

Lessons from Nanoscience:
A Lecture Note Series

Vol. **1**

Lessons from **Nanoelectronics** A New Perspective on Transport

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 **World Scientific**

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Detailed Contents

<i>Preface</i>	vii
<i>Some Symbols used</i>	ix
I. <i>The New Ohm's Law</i>	1
1. The Bottom-Up Approach	3
2. Why Electrons Flow	15
2.1. <i>Two Key Concepts</i>	18
2.2. <i>Fermi Function</i>	18
2.3. <i>Non-equilibrium: Two Fermi Functions</i>	21
2.4. <i>Linear Response</i>	22
2.5. <i>Difference in "Agenda" Drives the Flow</i>	24
3. The Elastic Resistor	27
3.1. <i>How an Elastic Resistor Dissipates Heat</i>	30
3.2. <i>Conductance of an Elastic Resistor</i>	32
3.3. <i>Why an Elastic Resistor is Relevant</i>	35
4. Ballistic and Diffusive Transport	39
4.1. <i>Ballistic and Diffusive Transfer Times</i>	42
4.2. <i>Channels for Conduction</i>	45
5. Conductivity	47
5.1. <i>$E(p)$ or $E(k)$ Relations</i>	52
5.2. <i>Counting States</i>	53
5.3. <i>Drude Formula</i>	55
5.4. <i>Is Conductivity proportional to Electron Density?</i>	59
5.5. <i>Quantized Conductance</i>	61
6. Diffusion Equation for Ballistic Transport	65
6.1. <i>Electrochemical Potentials Out of Equilibrium</i>	72
6.2. <i>Currents in Terms of Non-Equilibrium Potentials</i>	76

7.	What about Drift?	79
	7.1. Boltzmann Transport Equation, BTE	82
	7.2. Diffusion Equation from BTE	85
	7.3. Equilibrium Fields Do Matter	88
	7.4. The Two Potentials	89
8.	Electrostatics is Important	93
	8.1. The Nanotransistor	94
	8.2. Why the Current Saturates	96
	8.3. Role of Charging	98
	8.4. Rectifier Based on Electrostatics	102
	8.5. Extended Channel Model	104
9.	Smart Contacts	111
	9.1. Why <i>p-n</i> Junctions are Different	112
	9.2. Contacts are Fundamental	119
II.	Old Topics in New Light	123
10.	Thermoelectricity	125
	10.1. Seebeck Coefficient	129
	10.2. Thermoelectric Figures of Merit	131
	10.3. Heat Current	133
	10.4. "Delta Function" Thermoelectric	138
11.	Phonon Transport	145
	11.1. Phonon Heat Current	147
	11.2. Thermal Conductivity	151
12.	Measuring Electrochemical Potentials	155
	12.1. The Landauer Formulas	161
	12.2. Büttiker Formula	165
13.	Hall Effect	173
	13.1. Why <i>n-</i> and <i>p-</i> Conductors Are Different	178
	13.2. Spatial Profile of Electrochemical Potential	179
	13.3. Measuring the Potential	184
	13.4. Non-Reciprocal Circuits	188

14.	Spin Valve	191
	14.1. <i>Mode Mismatch and Interface Resistance</i>	194
	14.2. <i>Spin Potentials</i>	201
	14.3. <i>Spin-Torque</i>	209
	14.4. <i>Polarizers and Analyzers</i>	217
15.	Kubo Formula	221
	15.1. <i>Kubo Formula for an Elastic Resistor</i>	224
	15.2. <i>Onsager Relations</i>	227
16.	Second Law	229
	16.1. <i>Asymmetry of Absorption and Emission</i>	233
	16.2. <i>Entropy</i>	235
	16.3. <i>Law of Equilibrium</i>	240
	16.4. <i>Fock Space States</i>	242
	16.5. <i>Alternative Expression for Entropy</i>	246
17.	Fuel Value of Information	251
	17.1. <i>Information-Driven Battery</i>	255
	17.2. <i>Fuel Value Comes From Knowledge</i>	258
	17.3. <i>Landauer's Principle</i>	260
	17.4. <i>Maxwell's Demon</i>	261
III.	Contact-ing Schrödinger	265
18.	The Model	267
	18.1. <i>Schrödinger Equation</i>	270
	18.2. <i>Electron-Electron Interactions</i>	275
	18.3. <i>Differential to Matrix Equation</i>	278
	18.4. <i>Choosing Matrix Parameters</i>	281
19.	Non-Equilibrium Green's Functions (NEGF)	293
	19.1. <i>One-level Resistor</i>	299
	19.2. <i>Multi-level Resistors</i>	308
	19.3. <i>Conductance Functions for Coherent Transport</i>	314
	19.4. <i>Elastic Dephasing</i>	315
20.	Can Two Offer Less Resistance than One?	321
	20.1. <i>Modeling 1D Conductors</i>	322

20.2.	<i>Quantum Resistors in Series</i>	326
20.3.	<i>Potential Drop Across Scatterer(s)</i>	331
21.	Quantum of Conductance	337
21.1.	<i>2D Conductor as 1D Conductors in Parallel</i>	337
21.2.	<i>Contact self-energy for 2D Conductors</i>	343
21.3.	<i>Quantum Hall Effect</i>	349
22.	Rotating an Electron	355
22.1.	<i>One-level Spin Valve</i>	359
22.2.	<i>Rotating Magnetic Contacts</i>	363
22.3.	<i>Spin Hamiltonians</i>	366
22.4.	<i>Vectors and Spinors</i>	369
22.5.	<i>Spin Precession</i>	374
22.6.	<i>From NEGF to Diffusion</i>	380
23.	Does NEGF Include “Everything”?	389
23.1.	<i>Coulomb Blockade</i>	392
23.2.	<i>Fock Space Description</i>	397
23.3.	<i>Entangled States</i>	402
24.	The Quantum and the Classical	409
24.1.	<i>Spin coherence</i>	410
24.2.	<i>Pseudo-spins</i>	412
24.3.	<i>Quantum Entropy</i>	415
24.4.	<i>Does Interaction Increase the Entropy?</i>	417
24.5.	<i>Spins and magnets</i>	419
	References / Further Reading	423
	Appendices	433
A.	<i>Fermi and Bose Function Derivatives</i>	433
B.	<i>Angular Averaging</i>	435
C.	<i>Hamiltonian with E- and B-Fields</i>	437
D.	<i>Transmission Line Parameters from BTE Equations</i>	439
E.	<i>NEGF Equations</i>	443
F.	<i>MATLAB Codes for Text Figures</i>	449