distinguish real keystream from a random bit stream. Additionally, it was indicated a strong correlation from his experimental results.

Contribution. In this paper, we propose a new attack on 9-round Salsa20 and 8-round ChaCha. We construct a distinguisher using double-bit differentials to improve Aumasson's method, called single-bit differential cryptanalysis[1]. In our attack, the adversary chooses the input pair $X, X^{\prime}$ with a one-bit differential in the same way for a singlebit differential. Then, the adversary collects many output pairs by changing the input pair and observing the double-bit difference from the output pair. Finally, the adversary observes a correlation of the double-bit of the output pair and distinguishes keystream from the random bits. We searched correlations to compute 2-3 days using a PC, and
found strong correlations in 9-round Salsa20 and 8-round ChaCha. This results suggest that the double-bit differential cryptanalysis is more powerful attack than the single-bit differential cryptanalysis and it reduces total cost of attacks on Salsa20 and ChaCha. The double-bit differential cryptanalysis has potential to apply a wide range of stream ciphers; a double-bit correlation may be found in case that even if no single-bit correlation is found.

The rest of the paper is organized as follows; in section 2, we describe specifications of Salsa20 and ChaCha. Next, we define the scenario of a distinguishing attack and explain details of the distinguishing attack in section 3. Then, we demonstrate that the attack achieves a reasonable level of efficacy from the experimental results in section 4. Finally, we conclude this paper in section 5.

## 2 Latin Dances

In this section, we describe the specifications of Salsa20[5] and ChaCha[3].

### 2.1 Salsa20

Algorithm 1 shows Salsa20 algorithm. The stream cipher Salsa20 operates on 32-bit words, takes as input a 256 -bit key $k=\left(k_{0}, k_{1}, \ldots, k_{7}\right)$ or 128-bit key $k=\left(k_{0}, k_{1}, \ldots, k_{3}\right)$ and a 64 -bit nonce $v=\left(v_{0}, v_{1}\right)$, and produces a sequence of 512-bit keystream blocks. The $i$-th block is the output of the Salsa20 function that takes as input the key, the nonce, and a 64-bit counter $t=\left(t_{0}, t_{1}\right)$ corresponding to the integer $i$. This function acts on the $4 \times 4$ matrix of 32 -bit words written as:

$$
\begin{aligned}
& X=\left(\begin{array}{llll}
x_{0} & x_{1} & x_{2} & x_{3} \\
x_{4} & x_{5} & x_{6} & x_{7} \\
x_{8} & x_{9} & x_{10} & x_{11} \\
x_{12} & x_{13} & x_{14} & x_{15}
\end{array}\right)=\left(\begin{array}{llll}
\tau_{0} & k_{0} & k_{1} & k_{2} \\
k_{3} & \tau_{1} & v_{0} & v_{1} \\
i_{0} & i_{1} & \tau_{2} & k_{4} \\
k_{5} & k_{6} & k_{7} & \tau_{3}
\end{array}\right) \text { or, } \\
& X=\left(\begin{array}{llll}
x_{0} & x_{1} & x_{2} & x_{3} \\
x_{4} & x_{5} & x_{6} & x_{7} \\
x_{8} & x_{9} & x_{10} & x_{11} \\
x_{12} & x_{13} & x_{14} & x_{15}
\end{array}\right)=\left(\begin{array}{cccc}
\sigma_{0} & k_{0}^{\prime} & k_{1}^{\prime} & k_{2}^{\prime} \\
k_{3}^{\prime} & \sigma_{1} & v_{0} & v_{1} \\
i_{0} & i_{1} & \sigma_{2} & k_{0}^{\prime} \\
k_{1}^{\prime} & k_{2}^{\prime} & k_{3}^{\prime} & \sigma_{3}
\end{array}\right),
\end{aligned}
$$

where $\sigma$ and $\tau$ are constants dependent on the key length.
Then a keystream block $Z$ is defined as:

$$
Z=X+X^{20}
$$

where $X^{r}=\operatorname{Round}^{r}(X)$ with the round function of Salsa20 and + is word-wise addition modulo $2^{32}$. If $Z=X+X^{r}$, it is called " $r$-round Salsa20". A round function is called a doubleround function, and it consists of a columnround function followed by a rowround function. The doubleround function of Salsa20 is repeated 10 times. A vector $\left(x_{0}, x_{1}, x_{2}, x_{3}\right)$ of four words is transformed into $\left(z_{0}, z_{1}, z_{2}, z_{3}\right)$ by calculating as:

```
Algorithm 1. Algorithm of Salsa20
INPUT: Initial matrix \(X, r \in \mathbb{N}\)
OUTPUT: \(Z=X+X^{r}\)
    \(X^{\prime} \leftarrow X\)
    for \(l=0\) up to \(\frac{r}{2}\) do
        \(\left(x_{0}^{\prime}, x_{1}^{\prime}, x_{2}^{\prime}, x_{3}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{0}^{\prime}, x_{1}^{\prime}, x_{2}^{\prime}, x_{3}^{\prime}\right) / * 3-6\) :Colmnround */
        \(\left(x_{5}^{\prime}, x_{6}^{\prime}, x_{7}^{\prime}, x_{4}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{5}^{\prime}, x_{6}^{\prime}, x_{7}^{\prime}, x_{4}^{\prime}\right)\)
        \(\left(x_{10}^{\prime}, x_{11}^{\prime}, x_{8}^{\prime}, x_{9}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{10}^{\prime}, x_{11}^{\prime}, x_{8}^{\prime}, x_{9}^{\prime}\right)\)
        \(\left(x_{15}^{\prime}, x_{12}^{\prime}, x_{13}^{\prime}, x_{14}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{15}^{\prime}, x_{12}^{\prime}, x_{13}^{\prime}, x_{14}^{\prime}\right)\)
        \(\left(x_{0}^{\prime}, x_{4}^{\prime}, x_{8}^{\prime}, x_{12}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{0}^{\prime}, x_{4}^{\prime}, x_{8}^{\prime}, x_{12}^{\prime}\right) \quad / * 7-10\) :Rowround */
        \(\left(x_{5}^{\prime}, x_{9}^{\prime}, x_{13}^{\prime}, x_{1}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{5}^{\prime}, x_{9}^{\prime}, x_{13}^{\prime}, x_{1}^{\prime}\right)\)
        \(\left(x_{10}^{\prime}, x_{14}^{\prime}, x_{2}^{\prime}, x_{6}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{10}^{\prime}, x_{14}^{\prime}, x_{2}^{\prime}, x_{6}^{\prime}\right)\)
        \(\left(x_{15}^{\prime}, x_{[3}^{\prime}, x_{7}^{\prime}, x_{11}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{15}^{\prime}, x_{[3}^{\prime}, x_{7}^{\prime}, x_{11}^{\prime}\right)\)
    end for
    return \(X+X^{\prime}\)
```

$$
\begin{array}{r}
z_{1}=x_{1} \oplus\left(\left(x_{0}+x_{3}\right) \lll 7\right) \\
z_{2}=x_{2} \oplus\left(\left(z_{1}+x_{0}\right) \lll 9\right) \\
z_{3}=x_{3} \oplus\left(\left(z_{2}+z_{1}\right) \lll 13\right) \\
z_{0}=x_{0} \oplus\left(\left(z_{3}+z_{2}\right) \lll 18\right)
\end{array}
$$

This nonlinear operation is called a quarterround function and it is a basic part of the columnround function where it is applied to columns $\left(x_{0}, x_{4}, x_{8}, x_{12}\right),\left(x_{5}, x_{9}, x_{13}, x_{1}\right)$, ( $x_{10}, y_{14}, y_{2}, y_{6}$ ) and ( $y_{15}, y_{3}, y_{7}, y_{11}$ ), and then rowround function transforms rows ( $x_{0}, x_{1}$, $\left.x_{2}, x_{3}\right),\left(x_{4}, x_{5}, x_{6}, x_{7}\right),\left(x_{8}, x_{9}, x_{10}, x_{11}\right)$, and $\left(x_{12}, x_{13}, x_{14}, x_{15}\right)$.

### 2.2 ChaCha

Algorithm 2 shows ChaCha algorithm. ChaCha is similar to Salsa20 except the following two points. First, the composition of the quarterround function is defined as below.

$$
\begin{array}{lll}
z_{0}=z_{0}+z_{1}, & z_{3}=z_{3} \oplus z_{0}, & z_{3}=z_{3} \lll 16, \\
z_{2}=z_{2}+z_{3}, & z_{1}=z_{1} \oplus z_{2}, & z_{1}=z_{1} \lll 12, \\
z_{0}=z_{0}+z_{1}, & z_{3}=z_{3} \oplus z_{0}, & z_{3}=z_{3} \ll 8, \\
z_{2}=z_{2}+z_{3}, & z_{1}=z_{1} \oplus z_{2}, & z_{1}=z_{1} \lll 7
\end{array}
$$

Second, the composition of the initial matrix defined as below.

