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Benjamin Roberts, Yevgeny V. Stadnik, V. A. Dzuba, Victor V. Flambaum ...+2 more authors

Institutions: University of New South Wales, University of Mainz, University of California, Berkeley

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Limiting P -Odd Interactions of Cosmic Fields with Electrons, Protons, and Neutrons

B. M. Roberts,^{1,*} Y. V. Stadnik,^{1,†} V. A. Dzuba,¹ V. V. Flambaum,^{1,2} N. Leefer,³ and D. Budker^{3,4,5}

¹*School of Physics, University of New South Wales, Sydney 2052, Australia*

²*New Zealand Institute for Advanced Study, Massey University, Auckland 0745, New Zealand*

³*Helmholtz Institute Mainz, Johannes Gutenberg University, 55099 Mainz, Germany*

⁴*Department of Physics, University of California at Berkeley, Berkeley, California 94720-7300, USA*

⁵*Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA*

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We propose methods for extracting limits on the strength of P -odd interactions of pseudoscalar and pseudovector cosmic fields with electrons, protons, and neutrons, by exploiting the static and dynamic parity-nonconserving amplitudes and electric dipole moments they induce in atoms. Candidates for such fields are dark matter (including axions) and dark energy, as well as several more exotic sources described by Lorentz-violating standard model extensions. Atomic calculations are performed for H, Li, Na, K, Rb, Cs, Ba⁺, Tl, Dy, Fr, and Ra⁺. From these calculations and existing measurements in Dy, Cs, and Tl, we constrain the interaction strengths of the parity-violating static pseudovector cosmic field to be 7×10^{-15} GeV with an electron, and 3×10^{-8} GeV with a proton.

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Introduction.—Among the most important unanswered questions in fundamental physics are the strong CP problem, the puzzling observation that quantum chromodynamics (QCD) does not appear to violate the combined charge-parity (CP) symmetry, see, e.g., [1–3], and dark matter and dark energy, see, e.g., [4,5]. One elegant solution to the strong CP problem invokes the introduction of a pseudoscalar particle known as the axion [2] (see also [6–8]). It has been noted that the axion may also be a promising cold dark matter (CDM) candidate. Thus axions, if detected, could resolve both the CDM and strong CP problems [9].

The possibility of cosmic pseudovector fields has been proposed in, e.g., Lorentz-invariance-violating standard model extensions [10]. Limits on the spatial components of this pseudovector cosmic field have been extracted for the interaction with electrons, protons, and neutrons, see, e.g., Ref. [11] and references therein.

In this Letter, we extract direct limits on the coupling of the temporal component of a static pseudovector cosmic field with electrons and protons, demonstrating that parity-violating effects can indeed be used to obtain such limits. We also outline a method for how limits can be placed on the interaction strengths of dynamic cosmic fields with fermions using oscillating atomic parity-violation effects.

The existence of a cosmic field that interacts with electrons or nucleons in a parity-violating manner would induce a mixing of opposite-parity states and lead to observable effects, including parity nonconservation (PNC) amplitudes and atomic electric dipole moments (EDMs), the measurement of which would probe the properties of the fields that gave rise to them [12–16]. PNC amplitudes are electric dipole ($E1$) transitions between states of the same

nominal parity. Conventionally, the main contribution to these come from a Z^0 -boson exchange between the nucleus and atomic electrons, see, e.g., [17,18]. Studies of atomic PNC and EDMs are relatively inexpensive low-energy tests of the standard model that are complementary to direct tests performed at high energy. Measurements and calculations of the Cs $6s$ - $7s$ PNC amplitude stand as the most precise atomic test of the electroweak theory to date, see, e.g., [19–23].

We perform calculations of cosmic-field-induced PNC amplitudes and atomic EDMs for several atoms and ions. In conjunction with experimental data, these calculations are necessary for determining or placing limits on important pseudoscalar and pseudovector cosmic-field parameters. We combine these calculations with the results of existing PNC experiments in Cs, Tl, and Dy to extract limits on the interaction strength of a static pseudovector field with electrons and protons. The same method can be directly applied to extract a limit for neutrons when appropriate experimental data become available.

