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Loss Performance Analysis of an Isolated Power Supply for Ultrafast Tracking Converters

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Abstract—This paper presents the loss performance analysis of an isolated power supply that is designed for ultra-fast tracking converters. The results of the analysis provide insights into the operation of the proposed power supply, how each physical component contributes to the total loss, and how its efficiency may be further improved.

Keywords—Dc-dc power converters, loss measurement, magnetic losses, switching loss.

I. INTRODUCTION

Power supply designed for fast output voltage transient applications should meet certain requirements regarding their input-to-output parasitic capacitance. Specifically, the circuit input-to-output capacitance should be as low as possible in order to mitigate the transmission of common mode noise generated by the fast output voltage transients [1]-[4]. First, [1] proposed an isolated power supply with a power rating of 36 V/5 W and a ring core transformer with an inter-winding capacitance of 1 pF. Next, [2], [3], and [4] introduced a prototype using the same topology as in [1], but the power rating was increased to 60 V/300 W and the proposed transformer had an inter-winding capacitance of 10 pF.

Reference [2] and [3] also described the circuit operation, control, and general structure of the proposed transformer in addition to the circuit topology. However, the loss performance analysis of the converters had not been addressed. The topology introduced in [1] and studied in [2]-[3] is shown in Fig. 1.

This paper addresses the loss performance analysis of the converter proposed in [1]-[4]. The detail of the circuit operation will not be covered in this paper; they can be found in [2] and [3]. Instead, this paper will focus on the loss performance of the converter prototype proposed in [3]. It will be shown that the loss calculation matches well with the experiments. The results suggest how each physical component contributes to the total loss, and how its efficiency may be further improved.

II. CONVERTER OPERATION AND ITS INFLUENCE ON INDIVIDUAL LOSS

The converter proposed in [2], [3] and studied in this paper for its loss performance is shown in Fig. 1. The specification of the prototype is shown in Table I. It consists of a full-bridge

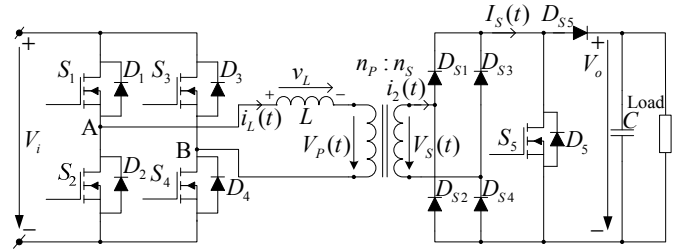


Fig. 1. The topology of the proposed power supply.

TABLE I. PROTOTYPE SPECIFICATION

Input voltage	400 V
Output voltage	60 V
Output current	5 A
Maximum output power	300 W
Leakage inductance	170 μ H

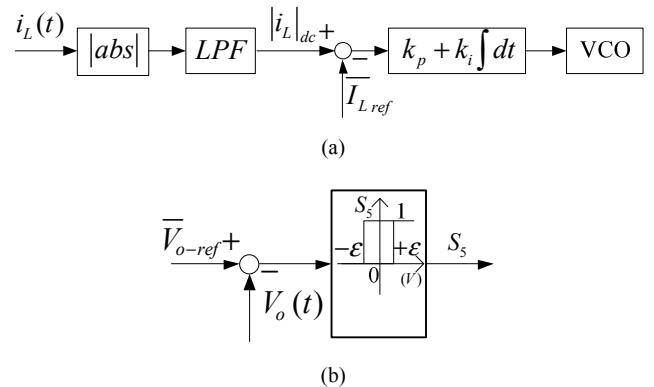


Fig. 2. Control block diagram. (a) Average current mode control in the primary side and (b) hysteresis control in the secondary side.

on the primary side and a proposed shunt regulator on the secondary side. The two sides are linked by a transformer that has an extremely low interwinding capacitance of 10 pF. This makes the power supply suitable for supplying energy to applications with fast changes in voltage such as the ultrafast tracking converters. Because of the transformer winding structure that minimizes the interwinding capacitance, the resulting leakage inductance L is large, which is 170 μ H [3]. This inductance is used as the main energy storage component to transfer current from the primary to the secondary side. There is no external inductor added to the circuit structure except for the leakage inductor of the proposed transformer.