$$
X=\left(\begin{array}{cccc}
\sigma_{0} & \sigma_{1} & \sigma_{2} & \sigma_{3} \\
k_{0}^{\prime} & k_{1}^{\prime} & k_{2}^{\prime} & k_{3}^{\prime} \\
k_{0}^{\prime} & k_{1}^{\prime} & k_{2}^{\prime} & k_{3}^{\prime} \\
v_{0} & v_{1} & i_{0} & i_{1}
\end{array}\right) \text {, or }\left(\begin{array}{llll}
\tau_{0} & \tau_{1} & \tau_{2} & \tau_{3} \\
k_{0} & k_{1} & k_{2} & k_{3} \\
k_{4} & k_{5} & k_{6} & k_{7} \\
v_{0} & v_{1} & i_{0} & i_{1}
\end{array}\right)
$$

```
Algorithm 2. Algorithm of ChaCha
INPUT: Initial matrix \(X, r \in \mathbb{N}\)
OUTPUT: \(Z=X+X^{r}\)
    \(X^{\prime} \leftarrow X\)
    for \(l=0\) up to \(\frac{r}{2}\) do
        \(\left(x_{0}^{\prime}, x_{4}^{\prime}, x_{8}^{\prime}, x_{12}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{0}^{\prime}, x_{4}^{\prime}, x_{8}^{\prime}, x_{12}^{\prime}\right) / * 3-6:\) Colmnround */
        \(\left(x_{1}^{\prime}, x_{5}^{\prime}, x_{9}^{\prime}, x_{13}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{1}^{\prime}, x_{5}^{\prime}, x_{9}^{\prime}, x_{13}^{\prime}\right)\)
        \(\left(x_{2}^{\prime}, x_{6}^{\prime}, x_{10}^{\prime}, x_{14}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{2}^{\prime}, x_{6}^{\prime}, x_{10}^{\prime}, x_{14}^{\prime}\right)\)
        \(\left(x_{3}^{\prime}, x_{7}^{\prime}, x_{11}^{\prime}, x_{15}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{3}^{\prime}, x_{7}^{\prime}, x_{11}^{\prime}, x_{15}^{\prime}\right)\)
        \(\left(x_{0}^{\prime}, x_{5}^{\prime}, x_{10}^{\prime}, x_{15}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{0}^{\prime}, x_{5}^{\prime}, x_{10}^{\prime}, x_{15}^{\prime}\right) / * 7-10\) :Rowround */
        \(\left(x_{1}^{\prime}, x_{6}^{\prime}, x_{11}^{\prime}, x_{12}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{1}^{\prime}, x_{6}^{\prime}, x_{11}^{\prime}, x_{12}^{\prime}\right)\)
        \(\left(x_{2}^{\prime}, x_{7}^{\prime}, x_{8}^{\prime}, x_{13}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{2}^{\prime}, x_{7}^{\prime}, x_{8}^{\prime}, x_{13}^{\prime}\right)\)
        \(\left(x_{3}^{\prime}, x_{4}^{\prime}, x_{9}^{\prime}, x_{14}^{\prime}\right) \leftarrow\) quarterround \(\left(x_{3}^{\prime}, x_{4}^{\prime}, x_{9}^{\prime}, x_{14}^{\prime}\right)\)
    end for
    return \(X+X^{\prime}\)
```


## 3 Attack on Latin Dances

In this section, we discuss a distinguishing attack on Salsa20 and ChaCha. First, we define the semi-regular distinguisher and explain construction of the distinguisher. Next, we propose a distinguishing attack using double-bit differentials. Finally, we analyze the attack based on experimental results using a PC and estimate the number of keystream bits required for the attack and time complexity of the attack.

### 3.1 Types of Distinguisher

Three types of a distinguisher are known[24] as below.

1. Regular Distinguisher.

The adversary selects a single key/IV randomly and produces keystream bits, seeded by the chosen key/IV, which is long enough to distinguish it from a random bit stream with a high probability.
2. Prefix Distinguisher.

The adversary uses many randomly chosen key/IV's rather than a single key and a few specified bytes from each of the keystream bits generated by those key/IV's.
3. Hybrid Distinguisher.

The adversary uses many key/IV's and for each key/IV the adversary collects long keystream bits.

In this paper, we define the Semi-regular Distinguisher as follows;
Semi-regular Distinguisher. An adversary uses a single random key and enough randomly chosen IVs to distinguish keystream from random bits with a high probability. The adversary's ability is intermediate between a regular distinguisher and prefix distinguisher.

### 3.2 Construction of Distinguisher

The adversary chooses a key at random. Then the adversary randomly generates IV and inputs matrix $X, X^{\prime}$ that has a difference of $i$-th bit. The number of inputs is $m$. Output sequences are $\left\{z_{0}, \cdots, z_{m-1}\right\},\left\{z_{0}^{\prime}, \cdots, z_{m-1}^{\prime}\right\}$, where $z_{i}, z_{i}^{\prime} \in\{0,1\}$. After that, the adversary observes $t_{i}=z_{i} \oplus z_{i}^{\prime}$, $(0 \leq i<m)$, where $\oplus$ is exclusive-or.