Theory.—The Lagrangian densities for the interaction between fermions and a pseudoscalar (PS) field via a derivative-type and a direct pseudoscalar coupling read

$$\mathcal{L}_{i\gamma^5}^{\text{PS}} = \eta \hbar (\partial_\mu \phi) \bar{\psi} \gamma^\mu \gamma^5 \psi \quad (1)$$

and

$$\mathcal{L}_{i\gamma^0\gamma^5}^{\text{PS}} = -i\zeta m_f c^2 \phi \bar{\psi} \gamma^5 \psi, \quad (2)$$

respectively, where ψ is the fermion wave function with $\bar{\psi} \equiv \psi^\dagger \gamma^0$, η and ζ are dimensionless coupling constants (into which we have absorbed the amplitude of the field), γ^0 and γ^5 are Dirac matrices, and m_f is the mass of the fermion.

In the above equations, $\phi = \phi(\mathbf{r}, t)$ is the dynamic PS field in question. Below we show that interactions (1) and (2) involving a static field do not lead to atomic parity-violating effects. With the assumption that the motion of the observer with respect to the field is slow compared to the speed of light, we can express this field as $\phi(\mathbf{r}, t) = \cos(\omega_\phi t)$, for a particular choice of phase [16], where $\hbar\omega_\phi$ is the energy of the field excitation. The time-derivative part of the PS γ^5 interaction (1), and the PS $i\gamma^0\gamma^5$ interaction (2), lead to the interaction Hamiltonians

$$\hat{h}_{\gamma^5}^{\text{PS}} = \eta\hbar\omega_\phi \sin(\omega_\phi t)\gamma^5, \quad (3)$$

$$\hat{h}_{i\gamma^0\gamma^5}^{\text{PS}} = i\zeta m_f c^2 \cos(\omega_\phi t)\gamma^0\gamma^5. \quad (4)$$

The Lagrangian density for the interaction of fermions with a pseudovector (PV) cosmic field is

$$\mathcal{L}_{\gamma^5}^{\text{PV}} = b_\mu \bar{\psi} \gamma^\mu \gamma^5 \psi, \quad (5)$$

where we have absorbed the strength of the interaction into the components of the field, $b_\mu = (b_0, -\mathbf{b})$. The time component of this coupling leads to the interaction Hamiltonian

$$\hat{h}_{\gamma^5}^{\text{PV}} = b_0(t)\gamma^5, \quad (6)$$

which could be either static [$b_0(t) = b_0$] or dynamic [$b_0(t) = b_0 \sin(\omega_b t)$].

Interaction with electrons.—The interactions (3) and (4) with electrons induce small, oscillating contributions to PNC amplitudes and atomic EDMs. The effects of (6) mimic those of (3) in the dynamic case, and mimic the conventional nuclear-spin-independent weak-charge (Q_W)-induced PNC signal in the static case.

The matrix elements of the γ^5 and $i\gamma^0\gamma^5$ operators are not entirely independent; they are related via

$$\langle b | \sum_{\iota} i\gamma_{\iota}^0 \gamma_{\iota}^5 | a \rangle = (i/2m_e c^2)(E_b - E_a) \langle b | \sum_{\iota} \gamma_{\iota}^5 | a \rangle, \quad (7)$$

where the states a and b are eigenstates of the atomic Hamiltonian, \hat{H} , with eigenvalues E_a and E_b , respectively, and the index ι stands for summation over electrons. Equation (7) follows directly from the identity $i\gamma_{\iota}^0 \gamma_{\iota}^5 = (i/2m_e c^2)[\hat{H}, \gamma_{\iota}^5]$, which holds for the atomic Dirac Hamiltonian including electromagnetic interactions.

We now show that a static PS interaction cannot give rise to observable P -odd effects in atoms in the lowest order (though, note that a static pseudovector field can). To see this for a derivative-type coupling, note that the time-derivative term in (1) vanishes for static ϕ , and that the spatial-derivative term in (1) is proportional to $(\nabla\phi) \cdot \boldsymbol{\sigma}_e$ (in the nonrelativistic limit), and does not contribute to the mixing of opposite-parity atomic states. To see this for the pseudoscalar coupling (2), we write the perturbed wave function for atomic state a to first order as $|\tilde{a}\rangle = |a\rangle - (i\zeta/2)\Sigma_{\iota}\gamma_{\iota}^5|a\rangle$, where we have used the relation (7). Hence, the first-order correction induced by the static

PS interaction (2) to the amplitude of an electromagnetic interaction, which has the form $j_\mu A^\mu = \psi_b^\dagger (A^0 + \boldsymbol{\alpha} \cdot \mathbf{A}) \psi_a$, where $A^\mu = (A^0, \mathbf{A})$ is the photon field and $\boldsymbol{\alpha}$ is a Dirac matrix, is reduced to $\langle b | [\boldsymbol{\alpha}, \gamma^5] \cdot \mathbf{A} | a \rangle = 0$. There are thus no corrections to electromagnetic amplitudes, including PNC amplitudes and atomic EDMs.