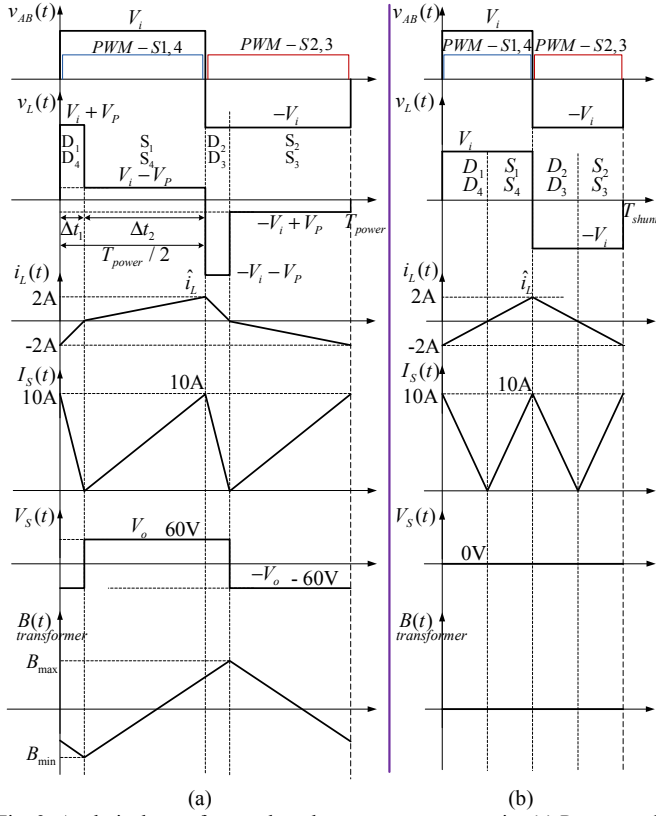


Fig. 3. Analytical waveforms when the converter operates in: (a) Power mode and (b) shunt mode.

The converter circuit operation is briefly sated in this section. The detail can be found in Section VI of [3]. It is very important to understand different operation modes of the proposed converter in order to analyze the individual loss.

There are two control loops whose block diagrams are shown in Fig. 2. The secondary side controller regulates the output voltage to be constant at 60 V. The output voltage is sensed by a voltage divider and compared to a hysteresis reference to switch ON and OFF the shunt switch S_5 .

When S_5 is OFF, the converter operates in its *power mode*, which is shown in Fig. 3(a); the output voltage increases because the output current $I_S(t)$ supplies energy to the load. Vice versa, when S_5 is ON, shunting the secondary side, the converter operates in its *shunt mode* (see Fig. 3(b)); the output voltage decreases because the secondary current $I_S(t)$ is isolated from the load. On the primary side control, the primary side current i_L is sensed. It is rectified and filtered to produce a rectified-dc value. This value is then compared to a rectified-dc reference and processed by an analog proportional-integrator (PI) controller. The output of the PI controller is fed to a voltage-controlled oscillator (VCO) that will automatically adjust the switching frequency to keep the rectified primary dc current to be constant at 1 A dc. The duty cycle of the primary switches is regulated at 50 %. With a turns ratio of 5:1, the rectified dc current at the secondary side is controlled at 5 A dc.

When the converter operates in power mode, the output power is 300 W because the output current $I_S(t)$ which has a dc value of 5 A is supplying the load whose voltage is regulated at 60 V dc. On the other hand, when the converter operates in shunt mode, the output current $I_S(t)$ is isolated from the load, circulating through S_5 ; the output power is zero. The converter is constantly switching between the power mode and shunt mode. It depends on the output power level to determine how long the converter is operating in each mode. For example, if the converter is desired to deliver 300 W at the output, then it will fully operate in power mode. If the converter is desired to shut down the output power, or to not deliver any power at all, then the converter will entirely operate in shunt mode. The higher the output power (closer to 300 W) the longer time the converter operates in power mode.

Therefore, if the converter outputs a power of P_{out} , then the duty cycle in which the converter operates in power mode will be:

$$d_{power} = \frac{P_{out}}{P_{max}}, \quad (1)$$

where P_{max} is the maximum output power of the converter. In this design, P_{max} is equal to 300 W. Likewise, the duty cycle in which the converter operates in shunt mode is:

$$d_{shunt} = \frac{P_{max} - P_{out}}{P_{max}} = 1 - d_{power} \quad (2)$$

Duty cycle d_{shunt} is also the duty cycle of turning-on shunt switch S_5 . It is noticed that d_{power} and d_{shunt} changes with output power.