If $\left\{z_{0}, \cdots, z_{m-1}\right\},\left\{z_{0}^{\prime}, \cdots, z_{m-1}^{\prime}\right\}$ were random bit sequences, the probabilities:

$$
\begin{aligned}
\operatorname{Pr}\left[t_{i}=1\right] & =\operatorname{Pr}\left[t_{i}=0\right] \\
& =\frac{1}{2},(0 \leq i<m)
\end{aligned}
$$

are hold.
If $\left\{z_{0}, \cdots, z_{m-1}\right\}$ and $\left\{z_{0}^{\prime}, \cdots, z_{m-1}^{\prime}\right\}$ were keystream bits from a stream cipher, we obtain the following equations:

$$
\begin{aligned}
& \operatorname{Pr}\left[t_{i}=1\right]=\frac{1}{2}\left(1+\varepsilon_{d}\right) \\
& \operatorname{Pr}\left[t_{i}=0\right]=\frac{1}{2}\left(1-\varepsilon_{d}\right),(0 \leq i<m)
\end{aligned}
$$

In this instance, the number of keystream bits required for a distinguishing attack is $O\left(\varepsilon_{d}^{-2}\right)$, where $\varepsilon_{d}$ is the differential bias explained in Section 3.3 If $\varepsilon_{d}$ is large enough, an adversary can distinguish keystream bits from random bit sequences. For example $\varepsilon_{d}$ is sufficiently large for 7 -round Salsa20 to distinguish keystream bits[22]. We propose a double-bit distinguisher for 9 -round Salsa20 and 8-round ChaCha in the later section.

### 3.3 Distinguishing Attack Using Double-Bit Differentials

In this section, we propose a distinguishing attack using double-bit differentials, which extends the single-bit distinguishing attack in[22]. Let $x_{i}, x_{i}^{\prime}$ be the $i$-th word of the initial matrix $X, X^{\prime}$, and $j$-th bit of $x_{i}$ is denoted $\left[x_{i}\right]_{j}$. Then, let $\left[\Delta_{i}^{r}\right]_{j}$ be a differential of $j$-th bit of $i$-th word after $r$ rounds, where $\left[\Delta_{i}^{0}\right]_{j}=\left[x_{i}\right]_{j} \oplus\left[x_{i}^{\prime}\right]_{j}$. In[22], the differential of $r$ rounds output under $\left[\Delta_{i}^{0}\right]_{j}=1$ is denoted $\left(\left[\Delta_{p}^{r}\right]_{q}\left[\left[\Delta_{i}^{0}\right]_{j}\right){ }^{1}\right.$, and a single-bit differential is defined by

$$
\operatorname{Pr}\left(\left[\Delta_{p}^{r}\right]_{q} \mid\left[\Lambda_{i}^{0}\right]_{j}\right)=\frac{1}{2}\left(1+\left|\varepsilon_{s}\right|\right)
$$

The bias $\varepsilon_{s}$ represents the strength of the correlations between one bit in input and one bit in output. If a keystream bit is pseudorandom, $\varepsilon_{s}$ must come close to 0 . Aumasson indicated significant differentials between keystream bits and random bit sequences in 8 rounds of Salsa20 and 7 rounds of ChaCha. However, he could not find a significant differential, where there were more than 9 rounds and 7 rounds.

[^0]In a distinguishing attack using double-bit differentials, the bias $\varepsilon_{d}$ of the output differential is defined by

$$
\operatorname{Pr}\left(\left(\left[\Delta_{p}^{r}\right]_{q} \oplus\left[\Delta_{s}^{r}\right]_{t}=1\right)\left[\left[\Delta_{i}^{0}\right]_{j}\right)=\frac{1}{2}\left(1+\left|\varepsilon_{d}\right|\right)\right.
$$

When $\varepsilon_{s}$ is zero, pairs of $(p, q),(s, t)$ have no significant single-bit differentials. That means zero and one appear with a probability of $\frac{1}{2}$. In other words, a single-bit differential only indicates a frequency of $\left[\Delta_{p}^{r}\right]_{q}=1$. There is a possibility that a correlation exists between cases of $\left[\Lambda_{p}^{r}\right]_{q}=1$ and $\left[\Delta_{s}^{r}\right]_{t}=1$. If the bias $\varepsilon_{d} \neq 0$, a double-bit differential indicates such correlations.