To analyze the dynamic effects, we apply first-order time-dependent perturbation theory—see Ref. [16] for further details. We now make the assumption that the energy of the field particle is much smaller than the energy separation between all opposite-parity states of interest, i.e., $\hbar\omega_{\phi/b} \ll |E_{a,b} - E_n|$ for all n . For a relatively light field particle, there is no loss of generality in making this assumption, except in the case where the atomic system of interest possesses close levels of opposite parity. This case will be investigated for Dy.

With this, we can present four comparatively simple formulas for the dynamic PNC amplitudes and atomic EDMs induced by the PS interactions (3) and (4),

$$E_{\text{PNC}}^{\text{PS}}(\gamma^5) = \eta\hbar\omega_\phi \sin(\omega_\phi t) K_{\text{PNC}}, \quad (8)$$

$$E_{\text{PNC}}^{\text{PS}}(i\gamma^0\gamma^5) = \frac{\zeta\hbar\omega_\phi}{2} \sin(\omega_\phi t) K_{\text{PNC}}, \quad (9)$$

$$d_{\text{EDM}}^{\text{PS}}(\gamma^5) = -2i\eta\hbar^2\omega_\phi^2 \cos(\omega_\phi t) K_{\text{EDM}}, \quad (10)$$

$$d_{\text{EDM}}^{\text{PS}}(i\gamma^0\gamma^5) = -i\zeta\hbar^2\omega_\phi^2 \cos(\omega_\phi t) K_{\text{EDM}}. \quad (11)$$

For the PV interaction (6), the induced PNC amplitude,

$$E_{\text{PNC}}^{\text{PV}} = b_0(t) K_{\text{PNC}}, \quad (12)$$

can be either static, with $b_0(t) = b_0$, or dynamic, with $b_0(t) = b_0 \sin(\omega_b t)$. In the dynamic case, the PV interaction (6) also gives rise to an oscillating atomic EDM,

$$d_{\text{EDM}}^{\text{PV}} = -2ib_0\hbar\omega_b \cos(\omega_b t) K_{\text{EDM}}. \quad (13)$$

In the above equations, we have defined what will be henceforth denoted atomic structure coefficients,

$$K_{\text{PNC}} = \sum_{n,\iota,j} \left[\frac{\langle b | \mathbf{d}_\iota | n \rangle \langle n | \gamma_j^5 | a \rangle}{E_a - E_n} + \frac{\langle b | \gamma_j^5 | n \rangle \langle n | \mathbf{d}_\iota | a \rangle}{E_b - E_n} \right], \quad (14)$$

$$K_{\text{EDM}} = \sum_{n,\iota,j} [(\langle a | \mathbf{d}_\iota | n \rangle \langle n | \gamma_j^5 | a \rangle) / (E_a - E_n)^2], \quad (15)$$

where $\mathbf{d}_\iota = -e\mathbf{r}_\iota$ is the $E1$ operator, and the indices ι and j stand for the summation over atomic electrons.

Formulas (8)–(13) provide the link between the atomic-structure calculations and the fundamental physics necessary to extract quantitative information about the fields in question. In deriving these equations we made use of Eq. (7). Notice that the atomic-structure coefficients are the same for the γ^5 and $i\gamma^0\gamma^5$ cases.

The K_{PNC} coefficients vanish in the nonrelativistic limit [16]. In the calculations, this leads to significant

cancellation between terms in the sum (14). If the calculations were exact, this would eliminate the nonrelativistic part of the amplitude and leave only the relativistic corrections, constituting the correct result. In practice, however, the cancellation leads to significant instabilities in the calculations. To bypass this problem, we express the γ^5 operator via the exact relation

$$\gamma^5 = (i/c)[\hat{H}, \hat{\Sigma}_i \cdot \mathbf{r}_i] + 2\gamma_i^5 \hat{K}_i, \quad (16)$$

where $\hat{\Sigma}$ is the Dirac spin matrix, $\hat{K} = -1 - \boldsymbol{\sigma} \cdot \mathbf{L}$ [$\hat{K}\Omega_\kappa = \kappa\Omega_\kappa$ for the spherical spinor Ω_κ with $\kappa = (l-j)(2j+1)$], where \hat{H} is the atomic Dirac-Coulomb Hamiltonian, \mathbf{L} and l are the operator and value of the orbital angular momentum, and j is the total angular momentum of the single-electron atomic states. The commutator in (16) cancels exactly in the amplitude, and does not contribute. We thus calculate the K_{PNC} coefficients free of large cancellation by using only the last term in (16).