During shunt mode, the switching frequency of the primary side switches, f_{shunt} , is 307 kHz. During power mode, the switching frequency, f_{power} , is 124 kHz. The detail of the derivation of the switching frequency can be found in Section VI of [3].

The switching between the two operation modes affect different individual loss in a different way because the current waveforms and switching frequency are switched between two modes. The losses that are affected by the switching of the operation modes are the switching losses of the primary side switches, the core loss and copper loss of the transformer, and the losses in D_{S5} and S_5 . For convenience, for the losses calculation involving the switching frequency, the normalized switching frequency is introduced:

$$f_{norm} = d_{power} f_{power} + d_{shunt} f_{shunt}. \quad (3)$$

It is also noticed that f_{norm} changes with the change in output power. For example, $f_{norm} = f_{power}$ when $P_{out} = P_{max}$, and $f_{norm} = f_{shunt}$ when $P_{out} = 0$.

On the contrary, the transition between the two operation modes does not affect the conduction losses of the primary side switches S_1-S_4 and the conduction loss of the diode

bridge consisting of D_{S1} — D_{S4} . This is because the currents flowing through these devices do not change their root-mean-square value regardless of the operation mode as shown in Fig. 3. This will also be observed in the next section from the formulas used to calculate these conduction losses.

III. LOSS PERFORMANCE ANALYSIS

A. Losses on the Primary Side Switches S_1 — S_4

The power dissipation of primary side MOSFETs consists mainly of conduction loss and switching loss:

$$P_{d_total} = P_{d_cnd} + P_{d_sw}, \quad (4)$$

where P_{d_total} is the total loss in the four primary switches, P_{d_cnd} is the total conduction loss, and P_{d_sw} is the total switching loss. At any instant of a full switching period, there are maximum two MOSFETs conducting. Therefore, the conduction power loss in one primary side switch, $P_{cnd-1MOS}$, is:

$$P_{cnd-1MOS} = R_{DS-on} I_{rms}^2 = R_{DS-on} \left(\frac{I_{peak}}{\sqrt{3}} \sqrt{d} \right)^2, \quad (5)$$

where I_{rms} is the root-mean-square value of the current flowing through a primary switch during a period, I_{peak} is the peak current value, $I_{peak} = 2$ A, and d is the duty cycle of the current, $d = 0.5$ (see Fig. 4). R_{DS-on} is the on resistance of the drain to source of the MOSFET. $R_{DS-on} = 1.1 \Omega$ at 65°C and a gate-source voltage of 10 V. The power MOSFET on the primary side uses part IRF840 from Vishay whose datasheet can be found in [5].

From (5), the conduction loss does not change regardless of the operation mode in which the converter is operating. This is because the root-mean-square value of the current is the same in both modes. The total conduction loss in the whole four primary side MOSFETs, P_{d_cnd} , is therefore:

$$P_{d_cnd} = 4P_{cnd-1MOS} = 2.93 \text{ W}. \quad (6)$$

At the turning-on transitions of the MOSFETs, the transitions are made from the body diode in the same MOSFET to its channel. For example, the transition are from D_1 to S_1 , D_2 to S_2 , D_3 to S_3 , and D_4 to S_4 . Because the MOSFETs are conducting, the voltages across them are zero. It is also observed that the currents conducting through them are crossing the zero value. This characteristic can be observed from Fig. 4. For this reason, there is no switching loss in the turn-on transitions.

The total switching loss during turn off in the whole four MOSFET is:

$$P_{d_sw} = 4P_{sw-1MOS} = 4E_{off} f_{sw} = 2V_i I_{peak} t_f f_{norm}, \quad (7)$$