In concrete terms, an adversary chooses $\left[\Delta_{i}^{0}\right]_{j}$ from a nonce $v$ or a counter $i$; therefore, $i$ and $j$ for Salsa20 are chosen within the ranges $7 \leq i<11,0 \leq j<32$. In ChaCha, $i$ and $j$ are chosen within the ranges $12 \leq i<16,0 \leq j<32$. The bias $\varepsilon_{d}$ is dependent on keys $k$, and it is difficult to calculate all values of $\varepsilon_{d}$ due to huge time complexity. The value $\varepsilon_{d}$ can be guessed as a median value $\varepsilon_{d}^{\star}$ as follows;

$$
\operatorname{Pr}_{k}\left(\left(\left[\Delta_{p}^{r}\right]_{q} \oplus\left[\Delta_{s}^{r}\right]_{t}=1\right) \mid\left[\Delta_{i}^{0}\right]_{j}\right)=\frac{1}{2}\left(1+\left|\varepsilon_{d}^{\star}\right|\right)
$$

## 4 Experimental Results

In this section, we discuss the experimental results for distinguishing attacks using double-bit differentials. In Section 4.1, we present an algorithm searching for the maximum double-bit differential. Then, we demonstrate efficacy of our method using experimental results.

### 4.1 Algorithm

In a distinguishing attack using double-bit differentials, the adversary previously has obtained the positions of the maximum double-bit differential in order to distinguish keystream bits from random bits. First, the adversary chooses a key $K$ at random and fixes it. Then, the adversary generates many input pairs which have a one-bit differential each other. After the calculation of the output pair corresponding to each input, the adversary searches all combinations of output positions for double-bit differentials, and calculate the median value to collect these differentials. Finally, the adversary calculates the averages of each median value with randomly changing keys.

Algorithm 3 shows details of the search algorithm. This algorithm requires $r, \alpha$ and $\beta \in \mathbb{N}$, where $r$ is a number of round, $\alpha$ is the number of trials required to calculate the average, and $\beta$ is the number of trials required to calculate the median. The balance between the precision of outputs and the time complexity depends on these parameters. We discuss the balance and our adoptions in section 4.2. After the choice of $K$ at step 3, the chosen key is used for the next loop (from step 4 to step 15). In the loop, we calculate the median values of the double-bit differential for fixed key $K$ are calculated. Values

```
Algorithm 3. Search for double-bit differentials
INPUT: \(r, \alpha, \beta \in \mathbb{N}\)
OUTPUT: Average of double-bit differential of \(r\) round
    Initialize all count by zero
    for \(l=0\) up to \(\alpha\) do
        Choose key \(K\) at random
        for \(k=0\) up to \(\beta\) do
            for all \(\left[U_{i}^{0}\right]_{j}\) such that \(i, j\) in controllable value do
            Choose \(X, X^{\prime}\) at random where \(X \oplus X^{\prime}=\left[\Delta_{i}^{0}\right]_{j}=1\)
            \(Z \leftarrow X+X^{r}\)
            \(Z^{\prime} \leftarrow X^{\prime}+X^{\prime r}\)
            for all \(\left[\Delta_{p}^{r}\right]_{q}\) such that \(0 \leq p<16,0 \leq q<32\) do
                    for all \(\left[\Delta_{s}^{r}\right]_{t}\) such that \(0 \leq s<16,0 \leq t<32\) do
                count \(_{p, q, r, s}[j] \leftarrow\left(\left[\Delta_{s}^{r}\right]_{t} \oplus\left[\Delta_{p}^{r}\right]_{q}\right)\)
                    end for
            end for
            end for
        end for
        median \(_{p, q, r, s}[i] \leftarrow\) median value of \(\operatorname{count}_{p, q, r, s}\) for all \((p, q, r, s)\)
    end for
    average \(_{p, q, r, s} \leftarrow\) average of median \(_{p, q, r, s}[i]\) for all \(i,(p, q, r, s)\)
    return average \(_{p, q, r, s}\)
```

[ $\left.\Lambda_{i}^{0}\right]_{j}$ for all $i, j$ of controllable value have to be chosen at step 5 , where controllable values are nonce or counter in the initial matrix (see Section 2, Section 3.2). Hence, in the case of Salsa20, we choose $i$ and $j$ within the ranges $7 \leq i<11,0 \leq j<32$, or in ChaCha, we choose them within the ranges $12 \leq i<16,0 \leq j<32$. From step 6 to step 13, we calculate the double-bit differential using XOR operation; the computational cost of these steps is dominant in the whole algorithm. The time complexity of the step is $\left(2^{9}\right)^{2} / 2=2^{17}$. Remaining computational costs of the algorithm is calculated as follows; the number of iterations of the loop from step 5 is $2^{7}$, and the number of iterations of the loop from step 2 and 4 is $\alpha \beta$. Thus, the total cost of the algorithm is $\alpha \beta \cdot 2^{24}$.