Interaction with nucleons.—The main contribution to the nuclear-spin-dependent PNC amplitude comes from the interaction of electrons with the anapole moment (AM), a P -odd, T -even nuclear moment that arises due to parity-violating nuclear forces [24]. The interaction between a PS or PV cosmic field and an unpaired proton or neutron will give rise to a contribution to the AM. This was considered for a PS field in Ref. [16].

In the case of the static PV interaction (6), the dimensionless constant quantifying the magnitude of the anapole moment can be expressed as $\tilde{\kappa}_a = \kappa_a + \kappa_b$, where κ_a is due to parity-violating nuclear forces, and κ_b is due to the PV field and is related to the field parameter b_0^N (the superscript denotes either a proton or neutron),

$$\kappa_b = [(2\sqrt{2}\hbar\pi\alpha\mu\langle r^2 \rangle)/G_F m_p c] b_0^N, \quad (17)$$

where m_p and μ are the mass and magnetic moment (in nuclear magnetons) of the unpaired nucleon, respectively, G_F is the Fermi constant, and we take the mean-square radius $\langle r^2 \rangle = \frac{3}{5} r_0^2 A^{2/3}$, with $r_0 = 1.2$ fm, and A the atomic mass number [16,24]. No new atomic calculations are required—a limit on b_0^N can be extracted directly from existing measurements and calculations of κ_a . Note that interactions with the dynamic PS (3) and PV (6) fields would induce oscillating nuclear anapole and Schiff moments, which would contribute to nuclear-spin-dependent PNC amplitudes and atomic EDMs, respectively [16].

Results and discussion.—Apart from Dy, we treat all the considered atoms as single-valence systems. We then use the correlation potential method to include core-valence correlations [21]. Core polarization and interactions with external fields are taken into account with the time-dependent Hartree-Fock method [21]. We estimate the uncertainty in these quantities from the effect that including correlations has on the values.

By expressing the second term on the right-hand side of (16) as $2\gamma^5 \hat{K} = -2\gamma^0 \gamma^5 (\gamma^0 \hat{K})$, and noting that single-particle states are eigenstates of $\gamma^0 \hat{K}$ (with eigenvalue κ), we can use Eq. (7) to invoke the closure relation, and the amplitude for single-particle states reduces to

$$K_{\text{PNC}} = (1/m_e c^2)(\kappa_b + \kappa_a) \langle b | \gamma^5 \mathbf{d} | a \rangle, \quad (18)$$

which requires no summation over intermediate states, does not contain significant cancellation, and can be calculated with relatively high accuracy.

For the K_{EDM} coefficients, the first term on the right-hand side of (16) dominates the amplitude—it scales as $1/c$ whereas the second term scales as $1/c^3$. Inserting $\gamma^5 \approx i/c[\hat{H}, \hat{\Sigma} \cdot \mathbf{r}]$ into (15), we see that the K_{EDM} coefficients scale proportionally with the static dipole polarizability, with corrections of the order $(1/c)^3$. We use this fact as a test of our calculations, and find excellent agreement using published polarizability values, see, e.g., [25]. Results of our calculations for the atomic structure coefficients K_{PNC} and K_{EDM} are presented in Table I.

The feature of Dy that makes it a particularly interesting system for the study of atomic PNC is the presence of two nearly degenerate opposite-parity states with the same total angular momentum, $J = 10$, at $E = 19797.96$ cm $^{-1}$. We use the notation A for the even-parity state and notation B for the odd-parity state, following Ref. [28]. The method we use for the calculations here closely follows previous calculations of PNC effects in Dy [29]. This particular configuration interaction (CI) method is described in greater detail in Ref. [30].