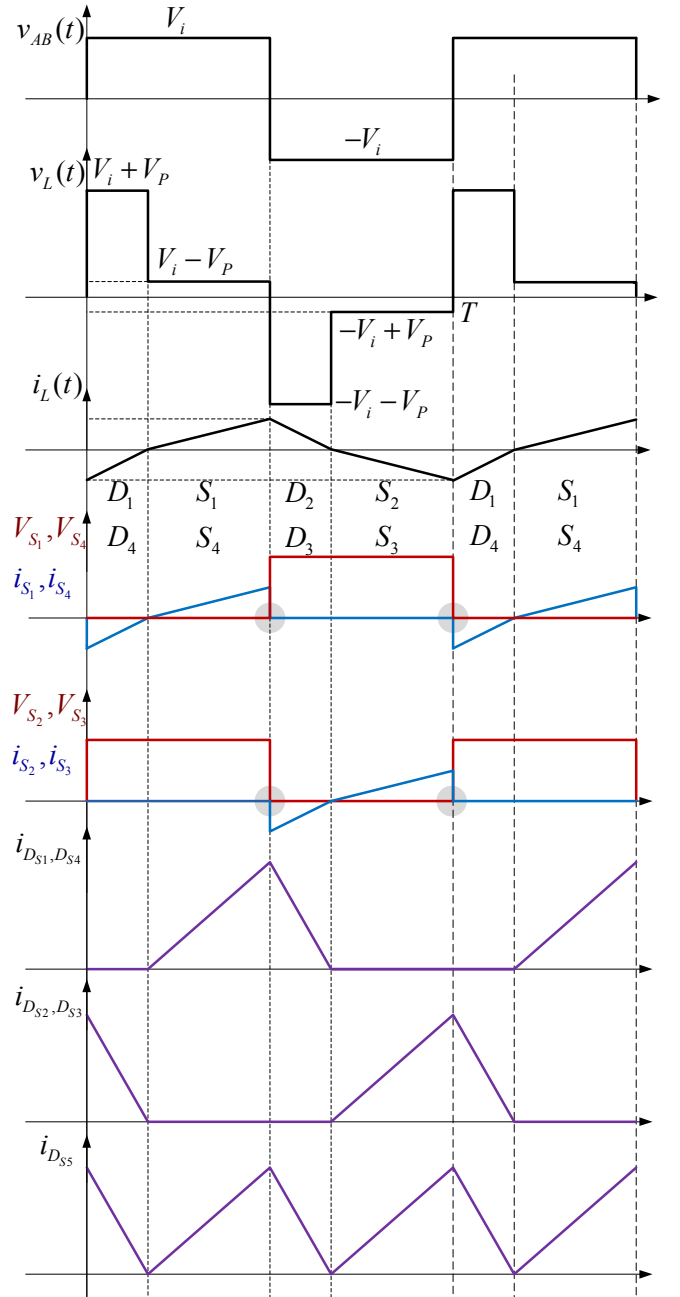


Fig. 4. The current and voltage waveforms across power switches and diodes.

where E_{off} is the energy loss during turn-off transients, I_{peak} is the peak current value during turn-off, and t_f is the fall time duration provided by the datasheet of the MOSFET, $t_f = 30$ ns.

B. Losses on the Secondary Side

1) Loss in the diode bridge D_{S1} — D_{S4}

The diode bridge uses part MBR10T100 from Vishay [6]. The loss in one diode, P_{1-D} , is:

$$P_{1-D} = V_{FM} I_{D-avg} + R_D I_{D-rms}^2, \quad (8)$$

where V_{FM} is the forward voltage drop. Its value is $V_{FM} = 0.57$ V at 125°C and 0.71 V at 25°C . The value of V_{FM} at 65°C is used in the calculation because the prototype is attached to two sufficiently large heat sinks that are expected to keep the temperature rise of the power switches to be within 40°C . Taking the linear interpolation of V_{FM} yields $V_{FM} = 0.65$ V.

R_D is approximated to be equal to the slope the diode current-voltage curve at the average operating forward current of 5 A. From the data-sheet of the part used, the value of R_D is 0.02 Ω . This value is taken into the loss estimation. Meanwhile, I_{D-avg} is the average value of the current flowing through each diode, $I_{D-avg} = 2.5$ A. I_{D-rms} is the root-mean-square value of the diode current, $I_{D-rms} = (I_{D-peak} / \sqrt{3}) \sqrt{d_D}$.

The duty cycle of the triangular current flowing through one diode is $d_D = 0.5$. The peak diode current value is $I_{D-peak} = 10$ A. Therefore, $I_{D-rms} = 4.1$ A.

Substituting these values to (8) yields $P_{1-D} = 1.96$ W. The total loss in the four diodes in the rectifier bridge is:

$$P_{D-bridge} = 4P_{1-D} = 7.83 \text{ W}. \quad (9)$$

It is noted that there is no reverse-recovery loss in the diode bridge since the diode parts are Schottky-effect diodes.