### 4.2 Results

In the distinguishing attack using double-bit differentials, we need to find the maximum values of $\varepsilon_{d}$. Accordingly, we conducted an experiment shown in Algorithm 3 to find the maximum values for Salsa20 and ChaCha. We input $\alpha=2^{12}$ and $\beta=2^{12}$. The total time complexity of the experiment is $2^{48}$ : the space of IV is 128 bits $\left(=2^{7}\right)$, the combination of output is $2^{18} / 2=2^{17}$, and the number of trials is $2^{24}$. A Intel Core i7 3.3 GHz PC requires 2 days computation for the experiment.

We sampled $2^{24}$ output pairs for each per one input pair. Let $\sigma$ be the variance of samples, $N$ be the average and $N^{\prime}$ is the population mean of $\left[\Lambda_{s}^{r}\right]_{t} \oplus\left[\Lambda_{p}^{r}\right]_{q}$, where $\sigma \approx \sqrt{N}$. The confidence interval is $\left[N^{\prime}-\theta, N^{\prime}+\theta\right]$ and $\theta \approx 2^{-12}$, where the confidence

Table 1. Salsa20 Distinguisher

| Round | key length | [ $\left[4_{i}^{0}\right]_{j}$ | $\left[\Delta_{p}^{r}\right]_{q}$ | $\left[4_{s}^{r}\right]_{t}$ | $\varepsilon_{d}^{\star}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | 256 | [ $\left[{ }_{6}^{0}\right]_{17}$ | $\left[4_{1}^{9}\right]_{15}$ | $\left[\Delta_{11}^{9}\right]_{22}$ | 0.003112 |
| 9 | 256 | $\left[4_{6}^{0}\right]_{17}$ | $\left[\Delta_{11}^{9}\right]_{22}$ | $\left[4_{1}^{9}\right]_{15}$ | 0.003112 |
| 9 | 256 | $\left[4_{8}^{0}\right]_{11}$ | $\left[4_{2}^{9}\right]_{16}$ | $\left[4_{7}^{9}\right]_{25}$ | 0.002292 |
| 9 | 256 | $\left[4_{8}^{0}\right]_{11}$ | [ $\left.4_{7}^{9}\right]_{25}$ | $\left[4_{2}^{9}\right]_{16}$ | 0.002292 |
| 9 | 256 | $\left.\left[{ }_{7}^{0}\right]_{19}\right]_{19}$ | $\left[4_{1}^{9}\right]_{26}$ | $\left[\Delta_{10}^{9}\right]_{18}$ | 0.001832 |
| 9 | 256 | $\left[4_{7}^{0}\right]_{19}$ | $\left[\Delta_{10}^{9}\right]_{18}$ | $\left[4_{1}^{9}\right]_{26}$ | 0.001832 |
| 9 | 256 | $\left[4_{7}^{0}\right]_{13}$ | $\left[4_{1}^{9}\right]_{16}$ | $\left[4_{3}^{9}\right]_{24}$ | 0.001216 |
| 9 | 256 | $\left[4_{7}^{0}\right]_{13}$ | $\left[4_{3}^{9}\right]_{24}$ | $\left[4_{1}^{9}\right]_{16}$ | 0.001216 |
| 9 | 256 | $\left[4_{6}^{0}\right]_{14}$ | $\left[4_{3}^{9}\right]_{19}$ | $\left[4_{4}^{9}\right]_{25}$ | 0.000619 |
| 9 | 256 | $\left[L_{6}^{0}\right]_{14}$ | $\left[4_{4}^{9}\right]_{25}$ | $\left[4_{3}^{9}\right]_{19}$ | 0.000619 |
| 9 | 128 | [ $\left.4_{6}^{0}\right]_{10}$ | $\left[L_{13}^{9}\right]_{18}$ | $\left[4_{1}^{9}\right]_{12}$ | 0.003657 |
| 9 | 128 | $\left[{ }_{6}^{0}\right]_{10}$ | $\left[4_{1}^{9}\right]_{12}$ | $\left[L_{13}^{9}\right]_{18}$ | 0.003657 |
| 9 | 128 | $\left[4_{8}^{0}\right]_{9}$ | $\left[\Delta_{12}^{9}\right]_{19}$ | $\left[\Delta_{13}^{9}\right]_{11}$ | 0.002112 |
| 9 | 128 | $\left[4_{8}^{0}\right]_{9}$ | $\left[\Delta_{13}^{9}\right]_{11}$ | $\left[\Delta_{12}^{9}\right]_{19}$ | 0.002112 |
| 9 | 128 | $\left[4_{7}^{0}\right]_{28}$ | $\left[\Delta_{11}^{9}\right]_{26}$ | $\left[4_{4}^{9}\right]_{18}$ | 0.001287 |
| 9 | 128 | $\left[4_{7}^{0}\right]_{28}$ | $\left[4_{4}^{9}\right]_{18}$ | $\left[L_{11}^{9}\right]_{26}$ | 0.001287 |
| 9 | 128 | $\left[4_{6}^{0}\right]_{7}$ | $\left[4_{1}^{9}\right]_{16}$ | $\left[4_{13}^{9}\right]_{28}$ | 0.000756 |
| 9 | 128 | $\left[4_{6}^{0}\right]_{7}$ | $\left[4_{13}^{9}\right]_{28}$ | $\left[4_{1}^{9}\right]_{16}$ | 0.000756 |
| 9 | 128 | $\left[\left[_{6}^{0}\right]_{14}\right.$ | $\left[4_{51}^{9}\right]_{11}$ | $\left[\Delta_{14}^{9}\right]_{25}$ | 0.000251 |
| 9 | 128 | $\left[L_{6}^{0}\right]_{14}$ | $\left[L_{14}^{9}\right]_{25}$ | $\left[L_{15}^{9}\right]_{11}$ | 0.000251 |