For Dy, it is the quantity $\langle B | \gamma^5 | A \rangle$ that is of direct interest, since here the transition between A and B is measured directly [28]. Because of the near degeneracy of the levels in Dy, the first term on the right-hand side of (16) does not contribute, and we perform calculations using $2\gamma^5 \hat{K}$ instead. To determine the uncertainty in this matrix element, we examine the effect of removing configuration states from the CI basis. Note that in the conventional PNC case, the relevant matrix element is highly dependent on the configurations used [29]. We find, however, that this makes little difference here, meaning the $\langle B | \gamma^5 | A \rangle$ matrix element is quite stable. We calculate this to be $0.7(2) \times 10^{-8} b_0$ a.u. = $50(20) b_0$ MHz.

TABLE I. Calculated PNC and EDM atomic structure coefficients for several atomic systems (a.u.).

	Transition	$K_{\text{PNC}}(i10^{-6})$	State	K_{EDM}
H	1s-2s	0.1447	1s	0.0164 ^a
Li	2s-3s	0.219(3)	2s	0.60(1)
Na	3s-4s	0.224(4)	3s	0.61(1)
K	4s-5s	0.242(4)	4s	1.09(5)
Rb	4s-3d _{3/2}	-0.307(6)		
	5s-6s	0.247(5)	5s	1.22(8)
Cs	5s-4d _{3/2}	-0.30(1)		
	6s-7s	0.256(5)	6s	1.6(2)
Ba ⁺	6s-5d _{3/2}	-0.22(3)		
	6s-5d _{3/2}	-0.02(1)		
Tl	6p _{1/2} -6p _{3/2}	0.22(5)	6p _{1/2}	0.19(3) ^a
Fr	7s-8s	0.253(6)	7s	1.3(2)
	7s-6d _{3/2}	-0.25(3)		
Ra ⁺	7s-6d _{3/2}	-0.08(3)		

^aFrom polarizability values of H [26] and Tl [27].

For the static case, the PV interaction manifests itself as a contribution to the PNC amplitude of a transition between two states of the same nominal parity. Therefore, by combining the results of the conventional (Q_W -induced) PNC experiments and calculations in Cs [20,23], Tl [31,32], and Dy [28,29], with the calculations of the cosmic-field-induced amplitudes from the present Letter, it is possible to extract limits on the value of the PV cosmic-field coupling constant b_0^e for electrons.

Combining the measured values for the AM of $\kappa_a(\text{Cs}) = 0.364(62)$ [20,33] and $\kappa_a(\text{Tl}) = -0.22(30)$ [31,34], with the values $\kappa_a(\text{Cs}) = 0.19(6)$ and $\kappa_a(\text{Tl}) = 0.17(10)$ from nuclear theory [35] (see also [18]) with Eq. (17), we have extracted limits on the parameter b_0^p that quantifies the interaction strength of a PV cosmic field with protons (since the anapole moment in both Cs and Tl is due to an unpaired proton). Note that ongoing AM measurements with Fr, Yb, and BaF will also lead to limits on the coupling to protons and neutrons [36–38]. We present both the electron and proton PV cosmic-field coupling limits in Table II.

For static effects, only measurements of static PNC amplitudes from conventional PNC experiments are needed to place limits on the cosmic-field parameters. For dynamic effects, however, a different style of experiment, in which one would measure small oscillations in the PNC amplitude or atomic EDM, is needed. The frequency and amplitude of these oscillations would enable one to extract values for the relevant field parameters [13,14,16]. For example, a determination of the frequency would provide the mass of the particle, and the amplitude of the oscillations would lead to a determination of the constants η , ζ , or b_0 .

The high sensitivity of atomic EDM experiments makes them promising for the study of the oscillating effects considered here. Further enhancement in the sensitivity of the EDM measurements can be obtained by tuning the experiment to a specific frequency, see, e.g., Refs. [13,14,16], where oscillating-EDM experiments have been recently considered. For example, axions with masses of 10^{-5} eV/ c^2 or 10^{-9} eV/ c^2 , corresponding to the “classical” and “anthropic” regions (see, e.g., [9]), would lead to oscillations with frequencies of the order of GHz and MHz, respectively. For the case of axions, the coherence time may be estimated from $\Delta\omega_a/\omega_a \sim (\frac{1}{2}m_a v^2/m_a c^2) \sim (v^2/c^2)$, where a virial velocity of $v \sim 10^{-3}c$ would be typical in our local Galactic neighborhood, and $\omega_a \approx m_a c^2/\hbar$ [13].