2) Loss in forward diode D_{S5}

Forward diode D_{S5} also uses part MBR10T100 from Vishay [6]. The forward average current flowing through diode D_{S5} is: $I_{D_{S5-avg}} = 5$ A (see Fig. 4). The root mean square of that current is: $I_{D_{S5-rms}} = (I_{D_{S5-peak}} / \sqrt{3}) \sqrt{d_{D_{S5}}} = 5.8$ A, where $d_{D_{S5}}$ is the duty cycle of the current, $d_{D_{S5}} = 1$, $I_{D_{S5-peak}}$ is the current peak value, $I_{D_{S5-peak}} = 10$ A. The forward voltage drop is $V_{FM} = 0.65$ V at 65°C . The value of R_D is 0.02 Ω .

The loss in forward diode D_{S5} is therefore:

$$P_{D_{S5}} = V_{FM} I_{D_{S5-avg}} + R_D I_{D_{S5-rms}}^2 = 3.92 \text{ W}. \quad (10)$$

3) Loss in shunt MOSFET S_5

Shunt MOSFET S_5 uses part IRF540 from Vishay [7], which has an on-resistance of 0.096 Ω at 65°C at a gate-source voltage of 10 V. The conduction loss is:

$$P_{D_{S5}} = R_{S_5-DS-on} I_{S_5-rms}^2 = 3.2 \text{ W}, \quad (11)$$

where I_{S_5-rms} is the root-mean-square value of the current flowing through S_5 during shunt mode.

Because the switching frequency of S_5 is small, the switching loss is small compared to the conduction loss and is ignored.

C. Losses in the Transformer

TABLE II. PARAMETERS OF MAGNETIC CORE AND WINDING GEOMETRIES OF THE TRANSFORMER

Material	N87
Dimension	36 mm × 23 mm × 15 mm
Turns ratio	55 : 11
Primary winding	Litz-wire 60 × 0.2 mm
Secondary winding	Copper 1 mm diameter
Effective cross sectional area	$A_e = 95.89 \text{ mm}^2$
Effective volume	$V_e = 8597 \text{ mm}^3$

TABLE III. FITTING COEFFICIENT OF THE CORE LOSS CALCULATION

K_{Fe}	25.2156
x	1.2786
y	2.5850
f_{eq}	$0.81 f$

The parameters of the magnetic core and material, and turns ratio are listed in Table II. The parameters of the magnetic core geometries and material characteristic can be found in [8] and [9], respectively. The detailed description of the transformer structure can be found in [3] and it will not be covered again in this paper.

According to the Modified Steinmetz Equation (MSE) reported in [10]-[16], the core loss per volume, P_{Fe-rel} , is:

$$P_{Fe-rel} = K_{Fe} f_{eq}^{x-1} \hat{B}^y f, \quad (12)$$

where K_{Fe} , x , and y are dependent on the core material. K_{Fe} , x , and y are based on Steinmetz equation and they can be extracted from curve-fitting the experimental ferrite loss in the datasheet in [9]. \hat{B} is the peak flux density, f is the switching frequency, and f_{eq} is the equivalent switching frequency. According to [10], f_{eq} is related to the switching frequency f and the shape of the flux density waveform by

$$f_{eq} = \frac{2}{\Delta B^2 \pi^2} \int_0^T \left(\frac{dB}{dt} \right)^2 dt, \quad (13)$$

where ΔB is the peak-to-peak value of the flux density, T is the period of the excitation. The equivalent switching frequency, f_{eq} , is equal to f if sinusoidal excitation is used.

In this converter, the excitation is based on a triangular wave form as shown in the bottom of Fig. 3. From (13), we have

$$\begin{aligned} f_{eq} &= \frac{2}{(2\hat{B})^2 \pi^2} \left(\int_0^{T/2} \left(\frac{2\hat{B}}{T/2} \right)^2 dt + \int_{T/2}^T \left(\frac{2\hat{B}}{T/2} \right)^2 dt \right) \\ &= \frac{2}{4\hat{B}^2 \pi^2} \left(\frac{16\hat{B}^2}{T^2} t \Big|_{t=0}^{t=T/2} + \frac{16\hat{B}^2}{T^2} t \Big|_{t=T/2}^{t=T} \right) \\ &= \frac{8}{\pi^2 T} = \frac{8}{\pi^2} f = 0.81 f. \end{aligned} \quad (14)$$

The results of these fitting coefficients are shown in Table III, where P_{Fe_rel} is in watt per cubic-meter.

The calculated core loss is $P_{Fe} = 2.39$ W. The calculated copper loss is 2.13 W in power mode and 2.97 W in shunt mode.

