

## LINEAR OPERATORS INEQUALITY FOR $n$ -CONVEX FUNCTIONS AT A POINT

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*Abstract.* We study necessary and sufficient conditions on linear operators  $A$  and  $B$  for inequality  $Af \leq Bf$  to hold for every function  $f$  that is  $n$ -convex at a point.

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