The most stringent limits on the P -odd interaction of the temporal component of a static PV field with electrons,

$|b_0^e| < 7 \times 10^{-15}$ GeV, and protons, $|b_0^p| < 3 \times 10^{-8}$ GeV, come from Dy and Cs, respectively. These limits on the temporal components, b_0 , which are derived from P -odd effects, are complementary to existing limits on the spatial components, \mathbf{b} , derived from P -even effects due to the interaction of static cosmic fields with electrons, protons, and neutrons, of 1.3×10^{-31} GeV [39], 6×10^{-32} GeV [40], and 8.4×10^{-34} GeV [41], respectively. For further details and a brief history on recent developments and improvements in these limits, we refer the reader to Refs. [11,42]. Note that analogous oscillating P -even interactions can also be sought [13,16].

The prospect that atomic systems could be used as a probe for CDM has been considered in the literature, see, e.g., [13,16,43–47]. In addition to inducing PNC effects and EDMs, pseudoscalar fields can also give rise to other phenomena, e.g., the axioelectric effect [48–51], and spin-gravity and spin-axion-momentum couplings [13,16,52,53]. Searches for cosmic-field-induced EDMs can also be performed, e.g., in solid-state, nuclear, and molecular systems. Static electron EDM and nuclear Schiff moment experiments in ferroelectrics are discussed in Refs. [54,55], for instance, and solid-state systems have already been proposed for use in the detection of axionic dark matter (see, e.g., [14,56]).

We have demonstrated that atomic experiments investigating the P -odd effects discussed here are a viable option for searching for evidence of pseudoscalar and pseudo-vector cosmic fields, and for placing constraints on their interaction strengths with electrons, protons, and neutrons. Finally, we mention that transient EDMs may also be induced by cosmic fields in the form of topological defects [57].

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TABLE II. Limits (1σ) on the interaction strengths of a PV cosmic field with electrons (b_0^e) and protons (b_0^p) in GeV.

PNC quantity		$ b_0^e $	$ b_0^p $
Cs	$E_{\text{PNC}}(6s-7s)$	2×10^{-14}	3×10^{-8}
Tl	$E_{\text{PNC}}(6p_{1/2}-6p_{3/2})$	2×10^{-12}	8×10^{-8}
Dy	$\langle A \hat{h} B\rangle$	7×10^{-15}	

*b.roberts@unsw.edu.au

†y.stadnik@unsw.edu.au

- [1] S. Weinberg, *Phys. Rev. Lett.* **37**, 657 (1976); S. Weinberg, *Phys. Rev. Lett.* **40**, 223 (1978).
- [2] R. D. Peccei and H. R. Quinn, *Phys. Rev. Lett.* **38**, 1440 (1977); R. D. Peccei and H. R. Quinn, *Phys. Rev. D* **16**, 1791 (1977).
- [3] F. Wilczek, *Phys. Rev. Lett.* **40**, 279 (1978); J. E. Moody and F. Wilczek, *Phys. Rev. D* **30**, 130 (1984).