IV. EXPERIMENTAL RESULTS

The prototype of the proposed power supply is shown in Fig. 5. Fig. 6 shows the transient response from power mode to shunt mode. In a similar way, the transient from shunt mode to power mode is shown in Fig. 7. The value of the output voltage threshold, ϵ , is set to 0.5 V. It can be observed that, both the inductor current and the output voltage are well regulated at their desired steady state values, which are 2 A peak and 60 V dc, respectively. The transient of the current from power mode to shunt mode and vice versa finishes within about 30 μ s and 40 μ s, respectively. The time needed for the inductor current to settle is mainly determined by the dynamic of the average current control scheme described in Fig. 2(a). Nevertheless, the transient and steady state are both stable and satisfactory. The behavior of the circuit matches accurately with the aforementioned circuit analysis.

The calculated break down loss is shown in Fig. 8. As can be seen, the loss in the primary side H-bridge accounts more than 60 % of the loss at low output power and around 40 % at high output power. The loss contributed by the diode bridge is constant because both the average and the root mean square value of the current flowing through the bridge is constant. The loss created by the forward diode D_{S5} and the shunt MOSFET S_5 is small compared to the loss in the H-bridge and the diode bridge. The loss in the transformer is also small compared to the dominant losses which are losses in the H-bridge and the diode bridge. As output power reduces, the duration in which the converter operates in shunt mode increases linearly. Even though the losses in the combination of forward diode D_{S5} and the shunt MOSFET S_5 and in the transformer decrease with the decrease of output power, their rate of decrease is smaller than the rate of increase in the switching loss of the primary side switches. Therefore, the total loss increases with lower output power. Thus, the efficiency drops.

The measured and calculated total loss are shown in Fig. 9. The power measurement is carried out by the PPA5530 precision power analyzer. The accuracy claimed by the manufacturer is ± 0.4 % in the operation condition under test. It can be seen that the calculated total loss and the measured total loss match very well with each other. The largest discrepancy between the calculated loss and measured loss is 1.9 W at 222 W output power. This discrepancy constitutes 7.5 % difference between the calculated and measured total loss and 0.85 % difference between the calculated efficiency and the measured efficiency. One of the reasons that explain this discrepancy could be the accuracy of the precision power analyzer used. Nevertheless, the calculated total loss is able to predict the trend of the total loss. It is asymptotical to the measured total loss. It has been proven that the loss is approxi-

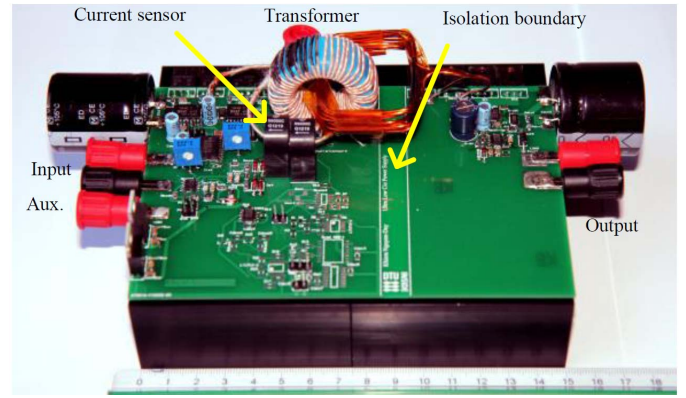


Fig. 5. A photo of the prototype of the proposed converter.

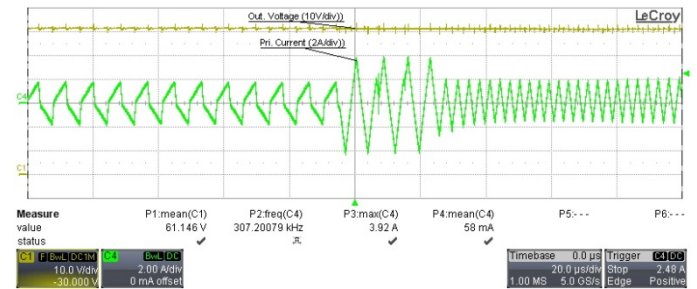


Fig. 6. Transient response from power mode to shunt mode. Top: output voltage (10V/div); bottom: inductor current (2A/div); time scale: 20 μ s/div.