coefficient is $95 \%$. In our experiment, $\varepsilon_{d}^{\star}$ is larger than $2^{-12}$; thus, the results obtained from the experiment are reliable.

The results for the maximum values of $\varepsilon_{d}^{\star}$ are shown in table 11 and table 2] In Salsa20, the maximum value of $\varepsilon_{d}^{\star}$ is 0.003112 . In[24], the number of streams for the distinguisher was estimated as $N=0.4624 \cdot M^{2}$, where $\frac{1}{M}=P\left[z_{j} \oplus z_{j^{\prime}}\right]-\frac{1}{2}$. Therefore, if the adversary obtains $2^{16}$ keystreams bits in Salsa20, the keystream bits can be distinguished keystream from random bit sequences. The adversary can also distinguish keystream bits from random bit sequences using only two bits of keystream in case of ChaCha.

We compare our results with existing results in Table 3. The best attack was proposed by Aumasson et al.[22] and it covers the 8 -round version of Salsa20 using a 256-bit key with an estimated complexity of $2^{251}$. Regarding the 128 -bit key, Aumasson proposed key-recovery attacks for the reduced versions with up to 7 rounds[22] with an estimated complexity of $2^{111}$. For ChaCha, Aumasson attacked the 6 -round version with an estimated complexity of $2^{139}$ and the 7 -round version with an estimated complexity of $2^{248}$ using a 256 -bit key. Regarding the 128 -bit key, Aumasson proposed key-recovery attacks for the reduced versions with up to 7 rounds with an estimated complexity of $2^{107}$ [22]. Our results show that our distinguishing attacks are lower cost (i.e. time and memory complexity) than the above results of existing researches. In both Salsa20 and ChaCha, an adversary could attack more rounds version with lower cost. Especially, for ChaCha, we estimated that an adversary only required 2 input pairs for a distinguisher.