- [4] G. Bertone, D. Hooper, and J. Silk, *Phys. Rep.* **405**, 279 (2005); D. N. Spergel *et al.*, *Astrophys. J. Suppl. Ser.* **170**, 377 (2007); R. Agnese *et al.*, *Phys. Rev. Lett.* **111**, 251301 (2013).
- [5] A. G. Riess *et al.*, *Astron. J.* **116**, 1009 (1998); S. Perlmutter *et al.*, *Astrophys. J.* **517**, 565 (1999).
- [6] J. E. Kim, *Phys. Rev. Lett.* **43**, 103 (1979).
- [7] M. A. Shifman, A. I. Vainshtein, and V. I. Zakharov, *Nucl. Phys.* **B166**, 493 (1980); A. R. Zhitnitsky, *Yad. Fiz.* **31**, 1024 (1980) [*Sov. J. Nucl. Phys.* **31**, 529 (1980)].
- [8] M. Dine, W. Fischler, and M. Srednicki, *Phys. Lett.* **104B**, 199 (1981).
- [9] J. E. Kim and G. Carosi, *Rev. Mod. Phys.* **82**, 557 (2010); N. Brambilla *et al.*, [arXiv:1404.3723](https://arxiv.org/abs/1404.3723); H. Baer *et al.*, [arXiv:1407.0017](https://arxiv.org/abs/1407.0017).
- [10] D. Colladay and V. A. Kostelecký, *Phys. Rev. D* **55**, 6760 (1997).
- [11] V. A. Kostelecký and N. Russell, *Rev. Mod. Phys.* **83**, 11 (2011); V. A. Kostelecký and N. Russell, [arXiv:0801.0287](https://arxiv.org/abs/0801.0287).
- [12] P. Bolokhov, M. Pospelov, and M. Romalis, *Phys. Rev. D* **78**, 057702 (2008).
- [13] P. W. Graham and S. Rajendran, *Phys. Rev. D* **84**, 055013 (2011); P. W. Graham and S. Rajendran, *Phys. Rev. D* **88**, 035023 (2013).
- [14] D. Budker, P. W. Graham, M. Ledbetter, S. Rajendran, and A. O. Sushkov, *Phys. Rev. X* **4**, 021030 (2014).
- [15] N. Leefer and M. A. Hohensee, [arXiv:1307.6762](https://arxiv.org/abs/1307.6762).
- [16] Y. V. Stadnik and V. V. Flambaum, *Phys. Rev. D* **89**, 043522 (2014).
- [17] I. B. Khriplovich, *Parity Nonconservation in Atomic Phenomena* (Gordon and Breach, Philadelphia, 1991).
- [18] J. S. M. Ginges and V. V. Flambaum, *Phys. Rep.* **397**, 63 (2004).
- [19] M.-A. Bouchiat, J. Guena, L. Hunter, and L. Pottier, *Phys. Lett.* **117B**, 358 (1982).
- [20] C. S. Wood *et al.*, *Science* **275**, 1759 (1997).
- [21] V. A. Dzuba, V. V. Flambaum, and O. P. Sushkov, *Phys. Lett. A* **141**, 147 (1989).
- [22] S. A. Blundell, J. Sapirstein, and W. R. Johnson, *Phys. Rev. D* **45**, 1602 (1992); M. G. Kozlov, S. G. Porsev, and I. I. Tupitsyn, *Phys. Rev. Lett.* **86**, 3260 (2001); A. A. Vasilyev, I. M. Savukov, M. S. Safronova, and H. G. Berry, *Phys. Rev. A* **66**, 020101 (2002); V. A. Dzuba, V. V. Flambaum, and J. S. M. Ginges, *Phys. Rev. D* **66**, 076013 (2002); S. G. Porsev, K. Beloy, and A. Derevianko, *Phys. Rev. Lett.* **102**, 181601 (2009); S. G. Porsev, K. Beloy, and A. Derevianko, *Phys. Rev. D* **82**, 036008 (2010).
- [23] V. A. Dzuba, J. C. Berengut, V. V. Flambaum, and B. Roberts, *Phys. Rev. Lett.* **109**, 203003 (2012).
- [24] V. V. Flambaum, I. B. Khriplovich, and O. P. Sushkov, *Phys. Lett.* **146B**, 367 (1984).
- [25] P. Schwerdtfeger, <http://ctcp.massey.ac.nz/dipole-polarizabilities>.
- [26] L.-Y. Tang, Y.-H. Zhang, X.-Z. Zhang, J. Jiang, and J. Mitroy, *Phys. Rev. A* **86**, 012505 (2012).
- [27] T. M. Miller, *CRC Handbook of Chemistry and Physics* (CRC Press, New York, 2002).
- [28] A. T. Nguyen, D. Budker, D. DeMille, and M. Zolotarev, *Phys. Rev. A* **56**, 3453 (1997).
- [29] V. A. Dzuba and V. V. Flambaum, *Phys. Rev. A* **81**, 052515 (2010).
- [30] V. A. Dzuba and V. V. Flambaum, *Phys. Rev. A* **77**, 012514 (2008).