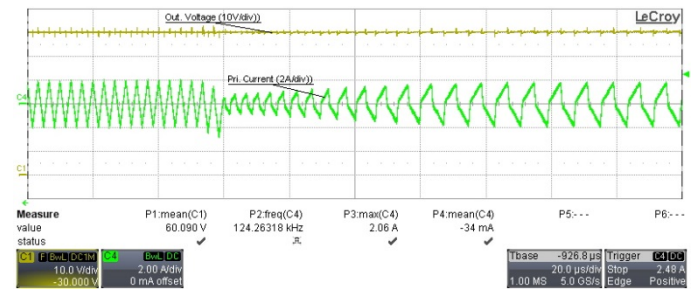


Fig. 7. Transient response from shunt mode to power mode. Top: output voltage (10V/div); bottom: inductor current (2A/div); time scale: 20 μ s/div.

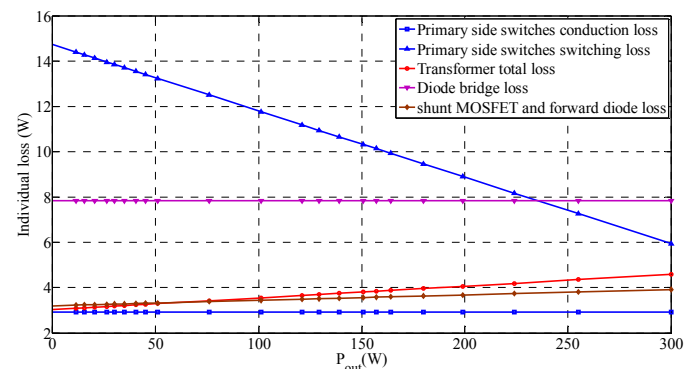


Fig. 8. Calculated breakdown loss.

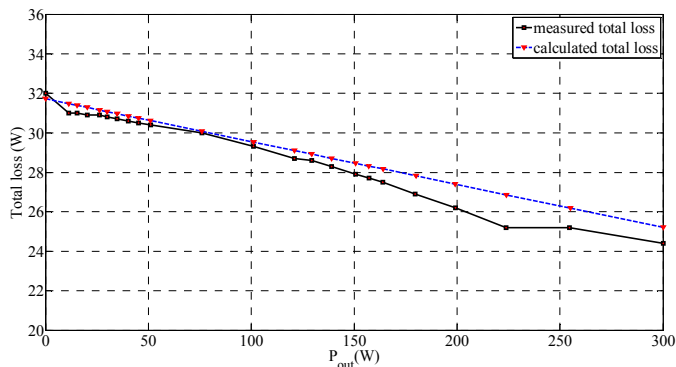


Fig. 9. Measured and calculated total loss.

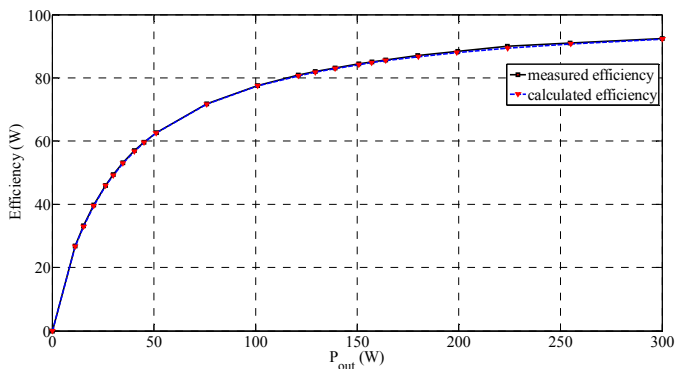


Fig. 10. Measured and calculated efficiency.

mated to be a linear combination of the shunt mode loss and power mode loss, as described in Section II.

The highest efficiency is 92.4 %, which is shown in Fig. 10. In general, the overall efficiency of the converter is satisfactory particularly in the range of 1/3 of the nominal power to the nominal power. The efficiency in this range is from 77.5 % to 92.4 %.

The calculated results show that the primary side switching loss is the predominant loss in the converter. Therefore, in order to further improve the efficiency of the converter, it is suggested that future design focus on reducing the switching loss on the primary side. It may be achieved by selection of different MOSFET part that is faster and hence yields lower switching loss.

V. CONCLUSION

This paper has dealt with the loss performance analysis of a novel power supply specially designed for ultra-fast tracking converters. The methods of calculating loss associated with each major physical device have been presented. The calculated total losses have been proven to match well with the measured data. The results of this analysis can serve as a guidance about which physical elements should be taken into account when the overall efficiency is of concern.

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