Table 2. ChaCha Distinguisher

| Round | key length | $\left[4_{i}^{0}\right]_{j}$ | $\left[\Delta_{p}^{r}\right]_{q}$ | $\left[U_{s}^{r}\right]_{t}$ | ${ }_{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8 | 256 | $\left[4_{13}^{0}\right]_{13}$ | $\left[\Delta_{3}^{8}\right]_{16}$ | $\left[4_{14}^{8}\right]_{24}$ | 0.890259 |
| 8 | 256 | $\left[4_{13}^{0}\right]_{13}$ | $\left.{ }^{[14}{ }_{14}^{8}\right]_{24}$ | $\left[4_{3}^{8}\right]_{16}$ | 0.890259 |
| 8 | 256 | $\left[\Delta_{14}^{0}\right]_{14}$ | $\left[4_{0}^{8}\right]_{17}$ | $\left[4_{15}^{8}\right]_{25}$ | 0.878544 |
| 8 | 256 | $\left[4_{14}^{0}\right]_{14}$ | $\left[L_{15}^{8}\right]_{25}$ | $\left[4_{0}^{8}\right]_{17}$ | 0.878544 |
| 8 | 256 | $\left[4_{13}^{0}\right]_{15}$ | [43 $\left.{ }_{3}^{8}\right]_{18}$ | [ $\left.\Delta_{14}^{8}\right]_{26}$ | 0.878052 |
| 8 | 256 | $\left[4_{13}^{0}\right]_{15}$ | $\left[\Delta_{14}^{8}\right]_{26}$ | $\left[4_{3}^{8}\right]_{18}$ | 0.878052 |
| 8 | 256 | $\left[4_{12}^{0}\right]_{13}$ | [ $\left.4_{2}^{8}\right]_{16}$ | $\left[4_{13}^{8}\right]_{24}$ | 0.871461 |
| 8 | 256 | $\left[4_{12}^{0}\right]_{13}$ | $\left[\Delta_{13}^{8}\right]_{24}$ | $\left[4_{2}^{8}\right]_{16}$ | 0.871461 |
| 8 | 256 | $\left[4_{13}^{0}\right]_{14}$ | $\left[4_{3}^{8}\right]_{17}$ | $\left[_{14}^{8}{ }^{2}\right]_{25}$ | 0.871338 |
| 8 | 128 | $\left[4_{12}^{0}\right]_{13}$ | $\left[L_{12}^{8}\right]_{19}$ | $\left[4_{14}^{8}\right]_{1}$ | 0.781044 |
| 8 | 128 | $\left[\Delta_{12}^{0}\right]_{13}$ | $\left[4_{14}^{8}\right]_{1}$ | $\left[\Delta_{12}^{8}\right]_{19}$ | 0.781044 |
| 8 | 128 | [4 $\left.4_{13}^{0}\right]_{14}$ | $\left[\Delta_{20}^{8}\right]_{18}$ | [ $\left.\Delta_{15}^{8}\right]_{12}$ | 0.761928 |
| 8 | 128 | $\left[4_{13}^{0}\right]_{14}$ | $\left[L_{15}^{8}\right]_{12}$ | $\left[L_{20}^{8}\right]_{18}$ | 0.761928 |
| 8 | 128 | $\left[\Delta_{14}^{0}\right]_{11}$ | $\left[4_{14}^{8}\right]_{1}$ | $\left[\Delta_{11}^{8}\right]_{13}$ | 0.741681 |
| 8 | 128 | $\left[4_{14}^{0}\right]_{11}$ | $\left[\Delta_{11}^{8}\right]_{13}$ | $\left[4_{14}^{8}\right]_{1}$ | 0.741681 |
| 8 | 128 | $\left[4_{13}^{0}\right]_{9}$ | $\left[4_{14}^{8}\right]_{8}$ | $\left[4_{13}^{8}{ }^{\text {d }}{ }^{8}\right.$ | 0.739875 |
| 8 | 128 | $\left[4_{13}^{0}\right]_{9}$ | $\left[_{13}^{8}\right]_{24}$ | $\left[4_{14}^{8}\right]_{8}$ | 0.739875 |
| 8 | 128 | $\left[4_{13}^{0}\right]_{11}$ | $\left[\Delta_{19}^{8}\right]_{21}$ | $\left[4_{7}^{8}\right]_{1}$ | 0.720158 |
| 8 | 128 | $\left[L_{13}^{0}\right]_{11}$ | $\left[4_{7}^{8}\right]_{1}$ | $\left[L_{19}^{8}\right]_{21}$ | 0.720158 |

Table 3. Time complexity

| Type | Round/Key length | time complexity | Reference |
| :---: | :---: | :---: | :---: |
| Salsa20 | $5 / 256$ | $2^{248}$ | $[9]$ |
| Salsa20 | $6 / 256$ | $2^{139}$ | $[22]$ |
| Salsa20 | $7 / 256$ | $2^{151}$ | $[22]$ |
| Salsa20 | $8 / 256$ | $2^{251}$ | $[22]$ |
| Salsa20 | $9 / 256$ | $2^{16}$ | This work |
| Salsa20 | $8 / 128$ | $2^{111}$ | $[22]$ |
| Salsa20 | $9 / 128$ | $2^{16}$ | This work |
| ChaCha | $6 / 256$ | $2^{139}$ | $[22]$ |
| ChaCha | $7 / 256$ | $2^{248}$ | $[22]$ |
| ChaCha | $8 / 256$ | 2 | This work |
| ChaCha | $6 / 128$ | $2^{107}$ | $[22]$ |
| ChaCha | $8 / 128$ | 2 | This work |

## 5 Concluding Remarks

We proposed new distinguishing attacks on 9-round Salsa20 and 8-round ChaCha, which uses double-bit differentials. The complexities of the introduced attacks are $2^{16}$ in 9 -round Salsa20 and 2 in 8-round ChaCha, which are much less than the complexities of an exhaustive key search and existing attacks. Our attacks could not be directly applied to the full-round Salsa20 and the full-round ChaCha due to computational complexities
for finding double-bit differentials; thus, these ciphers are not presently under threat. Obviously, the distinguishing attack using double-bit differentials can be extended to distinguishing attacks using a triple-bit differential or more-bit differentials. We will improve the applicability of our method to extend the number of bits for differentials in our future research.

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[^0]:    ${ }^{1}$ This notation is different from [22] in a precise sense. We defined the reduced version as $X+X^{r}$ where $r$ is the number of rounds.