- [31] P. A. Vetter, D. M. Meekhof, P. K. Majumder, S. K. Lamoreaux, and E. N. Fortson, *Phys. Rev. Lett.* **74**, 2658 (1995).
- [32] M. G. Kozlov, S. G. Porsev, and W. R. Johnson, *Phys. Rev. A* **64**, 052107 (2001).
- [33] V. V. Flambaum and D. W. Murray, *Phys. Rev. C* **56**, 1641 (1997).
- [34] I. B. Khriplovich, *Phys. Lett. A* **197**, 316 (1995).
- [35] V. F. Dmitriev and V. B. Telitsin, *Nucl. Phys.* **A613**, 237 (1997); V. F. Dmitriev and V. B. Telitsin, *Nucl. Phys.* **A674**, 168 (2000); W. C. Haxton, C.-P. Liu, and M. J. Ramsey-Musolf, *Phys. Rev. Lett.* **86**, 5247 (2001); W. C. Haxton, C.-P. Liu, and M. J. Ramsey-Musolf, *Phys. Rev. C* **65**, 045502 (2002).
- [36] K. Tsigutkin, D. R. Dounas-Frazer, A. Family, J. E. Stalnaker, V. V. Yashchuk, and D. Budker, *Phys. Rev. Lett.* **103**, 071601 (2009); K. Tsigutkin, D. R. Dounas-Frazer, A. Family, J. E. Stalnaker, V. V. Yashchuk, and D. Budker, *Phys. Rev. A* **81**, 032114 (2010).
- [37] S. Aubin *et al.*, *Hyperfine Interact.* **214**, 163 (2013).
- [38] D. DeMille, S. B. Cahn, D. Murphree, D. A. Rahmlo, and M. G. Kozlov, *Phys. Rev. Lett.* **100**, 023003 (2008); S. B. Cahn, J. Ammon, E. Kirilov, Y. V. Gurevich, D. Murphree, R. Paolino, D. A. Rahmlo, M. G. Kozlov, and D. DeMille, *Phys. Rev. Lett.* **112**, 163002 (2014).
- [39] B. R. Heckel, E. G. Adelberger, C. E. Cramer, T. S. Cook, S. Schlamminger, and U. Schmidt, *Phys. Rev. D* **78**, 092006 (2008).
- [40] J. M. Brown, S. J. Smullin, T. W. Kornack, and M. V. Romalis, *Phys. Rev. Lett.* **105**, 151604 (2010).
- [41] F. Allmendinger, W. Heil, S. Karpuk, W. Kilian, A. Scharth, U. Schmidt, A. Schnabel, Yu. Sobolev, and K. Tullney, *Phys. Rev. Lett.* **112**, 110801 (2014).
- [42] V. A. Kostelecký and C. D. Lane, *Phys. Rev. D* **60**, 116010 (1999).
- [43] M. Pospelov, A. Ritz, and M. Voloshin, *Phys. Rev. D* **78**, 115012 (2008).
- [44] S. G. Karshenboim and V. V. Flambaum, *Phys. Rev. A* **84**, 064502 (2011).
- [45] M. Pospelov, S. Pustelny, M. P. Ledbetter, D. F. J. Kimball, W. Gawlik, and D. Budker, *Phys. Rev. Lett.* **110**, 021803 (2013).
- [46] A. Derevianko and M. Pospelov, [arXiv:1311.1244](https://arxiv.org/abs/1311.1244).
- [47] K. Blum, R. T. D'Angelo, M. Lisanti, and B. R. Safdi, [arXiv:1401.6460](https://arxiv.org/abs/1401.6460).
- [48] F. T. Avignone III, *J. Phys. Conf. Ser.* **173**, 012015 (2009).
- [49] A. Derevianko, V. A. Dzuba, V. V. Flambaum, and M. Pospelov, *Phys. Rev. D* **82**, 065006 (2010).
- [50] V. A. Dzuba, V. V. Flambaum, and M. Pospelov, *Phys. Rev. D* **81**, 103520 (2010).
- [51] A. V. Derbin, S. V. Bakhlanov, I. S. Dratchnev, A. S. Kayunov, and V. N. Muratova, *Eur. Phys. J. C* **73**, 2490 (2013).
- [52] D. F. J. Kimball, I. Lacey, J. Valdez, J. Swiatkowski, C. Rios, R. Peregrina-Ramirez, C. Montcrieffe, J. Kremer, J. Dudley, and C. Sanchez, *Ann. Phys. (Berlin)* **525**, 514 (2013).
- [53] B. J. Venema, P. K. Majumder, S. K. Lamoreaux, B. R. Heckel, and E. N. Fortson, *Phys. Rev. Lett.* **68**, 135 (1992).
- [54] S. Eckel, A. O. Sushkov, and S. K. Lamoreaux, *Phys. Rev. Lett.* **109**, 193003 (2012).
- [55] D. Budker, S. K. Lamoreaux, A. O. Sushkov, and O. P. Sushkov, *Phys. Rev. A* **73**, 022107 (2006).
- [56] C. Beck, *Phys. Rev. Lett.* **111**, 231801 (2013).
- [57] Y. V. Stadnik and V. V. Flambaum, [arXiv:1405.5337](https://arxiv.org/abs/1405.5337).